

# Closing in on critical net-baryon fluctuations: cumulants up to 3<sup>rd</sup> order in Pb-Pb collisions with ALICE

(arXiv:2206.03343)



**Mesut Arslanok**

Yale University / CERN

- Why fluctuations?
- How to link experiment to theory
- Experimental challenges
- What did/will we learn?

CERN LHC Seminar, 21 June 2022, Geneva, Switzerland

Yale



Wright  
Laboratory



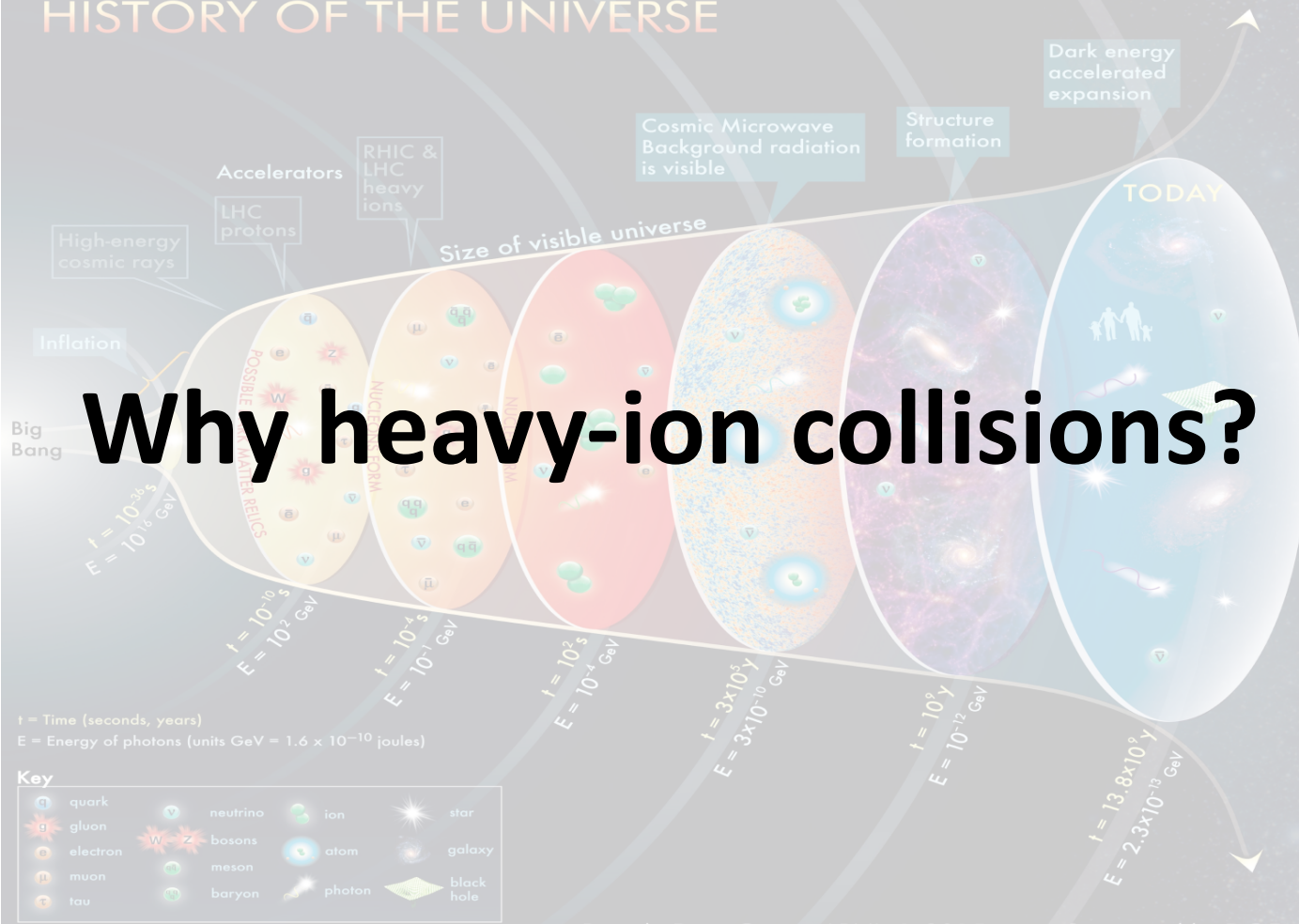
In part supported by

U.S. DEPARTMENT OF  
**ENERGY**

Office of  
Science



# HISTORY OF THE UNIVERSE



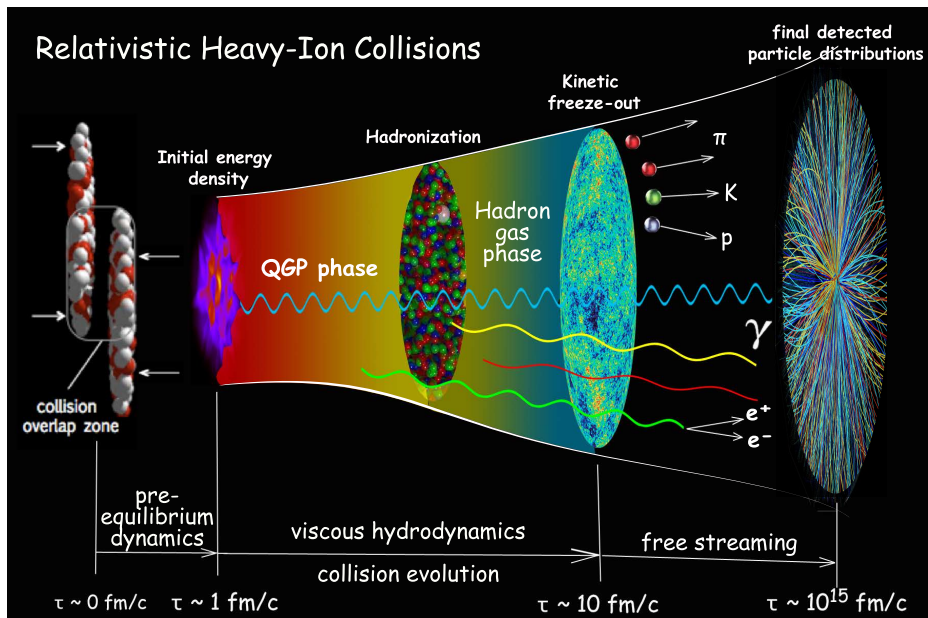
t = Time (seconds, years)  
 E = Energy of photons (units GeV =  $1.6 \times 10^{-10}$  joules)

The concept for the above figure originated in a 1986 paper by Michael Turner.

# Quark-gluon plasma (QGP)

A state of matter where the **quarks and gluons are the relevant degrees of freedom**, exist at few  $\mu\text{s}$  after the Big-Bang

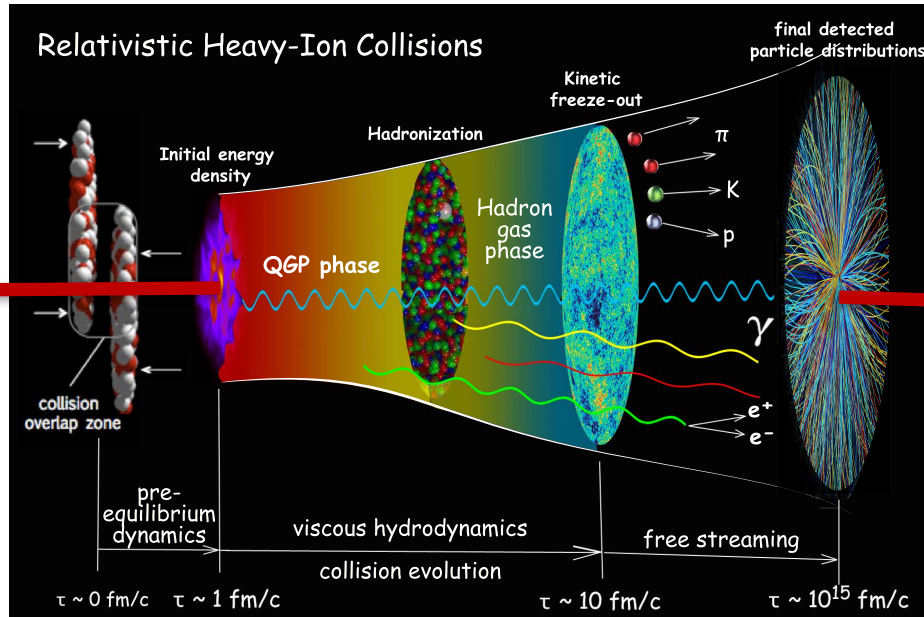
- ✓ **Chiral symmetry:**  $m_p \approx 937 \text{ MeV} \leftrightarrow 2m_u + m_d \approx 10 \text{ MeV}$
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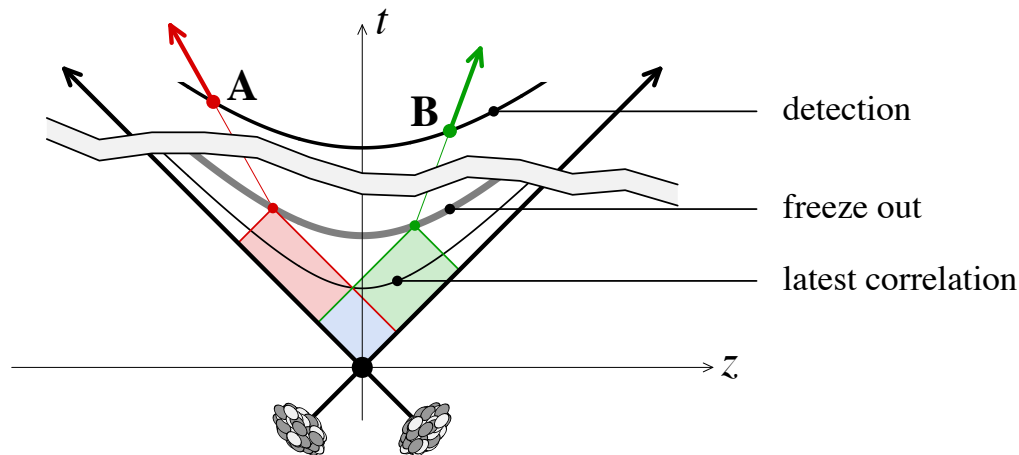
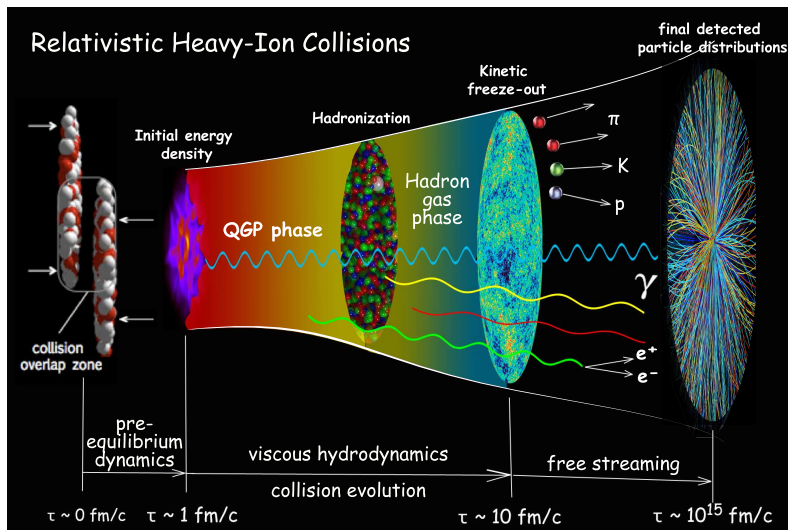


**“Psychoanalysis” of Matter**



# Quark-gluon plasma (QGP)

Dumitru, Gelis, McLerran, Venugopalan, Nucl. Phys. A810 (2008) 91



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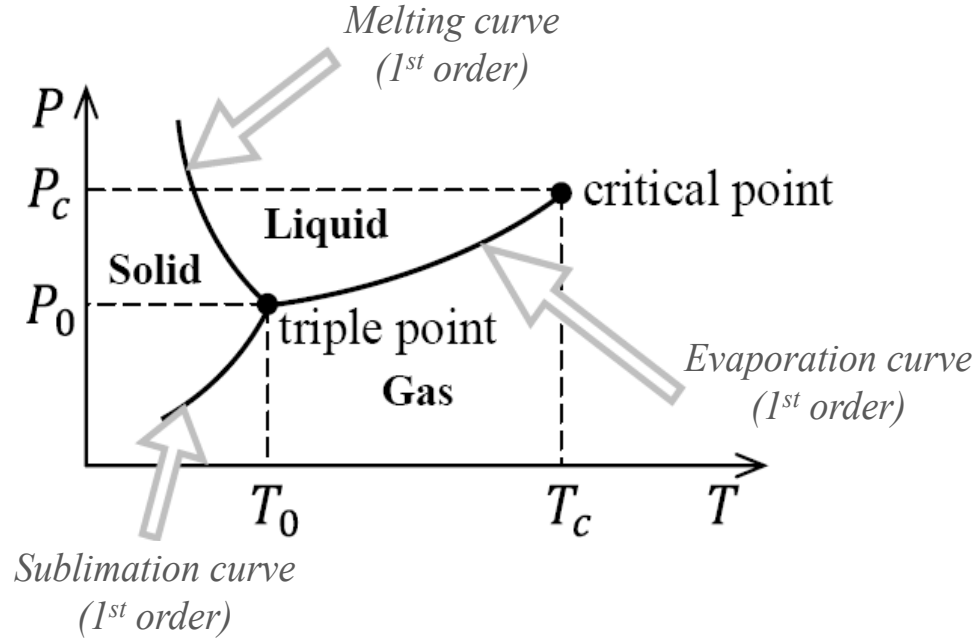
$$\tau \leq \tau_{\text{freeze out}} e^{-\frac{1}{2}|y_A - y_B|}$$

**Only early correlations can be long range in rapidity**



# Nature of phase transition

## Phase diagram of water (Electro-magnetic interactions)

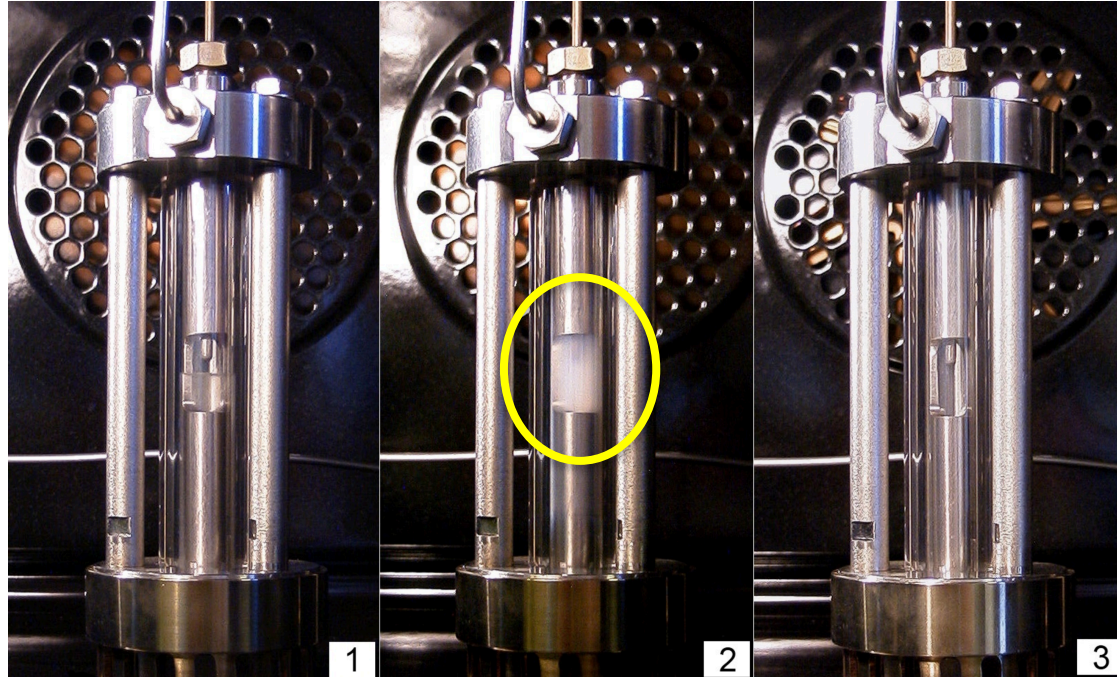


- **1<sup>st</sup> order phase transition:** mixed phase
- **At the critical point (CP):** phase boundaries vanish and **correlation length** diverges → only one phase exists



# Critical opalescence: 2<sup>nd</sup> order phase transition

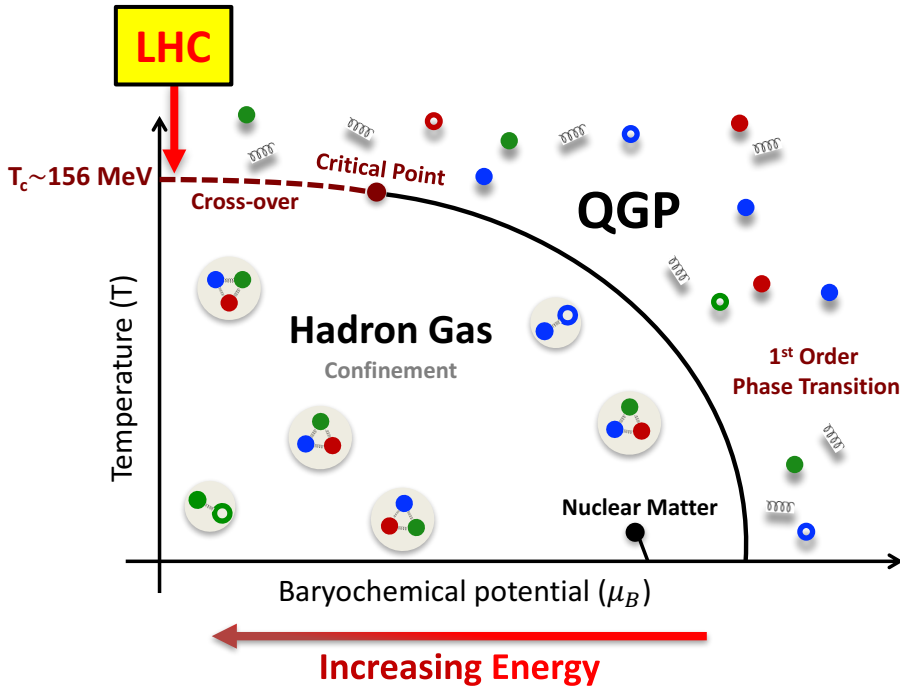
- Density of the gas and the thermal motion of the liquid is so great that **gas and liquid are the same**
- **Density fluctuations** are comparable to the wavelength of light → light is scattered and causes cloudy appearance



Heating a mass of ethane in a constant volume



# Nature of QCD phase transition



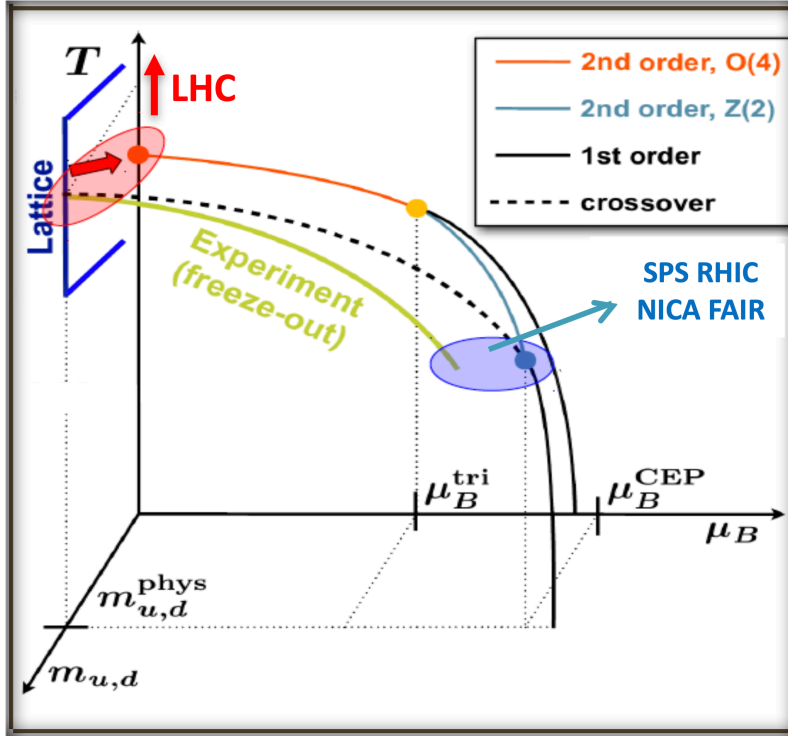
- How close are we to  $\mu_B = 0$  at LHC energies?
- Nature of cross over transition at  $\mu_B \sim 0$  MeV?  
⇒ no experimental confirmation





# Nature of QCD phase transition

F. Karsch, Schleching 2016



- How close are we to  $\mu_B = 0$  at LHC energies?
- Nature of cross over transition at  $\mu_B \sim 0$  MeV?  
⇒ no experimental confirmation
- Vanishing  $u, d$  quark masses?  
⇒ vicinity to 2<sup>nd</sup> order  $O(4)$  criticality  
⇒ pseudocritical features at the crossover due to massless modes  
⇒ **long range correlations & increased fluctuations**





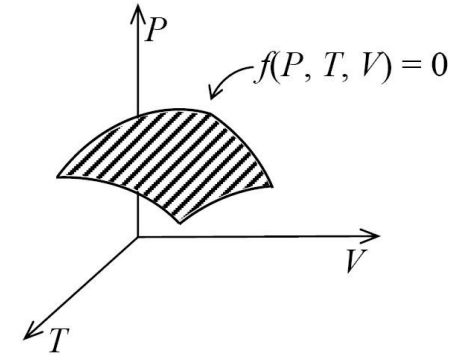
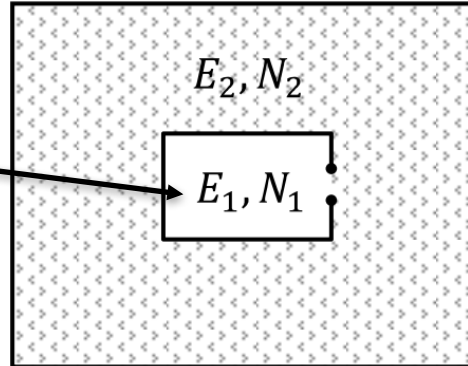
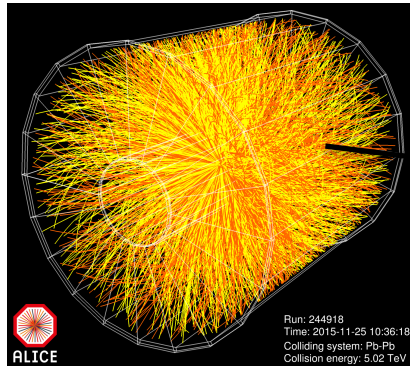
**What kind of a system  
are we dealing with?**



ALICE

Run: 244918  
Time: 2015-11-25 10:36:18  
Colliding system: Pb-Pb  
Collision energy: 5.02 TeV

# Thermodynamics of heavy-ion collision

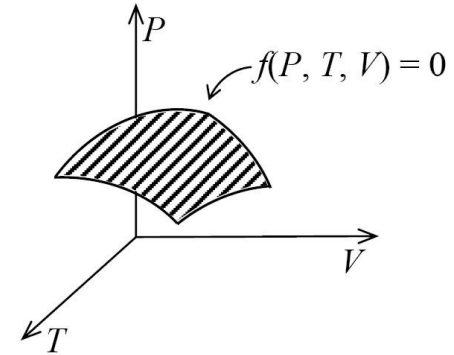
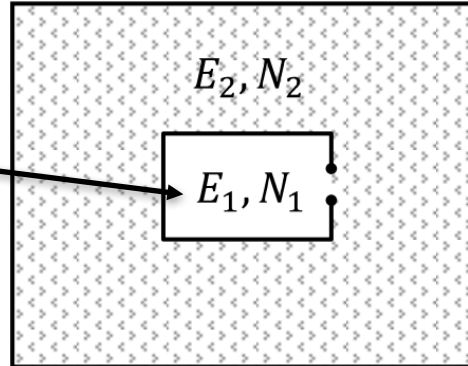
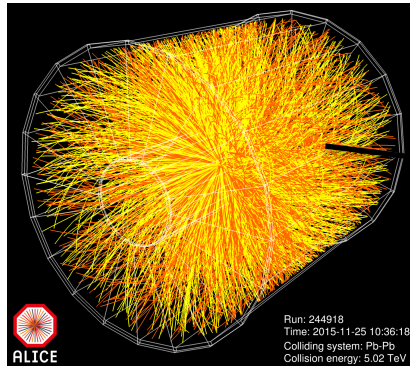


Grand canonical ensemble where particles are in a thermal equilibrium

- Energy ( $E$ ) and number of particles ( $N$ ) are **not conserved** in each microstate
- EOS can be represented **by a surface** in the state space spanned by  $P$ ,  $V$  and  $T$



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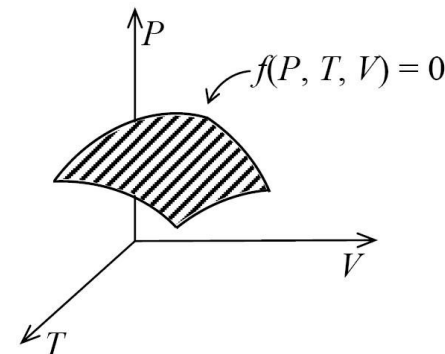
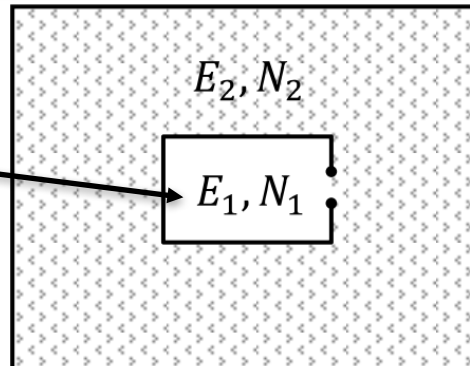
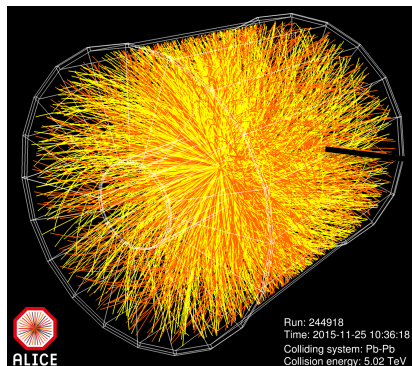


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- Conservation laws are applied **on average**
- Chemical potential ( $\mu_B$ ), Volume ( $V$ ) and Temperature ( $T$ ) are constant
- For a given state  $E_j$  and  $N_j$  **grand canonical partition function**

$$Z_{GCE}(T, V, \mu) = \sum_j \exp\left[-\frac{E_j - \mu N_j}{T}\right] \quad \Rightarrow \quad \langle N \rangle = \sum_j N_j p_j = T \left. \frac{\partial \ln Z_{GCE}}{\partial \mu} \right|_V$$



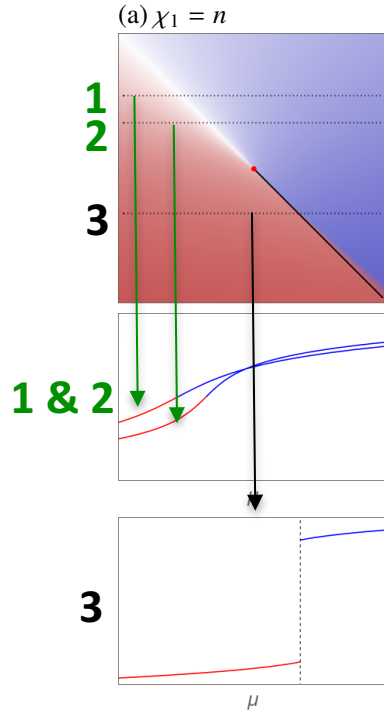
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$$\langle N \rangle = \sum_j N_j p_j = T \left. \frac{\partial \ln Z_{GCE}}{\partial \mu} \right|_V \quad \rightarrow \quad n \equiv \frac{\langle N \rangle}{V} = \left( \frac{\partial P}{\partial \mu} \right)_T \quad \rightarrow \quad \chi_k = \left( \frac{\partial^k P}{\partial \mu^k} \right)_T = \left( \frac{\partial^{k-1} n}{\partial \mu^{k-1}} \right)_T$$



