

Mysteries under a *strong* lens

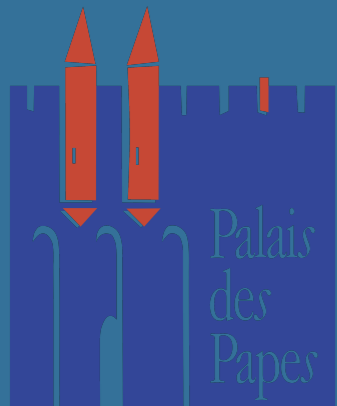
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4th May 2023

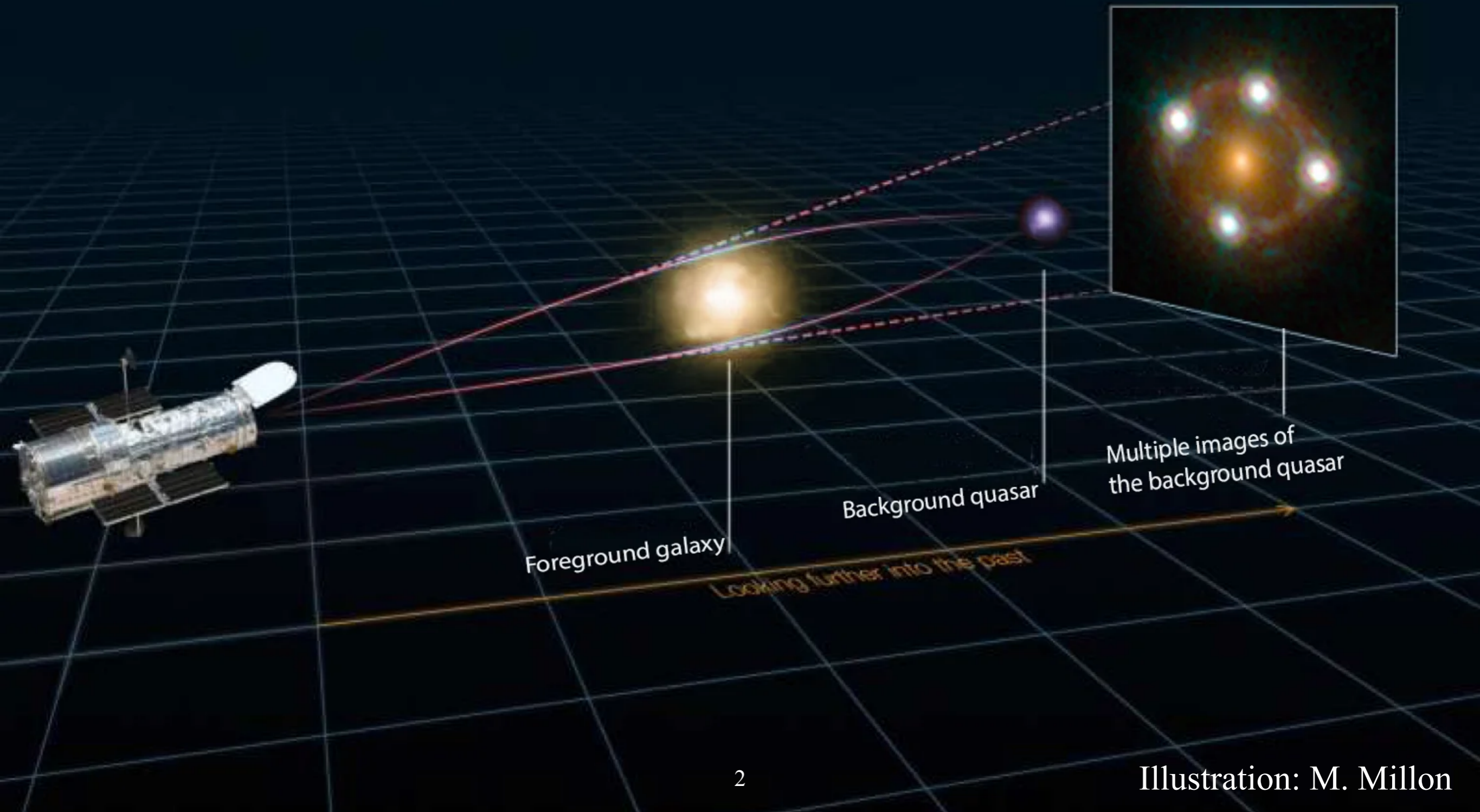
Based on

C.D., M. Millon, T. Baker, [arXiv:2301.05574]



