

Implications of LHCb measurements and  
future prospects

21/10/2022



# A bridge to new physics

Bridge solutions for  $a_\mu$  and  $b \rightarrow s\ell\ell$   
anomalies

arXiv:2205.04480

G. Guedes, PO

Pablo Olgoso

**FTAE**  
High Energy Theory



*ugr*

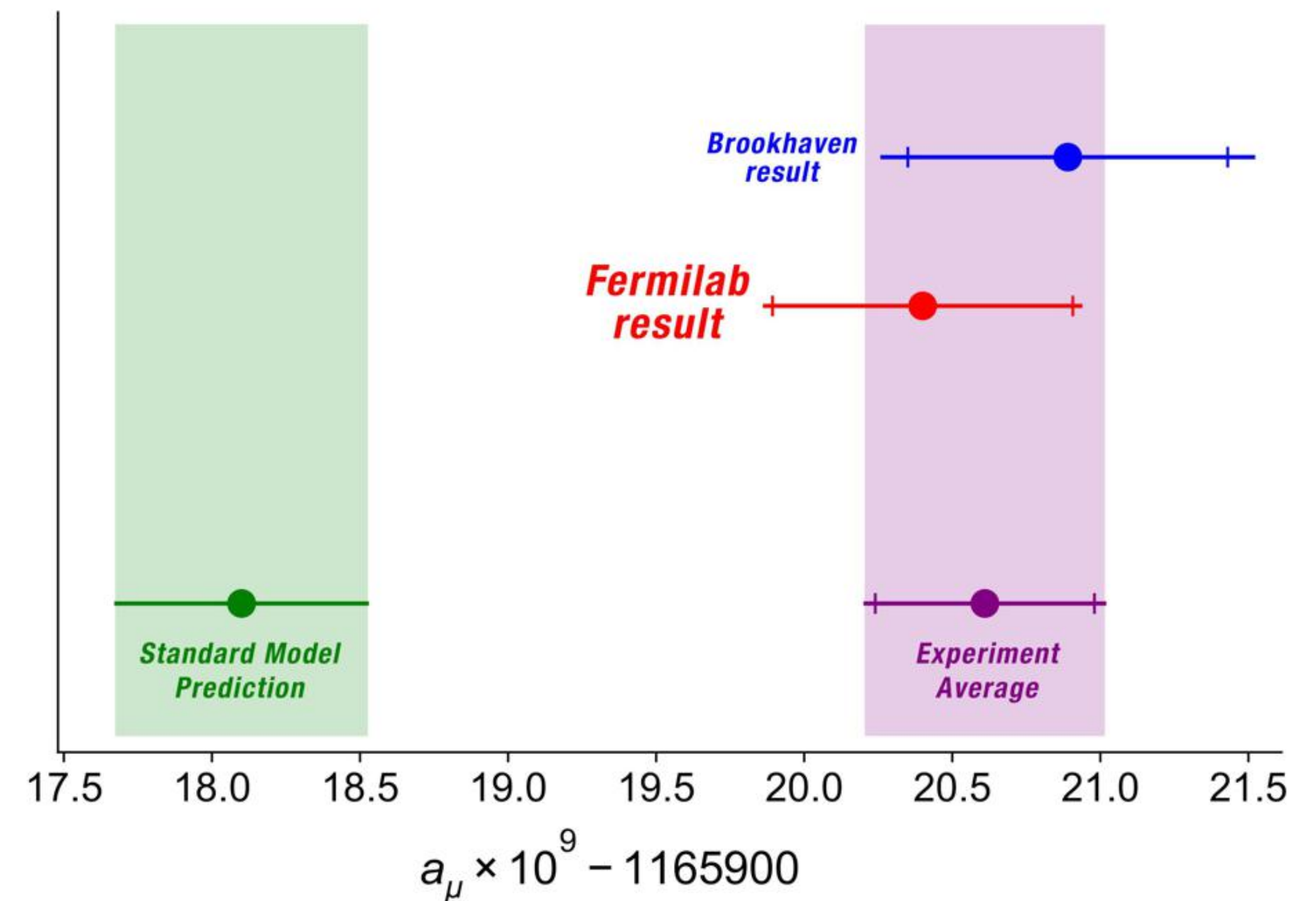
Universidad  
de **Granada**

# The $g-2$ anomaly

- There has been a big effort to explain the discrepancy between the SM prediction and the observed value ( $4.2 \sigma$ ).
- Disagreement in HVP contributions to SM prediction (tension would be reduced to  $1.5 \sigma$ ).

[S. Borsanyi et al., 2022.12347]

[M. Cè et al., 2206.06582]



# The g-2 anomaly

- From the lens of the SMEFT, it is generated by the *dipole* operators:

$$\mathcal{O}_{eB} = (\bar{\ell}\sigma^{\mu\nu}e)HB_{\mu\nu} + \text{h.c.},$$
$$\mathcal{O}_{eW} = (\bar{\ell}\sigma^{\mu\nu}e)\sigma^I HW_{\mu\nu}^I + \text{h.c..}$$

[J. Aebischer, W. Dekens, E. Jenkins, A. Manohar, D. Sengupta, P. Stoffer, 2102.08954]

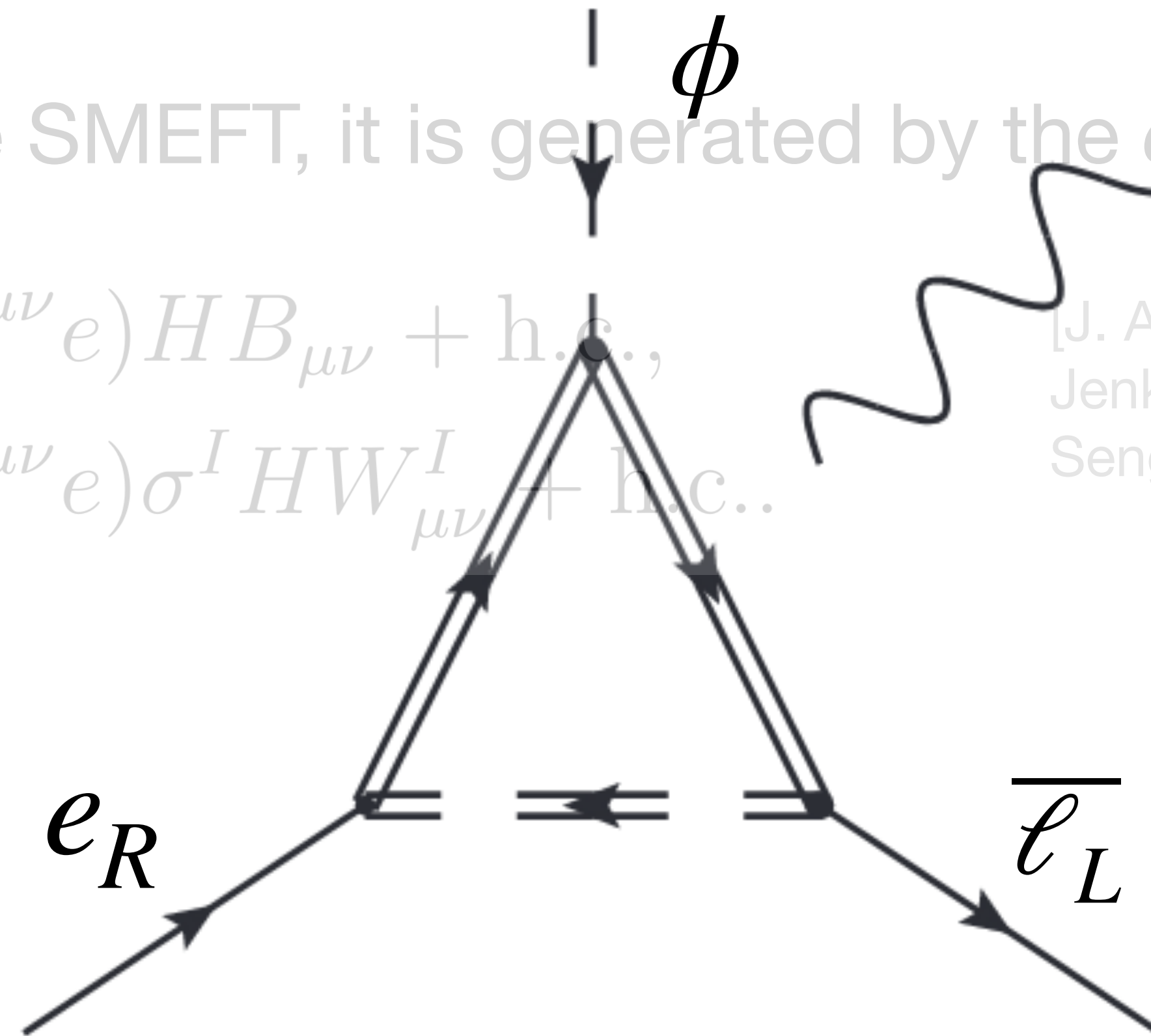
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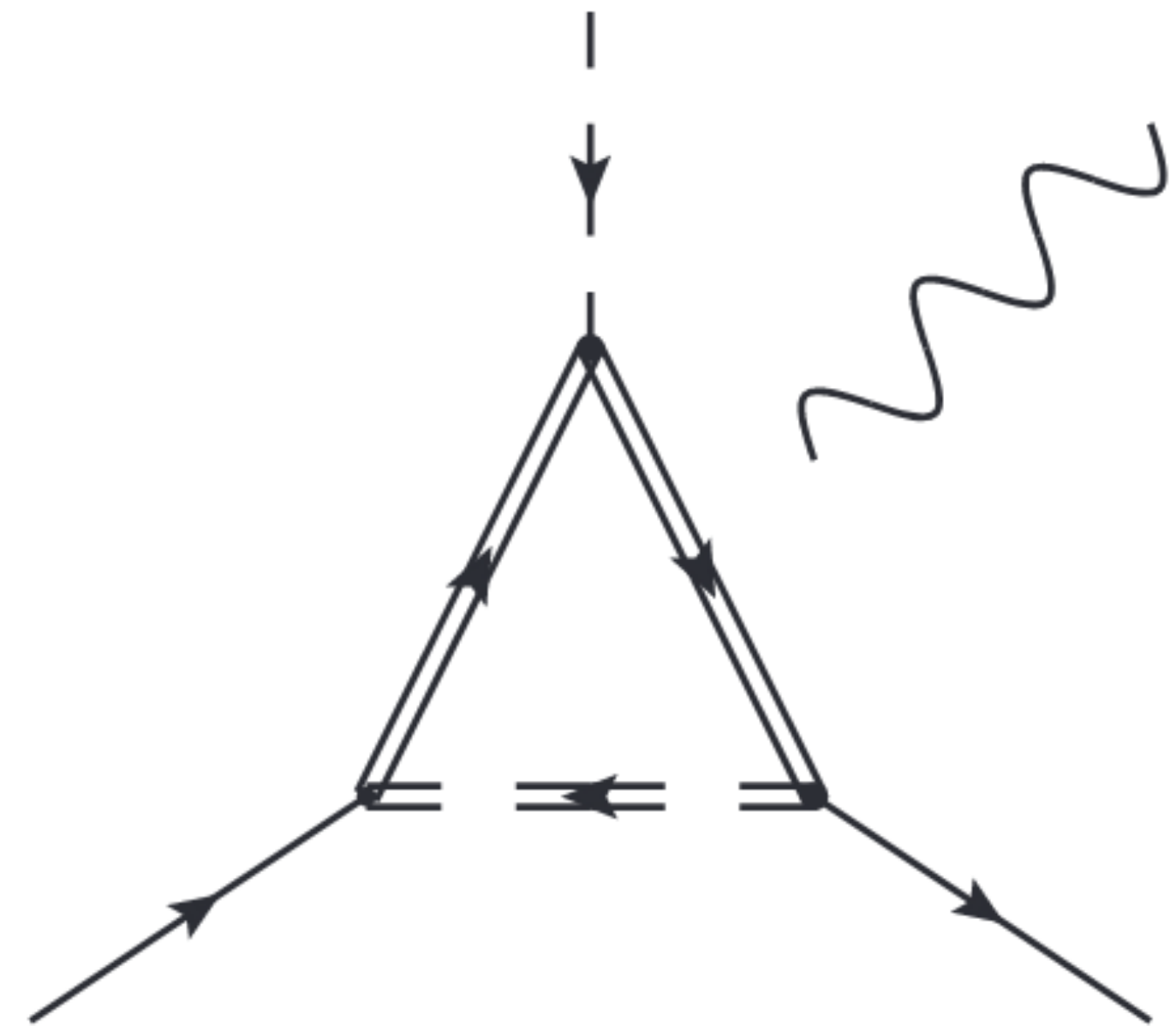
[J. Aebischer, W. Dekens, E. Jenkins, A. Manohar, D. Sengupta, P. Stoffer, 2102.08954]

