Neutrino Physics

Boris Kayser
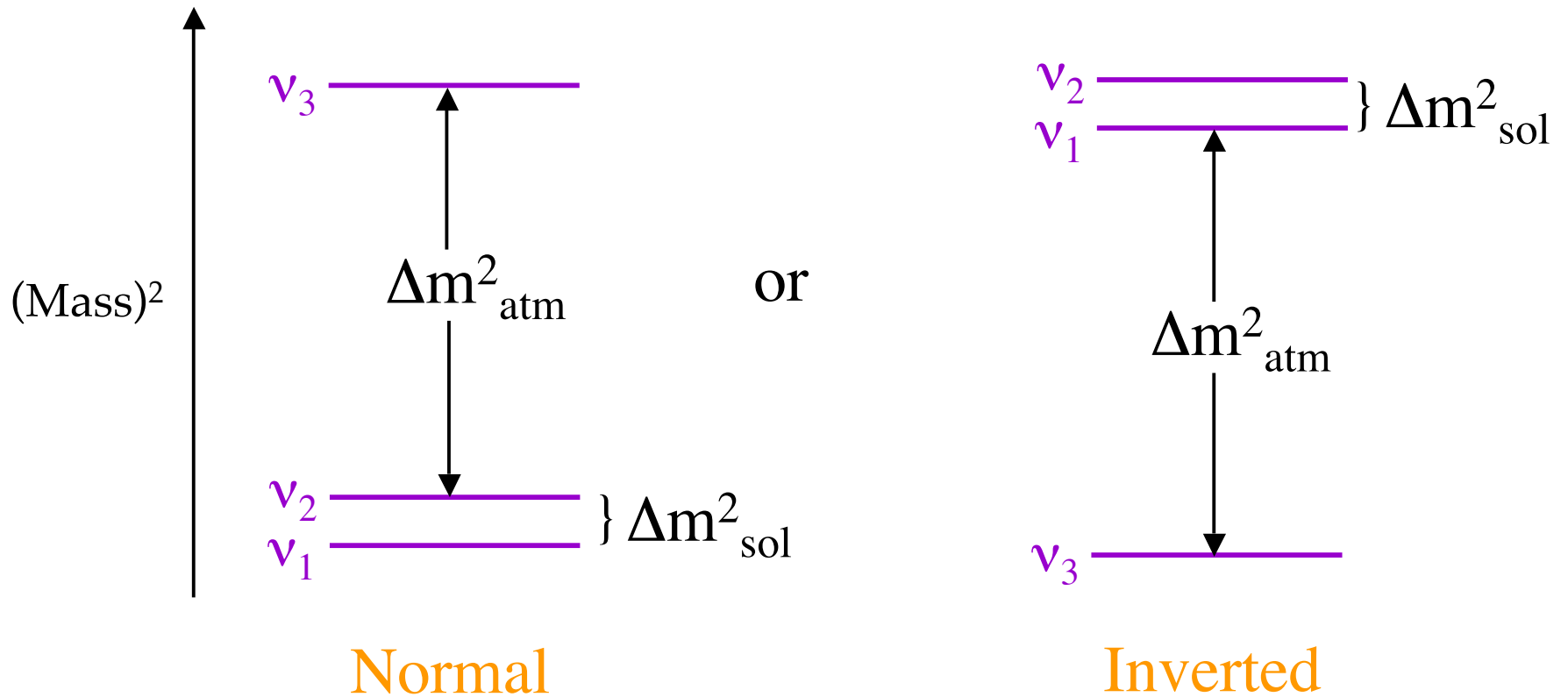**ESHEP**
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Printed Slides # 2

What We
Have Learned
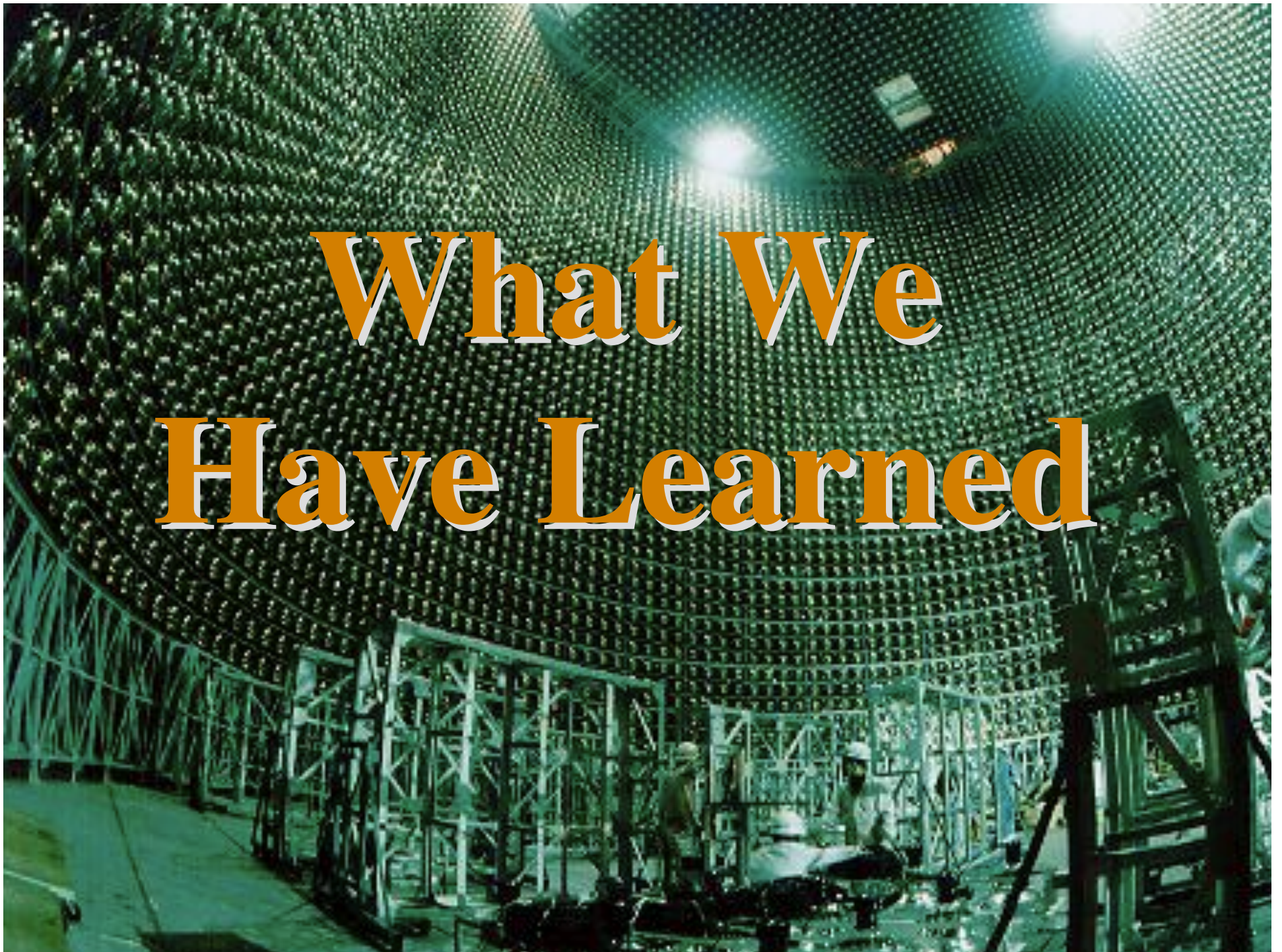
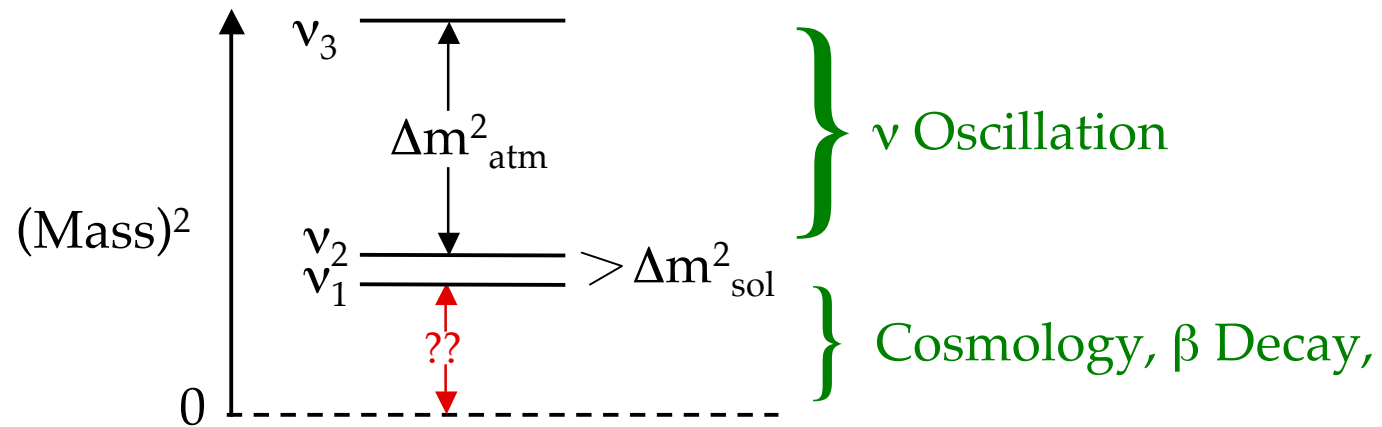# The (Mass)² Spectrum

$$\Delta m^2_{sol} \cong 7.5 \times 10^{-5} \text{ eV}^2, \quad \Delta m^2_{atm} \cong 2.3 \times 10^{-3} \text{ eV}^2$$

The Absolute Scale of Neutrino Mass

How far above zero is the whole pattern?