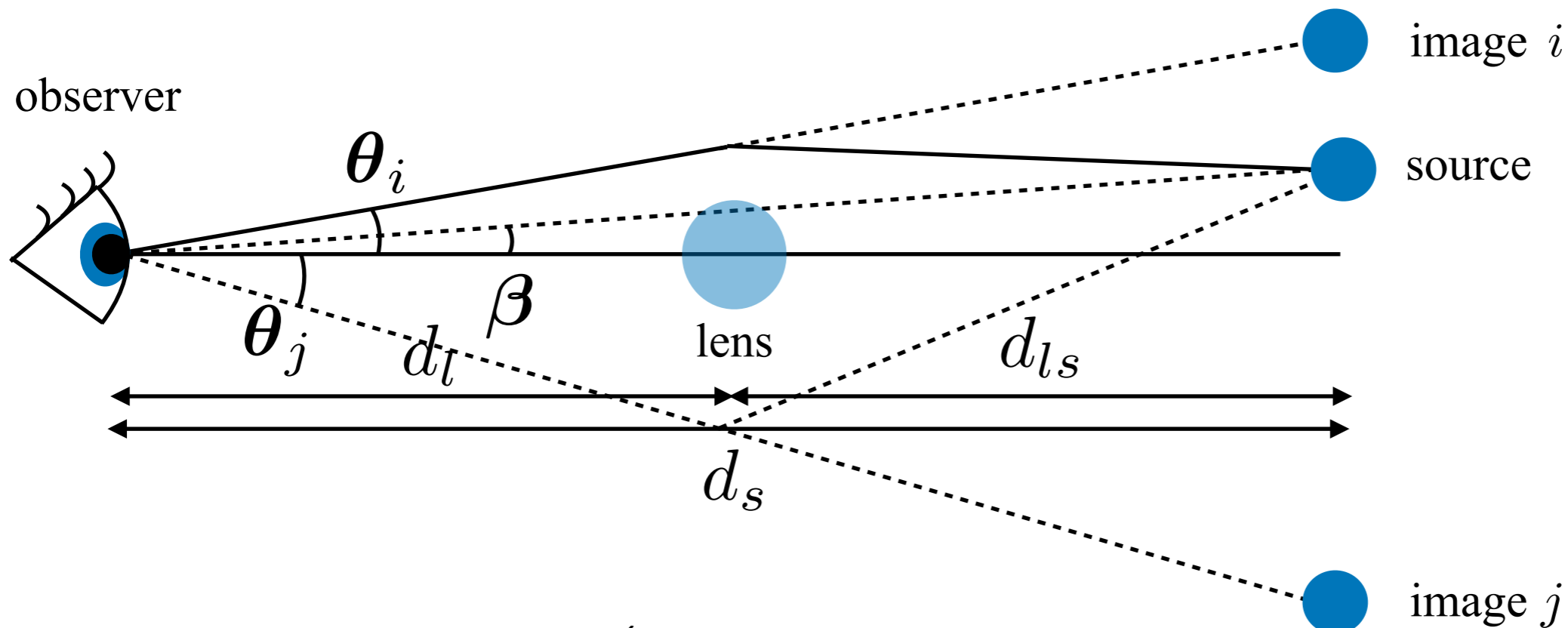
Time delay cosmography

H0LiCOW/TDCOSMO collab.
COSMOGRAIL
C.D., M. Millon, T. Baker, 2023



Time delay cosmography

K. Wong et al., 2019
H0LiCOW/TDCOSMO



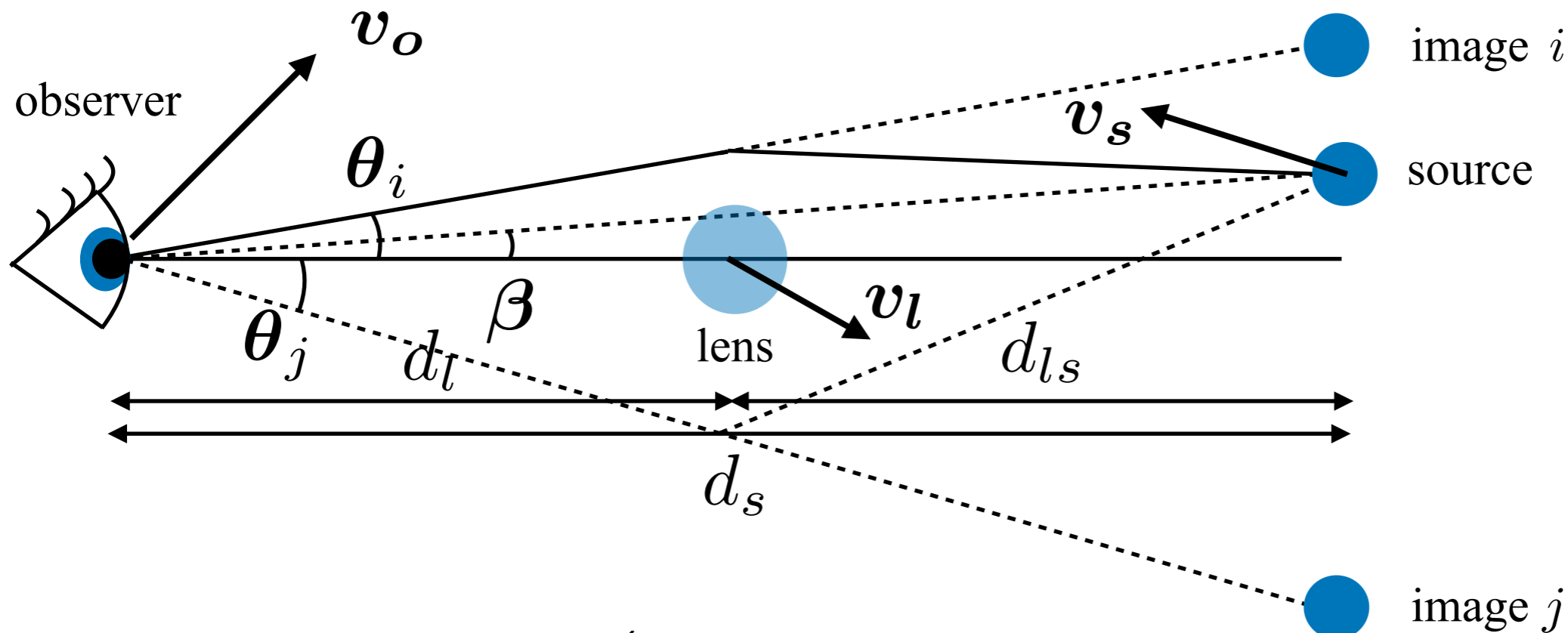
$$c\Delta t_{ij} = (1 + z_l) \frac{d_l d_s}{d_{ls}} \left(\frac{(\theta_i - \beta)^2}{2} - \frac{(\theta_j - \beta)^2}{2} - \left[\Psi(\theta_i) - \Psi(\theta_j) \right] \right)$$

