

# Heavy Fermions and Flavor Physics beyond the SM

**Paride Paradisi**

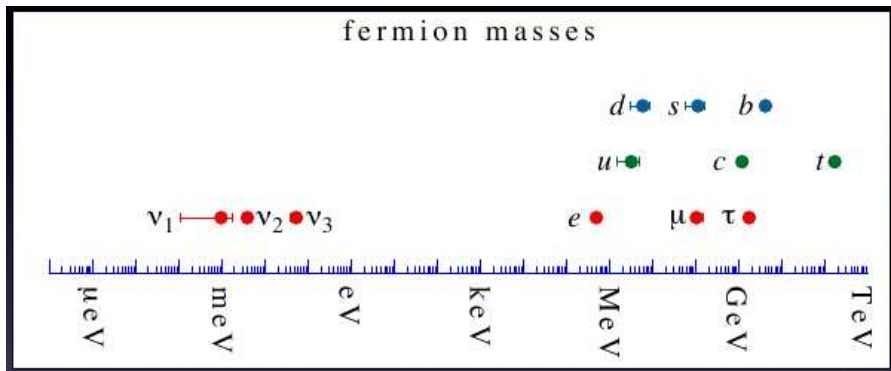


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Portoroz 2011: The Role of Heavy Fermions in Fundamental Physics  
April 11, 2011, Portoroz, Slovenija

- **The origin of flavour is still, to a large extent, a mystery. The most important open questions can be summarized as follow:**
  - ▶ Which is the organizing principle behind the observed pattern of fermion masses and mixing angles?
  - ▶ Are there extra sources of flavour symmetry breaking beside the SM Yukawa couplings which are relevant at the TeV scale?
- **Related important questions are:**
  - ▶ Which is the role of **flavor physics** in the **LHC** era?
  - ▶ Do we expect to understand the (SM and NP) **flavor puzzles** through the synergy and interplay of **flavor physics** and the **LHC**?

# The fermion mass puzzle



$$|V_{\text{CKM}}| \sim \begin{pmatrix} 1 & \lambda_c & \lambda_c^3 \\ \lambda_c & 1 & \lambda_c^2 \\ \lambda_c^3 & \lambda_c^2 & 1 \end{pmatrix}, \quad |V_{\text{PMNS}}| \simeq \begin{pmatrix} 0.79 - 0.86 & 0.50 - 0.61 & 0.0 - 0.2 \\ 0.25 - 0.53 & 0.47 - 0.73 & 0.56 - 0.79 \\ 0.21 - 0.51 & 0.42 - 0.69 & 0.61 - 0.83 \end{pmatrix}_{3\sigma}$$

**Hierarchical**

**Anarchic / Tribimaximal**

- $\mathcal{L}_{Kinetic+Gauge}^{SM} + \mathcal{L}_{Higgs}^{SM}$  has a large  $U(3)^5$  global **flavour symmetry**

$$\mathbf{G} = \mathbf{U}(3)^5 = \mathbf{U}(3)_u \otimes \mathbf{U}(3)_d \otimes \mathbf{U}(3)_Q \otimes \mathbf{U}(3)_e \otimes \mathbf{U}(3)_L$$

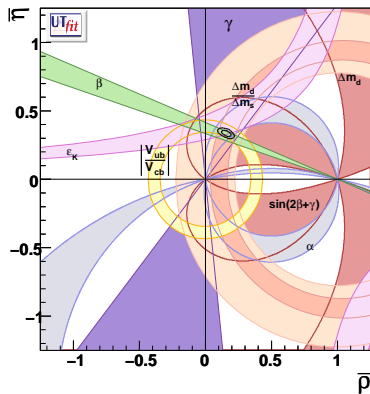
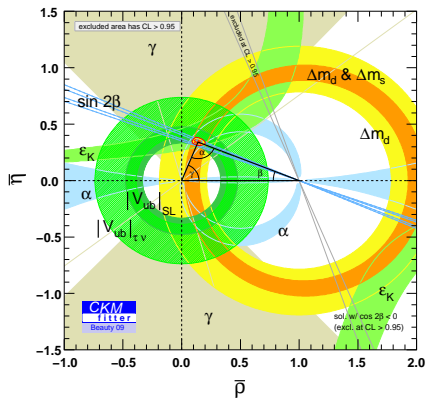
- $\mathcal{L}_{Yukawa} = \bar{Q}_L \mathbf{Y}_D D_R \phi + \bar{Q}_L \mathbf{Y}_U U_R \tilde{\phi} + \bar{L}_L \mathbf{Y}_L E_R \phi + h.c$  break  $G$  down to

$$\mathbf{G} \rightarrow \mathbf{U}(1)_B \times \mathbf{U}(1)_e \times \mathbf{U}(1)_\mu \times \mathbf{U}(1)_\tau$$

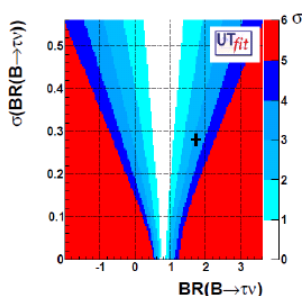
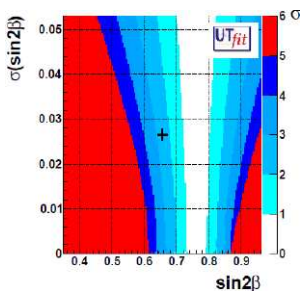
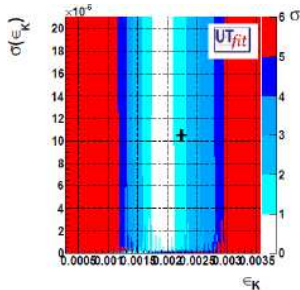
- CKM matrix:**  $Y_U = V_{CKM} \times \text{diag}(y_u, y_c, y_t)$  for  $Y_D = \text{diag}(y_d, y_s, y_b)$

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} n \begin{matrix} e^- \\ \bar{p} \end{matrix} & K \begin{matrix} \ell^- \\ \bar{\pi} \end{matrix} & B \begin{matrix} \ell^- \\ \bar{\pi} \end{matrix} \\ D \begin{matrix} \ell^- \\ \bar{\pi} \end{matrix} & D \begin{matrix} \ell^- \\ \bar{K} \end{matrix} & B \begin{matrix} \ell^- \\ \bar{D} \end{matrix} \\ B^0 \begin{matrix} \ell^- \\ \bar{B}^0 \end{matrix} & B_s \begin{matrix} \ell^- \\ \bar{B}_s \end{matrix} & t \begin{matrix} W \\ b \end{matrix} \end{pmatrix}$$