Oscillation Data $\Rightarrow \sqrt{\Delta m^2_{atm}} < $ Mass[Heaviest ν_i]

The Upper Bound From Cosmology

Neutrino mass affects large scale structure.

Cosmological Data + Cosmological Assumptions $\Rightarrow$

$$\Sigma\, m_i < (0.17 - 1.0) \text{ eV} .$$

Mass(ν_i) $\longrightarrow$

$\left(\begin{array}{c} \text{Seljak, Slosar, McDonald} \\ \text{Hannestad; Pastor} \end{array} \right)$

If there are only 3 neutrinos,

$$0.04 \text{ eV} \lesssim \text{Mass[Heaviest } \nu_i] < (0.07 - 0.4) \text{ eV}$$

$\sqrt{\Delta m^2_{atm}}$

Cosmology $\longrightarrow$

The Upper Bound From Tritium

Cosmology is wonderful, but there are known loopholes in its argument concerning neutrino mass.

The absolute neutrino mass can in principle also be measured by the kinematics of β decay.

Tritium decay: $\quad ^3H \rightarrow {}^3He + e^- + \overline{\nu_i}$; $i = 1, 2,$ or 3
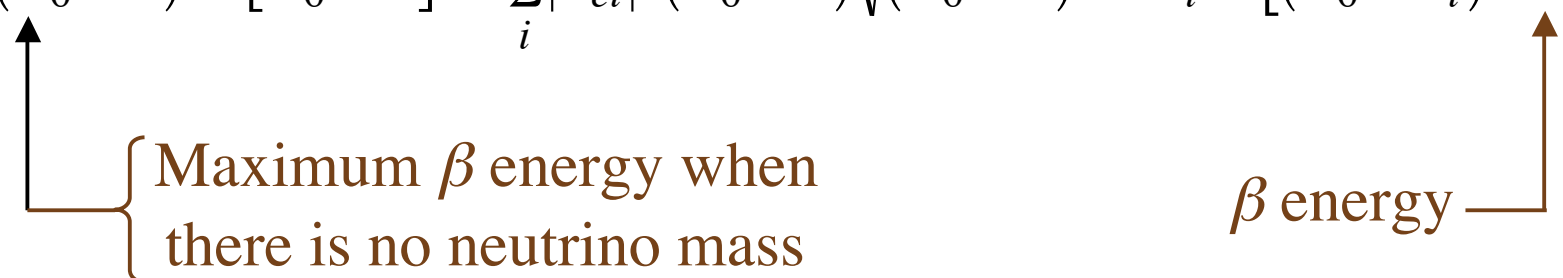
$$BR\left({}^3H \rightarrow {}^3He + e^- + \overline{\nu_i} \right) \propto |U_{ei}|^2$$

In $^3H \rightarrow {}^3He + e^- + \overline{\nu_i}$, the bigger m_i is, the smaller the maximum electron energy is.

There are 3 separate thresholds in the β energy spectrum.

The β energy spectrum is modified according to —

$$(E_0 - E)^2 \Theta[E_0 - E] \Rightarrow \sum_i |U_{ei}|^2 (E_0 - E)\sqrt{(E_0 - E)^2 - m_i^2}\, \Theta\big[(E_0 - m_i) - E\big]$$

Maximum β energy when there is no neutrino mass

β energy

Present experimental energy resolution is insufficient to separate the thresholds.

Measurements of the spectrum bound the average neutrino mass —

$$\langle m_\beta \rangle = \sqrt{\sum_i |U_{ei}|^2 m_i^2}$$

Presently: $\langle m_\beta \rangle < 2\ \text{eV}$

Mainz & Troitzk

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Leptonic Mixing

This has the consequence that —

Mass eigenstate

Flavor eigenstate

$$|\nu_i> = \sum_\alpha U_{\alpha i} |\nu_\alpha> \ .$$

e, μ, or τ

Leptonic Mixing Matrix

Flavor-α fraction of $\nu_i = |U_{\alpha i}|^2$.

When a ν_i interacts and produces a charged lepton, the probability that this charged lepton will be of flavor α is $|U_{\alpha i}|^2$.

The spectrum, showing its approximate flavor content, is

$\sin^2\theta_{13}$

ν_3

Δm^2_{atm}

ν_2
ν_1
$\left.\right\}\Delta m^2_{sol}$

or

(Mass)^2

ν_2
ν_1
$\left.\right\}\Delta m^2_{sol}$

Δm^2_{atm}

ν_3

$\sin^2\theta_{13}$

Normal   **Inverted**

$\nu_e\,[\,|U_{ei}|^2]$ $\nu_\mu[\,|U_{\mu i}|^2]$ $\nu_\tau\,[\,|U_{\tau i}|^2]$

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Bounded by reactor exps. with L ~ 1 km

From max. atm. mixing, $\nu_3 \cong \dfrac{\nu_\mu + \nu_\tau}{\sqrt{2}}$

ν_3

(Mass)²

Δm^2_{atm} ← $\begin{cases} \text{From } \nu_\mu(\text{Up}) \text{ oscillate} \\ \quad \text{but } \nu_\mu(\text{Down}) \text{ don't} \end{cases}$

$\begin{cases} \text{In LMA–MSW, } P_{sol}(\nu_e \to \nu_e) \\ = \nu_e \text{ fraction of } \nu_2 \end{cases}$

ν_2

ν_1

$\Big\} \Delta m^2_{sol}$ ← From distortion of $\overline{\nu}_e$(reactor) and ν_e(solar) spectra

$\begin{cases} \text{From max. atm. mixing, } \nu_1 + \nu_2 \\ \text{includes } (\nu_\mu - \nu_\tau)/\sqrt{2} \end{cases}$

$\nu_e \, [\,|U_{ei}|^2]$ $\nu_\mu \, [\,|U_{\mu i}|^2]$ $\nu_\tau \, [\,|U_{\tau i}|^2]$

