

Drell-Yan tails as a probe of New Physics

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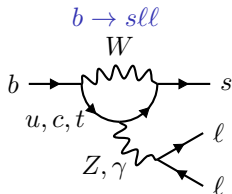
CERN

Intro and motivation

- TeV-scale New Physics (NP) is motivated e.g. by the hierarchy problem
- Such NP cannot have generic flavour structure
→ see e.g. $K - \bar{K}$ mixing $\Rightarrow \Lambda_{NP} \geq 10^{5-6}$ TeV
- For $\Lambda \gg v$, effects can be parametrised in SMEFT
- Need to study the flavour structure of the SMEFT
(2499 parameters at $d = 6$)
- B anomalies give some hints for NP in semileptonic interactions
- Constrain the same operators also at high- p_T (Drell-Yan tails)

B anomalies

(see talks by P. Hamilton, S. Klaver and C. Langenbruch)



LFU ratios:

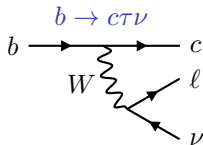
$$R_{X_s} = \frac{\mathcal{B}(B \rightarrow X_s \mu \mu)}{\mathcal{B}(B \rightarrow X_s e e)}$$

$$X_s = K, K^*, K_S, \phi$$

Other observables:

$$\mathcal{B}(B_s \rightarrow \mu \mu), \mathcal{B}(B_s \rightarrow \phi \mu \mu), \dots$$

- Deficit in muons



New results this week!

LFU ratios:

$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \nu)}{\mathcal{B}(B \rightarrow D^{(*)} \ell \nu)}$$

$$\ell = \mu, e$$

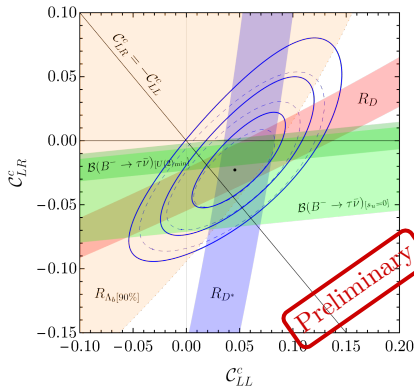
- Excess of τ leptons
- Many other ratios...

Combined explanations suggest TeV-scale new physics coupled mainly to the 3rd generation

$b \rightarrow cl\nu$

$$\mathcal{L}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{cb} [(1 + C_{LL}^c) \mathcal{O}_{LL}^c - 2C_{LR}^c \mathcal{O}_{LL}^c]$$

[Aebischer, Isidori, Pesut, Stefaneke, Wilsch, WIP]



$$\mathcal{O}_{LL}^c = (\bar{c}_L \gamma_\mu b_L)(\bar{\tau}_L \gamma^\mu \nu_L)$$

$$\mathcal{O}_{LR}^c = (\bar{c}_L b_R)(\bar{\tau}_R \nu_L)$$

- Compatible with left-handed scenario
- Contribution of right-handed currents also possible

Includes the new R_D/R_{D^*} measurements

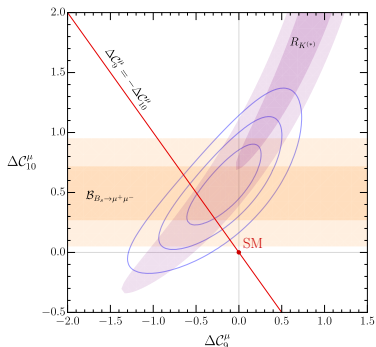
$b \rightarrow sll$

$$\mathcal{L}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{ts}^* V_{tb} \frac{\alpha}{4\pi} \sum_{\alpha, \ell} C_{\alpha}^{\ell} O_{\alpha}^{\ell}$$

$$O_9^{\ell} = (\bar{s}_L \gamma_{\mu} b_L)(\bar{\ell} \gamma^{\mu} \ell)$$

$$O_{10}^{\ell} = (\bar{s}_L \gamma_{\mu} b_L)(\bar{\ell} \gamma^{\mu} \gamma_5 \ell)$$

[Cornella et al. 2103.16558]



- $C_i^{\ell} = C_i^{\text{SM}} + \Delta C_i^{\ell}$
- Fit compatible with purely left-handed solution ($\Delta C_9 = -\Delta C_{10}$)
- LH NP preferred over SM at $\sim 5\sigma$ with clean observables only
- Including all $b \rightarrow sll$ observables: $\gg 5\sigma$

[1903.09578, 2011.01212, 2103.12738, 2103.13370]

- Global significance of NP: $\sim 4\sigma$

[Isidori et al. 2104.05631]

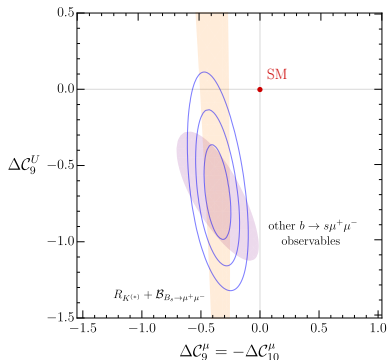
$b \rightarrow sll$

$$\mathcal{L}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{ts}^* V_{tb} \frac{\alpha}{4\pi} \sum_{\alpha,\ell} C_\alpha^\ell O_\alpha^\ell$$

$$O_9^\ell = (\bar{s}_L \gamma_\mu b_L)(\bar{\ell} \gamma^\mu \ell)$$

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[Cornella et al. 2103.16558]



- $C_i^\ell = C_i^{\text{SM}} + \Delta C_i^\ell$
- Separate LFU shift from LH new physics contribution:

$$\Delta C_i^U = C_i^e - C_i^{\text{SM}}$$

$$C_9^\mu = C_9^{\text{SM}} + \Delta C_9^U + \Delta C_L^\mu$$

$$C_{10}^\mu = C_{10}^{\text{SM}} - \Delta C_L^\mu$$

- Note: $\Delta C_{10}^U = 0$

A combined EFT explanation

- Left-handed charged current and neutral current operators related by $SU(2)_L$ symmetry:

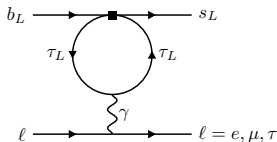
$$(\bar{u}_L^i \gamma_\mu d_L^j)(\bar{\ell}_L^\alpha \gamma^\mu \nu_L^\beta) \xleftrightarrow{SU(2)_L} (\bar{d}_L^i \gamma_\mu d_L^j)(\bar{\ell}_L^\alpha \gamma^\mu \ell_L^\beta)$$

- Minimal combined description in SMEFT, purely left-handed:

$$\mathcal{L} = -\frac{2}{v^2} \sum_a C_{LL}^{ij\alpha\beta} (\bar{q}_L^i \gamma_\mu \ell_L^\alpha)(\bar{\ell}_L^\beta \gamma^\mu q_L^j)$$

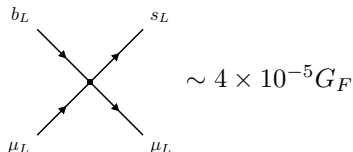
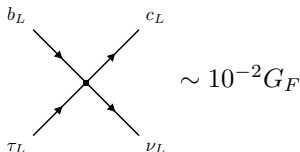
- R_D sets the size of $C_{LL}^{23\tau\tau}$
 \rightarrow RGE gives ΔC_9^U at $\mu \sim 5$ GeV

[Crivellin et al. 1807.02068]



What are the relative sizes of the $C^{ij\alpha\beta}$?

“Flavoured” SMEFT for the B -anomalies



- Suggests NP coupled stronger to third generation fermions
- Compatible with the $U(2)$ flavour symmetry scenario: [1512.01560]
Couplings to 2nd generation suppressed by powers of $\epsilon_{q,l}$

(see talk by N. Selimović)

$$\mathcal{L} = -\frac{2}{v^2} \sum_a \mathcal{C}_a^{ij\alpha\beta} \mathcal{O}_a^{ij\alpha\beta}$$

$$\mathcal{C}_{LL}^{33\tau\tau} \sim 0.01 \quad (\sim 10^{-2} G_F)$$

$U(2)$ scaling:

$$\mathcal{C}_{LL}^{23\tau\tau} \sim \epsilon_q \mathcal{C}_{LL}^{33\tau\tau} \quad \epsilon_q, \epsilon_l \sim 0.1$$

$$\mathcal{C}_{LL}^{23\mu\mu} \sim \epsilon_q \epsilon_l^2 \mathcal{C}_{LL}^{33\tau\tau}$$

$$\mathcal{O}_{LL}^{ij\alpha\beta} = (\bar{q}_L^i \gamma_\mu \ell_L^\alpha) (\bar{\ell}_L^\beta \gamma^\mu q_L^j)$$

$$\mathcal{O}_{LR}^{ij\alpha\beta} = (\bar{q}_L^i \gamma_\mu \ell_L^\alpha) (\bar{e}_R^\beta \gamma^\mu d_R^j)$$

$$\mathcal{O}_{RR}^{ij\alpha\beta} = (\bar{d}_R^i \gamma_\mu e_R^\alpha) (\bar{e}_R^\beta \gamma^\mu d_R^j)$$

+ all couplings with RH
light fields set to zero



“Flavoured” SMEFT for the B -anomalies

$$\mathcal{L} = -\frac{2}{v^2} \sum_a \mathcal{C}_a^{ij\alpha\beta} \mathcal{O}_a^{ij\alpha\beta}$$