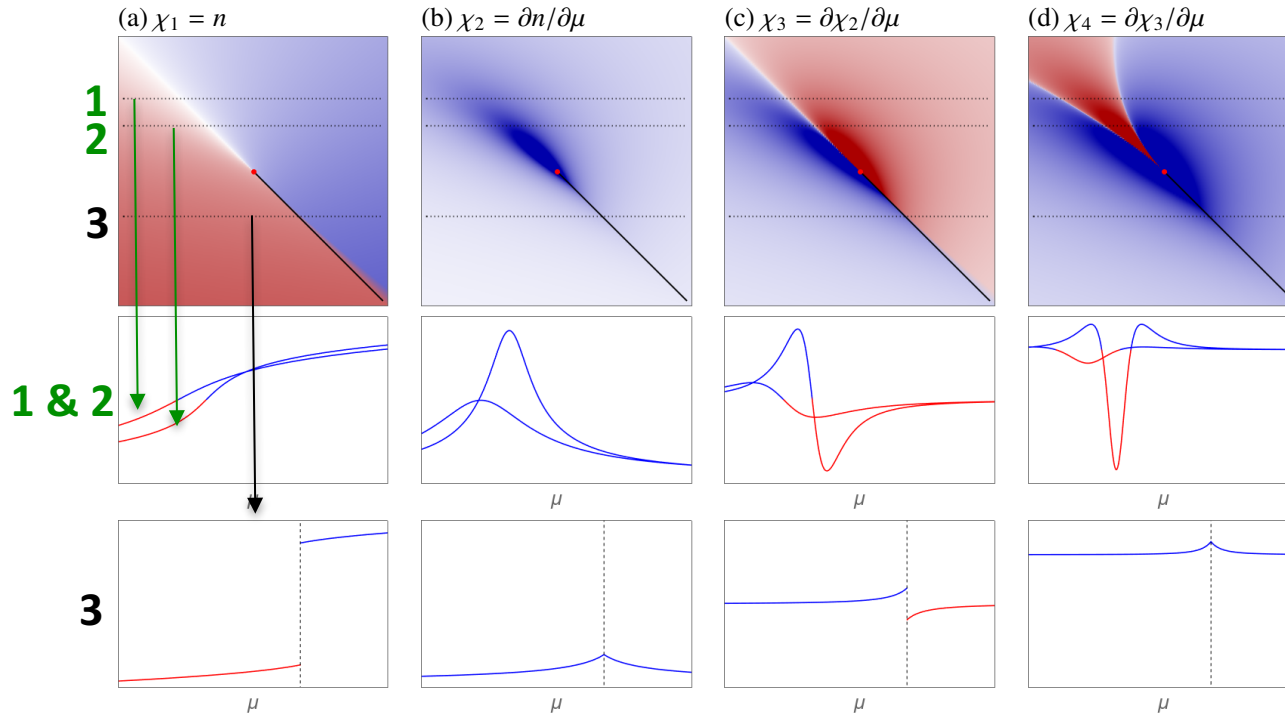
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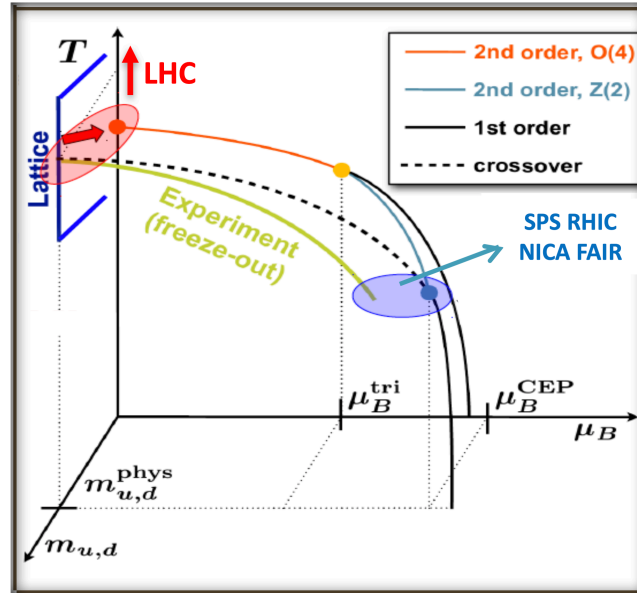
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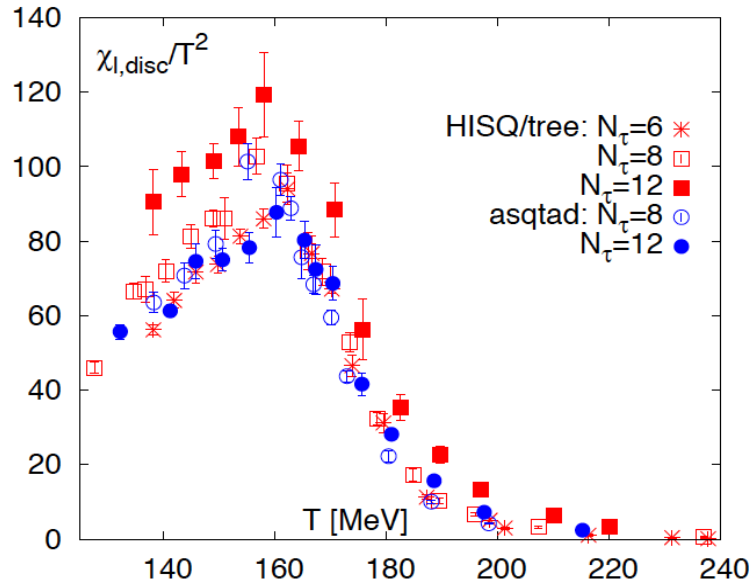
# How to link theory to Experiment?

→ Lattice QCD



# Light quark susceptibilities

$$\langle \bar{\psi}\psi \rangle_l^{n_f=2} = \frac{T}{V} \frac{\partial \ln Z}{\partial m_l} \quad \rightarrow \quad \chi_{m,l} = \frac{\partial}{\partial m_l} \langle \bar{\psi}\psi \rangle_l^{n_f=2}$$

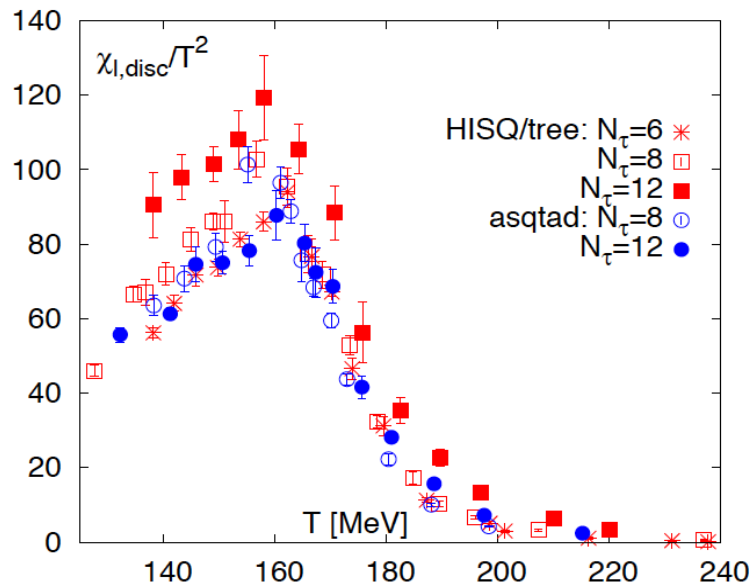


HotQCD Collaboration, Phys.Rev. D85 (2012) 054503



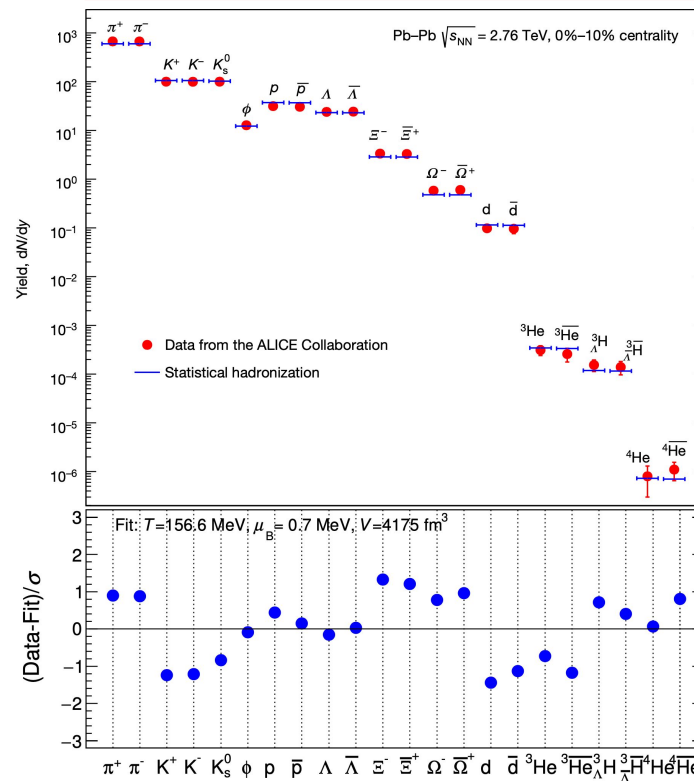
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HotQCD Collaboration, Phys.Rev. D85 (2012) 054503

$$T_{pc} = 156.5 \pm 1.5 \text{ MeV} \approx T_{fo}^{\text{ALICE}}$$



A. Andronic, et. al. Nature 561 (2018) 321, Phys. Lett. B 792 (2019) 304



# Hunting for criticality: Cumulants of net-charge distributions

LOCD

Baryon number (**B**), Strangeness (**S**), Electric charge (**Q**), Charm (**C**)

$$\chi_{klmn}^{BQSC} = \left. \frac{\partial^{(k+l+m+n)} [P(\hat{\mu}_B, \hat{\mu}_Q, \hat{\mu}_S, \hat{\mu}_C) / T^4]}{\partial \hat{\mu}_B^k \partial \hat{\mu}_Q^l \hat{\mu}_S^m \partial \hat{\mu}_C^n} \right|_{\vec{\mu}=0}$$



EXPERIMENT

$$\Delta N_B = X = N_B - N_{\bar{B}}$$

$\kappa_n \rightarrow$  central moments of X

$$\hat{\chi}_2^B = \frac{\kappa_2(\Delta N_B)}{VT^3} \rightarrow \frac{\kappa_4(\Delta N_B)}{\kappa_2(\Delta N_B)} = \frac{\hat{\chi}_4^B}{\hat{\chi}_2^B}$$

**Effect of volume fluctuations:**

P. Braun-Munzinger, A. Rustamov, J. Stachel, Nucl. Phys. A960 (2017) 114



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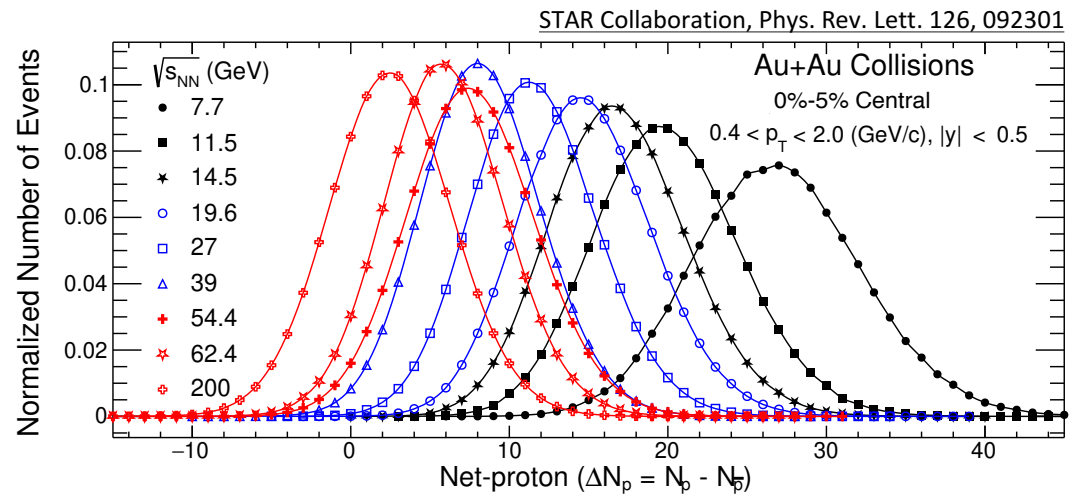


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- Critical signals are hidden in the tails
- Experimentally very challenging

**Effect of volume fluctuations:**

P. Braun-Munzinger, A. Rustamov, J. Stachel, Nucl. Phys. A960 (2017) 114



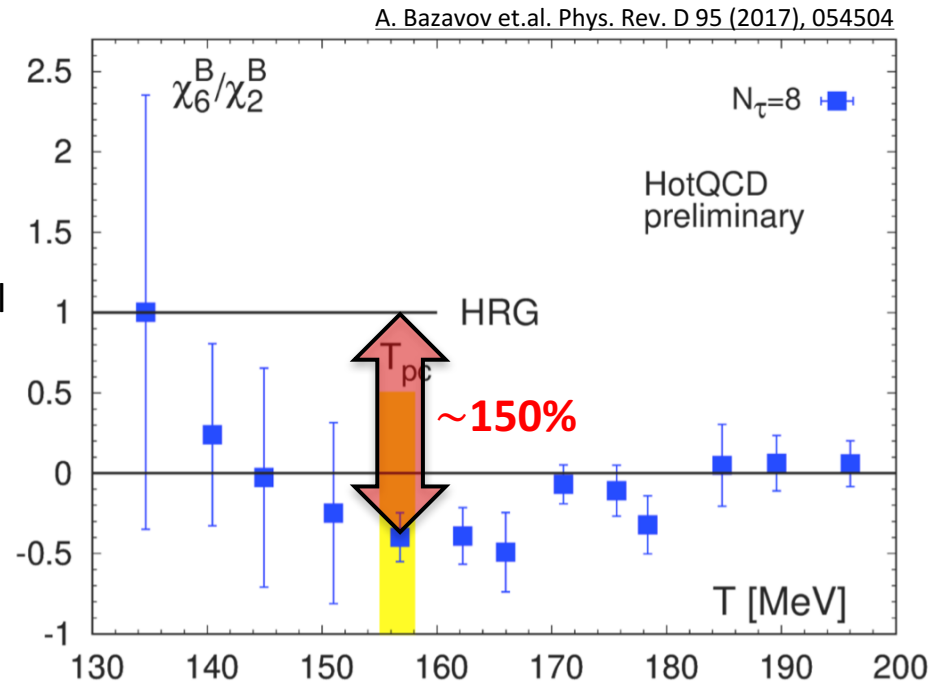
# What does theory tell us?

- 1) Baseline:** Difference between two independent Poissonian distributions (Skellam distr.)  
 $\Rightarrow \kappa_n/\kappa_2$  is **0 (odd)** or **1 (even)**
- 2) Up to 3<sup>rd</sup> order** Hadron Resonance Gas (HRG) model agrees with LQCD at  $\mu_B = 0$
- 3) Higher order**  $\rightarrow$  larger deviation from baseline



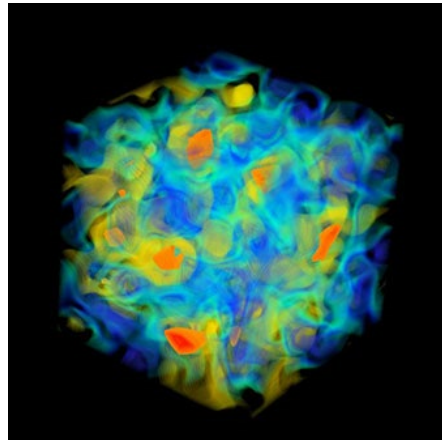
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- 3) **Higher order** → larger deviation from baseline
- 4) **Holy grail:** Critical behavior as from 6<sup>th</sup> order  
⇒ 4<sup>th</sup> order ~30%, 6<sup>th</sup> order ~150%

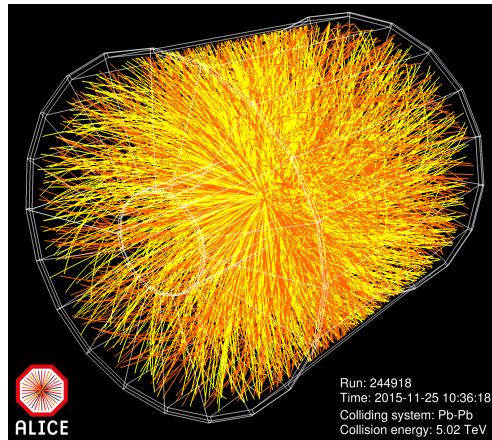


# LQCD vs Experiment: Caveats

- ✓ Experiments measure final state of the **dynamical evolution**, while LQCD calculates an **equilibrium**
- ✓ Fluctuations are typically calculated in **coordinate space** but measured in **momentum space**
- ✓ LQCD suffers from **sign problem at large  $\mu_B$**



LQCD@BNL



ALICE data

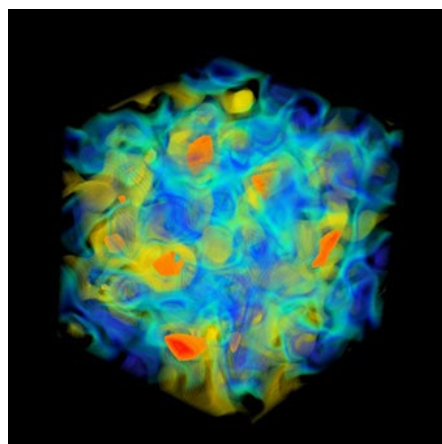




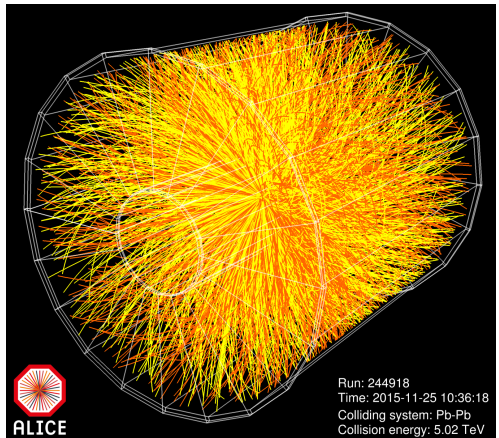
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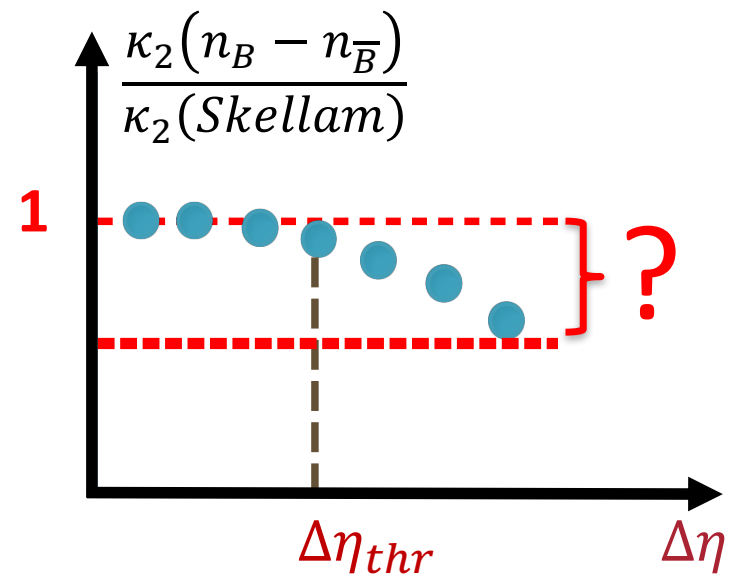
- ✓ Fluctuations of conserved charges appear only inside **finite acceptance**
- ✓ In the limit of very small acceptance → only **Poissonian fluctuations**



LQCD@BNL

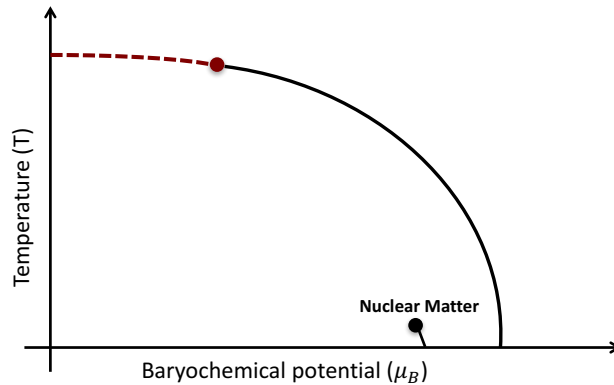
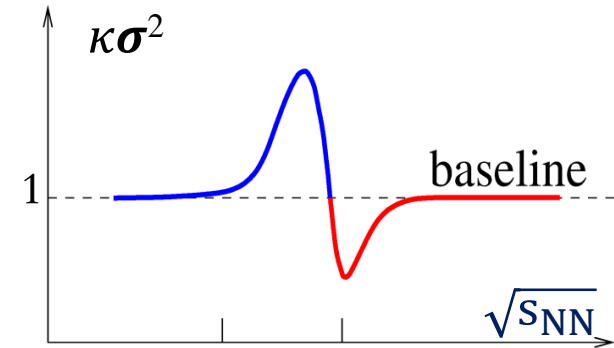


ALICE data



# E.g.: Expectation from beam energy scan

## Non-monotonic behavior as a function of energy

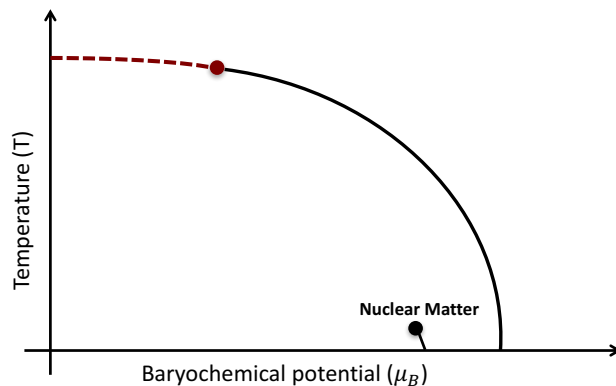
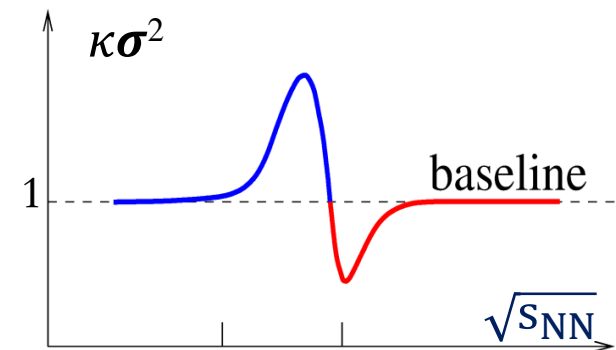


M. Stephanov, PRL102, 032301 (2009), PRL107, 052301 (2011)



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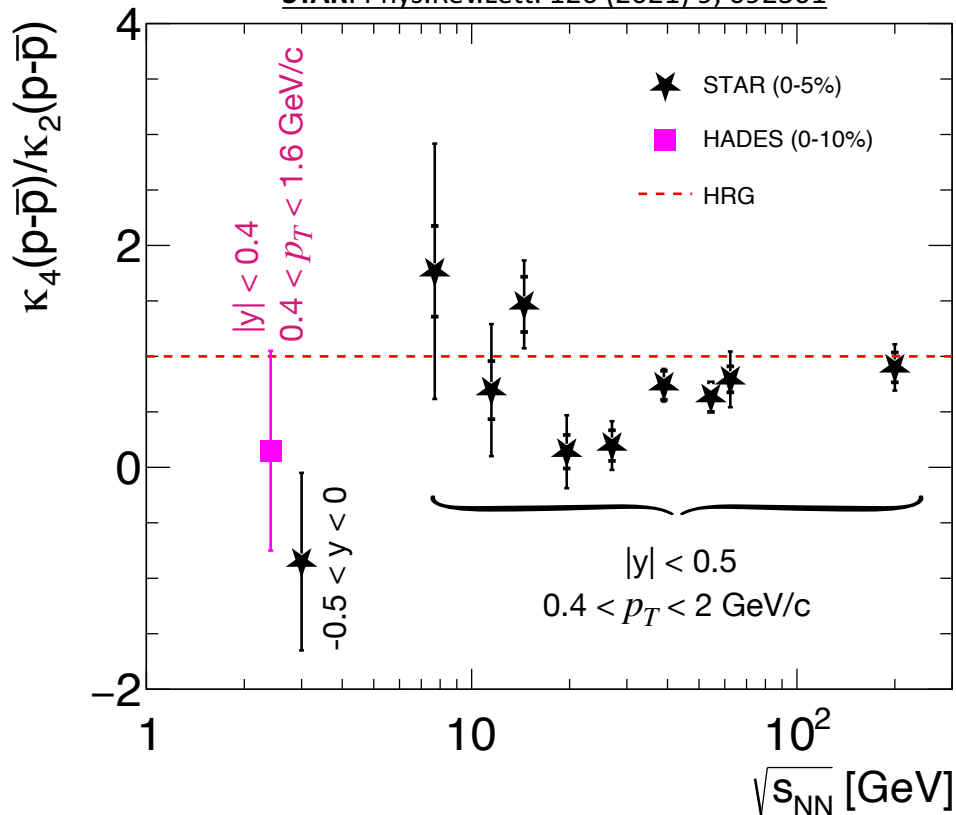
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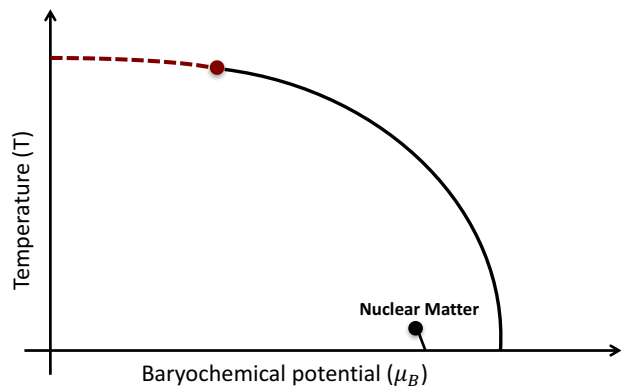
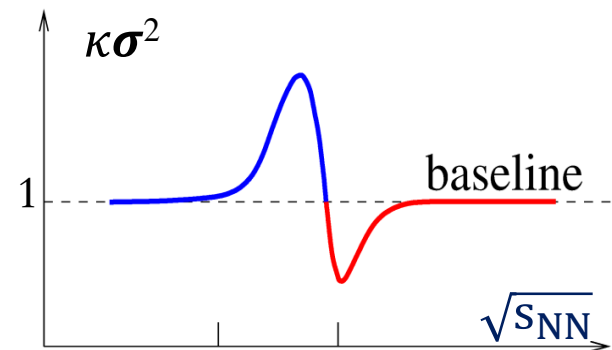
HADES: Phys.Rev.C 102 (2020) 2, 024914