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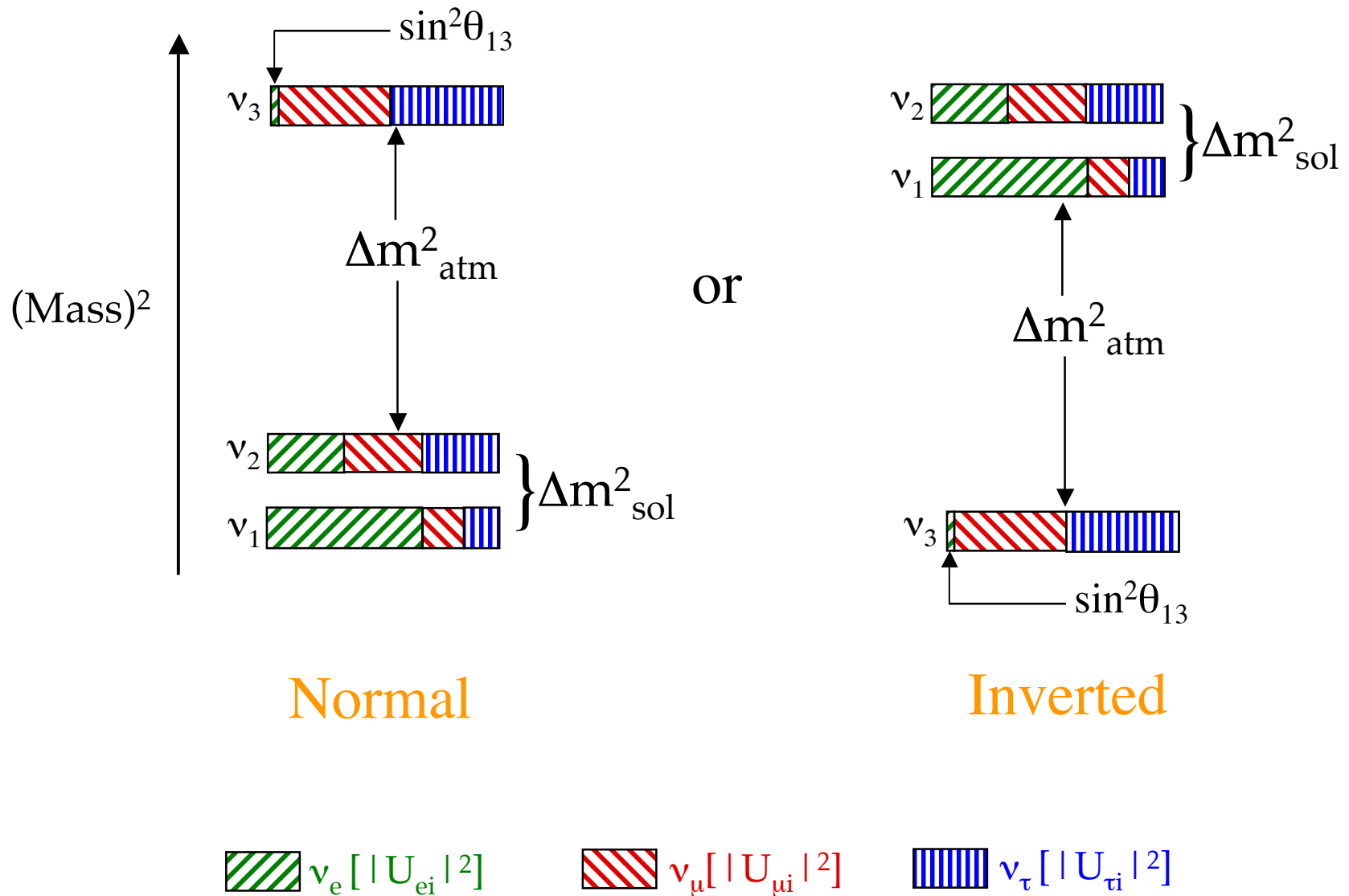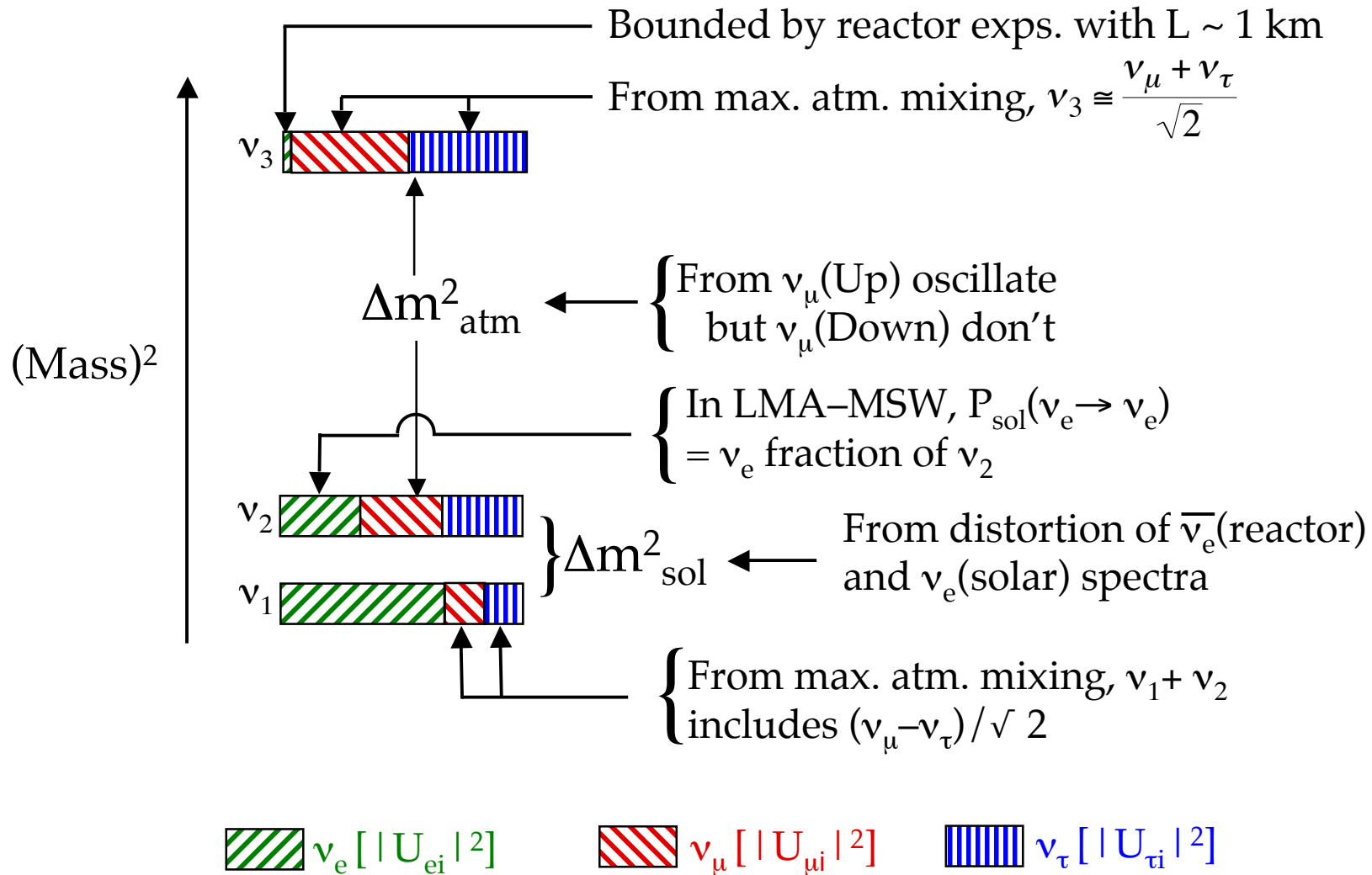
The Mixing Matrix

Atmospheric   Cross-Mixing   Solar

$$U = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \times \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{bmatrix} \times \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\times \begin{bmatrix} e^{i\alpha_1/2} & 0 & 0 \\ 0 & e^{i\alpha_2/2} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Hints??

$c_{ij} \equiv \cos\theta_{ij}$
$s_{ij} \equiv \sin\theta_{ij}$

Majorana C̸P̸
phases

$\theta_{12} \approx \theta_{sol} \approx 34°, \quad \theta_{23} \approx \theta_{atm} \approx 39\text{-}51°, \quad \theta_{13} \lesssim 12°$

δ would lead to $P(\overline{\nu}_\alpha \to \overline{\nu}_\beta) \neq P(\nu_\alpha \to \nu_\beta)$. C̸P̸

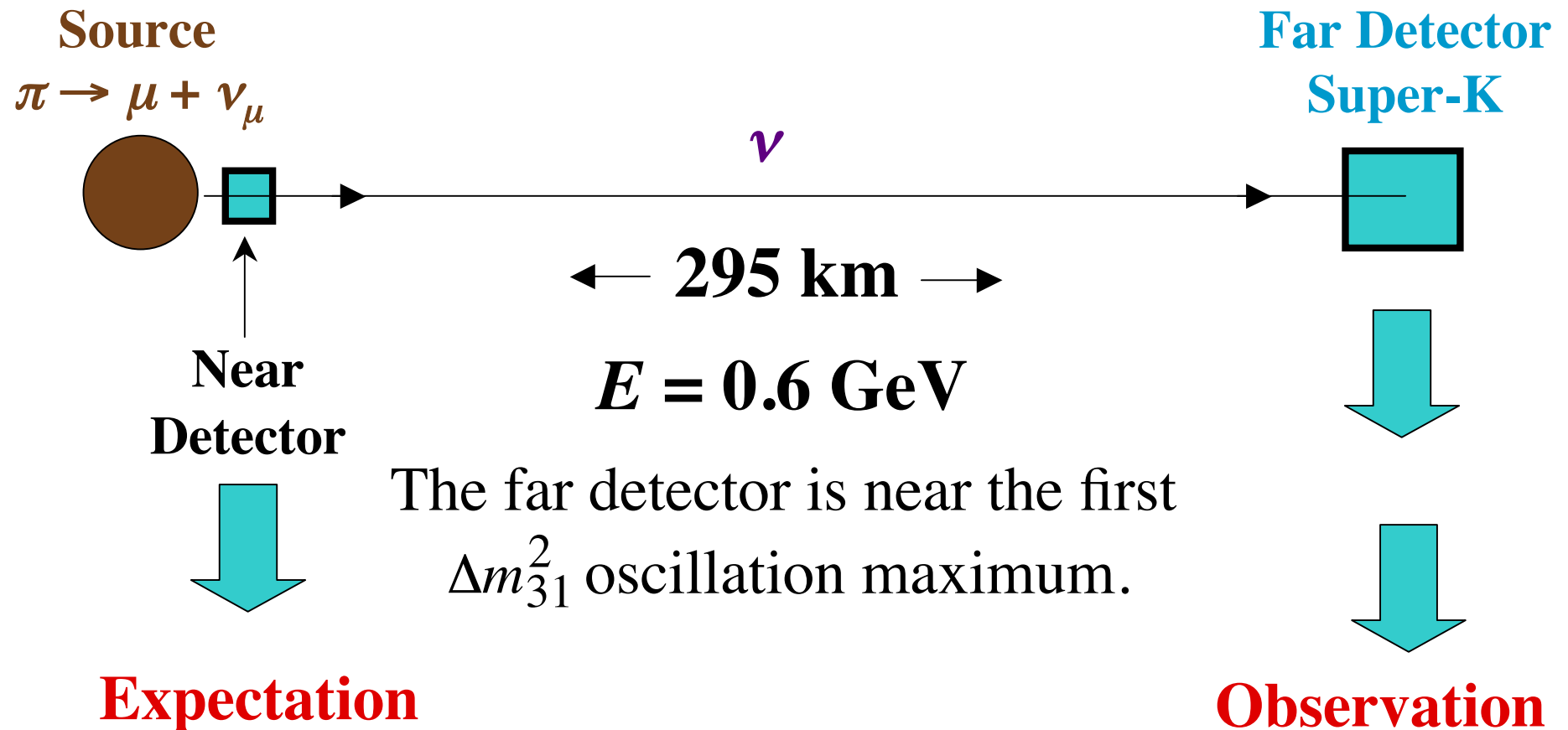But note the crucial role of $s_{13} \equiv \sin\theta_{13}$.

