

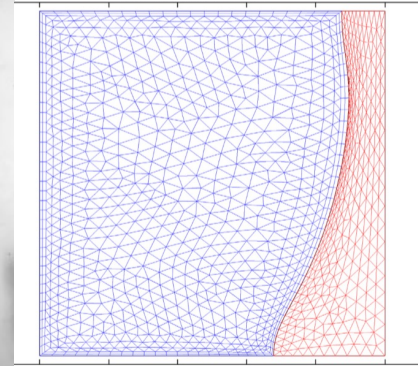
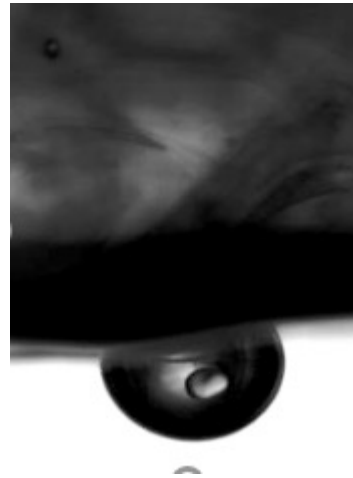
European Course of Cryogenics 2022

Cryogenic Multiphase Heat & Mass Transfer

Srini Vanapalli

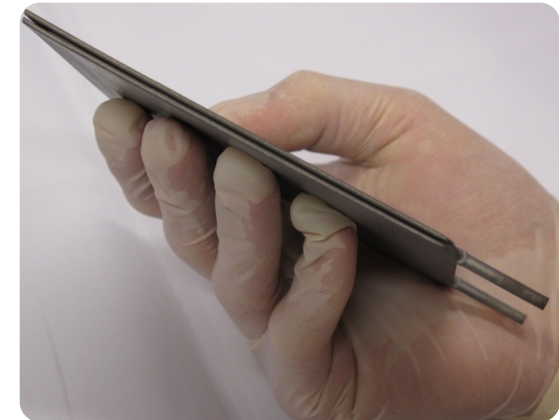
Heat and mass transfer at low temperature

- a. Seeking solutions for velocity, pressure and temperature fields in liquid and vapor phases, temperature field in the solid
- b. Scaling to real applications in life sciences and energy



Cryogenic environment

- a. Low temperatures from 200 K to 20 K
- b. Thermo-physical properties change strongly with temperature
- c. Heat fluxes always present



How to participate?



Click on the projected screen to start the question



#1 CO2 production

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 You cannot vote anymore



Carbon dioxide snow is produced by expanding liquid CO₂ through an orifice.

Estimate the amount of snow produced in kg, when one kg of saturated liquid CO₂ at 290 K is expanded through an orifice.

Click on the projected screen to start the question

24

24

24

wooclap



85 %



24



i



25 %

CO₂ molecule

#2 CO2 properties

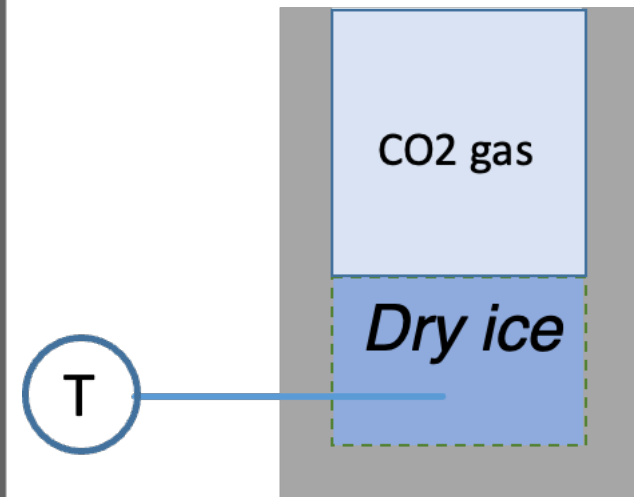
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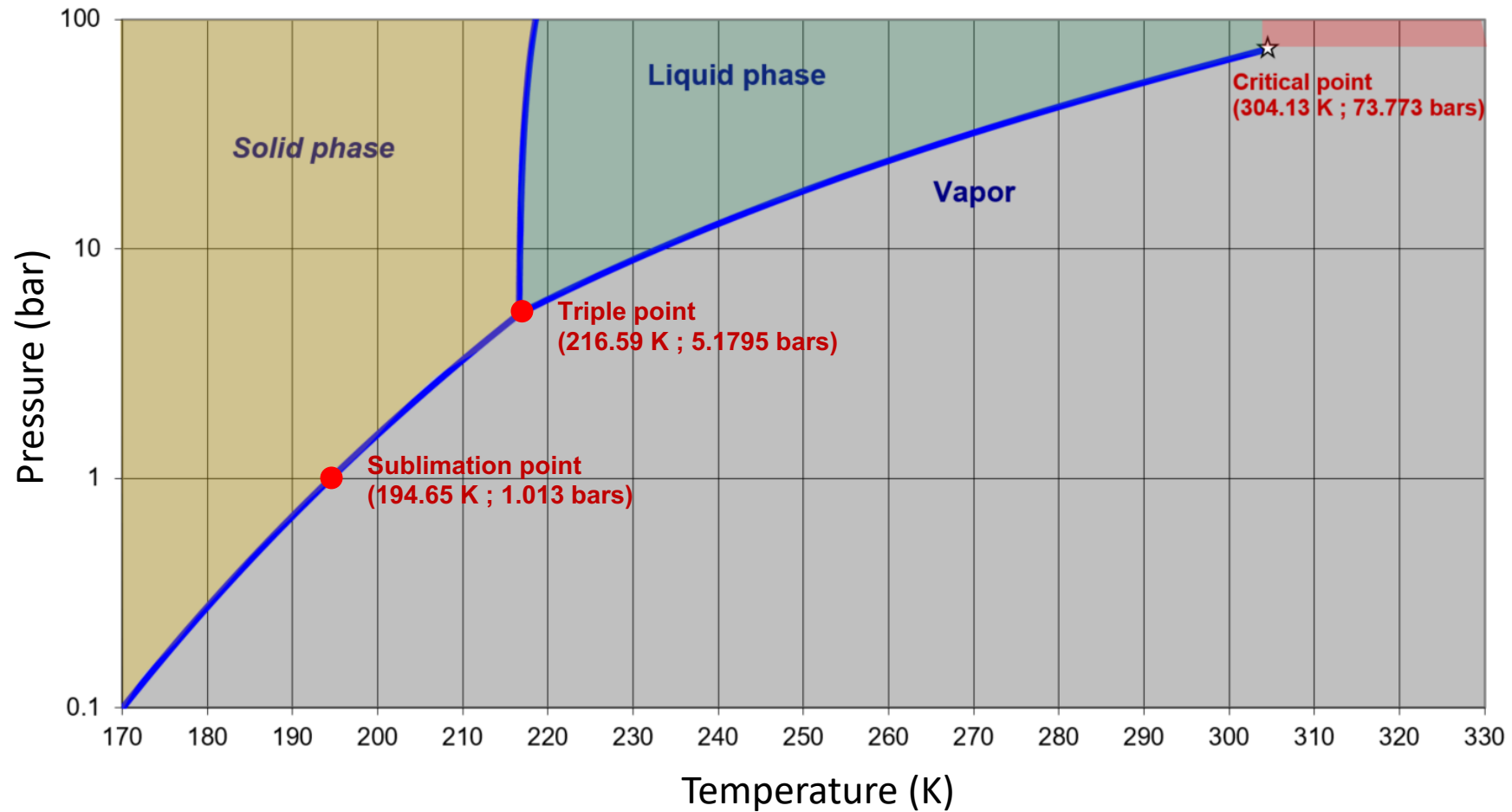
Figure A (below) shows a situation with dry ice in a vessel. The species above the dry ice is CO₂ at 1 bar. A temperature sensor is placed in the dry ice. What would be the temperature recording?