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$U(2)$ scaling:

$$\mathcal{C}_{LL}^{23\tau\tau} \sim \epsilon_q \mathcal{C}_{LL}^{33\tau\tau} \quad \epsilon_q, \epsilon_l \sim 0.1$$

$$\mathcal{C}_{LL}^{23\mu\mu} \sim \epsilon_q \epsilon_l^2 \mathcal{C}_{LL}^{33\tau\tau}$$

$$\mathcal{O}_{LL}^{ij\alpha\beta} = (\bar{q}_L^i \gamma_\mu \ell_L^\alpha) (\bar{\ell}_L^\beta \gamma^\mu q_L^j)$$

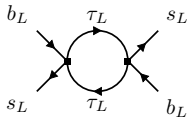
$$\mathcal{O}_{LR}^{ij\alpha\beta} = (\bar{q}_L^i \gamma_\mu \ell_L^\alpha) (\bar{e}_R^\beta \gamma^\mu d_R^j)$$

$$\mathcal{O}_{RR}^{ij\alpha\beta} = (\bar{d}_R^i \gamma_\mu e_R^\alpha) (\bar{e}_R^\beta \gamma^\mu d_R^j)$$

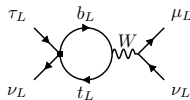
+ all couplings with RH
light fields set to zero

Constraints from other low-energy observables:

$$\Delta F = 2$$



τ LFU tests



“Flavoured” SMEFT for the B -anomalies

$$\mathcal{L} = -\frac{2}{v^2} \sum_a \mathcal{C}_a^{ij\alpha\beta} \mathcal{O}_a^{ij\alpha\beta}$$

$$\mathcal{C}_{LL}^{33\tau\tau} \sim 0.01 \quad (\sim 10^{-2} G_F)$$

$U(2)$ scaling:

$$\mathcal{O}_{LL}^{ij\alpha\beta} = (\bar{q}_L^i \gamma_\mu \ell_L^\alpha) (\bar{\ell}_L^\beta \gamma^\mu q_L^j)$$

$$\mathcal{C}_{LL}^{23\tau\tau} \sim \epsilon_q \mathcal{C}_{LL}^{33\tau\tau} \quad \epsilon_q, \epsilon_l \sim 0.1$$

$$\mathcal{O}_{LR}^{ij\alpha\beta} = (\bar{q}_L^i \gamma_\mu \ell_L^\alpha) (\bar{e}_R^\beta \gamma^\mu d_R^j)$$

$$\mathcal{C}_{LL}^{23\mu\mu} \sim \epsilon_q \epsilon_l^2 \mathcal{C}_{LL}^{33\tau\tau}$$

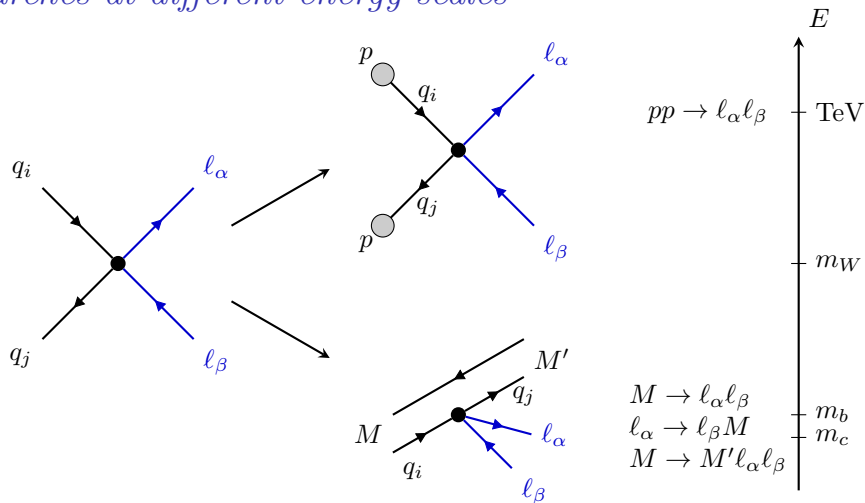
$$\mathcal{O}_{RR}^{ij\alpha\beta} = (\bar{d}_R^i \gamma_\mu e_R^\alpha) (\bar{e}_R^\beta \gamma^\mu d_R^j)$$

+ all couplings with RH
light fields set to zero

R_D/R_{D^*} point to the TeV-scale
 \Rightarrow we can probe the same interactions
also at high-energies



Searches at different energy scales



High- p_T searches can probe the same operators directly constrained by flavour-physics experiments

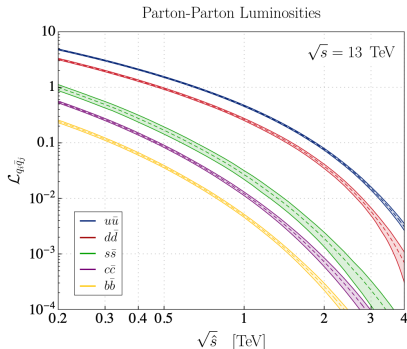
[see also 1609.07138, 1704.09015, 1811.07920, 2003.12421, ...]

Flavour in Drell-Yan tails

[Angelescu, Faroughy, Sumensari 2002.05684]

- 5 active flavours in the proton
- Drell-Yan at LHC:
 - $pp \rightarrow \ell_\alpha^+ \ell_\beta^-$
 - $pp \rightarrow \ell_\alpha^+ \nu_\beta$
- Hadronic cross-section:

$$\sigma(pp \rightarrow \ell_\alpha \ell_\beta) = \mathcal{L}_{ij} \times \hat{\sigma}_{ij}^{\alpha\beta}$$



- $\hat{\sigma}_{ij}^{\alpha\beta} = \hat{\sigma}(q_i \bar{q}_j \rightarrow \ell_\alpha \ell_\beta)$ partonic cross-section
→ energy-enhanced in the EFT. With 4-fermion operators:

$$\hat{\sigma}_{ij}^{\alpha\beta} \propto \frac{\hat{s}^2}{\Lambda^4}$$

- Heavy flavours suppressed by parton luminosities \mathcal{L}_{ij}
- Energy enhancement can overcome PDF suppression

Example: charm observables

[Fuentes-Martín, Greljo, Camalich, Ruiz-Alvarez 2003.12421]

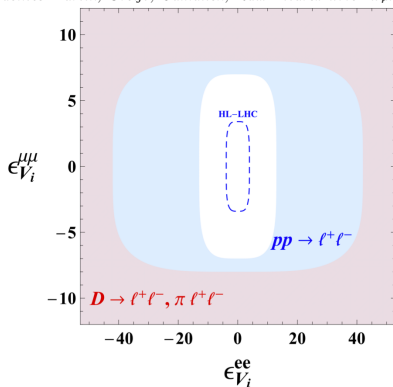
Compare constraints on semileptonic interactions involving charm quarks:

- D meson decays: $c \rightarrow ull$
- Drell-Yan: $cu \rightarrow ll$

LHC already provides better constraints!

Other examples:

- de Blas, Chala, Santiago 1307.5068
- Angelescu, Faroughy, Sumensari 2002.05684
- Dawson, Giardino, Ismail 1811.12260
- Marzocca, Min, Son 2008.07541

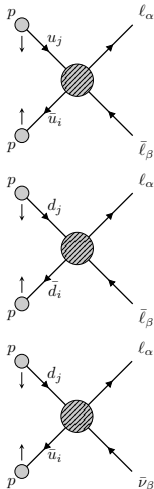


Drell-Yan cross-section

Parton-level amplitude:

$$\begin{aligned}
 \mathcal{A}(\bar{q}_i q'_j \rightarrow \ell_\alpha \bar{\ell}'_\beta) = \frac{1}{v^2} \sum_{XY} \{ & (\bar{\ell}_\alpha \gamma^\mu \mathbb{P}_X \ell'_\beta) (\bar{q}_i \gamma_\mu \mathbb{P}_Y q'_j) [\mathcal{F}_V^{XY, qq'}(\hat{s}, \hat{t})]_{\alpha\beta ij} \\
 & + (\bar{\ell}_\alpha \mathbb{P}_X \ell'_\beta) (\bar{q}_i \mathbb{P}_Y q'_j) [\mathcal{F}_S^{XY, qq'}(\hat{s}, \hat{t})]_{\alpha\beta ij} \\
 & + (\bar{\ell}_\alpha \sigma_{\mu\nu} \mathbb{P}_X \ell'_\beta) (\bar{q}_i \sigma^{\mu\nu} \mathbb{P}_Y q'_j) \delta^{XY} [\mathcal{F}_T^{XY, qq'}(\hat{s}, \hat{t})]_{\alpha\beta ij} \\
 & + (\bar{\ell}_\alpha \gamma_\mu \mathbb{P}_X \ell'_\beta) (\bar{q}_i \sigma^{\mu\nu} \mathbb{P}_Y q'_j) \frac{ik_\nu}{v} [\mathcal{F}_{D_q}^{XY, qq'}(\hat{s}, \hat{t})]_{\alpha\beta ij} \\
 & + (\bar{\ell}_\alpha \sigma^{\mu\nu} \mathbb{P}_X \ell'_\beta) (\bar{q}_i \gamma_\mu \mathbb{P}_Y q'_j) \frac{ik_\nu}{v} [\mathcal{F}_{D_\ell}^{XY, qq'}(\hat{s}, \hat{t})]_{\alpha\beta ij} \}
 \end{aligned}$$