$$\propto H_0^{-1}$$

$$H_0 = 73.3_{-1.8}^{+1.7} \text{ km s}^{-1} \text{ Mpc}^{-1}$$

Time delay cosmography

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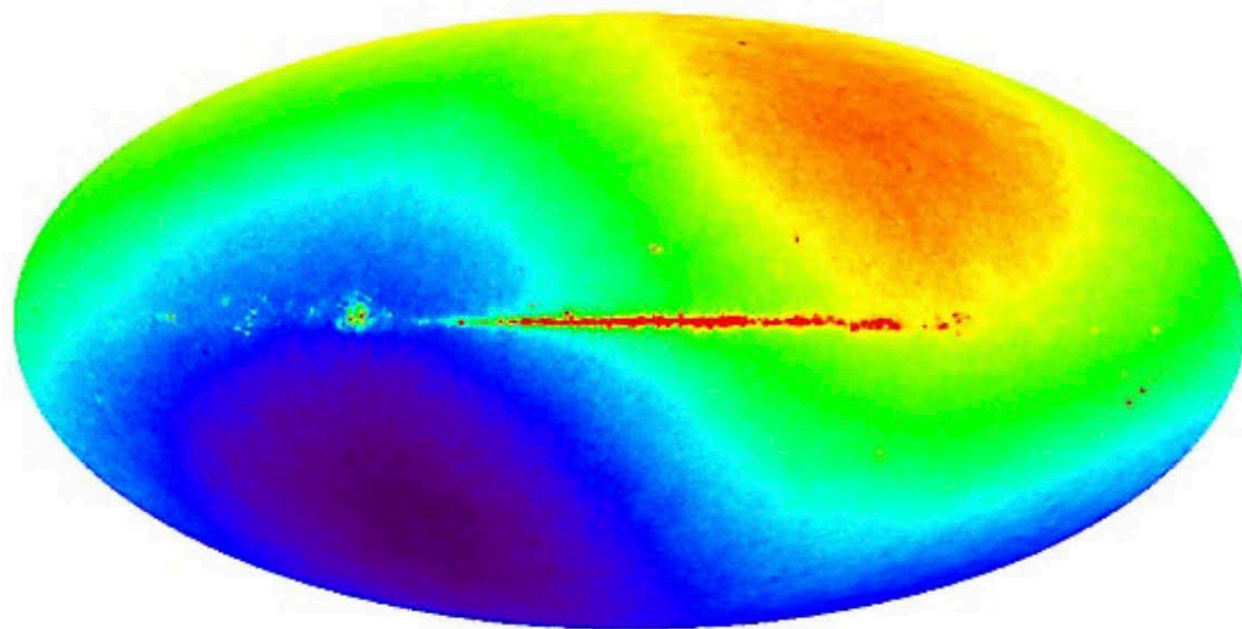
Old and new themes


J. Peebles, D. Wilkinson, 1968
E. Conklin, 1969, 1971, 1972
P. Henry, 1971
G. Ellis, J. Baldwin, 1984
M. Rubart & D. Schwarz 2013
J. Colin et al. 2017
C. Bengaly et al. 2018
N. Secrest et al. 2021, 2022
T. Siewert et al. 2021