STAR: Phys.Rev.Lett. 126 (2021) 9, 092301



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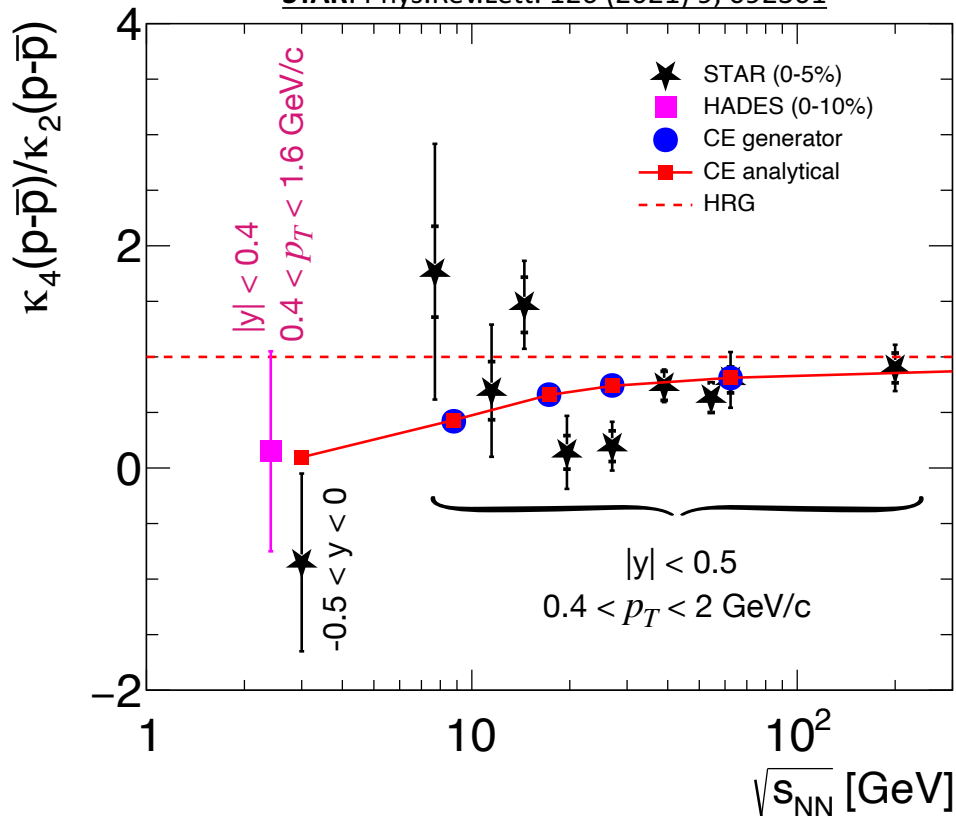
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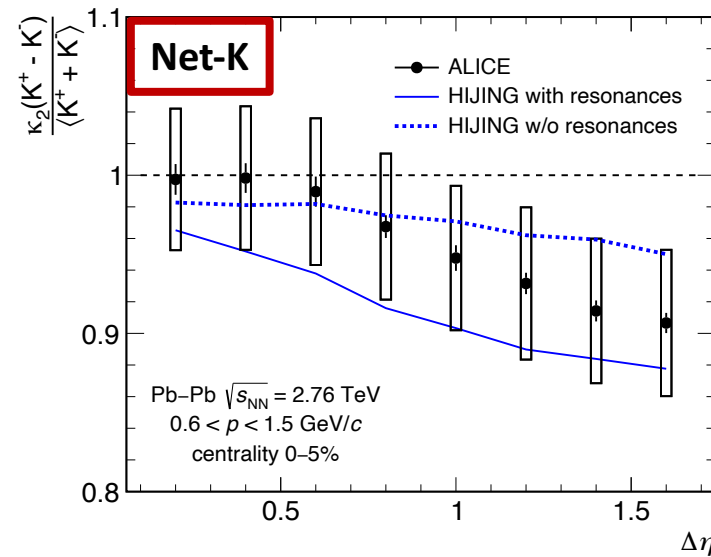
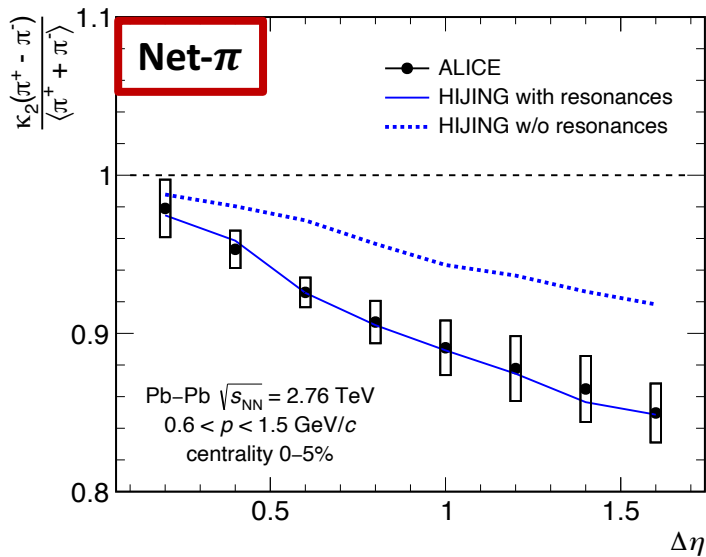
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# Net-(global) charge fluctuations

NEW



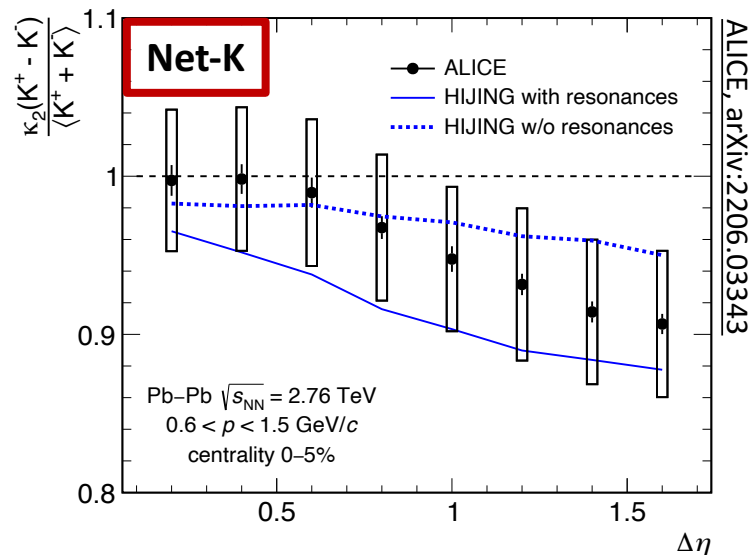
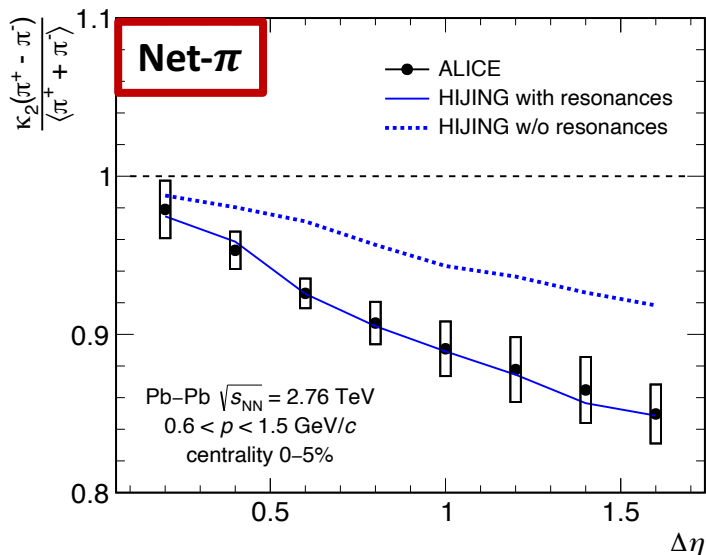
ALICE, arXiv:2206.03343

- **Net-Q,S:** → Strongly dominated by **resonance contributions**  
 (V. Vovchenko and V. Koch Phys. Rev. C 103, 044903 (2021))



# Net-(global) charge fluctuations

NEW



- **Net-Q,S:** → Strongly dominated by **resonance contributions**  
(V. Vovchenko and V. Koch Phys. Rev. C 103, 044903 (2021))
- **Net-B:**
  - Due to **isospin randomization**, at  $\sqrt{s_{NN}} > 10$  GeV **net-baryon ↔ net-proton**  
(M. Kitazawa, and M. Asakawa, Phys. Rev. C 86, 024904 (2012))
  - No resonance feeding  $p + \bar{p}$
  - **Best candidate for measuring charge susceptibilities is net-p**



# A Large Ion Collider Experiment

## Main detectors used:

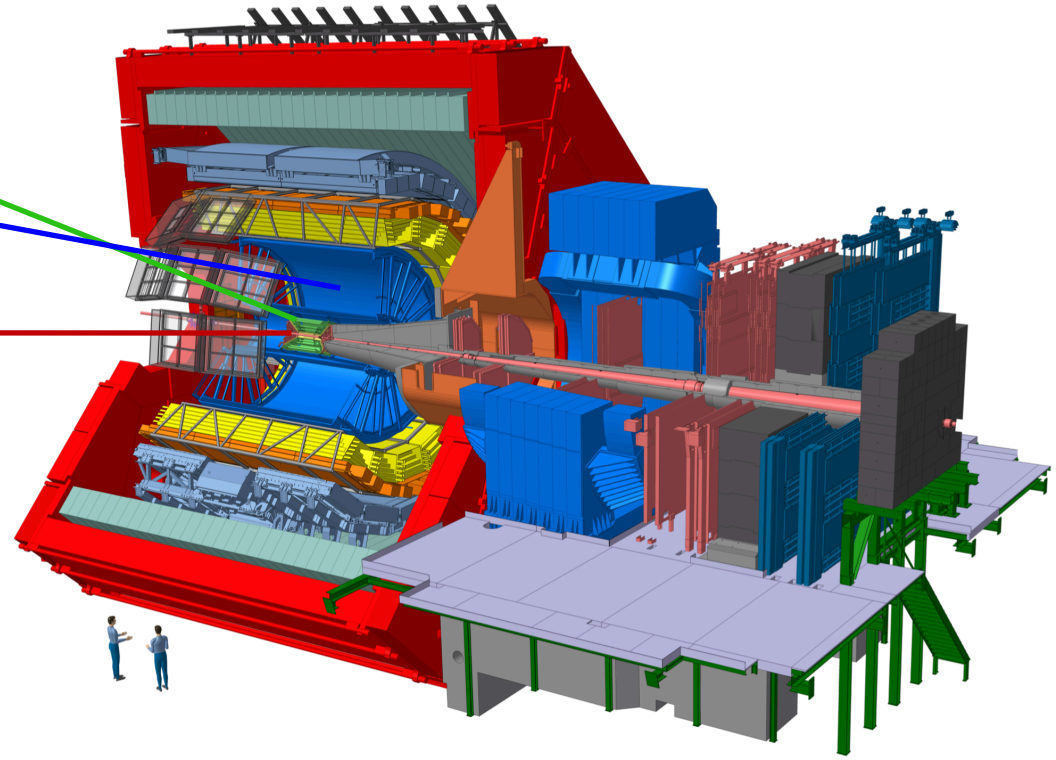
- Inner Tracking System (ITS) → Tracking and vertexing
- Time Projection Chamber (TPC) → Tracking and Particle Identification (PID)
- **V0** → Centrality determination

## Data Set:

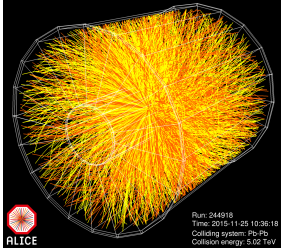
- $\sqrt{s_{NN}} = 5.02 \text{ TeV}$ ,  $\sim 78 \text{ M events}$
- $\sqrt{s_{NN}} = 2.76 \text{ TeV}$ ,  $\sim 13 \text{ M events}$

## Kinematic acceptance:

- $0.6 < p < [1.5, 2] \text{ GeV}/c$
- $|\eta| < 0.2, 0.4, \dots, 0.8$

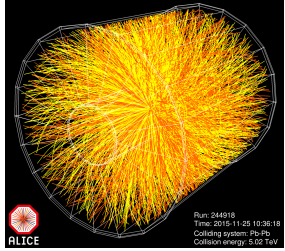


# Experimental challenges?



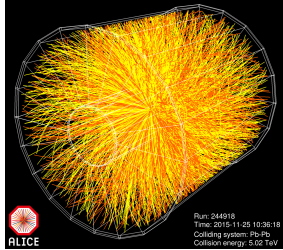


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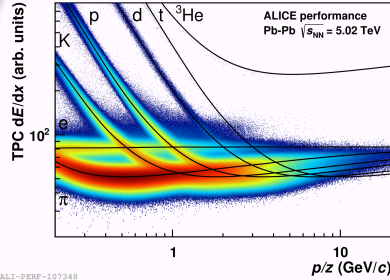


Event/track selection

# Experimental challenges?

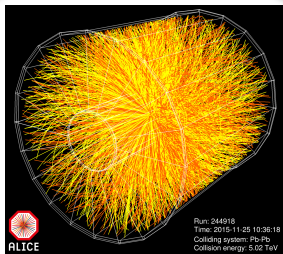


Event/track selection

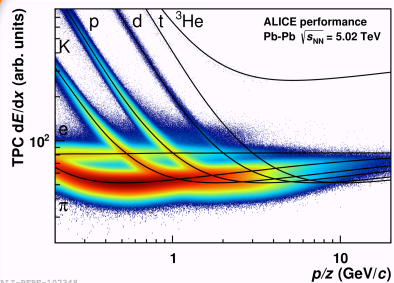


$dE/dx$  calibration and PID

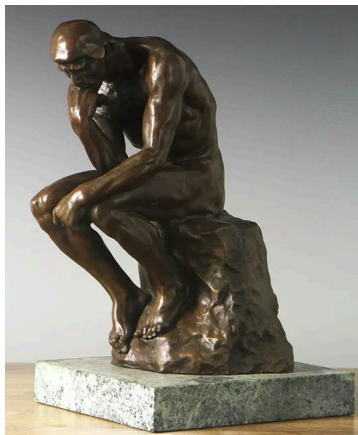
# Experimental challenges?



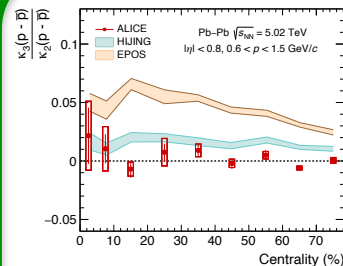
Event/track selection



ALICE-PPRF-107348

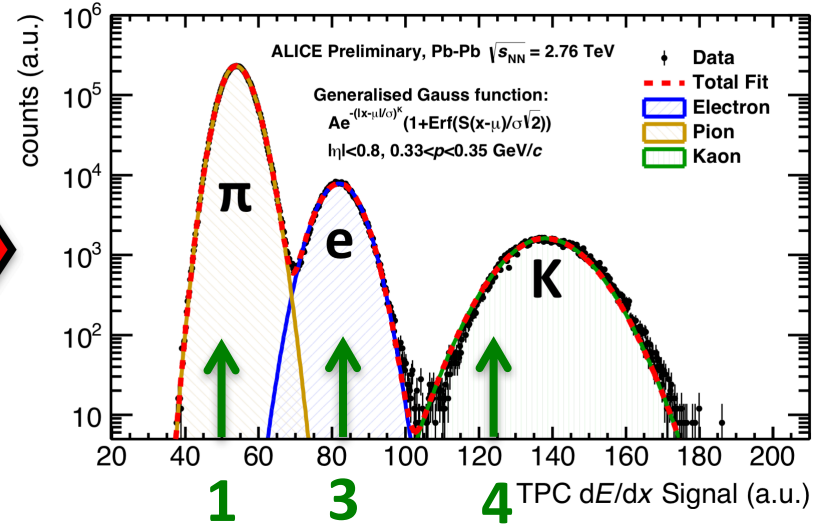
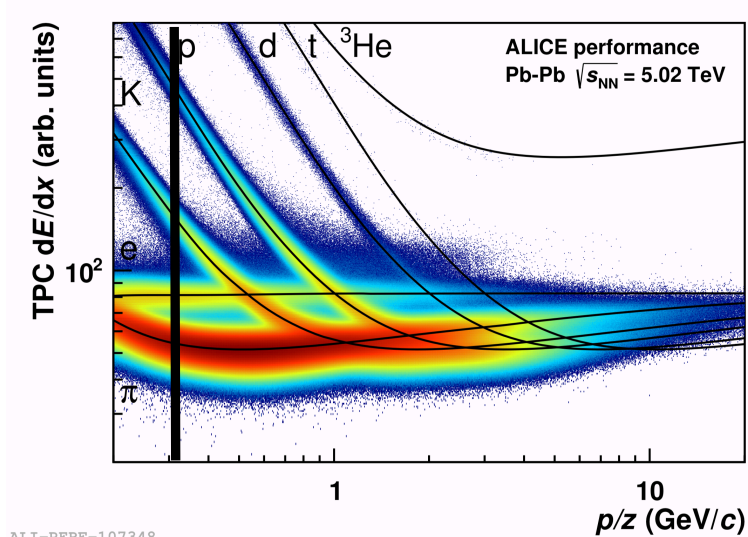


$dE/dx$  calibration and PID

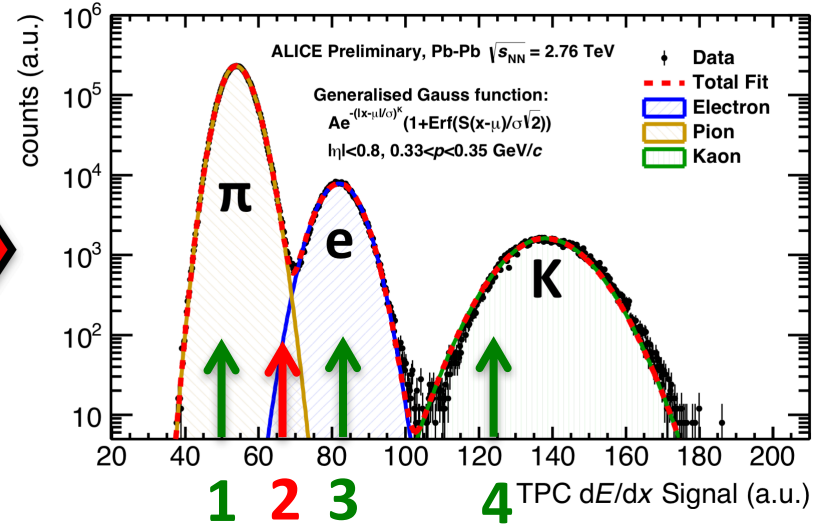
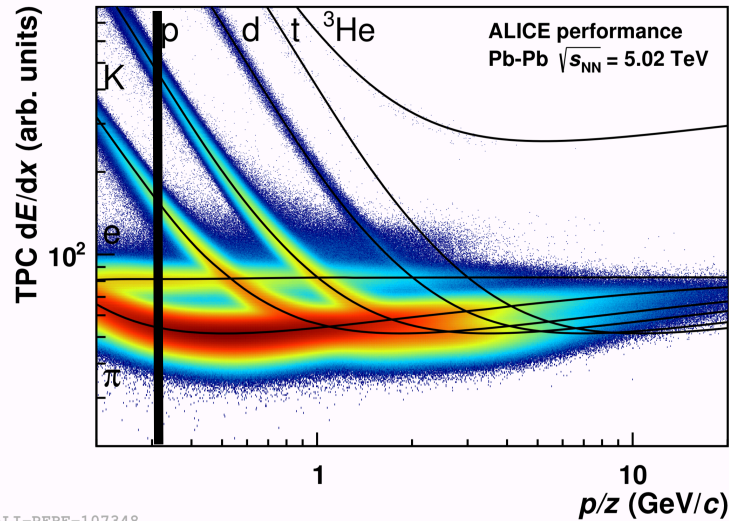


Efficiency correction

# Cut based approach vs Identity Method



# Cut based approach vs Identity Method



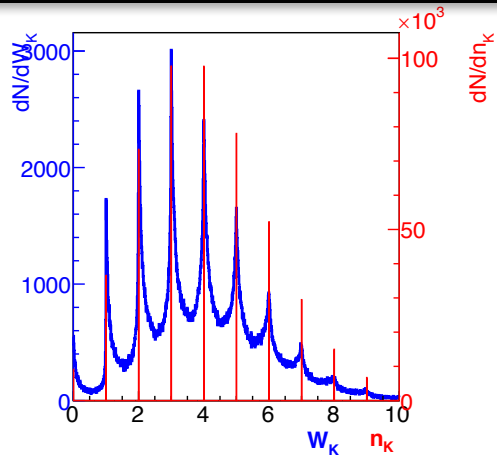
$$\omega_{\pi}^{(1)} = 1, \quad \omega_{\pi}^{(2)} \cong 0.6, \quad \omega_{\pi}^{(3)} = 0, \quad \omega_{\pi}^{(4)} = 0 \quad \Rightarrow \quad W_{\pi} = 1.6 \neq N_{\pi}$$

A. Rustamov, M. Gazdzicki, M. I. Gorenstein, PRC 86, 044906 (2012), PRC 84, 024902 (2011)

A. Rustamov, M. Arslanodk, Nucl. Instrum. A946 (2019) 162622}



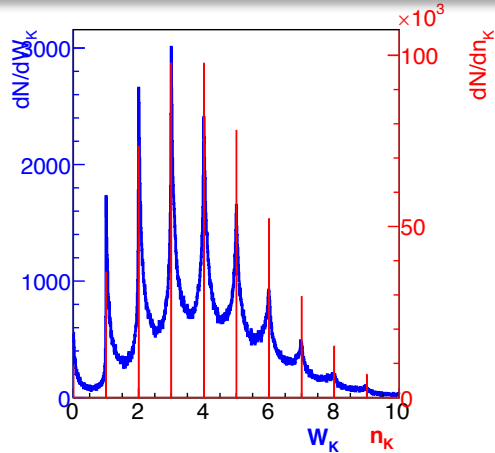
# Identity Method



$$\langle N_j^n \rangle = A^{-1} \langle W_j^n \rangle$$

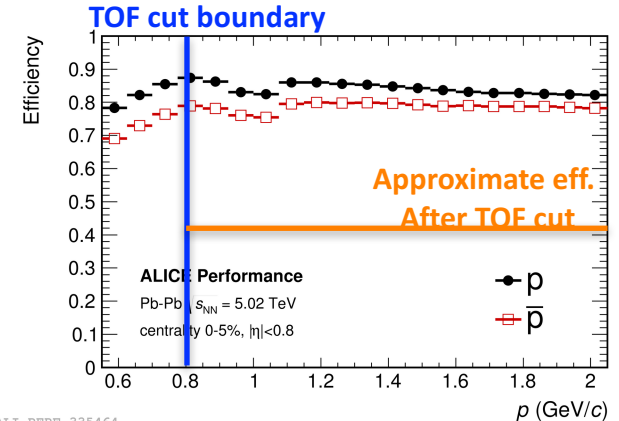


# Identity Method



$$\langle N_j^n \rangle = A^{-1} \langle W_j^n \rangle$$

- **Cut based approach**
  - Use additional detector information or reject a given phase space bin
  - Challenge: efficiency correction and contamination
- **Identity Method**
  - Gives folded multiplicity distribution
  - Easier to correct inefficiencies



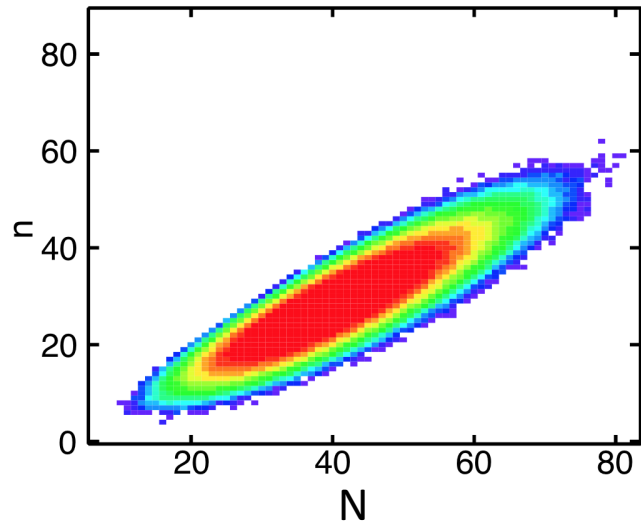
ALI-PERF-335464



## (2) Efficiency correction

### Hypergeometric detector response:

⇒ Draw  $N$  balls from the urn without returning balls to the urn  
( $n$ : reconstructed,  $N$ : generated multiplicity)

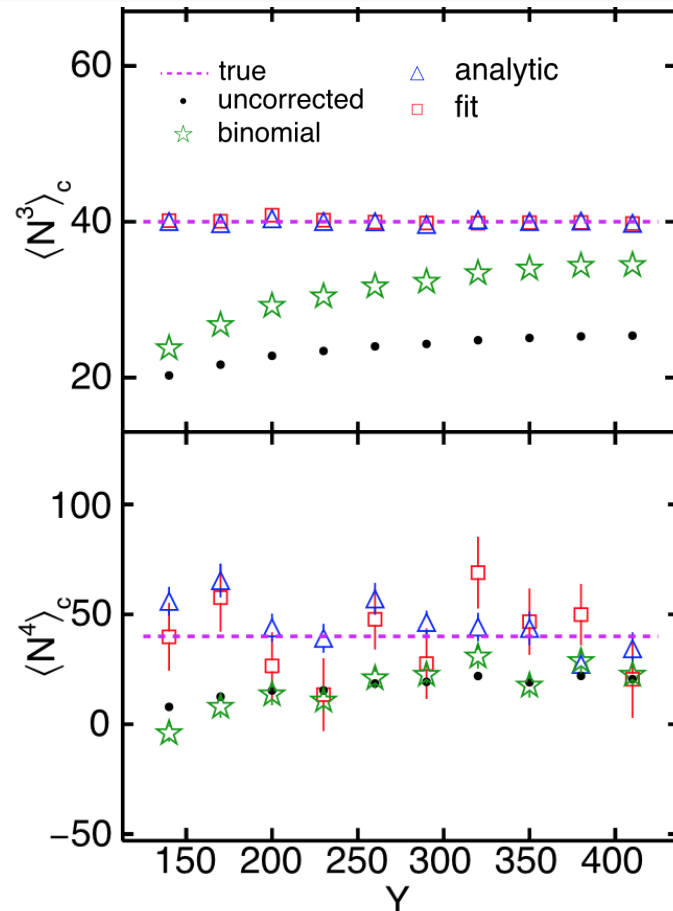
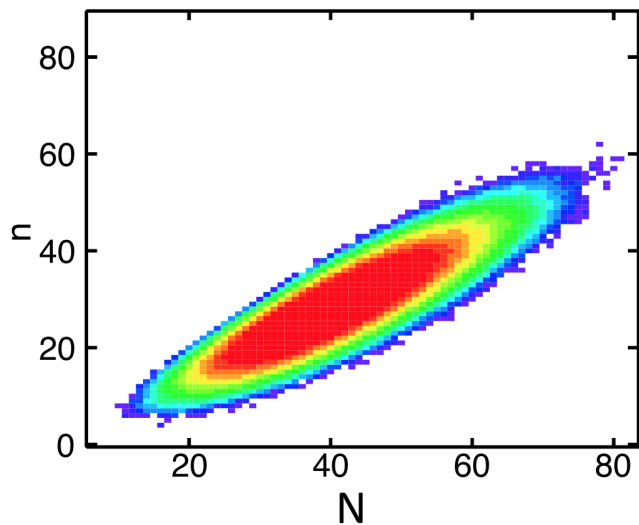




## (2) Efficiency correction

### Hypergeometric detector response:

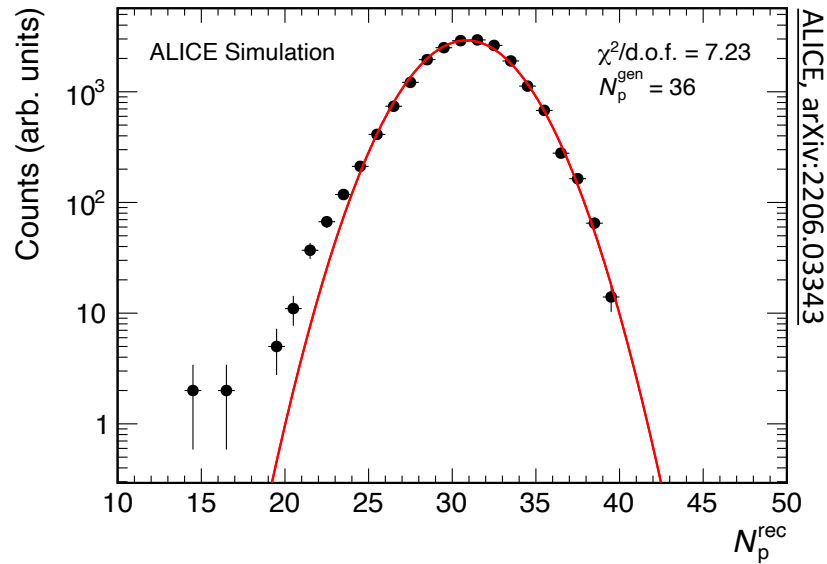
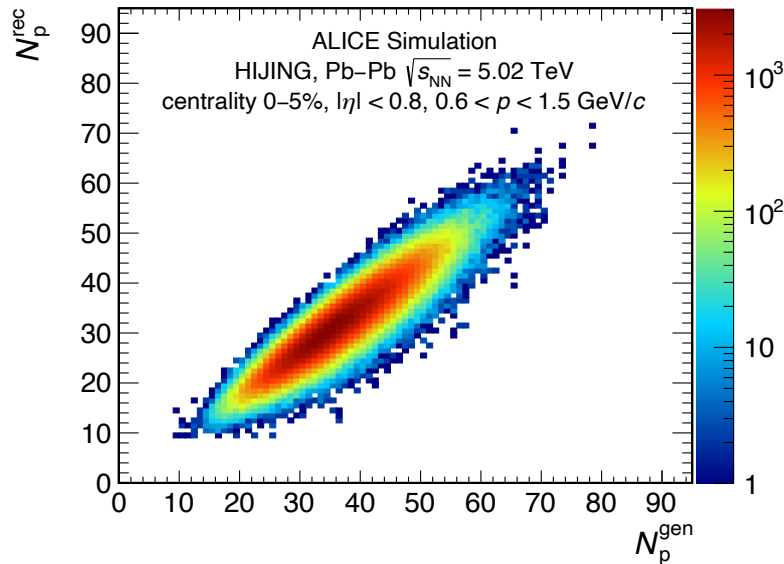
⇒ Draw  $N$  balls from the urn without returning balls to the urn  
( $n$ : reconstructed,  $N$ : generated multiplicity)