- $X, Y \in L, R$, $\hat{s} = k^2 = (p_\ell + p_{\ell'})^2$, $\hat{t} = (p_\ell - p_{q'})^2$
- General parametrisation of tree-level effects invariant under $SU(3)_c \times U(1)_e$
- Captures both local and non-local effects



Local and non-local contributions

$$\mathcal{F}_I(\hat{s}, \hat{t}) = \mathcal{F}_{I,\text{Reg}}(\hat{s}, \hat{t}) + \mathcal{F}_{I,\text{Poles}}(\hat{s}, \hat{t})$$

- Analytic function of \hat{s}, \hat{t}
- Describes contact interactions
→ SMEFT
- Expansion for $v^2, |\hat{s}|, |\hat{t}| < \Lambda^2$:

$$\mathcal{F}_{I,\text{Reg}}(\hat{s}, \hat{t}) = \sum_{n,m=0}^{\infty} \mathcal{F}_{I(n,m)} \left(\frac{\hat{s}}{v^2}\right)^n \left(\frac{\hat{t}}{v^2}\right)^m$$

- Isolated simple poles in \hat{s}, \hat{t}
- Non-local effects due to exchange of a mediator (SM and NP)

$$\mathcal{F}_{I,\text{Poles}}(\hat{s}, \hat{t}) = \sum_a \frac{v^2 \mathcal{S}_{I(a)}}{\hat{s} - \Omega_a} + \sum_b \frac{v^2 \mathcal{T}_{I(b)}}{\hat{t} - \Omega_b} - \sum_c \frac{v^2 \mathcal{U}_{I(c)}}{\hat{s} + \hat{t} + \Omega_c}$$

$$\Omega_i = m_i^2 - im_i \Gamma_i \quad \hat{u} = -\hat{s} - \hat{t}$$

This encapsulates all possible tree-level effects with purely leptonic final states

Hadronic cross-section

$$\begin{aligned}
 \mathcal{A}(\bar{q}_i q'_j \rightarrow \ell_\alpha \bar{\ell}_\beta) = \frac{1}{v^2} \sum_{XY} \{ & (\bar{\ell}_\alpha \gamma^\mu \mathbb{P}_X \ell'_\beta) (\bar{q}_i \gamma_\mu \mathbb{P}_Y q'_j) [\mathcal{F}_V^{XY, qq'}(\hat{s}, \hat{t})]_{\alpha\beta ij} \\
 & + (\bar{\ell}_\alpha \mathbb{P}_X \ell'_\beta) (\bar{q}_i \mathbb{P}_Y q'_j) [\mathcal{F}_S^{XY, qq'}(\hat{s}, \hat{t})]_{\alpha\beta ij} \\
 & + (\bar{\ell}_\alpha \sigma_{\mu\nu} \mathbb{P}_X \ell'_\beta) (\bar{q}_i \sigma^{\mu\nu} \mathbb{P}_Y q'_j) \delta^{XY} [\mathcal{F}_T^{XY, qq'}(\hat{s}, \hat{t})]_{\alpha\beta ij} \\
 & + (\bar{\ell}_\alpha \gamma_\mu \mathbb{P}_X \ell'_\beta) (\bar{q}_i \sigma^{\mu\nu} \mathbb{P}_Y q'_j) \frac{ik_\nu}{v} [\mathcal{F}_{D_q}^{XY, qq'}(\hat{s}, \hat{t})]_{\alpha\beta ij} \\
 & + (\bar{\ell}_\alpha \sigma^{\mu\nu} \mathbb{P}_X \ell'_\beta) (\bar{q}_i \gamma_\mu \mathbb{P}_Y q'_j) \frac{ik_\nu}{v} [\mathcal{F}_{D_\ell}^{XY, qq'}(\hat{s}, \hat{t})]_{\alpha\beta ij} \}
 \end{aligned}$$

parton-level
amplitude

$$\sigma_B(pp \rightarrow \ell_\alpha^- \ell_\beta^+) = \frac{1}{48\pi v^2} \sum_{XY, IJ} \sum_{ij} \int_{m_{\ell\ell_0}^2}^{m_{\ell\ell_1}^2} \frac{d\hat{s}}{s} \int_{-\hat{s}}^0 \frac{d\hat{t}}{v^2} M_{IJ}^{XY} \mathcal{L}_{ij} [\mathcal{F}_I^{XY, qq}]_{\alpha\beta ij} [\mathcal{F}_J^{XY, qq}]_{\alpha\beta ij}^*$$

interference
matrix

$$M^{XY}(\hat{s}, \hat{t}) = \begin{pmatrix} M_{VV}^{XY}(\hat{t}/\hat{s}) & 0 & 0 & 0 & 0 \\ 0 & M_{SS}^{XY}(\hat{t}/\hat{s}) & M_{ST}^{XY}(\hat{t}/\hat{s}) & 0 & 0 \\ 0 & M_{ST}^{XY}(\hat{t}/\hat{s}) & M_{TT}^{XY}(\hat{t}/\hat{s}) & 0 & 0 \\ 0 & 0 & 0 & \frac{\hat{s}}{v^2} M_{DD}^{XY}(\hat{t}/\hat{s}) & 0 \\ 0 & 0 & 0 & 0 & \frac{\hat{s}}{v^2} M_{DD}^{XY}(\hat{t}/\hat{s}) \end{pmatrix}$$

parton
luminosities

$$\mathcal{L}_{ij}(\hat{s}) \equiv \int_{\hat{s}/s}^1 \frac{dx}{x} \left[f_{\bar{q}_i}(x, \mu) f_{q_j}\left(\frac{\hat{s}}{sx}, \mu\right) + (\bar{q}_i \leftrightarrow q_j) \right]$$





High- p_T Tails

A Mathematica package for flavour physics in Drell-Yan tails

with D. Faroughy, F. Jaffredo, O. Sumensari and F. Wilsch

arXiv: 2207.10714, 2207.10756

<https://highpt.github.io/>



Universität
Zürich^{UZH}

HighPT: *Generalities*

- Includes (some of) the latest LHC Drell-Yan searches
- Large variety of NP scenarios:
 - SMEFT $d = 6, d = 8$ (σ computed up to $\mathcal{O}(\Lambda^{-4})$)
 - Bosonic mediators: leptoquarks (s -channel mediators will come in the future) \rightarrow propagation effects
- Allows to compute:
 - Hadronic cross-sections
 - Event yields
 - χ^2 likelihood as function of Wilson coefficients/coupling constants
- Includes a `python` output routine using `WCxf` to perform analyses outside `Mathematica`
 \rightarrow possible interface with other existing codes/tools
(e.g. `smelli/flavio`)

\rightarrow Extract bounds on form-factors/Wilson coefficients/NP couplings

LHC searches

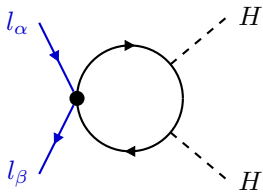
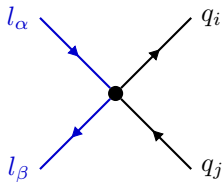
Process	Experiment	Luminosity	Ref.	x_{obs}	x
$pp \rightarrow \tau\tau$	ATLAS	139 fb^{-1}	2002.12223	$m_T^{\text{tot}}(\tau_h^1, \tau_h^2, \cancel{E}_T)$	$m_{\tau\tau}$
$pp \rightarrow \mu\mu$	CMS	140 fb^{-1}	2103.02708	$m_{\mu\mu}$	$m_{\mu\mu}$
$pp \rightarrow ee$	CMS	137 fb^{-1}	2103.02708	m_{ee}	m_{ee}
$pp \rightarrow \tau\nu$	ATLAS	139 fb^{-1}	ATLAS-CONF-2021-025	$m_T(\tau_h, \cancel{E}_T)$	$p_T(\tau)$
$pp \rightarrow \mu\nu$	ATLAS	139 fb^{-1}	1906.05609	$m_T(\mu, \cancel{E}_T)$	$p_T(\mu)$
$pp \rightarrow e\nu$	ATLAS	139 fb^{-1}	1906.05609	$m_T(e, \cancel{E}_T)$	$p_T(e)$
$pp \rightarrow \tau\mu$	CMS	138 fb^{-1}	2205.06709	$m_{\tau_h\mu}^{\text{col}}$	$m_{\tau\mu}$
$pp \rightarrow \tau e$	CMS	138 fb^{-1}	2205.06709	$m_{\tau_h e}^{\text{col}}$	$m_{\tau e}$
$pp \rightarrow \mu e$	CMS	138 fb^{-1}	2205.06709	$m_{\mu e}$	$m_{\mu e}$