# Messages from the B-factories



**“Very likely, flavour and CP violation in FC processes are dominated by the CKM mechanism” (Nir)**



- 1  $\sim 6\%$  reduction of  $\epsilon_K^{\text{SM}}$   
[Buras & Guadagnoli; BG & Isidori]
- 2 smaller  $\hat{B}_K$  from unquenched analyses  
[Antonio et al. '08; Aubin et al. '10]
- 3 fit vs. exp.  $\approx -1.7\sigma$

- 1 fit vs. exp.  $\approx +2.6\sigma$

- 1  $B(B \rightarrow \ell \nu) \sim f_B^2 |V_{ub}|^2$
- 2  $B(B \rightarrow \ell \nu) / \Delta M_d \sim (\sin \beta / \sin \gamma)^2 / \hat{B}_{B_d}$
- 3 fit vs. exp.  $\approx -3.2\sigma$

**NEW:**  $\epsilon_K^{\text{SM}}$  @ NNLO QCD:

$\sim +3\%$  [Brod & Gorbahn, '10]

**Similar conclusions also by Lenz & Nierste + CKMfitter collaboration ('10)**

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \sum_{d=6} \frac{c_{ij}^{(6)}}{\Lambda_{\text{NP}}^2} \mathcal{O}_{ij}^{(6)}$$

[Isidori, Nir, Perez '10]

Operator	Bounds on $\Lambda$ (TeV)		Bounds on $c_{ij}$ ( $\Lambda = 1$ TeV)		Observables
	Re	Im	Re	Im	
$(\bar{s}_L \gamma^\mu d_L)^2$	$9.8 \times 10^2$	$1.6 \times 10^4$	$9.0 \times 10^{-7}$	$3.4 \times 10^{-9}$	$\Delta m_K; \varepsilon_K$
$(\bar{s}_R d_L)(\bar{s}_L d_R)$	$1.8 \times 10^4$	$3.2 \times 10^5$	$6.9 \times 10^{-9}$	$2.6 \times 10^{-11}$	$\Delta m_K; \varepsilon_K$
$(\bar{c}_L \gamma^\mu u_L)^2$	$1.2 \times 10^3$	$2.9 \times 10^3$	$5.6 \times 10^{-7}$	$1.0 \times 10^{-7}$	$\Delta m_D;  q/p , \phi_D$
$(\bar{c}_R u_L)(\bar{c}_L u_R)$	$6.2 \times 10^3$	$1.5 \times 10^4$	$5.7 \times 10^{-8}$	$1.1 \times 10^{-8}$	$\Delta m_D;  q/p , \phi_D$
$(\bar{b}_L \gamma^\mu d_L)^2$	$5.1 \times 10^2$	$9.3 \times 10^2$	$3.3 \times 10^{-6}$	$1.0 \times 10^{-6}$	$\Delta m_{B_d}; S_{B_d \rightarrow \psi K}$
$(\bar{b}_R d_L)(\bar{b}_L d_R)$	$1.9 \times 10^3$	$3.6 \times 10^3$	$5.6 \times 10^{-7}$	$1.7 \times 10^{-7}$	$\Delta m_{B_d}; S_{B_d \rightarrow \psi K}$
$(\bar{b}_L \gamma^\mu s_L)^2$	$1.1 \times 10^2$	$1.1 \times 10^2$	$7.6 \times 10^{-5}$	$7.6 \times 10^{-5}$	$\Delta m_{B_s}$
$(\bar{b}_R s_L)(\bar{b}_L s_R)$	$3.7 \times 10^2$	$3.7 \times 10^2$	$1.3 \times 10^{-5}$	$1.3 \times 10^{-5}$	$\Delta m_{B_s}$



**“Generic” flavor violating sources at the TeV scale are excluded**

- SM without Yukawa interactions:  $U(3)^5$  global **flavour symmetry**

$$\mathbf{U(3)}_u \otimes \mathbf{U(3)}_d \otimes \mathbf{U(3)}_Q \otimes \mathbf{U(3)}_e \otimes \mathbf{U(3)}_L$$

- Yukawa interactions break this symmetry
- Proposal for any New Physics model:

**Yukawa structures as the **only** sources of flavour violation**



**Minimal Flavour Violation** [D'Ambrosio et al. '02]

**Notice that MFV allows new “flavour blind” CPV phases!**

[Kagan et al. '09] (model-independent)

[Ellis et al. '07] (SUSY)

[Colangelo et al., '08], [Smith et al. '09] (SUSY)

[Altmannshofer et al., '08,'09], [P.P & Straub, '09] (SUSY)

[Buras et al., '10,'10] (2HDM)



# MFV & the NP flavor puzzle

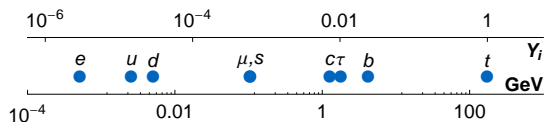
$$(c_{\text{MFV}}^{\Delta F=1})_{ij} \sim V_{ij}^* V_{ij}, \quad (c_{\text{MFV}}^{\Delta F=2})_{ij} \sim (V_{ij}^* V_{ij})^2$$

$\Delta F = 1, 2$ MFV operators	$\Lambda(\text{TeV})$	Observables
$H^\dagger \left( \bar{D}_R Y^{d\dagger} Y^u Y^{u\dagger} \sigma_{\mu\nu} Q_L \right) (e F_{\mu\nu})$	6.1 TeV	$B \rightarrow X_s \gamma, B \rightarrow X_s \ell^+ \ell^-$
$\frac{1}{2} (\bar{Q}_L Y^u Y^{u\dagger} \gamma_\mu Q_L)^2$	5.9 TeV	$\epsilon_K, \Delta m_{B_d}, \Delta m_{B_s}$
$H_D^\dagger \left( \bar{D}_R Y^{d\dagger} Y^u Y^{u\dagger} \sigma_{\mu\nu} T^a Q_L \right) (g_s G_{\mu\nu}^a)$	3.4 TeV	$B \rightarrow X_s \gamma, B \rightarrow X_s \ell^+ \ell^-$
$\left( \bar{Q}_L Y^u Y^{u\dagger} \gamma_\mu Q_L \right) (\bar{E}_R \gamma_\mu E_R)$	2.7 TeV	$B \rightarrow X_s \ell^+ \ell^-, B_s \rightarrow \mu^+ \mu^-$
$\left( \bar{Q}_L Y^u Y^{u\dagger} \gamma_\mu Q_L \right) (e D_\mu F_{\mu\nu})$	1.5 TeV	$B \rightarrow X_s \ell^+ \ell^-$