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Recent Evidence For Non-Zero θ_{13}

In an experiment where L/E is too small for the small splitting $\Delta m_{21}^2 \equiv m_2^2 - m_1^2$ to be seen,
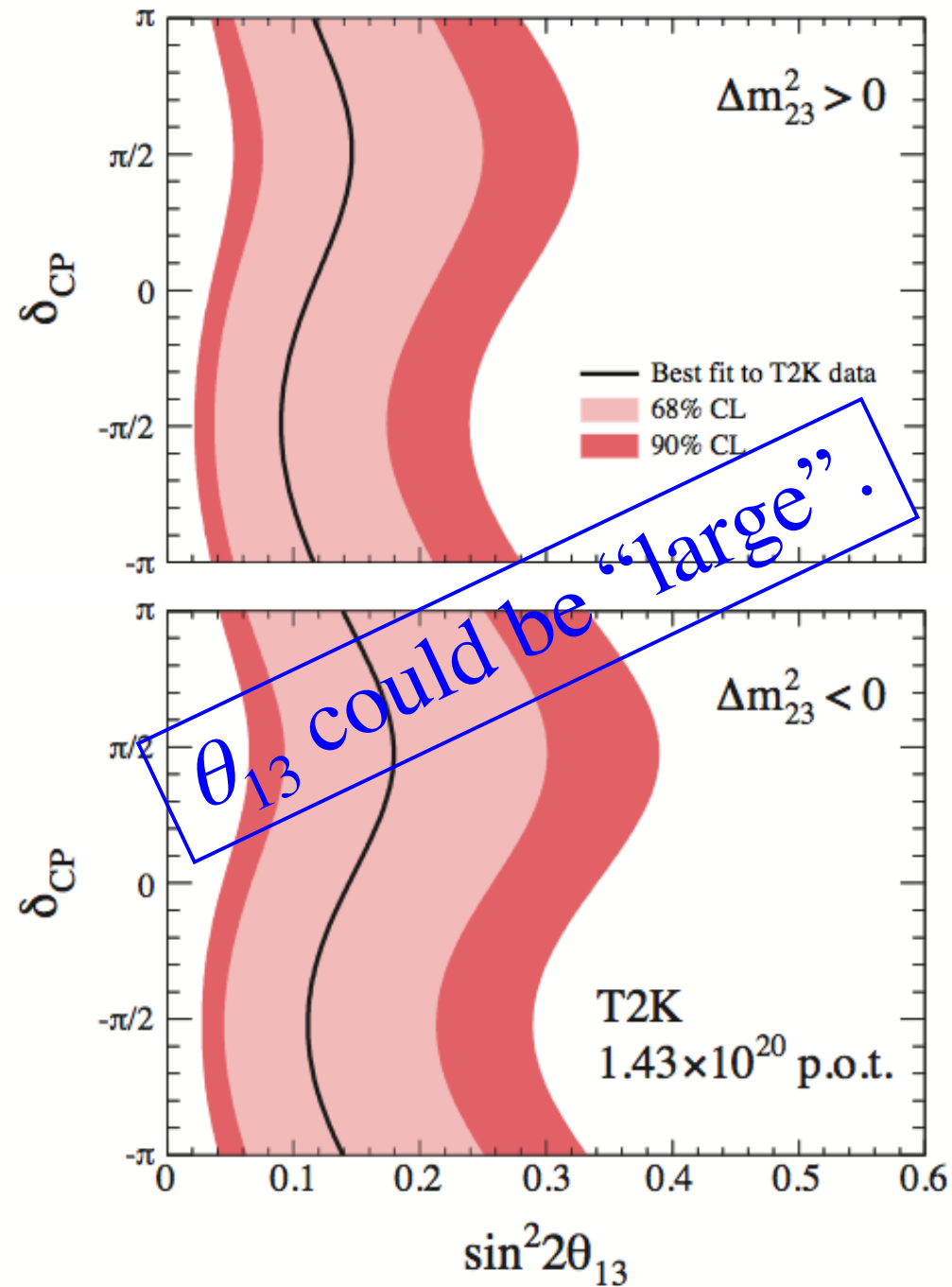
$$P\left(\nu_\mu \to \nu_e\right) \cong 4\left|U_{\mu 3}U_{e 3}\right|^2 \sin^2\left(\Delta m_{31}^2 \frac{L}{4E}\right)$$

$$= \boxed{\sin^2 2\theta_{13}}\, \sin^2 \theta_{23} \sin^2\left(\Delta m_{31}^2 \frac{L}{4E}\right)$$

T2K has looked for $\nu_\mu \to \nu_e$ in a long-baseline experiment:

The T2K experiment (Designed to seek $\nu_\mu \rightarrow \nu_e$)

Source

$\pi \rightarrow \mu + \nu_\mu$

ν

Far Detector
Super-K

$\longleftarrow$ **295 km** $\longrightarrow$

Near Detector

$E = 0.6$ **GeV**

The far detector is near the first Δm_{31}^2 oscillation maximum.

Expectation

Observation

T2K sees 6 ν_e candidate events in the far detector, whereas 1.5 are expected if $\theta_{13} = 0$.

$\Delta m^2_{23} > 0$

Best fit to T2K data
68% CL
90% CL

θ_{13} could be "large".

$\Delta m^2_{23} < 0$

T2K
1.43×10^{20} p.o.t.

δ_{CP}

$\sin^2 2\theta_{13}$

These take the Δm^2_{21} contributions and matter effects into account.

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MINOS, not designed to look for $\nu_\mu \rightarrow \nu_e$, sees
62 candidate events where 50 are expected if $\theta_{13} = 0$.

While not highly significant by itself,
this result is consistent with that from T2K.

There Is Nothing Special About θ_{13}

All mixing angles must be nonzero for ~~CP~~ in oscillation.

For example —

$$P(\bar{\nu}_\mu \to \bar{\nu}_e) - P(\nu_\mu \to \nu_e) = 2\cos\theta_{13}\sin 2\theta_{13}\sin 2\theta_{12}\sin 2\theta_{23}\sin\delta$$

$$\times \sin\left(\Delta m^2{}_{31}\frac{L}{4E}\right)\sin\left(\Delta m^2{}_{32}\frac{L}{4E}\right)\sin\left(\Delta m^2{}_{21}\frac{L}{4E}\right)$$

In the factored form of U, one can put
δ next to θ_{12} instead of θ_{13}.

The Majorana C̶P̶ Phases

The phase α_i is associated with
neutrino mass eigenstate ν_i:

$$U_{\alpha i} = U^0_{\alpha i} \exp(i\alpha_i/2) \text{ for all flavors } \alpha.$$

$$\text{Amp}(\nu_\alpha \rightarrow \nu_\beta) = \sum_i U_{\alpha i}^* \exp(- im_i^2 L/2E) \, U_{\beta i}$$

is insensitive to the Majorana phases α_i.

Only the phase δ can cause CP violation in
neutrino oscillation.

Looking to the Future

The Open Questions

- What is the absolute scale
of neutrino mass?

- Are neutrinos their own antiparticles?

- Are there *more* than 3 mass eigenstates?

- Are there "sterile" neutrinos?

- What are the neutrino magnetic
and electric dipole moments?

What is θ_{13}?
How close to maximal is θ_{23}?

- Is the spectrum like ▬▬ or ▬▬ ?