- For a comprehensive review of the status of solutions, see:

[P. Athron, C. Balázs, D. Jacob, W. Kotlarski, D. Stöckinger, H. Stöckinger-Kim, 2104.03691]

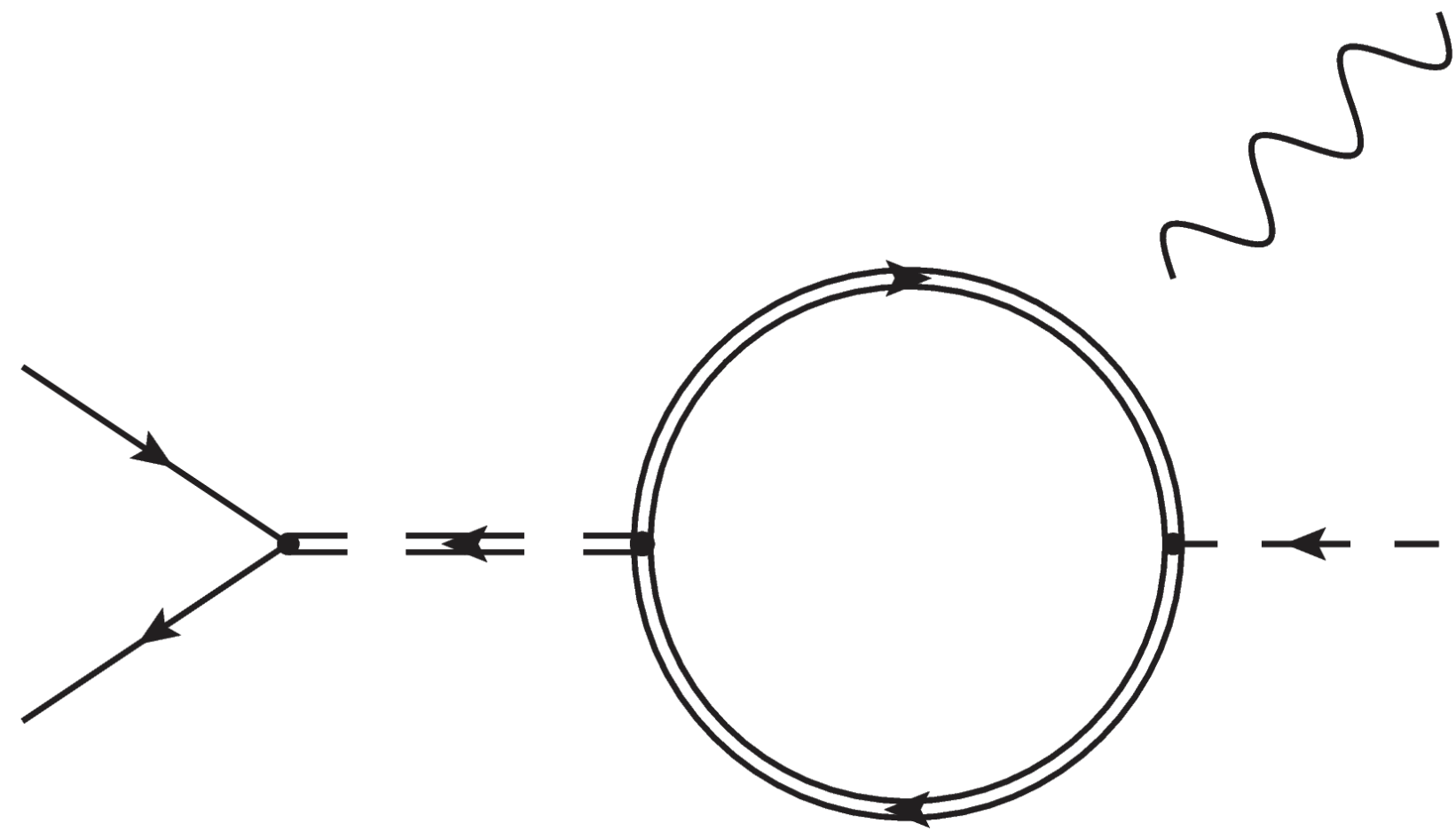
# Chirally enhanced solutions

- $\mathcal{O}(TeV)$  solutions need chirally enhanced contributions, i.e., not proportional to the muon's Yukawa.
- Chirality flip comes from:
  - Top Yukawa (S1 leptoquark).
  - Heavy VL fermions.



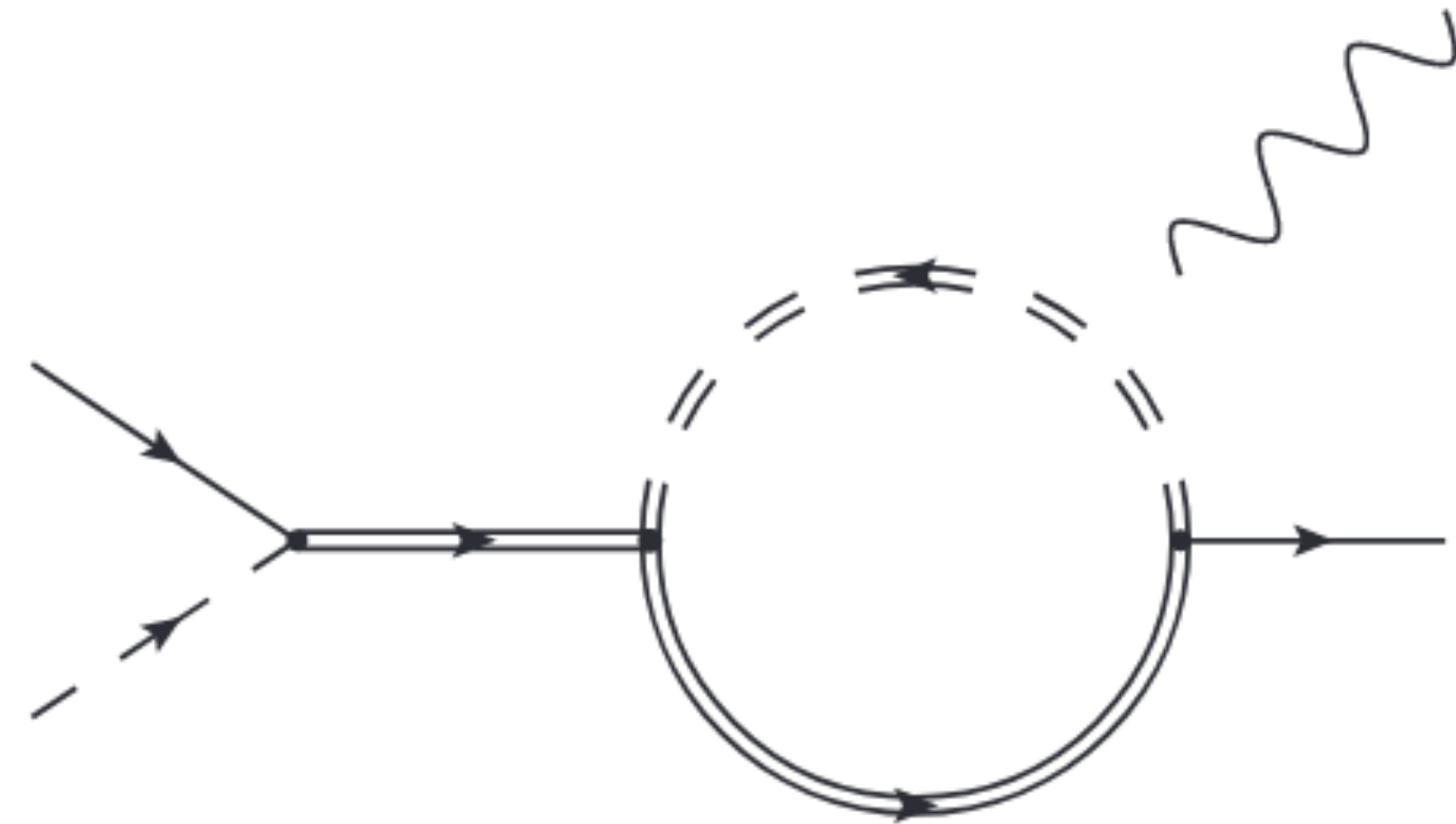
# The bridge diagram

- In this work we focus on the *bridge* topology:



$$\Phi \sim (1, 2, 1/2)$$

(No contribution)



$$E \sim (1, 1, -1)$$

$$\Delta \sim (1, 2, -1/2)$$

$$\Sigma \sim (1, 3, -1)$$

# The bridge diagram

- General results:

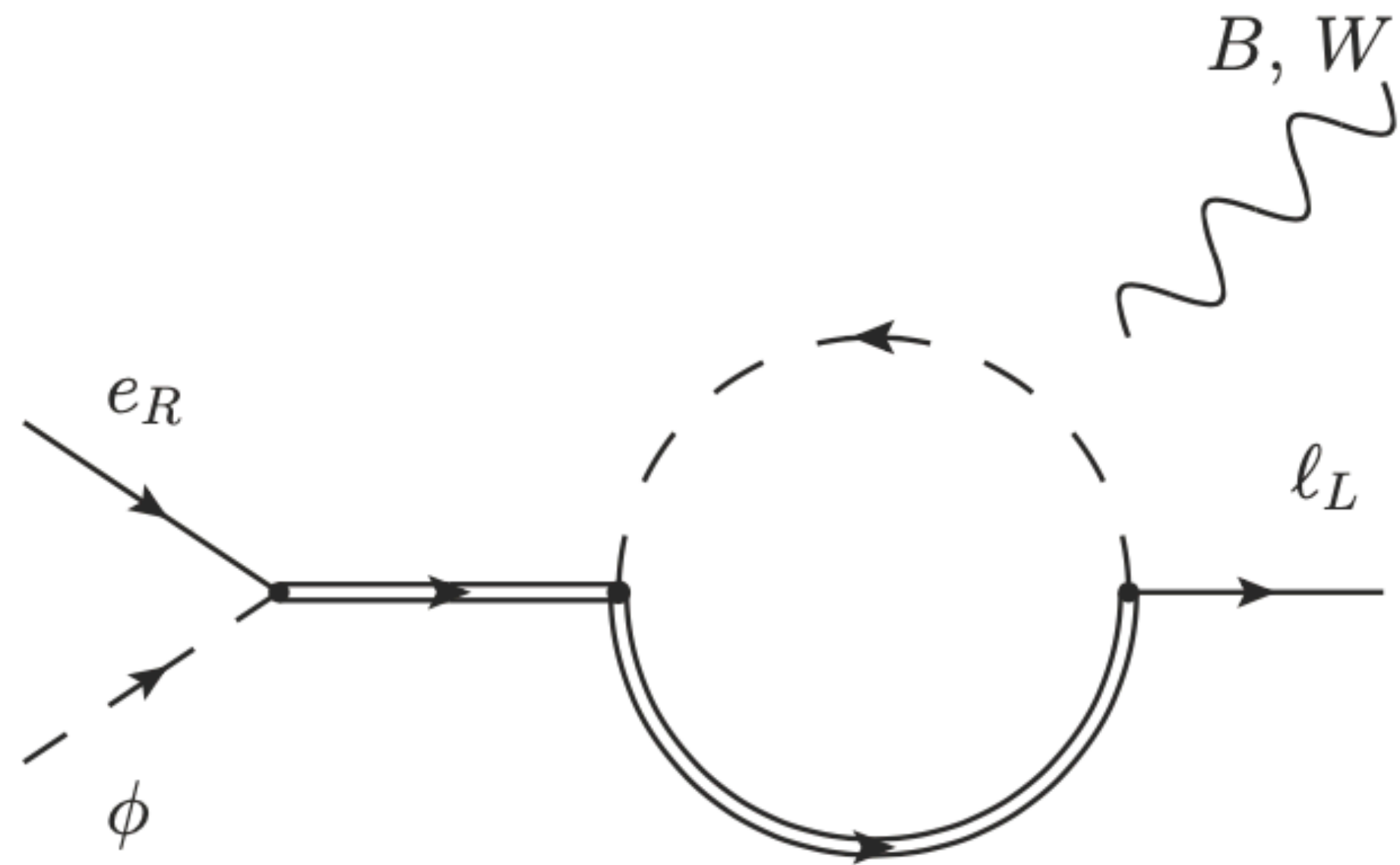
$$\alpha_{e\gamma}^{2,2} = \frac{iN_c e}{4} y_M y_F y_b^R \sum_{IJ} T_{I2J} \left[ \gamma_\Psi T_{I'I}^{\gamma,\Psi} T'_{2JI'} + \gamma_\Phi T_{JJ'}^{\gamma,\Phi} T'_{2IJ'} \right]$$

$$\gamma_\Psi = \frac{-iM_\Psi}{(4\pi)^2 M_\Delta} \frac{M_\Psi^4 - 4M_\Psi^2 M_\Phi^2 + 3M_\Phi^4 + 2M_\Phi^4 \text{Log} [M_\Psi^2 / M_\Phi^2]}{(M_\Psi^2 - M_\Phi^2)^3},$$

$$\gamma_\Phi = -\frac{iM_\Psi}{(4\pi)^2 M_\Delta} \frac{M_\Psi^4 - M_\Phi^4 - 2M_\Psi^2 M_\Phi^2 \text{Log} [M_\Psi^2 / M_\Phi^2]}{(M_\Psi^2 - M_\Phi^2)^3}.$$

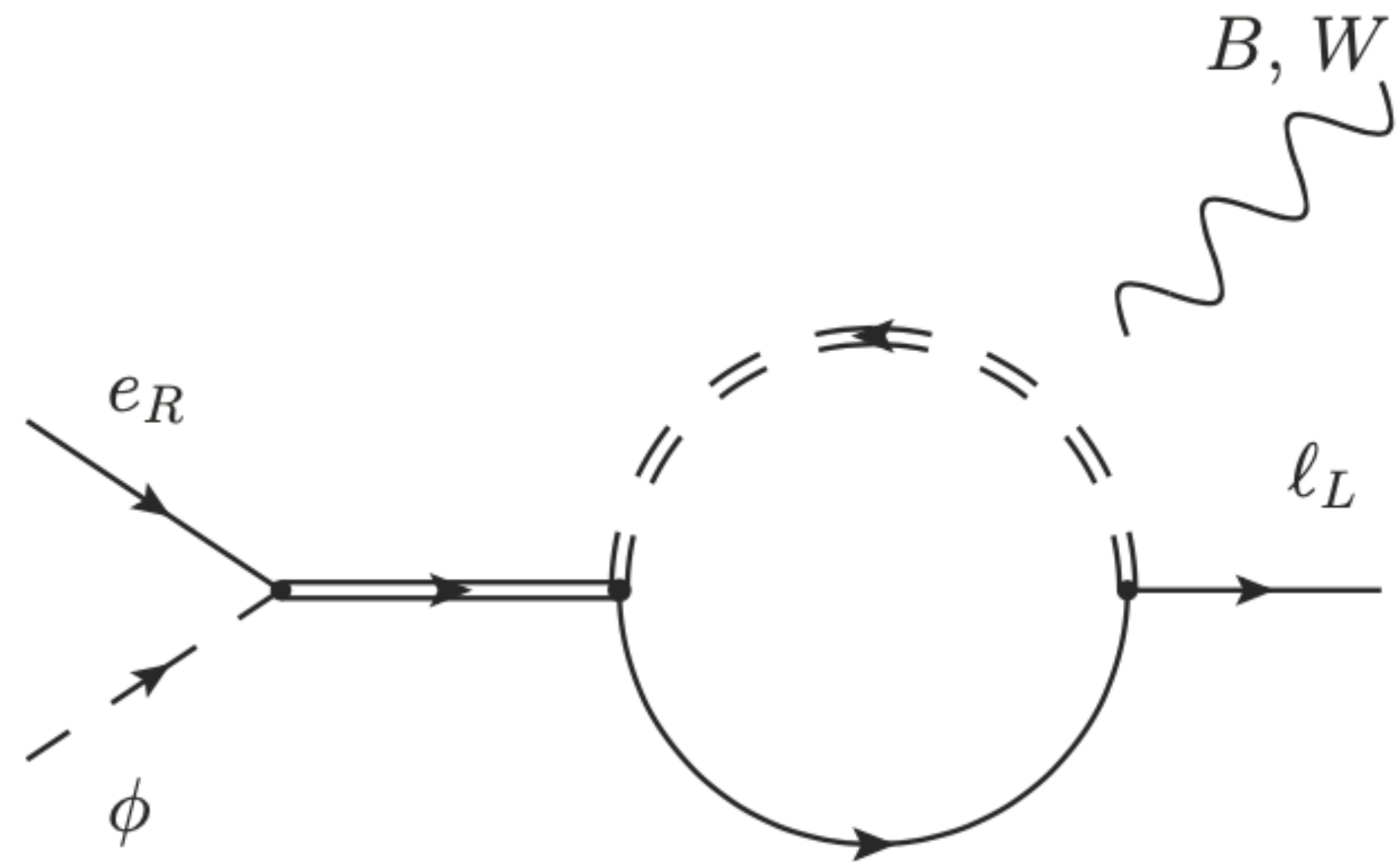


# 2 field extensions



(a)