Leptoquarks in HighPT

	SM rep.	Spin	\mathcal{L}_{int}
S_1	$(\bar{\mathbf{3}}, \mathbf{1}, 1/3)$	0	$\mathcal{L}_{S_1} = [y_1^L]_{i\alpha} S_1 \bar{q}_i^c \ell_\alpha + [y_1^R]_{i\alpha} S_1 \bar{u}_i^c e_\alpha + [\tilde{y}_1^R]_{i\alpha} S_1 \bar{d}_i^c N_\alpha + \text{h.c.}$
\tilde{S}_1	$(\bar{\mathbf{3}}, \mathbf{1}, 4/3)$	0	$\mathcal{L}_{\tilde{S}_1} = [\tilde{y}_1^R]_{i\alpha} \tilde{S}_1 \bar{d}_i^c e_\alpha + \text{h.c.}$
U_1	$(\mathbf{3}, \mathbf{1}, 2/3)$	1	$\mathcal{L}_{U_1} = [x_1^L]_{i\alpha} \bar{q}_i \psi_1 l_\alpha + [x_1^R]_{i\alpha} \bar{d}_i \psi_1 e_\alpha + [\bar{x}_1^R]_{i\alpha} \bar{u}_i \psi_1 N_\alpha + \text{h.c.}$
\tilde{U}_1	$(\mathbf{3}, \mathbf{1}, 5/3)$	1	$\mathcal{L}_{\tilde{U}_1} = [\tilde{x}_1^R]_{i\alpha} \bar{u}_i \tilde{\psi}_1 e_\alpha + \text{h.c.}$
R_2	$(\mathbf{3}, \mathbf{2}, 7/6)$	0	$\mathcal{L}_{R_2} = -[y_2^L]_{i\alpha} \bar{u}_i R_2 \ell_\alpha + [y_2^R]_{i\alpha} \bar{q}_i e_\alpha R_2 + \text{h.c.}$
\tilde{R}_2	$(\mathbf{3}, \mathbf{2}, 1/6)$	0	$\mathcal{L}_{\tilde{R}_2} = -[\tilde{y}_2^L]_{i\alpha} \bar{d}_i \tilde{R}_2 \ell_\alpha + [\tilde{y}_2^R]_{i\alpha} \bar{q}_i N_\alpha \tilde{R}_2 + \text{h.c.}$
V_2	$(\bar{\mathbf{3}}, \mathbf{2}, 5/6)$	1	$\mathcal{L}_{V_2} = [x_2^L]_{i\alpha} \bar{d}_i^c \psi_2 \ell_\alpha + [x_2^R]_{i\alpha} \bar{q}_i^c \psi_2 e_\alpha + \text{h.c.}$
\tilde{V}_2	$(\bar{\mathbf{3}}, \mathbf{2}, -1/6)$	1	$\mathcal{L}_{\tilde{V}_2} = [\tilde{x}_2^L]_{i\alpha} \bar{u}_i^c \tilde{\psi}_2 \ell_\alpha + [\tilde{x}_2^R]_{i\alpha} \bar{q}_i^c \tilde{\psi}_2 N_\alpha + \text{h.c.}$
S_3	$(\bar{\mathbf{3}}, \mathbf{3}, 1/3)$	0	$\mathcal{L}_{S_3} = [y_3^L]_{i\alpha} \bar{q}_i^c \epsilon (\tau^I S_3^I) l_\alpha + \text{h.c.}$
U_3	$(\mathbf{3}, \mathbf{3}, 2/3)$	1	$\mathcal{L}_{U_3} = [x_3^L]_{i\alpha} \bar{q}_i (\tau^I \psi_3^I) l_\alpha + \text{h.c.}$

Digression on RGE effects: EW precision observables



Semileptonic operator at scale Λ :

$$[\mathcal{O}_{lq}^{(3)}]_{\alpha\beta ij} = (\bar{l}_\alpha \gamma_\mu \sigma^I l_\beta) (\bar{q}_i \gamma^\mu \sigma^I q_j)$$

RGE:

[1310.4838]

$$[\dot{\mathcal{C}}_{Hl}^{(3)}]_{\alpha\beta} \supset 2N_c [\mathcal{C}_{lq}^{(3)}]_{\alpha\beta kl} [Y_d^\dagger Y_d + Y_u^\dagger Y_u]_{lk}$$

$$[\mathcal{O}_{Hl}^{(3)}]_{\alpha\beta} = (H^\dagger i D_\mu \sigma^I H) (\bar{l}_\alpha \gamma^\mu \sigma^I l_\beta)$$

→ Modification of W couplings to leptons:

$$\mathcal{L}_{\text{eff}}^W = -\frac{g}{\sqrt{2}} \sum_{\alpha,\beta} \left[g_{\ell_L}^W{}^{\alpha\beta} (\bar{\ell}_{L\alpha} \gamma^\mu \nu_{L\beta}) \right] W_\mu + \text{h.c.}$$

$$g_{\ell_L}^W{}^{\alpha\beta} = \delta_{\alpha\beta} + \frac{v^2}{\Lambda^2} [\mathcal{C}_{Hl}^{(3)}]_{\alpha\beta}$$

e.g. $W \rightarrow \tau\nu, \dots$

Example: leptoquark solutions for R_D, R_{D^*}

(see talks by B. Allanach, U.

Haisch, F. Jaffredo, N. Selimović)

Three possible scenarios:

[2103.12504]

- U_1 :

$$[\mathcal{C}_{lq}^{(1)}]_{3323} = [\mathcal{C}_{lq}^{(3)}]_{3323}, \quad [\mathcal{C}_{lq}^{(1)}]_{3333} = [\mathcal{C}_{lq}^{(3)}]_{3333}$$

+ possibility of RH currents

- S_1 :

$$[\mathcal{C}_{lq}^{(1)}]_{3333} = -[\mathcal{C}_{lq}^{(3)}]_{3333}, \quad [\mathcal{C}_{lequ}^{(1)}]_{3332} = -4[\mathcal{C}_{lequ}^{(3)}]_{3332}$$

- R_2 :

$$[\mathcal{C}_{lequ}^{(1)}]_{3332} = 4[\mathcal{C}_{lequ}^{(3)}]_{3332}$$

Compare the combined constraints from low-energy, EW and high- p_T
between the EFT approach and the explicit mediators

→ Choosing two LQ couplings at a time corresponds to more than two SMEFT operators, get more correlations between different observables

Tree-level LQ matching

Field	S_1	R_2	U_1
Quantum Numbers	$(\bar{\mathbf{3}}, \mathbf{1}, 1/3)$	$(\mathbf{3}, \mathbf{2}, 7/6)$	$(\mathbf{3}, \mathbf{1}, 2/3)$
$[\mathcal{C}_{ledq}]_{\alpha\beta ij}$	–	–	$2[x_1^L]_{i\alpha}^* [x_1^R]_{j\beta}$
$[\mathcal{C}_{lequ}^{(1)}]_{\alpha\beta ij}$	$\frac{1}{2}[y_1^L]_{i\alpha}^* [y_1^R]_{j\beta}$	$-\frac{1}{2}[y_2^R]_{i\beta} [y_2^L]_{j\alpha}^*$	–
$[\mathcal{C}_{lequ}^{(3)}]_{\alpha\beta ij}$	$-\frac{1}{8}[y_1^L]_{i\alpha}^* [y_1^R]_{j\beta}$	$-\frac{1}{8}[y_2^R]_{i\beta} [y_2^L]_{j\alpha}^*$	–
$[\mathcal{C}_{eu}]_{\alpha\beta ij}$	$\frac{1}{2}[y_1^R]_{j\beta} [y_1^R]_{i\alpha}^*$	–	–
$[\mathcal{C}_{ed}]_{\alpha\beta ij}$	–	–	$-[x_1^R]_{i\beta} [x_1^R]_{j\alpha}^*$
$[\mathcal{C}_{\ell u}]_{\alpha\beta ij}$	–	$-\frac{1}{2}[y_2^L]_{i\beta} [y_2^L]_{j\alpha}^*$	–
$[\mathcal{C}_{qe}]_{ij\alpha\beta}$	–	$-\frac{1}{2}[y_2^R]_{i\beta} [y_2^R]_{j\alpha}^*$	–
$[\mathcal{C}_{lq}^{(1)}]_{\alpha\beta ij}$	$\frac{1}{4}[y_1^L]_{i\alpha}^* [y_1^L]_{j\beta}$	–	$-\frac{1}{2}[x_1^L]_{i\beta} [x_1^L]_{j\alpha}^*$
$[\mathcal{C}_{lq}^{(3)}]_{\alpha\beta ij}$	$-\frac{1}{4}[y_1^L]_{i\alpha}^* [y_1^L]_{j\beta}$	–	$-\frac{1}{2}[x_1^L]_{i\beta} [x_1^L]_{j\alpha}^*$



U_1 LQ-inspired EFT: HighPT example

$$[C_{lq}^{(1)}]_{3323} = [C_{lq}^{(3)}]_{3323}, \quad [C_{lq}^{(1)}]_{3333} = [C_{lq}^{(3)}]_{3333}$$

Computing the LHC likelihood for $pp \rightarrow \tau\tau, \tau\nu$:

```
ln(*)=  $\chi^2_{\tau\tau}$  = Plus @@ ChiSquareLHC["di-tau-ATLAS", Coefficients -> {  
  WC["lq1", {3, 3, 3, 3}],  
  WC["lq3", {3, 3, 3, 3}],  
  WC["lq1", {3, 3, 2, 3}],  
  WC["lq3", {3, 3, 2, 3}]  
}];
```