Observable	Experiment	MFV prediction	SM prediction
$\mathcal{A}_{\text{CP}}(B_s \rightarrow \psi\phi)$	[0.10, 1.44] @ 95% CL	0.04(5)	0.04(2)
$\mathcal{A}_{\text{CP}}(B \rightarrow X_s \gamma)$	< 6% @ 95% CL	< 0.02	< 0.01
$\mathcal{B}(B_d \rightarrow \mu^+ \mu^-)$	< $1.8 \times 10^{-8}$	< $1.2 \times 10^{-9}$	$1.3(3) \times 10^{-10}$
$\mathcal{B}(B \rightarrow X_s \tau^+ \tau^-)$	–	< $5 \times 10^{-7}$	$1.6(5) \times 10^{-7}$
$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})$	< $2.6 \times 10^{-8}$ @ 90% CL	< $2.9 \times 10^{-10}$	$2.9(5) \times 10^{-11}$

[D'Ambrosio et al. '02; Hurth et al. '08, Isidori, Nir & Perez '10]

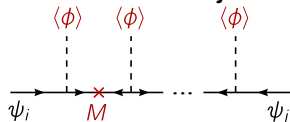
# SM vs. NP flavor puzzle



$$V_{\text{CKM}} \sim \begin{pmatrix} \bullet & \bullet & \bullet & \dots \\ \bullet & \bullet & \bullet & \dots \\ \bullet & \bullet & \bullet & \dots \\ \dots & \dots & \dots & \dots \end{pmatrix}$$

- Froggat-Nielsen '79: Hierarchies from SSB of a Flavour Symmetry

$$\epsilon = \frac{\langle \phi \rangle}{M} \ll 1 \Rightarrow Y_{ij} \propto \epsilon^{(a_i+b_j)}$$



- Flavor Models flavor protection

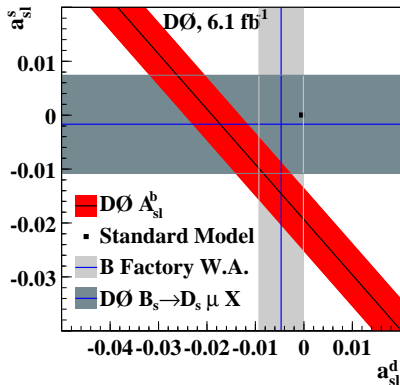
[Lalak, Pokorski & Ross '10]

Operator	$U(1)$	$U(1)^2$	$SU(3)$	MFV
$(\bar{Q}_L X_{LL}^Q Q_L)_{12}$	$\lambda$	$\lambda^5$	$\lambda^3$	$\lambda^5$
$(\bar{D}_R X_{RR}^D D_R)_{12}$	$\lambda$	$\lambda^{11}$	$\lambda^3$	$(y_d y_s) \times \lambda^5$
$(\bar{Q}_L X_{LR}^D D_R)_{12}$	$\lambda^4$	$\lambda^9$	$\lambda^3$	$y_s \times \lambda^5$

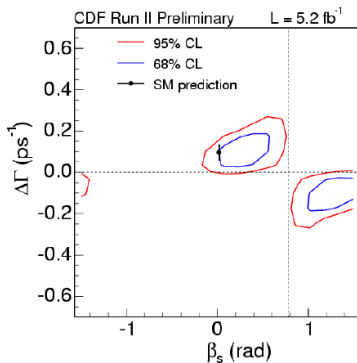
- **High-energy frontier**: A unique effort to determine the NP scale
- **High-intensity frontier** (flavor physics): A collective effort to determine the flavor structure of NP

Where to look for **New Physics** at the low energy?

- Processes very **suppressed** or even **forbidden** in the SM
  - ▶ FCNC processes ( $\mu \rightarrow e\gamma$ ,  $\tau \rightarrow \mu\gamma$ ,  $B_{s,d}^0 \rightarrow \mu^+\mu^-$ ,  $K \rightarrow \pi\nu\bar{\nu}$ )
  - ▶ CPV effects in the electron/neutron EDMs,  $d_{e,n}\dots$
  - ▶ FCNC & CPV in  $B_{s,d}$  decay/mixing &  $D$  mixing amplitudes
- Processes predicted with **high precision** in the SM
  - ▶ EWPO as  $\Delta\rho$ ,  $(g-2)_\mu\dots$
  - ▶ LU in  $R_M^{e/\mu} = \Gamma(K(\pi) \rightarrow e\nu)/\Gamma(K(\pi) \rightarrow \mu\nu)$



$$A_{SL}^q \equiv \frac{\Gamma(\bar{B}_q \rightarrow l^+ X) - \Gamma(B_q \rightarrow l^- X)}{\Gamma(\bar{B}_q \rightarrow l^+ X) + \Gamma(B_q \rightarrow l^- X)},$$



$$S_{\psi\phi} = \sin(2|\beta_s| - 2\phi_{B_s})$$

New Physics in the  $B_s$  mixing phase?

## Brief status of Lepton Flavor Violation searches

## tau LFV

- ▶ past: CLEO explored up to BRs  $\sim 10^{-6}$
- ▶ **present: B-factories are completing exploration up to BRs  $\sim 10^{-8}$**
- ▶ future: Super Flavor Factories can explore up to BRs  $\sim 10^{-10}$
- ▶  $\tau \rightarrow \mu \gamma$  is the most sensitive channel for most mainstream NP models

## muon LFV

- ▶ past: LAMPF, MEGA,  $\text{BF}(\mu \rightarrow e \gamma) < 1.2 \cdot 10^{-11}$  at 90% CL
- ▶ past: SINDRUM II,  $\text{BF}(\mu \rightarrow e \text{ in nucleon field}) < 7 \cdot 10^{-13}$  at 90% CL
- ▶ **present: MEG,  $\text{BF}(\mu \rightarrow e \gamma) < 1.5 \cdot 10^{-11}$  at 90% CL, (sensitivity  $6 \cdot 10^{-12}$ )**
- ▶ future: MEG will soon reach sensitivity  $\sim 10^{-13}$
- ▶ future: Mu2E and COMET/PRISM can much increase reach on  $\text{BF}(\mu \rightarrow e \text{ in nucleon field})$

Process	Expected 90% CL upper limit	$3\sigma$ evidence reach
$\text{BF}(\tau \rightarrow \mu \gamma)$	$2.4 \cdot 10^{-9}$	$5.4 \cdot 10^{-9}$
$\text{BF}(\tau \rightarrow e \gamma)$	$3.0 \cdot 10^{-9}$	$6.8 \cdot 10^{-9}$
$\text{BF}(\tau \rightarrow \ell \ell)$	$2.3\text{--}8.2 \cdot 10^{-10}$	$1.2\text{--}4.0 \cdot 10^{-9}$

[Lusiani @ HQL10]

**The soft-sector contains a huge number of FV and/or CPV parameters: natural  $O(1)$  values for these parameters are excluded by the exp. data**