- Do neutrino interactions violate CP?
  Is $P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta) \neq P(\nu_\alpha \rightarrow \nu_\beta)$?

- What can neutrinos and the universe tell us about one another?

- Is CP violation involving neutrinos the key to understanding the matter – antimatter asymmetry of the universe?

- What physics is behind neutrino mass?

- What surprises are in store?
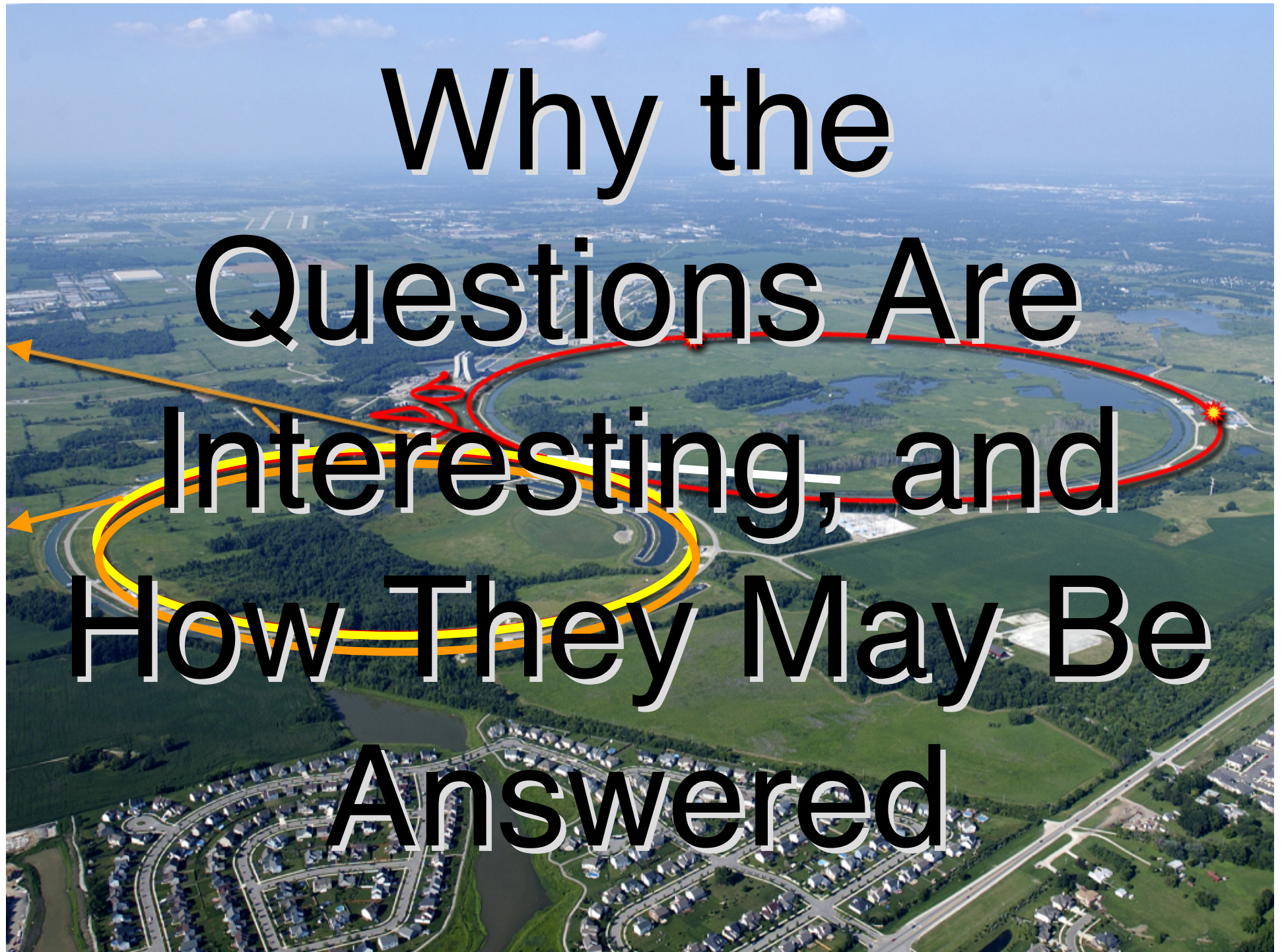
Why the Questions Are Interesting, and How They May Be Answered

Does $\bar{\nu} = \nu$?

What Is the Question?

For each *mass eigenstate* ν_i , and *given helicty* h, does —

- $\overline{\nu}_i(h) = \nu_i(h)$ (Majorana neutrinos)

or

- $\overline{\nu}_i(h) \neq \nu_i(h)$ (Dirac neutrinos) ?

Equivalently, do neutrinos have *Majorana masses*? If they do, then the mass eigenstates are *Majorana neutrinos*.

Majorana Masses

Their effect:

Majorana mass ↓

$\overline{\nu}$ ✕ ν or ν ✕ $\overline{\nu}$
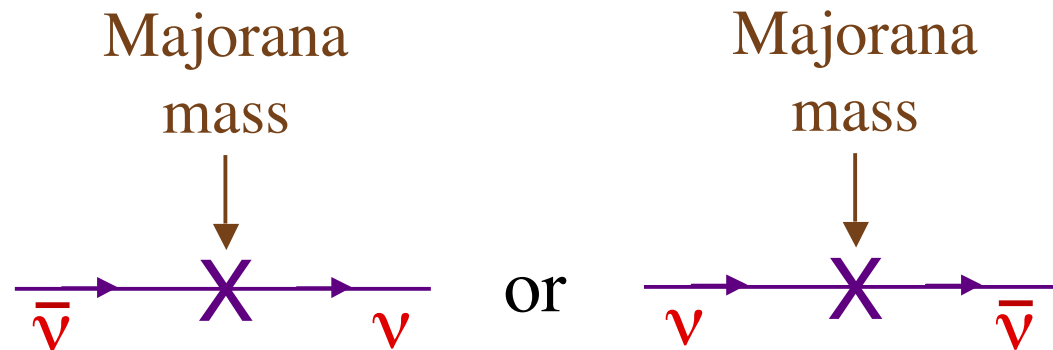
Majorana mass ↓

Majorana masses mix ν and $\overline{\nu}$, so they do not conserve the Lepton Number L that distinguishes leptons from antileptons:

$$L(\nu) = L(\ell^-) = -L(\overline{\nu}) = -L(\ell^+) = 1$$

A Majorana mass for any fermion f causes $f \leftrightarrow \bar{f}$.

Quark and *charged-lepton* Majorana masses
are forbidden by electric charge conservation.

Neutrino Majorana masses would make

the neutrinos *very* distinctive.

*Majorana neutrino masses have a different origin
than the quark and charged-lepton masses.*

In the SM, the top quark mass comes from —

Higgs field

Coupling constant

Top quark mass m_t

$$G_t H^0 \bar{t}_R t_L \Rightarrow G_t \langle H^0 \rangle_0 \bar{t}_R t_L$$

Vacuum expectation value

Such an operator does **not** mix quark and antiquark.

Its effect:

$\overset{(-)}{t}$ $\overset{(-)}{t}$

m_t

A Majorana mass term **does** mix neutrino and antineutrino.

A Majorana mass term must have a different origin than the quark and charged-lepton masses.

Why Majorana Masses ➡ Majorana Neutrinos

As a result of $K^0 \longleftrightarrow \overline{K^0}$ mixing, the neutral K mass eigenstates are —

$$K_{S,L} \cong (K^0 \pm \overline{K^0})/\sqrt{2} \; . \qquad \overline{K_{S,L}} = K_{S,L} \; .$$

Majorana masses induce $\nu \longleftrightarrow \overline{\nu}$ mixing.

As a result of $\nu \longleftrightarrow \overline{\nu}$ mixing, the neutrino mass eigenstate is —

$$\nu_i = \nu + \overline{\nu} \; . \qquad \overline{\nu}_i = \nu_i \; .$$

SM Interactions Of A Dirac Neutrino

We have 4 mass-degenerate states:

ν — makes ℓ^- Conserved L   +1

$\overline{\nu}$ — makes ℓ^+ –1

ν —

$\overline{\nu}$ —

These states, when Ultra Rel., do not interact.