Click on the projected screen to start the question

FIGURE A



What is the dry ice temperature? $-78.5\text{ }^{\circ}\text{C}$?



#3 CO₂ properties

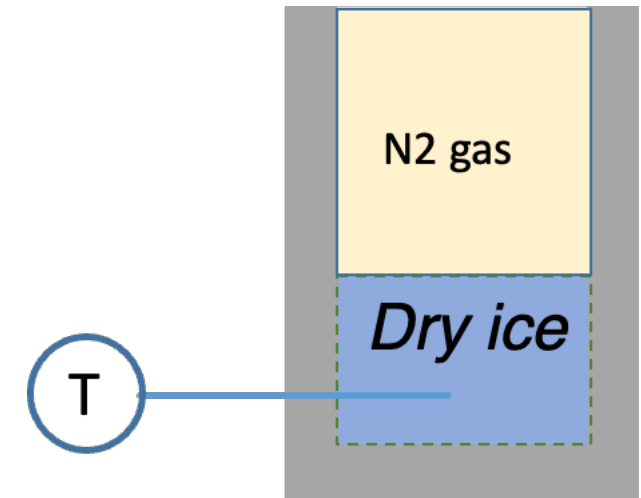
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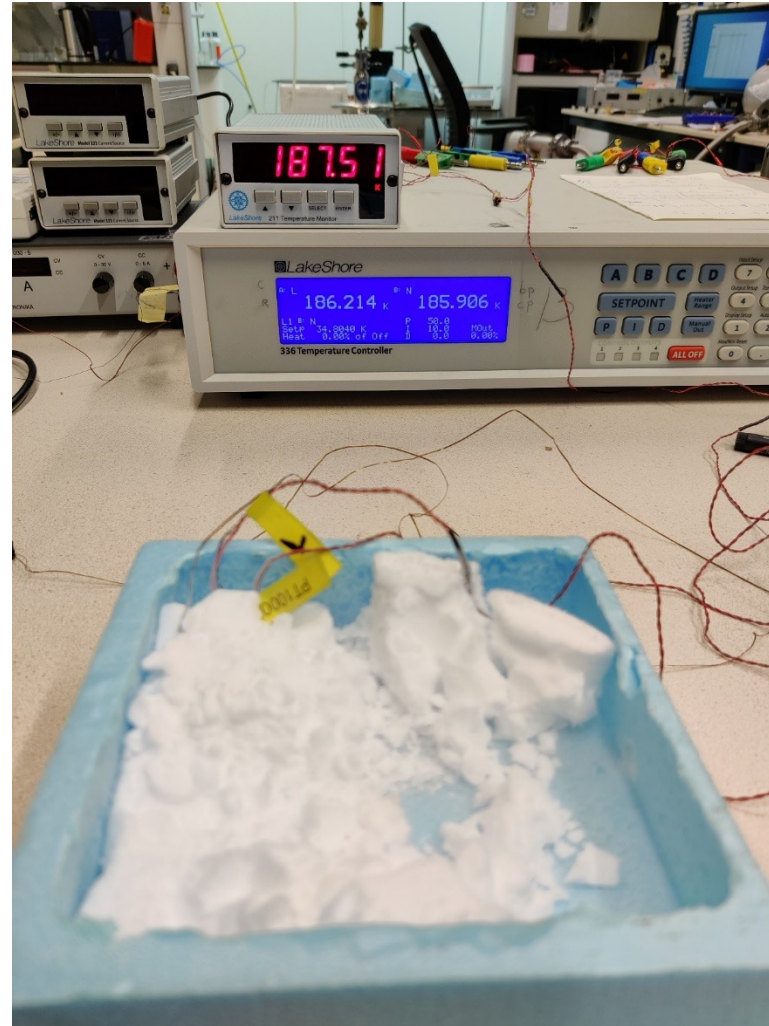
Figure B (below) shows a situation with dry ice in a vessel. The species above the dry ice is Nitrogen at 1 bar. A temperature sensor is placed in the dry ice. What would be the likely temperature recording?

