## Anomalous $t W b$ couplings Interplay of top and bottom physics <br>  <br> Jure Drobnak <br>  <br> Ljubljana, Slovenija

12. 4. 2011, Portorož

The role of heavy fermions in fundamental physics

## Outline of the talk

- Anomalous $t W b$ couplings and top quark decays.
- Effects on helicity fractions of $W$ boson.
- Analysis at NLO in QCD.
- Direct constraints.
- Anomalous $t W b$ couplings and $B_{d, s}-\bar{B}_{d, s}$ mixing.
- Effects on the the mixing amplitude $M_{12}$.
- Can these effects complie with the favored non-SM $M_{12}$ values from recent fits?
- If so, what kind of helicity fractions do they predict? $\leftarrow$ interplay
- Conclusions.


## Helicity fractions of $W$ boson in

$$
t \rightarrow b W
$$

- We can split the decay width $\Gamma(t \rightarrow W b)$ with respect to the polarization of the $W$ boson.

$$
\Gamma_{t \rightarrow b W}=\Gamma_{L}+\Gamma_{-}+\Gamma_{+}, \quad \mathcal{F}_{i}=\Gamma_{i} / \Gamma
$$

- Helicity fractions $\mathcal{F}_{i}$ are accessable through angular distribution of final state leptons M. Fischer et al. hep-ph/0011075

$\frac{1}{\Gamma} \frac{\mathrm{~d} \Gamma}{\mathrm{~d} \cos \theta}=\frac{3}{8}(1+\cos \theta)^{2} \mathcal{F}_{+}+\frac{3}{8}(1-\cos \theta)^{2} \mathcal{F}_{-}+\frac{3}{4} \sin ^{2} \theta \mathcal{F}_{L}$


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$$

Theory side

- The "transverse plus" component is highly surpressed!
- Non-zero $\mathcal{F}_{+}$in SM comes from QCD and EW corrections, $m_{b} \neq 0$.

$$
\mathcal{F}_{L}^{\mathrm{SM}}=0.687(5)
$$

$$
\mathcal{F}_{+}^{\mathrm{SM}}=0.0017(1)
$$ 1005.2625

> H. S. Do et al. hep-ph/0209185

> M. Fischer et al.
> hep-ph/0101322


- Measured $\mathcal{F}_{+}>0.2 \%$ would indicate new physics effect!


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$$

## Experiment side

- Most recent measurements from Tevatron

| $\mathcal{F}_{L}=0.88(13)$ | $\mathcal{F}_{+}=-0.15(9)$ | CDF |
| :--- | :--- | :---: |
| ${ }_{1003.0224}$ |  |  |
| $\mathcal{F}_{L}=0.67(10)$ | $\mathcal{F}_{+}=0.023(53)$ | D0 |
| 1011.6549 |  |  |

- Projected sensitivity for LHC

$$
\sigma\left(\mathcal{F}_{+}\right)= \pm 0.002 \quad \sigma\left(\mathcal{F}_{L}\right)= \pm 0.02
$$



## NP in $t W b$ : effects on $\mathcal{F}_{i}$

Most general parameterization of $t W b$ vertex. J. A. Aguilar-Saavedra 0811.3842


- Helicity surpression present also in anomalous contributions.
- This mandates analysis at NLO in QCD.

J. Drobnak, J. F. Kamenik, S. Fajfer
1010.2402


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- Indirect $b \rightarrow s \gamma$ constrains on $a_{L, R}, b_{L R, R L}$ stronger than present or projected precision of direct $\mathcal{F}_{i}$ measurements. B. Grzadkowski, M. Misiak 0802.1413
- One exception: $b_{L R}$


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|  | $\mathrm{SM}\left(\delta a_{L}\right)$ | $a_{R}$ | $b_{R L}$ |
| :---: | :---: | :---: | :---: |
| $\mathcal{F}_{+}^{\mathrm{NLO}} / 10^{-3}$ | 1.32 | 1.34 | 1.34 |

- Presence of NP can not significantly affect $\mathcal{F}_{+}$ value!