T. Nonaka, M. Kitazawa, S. Esumi, Nucl. Instrum. Meth. A906 (2018) 10-17



Binomiality of the detector response is important for the efficiency correction



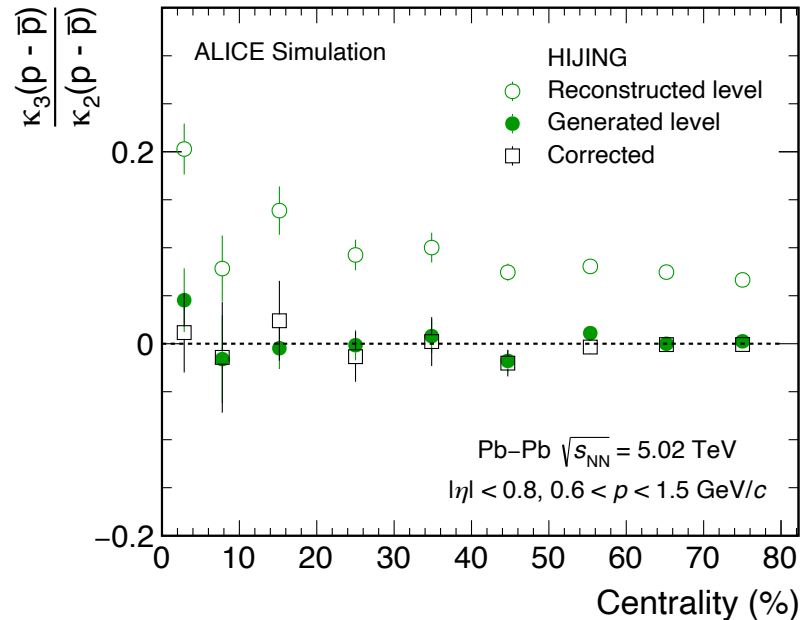
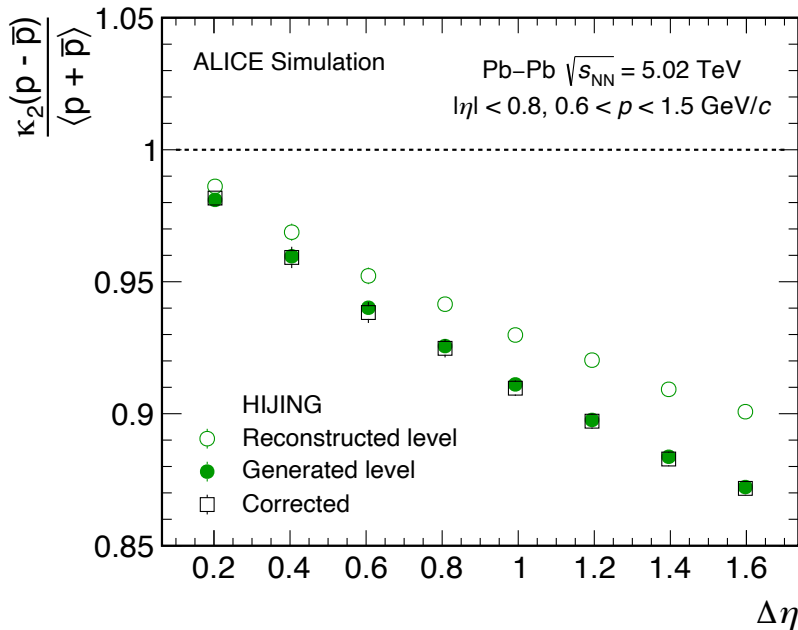
ALICE, arXiv:2206.03343

## Slight deviation from the binomial efficiency loss

- Event and track selection
- TPC  $dE/dx$  calibration in particular for the events with pileup  
M. Arslandok, E. Hellbär, M. Ivanov, R.H. Münzer and J. Wiechula, *Particles* 2022, 5(1), 84-95
- Realistic detector simulation

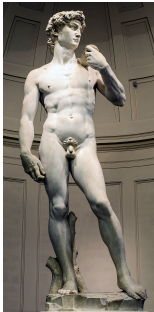


# MC closure



NEW

ALICE, arXiv:2206.03343

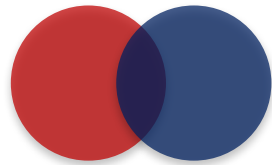
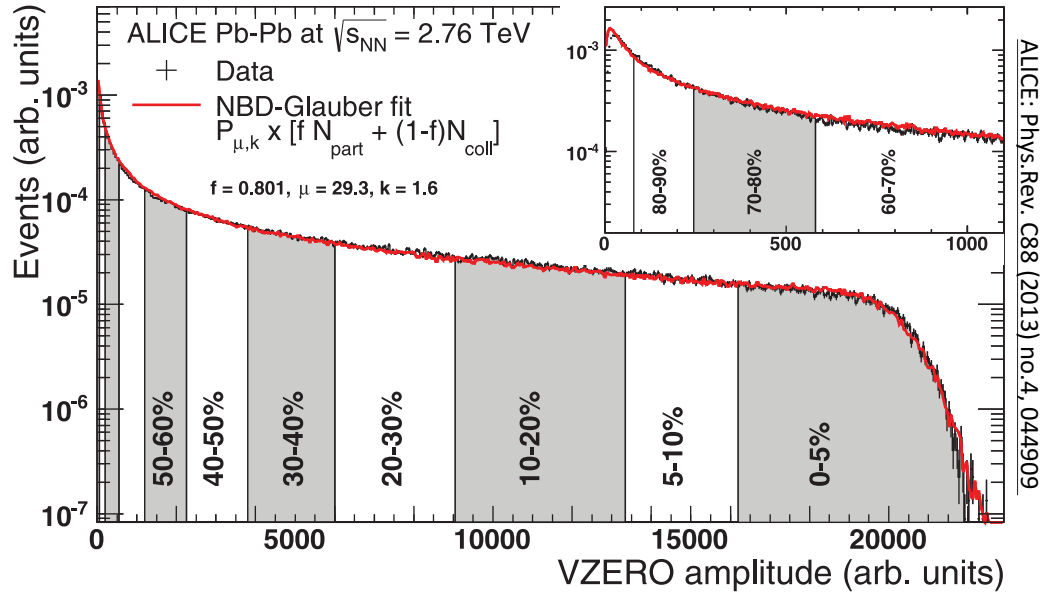


Very good closure despite the slight deviation from binomial loss

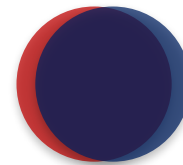
Efficiency correction with binomial assumption: T. Nonaka, M. Kitazawa, S. Esumi, Phys. Rev. C 95, 064912 (2017), Adam Bzdak, Volker Koch, Phys. Rev. C 86, 044904 (2012)



# (3) Volume fluctuations



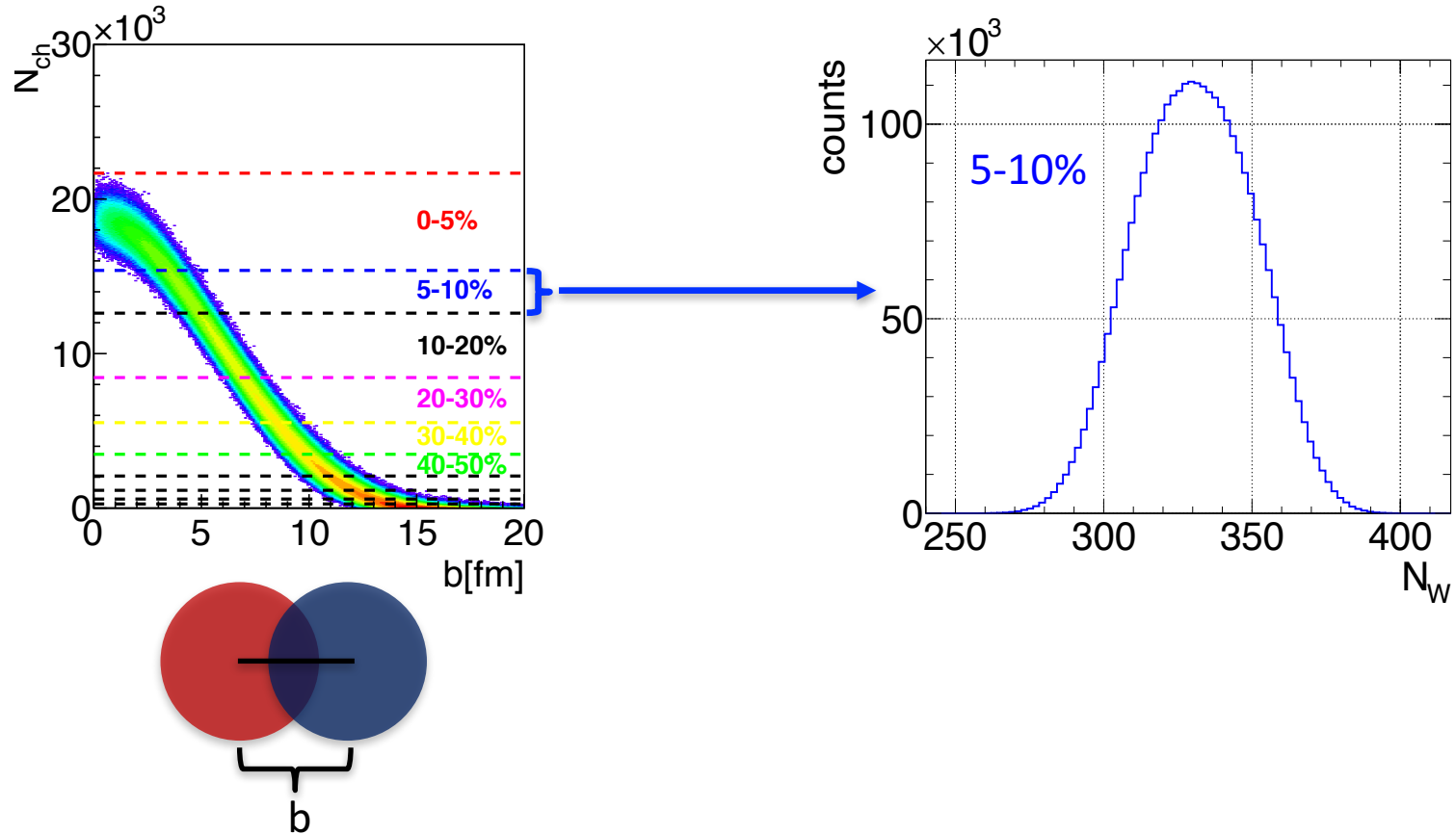
Peripheral collision



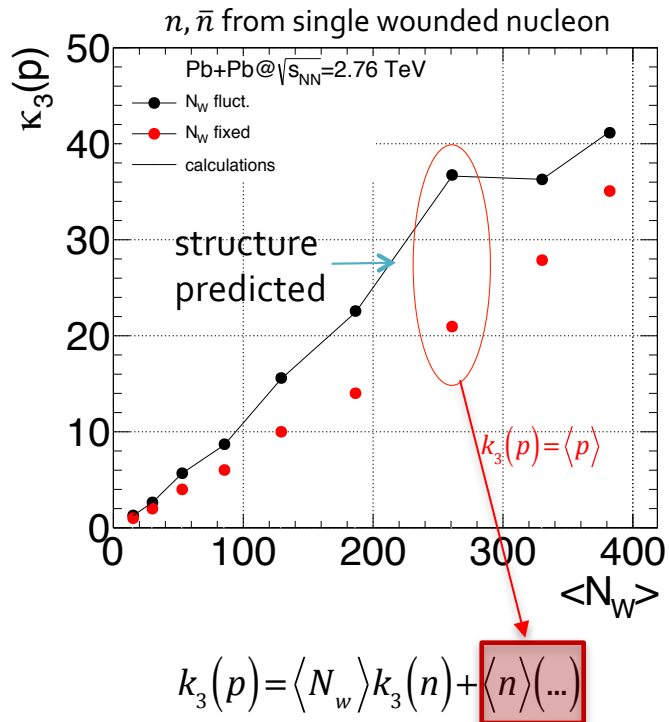
Central Collision



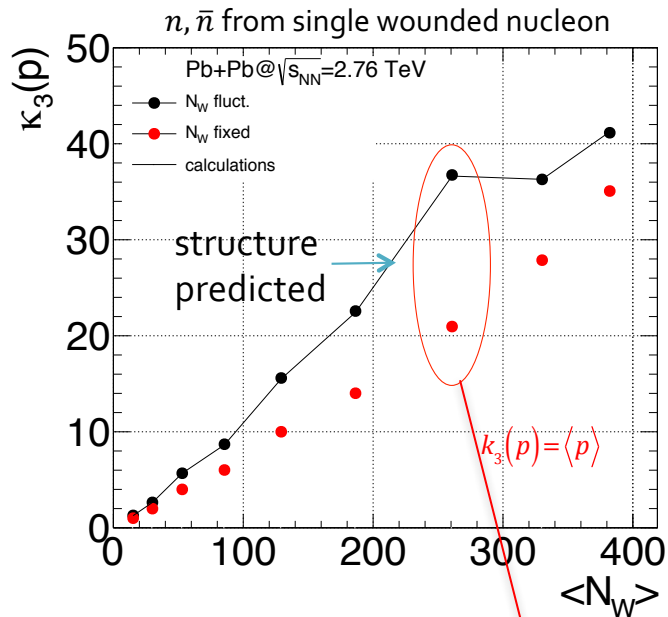
# Finite centrality bin width



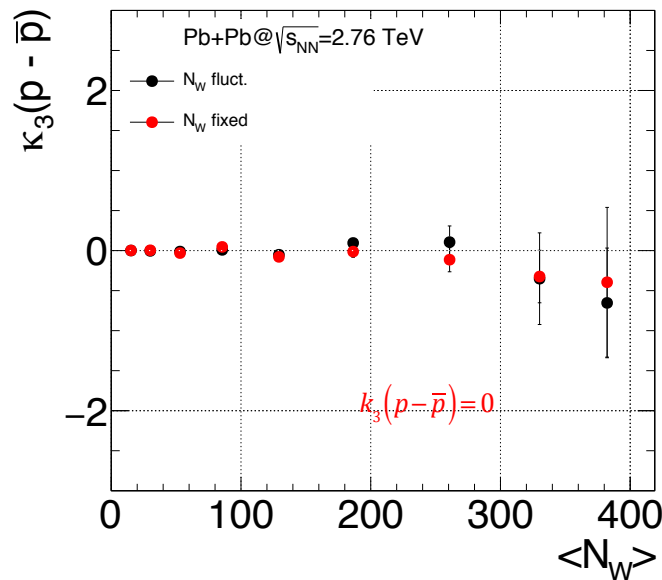
# Volume fluctuations at LHC energies



# Volume fluctuations at LHC energies



$$k_3(p) = \langle N_w \rangle k_3(n) + \langle n \rangle (\dots)$$



$$k_3(p - \bar{p}) = \langle N_w \rangle k_3(n - \bar{n}) + \langle n - \bar{n} \rangle (\dots)$$

P. Braun-Munzinger, A. Rustamov, J. Stachel  
Nucl. Phys. A 960 (2017) 114-130

Up to 3<sup>rd</sup> order net-proton cumulants are free from volume fluctuations



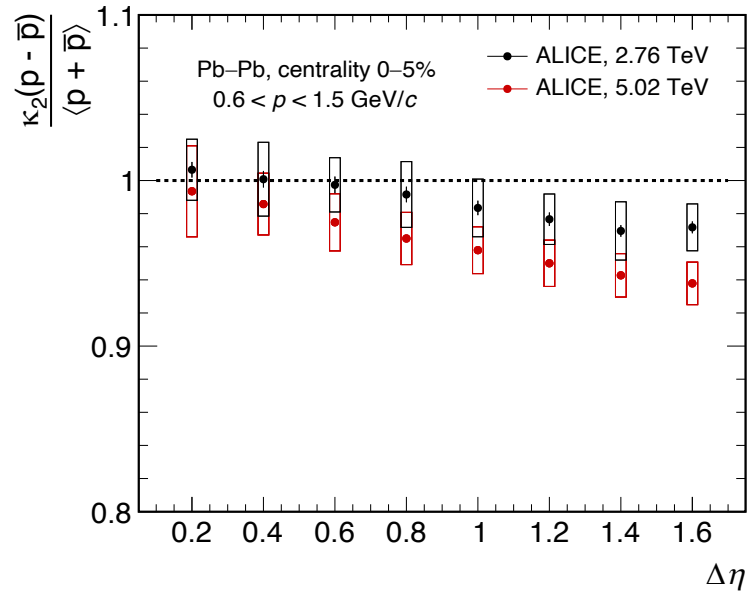
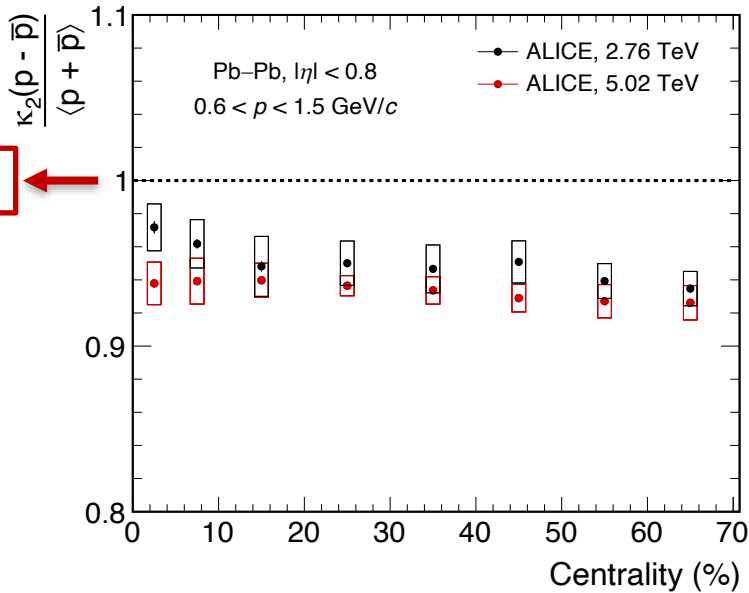
A 3D cutaway diagram of the ALICE experiment detector. The detector is a large, complex structure with various components highlighted in different colors: red for the main structure, blue for the central detector, yellow for the inner layers, and green for the base and support structures. Two small human figures are shown at the bottom left for scale. The text "What did we learn from ALICE 1 (2010-2018)?" is overlaid in the center.

**What did we learn from  
ALICE 1 (2010-2018)?**



# 2<sup>nd</sup> order cumulants of net-p

NEW



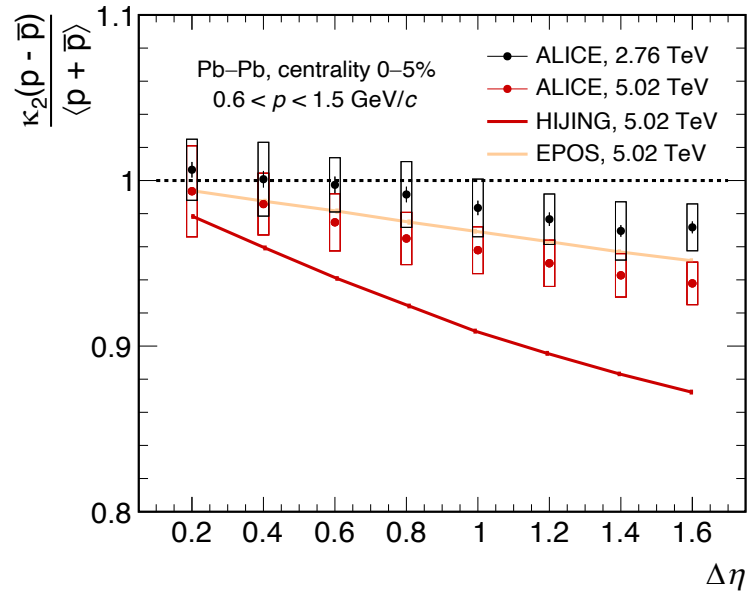
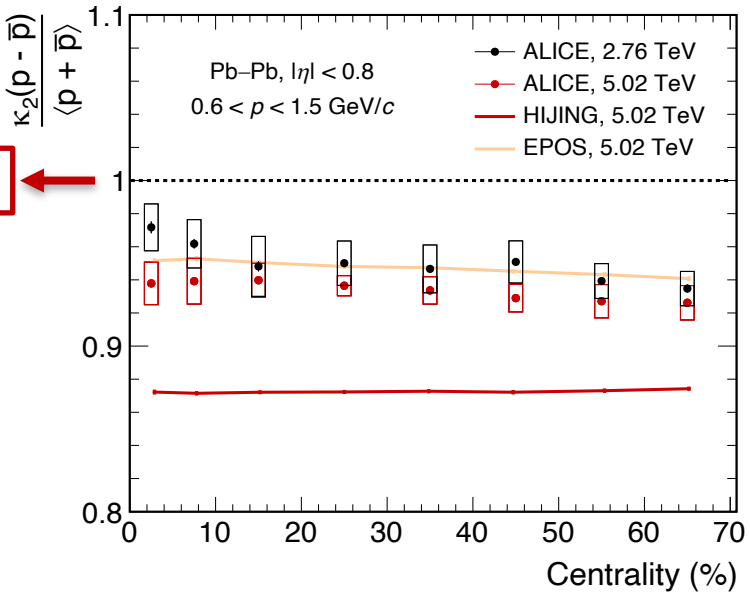
ALICE, arXiv:2206.03343

➤ Deviation from Skellam baseline



# 2<sup>nd</sup> order cumulants of net-p

NEW



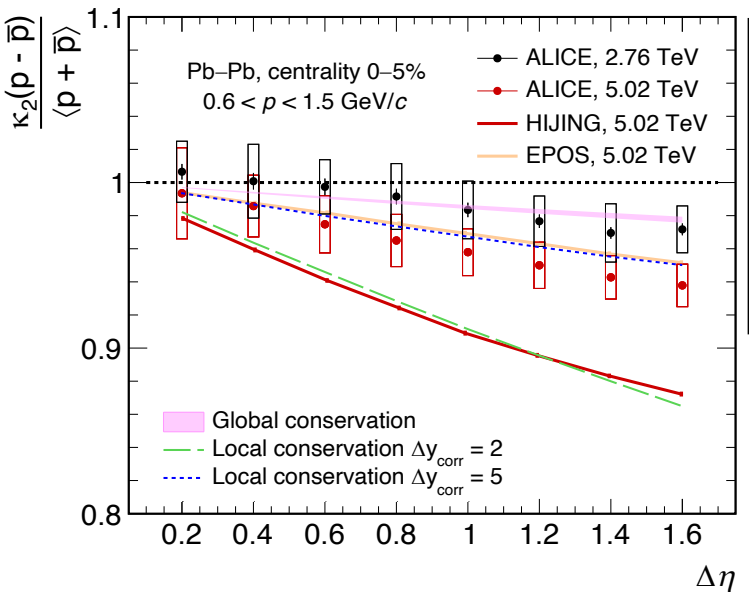
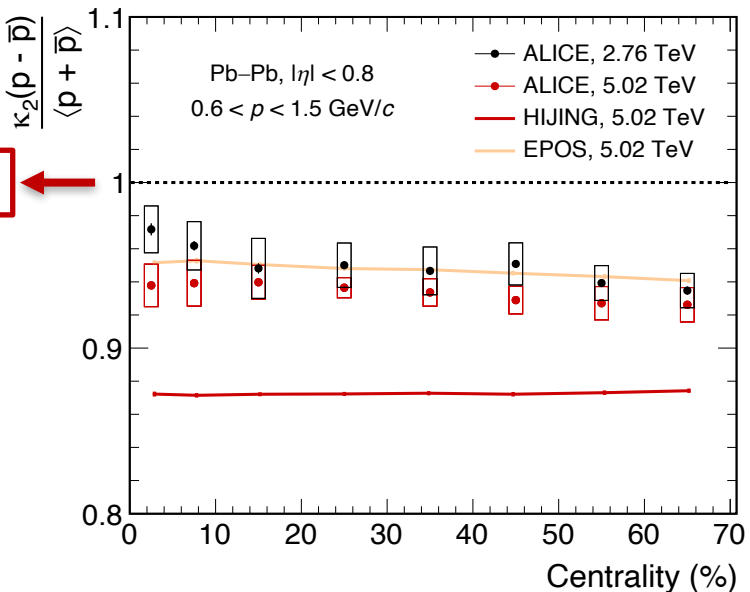
ALICE, arXiv:2206.03343

- Deviation from Skellam baseline
- EPOS agrees with ALICE data but HIJING deviates significantly



# 2<sup>nd</sup> order cumulants of net-p

NEW

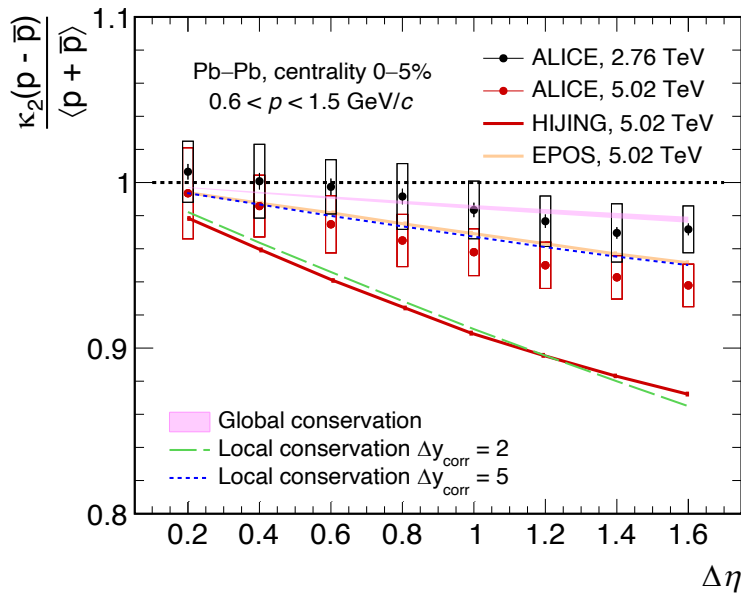
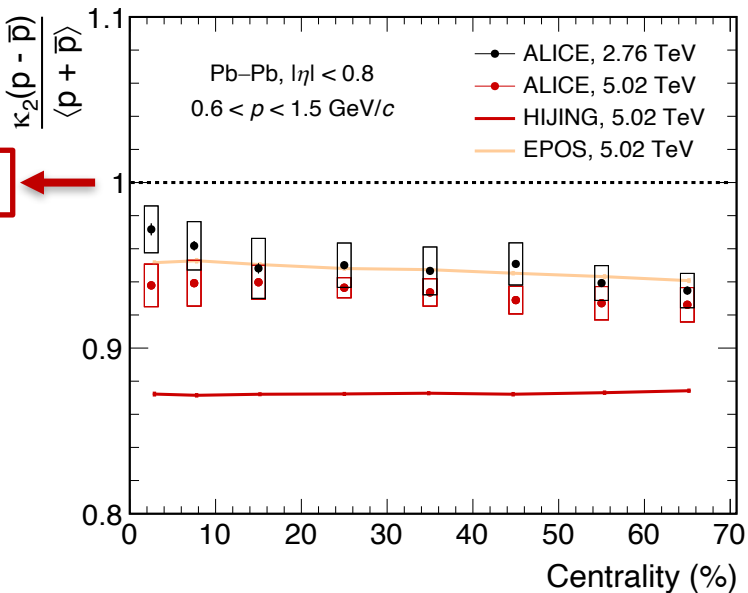