Click on the projected screen to start the question

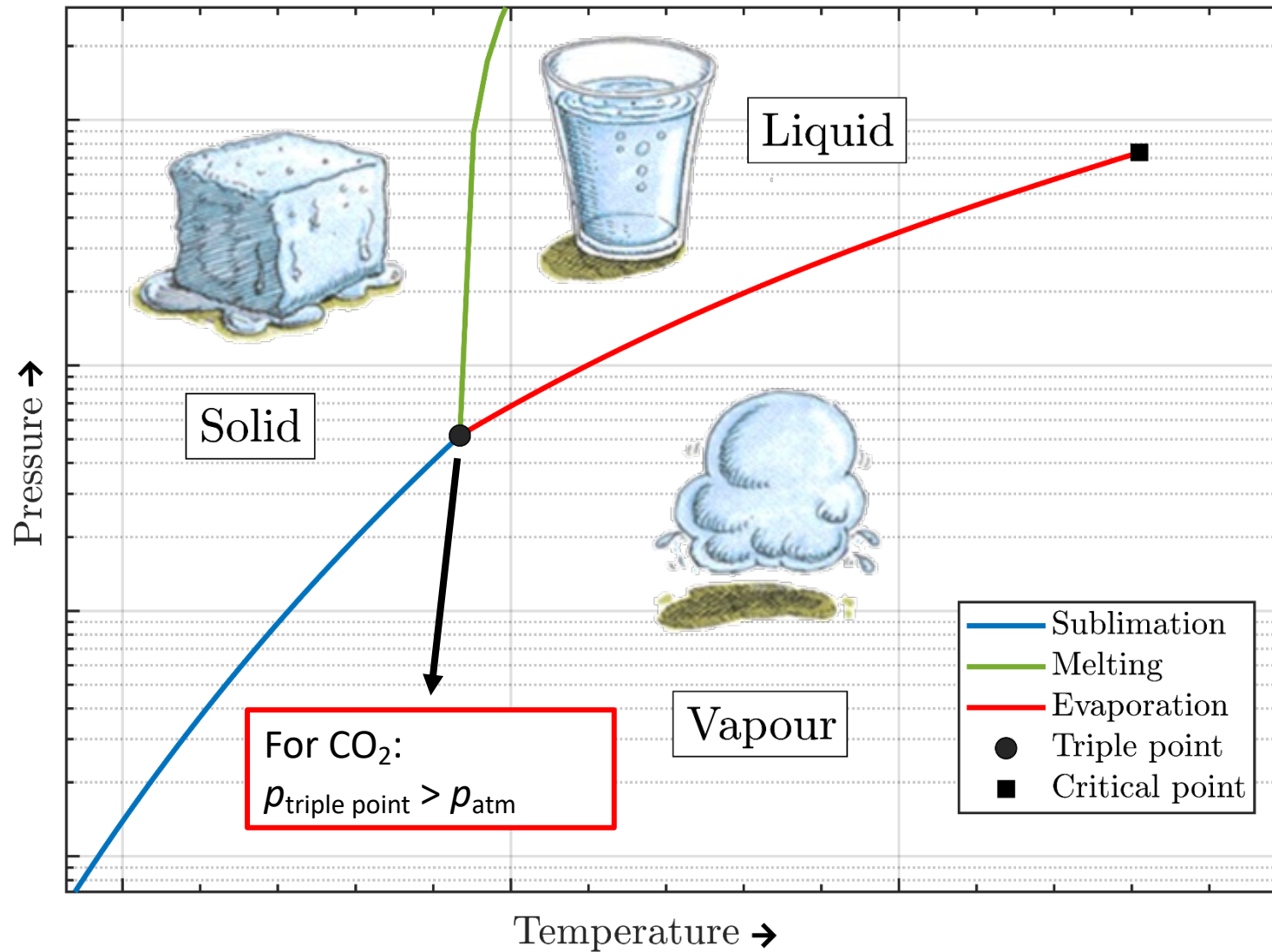
FIGURE B

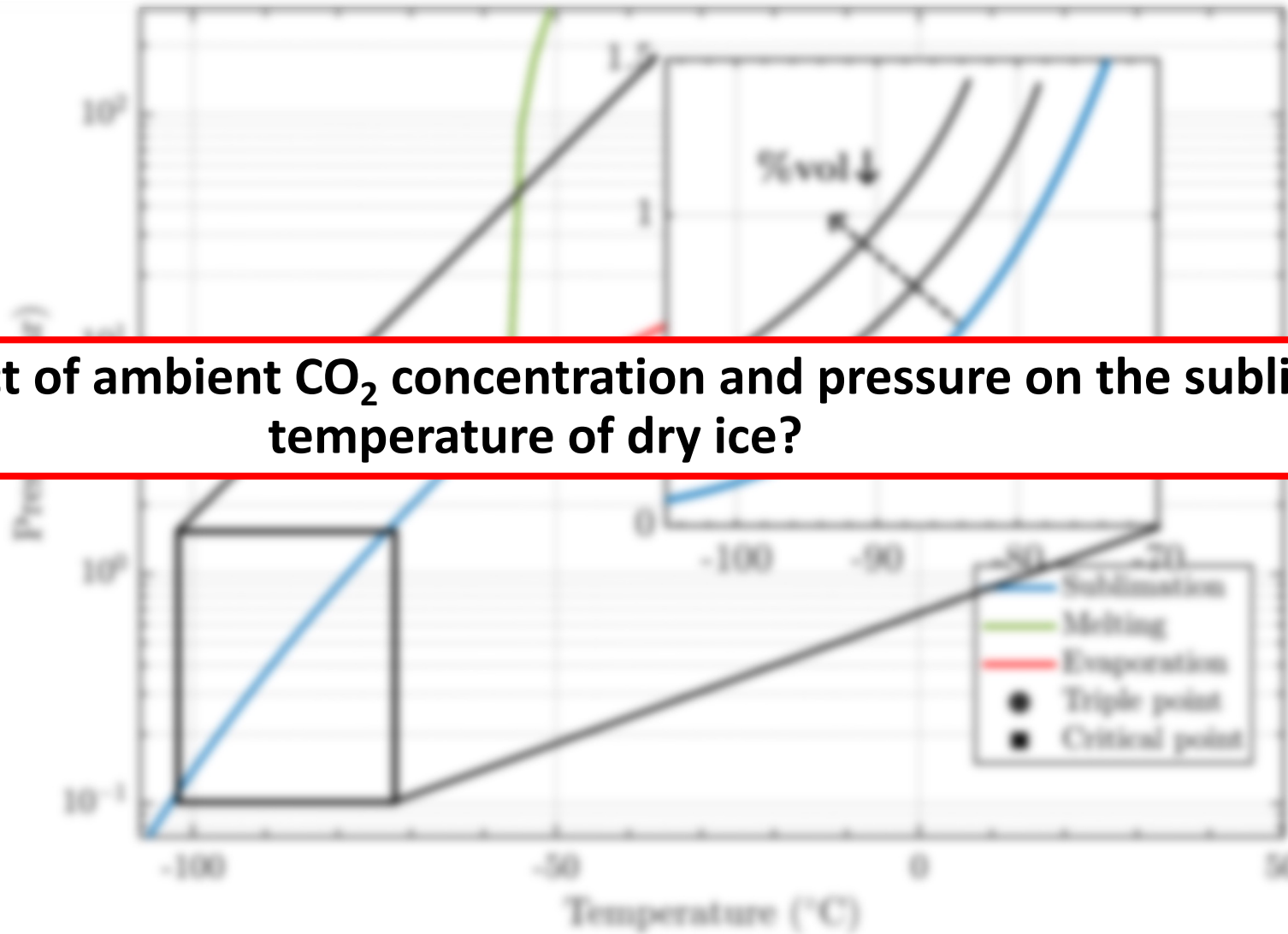


Temperature measurement of dry ice



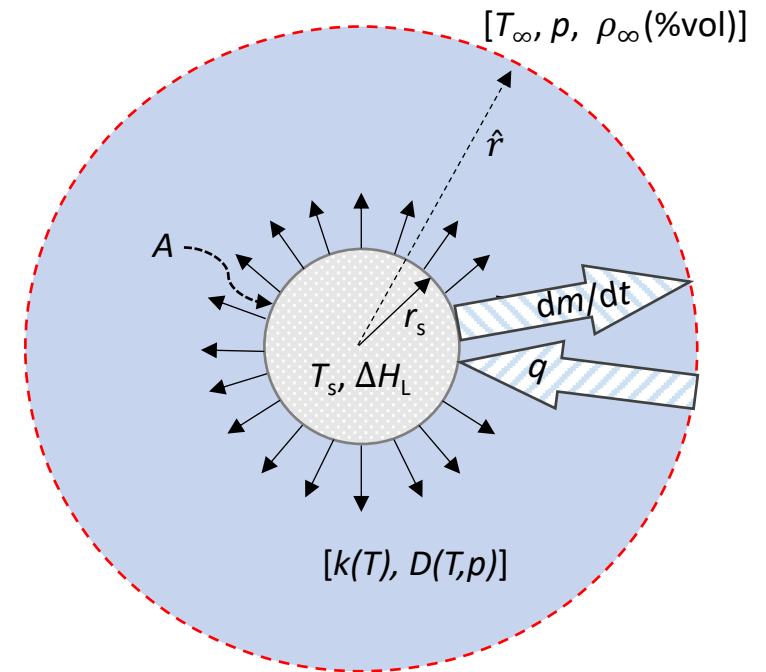
Thermodynamic phase diagram





What is the effect of ambient CO₂ concentration and pressure on the sublimation temperature of dry ice?

- Based on kinetics:
heat transfer input and mass transfer output.
- **Lumped** capacitance model
- **Stationary** ambient
- Heat transfer q → conductive
- Mass transfer dm/dt : → diffusive



- Heat conduction:

$$q = A \cdot k(T) \cdot \left. \frac{dT}{dr} \right|_{r=r_s}$$

- Mass diffusion:

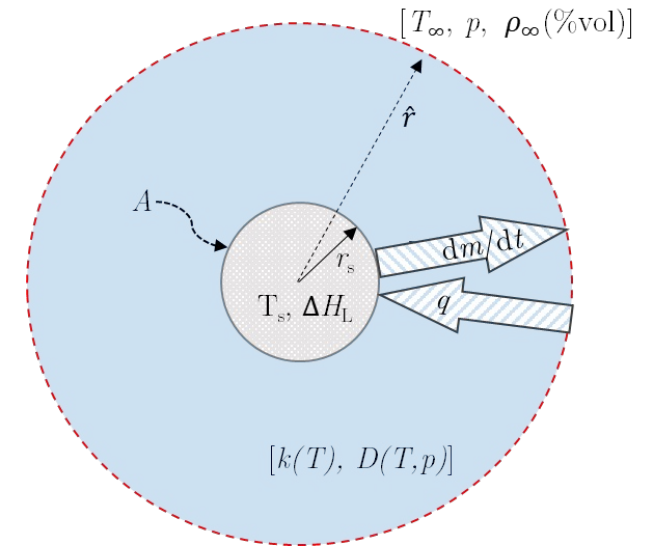
$$\frac{dm}{dt} = -A \cdot D(T, p) \cdot \left. \frac{d\rho}{dr} \right|_{r=r_s}$$