1) H_0 tension $(4 - 6)\sigma$ tension

2) Cosmic dipole tension

Primeval fireball

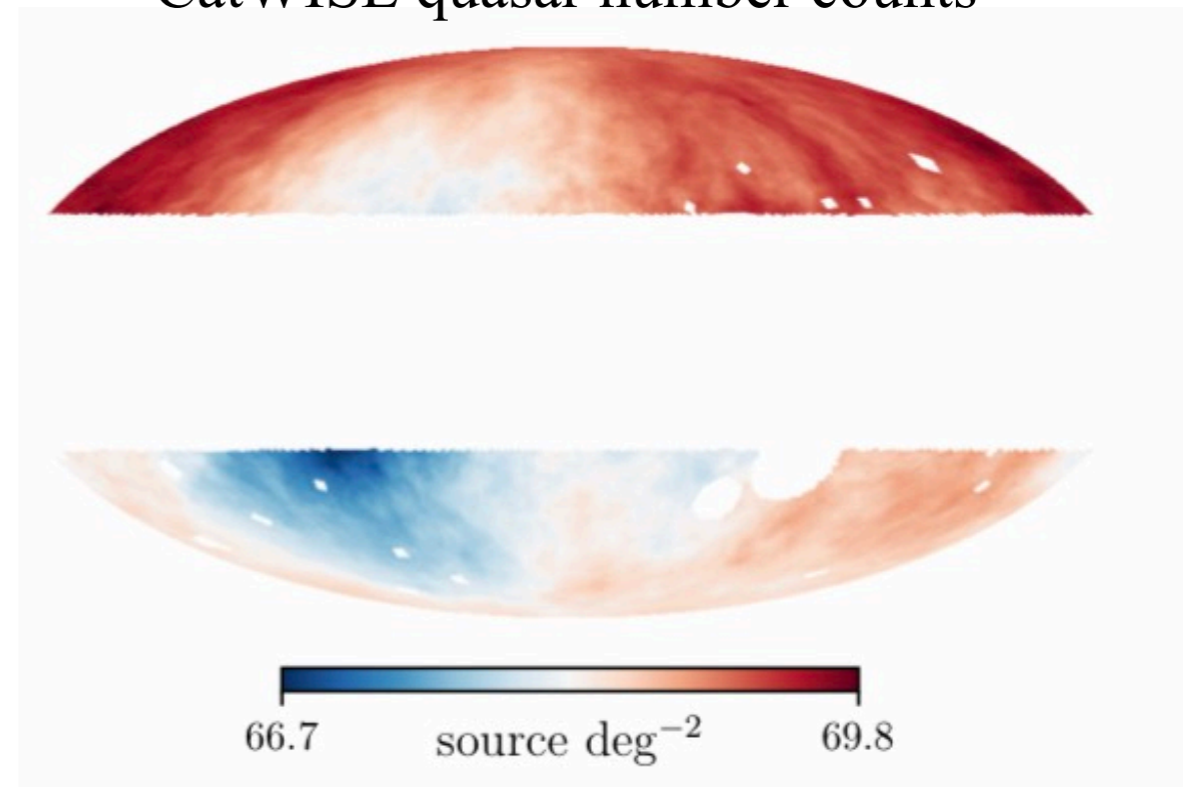


-4 mK  +4 mK

$$\|\mathbf{v}_o\| = (369.82 \pm 0.11) \text{ km s}^{-1}$$

$(2 - 5)\sigma$ tension

CatWISE quasar number counts

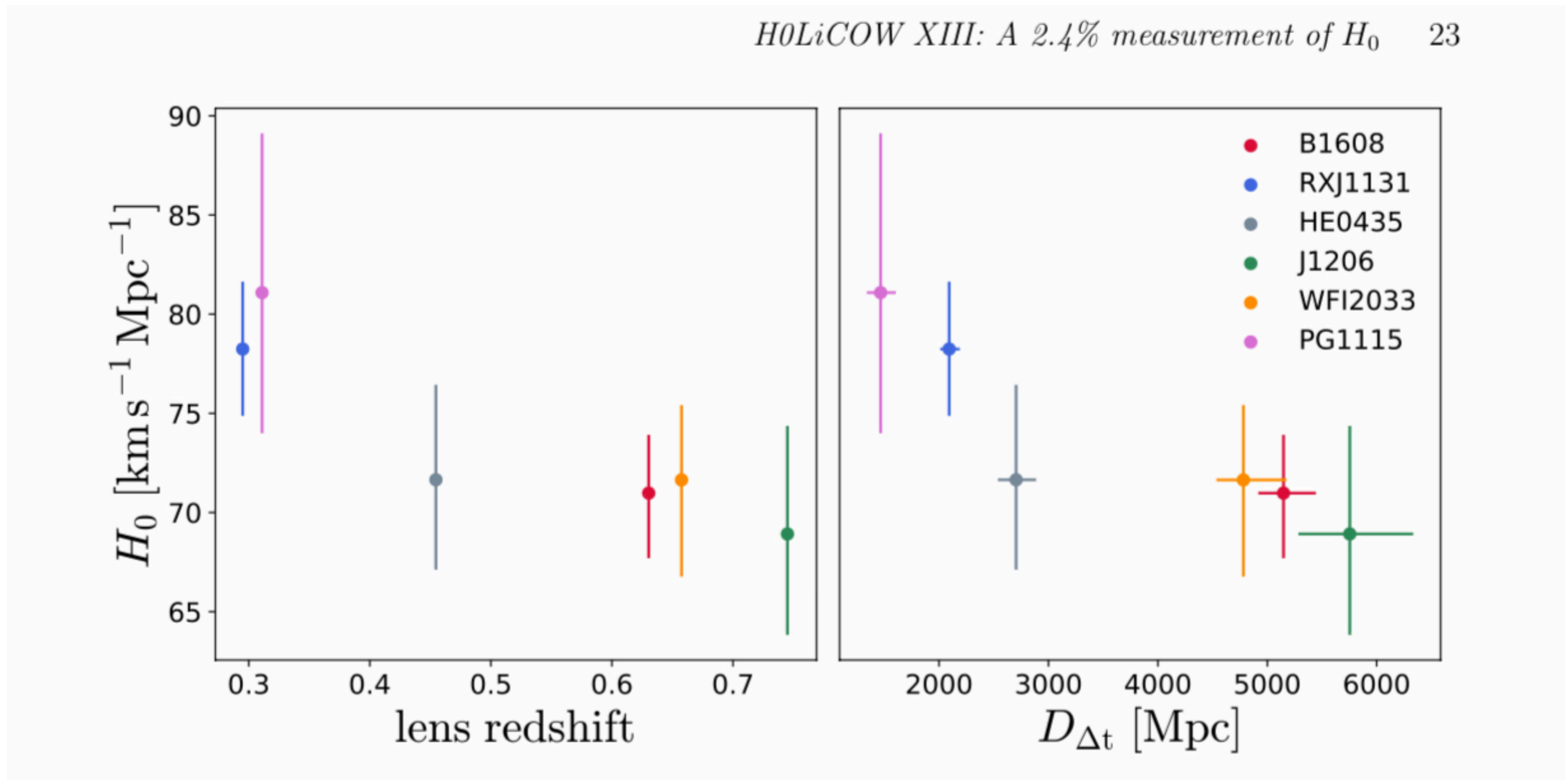


66.7  source deg⁻² 69.8

$$\|\mathbf{v}_o\| = (796 \pm 87) \text{ km s}^{-1}$$

Trend with lens redshift

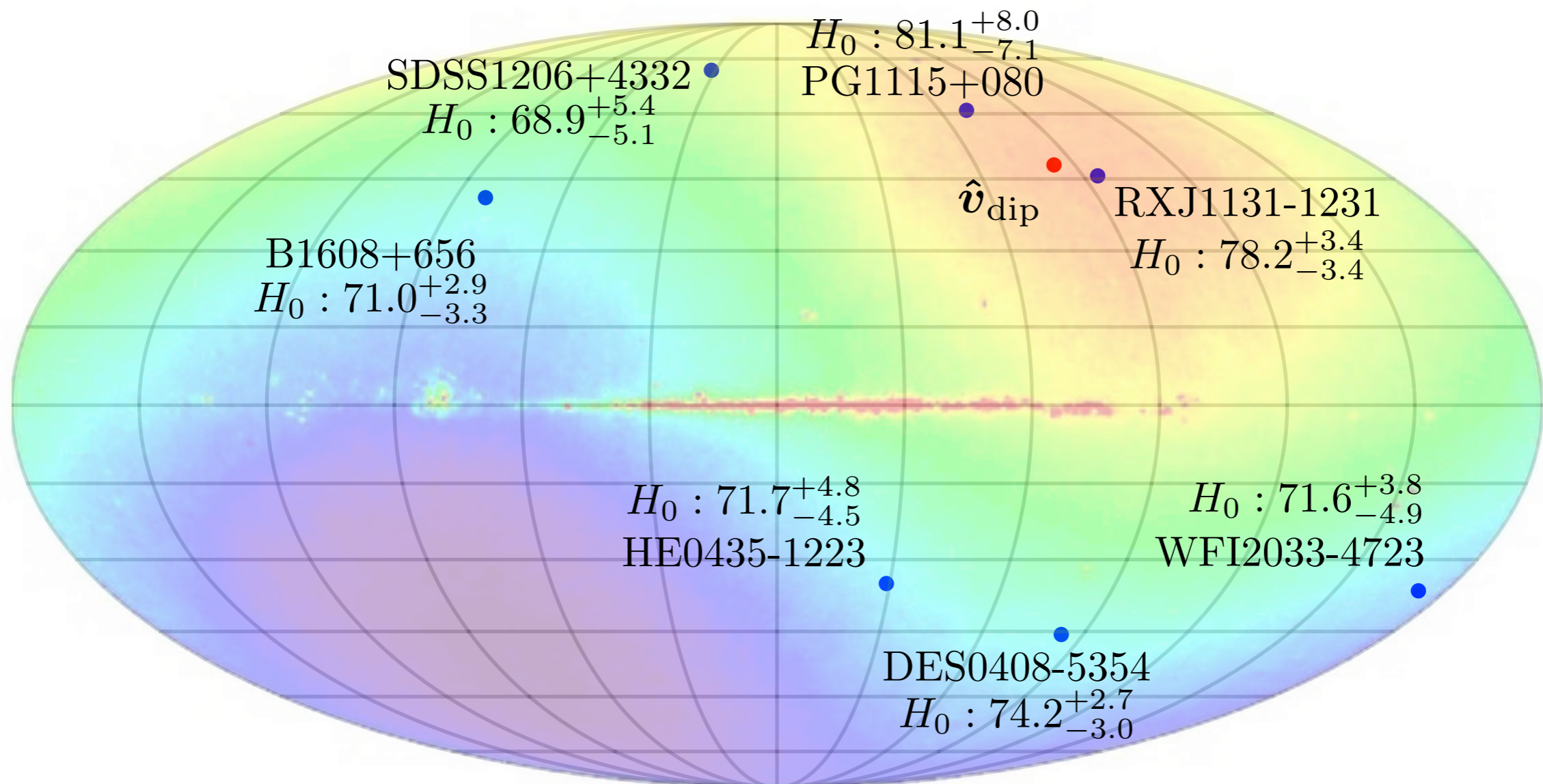
K. Wong et al., 2019



Sky distribution of the lenses

H0LiCOW

Chethan Krishnan, Roya Mohayaee,
Eoin Ó. Colgáin, M. M. Sheikh-
Jabbari, and L. Yin. Hints, 2022
C.D., M. Millon, T. Baker, 2023



Progress

C.D., M. Millon, T. Baker, 2023

$$c\Delta t_{ij} = (1 + z_l) \frac{d_l d_s}{d_{ls}} \left(\frac{(\theta_i - \beta)^2}{2} - \frac{(\theta_j - \beta)^2}{2} - [\Psi(\theta_i) - \Psi(\theta_j)] \right)$$

What are the observables?