Computing observable for di-tau-ATLAS search: [arXiv:2002.12223](https://arxiv.org/abs/2002.12223)

```
PROCESS      : pp ->  $\tau^-\tau^+$   
EXPERIMENT   : ATLAS  
ARXIV        : 2002.12223  
SOURCE       : hepdata  
OBSERVABLE   :  $m_{\tau}^{\text{tot}}$   
BINNING  $m_{\tau}^{\text{tot}}$  [GeV] : {150, 200, 250, 300, 350, 400, 450, 500, 600, 700, 800, 900, 1000, 1150, 1500}  
EVENTS OBSERVED : {1167., 1568., 1409., 1455., 1292., 650., 377., 288., 92., 57., 27., 14., 11., 13.}  
LUMINOSITY [fb-1] : 139  
BINNING  $\sqrt{s}$  [GeV] : {150, 200, 250, 300, 350, 400, 450, 500, 600, 700, 800, 900, 1000, 1150, 1500}  
BINNING  $p_T$  [GeV] : {0,  $\infty$ }
```

```
ln(*)=  $\chi^2_{\tau\nu}$  = Plus @@ ChiSquareLHC["mono-tau-ATLAS", Coefficients -> {  
  WC["lq1", {3, 3, 3, 3}],  
  WC["lq3", {3, 3, 3, 3}],  
  WC["lq1", {3, 3, 2, 3}],  
  WC["lq3", {3, 3, 2, 3}]  
}];
```


U_1 LQ-inspired EFT: HighPT example

$$[C_{lq}^{(1)}]_{3323} = [C_{lq}^{(3)}]_{3323}, \quad [C_{lq}^{(1)}]_{3333} = [C_{lq}^{(3)}]_{3333}$$

Flavour + EW likelihood:

```
ChiSquareFlavor[
  Observables → FlavorObservables["b->c,semileptonic"],
  Coefficients → {
    WC["lq1", {3, 3, 3, 3}],
    WC["lq3", {3, 3, 3, 3}],
    WC["lq1", {3, 3, 2, 3}],
    WC["lq3", {3, 3, 2, 3}]
  }
]
ChiSquareEW[Coefficients → {
  WC["lq1", {3, 3, 3, 3}],
  WC["lq3", {3, 3, 3, 3}],
  WC["lq1", {3, 3, 2, 3}],
  WC["lq3", {3, 3, 2, 3}]
}
]
```

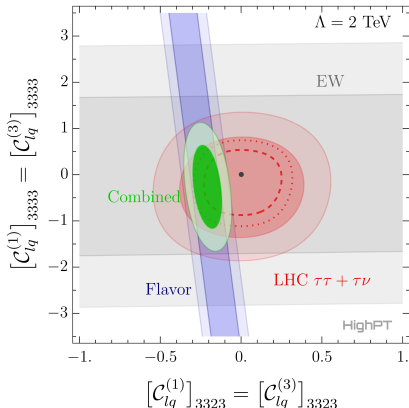
Preliminary

HighPT takes care of RGE in SMEFT,
match it to LEFT,
and evolve the LEFT coefficients
to the low-energy scale

Results: U_1 - LH couplings only

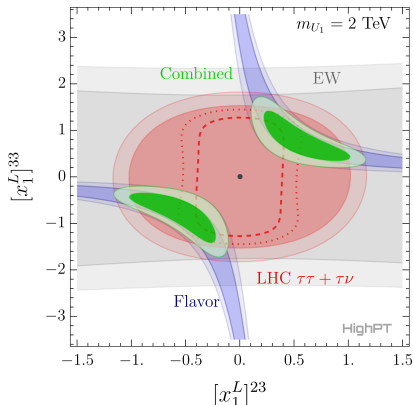
$$\mathcal{L}_{U_1} = [x_1^L]_{i\alpha} \bar{q}_i \Psi_1 l_\alpha + [x_1^R]_{i\alpha} \bar{d}_i \Psi_1 e_\alpha + [\bar{x}_1^R]_{i\alpha} \bar{u}_i \Psi_1 N_\alpha + \text{h.c.}$$

EFT



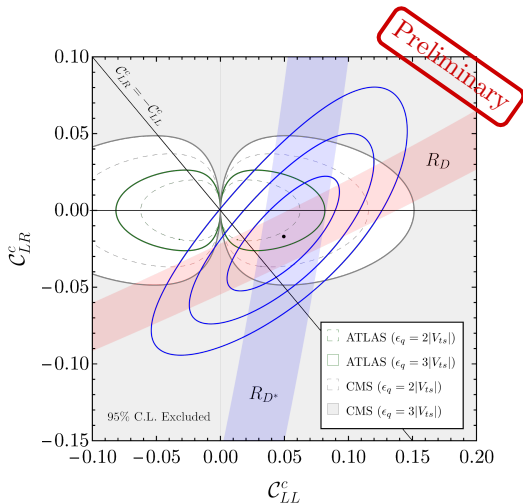
LQ model

$$U_1 \sim (\mathbf{3}, \mathbf{1}, 2/3)$$



[LA, Faroughy, Jaffredo, Sumensari, Wilsch 2207.10714]

Results: U_1 - Including RH currents



$$\mathcal{L}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}}V_{cb} \left[(1 + C_{LL}^c)\mathcal{O}_{LL}^c - 2C_{LR}^c\mathcal{O}_{LL}^c \right]$$

$$\mathcal{O}_{LL}^c = (\bar{c}_L\gamma_\mu b_L)(\bar{\tau}_L\gamma^\mu\nu_L)$$

$$\mathcal{O}_{LR}^c = (\bar{c}_L b_R)(\bar{\tau}_R\nu_L)$$

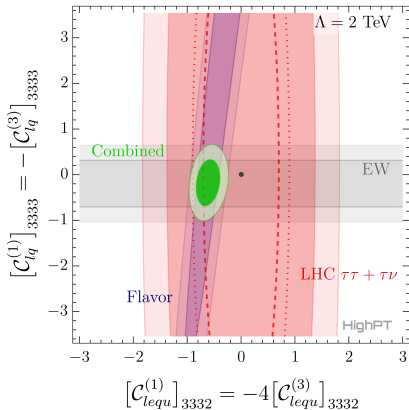
[Aebischer, Isidori, Pesut, Stefaneck, Wilsch, WIP]



Results: S_1

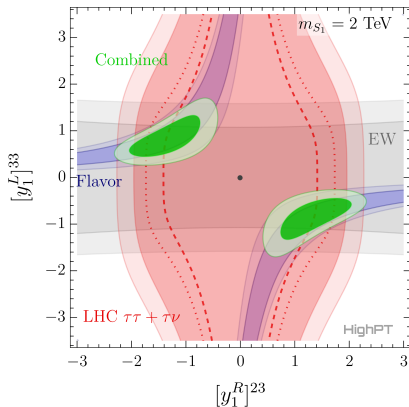
$$\mathcal{L}_{S_1} = [y_1^L]_{i\alpha} S_1 \bar{q}_i^c \ell_\alpha + [y_1^R]_{i\alpha} S_1 \bar{u}_i^c e_\alpha + [\bar{y}_1^R]_{i\alpha} S_1 \bar{d}_i^c N_\alpha + \text{h.c.}$$

EFT



LQ model

$$S_1 \sim (\mathbf{3}, 1, 1/3)$$

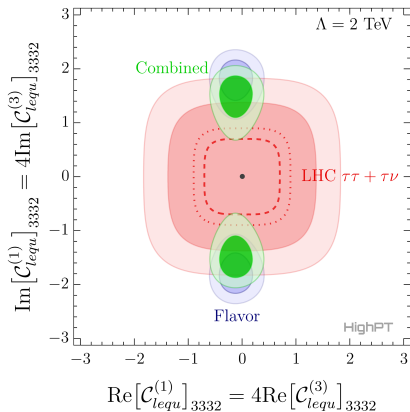


[LA, Faroughy, Jaffredo, Sumensari, Wilsch 2207.10714]

Results: R_2

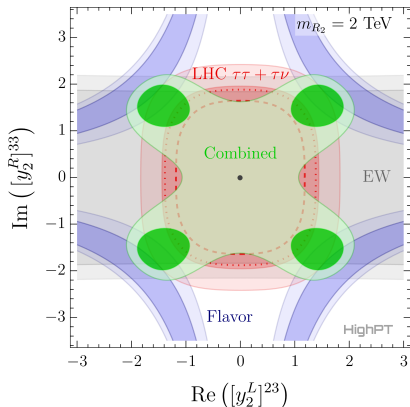
$$\mathcal{L}_{R_2} = -[y_2^L]_{i\alpha} \bar{u}_i R_2 \epsilon l_\alpha + [y_2^R]_{i\alpha} \bar{q}_i e_\alpha R_2 + \text{h.c.}$$

EFT



LQ model

$$R_2 \sim (\mathbf{3}, \mathbf{2}, 7/6)$$



[LA, Farouhy, Jaffredo, Sumensari, Wilsch 2207.10714]

Summary and outlook

- Drell-Yan tails can provide a useful complementary probe of NP to low-energy observables
- Also EW precision tests can play a role through RGE effects
- HighPT provides an easy-to-use framework to obtain the high- p_T likelihood from the LHC with the latest Run-2 data
- Can constrain both SMEFT and LQ scenarios ($m_{LQ} = 1, 2, 3$ TeV, more coming soon)
- low-energy + EW observables will be included in a future release
→ get likelihood as an analytic function of the Wilson Coefficients/LQ couplings
- Stay tuned!

Thank you!