## Flavor problem: solutions

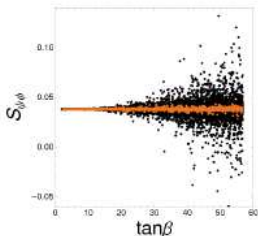
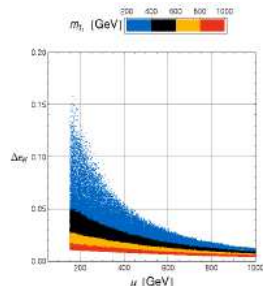
- 1 **Decoupling:**  $m_{SUSY} \gg \text{TeV}$ , the hierarchy problem is (partly) reintroduced
- 2 **Degeneracy:** sfermion masses nearly degenerate, e.g. gauge mediation, flavour models, MFV...
- 3 **Alignment:** quark and squark mass matrices aligned [Nir & Seiberg '93]

## CP problem: solutions

- 1 Degeneracy & Alignment do not solve the CP problem as flavor blind phases are allowed
- 2 **CPV from flavor effects**  $\Rightarrow$  EDMs suppressed by small mixing angles
- 3 Hp in flavor models: CP spontaneously broken in the flavor sector by flavon VEVs [Nir & Rattazzi '96]
- 4 Applying the same idea to MFV: CPV only from MFV-compatible terms breaking the flavour blindness [P.P & Straub, '09]

## 1 Kaon mixing

- ▶ The mixing amplitude  $M_{12}^K$  has no sensitivity to the new flavor blind phases
- ▶ Still,  $\epsilon_K \propto \text{Im}(M_{12}^K)$  can get a **positive NP contribution** up to 15%
- ▶ But only for a **very light SUSY spectrum**:  
 $\mu, m_{\tilde{t}_1} \simeq 200\text{GeV}$

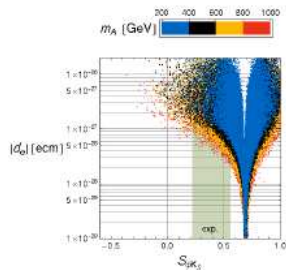
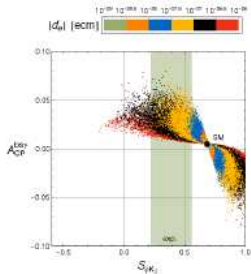
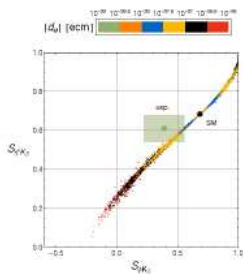


## 2 $B_d$ and $B_s$ mixing

- ▶ Leading NP contributions to  $M_{12}^{d,s}$  are **insensitive to the new phases** of a FBMSSM. (at least for moderate  $\tan \beta \dots$ )
- ▶ For large  $\tan \beta$ , the constraint from  $b \rightarrow s \gamma$  does not allow for sizeable effects
- ▶  $S_{\psi K_S}$  and  $S_{\psi \phi}$  are **SM like** ( $S_{\psi \phi} \simeq 0.03 - 0.05$ )

[Altmannshofer, Buras & P.P., '08]

# MSSM with MFV and “flavour blind” phases



- ▶ CP violating  $\Delta F = 0$  and  $\Delta F = 1$  dipole amplitudes can be strongly modified
- ▶  $S_{\phi K_S}$  and  $S_{\eta' K_S}$  can simultaneously be brought in **agreement with the data**
- ▶ sizeable and correlated effects in  $A_{CP}^{b \to \eta'} \simeq 1\% - 6\%$
- ▶ **lower bounds** on the electron and neutron EDMs at the level of  $d_{e,n} \gtrsim 10^{-26} \text{ ecm}$
- ▶ large and correlated effects in the CP asymmetries in  $B \rightarrow K^* \mu^+ \mu^-$  (WA, Ball, Bharucha, Buras, Straub, Wick)

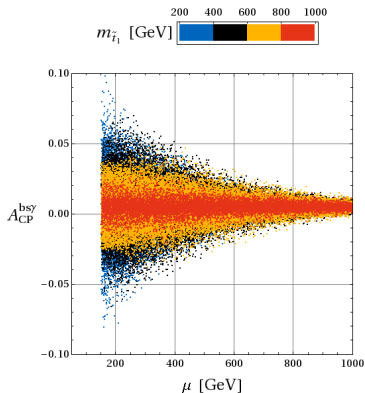
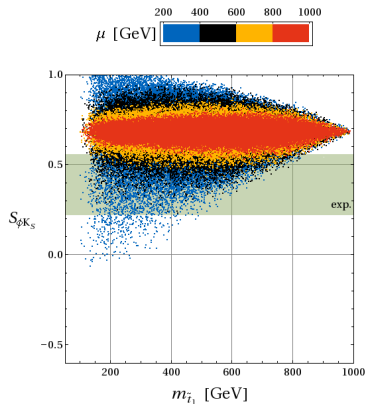
- ▶ the leading NP contributions to  $\Delta F = 2$  amplitudes are **not sensitive** to the new phases of the FBMSSM
- ▶ CP violation in meson mixing is **SM like**
- ▶ i.e. small effects in  $S_{\psi \phi}$ ,  $S_{\psi K_S}$  and  $\epsilon_K$
- ▶ in particular:  $0.03 < S_{\psi \phi} < 0.05$

A combined study of all these observables and their correlations constitutes a **very powerful test** of the FBMSSM

[Altmannshofer, Buras & P.P., '08]



# Implications for direct searches of SUSY particles



- ▶  $S_{\phi K_S} \simeq 0.4$  implies  $\mu \lesssim 600\text{GeV}$  and  $m_{\tilde{t}_1} \lesssim 700\text{GeV}$
- ▶  $A_{CP}^{bs\gamma} \gtrsim 2\%$  implies  $\mu \lesssim 600\text{GeV}$  and  $m_{\tilde{t}_1} \lesssim 800\text{GeV}$

[Altmannshofer, Buras & P.P., '08]

- **Neutrino Oscillation**  $\Rightarrow m_{\nu_i} \neq m_{\nu_j} \Rightarrow$  **LFV**
- **see-saw**:  $m_\nu = \frac{(m_\nu^D)^2}{M_R} \sim eV$ ,  $M_R \sim 10^{14-16} \Rightarrow m_\nu^D \sim m_{top}$
- **LFV** transitions like  $\mu \rightarrow e\gamma$  @ 1 loop with exchange of

- ▶  $W$  and  $\nu$  in the **SM** framework (**GIM**) with  $\Lambda_{NP} \equiv M_R$

$$Br(\mu \rightarrow e\gamma) \sim \frac{m_\nu^{D4}}{M_R^4} \leq 10^{-50}$$

- ▶  $\tilde{W}$  and  $\tilde{\nu}$  in the **MSSM** framework (**SUPER-GIM**) with  $\Lambda_{NP} \equiv \tilde{m}$

$$Br(\mu \rightarrow e\gamma) \sim \frac{m_\nu^{D4}}{\tilde{m}^4} \leq 10^{-11}$$