$$\{\Delta t'_{ij}, z'_l, z'_s, \theta'_i, \theta'_j\}$$

Physical effects from a boost

$$\beta = \frac{\|\mathbf{v}_o\|}{c} \simeq \mathcal{O}(10^{-3})$$

1) Time dilation

$$\Delta t' = \Delta t \sqrt{1 - \beta^2}$$

2) Doppler shift

$$1 + z' = (1 + z) \frac{\sqrt{1 - \beta^2}}{1 + \beta \cos(\theta)}$$

3) Aberration

$$\theta' = \theta - \beta \sin(\theta) + \mathcal{O}(\beta^2)$$

Accumulation of biases

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$$H_0 = \underbrace{\frac{\chi[z'_l]\chi[z'_s]}{\chi[z'_l, z'_s]} \frac{[\hat{\phi}(\boldsymbol{\theta}'_i, \boldsymbol{\beta}''_i) - \hat{\phi}(\boldsymbol{\theta}'_j, \boldsymbol{\beta}''_j)]}{\Delta t'_{ij}}}_{=H'_0 \text{ (inferred)}} \left(1 + \frac{c\Delta T_{ij}}{c\Delta t'_{ij}} \frac{v_o}{c} \right)$$

H_0 bias

$$\frac{\Delta H_0}{H'_0} = \frac{\Delta T_{ij}}{\Delta t'_{ij}} \frac{v_o}{c}$$

$$c\Delta T_{ij} = (1 + z'_l) \frac{d[z'_l]d[z'_s]}{d[z'_l, z'_s]} \left[\underbrace{(\tilde{\theta}'_i - \tilde{\beta}''_i)(\Theta_i - B''_i)}_{\text{angle bias}} - \underbrace{(\tilde{\theta}'_j - \tilde{\beta}''_j)(\Theta_j - B''_j)}_{\text{lens model bias}} - (P_i - P_j) \right]$$

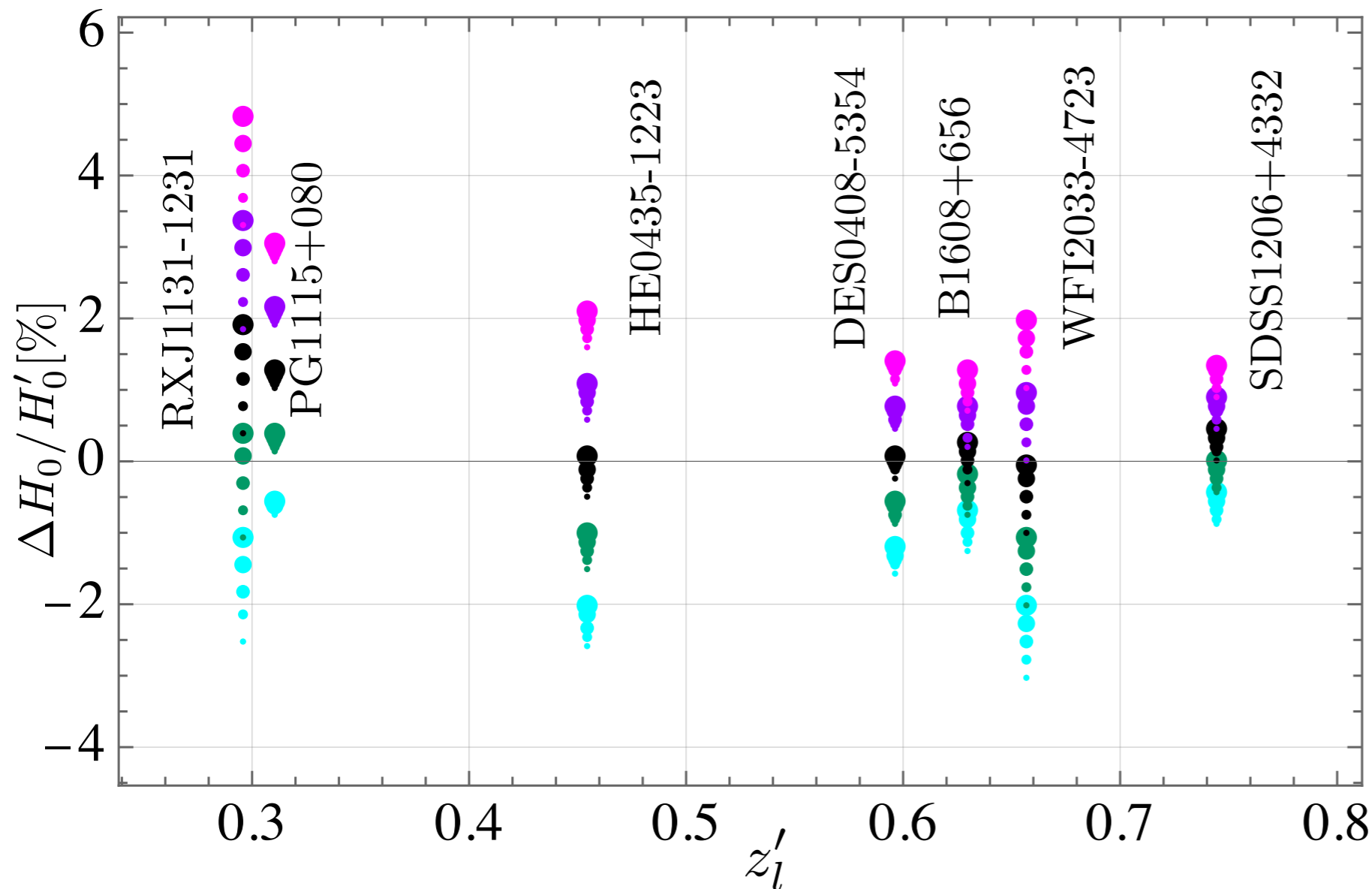
$$+ \frac{1 + z'_l}{d^2[z'_l, z'_s]} \left[\underbrace{Z_L d[z'_l]d[z'_l, z'_s]d[z'_s] + d[z'_l]d[z'_l, z'_s]D_S - d[z'_l]D_{LS}d[z'_s] + D_L d[z'_l, z'_s]d[z'_s]}_{\text{redshift and distance biases}} \right]$$

$$\times \left[\hat{\phi}(\tilde{\theta}'_i, \tilde{\beta}''_i) - \hat{\phi}(\tilde{\theta}'_j, \tilde{\beta}''_j) \right],$$