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- One exception: $b_{L R}$
- CDF measurement of $\mathcal{F}_{L}$ puts bounds on $b_{L R}$ that are competitive with indirect $b \rightarrow s \gamma$ constraints.

$$
\begin{aligned}
& b_{L R}<0.09,95 \% \text { C.L. from } \mathcal{F}_{+} \\
& b_{L R}<0.16,95 \% \text { C.L. from } b \rightarrow s \gamma
\end{aligned}
$$



$$
B_{d, s}-\bar{B}_{d, s} \boldsymbol{m i x i n g}
$$

$\rightarrow$ Tevatron experiments quantifying $B_{s}$ sector.
Some indications of NP

$$
B_{d, s}-\bar{B}_{d, s} \text { mixing }
$$

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## Some indications of NP

- $\Delta \Gamma_{s}$ vs. $\phi_{s}^{J / \psi \phi}$.

D0
CDF
Note 6093-CONF
Public Note 10206

## $B_{d, s}-\bar{B}_{d, s}$ mixing

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D0
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Public Note 10206

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D0
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Note 6093-CONF Public Note 10206

- Dimuon charge asymmetry.

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$>\Delta \Gamma_{s}$ vs. $\phi_{s}^{J / \psi \phi}$.
D0
CDF
Note 6093-CONF Public Note 10206

- Dimuon charge asymmetry.
- Tension between $\sin 2 \beta$ and
$\operatorname{Br}\left(B \rightarrow \tau \nu_{\tau}\right)$.
A. Lenz, U. Nierste and CKMfitter group
1008.1593

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- Could NP be hiding in $B_{d, s}-\bar{B}_{d, s}$ mixing?

$$
M_{12}^{(d, s)}=M_{12}^{(d, s) \mathrm{SM}} \Delta_{d, s}
$$

- Analyzed and found consistancy with present data. $\Delta_{d, s}=1$ disfavored!
Z. Ligeti, M. Papucci, G. Perez, J. Zupan 1006.0432
A. Lenz, U. Nierste and CKMfitter group
1008.1593


## NP in $t W b: B_{d, s}-\bar{B}_{d, s}$ mixing

- Anomalous $t W b$ can cause $\Delta_{d, s} \neq 1$ !
- Effective vertex notation sufficient for setting direct constraints from $t \rightarrow W b$ decays.
- For indirect constraints we take a step further: effective theory, described by the Lagrangian

$$
\mathcal{L}=\mathcal{L}_{\mathrm{SM}}+\frac{1}{\Lambda^{2}} \sum_{i} C_{i} \mathcal{Q}_{i}+\text { h.c. }+\mathcal{O}\left(1 / \Lambda^{3}\right)
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$$

- Restrictions:
- Dim. 6 operators, invariant under SM gauge group, involving charged quark currents with $W$.
- Minimal Flavor Violation.
- Rid tree level FCNCs and flavor universal interactions affecting $G_{F}$.


## NP in $t W b: B_{d, s}-\bar{B}_{d, s}$ mixing

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Simplest linear MFV

$$
\begin{aligned}
\mathcal{Q}_{R R} & =V_{t b}\left[\bar{t}_{R} \gamma^{\mu} b_{R}\right]\left(\phi_{u}^{\dagger} \mathrm{i} D_{\mu} \phi_{d}\right) \\
\mathcal{Q}_{L L} & =\left[\bar{Q}_{3}^{\prime} \tau^{a} \gamma^{\mu} Q_{3}^{\prime}\right]\left(\phi_{d}^{\dagger} \tau^{a} \mathrm{i} D_{\mu} \phi_{d}\right) \\
& -\left[\bar{Q}_{3}^{\prime} \gamma^{\mu} Q_{3}^{\prime}\right]\left(\phi_{d}^{\dagger} \mathrm{i} D_{\mu} \phi_{d}\right) \\
\mathcal{Q}_{L R t} & =\left[\bar{Q}_{3}^{\prime} \sigma^{\mu \nu} \tau^{a} t_{R}\right] \phi_{u} W_{\mu \nu}^{a}, \\
\mathcal{Q}_{L R b} & =\left[\bar{Q}_{3} \sigma^{\mu \nu} \tau^{a} b_{R}\right] \phi_{d} W_{\mu \nu}^{a}
\end{aligned}
$$

Same operator bases used in $b \rightarrow s \gamma$ decays

- Rotation to mass eigen-basis: $Q_{i}=\left(V_{k i}^{*} u_{L k}, b_{L i}\right), \bar{Q}_{3}^{\prime}=\bar{Q}_{i} V_{t i}^{*}$.