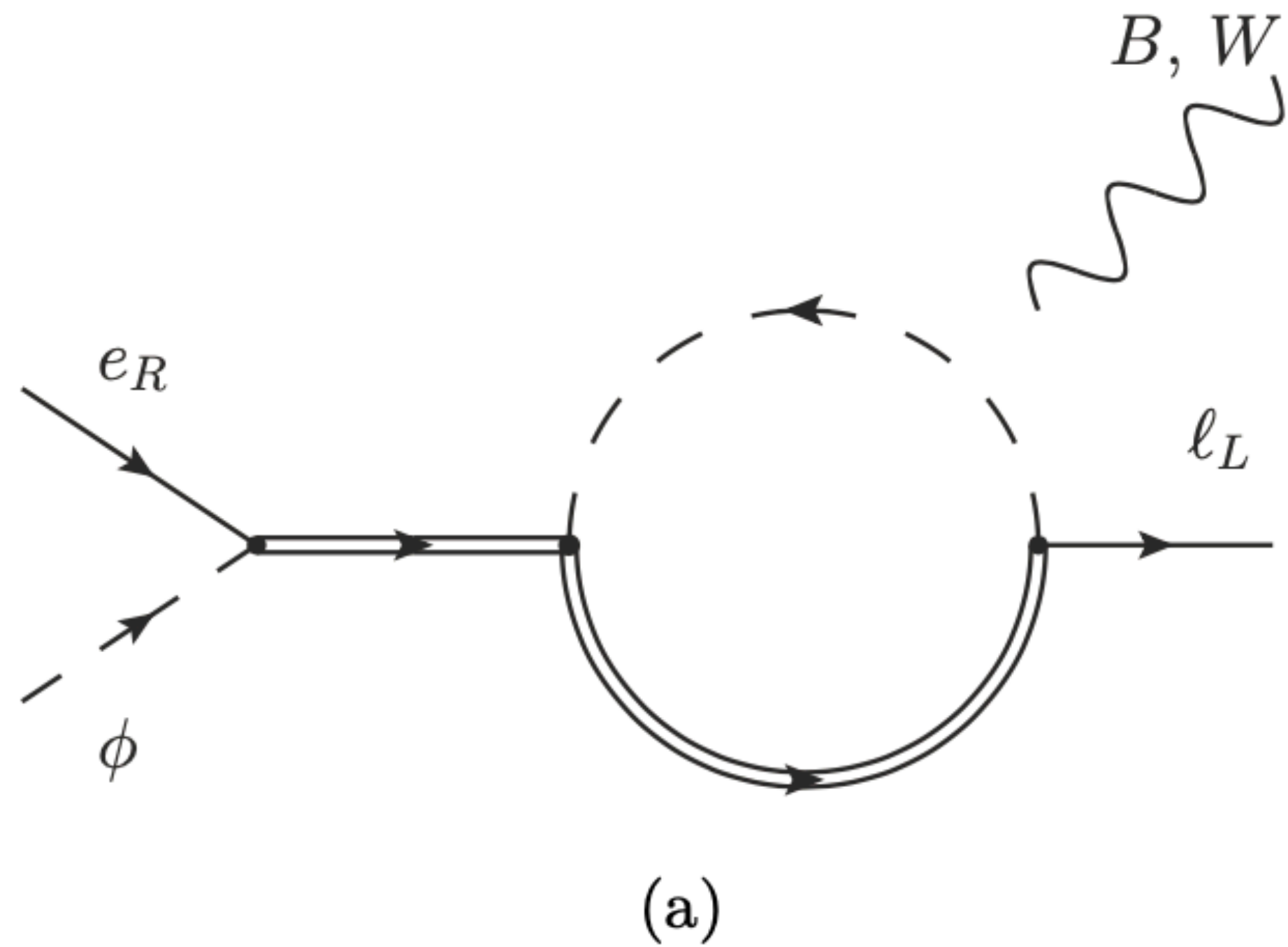
2 Fermion extension



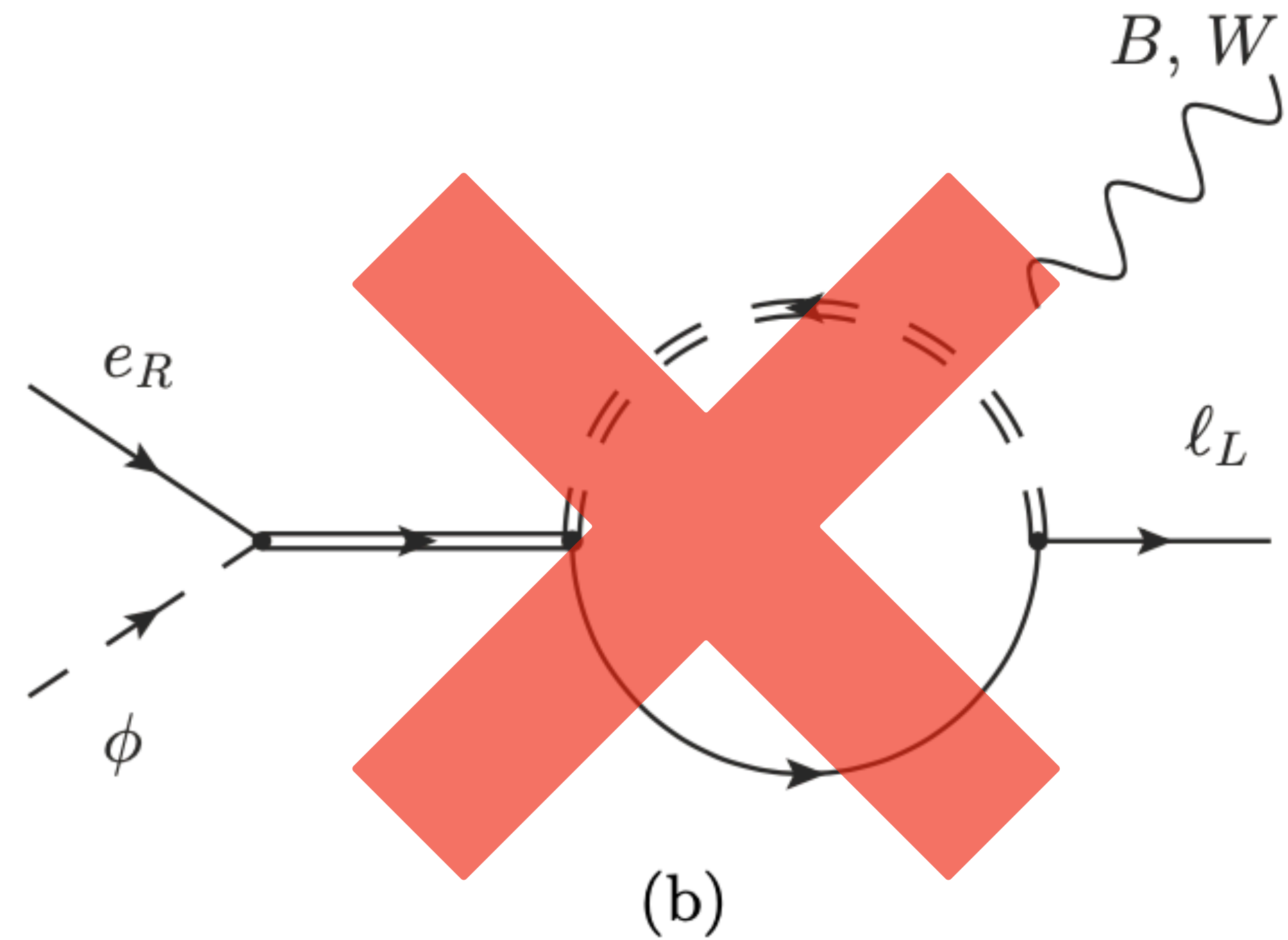
(b)

Fermion + Scalar extension

# 2 field extensions

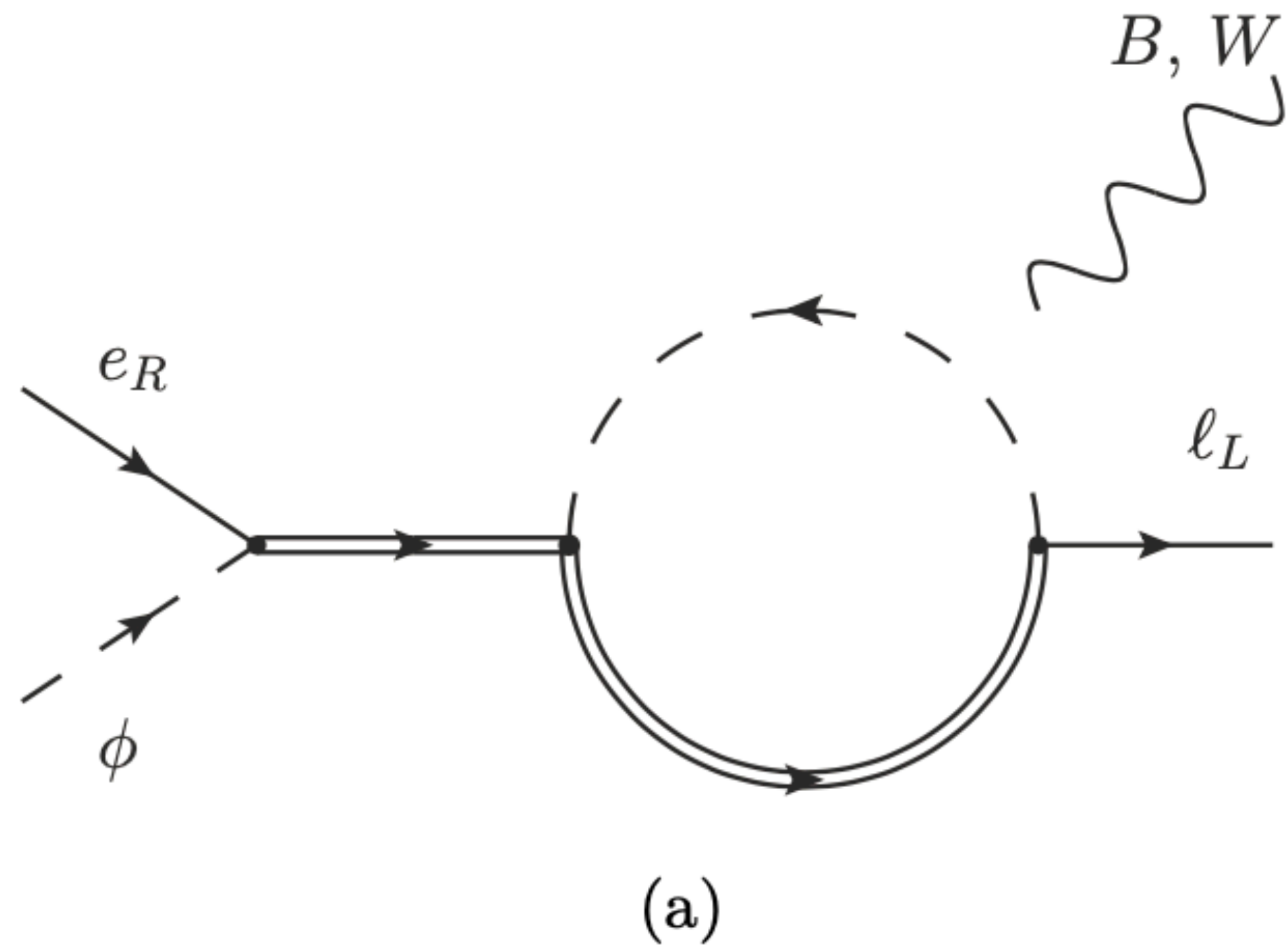


2 Fermion extension

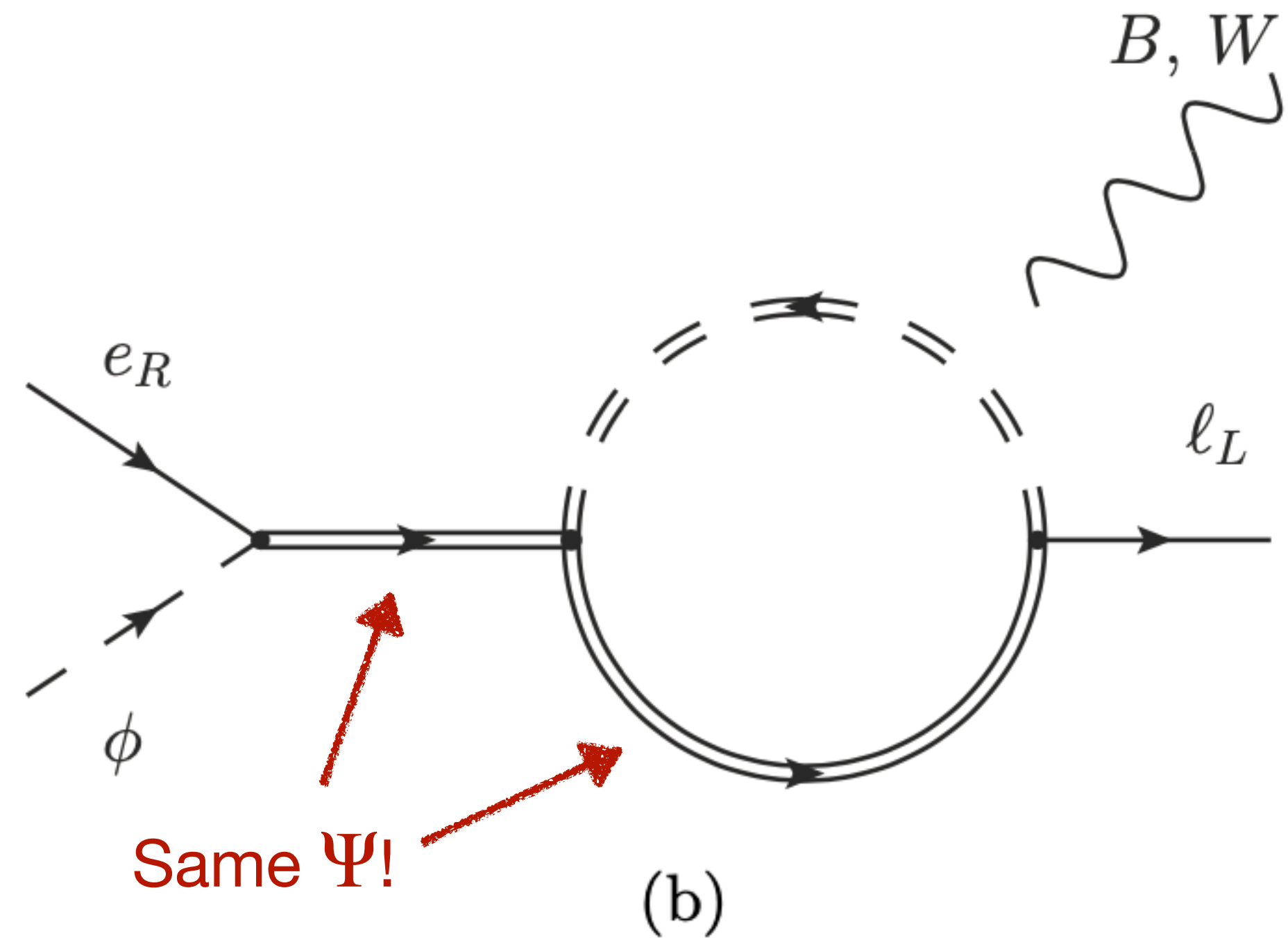


Fermion + Scalar extension

# 2 field extensions



2 Fermion extension



Fermion + Scalar extension

# 2 field extensions

Bridge	Other Fermion
$E \sim (1, 1, -1)$	$\Delta \sim (1, 2, -1/2)$
	$\Delta_3 \sim (1, 2, -3/2)$
	$E \sim (1, 1, -1)$
$\Delta \sim (1, 2, -1/2)$	$\Sigma \sim (1, 3, -1)$
	$N \sim (1, 1, 0)$
	$\Sigma_0 \sim (1, 3, 0)$
$\Sigma \sim (1, 3, -1)$	$\Delta \sim (1, 2, -1/2)$
	$\Delta_3 \sim (1, 2, -3/2)$