$\left(\begin{array}{c}\text{The weak interaction}\\\text{is Left Handed.}\end{array}\right)$
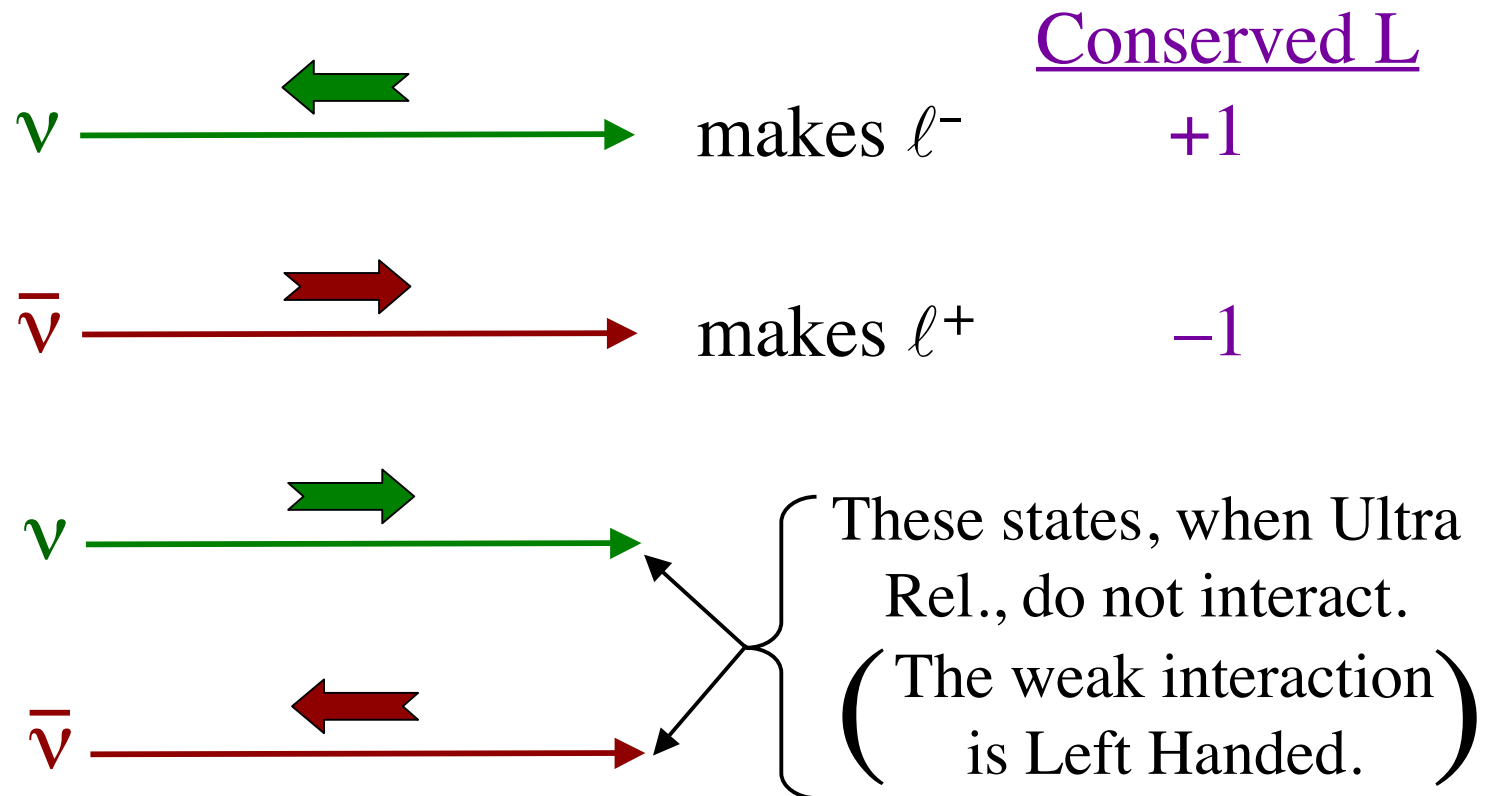
SM Interactions Of
A Majorana Neutrino

We have only 2 mass-degenerate states:

ν ———————→ makes ℓ^-
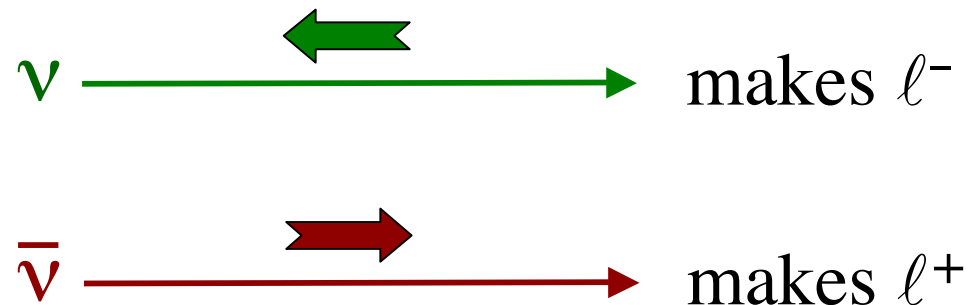
$\overline{\nu}$ ———————→ makes ℓ^+

The weak interactions violate *parity*.
(They can tell *Left* from *Right*.)

An incoming left-handed neutral lepton makes ℓ^-.

An incoming right-handed neutral lepton makes ℓ^+.

Can a Majorana Neutrino Have an Electric Charge *Distribution*?

$\mathcal{No!}$
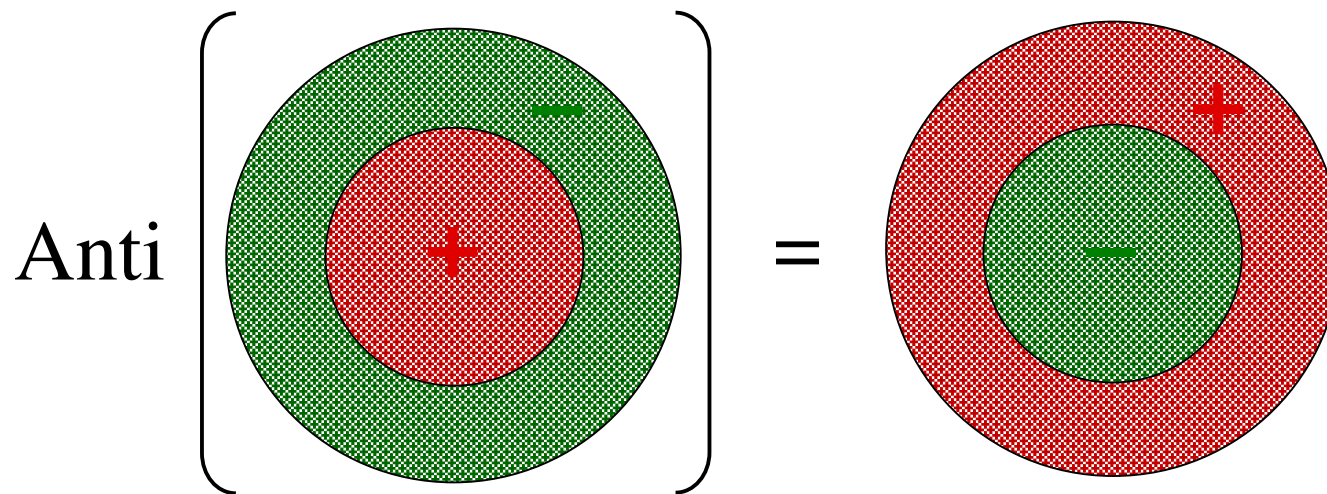
Anti $\left[\ \bigcirc\ \right]$ = $\bigcirc$

But for a Majorana neutrino —

Anti $(\nu) = \nu$

Majorana Masses Split Dirac Neutrinos

A Majorana mass term splits a Dirac neutrino into two Majorana neutrinos.
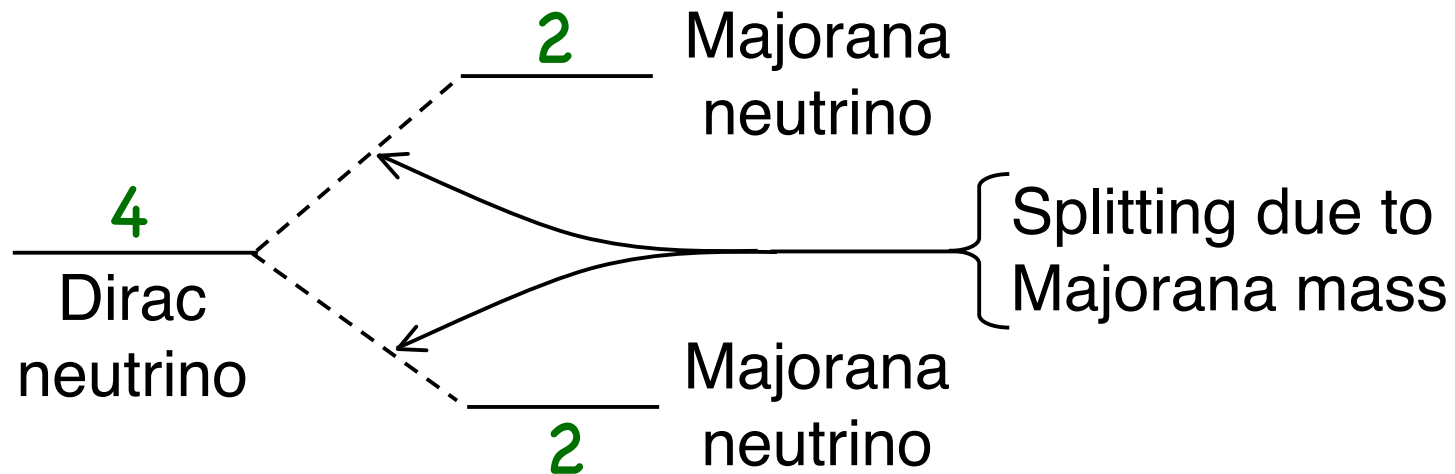
Why Most Theorists Expect Majorana Masses

The Standard Model (SM) is defined by the fields it contains, its symmetries (notably weak isospin invariance), and its renormalizability.