Time-delay cosmography

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$$H_0 = H'_0 \left(1 + \frac{\Delta H_0}{H'_0} \right)$$



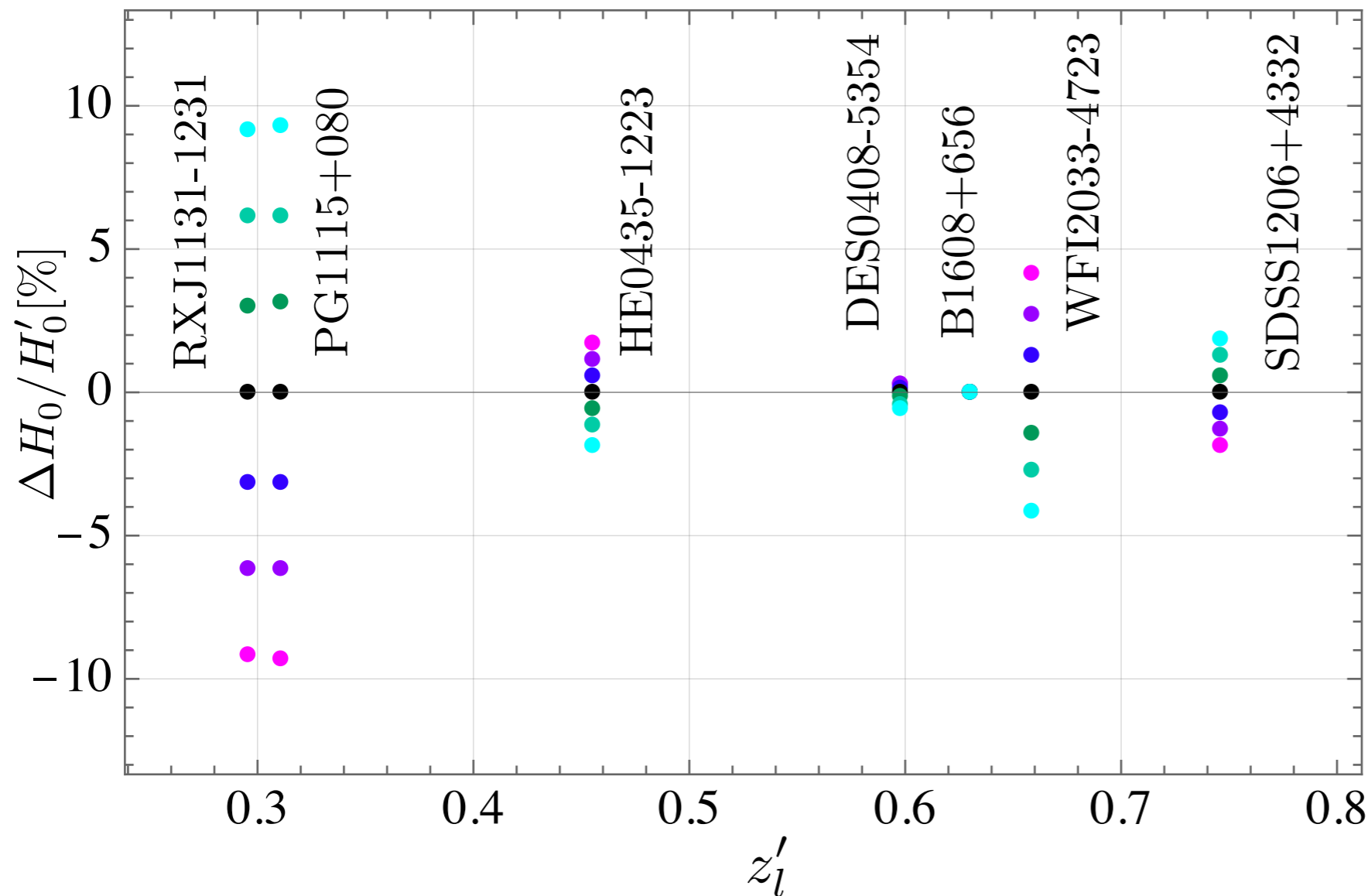
- $v_l^{\parallel} = -900 \text{ km s}^{-1}$
- $v_l^{\parallel} = -450 \text{ km s}^{-1}$
- $v_l^{\parallel} = 0 \text{ km s}^{-1}$
- $v_l^{\parallel} = 450 \text{ km s}^{-1}$
- $v_l^{\parallel} = 900 \text{ km s}^{-1}$

$v_s^{\parallel} \in [-900, 900] \text{ km s}^{-1}$
indicated with dot size

Time-delay cosmography

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$$H_0 = H'_0 \left(1 + \frac{\Delta H_0}{H'_0} \right)$$