- Deviation from Skellam baseline
- EPOS agrees with ALICE data but HIJING deviates significantly
- **Baryon number conservation?**
  - **ALICE data:** Long range correlations,  $\Delta y = \pm 2.5$  unit or longer → **Earlier in time**



# 2<sup>nd</sup> order cumulants of net-p

NEW

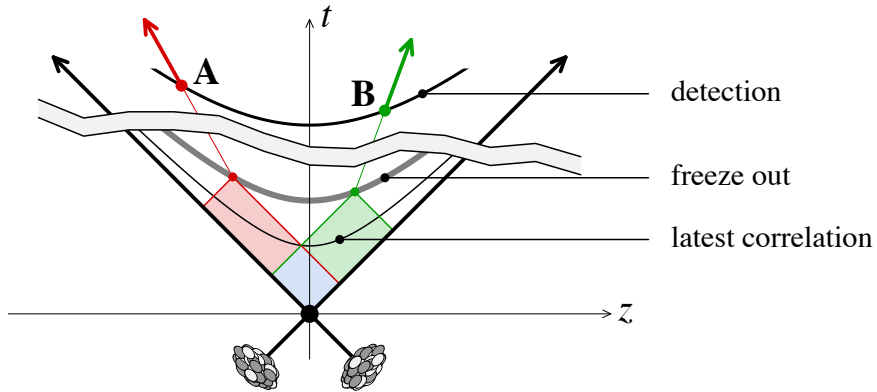


ALICE, arXiv:2206.03343

- Deviation from Skellam baseline
- EPOS agrees with ALICE data but HIJING deviates significantly
- **Baryon number conservation?**
  - **ALICE data:** Long range correlations,  $\Delta y = \pm 2.5$  unit or longer → **Earlier in time**
  - **HIJING:** Short range correlations,  $\Delta y = \pm 1$  unit → **Lund string fragmentation?**



# Lund String Fragmentation

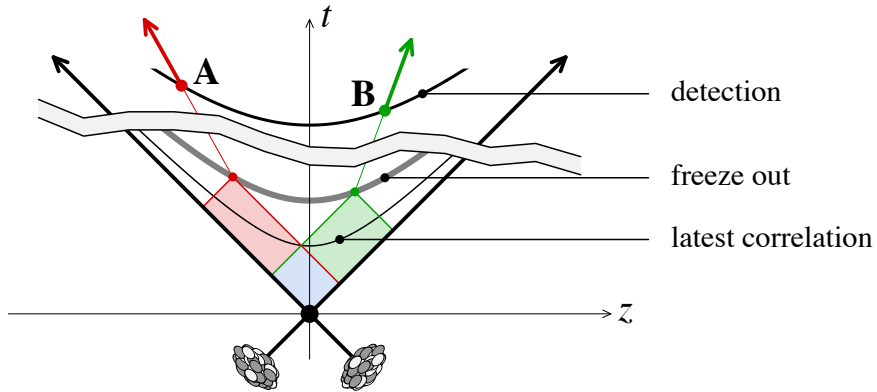


$$\tau \leq \tau_{\text{freeze out}} e^{-\frac{1}{2}|y_A - y_B|}$$

- Only early correlations can be long range in rapidity



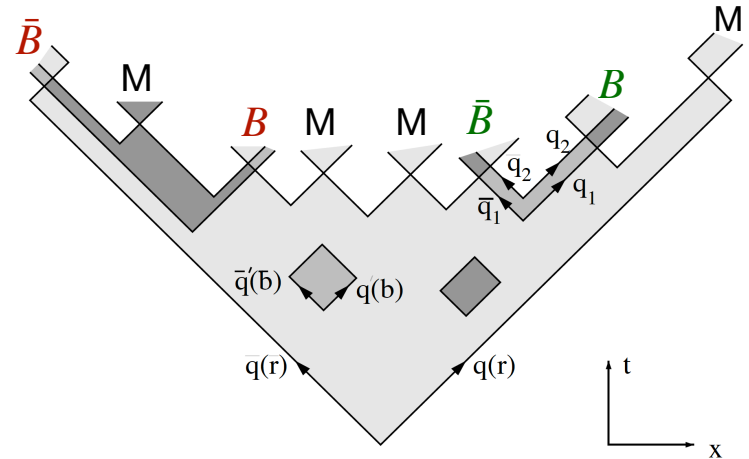
# Lund String Fragmentation



$$\tau \leq \tau_{\text{freeze out}} e^{-\frac{1}{2}|y_A - y_B|}$$

- Only early correlations can be long range in rapidity

## Popcorn mechanism



- Baryon production:  
→  $q\bar{q}$  is replaced by  $qq\bar{q}\bar{q}$  pair

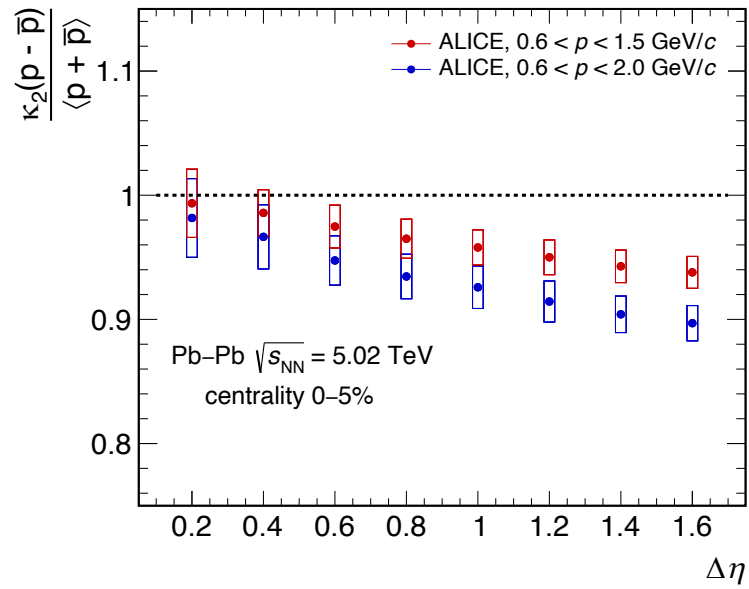
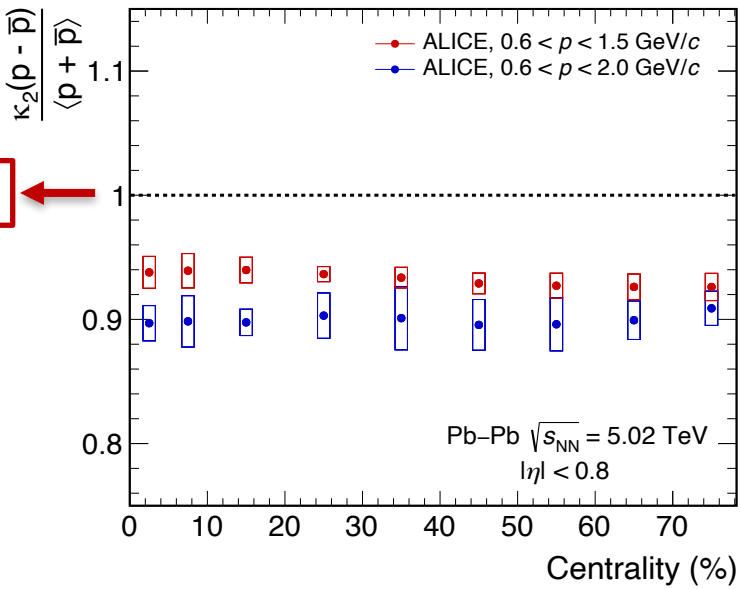
B. Andersson, G. Gustafson, G. Ingelman, T. Sjostrand  
Phys.Rept. 97 (1983) 31-145



# 2<sup>nd</sup> order cumulants of net-p: Acceptance dependence

NEW

Baseline



ALICE, arXiv:2206.03343

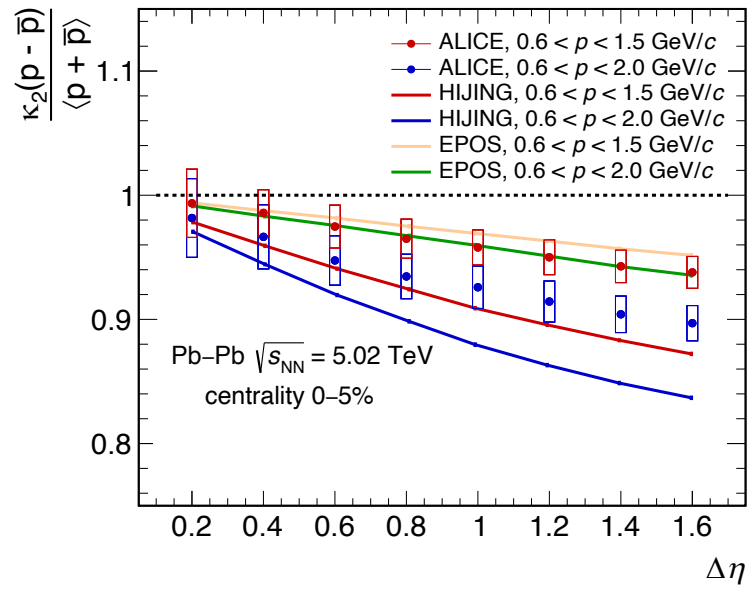
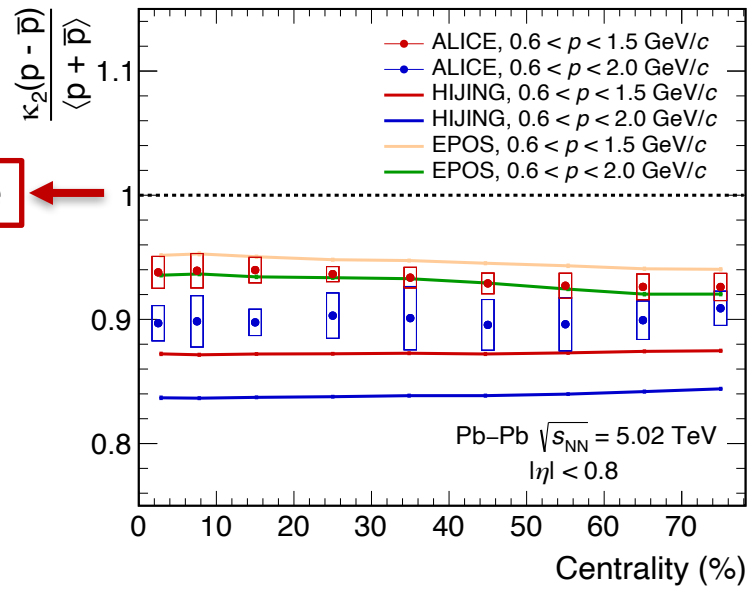
- **Consistent with the baryon number conservation picture**
  - Increase in fraction of accepted p,  $\bar{p}$  → stronger constraint of fluctuations due to baryon number conservation



# 2<sup>nd</sup> order cumulants of net-p: Acceptance dependence

NEW

Baseline



- **Consistent with the baryon number conservation picture**
  - Increase in fraction of accepted  $p, \bar{p} \rightarrow$  stronger constraint of fluctuations due to baryon number conservation
- **EPOS & HIJING** show this drop qualitatively

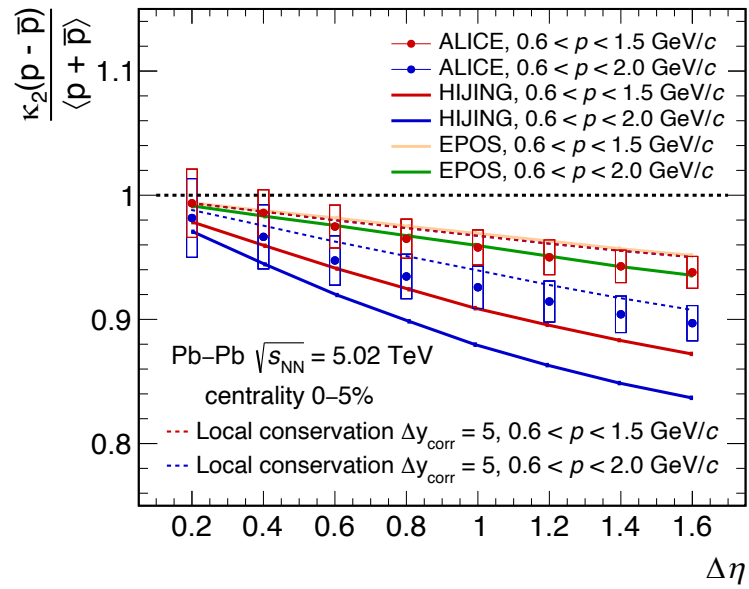
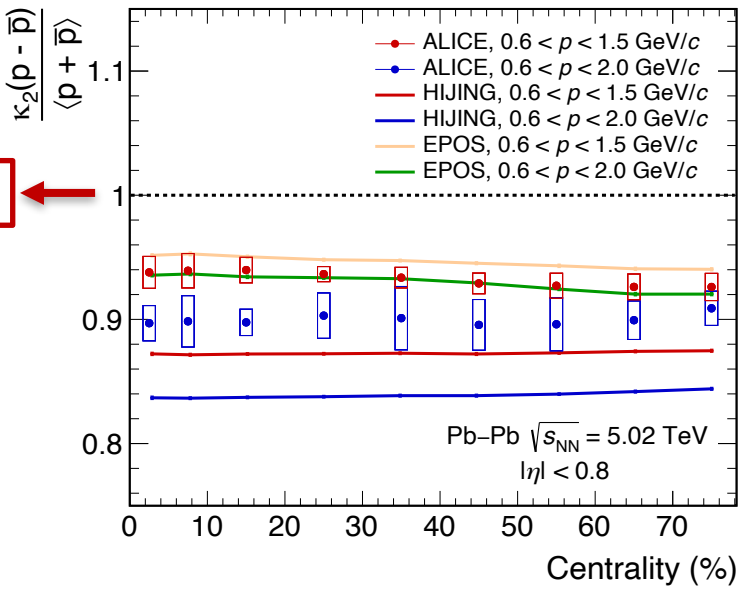




# 2<sup>nd</sup> order cumulants of net-p: Acceptance dependence

NEW

Baseline



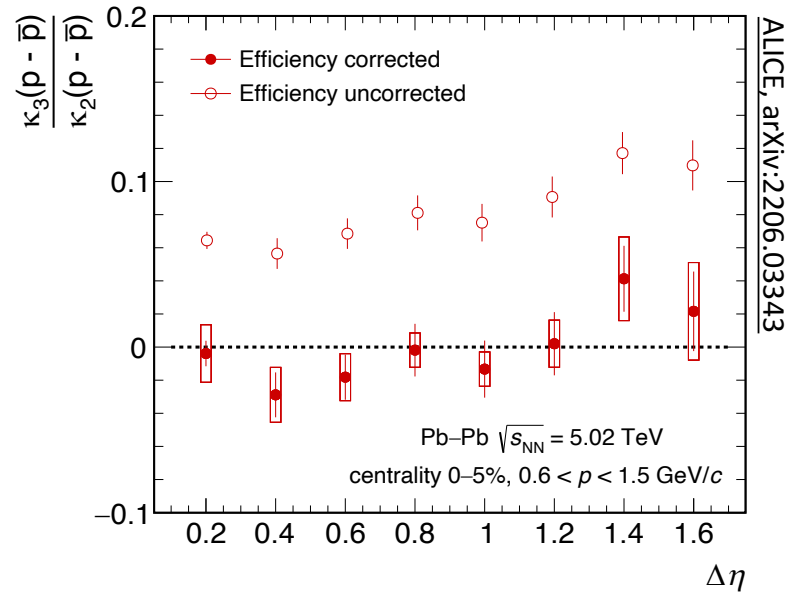
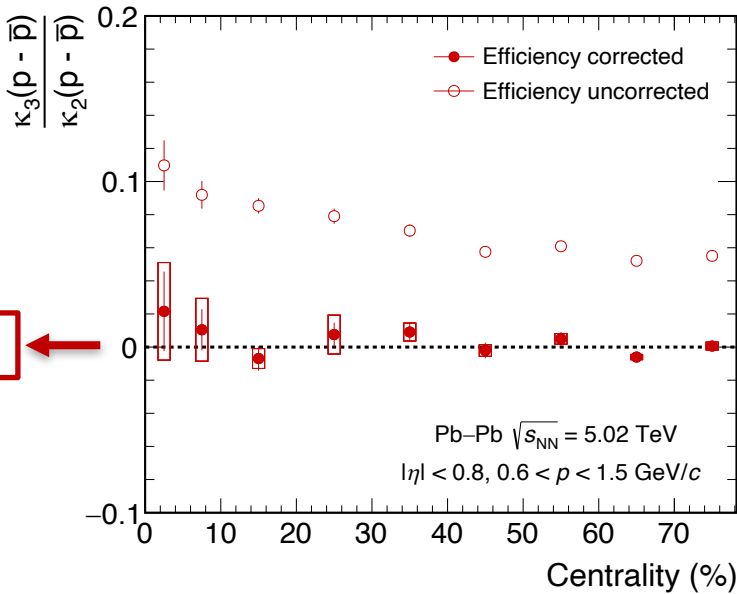
ALICE, arXiv:2206.03343

- **Consistent with the baryon number conservation picture**
  - Increase in fraction of accepted  $p, \bar{p} \rightarrow$  stronger constraint of fluctuations due to baryon number conservation
- **EPOS & HIJING** show this drop qualitatively



# 3<sup>rd</sup> order cumulants of net-p

NEW

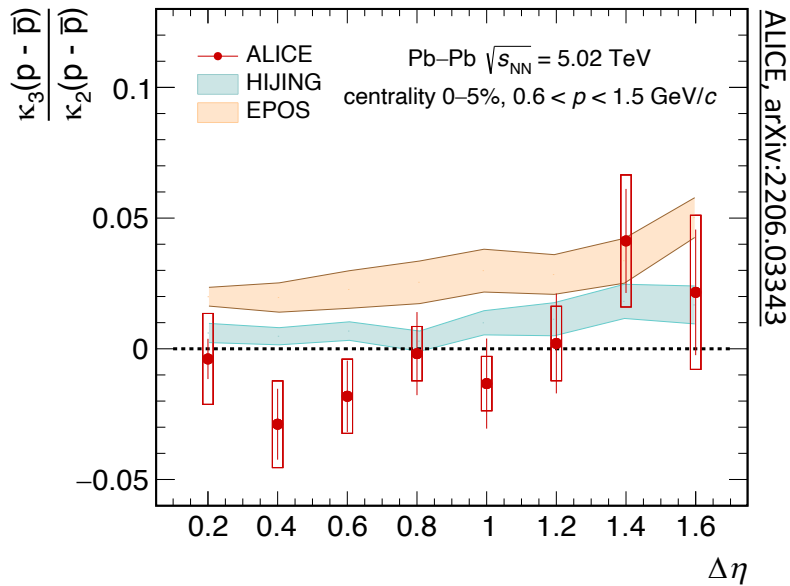
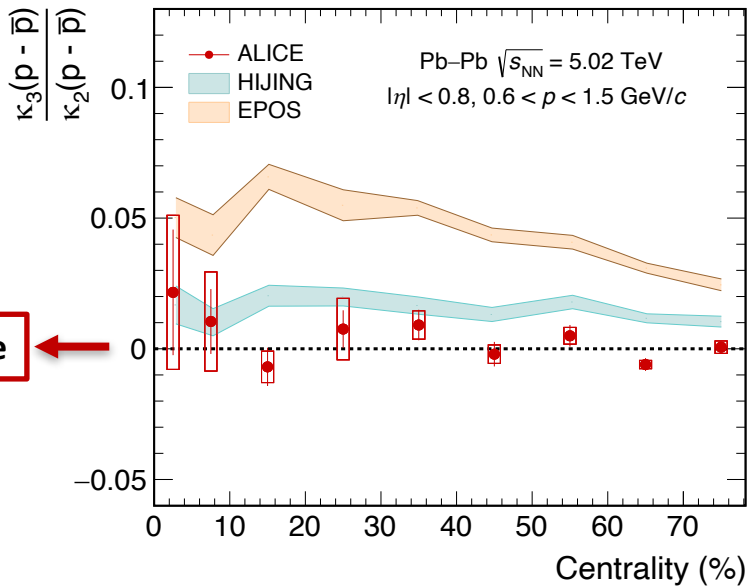


- Data agree with Skellam baseline “0” →  $\mu_B$  is very close to 0 at LHC energies
- Achieved precision of **better than 4%**



# 3<sup>rd</sup> order cumulants of net-p

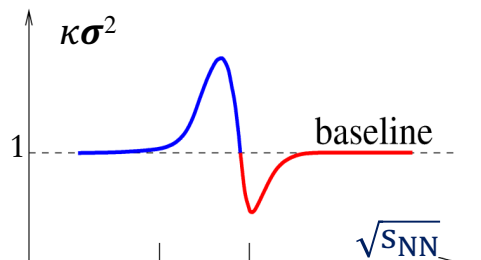
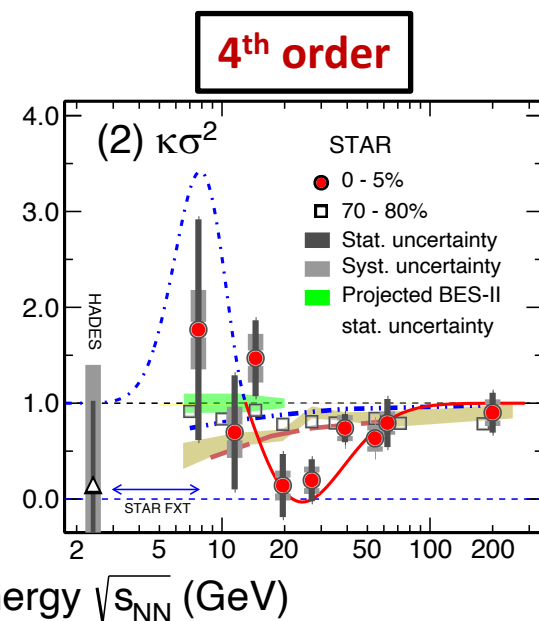
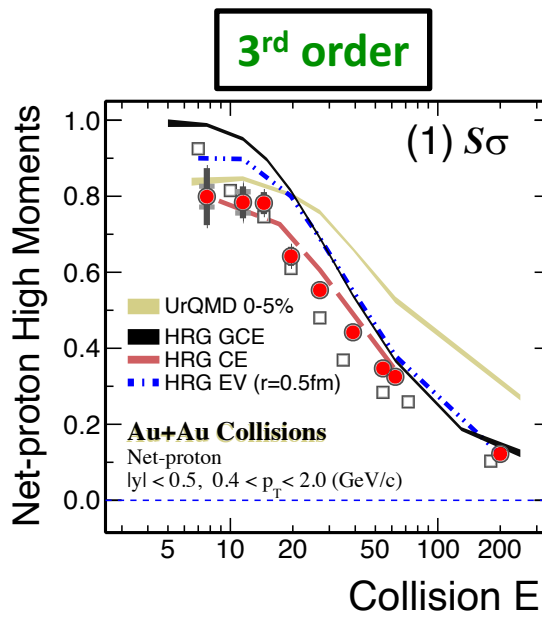
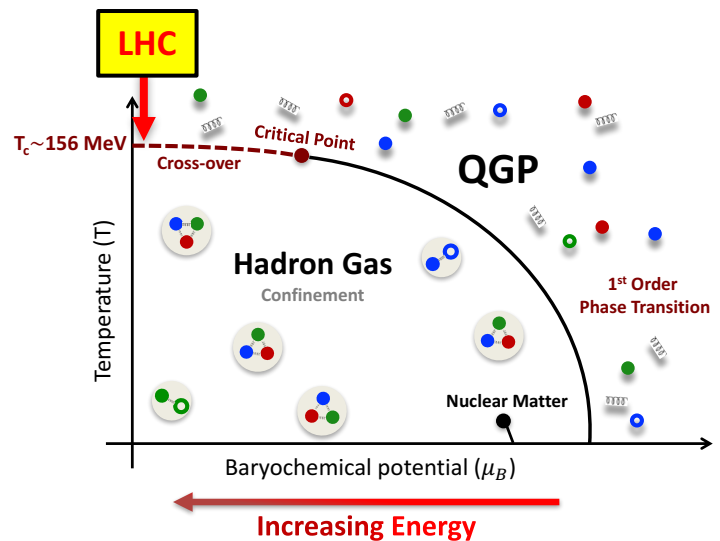
NEW

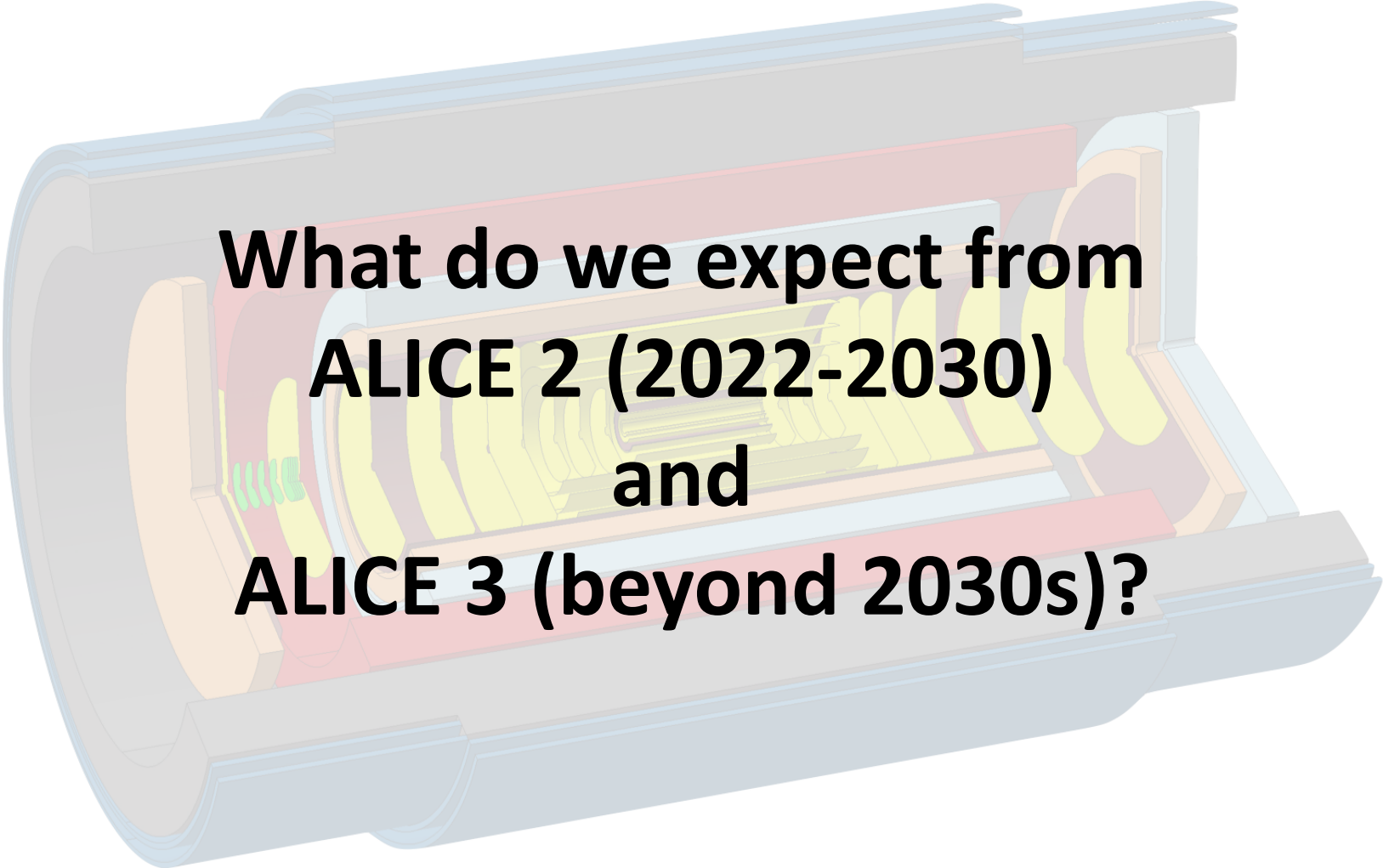


- Data agree with Skellam baseline “0” →  $\mu_B$  is very close to 0 at LHC energies
- Achieved precision of **better than 4%**
- **EPOS and HIJING deviate from “0”**
  - They conserve global charge but  $p/\bar{p}$  deviates from unity:  $1.025 \pm 0.004$  (EPOS),  $1.008 \pm 0.002$  (HIJING)
  - **Volume fluctuations** for 2<sup>nd</sup> and 3<sup>rd</sup> order cumulants are not negligible



# From STAR to LHC current status

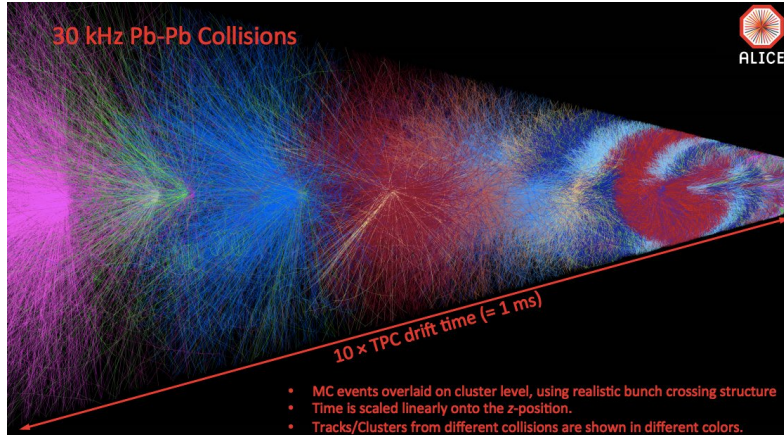


A 3D cutaway diagram of the ALICE detector, showing its complex internal structure. The detector is cylindrical and composed of several concentric layers. The outermost layer is a blue-grey shell. Inside, there are red and orange layers, followed by a central region with yellow and green components. The text is overlaid on the central part of the detector.