- Linked by latent heat:

$$q = \Delta H_L \cdot \frac{dm}{dt}$$

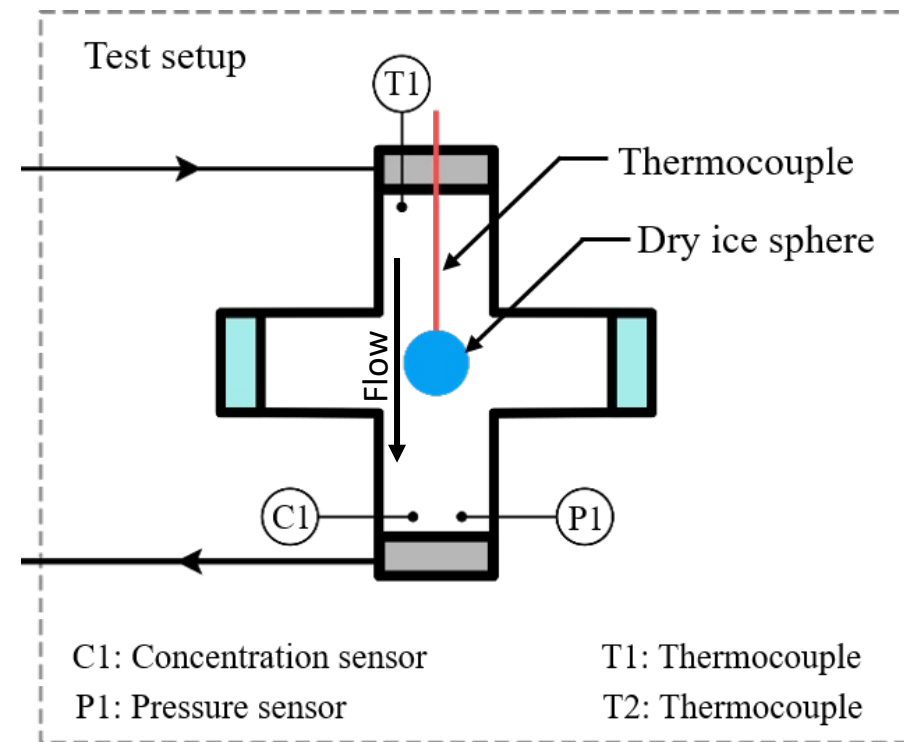
- Combines to:

$$\frac{d\rho}{dT} = - \frac{k(T)}{\Delta H_L \cdot D(T, p)}$$

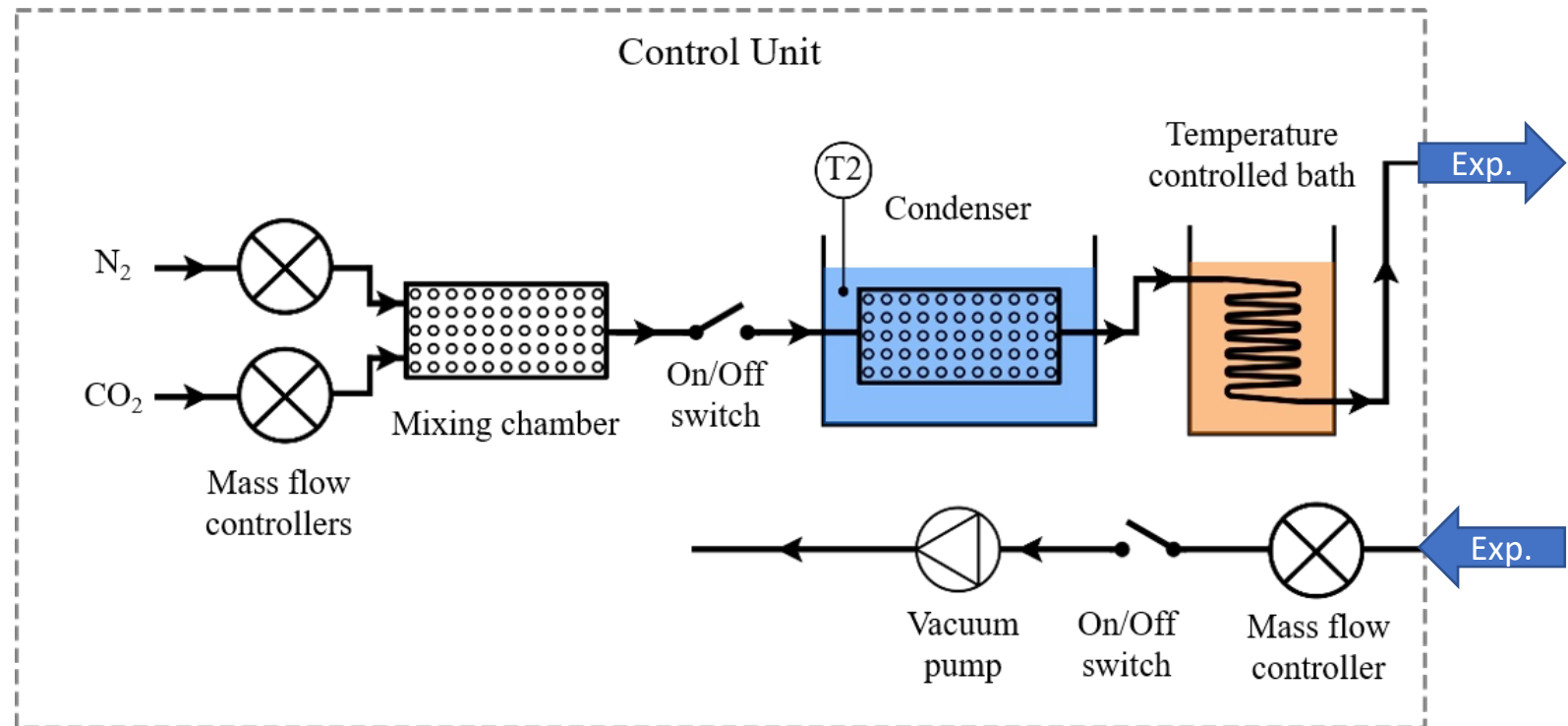


What is needed to characterise this 'wet-bulb' temperature?