[A. Freitas, J. Lykken, S. Kell, S. Westhoff, 1402.7065]

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$\Sigma \sim (1, 3, -1)$	$\Delta \sim (1, 2, -1/2)$
	$\Delta_3 \sim (1, 2, -3/2)$

[N. Arkani-Hamed and K. Harigaya, 2106.01373]

[N. Craig, I. Garcia, A. Vainshtein, Z. Zhang, 2112.05770]

[L. Rose, B. Harling and A. Pomarol, 2201.10572]

$$\Delta a_\mu = 0 !$$

[A. Freitas, J. Lykken, S. Kell, S. Westhoff, 1402.7065]

# 2 field extensions

Bridge	Other Fermion	Fermion	Scalar
$E \sim (1, 1, -1)$	$\Delta \sim (1, 2, -1/2)$ $\Delta_3 \sim (1, 2, -3/2)$	$E \sim (1, 1, -1)$	$\mathcal{S}_0 \sim (1, 1, 0)$ $\mathcal{S}_2 \sim (1, 1, -2)$
$\Delta \sim (1, 2, -1/2)$	$E \sim (1, 1, -1)$ $\Sigma \sim (1, 3, -1)$ $N \sim (1, 1, 0)$ $\Sigma_0 \sim (1, 3, 0)$	$\Delta \sim (1, 2, -1/2)$	$\mathcal{S}_0 \sim (1, 1, 0)$ $\mathcal{S}_1 \sim (1, 1, -1)$ $\Xi_0 \sim (1, 3, 0)$ $\Xi_1 \sim (1, 3, -1)$
$\Sigma \sim (1, 3, -1)$	$\Delta \sim (1, 2, -1/2)$ $\Delta_3 \sim (1, 2, -3/2)$	$\Sigma \sim (1, 3, -1)$	$\Xi_0 \sim (1, 3, 0)$ $\Xi_2 \sim (1, 3, -2)$

# 2 field extensions

Bridge	Other Fermion	Fermion	Scalar
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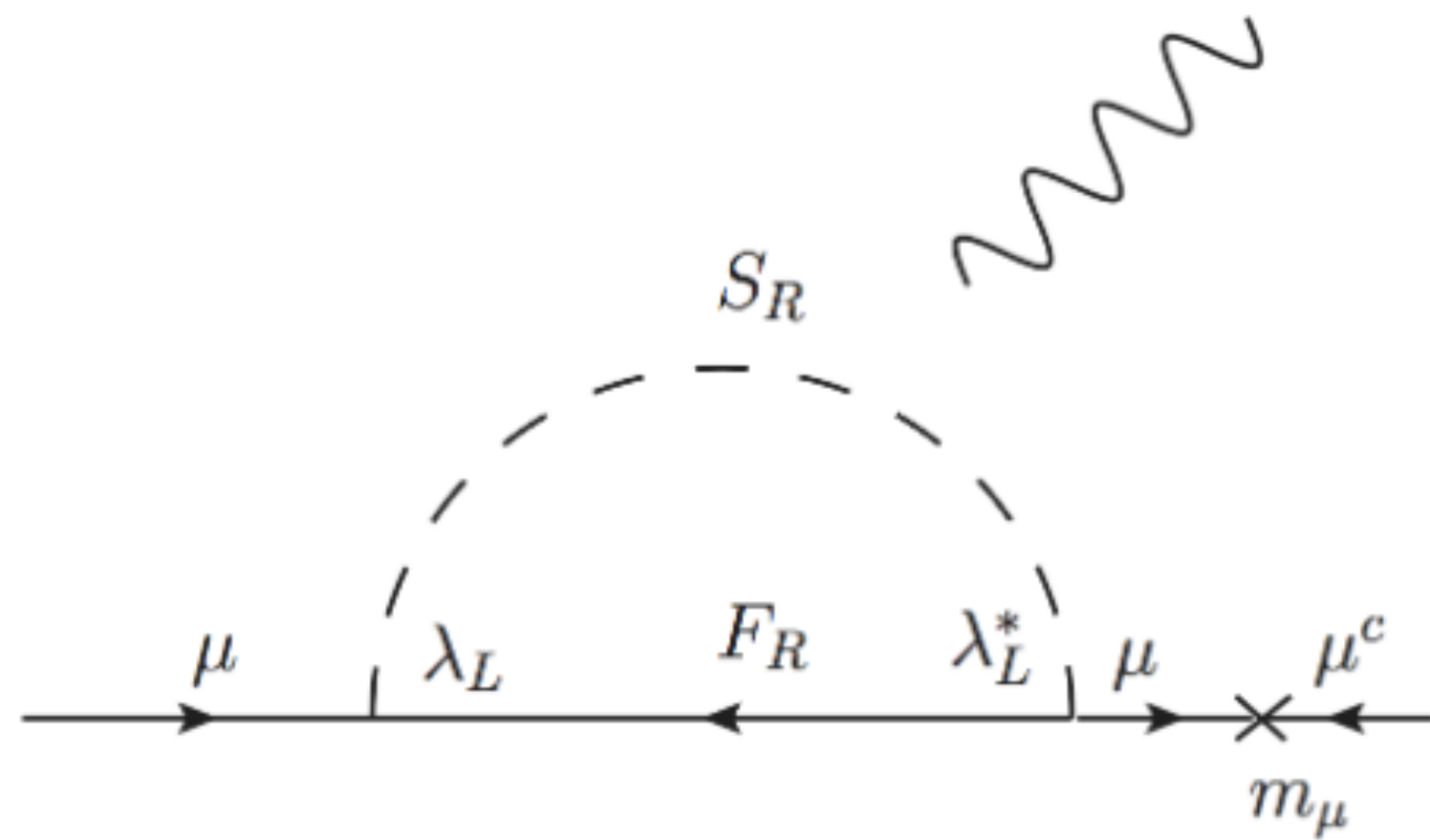
Excluded in the literature!

# 2 field extensions

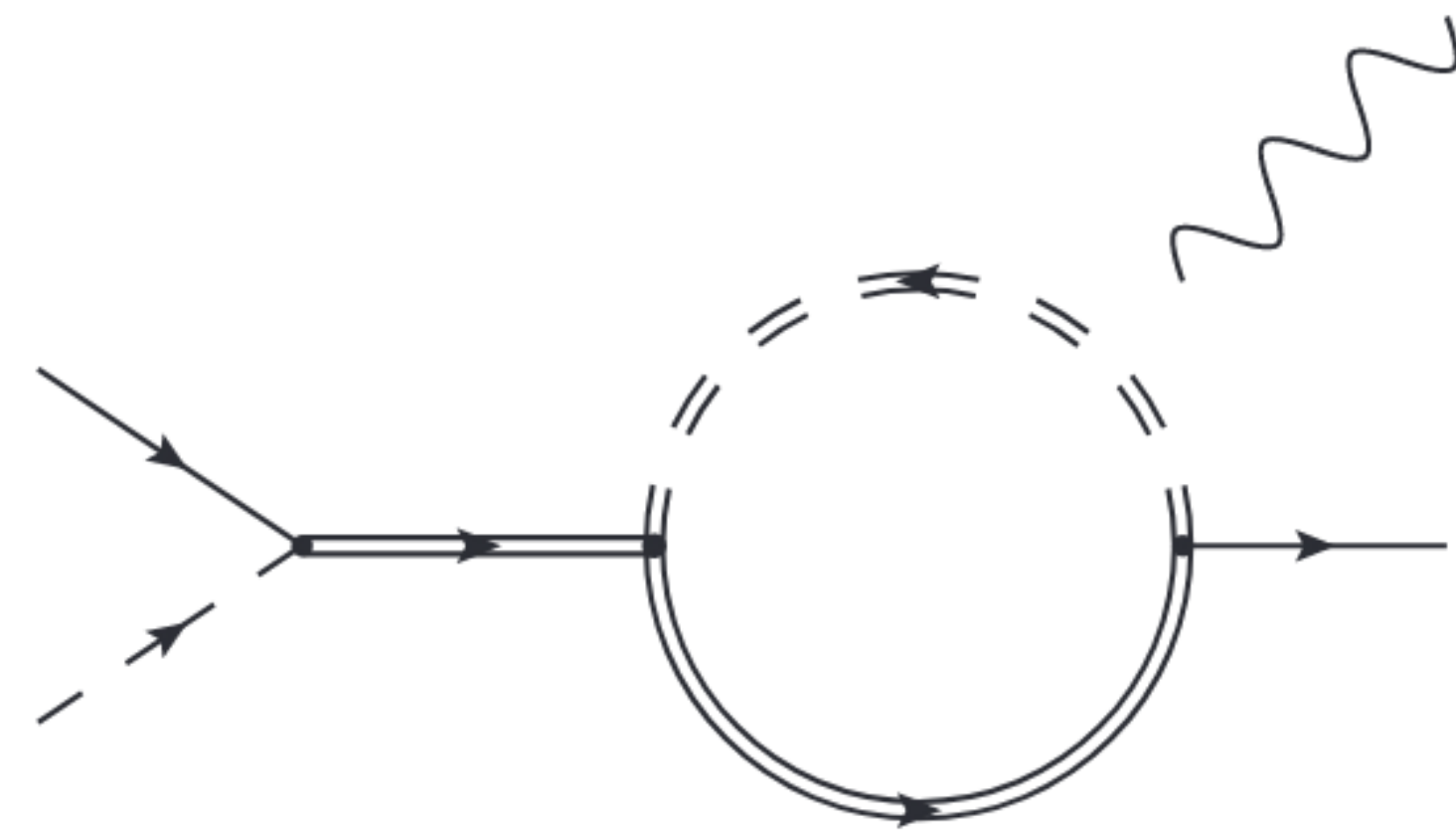
[P. Athron, C. Balázs, D. Jacob, W. Kotlarski, D. Stöckinger, H. Stöckinger-Kim, 2104.03691]

$$(\mathbf{1}, \mathbf{3}, 0)_0 \text{ and } (\mathbf{1}, \mathbf{2}, -1/2)_{1/2} \implies \Delta a_\mu < 0$$