⇓

- **LFV** signals are undetectable (**detectable**) in the SM (**MSSM**)

$$W = h^e L e^c H_1 + h^\nu L \nu^c H_2 + M_R \nu^c \nu^c + \mu H_1 H_2,$$

$$\mathcal{M}_\nu = -h^\nu M_R^{-1} h^{\nu T} v_2^2,$$

$$M_{\tilde{\ell}}^2 = \begin{pmatrix} m_L^2(1 + \delta_{LL}^{ij}) & (A - \mu t_\beta)m_\ell + m_L m_R \delta_{LR}^{ij} \\ (A - \mu t_\beta)m_\ell + m_L m_R \delta_{LR}^{ij \dagger} & m_R^2(1 + \delta_{RR}^{ij}) \end{pmatrix}$$

- If  $h^e = h_{ij}^e \delta_{ij}$  and  $M_R = (M_R)_{ij} \delta_{ij} \Rightarrow h^\nu \neq h_{ij}^\nu \delta_{ij}$  in general. Flavour universal SUSY breaking and yet large LFV from SUSY see-saw

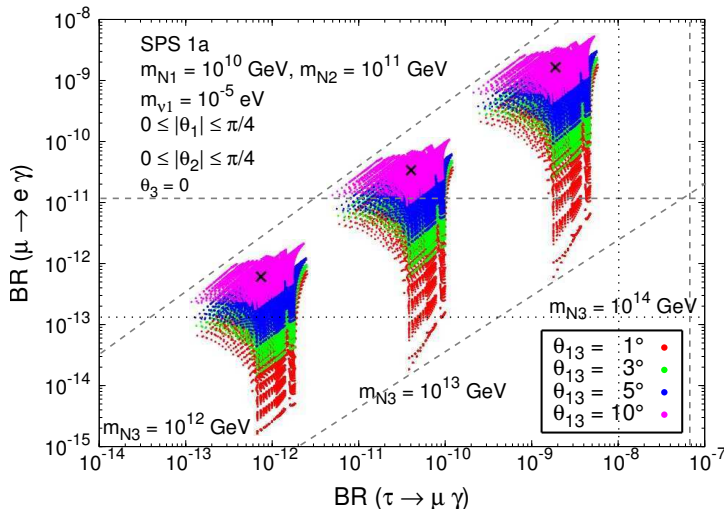
$$\delta_{LL}^{ij} \approx -\frac{3}{8\pi^2} (h^\nu h^{\nu \dagger})_{ij} \ln \frac{M_X}{M_R} \quad [\text{Borzumati \& Masiero, '86}]$$

- $h^\nu$  is unknown  $\Rightarrow$  No model independent predictions for LFV

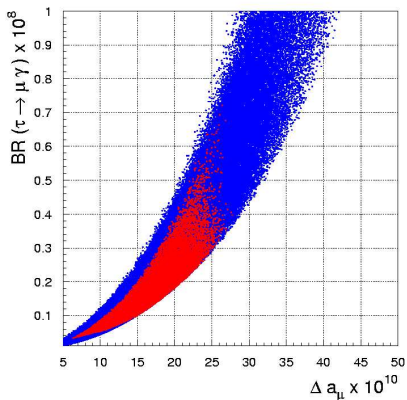
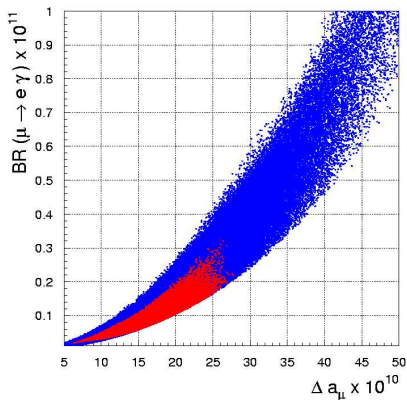
$$h^\nu = U_{\text{MNS}}^* \mathcal{D}_{\sqrt{\mathcal{M}_\nu}} R^T \mathcal{D}_{\sqrt{M_R}} \frac{1}{v_2} \quad [\text{Casas \& Ibarra, '01}]$$

$R^\dagger R = 1 \Rightarrow$  **three angles** and **three phases**

# $\mu \rightarrow e \gamma$ and $\tau \rightarrow \mu \gamma$ in SUSY see-saw



[Herrero et al., '06]



$$|\delta_{LL}^{12}| = 10^{-4} \text{ and } |\delta_{LL}^{23}| = 10^{-2},$$

[Isidori, Mescia, Paradisi & Ternes, 07]

$$BR(l_i \rightarrow l_j \gamma) \approx \left[ \frac{\Delta a_\mu}{20 \times 10^{-10}} \right]^2 \times \left\{ \begin{array}{ll} 1 \times 10^{-4} |\delta_{LL}^{12}|^2 & [\mu \rightarrow e] \\ 2 \times 10^{-5} |\delta_{LL}^{23}|^2 & [\tau \rightarrow \mu] \end{array} \right\}$$

## RG induced LFV interactions in SUSY GUTs

- **SUSY SU(5)** [Barbieri & Hall, '95]

$$(\delta_{LL}^{\tilde{q}})_{ij} \sim h^u h^{u\dagger}_{ij} \sim h_t^2 V_{CKM}^{ik} V_{CKM}^{kj*} \rightarrow (\delta_{RR}^{\tilde{l}})_{ij} \simeq (\delta_{LL}^{\tilde{q}})_{ij}$$

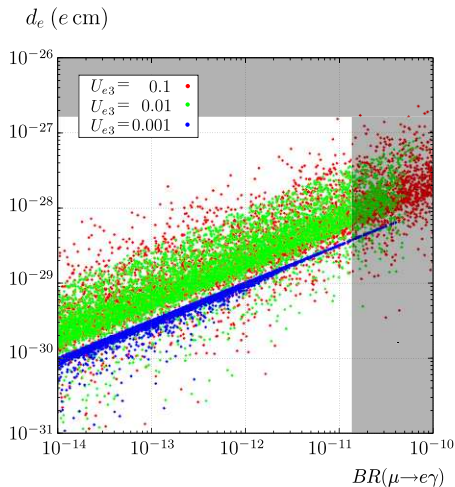
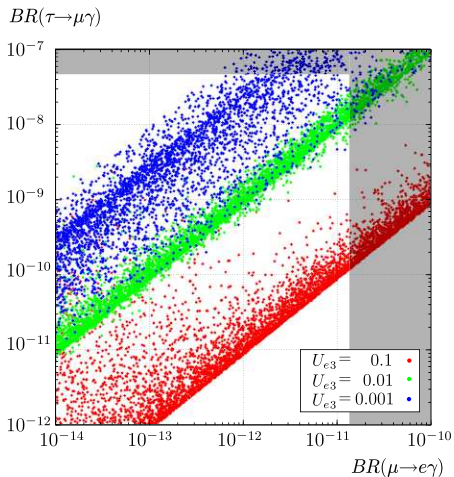
- **SUSY SU(5)+RN** [Yanagida et al., '95]

$$(\delta_{LL}^{\tilde{l}})_{ij} \sim (h^\nu h^{\nu\dagger})_{ij} \quad \& \quad (\delta_{RR}^{\tilde{l}})_{ij} \sim (h^u h^{u\dagger})_{ij}$$