- Controlled ambient
- Thermocouple inside a dry ice sample

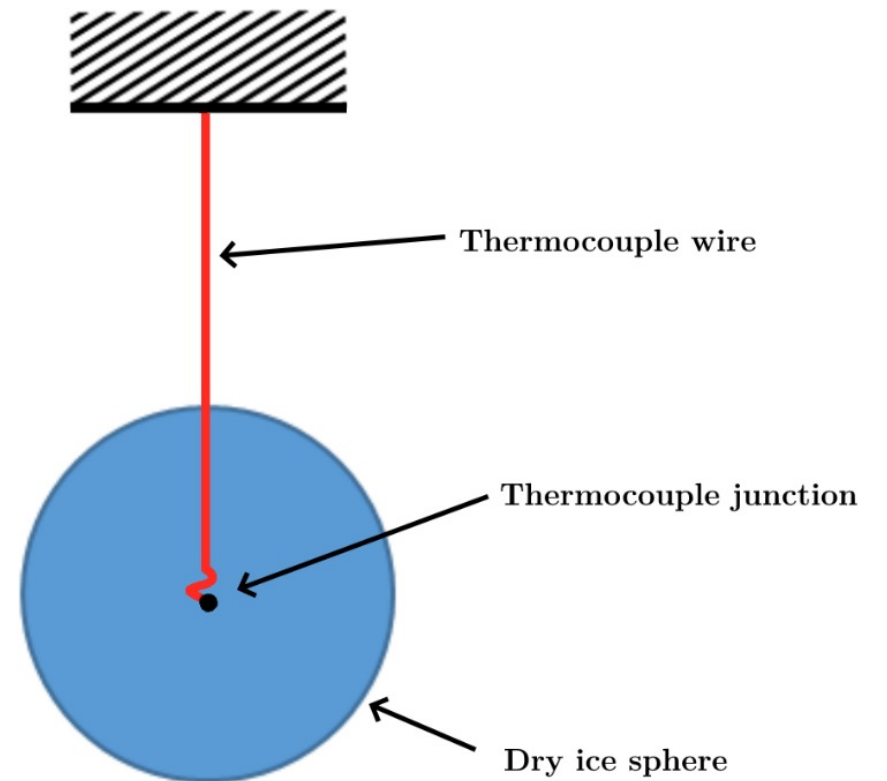
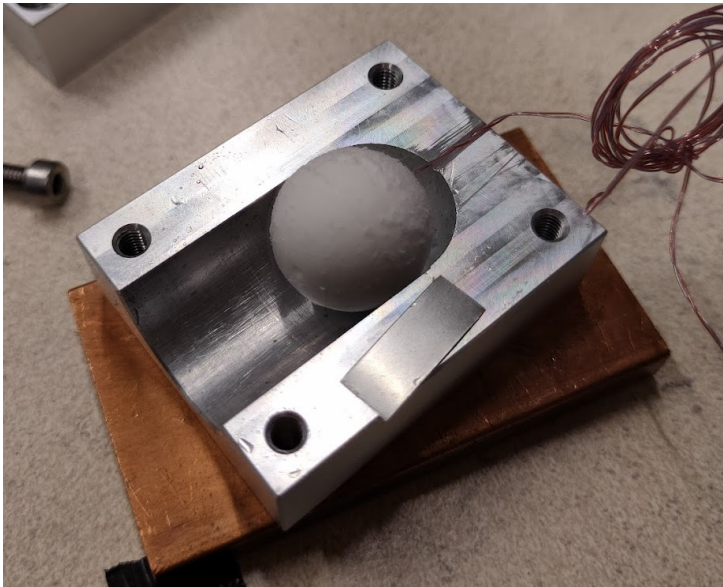


- Gas mixture:
 $\text{CO}_2 + \text{N}_2$
- Pressure regulation
 - Balancing flow