(irrespective of  $\mathbb{Z}_2$ )



Yukawa-suppressed:  $<0$



Bridge: no definite sign

$$\alpha_{e\gamma} = y_b y_M y_F f(M_\Delta, M_\Xi)$$

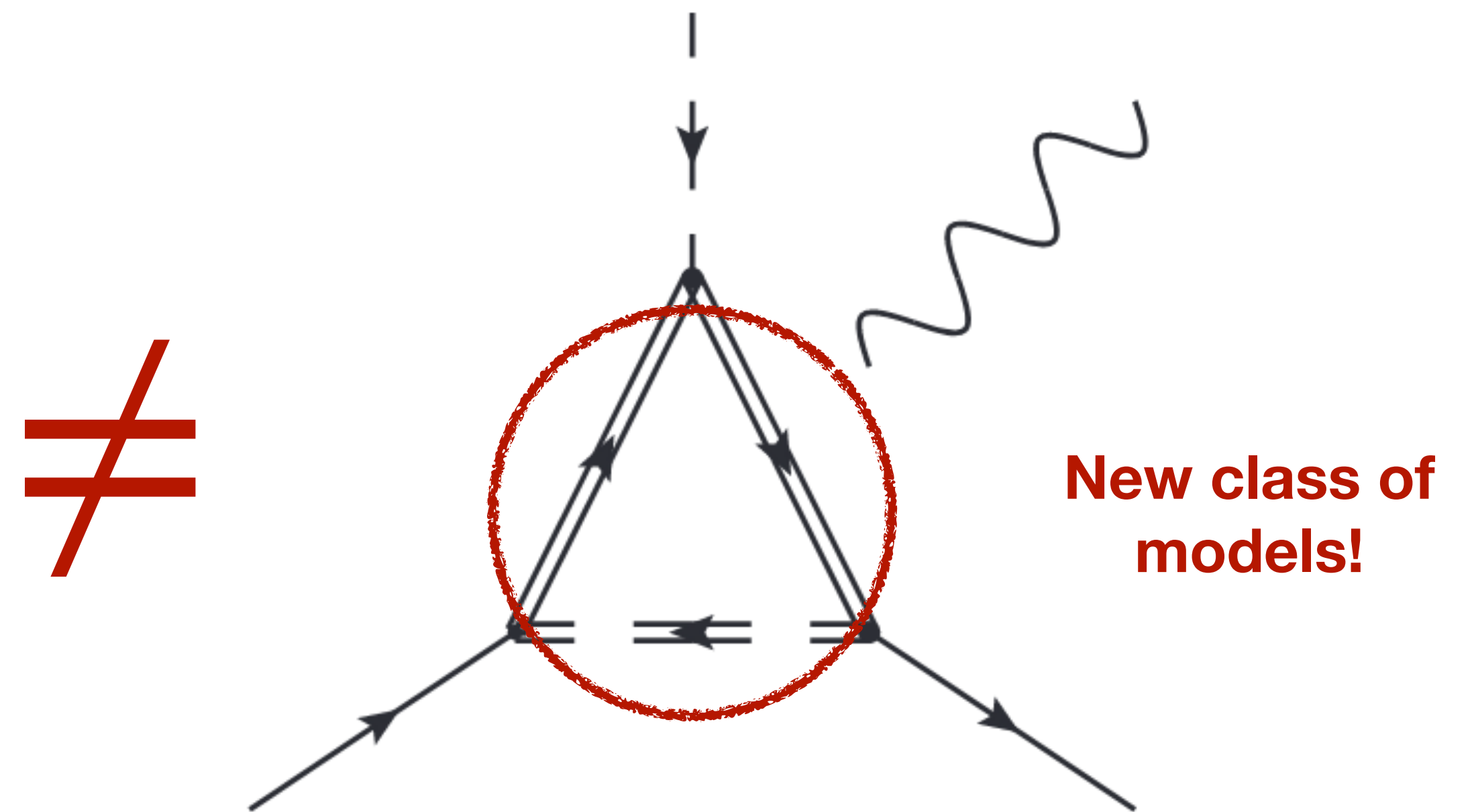


# 3 field extensions

Bridge	$(SU(2)_\Psi, SU(2)_\Phi)$
$E \sim (1, 1, -1)$	(1,1)
	(2,2)
	(3,3)
$\Delta \sim (1, 2, -1/2)$	(2,1)
	(2,3)
$\Sigma \sim (1, 3, -1)$	(2,2)
	(3,3)

# 3 field extensions

Bridge	$(SU(2)_\Psi, SU(2)_\Phi)$
$E \sim (1, 1, -1)$	(1,1)
	(2,2)
	(3,3)
$\Delta \sim (1, 2, -1/2)$	(2,1)
	(2,3)
	(3,3)
$\Sigma \sim (1, 3, -1)$	(2,2)
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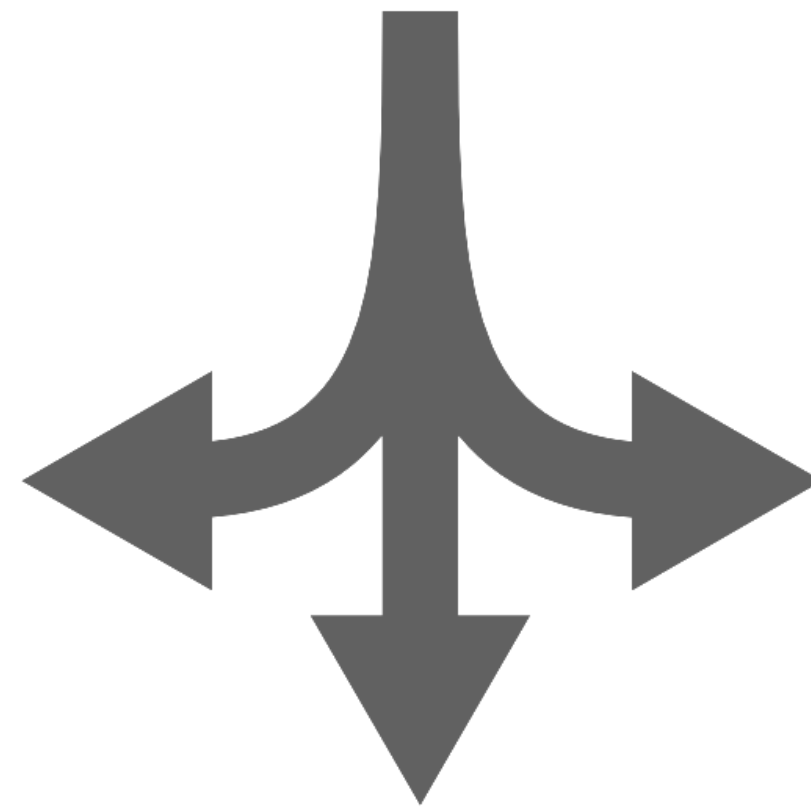


[A. Crivellin and M. Hoferichter, 2104.03202]  
 [L. Allwicher, L. Luzio, M. Fedele, F. Mescia, M. Nardecchia, 2105.13981]

# Connecting trees and bridges



Neutral B anomalies



Cabibbo angle anomaly



$$\Delta a_\mu$$

# Connecting trees and bridges

- $S_3$  leptoquark  $\sim (3,3, -1/3)$  to explain  $R_K^{(*)}$ .



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- $\Sigma \sim (1,3, -1)$  to explain CAA.



Tension between direct measurements of  $V_{us}$  and extraction from CKM unitarity ( $\sim 3 \sigma$  depending on the parametrization of  $\beta$  decays).

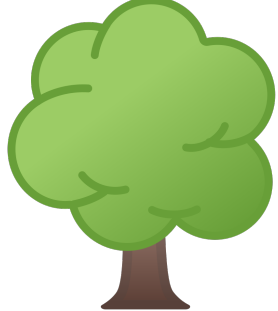
$$R(V_{us}) = 1 - \left( \frac{V_{ud}}{V_{us}} \right)^2 v^2 \left[ C_{H\ell}^{(3)} \right]_{22}$$

[M. Kirk, 2008.03261]

[A. Crivellin, F. Kirk, C. A. Manzari, M. Montull, 2008.01113]

Some tension with EWPD, worsened by CDF measurement.

# Connecting trees and bridges

- $S_3$  leptoquark  $\sim (3,3, -1/3)$  to explain  $R_K^{(*)}$ . 

- $\Sigma \sim (1,3, -1)$  to explain CAA. 

- $\Psi \sim (3,3, -4/3)$  to construct the bridge for  $\Delta a_\mu$



# One loop phenomenology

## Matchmakereft

A. Carmona, A. Lazopoulos, PO, J. Santiago  
2112.10787

Automatic full one loop matching

# One loop phenomenology

Matchma

A. Carmona, A. Lazopoulos  
2112.10

Automatic full one

```
F[105] == {
  ClassName      -> FH,
  Indices        -> {Index[Colour], Index[SU2W]},
  SelfConjugate  -> False,
  QuantumNumbers -> {Y -> -4/3},
  FullName       -> "heavy",
  Mass           -> MF,
  Width          -> 0
},

F[107] == {
  ClassName      -> HTri,
  Indices        -> {Index[SU2W]},
  SelfConjugate  -> False,
  QuantumNumbers -> {Y -> -1},
  FullName       -> "heavy",
  Mass           -> MT,
  Width          -> 0
},

S[107] == {
  ClassName      -> SH,
  Indices        -> {Index[Colour], Index[SU2W]},
  SelfConjugate  -> False,
  QuantumNumbers -> {Y -> -1/3},
  FullName       -> "heavy",
  Mass           -> MS,
  Width          -> 0
}
```



# One loop phenomenology

```
lag =  
yT[ff1] LLbar[sp1,ii,ff1].HTri[sp1,nn] Phi[jj] 2*Ta[nn,ii,jj]  
+ yQ[ff1] FHbar[sp1,cc,ii].LR[sp1,ff1] SH[cc,ii]  
+ YbridgeL HTribar[sp1,nn].left[FH[sp1,cc,ii]] SHbar[cc,jj]  
A. C I*fsu2[nn,ii,jj]  
+ YbridgeR HTribar[sp1,nn].right[FH[sp1,cc,ii]] SHbar[cc,jj]  
I*fsu2[nn,ii,jj]  
+ lamS[ff1,ff2] CC[QLbar[sp1,ii,ff1,cc]].LL[sp1,kk,ff2]  
Au Eps[ii,jj]2*Ta[nn,jj,kk] SHbar[cc,nn]
```

# One loop phenomenology

Matchmakereft

$$\alpha_{eW}[2, 2] \rightarrow \frac{3 g^2 M_F Y_{\text{bridgeR}} \left( M_F^2 - M_S^2 - M_S^2 \text{Log} \left[ \frac{M_F^2}{\mu^2} \right] + M_S^2 \text{Log} \left[ \frac{M_S^2}{\mu^2} \right] \right) y_Q[2] \times y_T[2]}{16 (M_F^2 - M_S^2)^2 M_T \pi^2}$$