## NP in $t W b: B_{d, s}-\bar{B}_{d, s}$ mixing

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- $\mathcal{Q}_{L L}$ and $\mathcal{Q}_{L R t}$ modify also $t W d$ and $t W s$ couplings


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Simplest linear MFV

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\mathcal{Q}_{L L}=\left[\bar{Q}_{3}^{\prime} \tau^{a} \gamma^{\mu} Q_{3}^{\prime}\right]\left(\phi_{d}^{\dagger} \tau^{a} \mathrm{i} D_{\mu} \phi_{d}\right)
$$

$$
-\left[\bar{Q}_{3}^{\prime} \gamma^{\mu} Q_{3}^{\prime}\right]\left(\phi_{d}^{\dagger} \mathrm{i} D_{\mu} \phi_{d}\right)
$$

$$
\mathcal{Q L R Q}^{L}=\left[\bar{Q}_{3}^{\prime} \sigma^{\mu \nu} \tau^{a} t_{R}\right] \phi_{u} W_{\mu \nu}^{a}
$$

$$
\left(\mathcal{Q}_{L R b}\right)=\left[\bar{Q}_{3} \sigma^{\mu \nu} \tau^{a} b_{R}\right] \phi_{d} W_{\mu \nu}^{a}
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- $\mathcal{Q}_{L L}^{\prime}$ and $\mathcal{Q}_{L R b}$ modify also $u W b$ and $c W b$ couplings


## Anomalous $t W b$ couplings and $M_{12}$



- The set of our seven dim-six operators contribute to $\Delta_{d, s}$
J. Drobnak, J. F. Kamenik, S. Fajfer 1102.4347

$$
\begin{aligned}
\Delta_{d, s} & =1-2.57 \kappa_{L L}+2.00 \kappa_{L L}^{\prime}-1.29 \kappa_{L L}^{\prime \prime}-1.54 \kappa_{L R t} \\
& -0.77 \kappa_{L R t}^{\prime}+\left\{4.48_{d}, 4.46_{s}\right\} \kappa_{R R}^{2}+\left\{4.15_{d}, 4.13_{s}\right\} \kappa_{L R b}^{2}
\end{aligned}
$$

- Analyze one operator at the time


## Anomalous $t W b$ couplings and $M_{12}$



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\end{aligned}
$$

- Analyze one operator at the time

1) $\kappa_{L L}=\frac{\operatorname{Re}\left[C_{L L}\right]}{\Lambda^{2} \sqrt{2} G_{F}}$ and $\kappa_{L R t}=\frac{\operatorname{Re}\left[C_{L R t}\right]}{\Lambda^{2} G_{F}}$ can not contribute new CPV phases. New bounds obtained

$$
\begin{aligned}
-0.082<\kappa_{L L}<0.078, & \text { at } 95 \% \text { C.L. }, \\
-0.14 & <\kappa_{L R t}<0.13,
\end{aligned} \text { at } 95 \% \text { C.L. } . ~ \$
$$



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\end{aligned}
$$

- Analyze one operator at the time

2) $\kappa_{R R}=\frac{C_{R R}}{\Lambda^{2} 2 \sqrt{2} G_{F}}$ and $\kappa_{L R b}=\frac{C_{L R b}}{\Lambda^{2} G_{F}}$ severely constrained by $b \rightarrow s \gamma$. Contribute to mixing only upon two insertions. No considerable effect on $\Delta_{d, s}$.

## Anomalous $t W b$ couplings and $M_{12}$



- The set of our seven dim-six operators contribute to $\Delta_{d, s}$

- Analyze one operator at the time

3) $\kappa_{L L}^{\prime(\prime \prime)}=\frac{C_{L L}^{\prime(\prime \prime)}}{\Lambda^{2} \sqrt{2} G_{F}}$ and $\kappa_{L R t}^{\prime}=\frac{C_{L R t}^{\prime}}{\Lambda^{2} G_{F}}$ not overly constrained by $b \rightarrow s \gamma$.

|  | Re | Im |
| :---: | :---: | :---: |
| $\kappa_{L L}^{\prime}$ | $-0.062_{-0.030}^{+0.063}$ | $-0.110_{-0.024}^{+0.029}$ |
| $\kappa_{L L}^{\prime \prime}$ | $0.097_{-0.048}^{+0.098}$ | $0.180_{-0.047}^{+0.037}$ |
| $\kappa_{L R t}^{\prime}$ | $0.160_{-0.160}^{+0.079}$ | $0.290_{-0.074}^{+0.062}$ |

Central fitted values and $1 \sigma$ intervals

- Up to $30 \%$ change in $\mathcal{F}_{+}$
- Up to $15 \%$ change in $\mathcal{F}_{L}$



## Conclusions

Helicity fractions can give information about $t W b$ coupling

- Possible measured $\mathcal{F}_{+} \gg 0.1 \%$ can not be explained by a simple effective vertex.
- Latest measurements of $\mathcal{F}_{L}$ give direct bounds on anomalous dipole couplings competitive with indirect bounds from $b \rightarrow s \gamma$ (MFV).