Leaving neutrino masses aside, anything allowed by the SM symmetries occurs in nature.

Majorana mass terms
are allowed by the SM symmetries.

Then quite likely *Majorana masses*
occur in nature too.

To Determine Whether Majorana Masses Occur in Nature

The Promising Approach — Seek

Neutrinoless Double Beta Decay $[0\nu\beta\beta]$

We are looking for a *small* Majorana neutrino mass. Thus, we will need *a lot* of parent nuclei (say, one ton of them).

Whatever diagrams cause $0\nu\beta\beta$, its observation
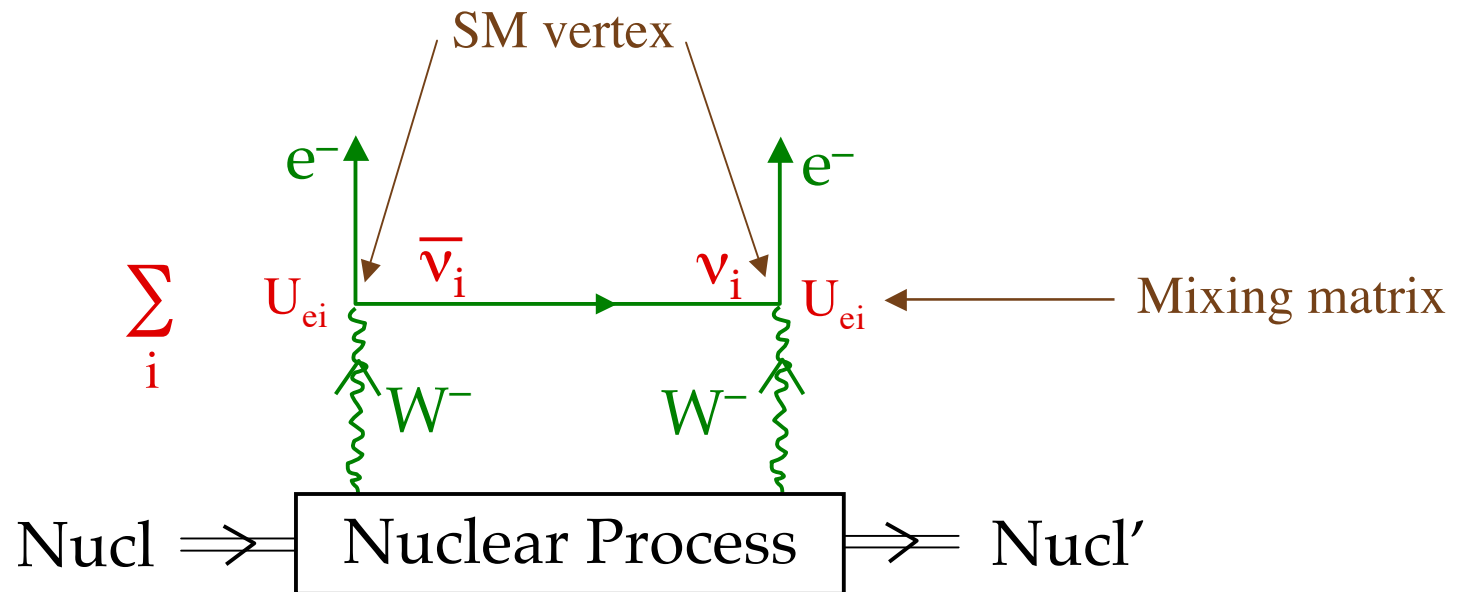would imply the existence of a Majorana mass term:

(Schechter and Valle)
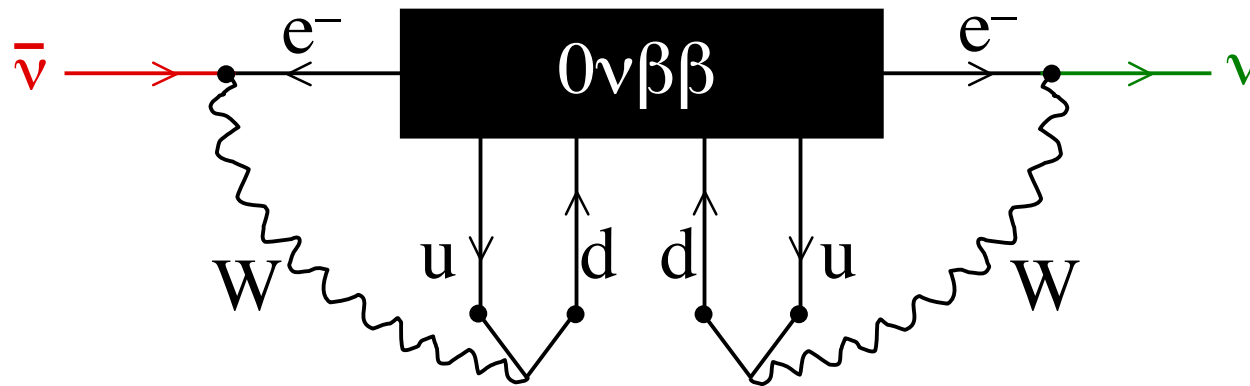
$\overline{\nu} \rightarrow \nu$: A (tiny) Majorana mass term

$\therefore 0\nu\beta\beta \implies \overline{\nu}_i = \nu_i$

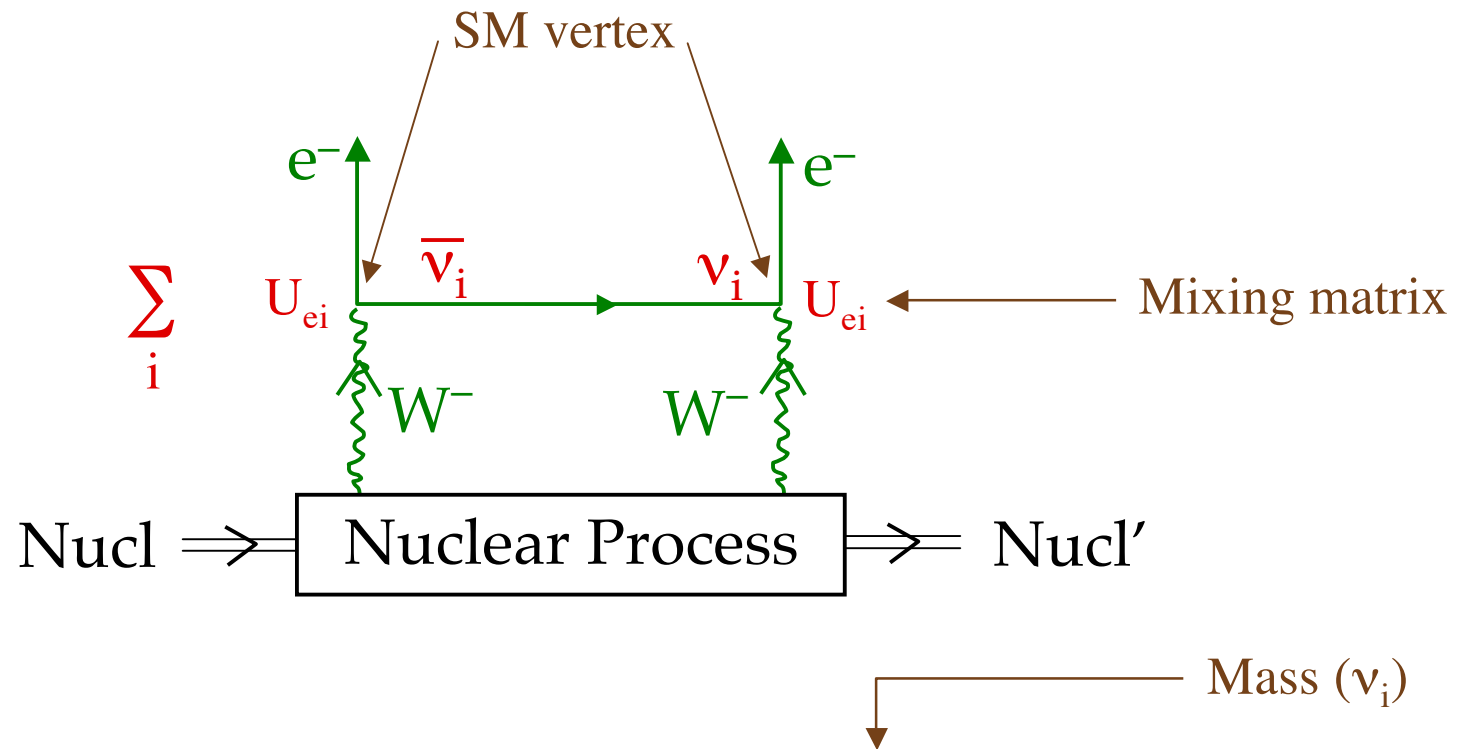# We anticipate that $0\nu\beta\beta$ is dominated by a diagram with Standard Model vertices:

But there could be other contributions to 0νββ,
which at the quark level is the process
dd → uuee.