Automatic full one loop matching

# One loop phenomenology

## Matchmakereft

A. Carmona, A. Lazopoulos, PO, J. Santiago  
2112.10787

Automatic full one loop matching

## smelli

P. Stangl 2012.12211

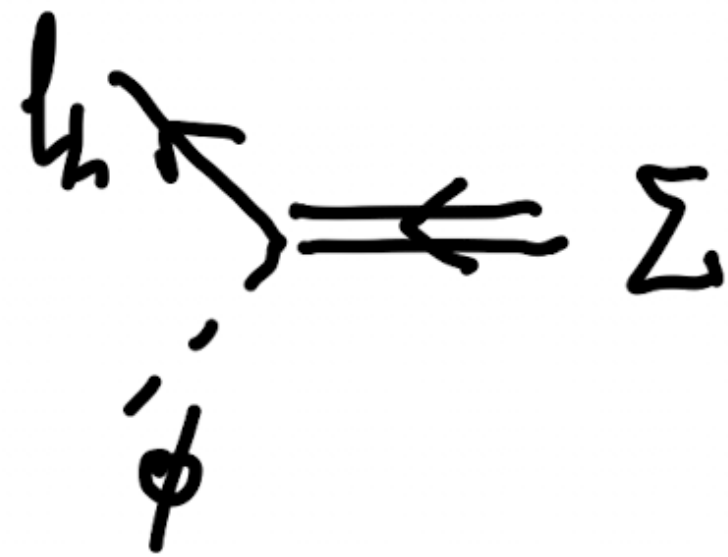
Fit to observables

# One loop phenomenology

$$\begin{aligned} \mathcal{L} \supset & y_T^i \bar{\ell}_{Li} \phi \sigma^I \Sigma_R^I + y_Q^i \bar{\Psi}_{QL}^I S_3^I \ell_{Ri} + y_b^L \epsilon^{IJK} \bar{\Sigma}_R^I \Psi_{Q,L}^J S_3^{K\dagger} \\ & + y_b^R \epsilon^{IJK} \bar{\Sigma}_L^I \Psi_{Q,R}^J S_3^{K\dagger} + \lambda_S^{ij} \bar{Q}_{Li}^c i \sigma^2 \sigma^I \ell_{Lj} S_3^{I\dagger} + \text{h.c.} \end{aligned}$$

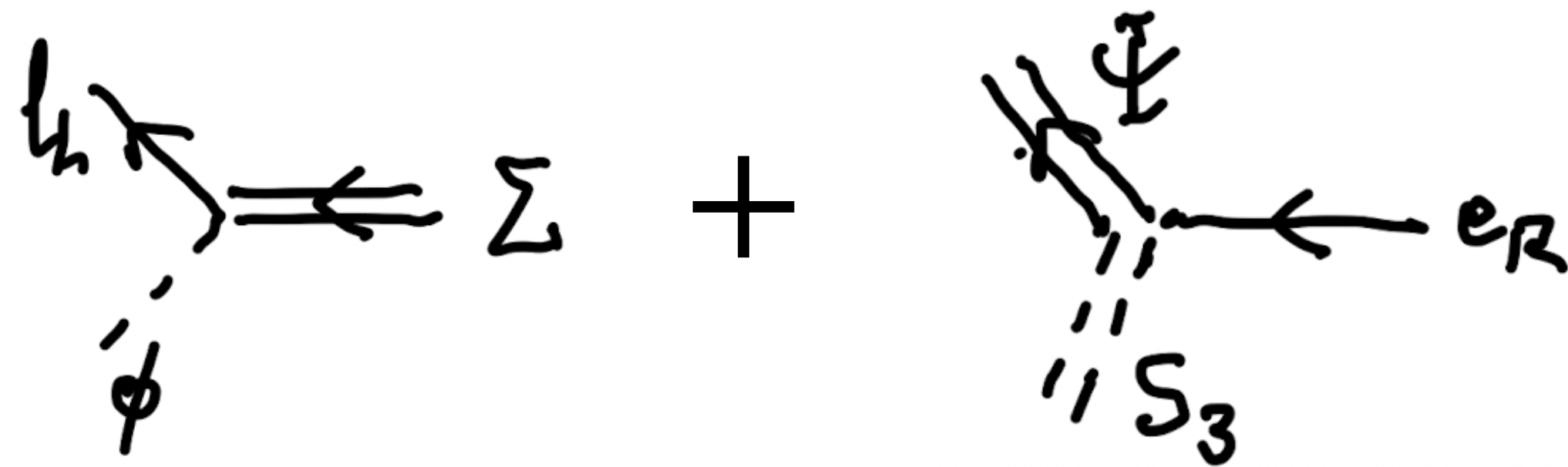
# One loop phenomenology

$$\mathcal{L} \supset \underbrace{y_T^i \bar{\ell}_{Li} \phi \sigma^I \Sigma_R^I}_{\text{red dashed box}} + y_Q^i \bar{\Psi}_{QL}^I S_3^I \ell_{Ri} + y_b^L \epsilon^{IJK} \bar{\Sigma}_R^I \Psi_{Q,L}^J S_3^{K\dagger} \\ + y_b^R \epsilon^{IJK} \bar{\Sigma}_L^I \Psi_{Q,R}^J S_3^{K\dagger} + \lambda_S^{ij} \bar{Q}_{Li}^c i\sigma^2 \sigma^I \ell_{Lj} S_3^{I\dagger} + \text{h.c.}$$



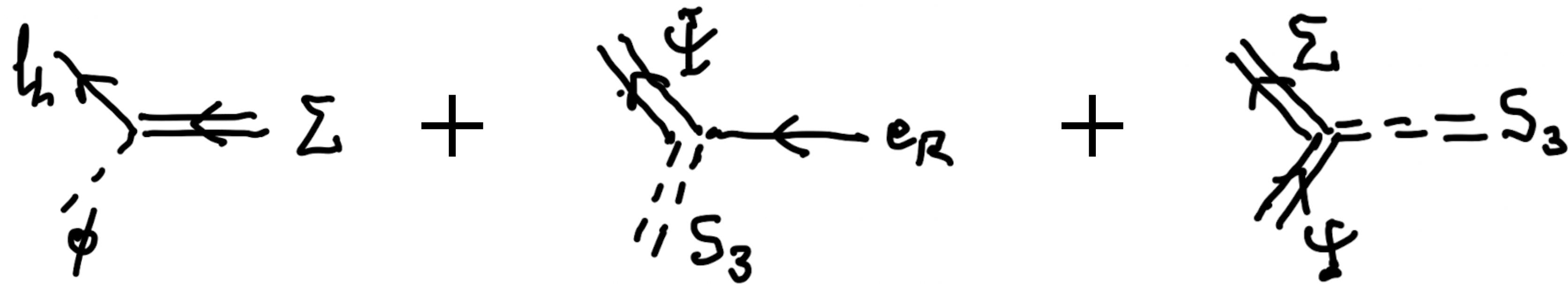
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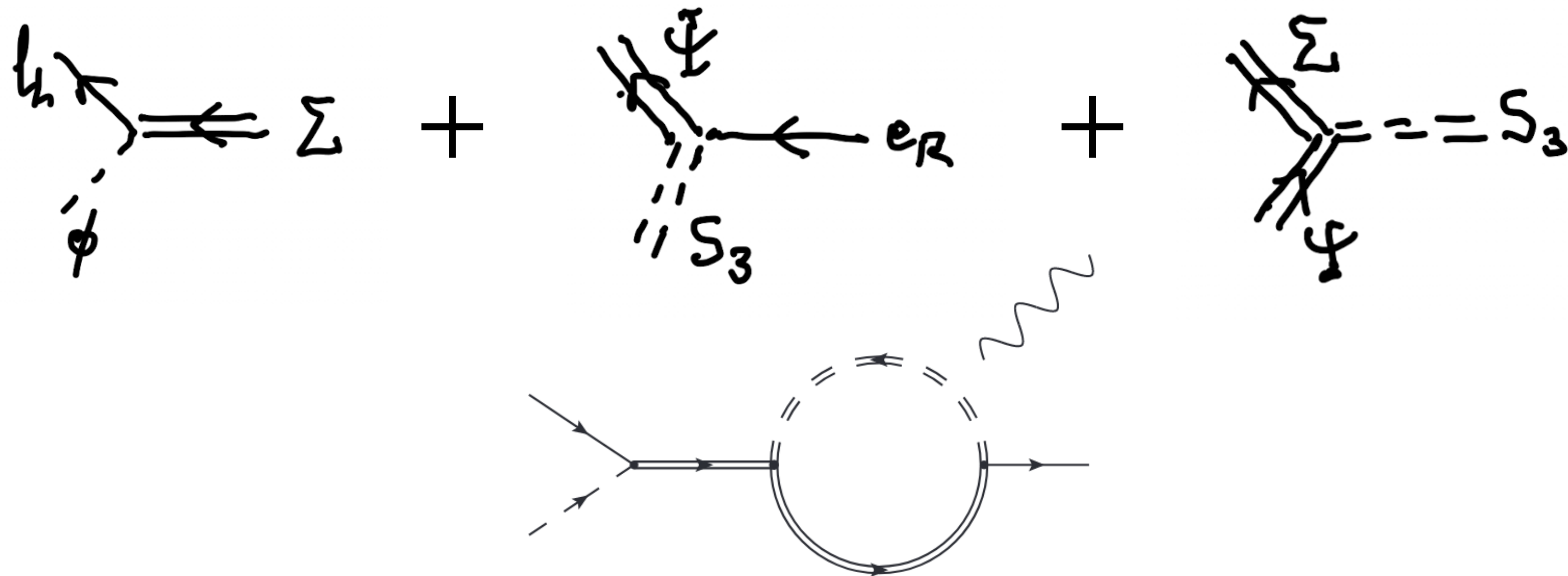
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# One loop phenomenology

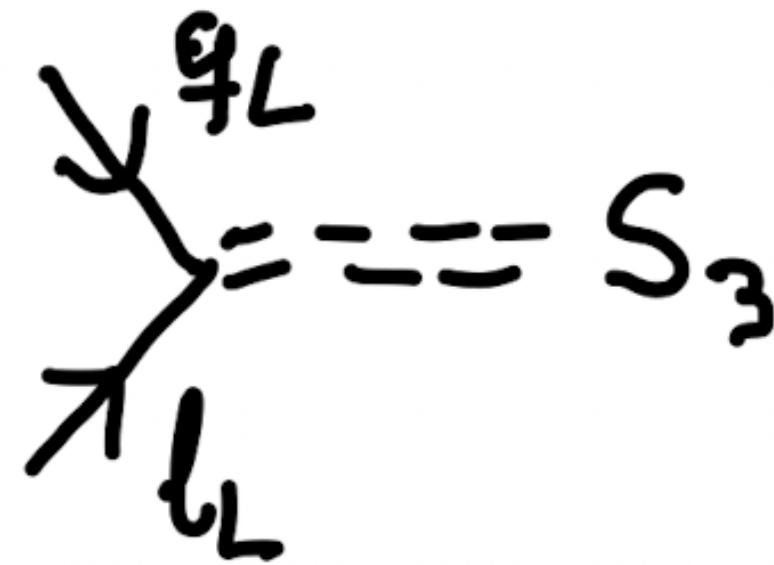
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# One loop phenomenology

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Defining the ratios:  $x_T \equiv y_T^\mu / M_T$      $x_F \equiv y_Q^\mu / M_F$      $x_S \equiv \lambda_S^{*s\mu} \lambda_S^{b\mu} / M_S^2$

Some considerations:

- $x_T$  bounded from EWPO:  $v x_T \leq 0.1(0.11)$
- No correction to the muon Yukawa!