**What do we expect from  
ALICE 2 (2022-2030)  
and  
ALICE 3 (beyond 2030s)?**

# Future of conserved charge fluctuations in ALICE

## ALICE 2 (2022-2030)

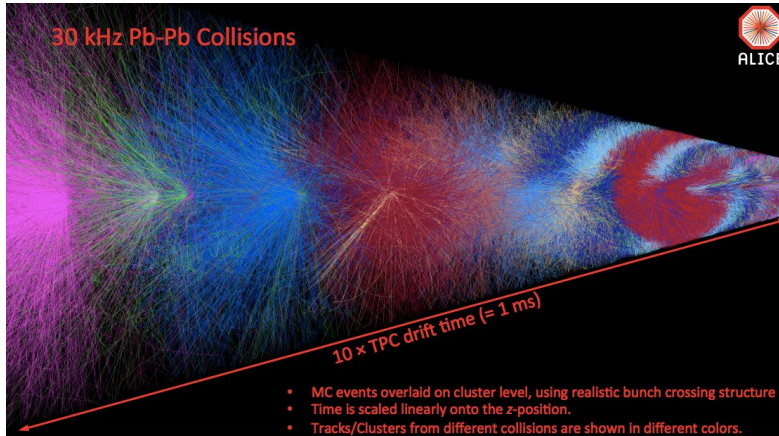


- ✓ **Continuous readout:**
  - ~ 50 kHz Pb-Pb min. bias
  - ~ 5 pileup events within the TPC
- ✓ **Improved vertexing**
- ✓ **High tracking efficiency at low  $p_T$**



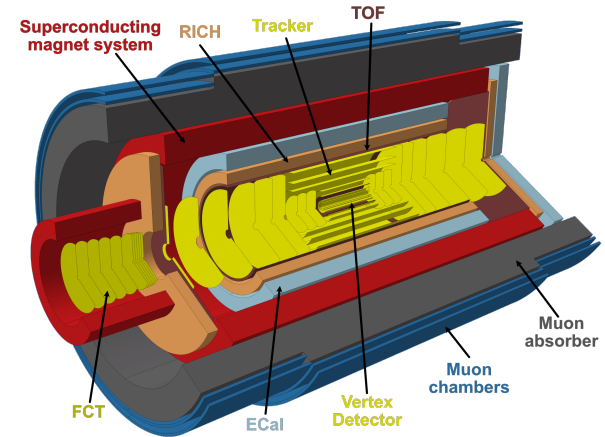
# Future of conserved charge fluctuations in ALICE

## ALICE 2 (2022-2030)



- ✓ **Continuous readout:**
  - $\sim 50$  kHz Pb-Pb min. bias
  - $\sim 5$  pileup events within the TPC
- ✓ **Improved vertexing**
- ✓ **High tracking efficiency at low  $p_T$**

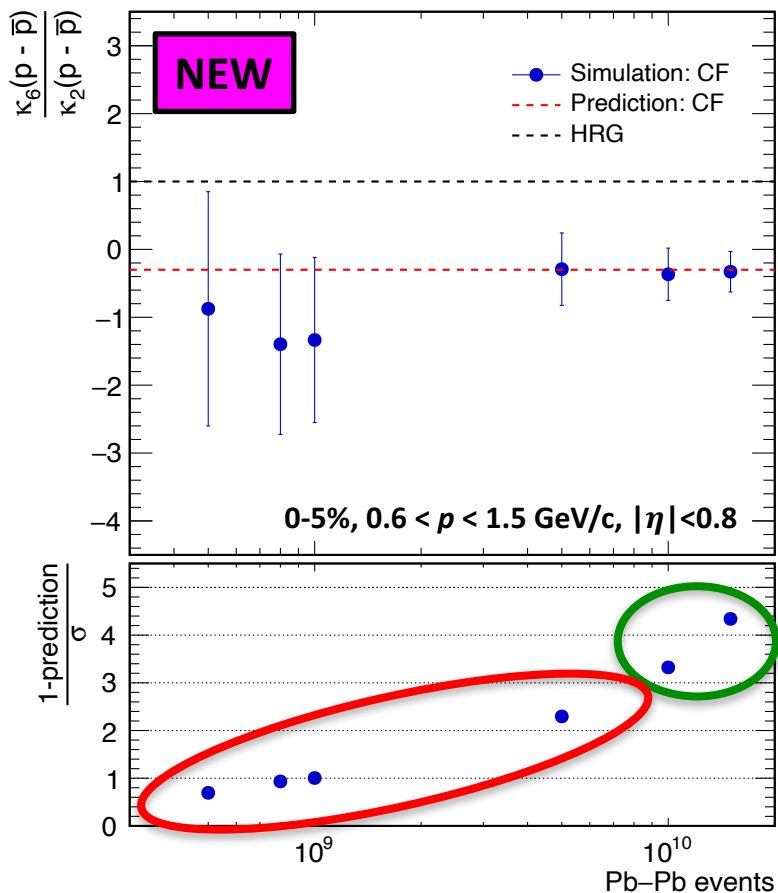
## ALICE 3 (beyond early 2030s)



- ✓ **High statistics** →  $O(10^9)$  billion events
- ✓ **Large acceptance** →  $|\eta| < 4$
- ✓ **High PID purity** →  $0.3 < p_T < 7$  GeV/c
- ✓ **High efficiency** →  $\sim 95\%$
- ✓ **Excellent vertexing** →  $O(3\mu\text{m})$  resolution



# Criticality in ALICE 2 and 3: 6<sup>th</sup> and higher order cumulants



➤ Simulation of the Critical Fluctuations (CF) is based on PQM model  
G. A. Almasi, B. Friman, and K. Redlich, *Phys. Rev.D*96 (2017), 014027

➤ **ALICE 2:**

→ More than 5 billion central Pb-Pb collisions is required

➤ **ALICE 3:**

→ **x3 larger statistics:**  $>4\sigma$  significance with ALICE 2 acceptance

**Net baryon and net strangeness fluctuations  
for  $|\eta| \leq 4$  and for 6<sup>th</sup> and higher order**

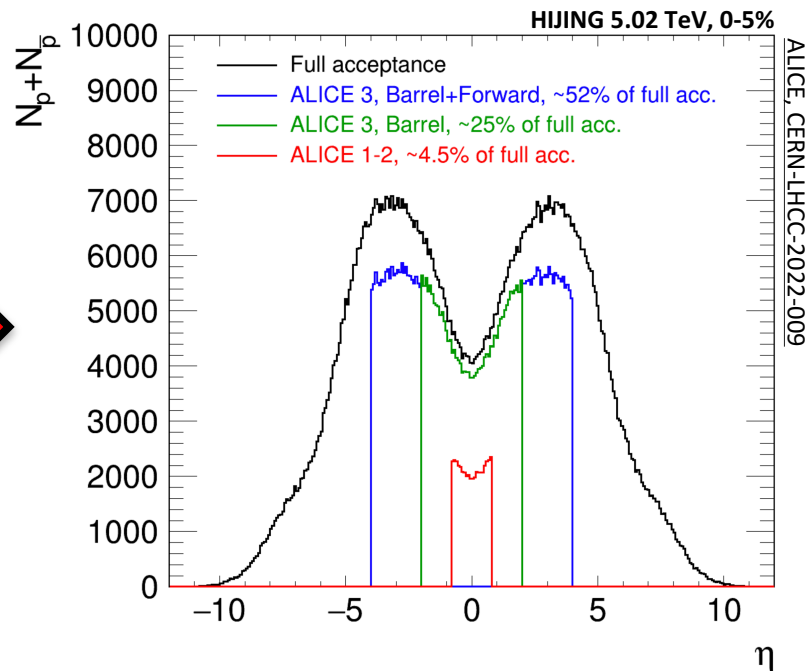
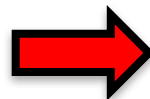
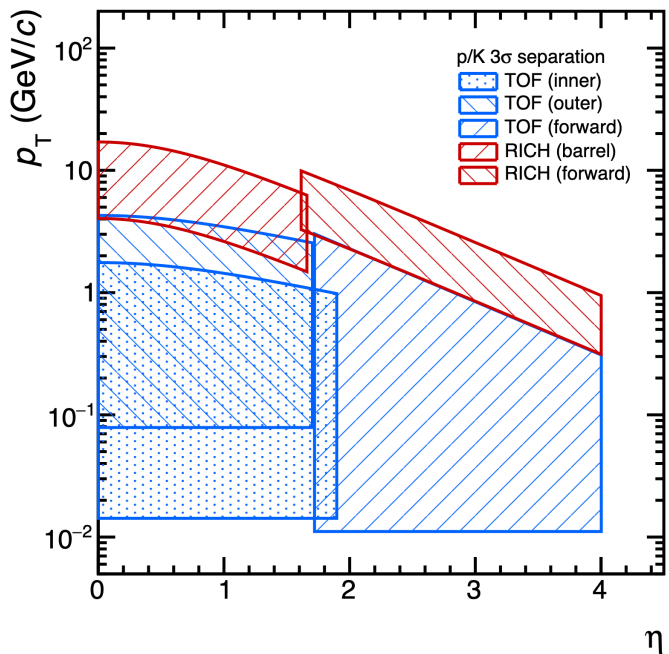




# ALICE 3: High PID purity in large kinematic acceptance

NEW

- ✓ Significant increase in the number of measured protons
- ✓ Larger acceptance: in  $p_T$  and  $\eta$ : ( $0.3 < p < 7$  GeV/c,  $|\eta| < 4$ )
- ✓ Smaller systematics: high PID purity and efficiency

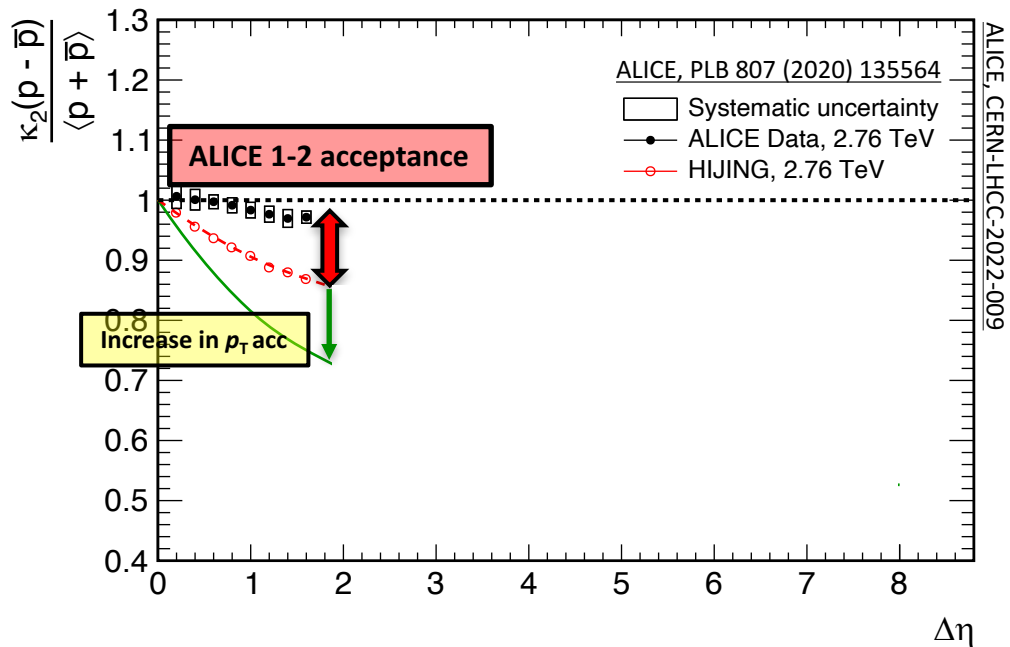


High precision & more differential measurements



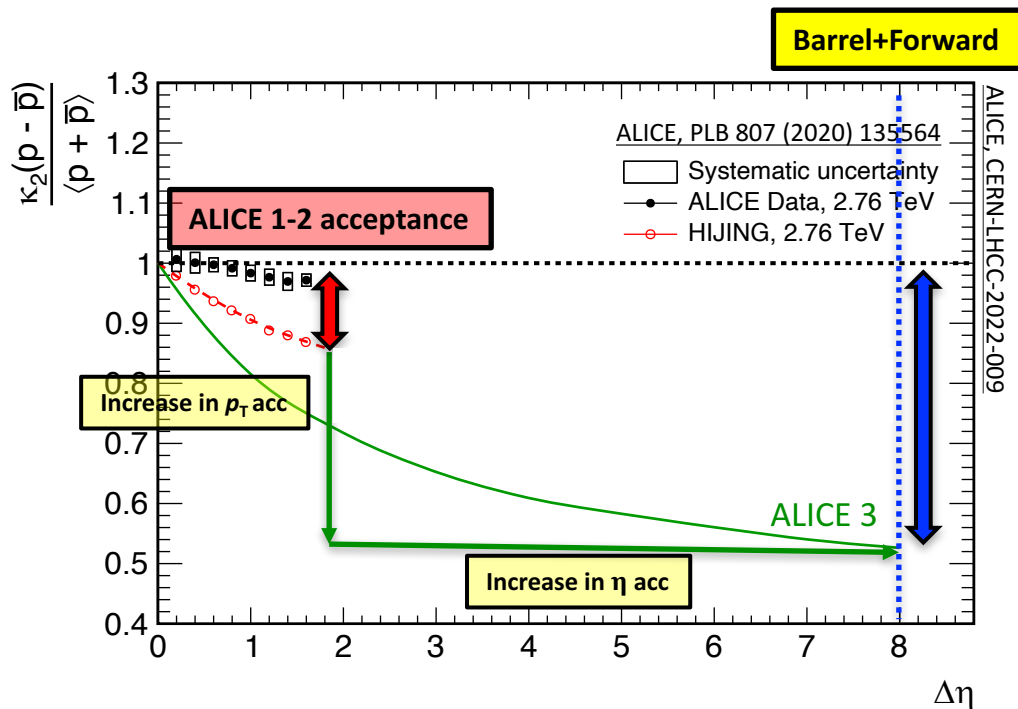
# ALICE 3: Correlation length $\rightarrow$ Baryon number conservation

NEW



# ALICE 3: Correlation length $\rightarrow$ Baryon number conservation

NEW



- Precise mapping of **correlation length of conserved charges, B, S, C**
- **Constraining individual dynamic signals** such as volume fluctuations, baryon number conservation, thermal blurring, annihilation, effect of hydrodynamic evolution etc.



# Summary

## What did we learn from ALICE 1?

- **Net-Q,S fluctuations:** → resonance contributions
- **Net-p fluctuations:**
  - ✓ **1<sup>st</sup> order:**  $T_{fo}^{ALICE} \sim T_{pc}^{LQCD}$
  - ✓ **2<sup>nd</sup> order:** Deviation from Skellam baseline is due to baryon number conservation
    - Long range correlations originating from **early phase of the collision**
  - ✓ **3<sup>rd</sup> order:** Up to 3<sup>rd</sup> order ALICE data agree with the LQCD expectations
    - $\mu_B$  is very close to 0 at LHC energies

## What do we expect from ALICE 2-3?

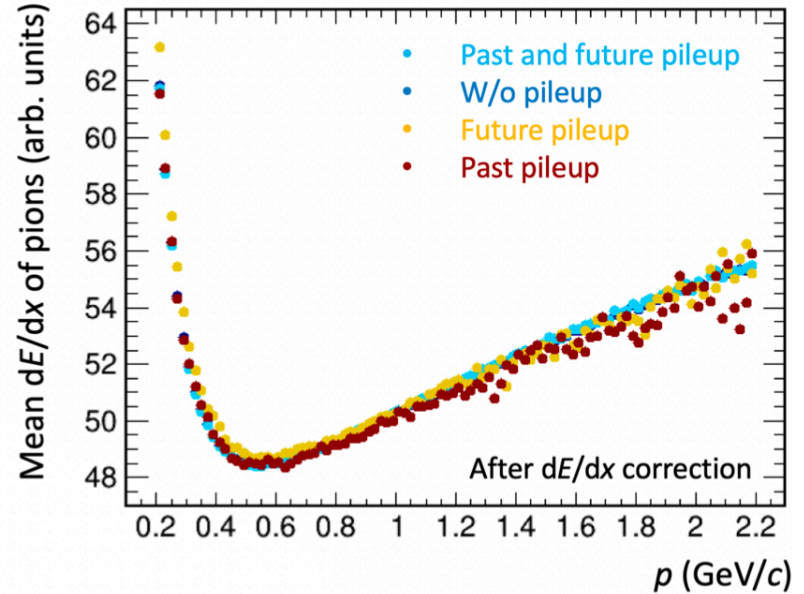
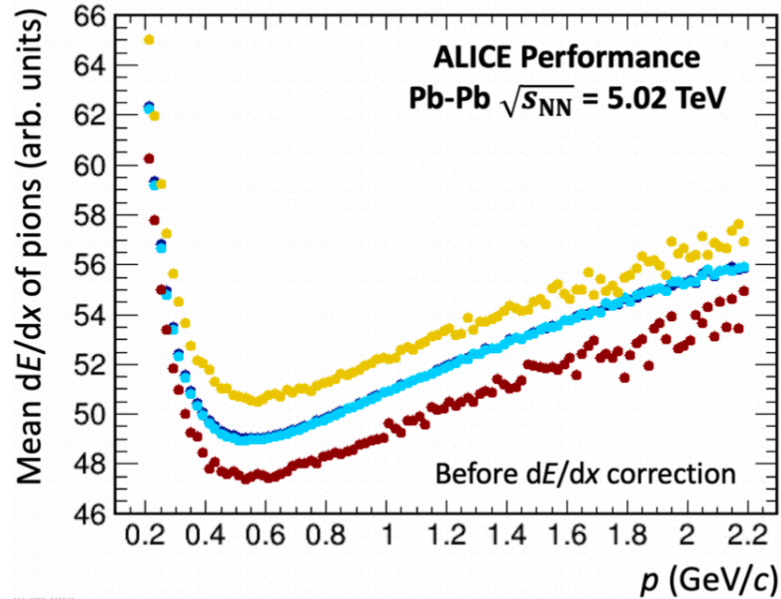
- **Criticality signals at 6<sup>th</sup> and higher order cumulants for B and S**
- Constraining **individual dynamic signals**
- **Correlation length** of conserved charges: B, S, C
- ...



**BACKUP**

# Effect of event pileup

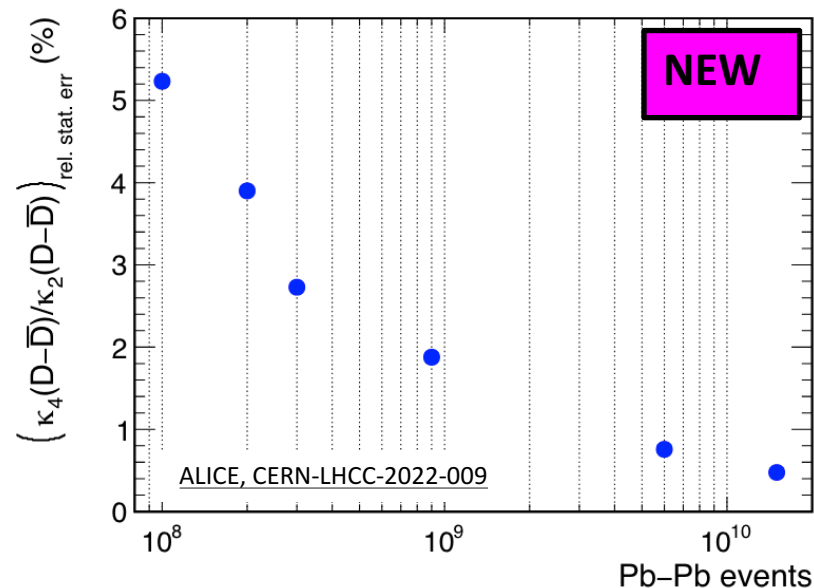
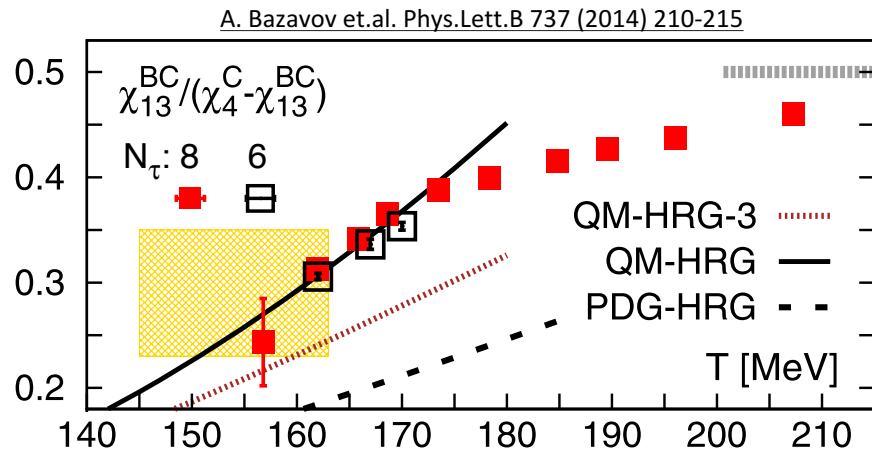
NEW



ALICE-PHNF-500043



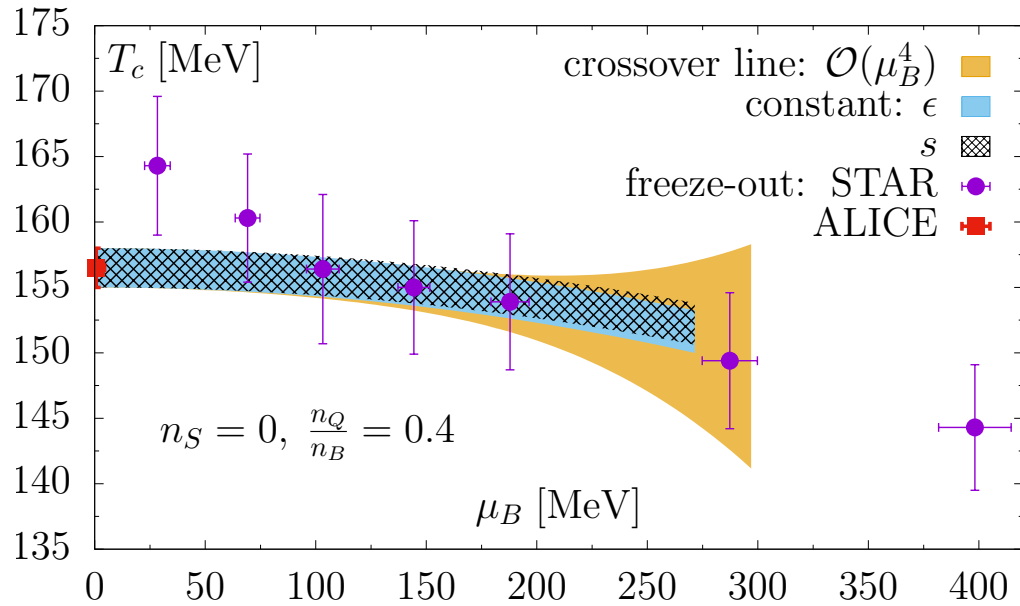
# ALICE 3: Net-charm fluctuations



- **2<sup>nd</sup> order** → **Correlation length of charm**
- **4<sup>th</sup> order** → Close to  $T_{pc}$  charmed baryon fluctuations are about 50% larger than expected in a HRG based on known charmed baryon resonances (PDG-HRG) → **missing states of QCD**



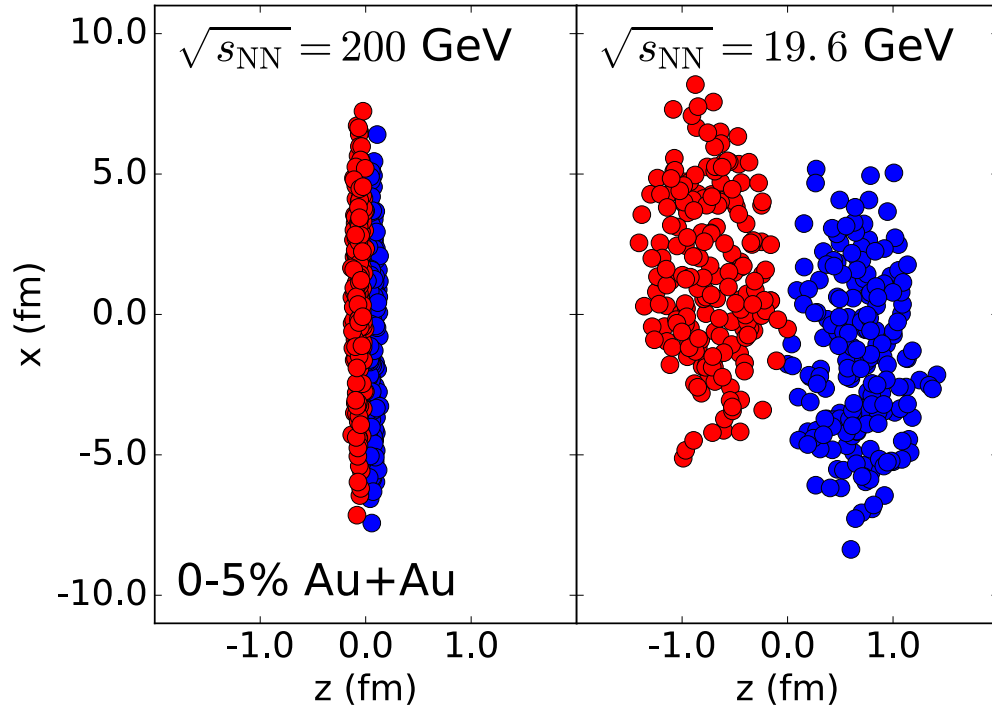
$$T_{pc} = 156.5 \pm 1.5 \text{ MeV} \approx T_{fo}^{\text{ALICE}}$$