- **SUSY SU(5)+RN** [Moroi, '00] & **SO(10)** [Chang, Masiero & Murayama, '02]

$$\sin \theta_{\mu\tau} \sim \frac{\sqrt{2}}{2} \Rightarrow (\delta_{LL}^{\tilde{l}})_{23} \sim 1 \Rightarrow (\delta_{RR}^{\tilde{q}})_{23} \sim 1$$

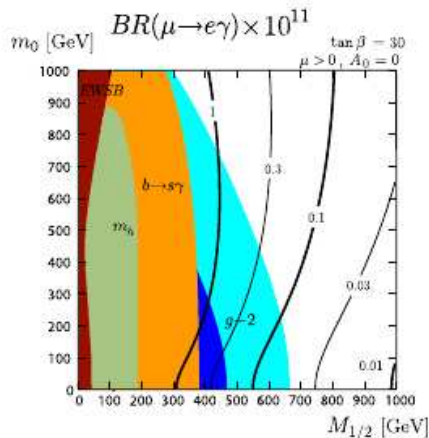
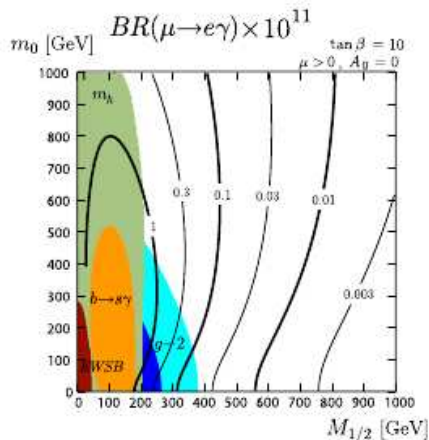
# $\mu \rightarrow e\gamma$ and $\tau \rightarrow \mu\gamma$ in SUSY SU(5)+RN



**hierarchical  $\nu_L$  and  $N_R$**

[Hisano, Nagai, Paradisi & Shimizu, '09]

# BR( $\mu \rightarrow e\gamma$ ) in $SU(5)_{RN}$ and the LHC reach

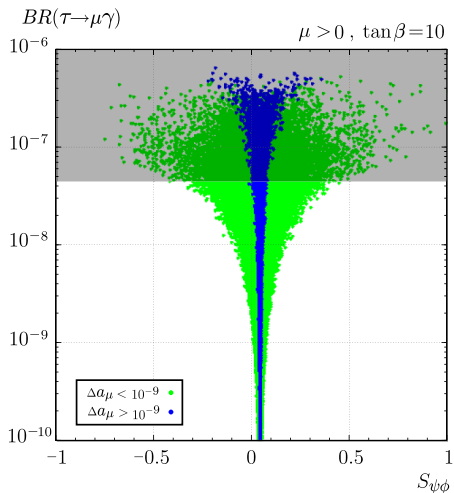


**hierarchical  $\nu_L$  and  $N_R$ ,  $U_{e3} = 0.1$ ,  $M_{N_3} = 10^{-13}$  GeV**

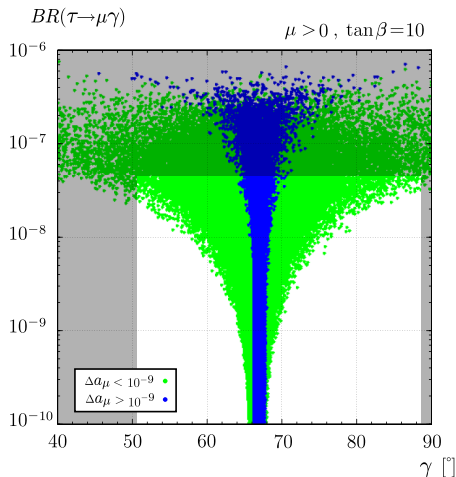
[Hisano, Nagai, Paradisi & Shimizu, '09]



# Quark-Lepton correlations in SUSY SU(5)+RN

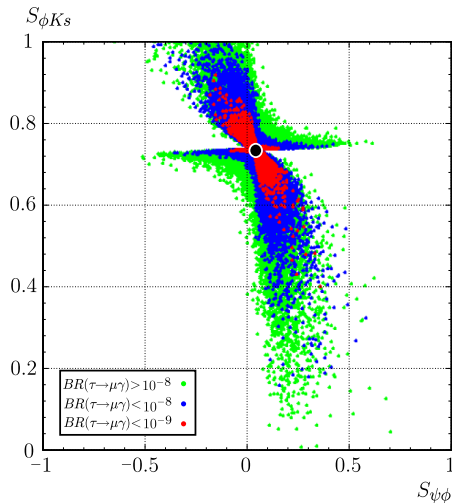
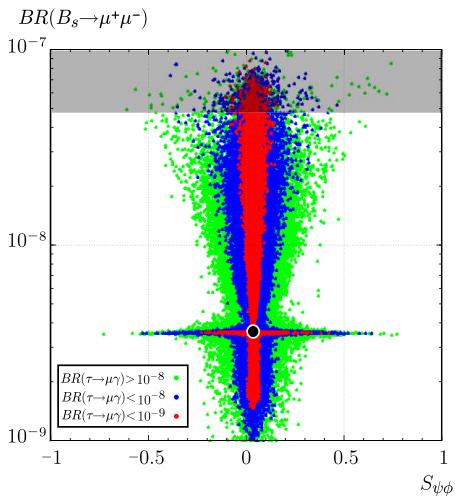


**hierarchical  $\nu_L$  and  $N_R$**



[Buras, Nagai & Paradisi, '10]

# Quark-Lepton correlations in SUSY SU(5)+RN



**hierarchical  $\nu_L$  and  $N_R$**

[Buras, Nagai & Paradisi, '10]