- $v_o = -3000 \text{ km s}^{-1}$
- $v_o = -2000 \text{ km s}^{-1}$
- $v_o = -1000 \text{ km s}^{-1}$
- $v_o = 0 \text{ km s}^{-1}$
- $v_o = 1000 \text{ km s}^{-1}$
- $v_o = 2000 \text{ km s}^{-1}$
- $v_o = 3000 \text{ km s}^{-1}$

$$v_l^{\parallel} = v_s^{\parallel} = 0$$

Conclusions

- The peculiar velocities have an impact on time delay cosmography,
- Corrections can reach the percent level for a single system.
- Combined, this is below 0.25% random uncertainty on H_0 and 0.24 % systematic bias.
- It goes in the *wrong* way to solve the Hubble tension or explain the trend with lens redshift.

Thank you!

I am happy to answer any questions you may have :)

Doppler shift

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Angular diameter distances from redshift

$$D_A(z) = \frac{c}{(1+z)H_0} \int_0^z \frac{dz'}{\sqrt{\Omega_{m0}(1+z')^3 + \Omega_{\Lambda 0}}}$$

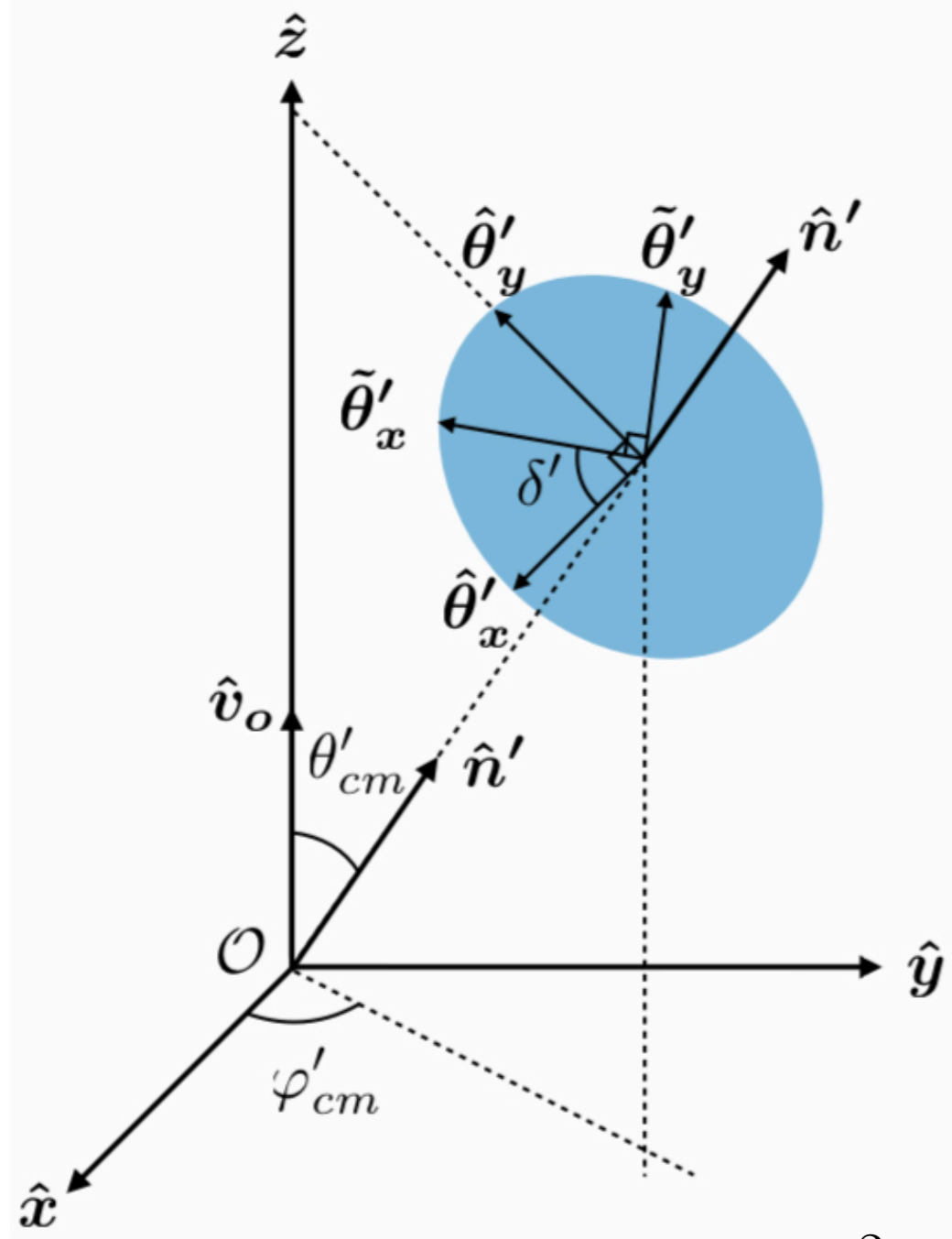
Observed redshift

$$1+z' = (1+z) \frac{\sqrt{1-\beta^2}}{1+\beta \cos(\theta)}$$

Cosmological redshift

Aberration

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$$\theta' = \theta - \beta \sin(\theta) + \mathcal{O}(\beta^2)$$

comoving

$$\tilde{\theta}_i = \tilde{\theta}'_i + \Theta_i \frac{v_o}{c}$$

observed corrections