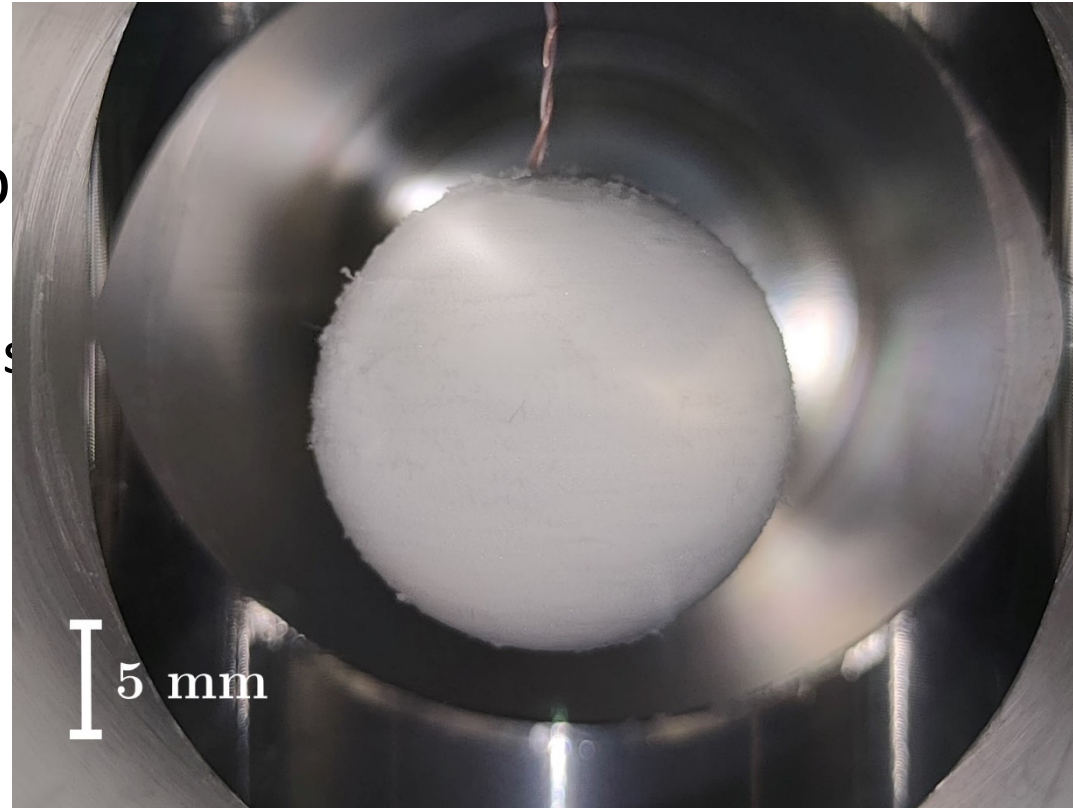


Making dry ice spheres

- Snow via Joule-Thompson expansion
- Compress into a **sphere**
- Radii of $r_s = 10$ mm & $r_s = 5$ mm

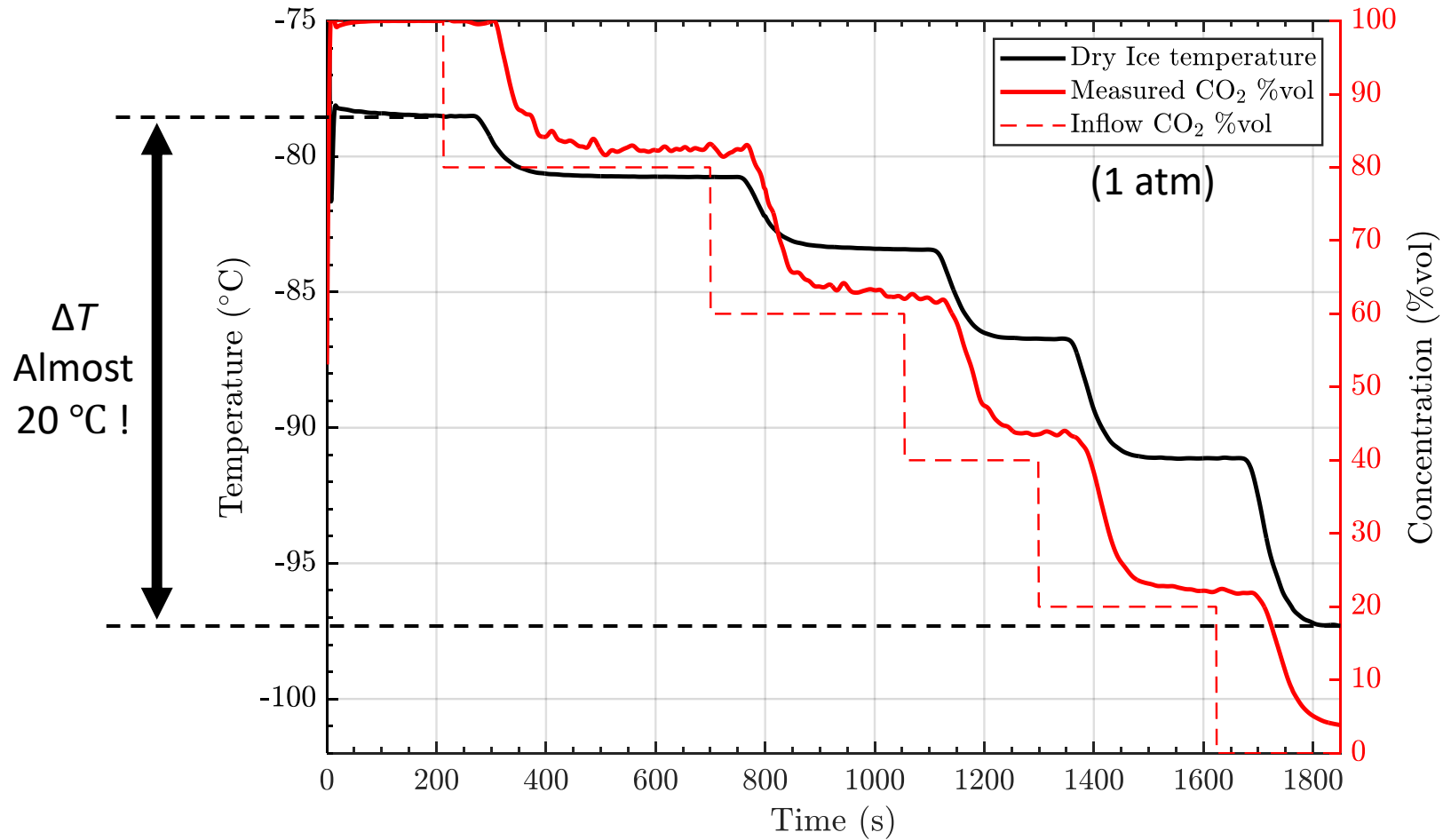


- Constant pressure experiment
 - Starting at 100 %vol
 - Vary concentration in steps
- Repeat for pressures
 - 0.6 to 1.3 bar
 - 100 mbar increments