Backup



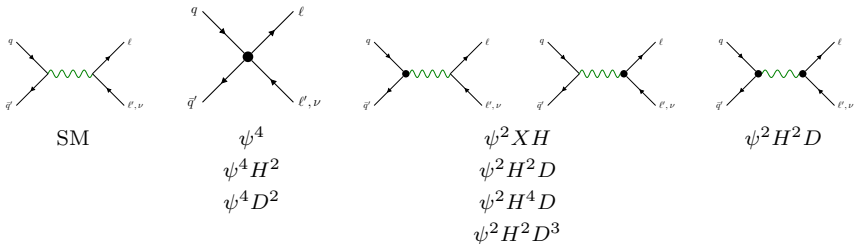
$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_{d,k} \frac{\mathcal{C}_k^{(d)}}{\Lambda^{d-4}} \mathcal{O}_k^{(d)} + \sum_{d,k} \left[\frac{\tilde{\mathcal{C}}_k^{(d)}}{\Lambda^{d-4}} \tilde{\mathcal{O}}_k^{(d)} + \text{h.c.} \right]$$

Cross-section up to $\mathcal{O}(\Lambda^{-4})$:

$$\hat{\sigma} \sim \int [d\Phi] \left\{ |\mathcal{A}_{\text{SM}}|^2 + \frac{v^2}{\Lambda^2} \sum_i 2 \text{Re}(\mathcal{A}_i^{(6)} \mathcal{A}_{\text{SM}}^*) \right. \\ \left. + \frac{v^4}{\Lambda^4} \left[\sum_{ij} 2 \text{Re}(\mathcal{A}_i^{(6)} \mathcal{A}_j^{(6)*}) + \sum_i 2 \text{Re}(\mathcal{A}_i^{(8)} \mathcal{A}_{\text{SM}}^*) \right] + \dots \right\}$$

- Include $|\mathcal{A}^{(6)}|^2$ contributions: LFV
- Only $d = 8$ terms interfering with the SM are relevant
- Basis:
 - $d = 6$: Warsaw [1008.4884]
 - $d = 8$: Murphy [2005.00059]

Relevant Feynman diagrams:



Parameter counting and energy scaling:

Dimension	$d = 6$			$d = 8$				
Operator classes	ψ^4	$\psi^2 H^2 D$	$\psi^2 XH$	$\psi^4 D^2$	$\psi^4 H^2$	$\psi^2 H^4 D$	$\psi^2 H^2 D^3$	
Amplitude scaling	E^2/Λ^2	v^2/Λ^2	vE/Λ^2	E^4/Λ^4	$v^2 E^2/\Lambda^4$	v^4/Λ^4	$v^2 E^2/\Lambda^4$	
Parameters	# $\mathbb{R}e$	456	45	48	168	171	44	52
	# $\mathbb{I}m$	399	25	48	54	63	12	12

SMEFT: Schematic form-factor matching

Vector form factor:

$$\mathcal{F}_V = \mathcal{F}_{V(0,0)} + \mathcal{F}_{V(1,0)} \frac{\hat{s}}{v^2} + \mathcal{F}_{V(0,1)} \frac{\hat{t}}{v^2} + \sum_a \frac{v^2 [\mathcal{S}_{(a,SM)} + \delta\mathcal{S}_{(a)}]}{\hat{s} - m_a^2 + im_a\Gamma_a}$$

Matching:

$$\mathcal{F}_{V(0,0)} = \frac{v^2}{\Lambda^2} \mathcal{C}_{\psi^4}^{(6)} + \frac{v^4}{\Lambda^4} \mathcal{C}_{\psi^4 H^2}^{(8)} + \frac{v^2 m_a^2}{\Lambda^4} \mathcal{C}_{\psi^2 H^2 D^3}^{(8)} + \dots,$$

$$\mathcal{F}_{V(1,0)} = \frac{v^4}{\Lambda^4} \mathcal{C}_{\psi^4 D^2}^{(8)} + \dots,$$

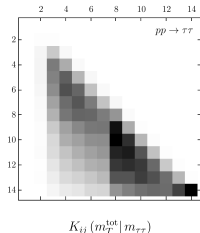
$$\mathcal{F}_{V(0,1)} = \frac{v^4}{\Lambda^4} \mathcal{C}_{\psi^4 D^2}^{(8)} + \dots,$$

$$\delta\mathcal{S}_{(a)} = \frac{m_a^2}{\Lambda^2} \mathcal{C}_{\psi^2 H^2 D}^{(6)} + \frac{v^2 m_a^2}{\Lambda^4} \left(\left[\mathcal{C}_{\psi^2 H^2 D}^{(6)} \right]^2 + \mathcal{C}_{\psi^2 H^4 D}^{(8)} \right) + \frac{m_a^4}{\Lambda^4} \mathcal{C}_{\psi^2 H^2 D^3}^{(8)} + \dots,$$

$$\frac{s}{s-\Omega} = 1 + \frac{\Omega}{s-\Omega}$$

Cross section \rightarrow event yield

- $\frac{d\sigma}{dx}$ computed analytically ($x = m_{\ell\ell}, p_T$)
- Need to compare with measured quantity
 $\frac{d\sigma}{dx_{\text{obs}}}$ ($x_{\text{obs}} = m_{\ell\ell}, m_T^{\text{tot}}, m_T, \dots$)



- For binned distributions, introduce Kernel matrix K

$$\sigma_q(x_{\text{obs}}) = \sum_{p=1}^M K_{pq} \sigma_p(x)$$

- K extracted with MC simulations using Madgraph + Pythia + Delphes
- One matrix K for any combination of interfering form-factors

The $U(2)$ paradigm

SM Yukawas respect approximate $U(2)^5$ symmetry:

[Barbieri et al. 1105.3396]

$$Y \simeq y_3 \left(\begin{array}{cc|c} 0 & 0 & 0 \\ 0 & 0 & 0 \\ \hline 0 & 0 & 1 \end{array} \right) \quad U(2)^5 = U(2)_q \times U(2)_\ell \times U(2)_u \times U(2)_d \times U(2)_e$$

Minimal breaking:

$$Y = y_3 \left(\begin{array}{c|c} \Delta & V \\ \hline 0 & 1 \end{array} \right) \quad |V_q| = \epsilon_q = \mathcal{O}(y_t V_{ts}) \quad |\Delta| \sim y_{c,s,\mu}$$

Does TeV-scale NP follow the same pattern?

- NP coupled mainly to 3rd generation
- Couplings to 2nd generation suppressed by powers of $\epsilon_{q,l} \sim 0.1$

[Barbieri et al. 1512.01560]

Example: LFU tests in charged current B decays

Low-energy effective description:

$$\mathcal{L}_{\text{eff}}^{b \rightarrow c \tau \nu} = -2\sqrt{2}G_F V_{cb} \left[(1 + C_{V_L})(\bar{c}_L \gamma_\mu b_L)(\bar{\tau}_L \gamma_\mu \nu_L) + C_{V_R}(\bar{c}_R \gamma_\mu b_R)(\bar{\tau}_L \gamma_\mu \nu_L) \right. \\ \left. + C_{S_L}(\bar{c}_R b_L)(\bar{\tau}_R \nu_L) + C_{S_R}(\bar{c}_L b_R)(\bar{\tau}_R \nu_L) + C_T(\bar{c}_R \sigma_{\mu\nu} b_L)(\bar{\tau}_R \sigma^{\mu\nu} \nu_L) \right] + \text{h.c.},$$

SMEFT matching:

$$C_{V_L} = -\frac{v^2}{\Lambda^2} \sum_i \frac{V_{2i}}{V_{23}} \left([C_{lq}^{(3)}]_{33i3} + [C_{Hq}^{(3)}]_{33} - \delta_{i3} [C_{Hl}^{(3)}]_{33} \right), \quad [\mathcal{O}_{lq}^{(1)}]_{ij\alpha\beta} = (\bar{l}_\alpha \gamma_\mu l_\beta)(\bar{q}_i \gamma^\mu q_j)$$

$$C_{V_R} = \frac{v^2}{2\Lambda^2} \frac{1}{V_{23}} [C_{Hud}^{(3)}]_{23}, \quad [\mathcal{O}_{lq}^{(3)}]_{ij\alpha\beta} = (\bar{l}_\alpha \gamma_\mu \sigma^I l_\beta)(\bar{q}_i \gamma^\mu \sigma^I q_j)$$

$$C_{S_L} = -\frac{v^2}{2\Lambda^2} \frac{1}{V_{23}} [C_{lequ}^{(1)}]_{3332}^*, \quad [\mathcal{O}_{lequ}^{(1)}]_{ij\alpha\beta} = (\bar{l}_\alpha e_\beta) \epsilon(\bar{q}_i u_j)$$

$$C_{S_R} = -\frac{v^2}{2\Lambda^2} \sum_{i=1}^3 \frac{V_{2i}^*}{V_{23}} [C_{ledq}]_{333i}^*, \quad [\mathcal{O}_{lequ}^{(3)}]_{ij\alpha\beta} = (\bar{l}_\alpha \sigma^{\mu\nu} e_\beta) \epsilon(\bar{q}_i \sigma_{\mu\nu} u_j)$$

$$C_T = -\frac{v^2}{2\Lambda^2} \frac{1}{V_{23}} [C_{lequ}^{(3)}]_{3332}^*, \quad [\mathcal{O}_{ledq}]_{ij\alpha\beta} = (\bar{l}_\alpha e_\beta)(\bar{d}_i q_j)$$

$$[\mathcal{O}_{Hq}^{(3)}]_{ij} = (H^\dagger i D_\mu \sigma^I H)(\bar{q}_i \gamma^\mu \sigma^I q_j)$$

$$[\mathcal{O}_{Hl}^{(3)}]_{\alpha\beta} = (H^\dagger i D_\mu \sigma^I H)(\bar{l}_\alpha \gamma^\mu \sigma^I l_\beta)$$