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- Anomalous top coupling affect $B-\bar{B}$ mixing.
- For MFV models with small bottom Yukawa effects, the bounds are competitive (in some cases improved) compared to $b \rightarrow s \gamma$.
- MVF models with large bottom Yukawa effects could accommodate the latest global fits (Complex Wilson coefficients).


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- Anomalous top coupling affect $B-\bar{B}$ mixing.
- For MFV models with small bottom Yukawa effects, the bounds are competitive (in some cases improved) compared to $b \rightarrow s \gamma$.
- MVF models with large bottom Yukawa effects could accommodate the latest global fits (Complex Wilson coefficients).
-Favored non-zero dipole Wilson coefficient affects the helicity fractions!
- In addition other observables "beyond helicity fractions" might be affected
J. A. Aguilar-Saavedra, J. Bernabeu
1005.5382


## Extra slides: MFV framework

- Lagrangian formally invariant under the SM flavor group
$\mathcal{G}^{\mathrm{SM}}=U(3)_{Q} \times U(3)_{u} \times U(3)_{d}$
- Only $\mathcal{G}^{\text {SM }}$ symmetry breaking spurionic fields in the theory are the up and down quark Yukawa matrices $Y_{u, d}$, formally transforming as $(3, \overline{3}, 1)$ and $(3,1, \overline{3})$ respectively.
- Most general $\mathcal{G}^{\mathrm{SM}}$ invariant quark bilinear flavor structures

$$
\bar{u} Y_{u}^{\dagger} \mathcal{A}_{u d} Y_{d} d, \quad \bar{Q} \mathcal{A}_{Q Q} Q, \quad \bar{Q} \mathcal{A}_{Q u} Y_{u} u, \quad \bar{Q} \mathcal{A}_{Q d} Y_{d} d
$$

where $\mathcal{A}_{x y}$ are arbitrary polynomials of $Y_{u} Y_{u}^{\dagger}$ and/or $Y_{d} Y_{d}^{\dagger}$,

- $\left\langle Y_{d}\right\rangle=\operatorname{diag}\left(m_{d}, m_{s}, m_{b}\right) / v_{d}$ and $\left\langle Y_{u}\right\rangle=V^{\dagger} \operatorname{diag}\left(m_{u}, m_{c}, m_{t}\right) / v_{u}$


## Extra slides: MFV framework

## Linear MFV

- Simplest case of linear MFV where within $\left\langle\mathcal{A}_{x y}\right\rangle$ higher powers of $\left\langle Y_{d} Y_{d}^{\dagger}\right\rangle \simeq \operatorname{diag}\left(0,0, m_{b}^{2} / v_{d}^{2}\right)$ can be neglected. Neglecting also contributions suppressed by first and second generation quark masses, the only relevant flavor contributions of the arbitrary $\mathcal{A}_{x y}$ structures

$$
\begin{gathered}
\bar{t}_{R} V_{t b} b_{R}, \\
\bar{Q}_{i} V_{t i}^{*} t_{R},
\end{gathered}
$$

$\bar{Q}_{i} Q_{i}$,
$\bar{Q}_{3} b_{R}$,

$$
\begin{gathered}
\bar{Q}_{i} V_{t i}^{*} V_{t j} Q_{j}, \\
\bar{Q}_{i} V_{t i}^{*} V_{t b} b_{R},
\end{gathered}
$$

## Extra slides: MFV framework

## Non-Linear MFV

- Generalization to MFV scenarios where large bottom Yukawa effects can be important.
- Higher powers of $\left\langle Y_{d} Y_{d}^{\dagger}\right\rangle$ within $\mathcal{A}_{x y}$ effectively project to the third generation in the down sector yielding the following additional flavor structures

$$
\bar{Q}_{3} Q_{3}, \quad \bar{Q}_{3} V_{t b}^{*} V_{t j} Q_{j}, \quad \bar{Q}_{3} V_{t b}^{*} t_{R}
$$