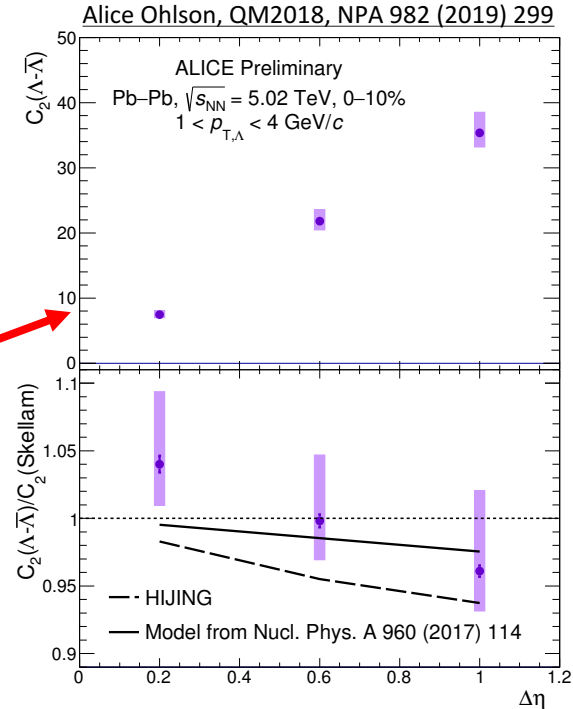
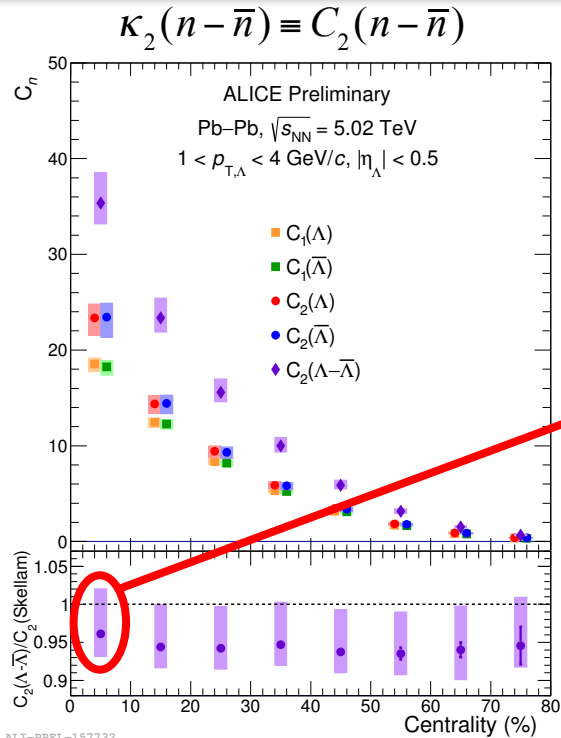
A. Andronic et.al. Nature 561 (2018) 321  
 HotQCD Collaboration, Phys.Lett. B795 (2019) 15,  
 S. Borsanyi et.al. Phys. Rev. Lett. 125, 052001 (2020)







# 2<sup>nd</sup> order Net- $\Lambda$ cumulants

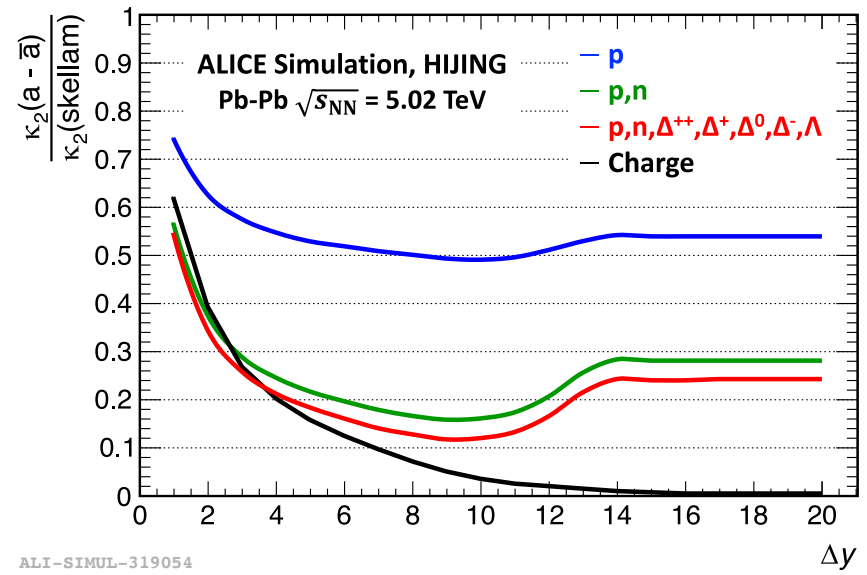
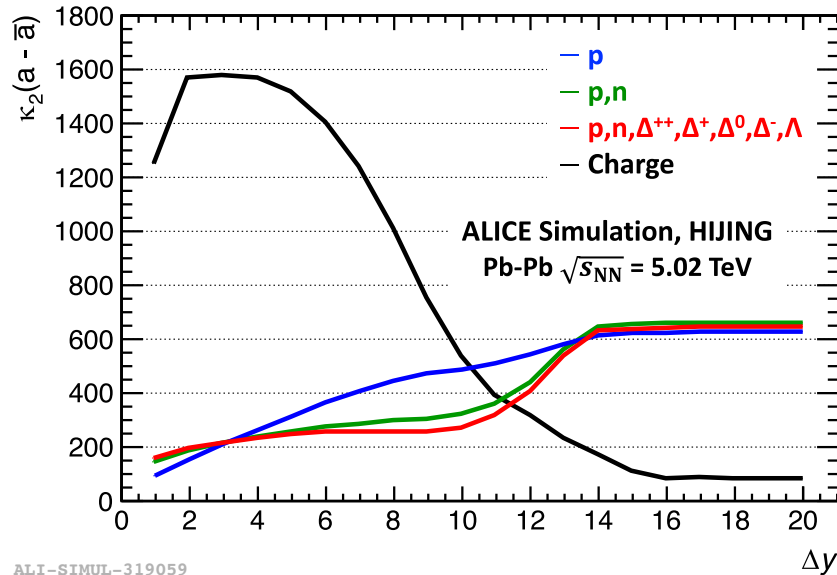


- Similar trend as for **net-p**
- Better precision is needed to disentangle global vs local conservation laws

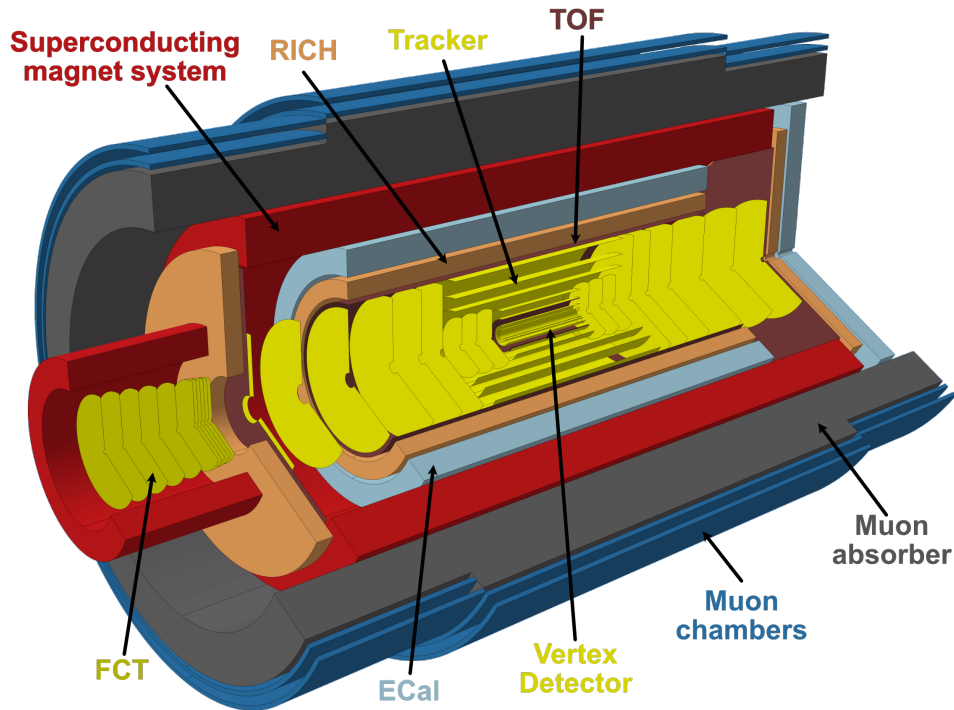


# 2<sup>nd</sup> order cumulants in full phase space

NEW



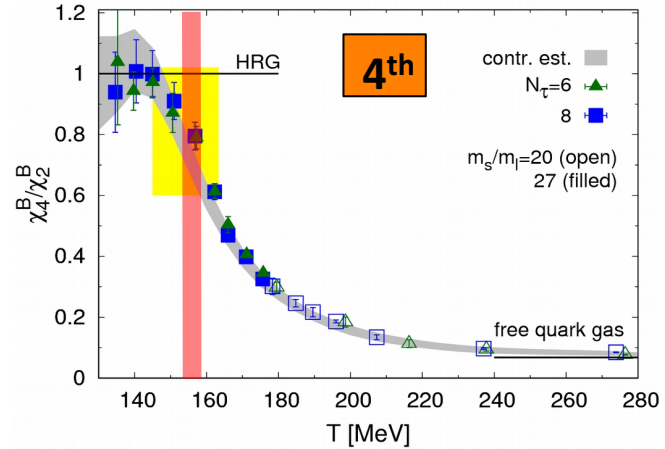
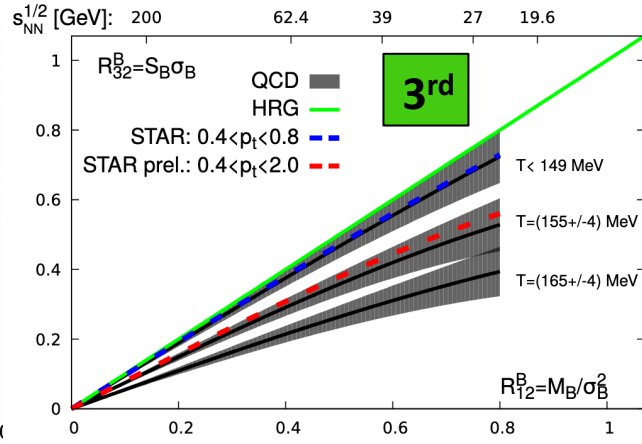
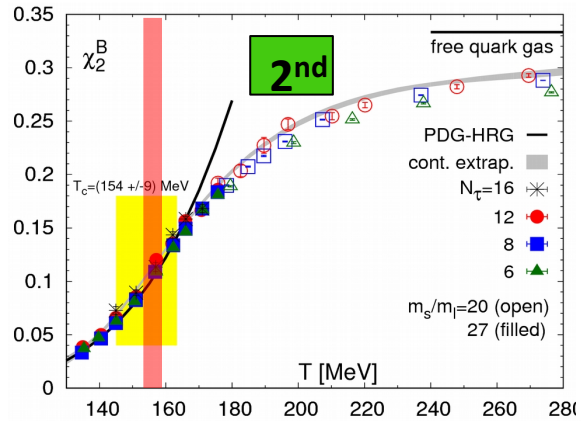
# ALICE 3



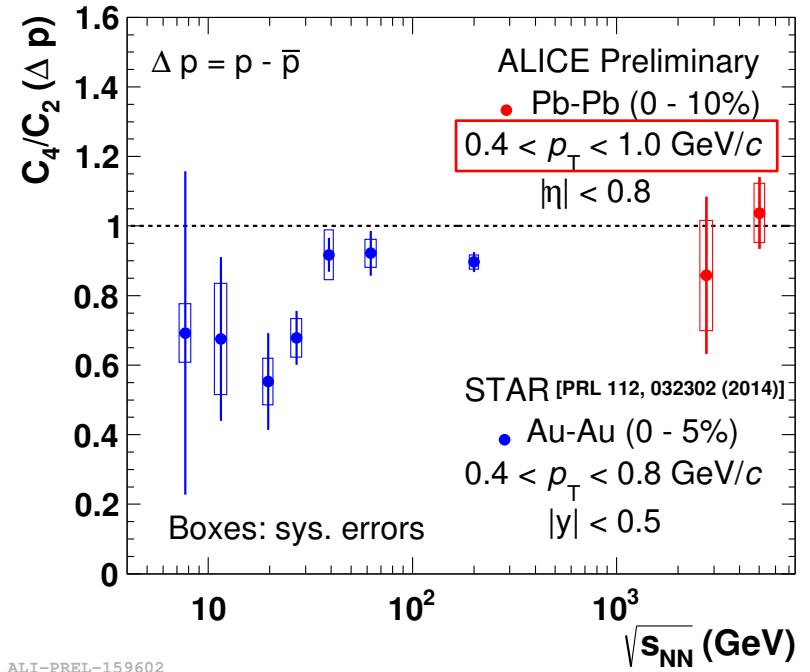
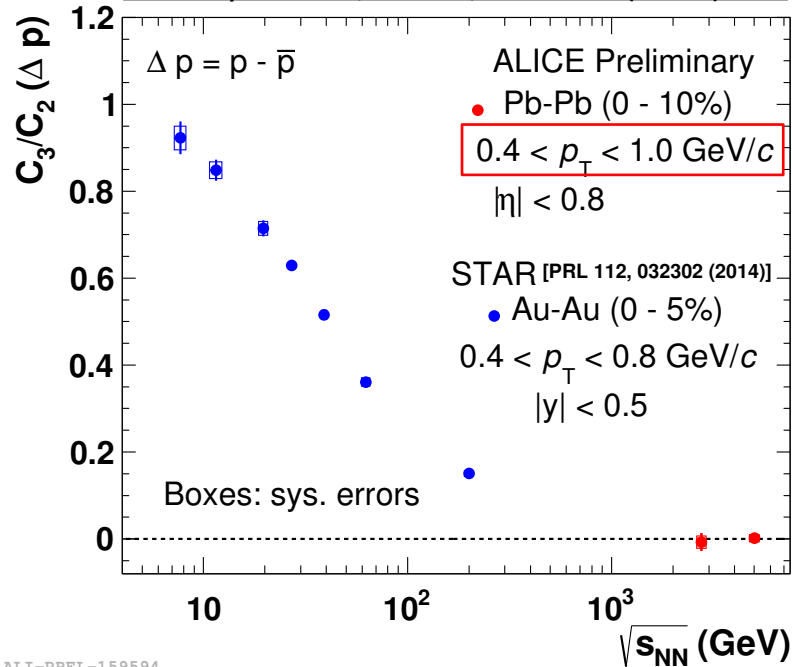
- ⇒ **Ultra-low material budget** for low  $p_T$  tracking
  - $X/X_0 \sim 0.05\%$  / layer
- ⇒ **Fast** to sample large luminosity
  - 50-100 x Run 3/4 → MHz level
- ⇒ **Large acceptance**
  - $|\eta| < 1.4$  (central barrel),  $|\eta| < 4$  (total)
- ⇒ **Excellent spatial resolution** for tracking and vertexing
  - Innermost layers:  $\sigma < 3\ \mu\text{m}$
  - Outer layers:  $\sigma \sim 5\ \mu\text{m}$
- ⇒ **Precise time measurements** for PID
  - $\sigma \sim 20\ \text{ps}$



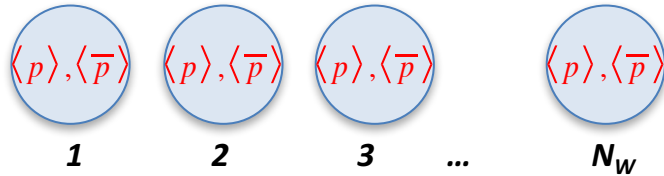
# Link to LQCD



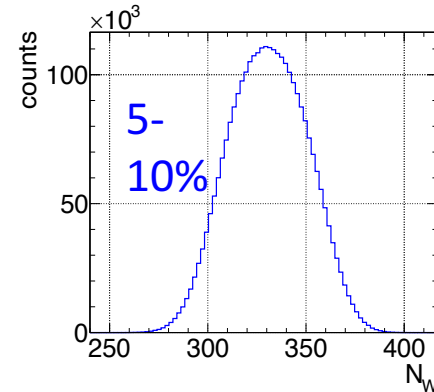
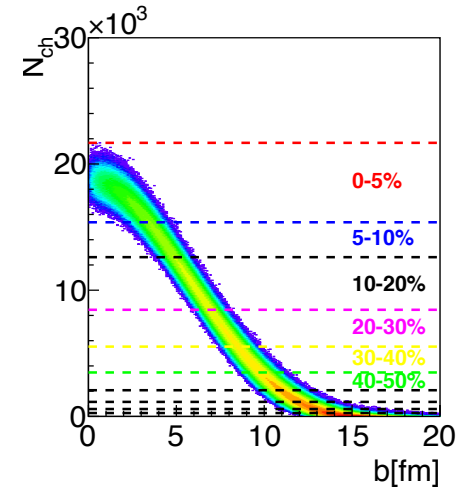
Nirbhay Kubera, QM18, NPA 982 (2019) 851



# Volume Fluctuations

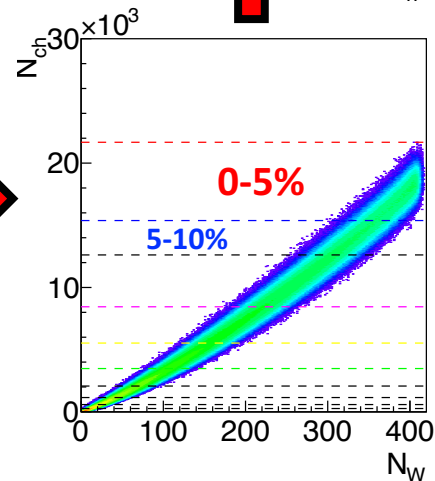
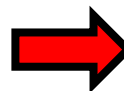
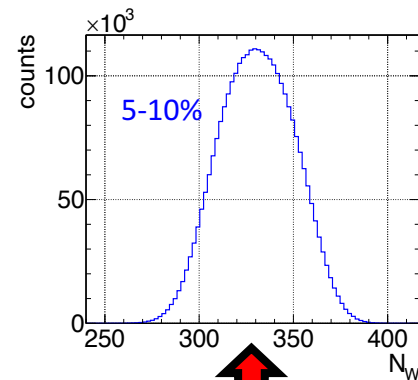
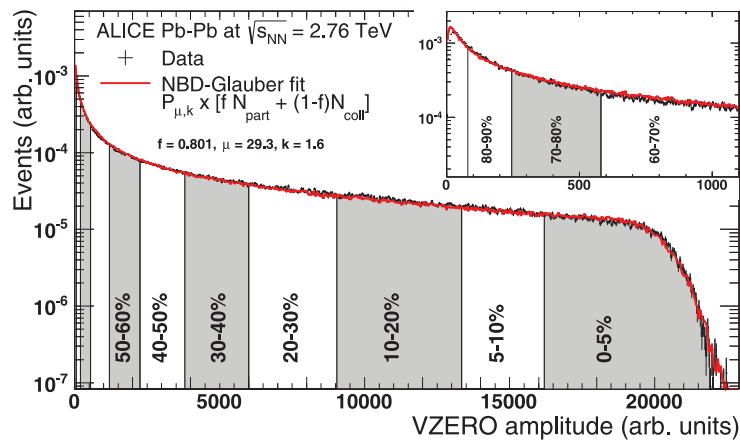
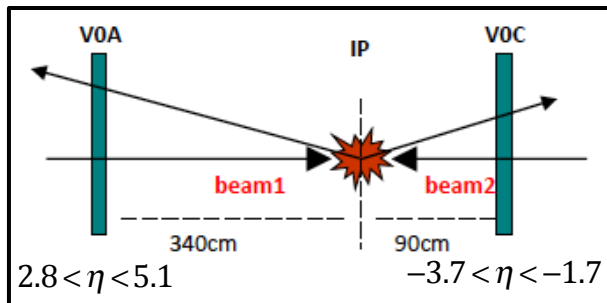


- $N_W$  fluctuates with **MC Glauber initial conditions**
- Each source is treated **Grand Canonically**
- Mean proton multiplicities taken **from real data**
- **Centrality selection like in experimental data**
- **Expected results without volume fluctuations**
  - Particles:  $k_n = N_w \langle n \rangle = \langle p \rangle = \langle \bar{p} \rangle$
  - Net-particles:  $k_n = \langle p \rangle + (-1)^n \langle \bar{p} \rangle$



# Volume Fluctuations

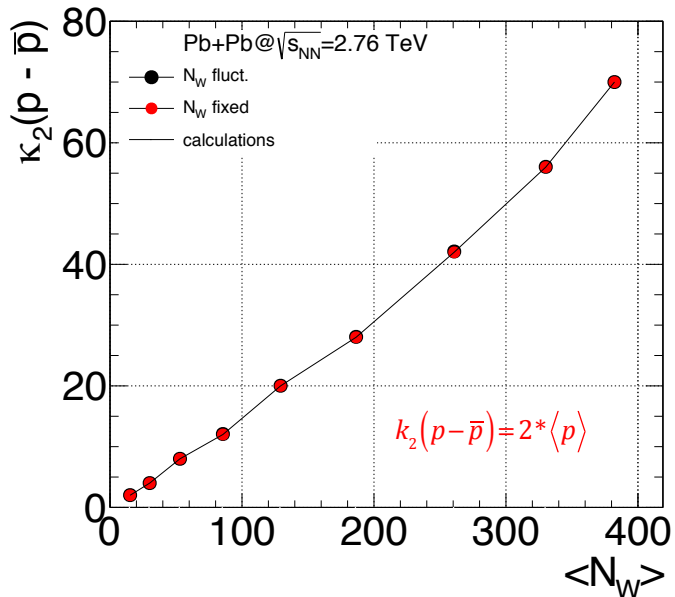
ALICE: Phys.Rev. C88 (2013) no.4, 044909





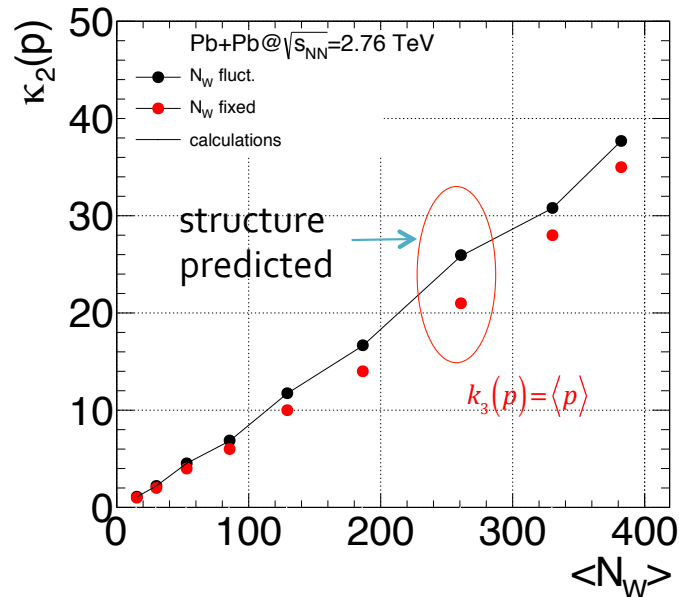
# Volume Fluctuations

150\*10<sup>6</sup> Events



$$k_2(p - \bar{p}) = \langle N_w \rangle k_2(n - \bar{n}) + \langle n - \bar{n} \rangle^2 k_2(N_w)$$

vanishes for ALICE



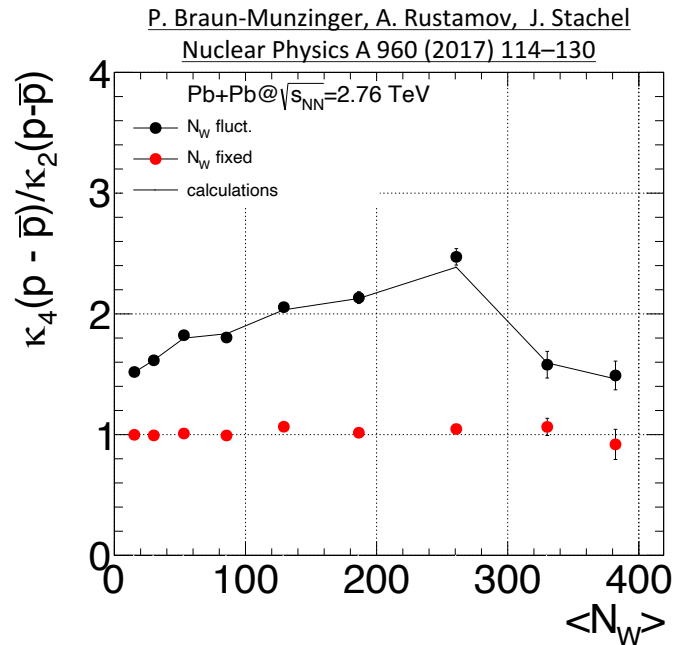
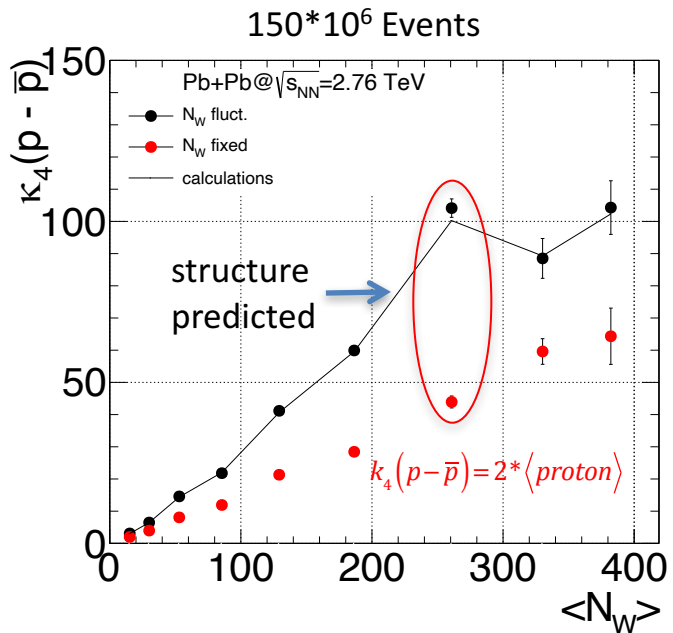
$$k_2(p) = \langle N_w \rangle k_2(n) + \langle n \rangle^2 k_2(N_w)$$

does not vanish

$n, \bar{n}$  from single wounded nucleon



# Volume Fluctuations



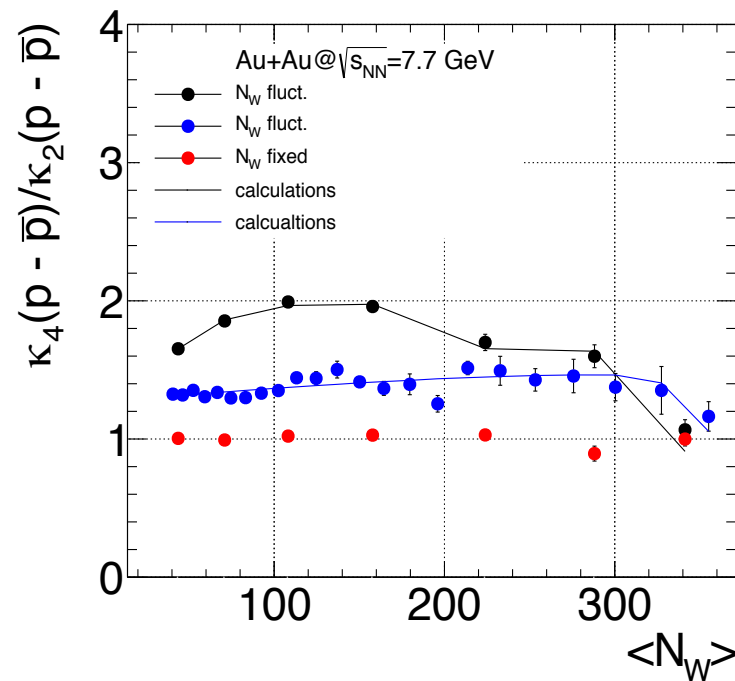
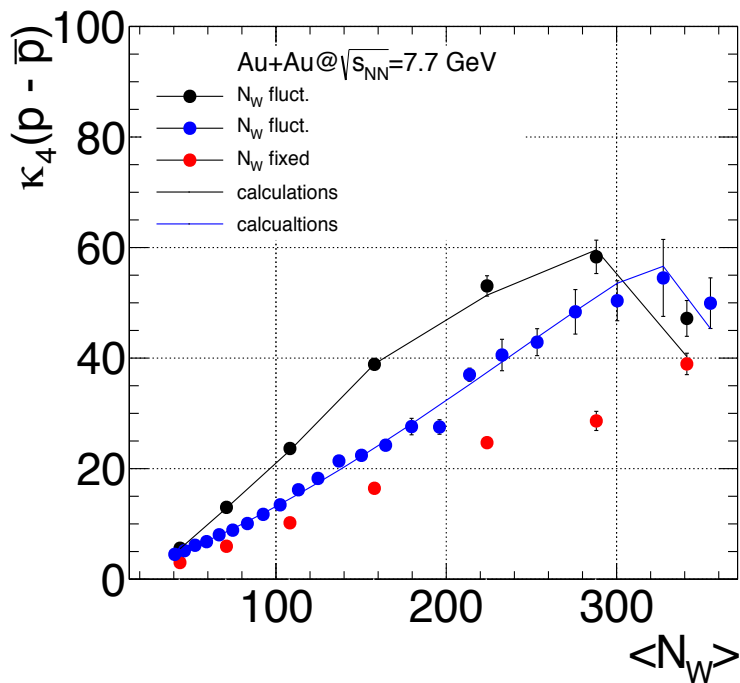
$$\kappa_4(p-\bar{p}) = \langle N_w \rangle \kappa_4(n-\bar{n}) + 3\kappa_2(n-\bar{n})^2 \kappa_2(N_w) + \langle n-\bar{n} \rangle (\dots)$$