SMEFT operators

$d = 6$	ψ^4	$pp \rightarrow \ell\ell$	$pp \rightarrow \ell\nu$
$\mathcal{O}_{lq}^{(1)}$	$(\bar{l}_\alpha \gamma^\mu l_\beta)(\bar{q}_i \gamma_\mu q_j)$	✓	—
$\mathcal{O}_{lq}^{(3)}$	$(\bar{l}_\alpha \gamma^\mu \tau^I l_\beta)(\bar{q}_i \gamma_\mu \tau^I q_j)$	✓	✓
\mathcal{O}_{lu}	$(l_\alpha \gamma^\mu l_\beta)(\bar{u}_i \gamma_\mu u_j)$	✓	—
\mathcal{O}_{ld}	$(\bar{l}_\alpha \gamma^\mu l_\beta)(\bar{d}_i \gamma_\mu d_j)$	✓	—
\mathcal{O}_{eq}	$(\bar{e}_\alpha \gamma^\mu e_\beta)(\bar{q}_i \gamma_\mu q_j)$	✓	—
\mathcal{O}_{eu}	$(\bar{e}_\alpha \gamma^\mu e_\beta)(\bar{u}_i \gamma_\mu u_j)$	✓	—
\mathcal{O}_{ed}	$(\bar{e}_\alpha \gamma^\mu e_\beta)(\bar{d}_i \gamma_\mu d_j)$	✓	—
$\mathcal{O}_{ledq} + \text{h.c.}$	$(l_\alpha e_\beta)(d_i q_j)$	✓	✓
$\mathcal{O}_{lequ}^{(1)} + \text{h.c.}$	$(\bar{l}_\alpha e_\beta)\varepsilon(\bar{q}_i u_j)$	✓	✓
$\mathcal{O}_{lequ}^{(3)} + \text{h.c.}$	$(\bar{l}_\alpha \sigma^{\mu\nu} e_\beta)\varepsilon(\bar{q}_i \sigma_{\mu\nu} u_j)$	✓	✓

SMEFT operators

$d = 6$	$\psi^2 H^2 D$	$pp \rightarrow \ell\ell$	$pp \rightarrow \ell\nu$
$\mathcal{O}_{Hl}^{(1)}$	$(\bar{l}_\alpha \gamma^\mu l_\beta)(H^\dagger i \overleftrightarrow{D}_\mu H)$	✓	–
$\mathcal{O}_{Hl}^{(3)}$	$(\bar{l}_\alpha \gamma^\mu \tau^I l_\beta)(H^\dagger i \overleftrightarrow{D}_\mu^I H)$	✓	✓
$\mathcal{O}_{Hq}^{(1)}$	$(\bar{q}_i \gamma^\mu q_j)(H^\dagger i \overleftrightarrow{D}_\mu H)$	✓	–
$\mathcal{O}_{Hq}^{(3)}$	$(\bar{q}_i \gamma^\mu \tau^I q_j)(H^\dagger i \overleftrightarrow{D}_\mu^I H)$	✓	✓
\mathcal{O}_{He}	$(\bar{e}_\alpha \gamma^\mu e_\beta)(H^\dagger i \overleftrightarrow{D}_\mu H)$	✓	–
\mathcal{O}_{Hu}	$(\bar{u}_i \gamma^\mu u_j)(H^\dagger i \overleftrightarrow{D}_\mu H)$	✓	–
\mathcal{O}_{Hd}	$(\bar{d}_i \gamma^\mu d_j)(H^\dagger i \overleftrightarrow{D}_\mu H)$	✓	–
$\mathcal{O}_{Hud} + \text{h.c.}$	$(\bar{u}_i \gamma^\mu d_j)(\tilde{H}^\dagger i D_\nu H)$	–	✓

SMEFT operators

$d = 6$	$\psi^2 XH + \text{h.c.}$	$pp \rightarrow \ell\ell$	$pp \rightarrow \ell\nu$
\mathcal{O}_{eW}	$(\bar{l}_\alpha \sigma^{\mu\nu} e_\beta) \tau^I H W_{\mu\nu}^I$	✓	✓
\mathcal{O}_{eB}	$(\bar{l}_\alpha \sigma^{\mu\nu} e_\beta) H B_{\mu\nu}$	✓	—
\mathcal{O}_{uW}	$(\bar{q}_i \sigma^{\mu\nu} u_j) \tau^I \tilde{H} W_{\mu\nu}^I$	✓	✓
\mathcal{O}_{uB}	$(\bar{q}_i \sigma^{\mu\nu} u_j) \tilde{H} B_{\mu\nu}$	✓	—
\mathcal{O}_{dW}	$(\bar{q}_i \sigma^{\mu\nu} d_j) \tau^I H W_{\mu\nu}^I$	✓	✓
\mathcal{O}_{dB}	$(\bar{q}_i \sigma^{\mu\nu} d_j) H B_{\mu\nu}$	✓	—



SMEFT operators

$d = 8$	$\psi^4 H^2$	$pp \rightarrow \ell\ell$	$pp \rightarrow \ell\nu$
$\mathcal{O}_{l^2 q^2 H^2}^{(1)}$	$(\bar{l}_\alpha \gamma^\mu l_\beta)(\bar{q}_i \gamma_\mu q_j)(H^\dagger H)$	✓	—
$\mathcal{O}_{l^2 q^2 H^2}^{(2)}$	$(\bar{l}_\alpha \gamma^\mu \tau^I l_\beta)(\bar{q}_i \gamma_\mu q_j)(H^\dagger \tau^I H)$	✓	—
$\mathcal{O}_{l^2 q^2 H^2}^{(3)}$	$(\bar{l}_\alpha \gamma^\mu \tau^I l_\beta)(\bar{q}_i \gamma_\mu \tau^I q_j)(H^\dagger H)$	✓	✓
$\mathcal{O}_{l^2 q^2 H^2}^{(4)}$	$(\bar{l}_\alpha \gamma^\mu l_\beta)(\bar{q}_i \gamma_\mu \tau^I q_j)(H^\dagger \tau^I H)$	✓	—
$\mathcal{O}_{l^2 q^2 H^2}^{(5)}$	$\epsilon^{IJK} (\bar{l}_\alpha \gamma^\mu \tau^I l_\beta)(\bar{q}_i \gamma_\mu \tau^J q_j)(H^\dagger \tau^K H)$	—	✓
$\mathcal{O}_{l^2 u^2 H^2}^{(1)}$	$(\bar{l}_\alpha \gamma^\mu l_\beta)(\bar{u}_i \gamma_\mu u_j)(H^\dagger H)$	✓	—
$\mathcal{O}_{l^2 u^2 H^2}^{(2)}$	$(\bar{l}_\alpha \gamma^\mu \tau^I l_\beta)(\bar{u}_i \gamma_\mu u_j)(H^\dagger \tau^I H)$	✓	—
$\mathcal{O}_{l^2 d^2 H^2}^{(1)}$	$(\bar{l}_\alpha \gamma^\mu l_\beta)(\bar{d}_i \gamma_\mu d_j)(H^\dagger H)$	✓	—
$\mathcal{O}_{l^2 d^2 H^2}^{(2)}$	$(\bar{l}_\alpha \gamma^\mu \tau^I l_\beta)(\bar{d}_i \gamma_\mu d_j)(H^\dagger \tau^I H)$	✓	—
$\mathcal{O}_{e^2 q^2 H^2}^{(1)}$	$(\bar{e}_\alpha \gamma_\mu e_\beta)(\bar{q}_i \gamma^\mu q_j)(H^\dagger H)$	✓	—
$\mathcal{O}_{e^2 q^2 H^2}^{(2)}$	$(\bar{e}_\alpha \gamma_\mu e_\beta)(\bar{q}_i \gamma^\mu \tau^I q_j)(H^\dagger \tau^I H)$	✓	—
$\mathcal{O}_{e^2 u^2 H^2}$	$(\bar{e}_\alpha \gamma^\mu e_\beta)(\bar{u}_i \gamma_\mu u_j)(H^\dagger H)$	✓	—
$\mathcal{O}_{e^2 d^2 H^2}$	$(\bar{e}_\alpha \gamma^\mu e_\beta)(\bar{d}_i \gamma_\mu d_j)(H^\dagger H)$	✓	—