## Abelian vs. Non-abelian flavor models

- Non-abelian models predict  $\approx$  **degenerate** 1st & 2nd sfermion masses
  - ▶ Suppressed contributions to  $1 \leftrightarrow 2$  transitions
  - ▶ Potentially large contributions to  $2 \leftrightarrow 3$  transitions
- In abelian models, sfermions of different generations need **not** be **degenerate**
  - ▶ A single  $U(1)$  &  $O(1)$  1-2 mass splitting lead to  $(\delta_{d,u}^{LL})_{12} \sim \mathcal{O}(\lambda)$
  - ▶  $U(1) \times U(1)$  allows *alignment* in the down sector  $(\delta_d^{LL})_{12} \approx 0 \Rightarrow (\delta_u^{LL})_{12} \sim \mathcal{O}(\lambda)$
  - ▶ Large effects in  $D^0$ - $\bar{D}^0$  mixing

## Chirality structure of flavour violating terms

- Different flavour symmetries lead to different patterns of flavour violation
- Mass insertions:  $M_d^2 = \text{diag}(\tilde{m}^2) + \tilde{m}^2 \begin{pmatrix} \delta_d^{LL} & \delta_d^{LR} \\ \delta_d^{RL} & \delta_d^{RR} \end{pmatrix}$
- $\delta^{LL}$ ,  $\delta^{RR}$ ,  $\delta^{LR}$  fixed by the flavour symmetry up to  $O(1)$  factors

## Representative (non-) abelian flavour models (not just 4 examples...!)

AC model  $U(1)$

[Agashe, Carone]

Large,  $O(1)$  RR  
mass insertions

AKM model  $SU(3)$

[Antusch, King, Malinsky]

Only CKM-like RR  
mass insertions

RVV model  $SU(3)$

[Ross, Velasco-S., Vives]

CKM-like LL & RR  
mass insertions

$\delta_{LL}$  model  $(S_3)^3$

[e.g. Hall, Murayama]

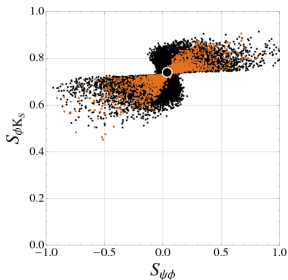
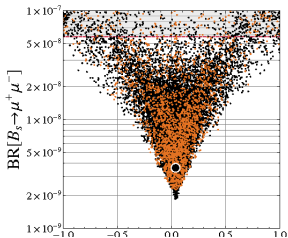
Only CKM-like LL  
mass insertions

$$\delta_d^{LL} \sim \begin{pmatrix} \cdot & 0 & 0 \\ 0 & \cdot & \lambda^2 \\ 0 & \lambda^2 & \cdot \end{pmatrix} \quad \delta_d^{LL} \sim \begin{pmatrix} \cdot & 0 & 0 \\ 0 & \cdot & 0 \\ 0 & 0 & \cdot \end{pmatrix} \quad \delta_d^{LL} \sim \begin{pmatrix} \cdot & \lambda^3 & \lambda^2 \\ \lambda^3 & \cdot & \lambda \\ \lambda^2 & \lambda & \cdot \end{pmatrix} \quad \delta_d^{LL} \sim \begin{pmatrix} \cdot & \lambda^5 & \lambda^3 \\ \lambda^5 & \cdot & \lambda^2 \\ \lambda^3 & \lambda^2 & \cdot \end{pmatrix}$$

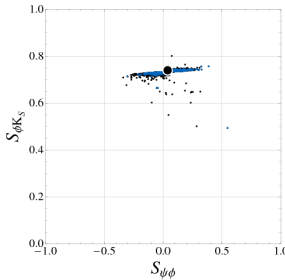
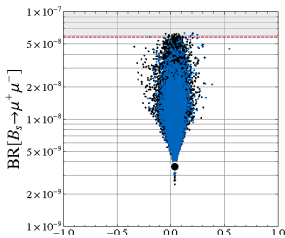
$$\delta_d^{RR} \sim \begin{pmatrix} \cdot & 0 & 0 \\ 0 & \cdot & 1 \\ 0 & 1 & \cdot \end{pmatrix} \quad \delta_d^{RR} \sim \begin{pmatrix} \cdot & \lambda^3 & \lambda^3 \\ \lambda^3 & \cdot & \lambda^2 \\ \lambda^3 & \lambda^2 & \cdot \end{pmatrix} \quad \delta_d^{RR} \sim \begin{pmatrix} \cdot & \lambda^3 & \lambda^2 \\ \lambda^3 & \cdot & \lambda \\ \lambda^2 & \lambda & \cdot \end{pmatrix} \quad \delta_d^{RR} \sim \begin{pmatrix} \cdot & 0 & 0 \\ 0 & \cdot & 0 \\ 0 & 0 & \cdot \end{pmatrix}$$

**Hp: CP is spontaneously broken in the flavor sector** [Nir & Rattazzi '96]

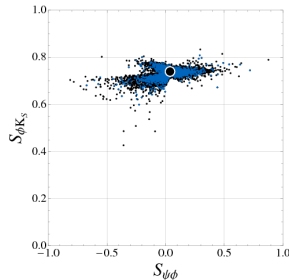
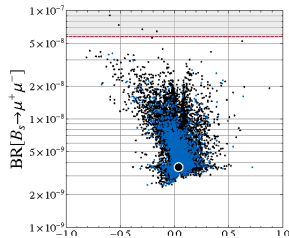
AC



AKM

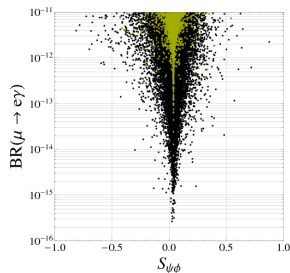
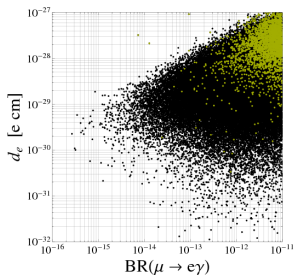
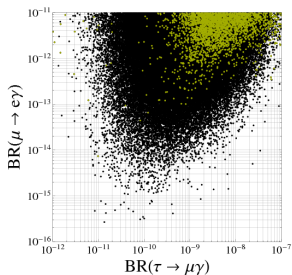


RVV



- Orange (Blue) points: UT tension solved through contribution to  $\Delta M_d / \Delta M_s$  ( $\epsilon_K$ )
- Scan ranges:  $m_0 < 2$  TeV,  $M_{1/2} < 1$  TeV,  $|A_0| < 3m_0$ ,  $5 < \tan \beta < 55$

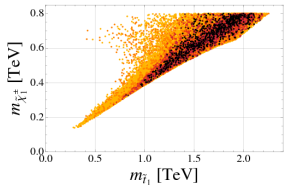
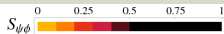
# Phenomenology of a SUSY SU(3) flavor models