$n, \bar{n} \rightarrow$  from single wounded nucleon

vanishes for ALICE

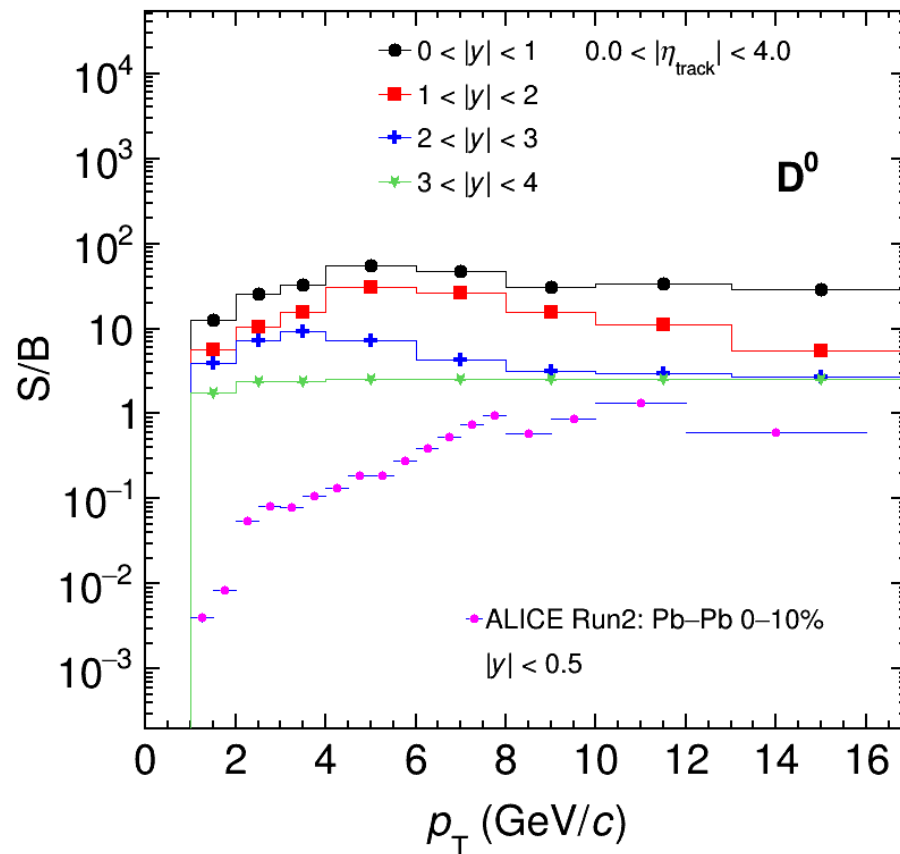


# Volume Fluctuations



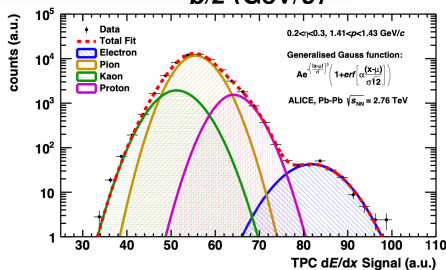
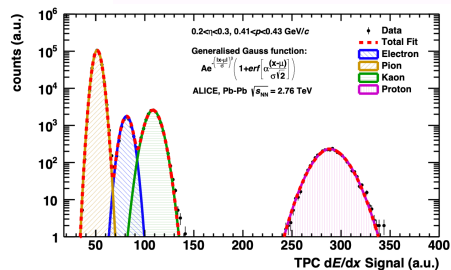
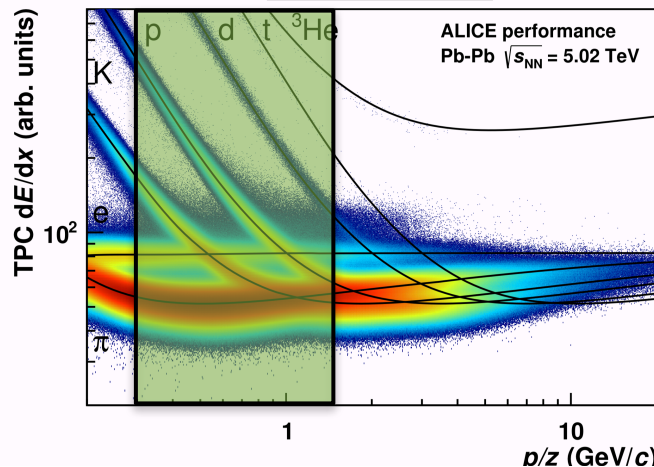
# Excellent vertexing: Charm fluctuations

- **Barrel PID improves S/B by a factor  $\sim 10$** 
  - Close to 'ideal PID'
  - Much smaller systematic uncertainty
- **Net charm fluctuations for  $|\eta| \leq 4$  and up to 4th moments**



# Identity Method in ALICE 3: Purity in PID

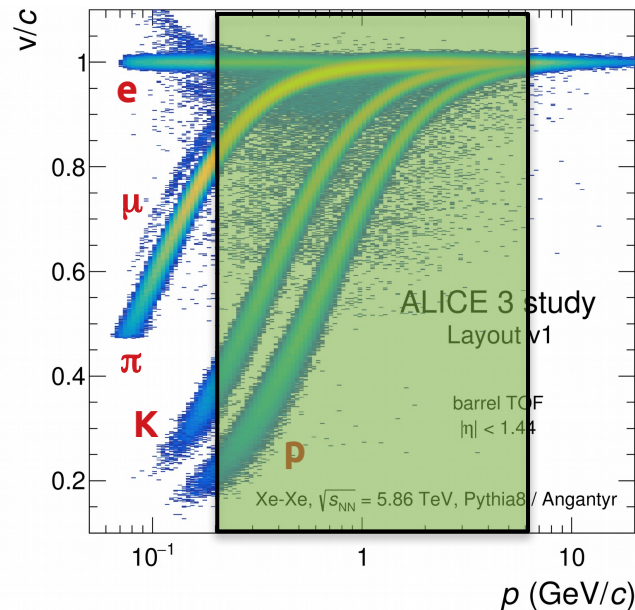
**ALICE 1-2**



- $0.6 < p < 1.5$  GeV/c
- $p > 0.8$  GeV/c  $\rightarrow$  less than one sigma separation

**ALICE 3**

Significant improvement in the purity + IM



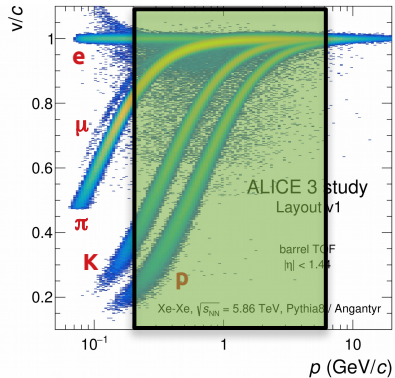
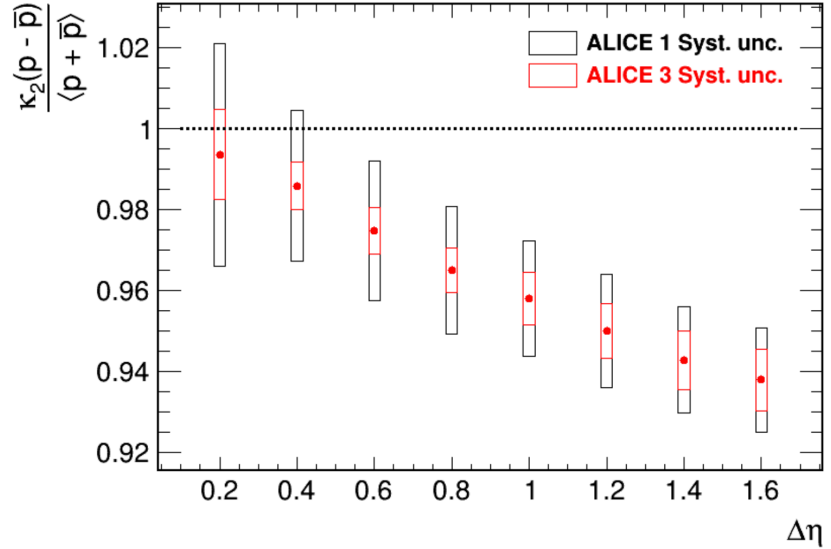
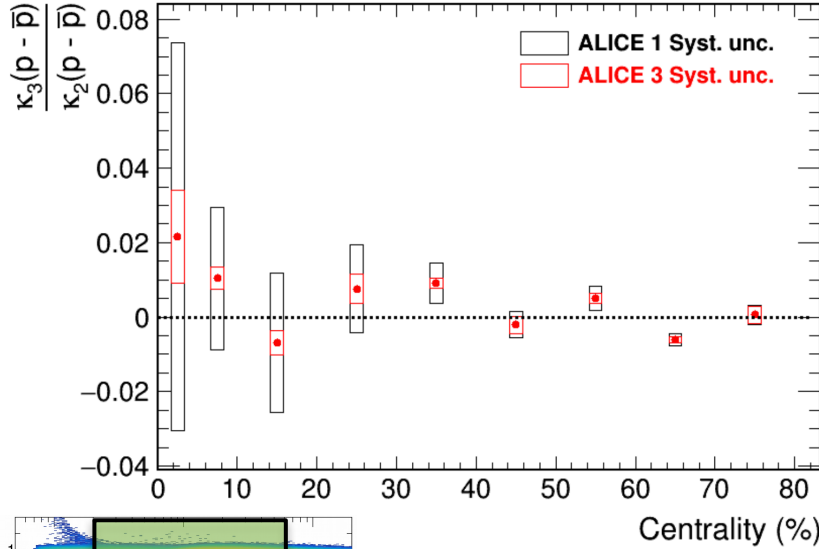
ALI-SIMUL-491825

- $0.3 < p < \sim 7$  GeV/c
- No full overlap of the TOF signal



# ALICE 3: Systematic uncertainties

NEW

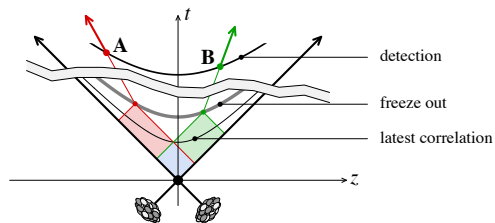
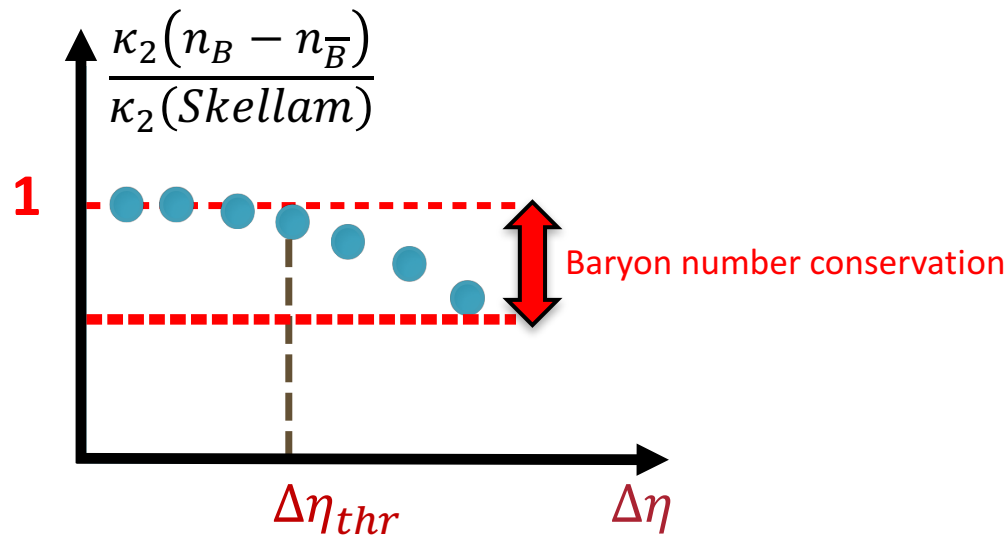
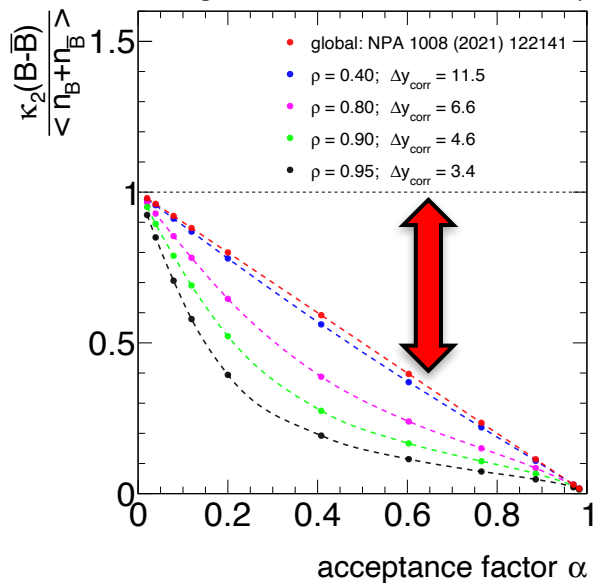


❖ **Main uncertainty is from the  $dE/dx$  fits, which will vanish in ALICE 3 (thanks to Identity Method (IM) and improved PID)**



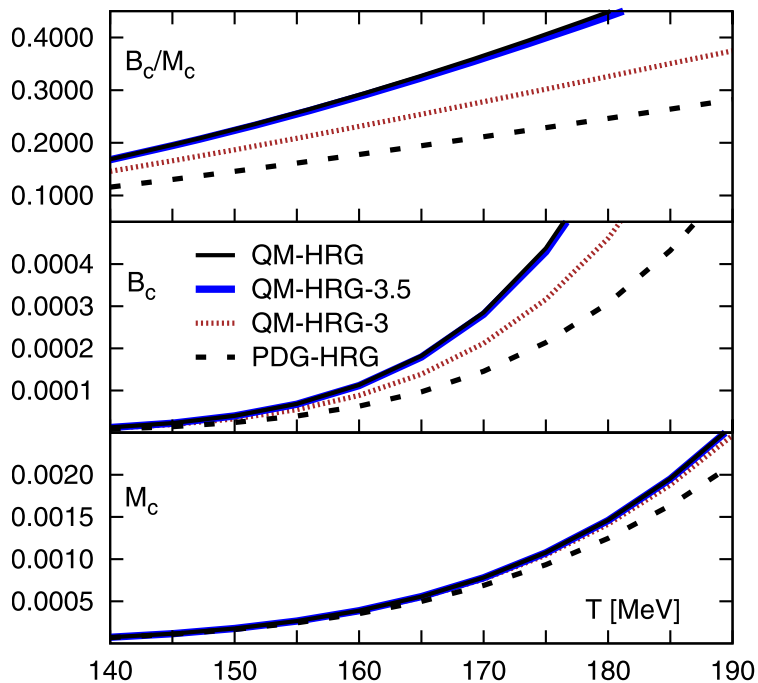
# 2<sup>nd</sup> order cumulants of net-p: Correlation length

P. Braun-Munzinger, A. Rustamov, J. Stachel, to be published



**Early correlations → long range in rapidity**





➤ Partial pressure of open charm mesons ( $M_c$ ) and baryons ( $B_c$ ) in a gas of uncorrelated hadrons,

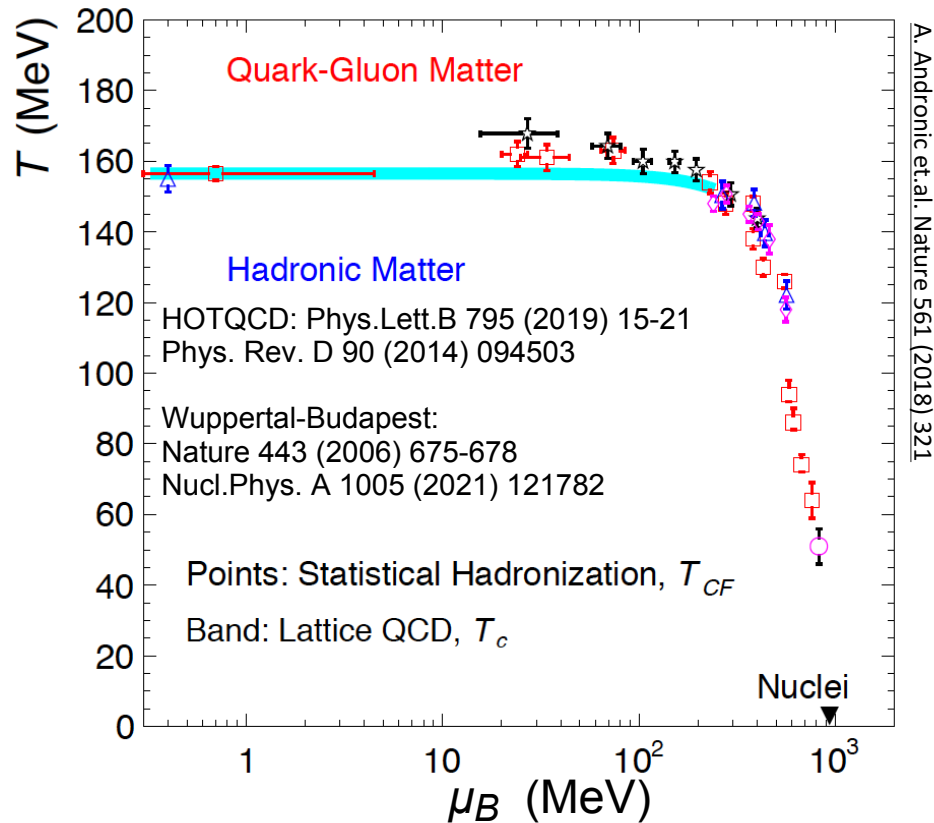
- **PDG-HRG**: All open charm resonances in PDG
- **QM-HRG**: Relativistic quark model.
- **QM-HRG-X**: open charm resonance spectrum is cut off at mass X GeV

➤ Below 160 MeV the latter coincides with the complete QM-HRG model results to better than 1 %.





# Motivation: Nature of the chiral phase transition



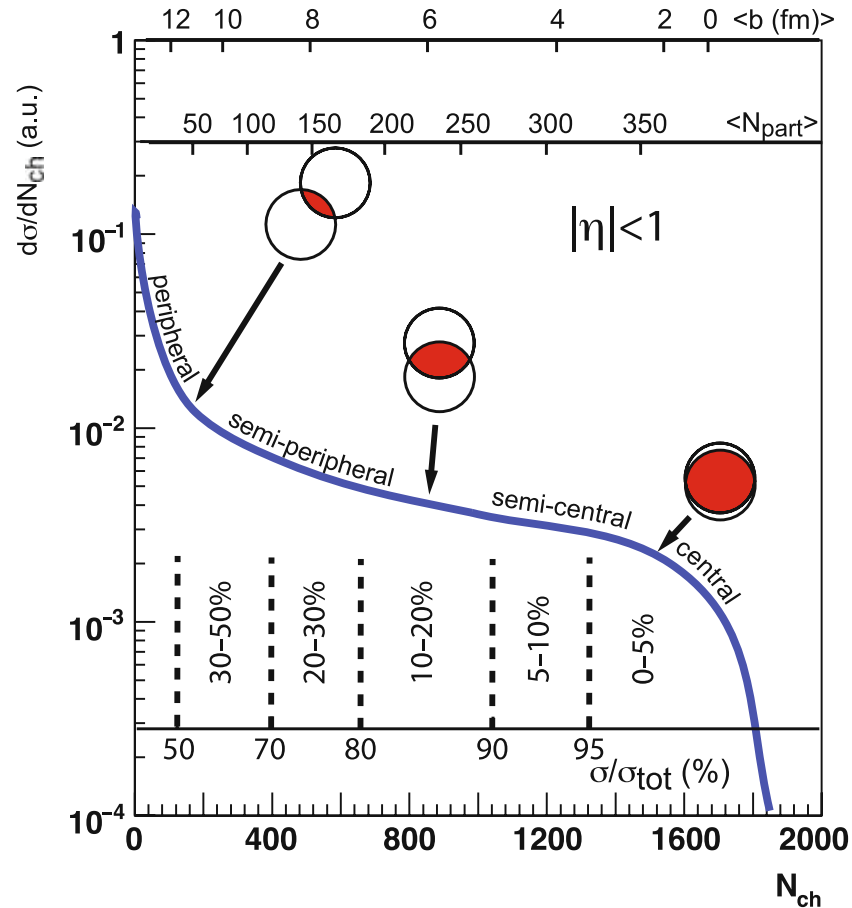
- Quantitative **agreement** of chemical freeze-out parameters **with most recent LQCD predictions** for  $\mu_B < 300$  MeV

$$\Rightarrow T_{pc}^{LQCD} \approx T_{fo}^{ALICE} = 156.5 \pm 3 \text{ MeV}$$

HotQCD Collaboration, Phys.Lett. B795 (2019) 15  
S. Borsanyi et.al. Phys. Rev. Lett. 125, 052001 (2020)

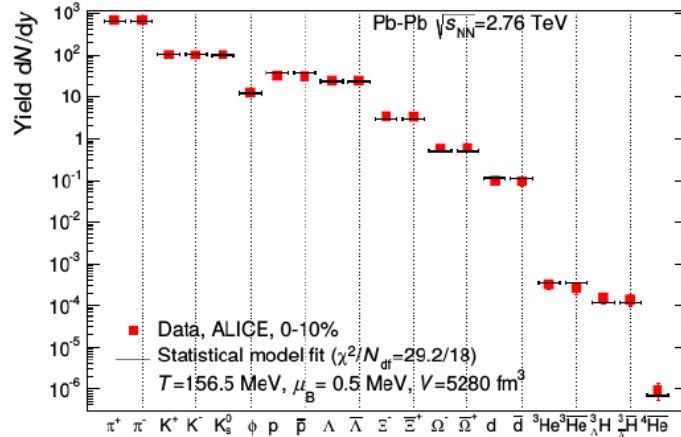


# Centrality



# Centrality

A. Andronic, P. Braun-Munzinger, J. Stachel and K. Redlich  
 Nature 561, 321–330 (2018), ALICE, PLB 726 (2013) 610



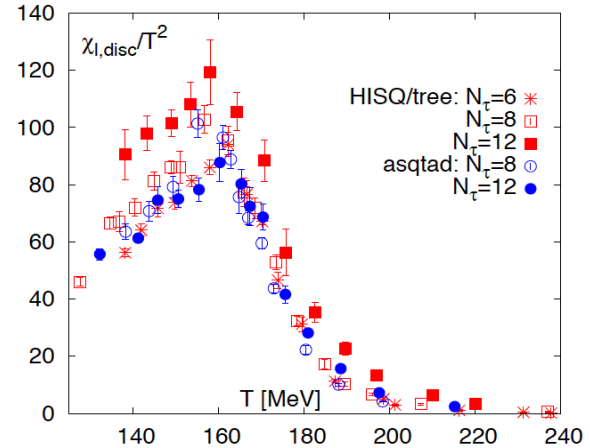
$$T_{fo}^{ALICE} = 156.5 \pm 3 \text{ MeV}$$

$$\langle N_i \rangle = V \frac{g_i}{2\pi^2} \int_0^\infty \frac{p^2 dp}{\exp[(E_i - \mu_i)/T] \pm 1}$$

$$\mu_i = \mu_B B_i + \mu_S S_i + \mu_I I_i$$

$$\chi^2 = \sum_{k=1}^n \frac{(\langle N_k^{\text{exp}} \rangle - \langle N_k^{\text{HRG}} \rangle)^2}{\sigma_k^2}$$

HotQCD Collaboration  
 Phys.Rev. D85 (2012) 054503, arXiv:1904.09951



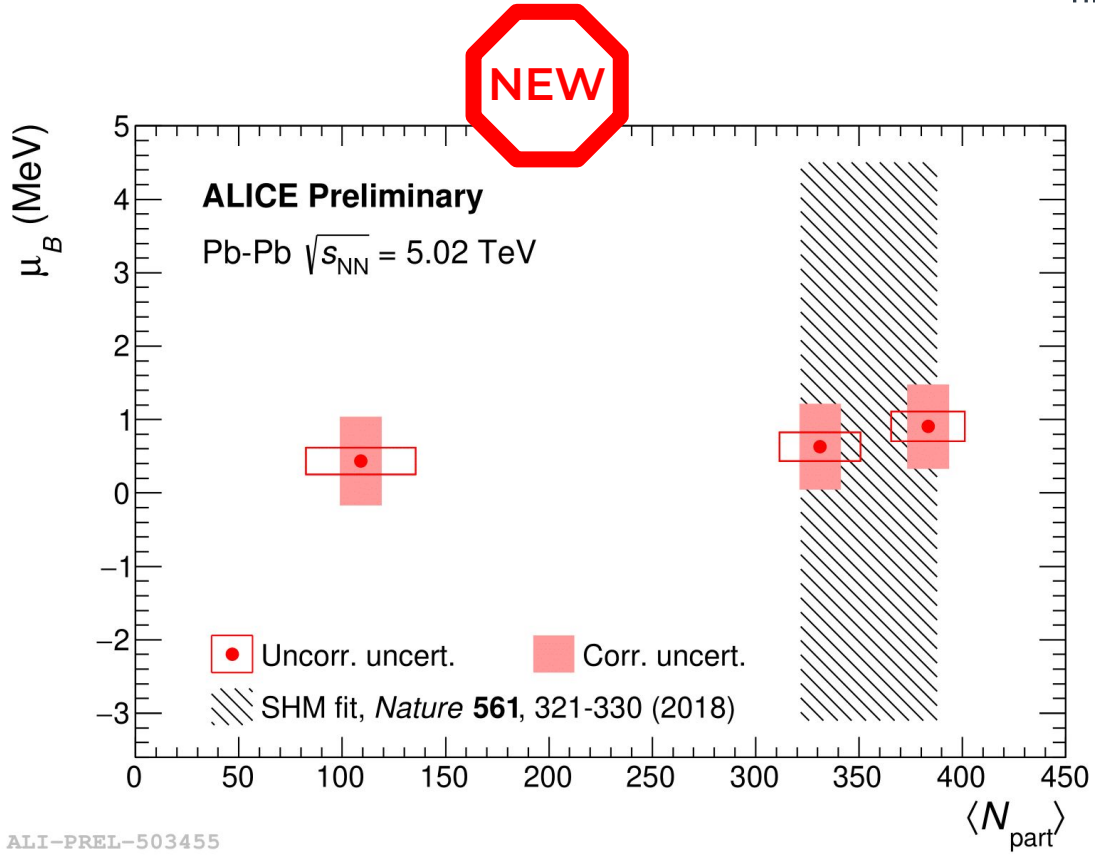
$$T_{pc} = 156.5 \pm 1.5 \text{ MeV}$$

$$\langle \bar{\psi}\psi \rangle_l^{n_f=2} = \frac{T}{V} \frac{\partial \ln Z}{\partial m_l}$$

$$\chi_{m,l} = \frac{\partial}{\partial m_l} \langle \bar{\psi}\psi \rangle_l^{n_f=2}$$



...



ALI-PREL-503455