SMEFT operators

$d = 8$	$\psi^4 D^2$	$pp \rightarrow \ell\ell$	$pp \rightarrow \ell\nu$
$\mathcal{O}_{l^2 q^2 D^2}^{(1)}$	$D^\nu (\bar{l}_\alpha \gamma^\mu l_\beta) D_\nu (\bar{q}_i \gamma_\mu q_j)$	✓	—
$\mathcal{O}_{l^2 q^2 D^2}^{(2)}$	$(\bar{l}_\alpha \gamma^\mu \overleftrightarrow{D}^\nu l_\beta) (\bar{q}_i \gamma_\mu \overleftrightarrow{D}_\nu q_j)$	✓	—
$\mathcal{O}_{l^2 q^2 D^2}^{(3)}$	$D^\nu (\bar{l}_\alpha \gamma^\mu \tau^I l_\beta) D_\nu (\bar{q}_i \gamma_\mu \tau^I q_j)$	✓	✓
$\mathcal{O}_{l^2 q^2 D^2}^{(4)}$	$(\bar{l}_\alpha \gamma^\mu \overleftrightarrow{D}^I l_\beta) (\bar{q}_i \gamma_\mu \overleftrightarrow{D}_\nu^I q_j)$	✓	✓
$\mathcal{O}_{l^2 u^2 D^2}^{(1)}$	$D^\nu (\bar{l}_\alpha \gamma^\mu l_\beta) D_\nu (\bar{u}_i \gamma_\mu u_j)$	✓	—
$\mathcal{O}_{l^2 u^2 D^2}^{(2)}$	$(\bar{l}_\alpha \gamma^\mu \overleftrightarrow{D}^\nu l_\beta) (\bar{u}_i \gamma_\mu \overleftrightarrow{D}_\nu u_j)$	✓	—
$\mathcal{O}_{l^2 d^2 D^2}^{(1)}$	$D^\nu (\bar{l}_\alpha \gamma^\mu l_\beta) D_\nu (\bar{d}_i \gamma_\mu d_j)$	✓	—
$\mathcal{O}_{l^2 d^2 D^2}^{(2)}$	$(\bar{l}_\alpha \gamma^\mu \overleftrightarrow{D}^\nu l_\beta) (\bar{d}_i \gamma_\mu \overleftrightarrow{D}_\nu d_j)$	✓	—
$\mathcal{O}_{e^2 q^2 D^2}^{(1)}$	$D_\nu (\bar{e}_\alpha \gamma_\mu e_\beta) D^\nu (\bar{q}_i \gamma^\mu q_j)$	✓	—
$\mathcal{O}_{e^2 q^2 D^2}^{(2)}$	$(\bar{e}_\alpha \gamma_\mu \overleftrightarrow{D}_\nu e_\beta) (\bar{q}_i \gamma^\mu \overleftrightarrow{D}^\nu q_j)$	✓	—
$\mathcal{O}_{e^2 u^2 D^2}^{(1)}$	$D^\nu (\bar{e}_\alpha \gamma^\mu e_\beta) D_\nu (\bar{u}_i \gamma_\mu u_j)$	✓	—
$\mathcal{O}_{e^2 u^2 D^2}^{(2)}$	$(\bar{e}_\alpha \gamma^\mu \overleftrightarrow{D}^\nu e_\beta) (\bar{u}_i \gamma_\mu \overleftrightarrow{D}_\nu u_j)$	✓	—
$\mathcal{O}_{e^2 d^2 D^2}^{(1)}$	$D^\nu (\bar{e}_\alpha \gamma^\mu e_\beta) D_\nu (\bar{d}_i \gamma_\mu d_j)$	✓	—
$\mathcal{O}_{e^2 d^2 D^2}^{(2)}$	$(\bar{e}_\alpha \gamma^\mu \overleftrightarrow{D}^\nu e_\beta) (\bar{d}_i \gamma_\mu \overleftrightarrow{D}_\nu d_j)$	✓	—

SMEFT operators

$d = 8$	$\psi^2 H^4 D$	$pp \rightarrow \ell\ell$
$\mathcal{O}_{l^2 H^4 D}^{(1)}$	$i(\bar{l}_\alpha \gamma^\mu l_\beta)(H^\dagger \overleftrightarrow{D}_\mu H)(H^\dagger H)$	✓
$\mathcal{O}_{l^2 H^4 D}^{(2)}$	$i(\bar{l}_\alpha \gamma^\mu \tau^I l_\beta)[(H^\dagger \overleftrightarrow{D}_\mu^I H)(H^\dagger H) + (H^\dagger \overleftrightarrow{D}_\mu H)(H^\dagger \tau^I H)]$	✓
$\mathcal{O}_{l^2 H^4 D}^{(3)}$	$\epsilon^{IJK}(\bar{l}_\alpha \gamma^\mu \tau^I l_\beta)(H^\dagger \overleftrightarrow{D}_\mu^J H)(H^\dagger \tau^K H)$	–
$\mathcal{O}_{l^2 H^4 D}^{(4)}$	$\epsilon^{IJK}(\bar{l}_\alpha \gamma^\mu \tau^I l_\beta)(H^\dagger \tau^J H)(D_\mu H)^\dagger \tau^K H$	–
$\mathcal{O}_{q^2 H^4 D}^{(1)}$	$i(\bar{q}_i \gamma^\mu q_j)(H^\dagger \overleftrightarrow{D}_\mu H)(H^\dagger H)$	✓
$\mathcal{O}_{q^2 H^4 D}^{(2)}$	$i(\bar{q}_i \gamma^\mu \tau^I q_j)[(H^\dagger \overleftrightarrow{D}_\mu^I H)(H^\dagger H) + (H^\dagger \overleftrightarrow{D}_\mu H)(H^\dagger \tau^I H)]$	✓
$\mathcal{O}_{q^2 H^4 D}^{(3)}$	$i\epsilon^{IJK}(\bar{q}_i \gamma^\mu \tau^I q_j)(H^\dagger \overleftrightarrow{D}_\mu^J H)(H^\dagger \tau^K H)$	–
$\mathcal{O}_{q^2 H^4 D}^{(4)}$	$\epsilon^{IJK}(\bar{q}_i \gamma^\mu \tau^I q_j)(H^\dagger \tau^J H)(D_\mu H)^\dagger \tau^K H$	–
$\mathcal{O}_{e^2 H^4 D}$	$i(\bar{e}_\alpha \gamma^\mu e_\beta)(H^\dagger \overleftrightarrow{D}_\mu H)(H^\dagger H)$	✓
$\mathcal{O}_{u^2 H^4 D}$	$i(\bar{u}_i \gamma^\mu u_j)(H^\dagger \overleftrightarrow{D}_\mu H)(H^\dagger H)$	✓
$\mathcal{O}_{d^2 H^4 D}$	$i(\bar{d}_i \gamma^\mu d_j)(H^\dagger \overleftrightarrow{D}_\mu H)(H^\dagger H)$	✓



SMEFT operators

$d = 8$	$\psi^2 H^2 D^3$	$pp \rightarrow \ell\ell$	$pp \rightarrow \ell\nu$
$\mathcal{O}_{l^2 H^2 D^3}^{(1)}$	$i(\bar{l}_\alpha \gamma^\mu D^\nu l_\beta) (D_{(\mu} D_{\nu)} H)^\dagger H$	✓	—
$\mathcal{O}_{l^2 H^2 D^3}^{(2)}$	$i(\bar{l}_\alpha \gamma^\mu D^\nu l_\beta) H^\dagger (D_{(\mu} D_{\nu)} H)$	✓	—
$\mathcal{O}_{l^2 H^2 D^3}^{(3)}$	$i(\bar{l}_\alpha \gamma^\mu \tau^I D^\nu l_\beta) (D_{(\mu} D_{\nu)} H)^\dagger \tau^I H$	✓	✓
$\mathcal{O}_{l^2 H^2 D^3}^{(4)}$	$i(\bar{l}_\alpha \gamma^\mu \tau^I D^\nu l_\beta) H^\dagger \tau^I (D_{(\mu} D_{\nu)} H)$	✓	✓
$\mathcal{O}_{e^2 H^2 D^3}^{(1)}$	$i(\bar{e}_\alpha \gamma^\mu D^\nu e_\beta) (D_{(\mu} D_{\nu)} H)^\dagger H$	✓	—
$\mathcal{O}_{e^2 H^2 D^3}^{(2)}$	$i(\bar{e}_\alpha \gamma^\mu D^\nu e_\beta) H^\dagger (D_{(\mu} D_{\nu)} H)$	✓	—
$\mathcal{O}_{q^2 H^2 D^3}^{(1)}$	$i(\bar{q}_i \gamma^\mu D^\nu q_j) (D_{(\mu} D_{\nu)} H)^\dagger H$	✓	—
$\mathcal{O}_{q^2 H^2 D^3}^{(2)}$	$i(\bar{q}_i \gamma^\mu D^\nu q_j) H^\dagger (D_{(\mu} D_{\nu)} H)$	✓	—
$\mathcal{O}_{q^2 H^2 D^3}^{(3)}$	$i(\bar{q}_i \gamma^\mu \tau^I D^\nu q_j) (D_{(\mu} D_{\nu)} H)^\dagger \tau^I H$	✓	✓
$\mathcal{O}_{q^2 H^2 D^3}^{(4)}$	$i(\bar{q}_i \gamma^\mu \tau^I D^\nu q_j) H^\dagger \tau^I (D_{(\mu} D_{\nu)} H)$	✓	✓
$\mathcal{O}_{u^2 H^2 D^3}^{(1)}$	$i(\bar{u}_i \gamma^\mu D^\nu u_j) (D_{(\mu} D_{\nu)} H)^\dagger H$	✓	—
$\mathcal{O}_{u^2 H^2 D^3}^{(2)}$	$i(\bar{u}_i \gamma^\mu D^\nu u_j) H^\dagger (D_{(\mu} D_{\nu)} H)$	✓	—
$\mathcal{O}_{d^2 H^2 D^3}^{(1)}$	$i(\bar{d}_i \gamma^\mu D^\nu d_j) (D_{(\mu} D_{\nu)} H)^\dagger H$	✓	—
$\mathcal{O}_{d^2 H^2 D^3}^{(2)}$	$i(\bar{d}_i \gamma^\mu D^\nu d_j) H^\dagger (D_{(\mu} D_{\nu)} H)$	✓	—