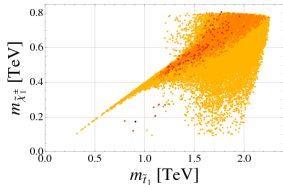
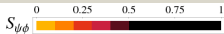
- Yellow points satisfy  $\Delta a_\mu > 10^{-9}$
- Scan ranges:  $m_0 < 2 \text{ TeV}$ ,  $M_{1/2} < 1 \text{ TeV}$ ,  $|A_0| < 3m_0$ ,  $5 < \tan \beta < 55$

[Altmannshofer, Buras, Gori, Paradisi and Straub, '09]

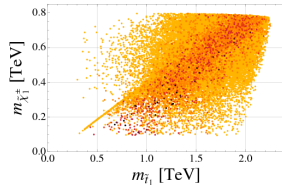
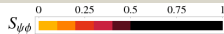
## AC



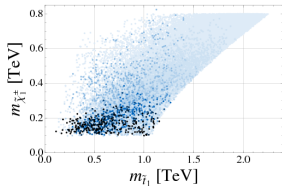
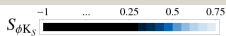
## AKM



## RVV



## delta LL



- Large effects in  $S_{\psi\phi}$  even possible for spectra beyond the LHC reach in the models with RH currents
- Large effects in  $S_{\phi K_S}$  not possible for spectra beyond the LHC reach in the  $\delta LL$  model

[Altmannshofer, Buras, Gori, Paradisi and Straub, '09]

**CPV in  $D^0 - \bar{D}^0 \sim \text{Im}((V_{cb}V_{ub})/(V_{cs}V_{us})) \sim 10^{-3}$  in the SM**

- $\langle D^0 | \mathcal{H}_{\text{eff}} | \bar{D}^0 \rangle = M_{12} - \frac{i}{2} \Gamma_{12}, \quad |D_{1,2}\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle$

- $\frac{q}{p} = \sqrt{\frac{M_{12}^* - \frac{i}{2}\Gamma_{12}^*}{M_{12} - \frac{i}{2}\Gamma_{12}}}, \quad \phi = \text{Arg}(q/p)$

- $x = \frac{\Delta M_D}{\Gamma} = 2\tau \text{Re} \left[ \frac{q}{p} (M_{12} - \frac{i}{2}\Gamma_{12}) \right]$

- $y = \frac{\Delta\Gamma}{2\Gamma} = -2\tau \text{Im} \left[ \frac{q}{p} (M_{12} - \frac{i}{2}\Gamma_{12}) \right]$

$$\mathbf{S}_f = 2\Delta Y_f = \frac{1}{\Gamma_D} \left( \hat{\Gamma}_{\bar{D}^0 \rightarrow f} - \hat{\Gamma}_{D^0 \rightarrow f} \right)$$

$$\eta_f^{\text{CP}} \mathbf{S}_f = x \left( \left| \frac{q}{p} \right| + \left| \frac{p}{q} \right| \right) \sin \phi - y \left( \left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right) \cos \phi$$

$$\mathbf{a}_{\text{SL}} = \frac{\Gamma(D^0 \rightarrow K^+ \ell^- \nu) - \Gamma(\bar{D}^0 \rightarrow K^- \ell^+ \nu)}{\Gamma(D^0 \rightarrow K^+ \ell^- \nu) + \Gamma(\bar{D}^0 \rightarrow K^- \ell^+ \nu)} = \frac{|q|^4 - |p|^4}{|q|^4 + |p|^4}$$

[Nir et al., Kagan et al., Petrov et al., Bigi et al., Buras et al., ...]



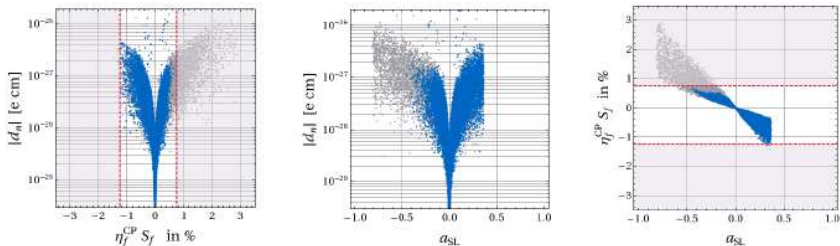


FIG. 3: Correlations between  $d_n$  and  $S_f$  (left),  $d_n$  and  $a_{SL}$  (middle) and  $a_{SL}$  and  $S_f$  (right) in SUSY alignment models. Gray points satisfy the constraints (8)-(10) while blue points further satisfy the constraint (11) from  $\phi$ . Dashed lines stand for the allowed range (18) for  $S_f$ .

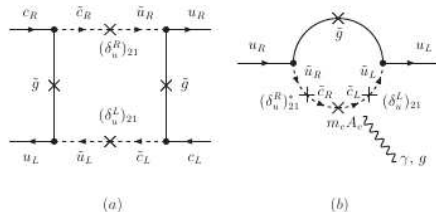






FIG. 2: Examples of relevant Feynman diagrams contributing (a) to  $D^0 - \bar{D}^0$  mixing and (b) to the up quark (C)EDM in SUSY alignment models.

# “DNA-Flavour Test”

	SSU(5)	AC	RVV2	AKM	$\delta$ LL	FBMSSM		
$S_{\phi K_S}$ $A_{CP}(B \rightarrow X_S \gamma)$ $B \rightarrow K^{(*)} \nu \bar{\nu}$ $\tau \rightarrow \mu \gamma$	★★★★	★★★★	●●	■	★★★★	★★★★		
$D^0 - \bar{D}^0$ $A_{7,8}(B \rightarrow K^* \mu^+ \mu^-)$ $A_9(B \rightarrow K^* \mu^+ \mu^-)$	■	★★★★	■	■	■	■		 vs. 
$S_{\psi \phi}$ $B_S \rightarrow \mu^+ \mu^-$	★★★★	★★★★	★★★★	★★★★	■	■		
$\epsilon_K$ $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ $K_L \rightarrow \pi^0 \nu \bar{\nu}$	★★★★	■	★★★★	★★★★	■	■		
$\mu \rightarrow e \gamma$ $\mu + N \rightarrow e + N$ $d_n$ $d_e$ $(g-2)_\mu$	★★★★	★★★★	★★★★	★★★★	★★★★	★★★★		
	★★★★	★★★★	★★★★	★★★★	★★★★	★★★★		
	★★★★	★★★★	★★★★	★★★★	●●	★★★★		
	★★★★	★★★★	★★★★	●●	■	★★★★		
	★★★★	★★★★	★★★★	●●	★★★★	★★★★		

[Altmannshofer et al., '09]

**The origin of flavour is still, to a large extent, a mystery. The most important open questions can be summarized as follow:**

- **Which is the organizing principle behind the observed pattern of fermion masses and mixing angles?**
- **Are there extra sources of flavour symmetry breaking beside the SM Yukawa couplings which are relevant at the TeV scale?**

**The synergy and interplay of flavor physics and the LHC will tell us a lot...**