An example from Supersymmetry:
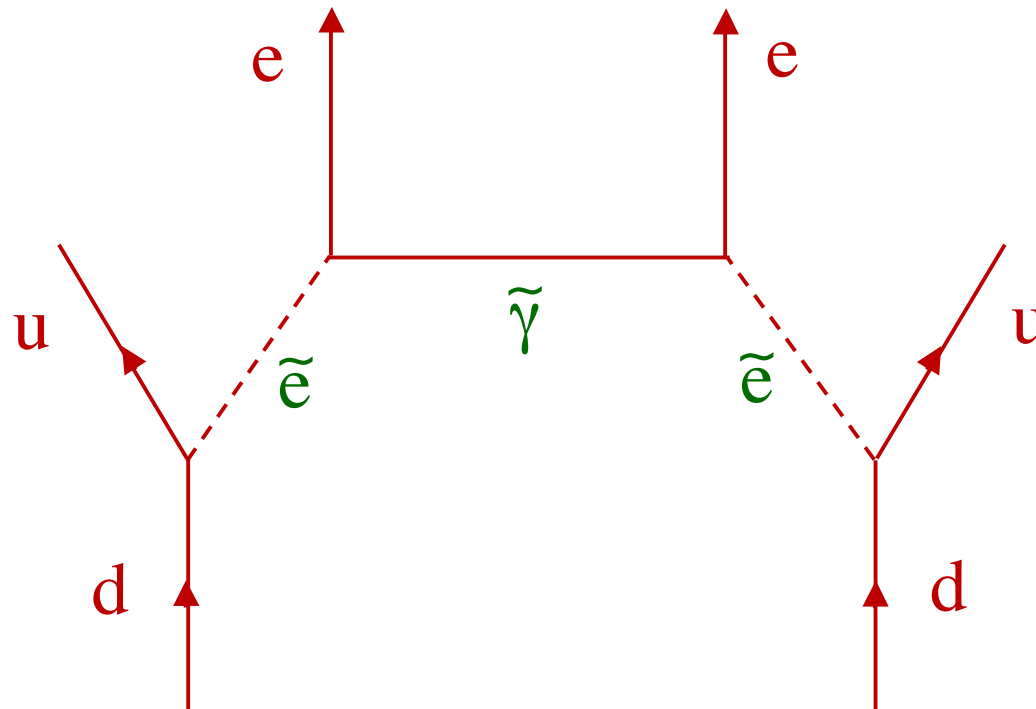
Assume the dominant mechanism is —

The $\overline{\nu}_i$ is emitted [RH + O{m_i/E}LH].

Thus, Amp [ν_i contribution] $\propto$ m_i

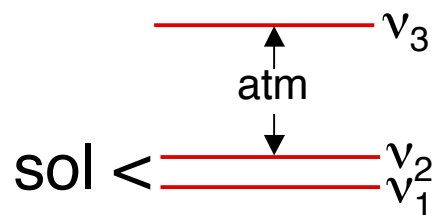$$\text{Amp}[0\nu\beta\beta] \propto \left| \sum m_i U_{ei}^2 \right| \equiv m_{\beta\beta}$$

How Large is $m_{\beta\beta}$?

How sensitive need an experiment be?

Note: $\Gamma = m_{\beta\beta}^2 \, |\text{Nuclear M.E.}|^2 \, \text{Phase Space}$
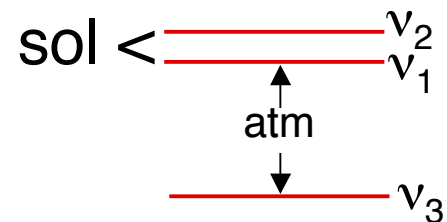
Suppose there are only 3 neutrino mass eigenstates. (More might help.)

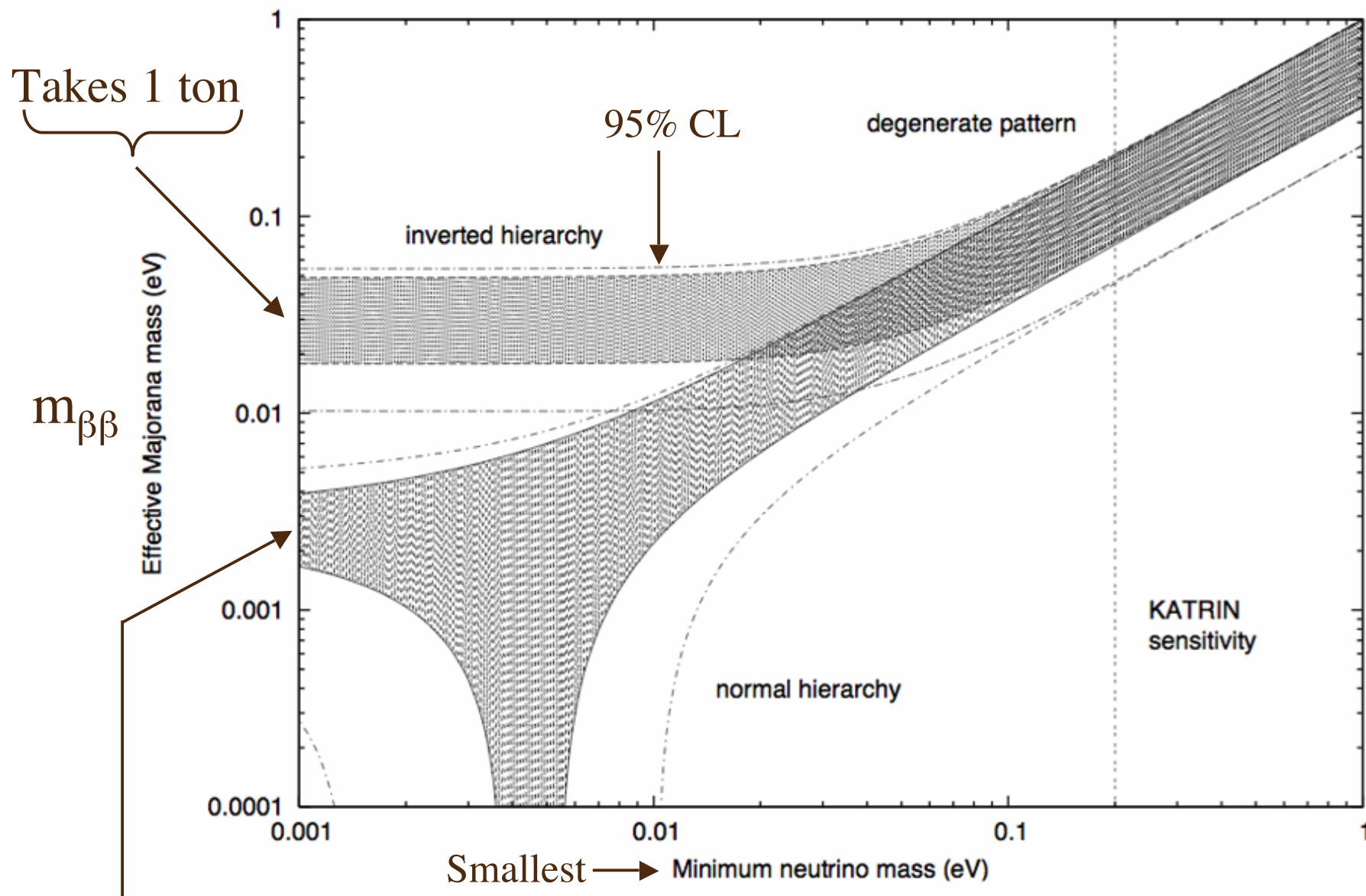Then the spectrum looks like —

Normal hierarchy   or   Inverted hierarchy

$m_{\beta\beta}$ *For Each Hierarchy*

There is no clear theoretical preference
for either hierarchy.

If the hierarchy is **inverted**—

then $0\nu\beta\beta$ searches with sensitivity
to $m_{\beta\beta} = 0.01$ eV have
a very good chance to see a signal.

*Sensitivity in this range is the target
for the next generation of experiments.*