# One loop phenomenology

$$\mathcal{L} \supset y_T^i \bar{\ell}_{Li} \phi \sigma^I \Sigma_R^I + y_Q^i \bar{\Psi}_{QL}^I S_3^I \ell_{Ri} + y_b^L \epsilon^{IJK} \bar{\Sigma}_R^I \Psi_{Q,L}^J S_3^{K\dagger} \\ + y_b^R \epsilon^{IJK} \bar{\Sigma}_L^I \Psi_{Q,R}^J S_3^{K\dagger} + \lambda_S^{ij} \bar{Q}_{Li}^c i \sigma^2 \sigma^I \ell_{Lj} S_3^{I\dagger} + \text{h.c.}$$

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We find the best fit point:

$$M_{S_3} = 2 \text{ TeV}$$

$$M_\Sigma = 3.4 \text{ TeV}$$

$$M_{\Psi_Q} = 4.6 \text{ TeV}$$

$$x_F = 0.2 \text{ TeV}^{-1}$$

$$x_T = 0.17 \text{ TeV}^{-1}$$

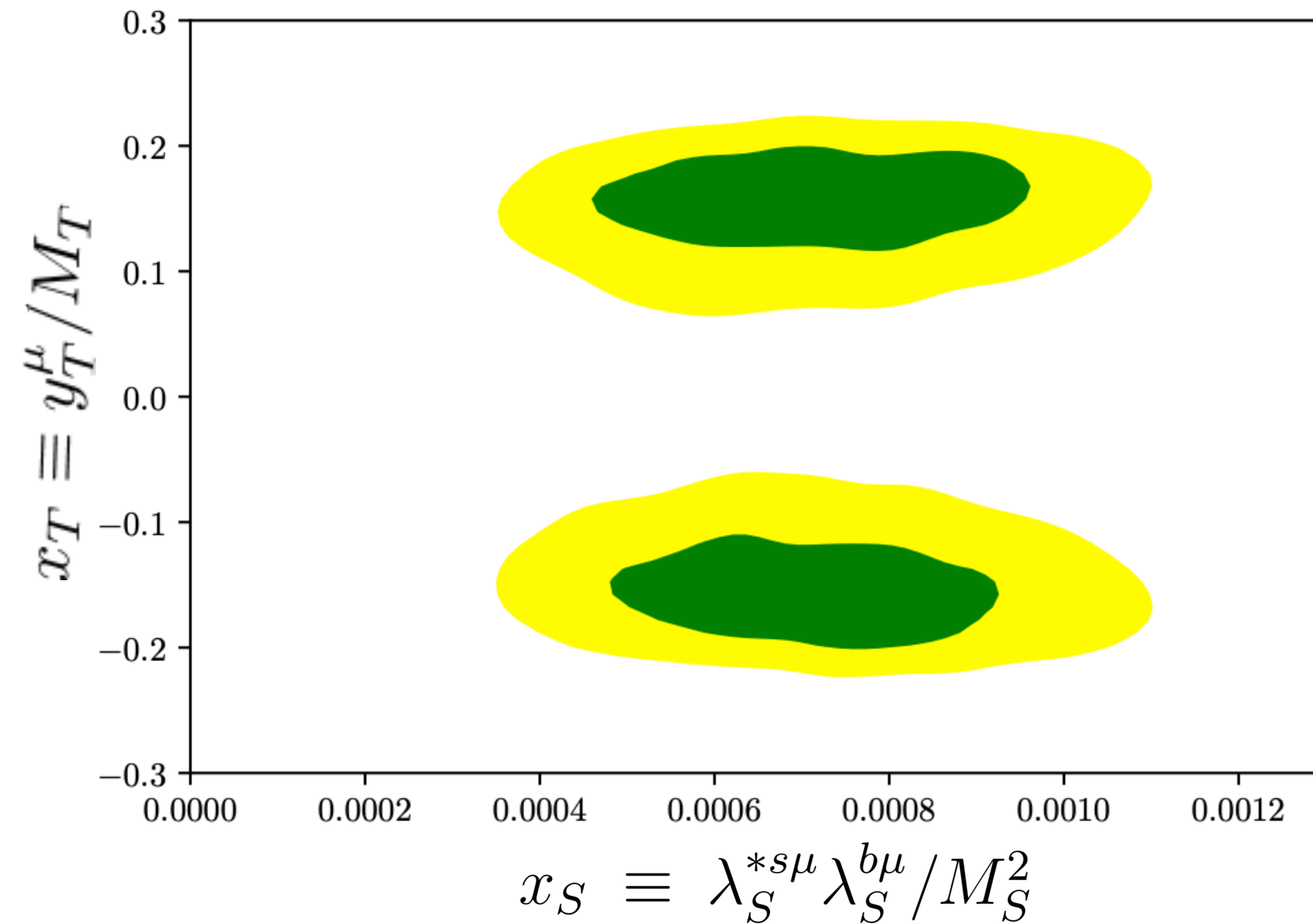
$$y_b^L = 0.10$$

$$x_S = 0.00078 \text{ TeV}^{-2}$$

$$\lambda_S^{b\mu} = 0.07$$

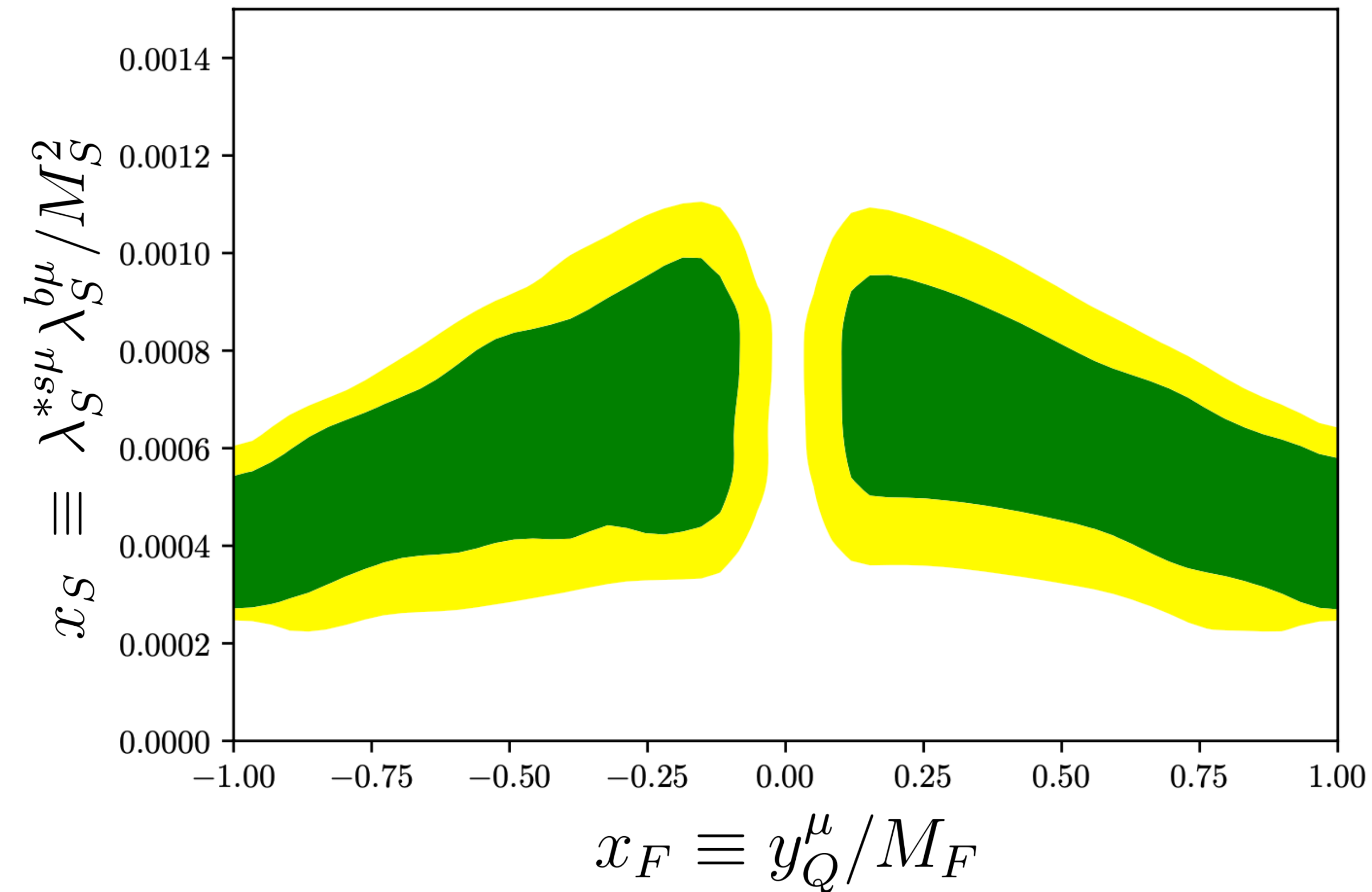
$$y_b^R = 0.13$$

# One loop phenomenology



- Results as expected from tree-level solutions.

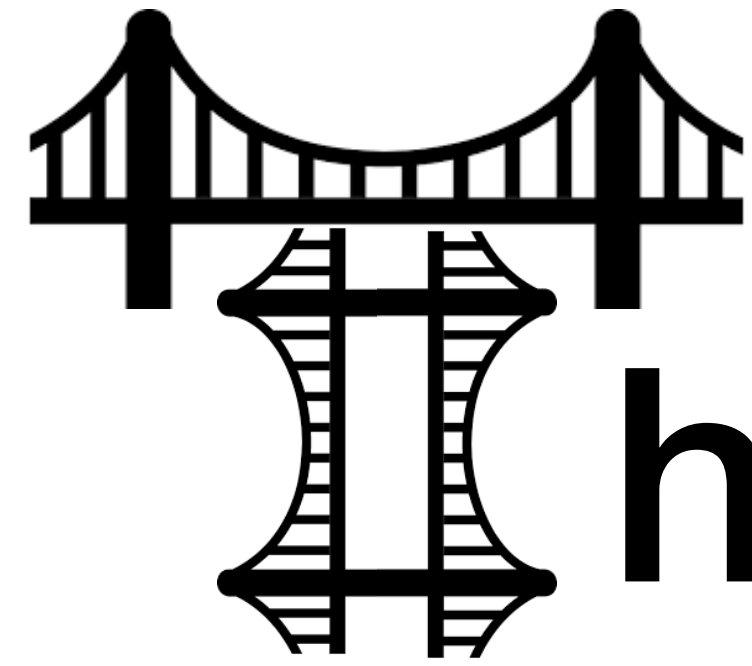
# One loop phenomenology



- Results as expected from tree-level solutions.
- Broad parameter space for couplings entering at one-loop.

# Conclusions

- We have classified and computed all possible bridge contributions to  $g-2$ .
- This opens new possibilities for SM extensions explaining this anomaly.
- A thorough classification still needed at one-loop.
- A complete classification of one-loop solutions to anomalies can be helpful to connect tree-level ones.



**hanks for your  
attention!**