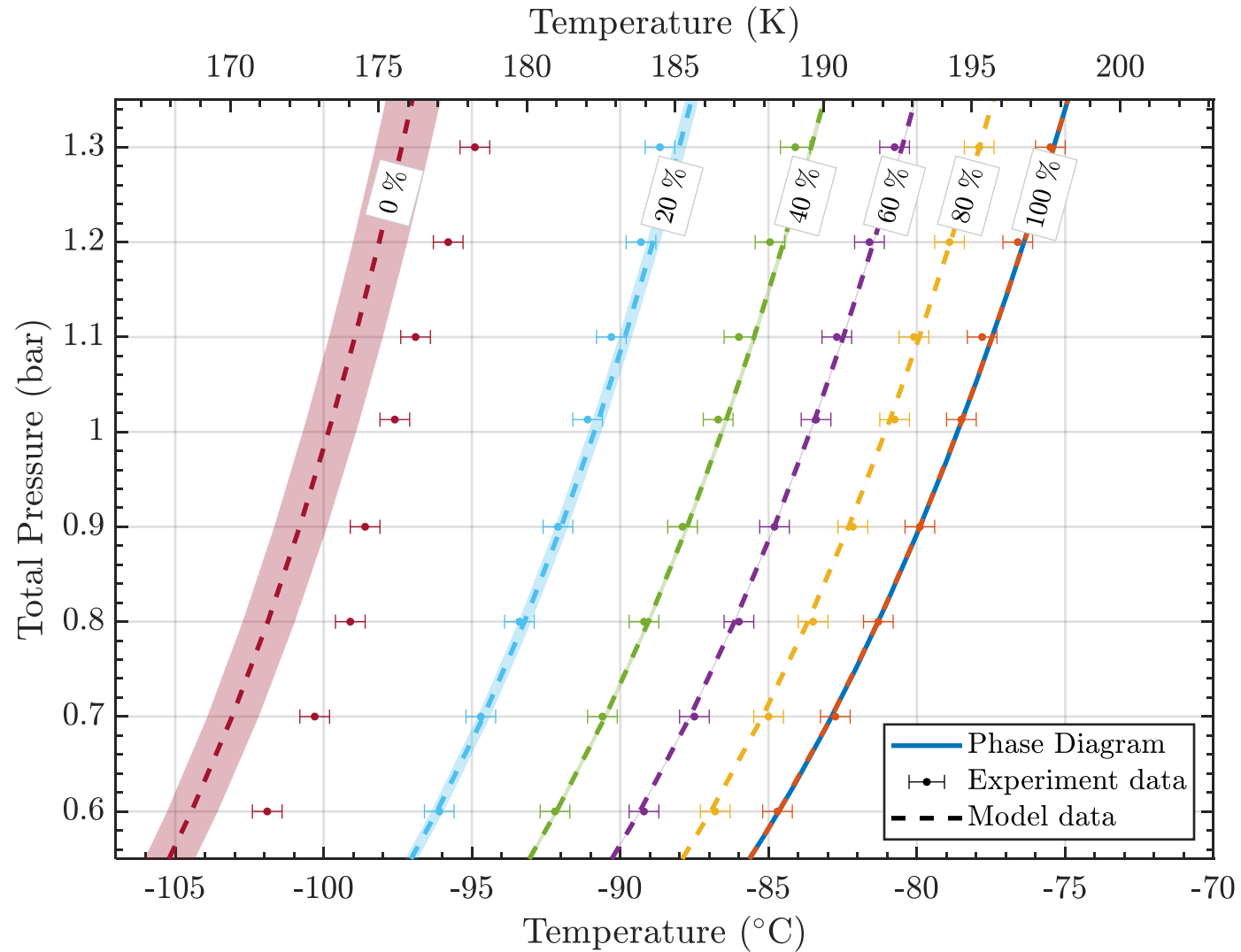


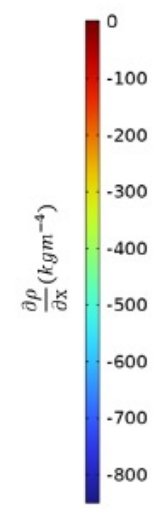
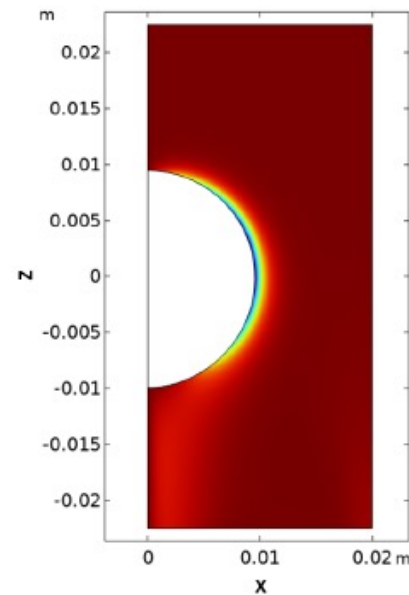
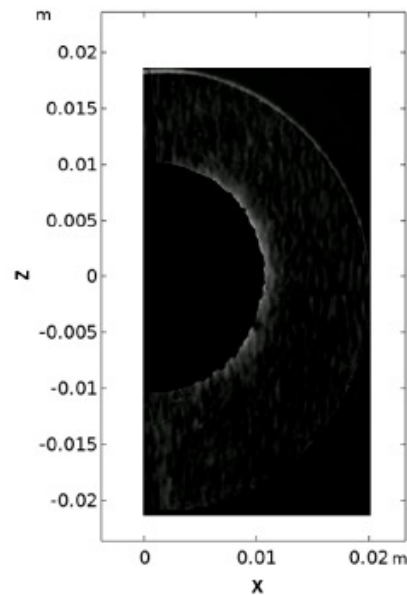
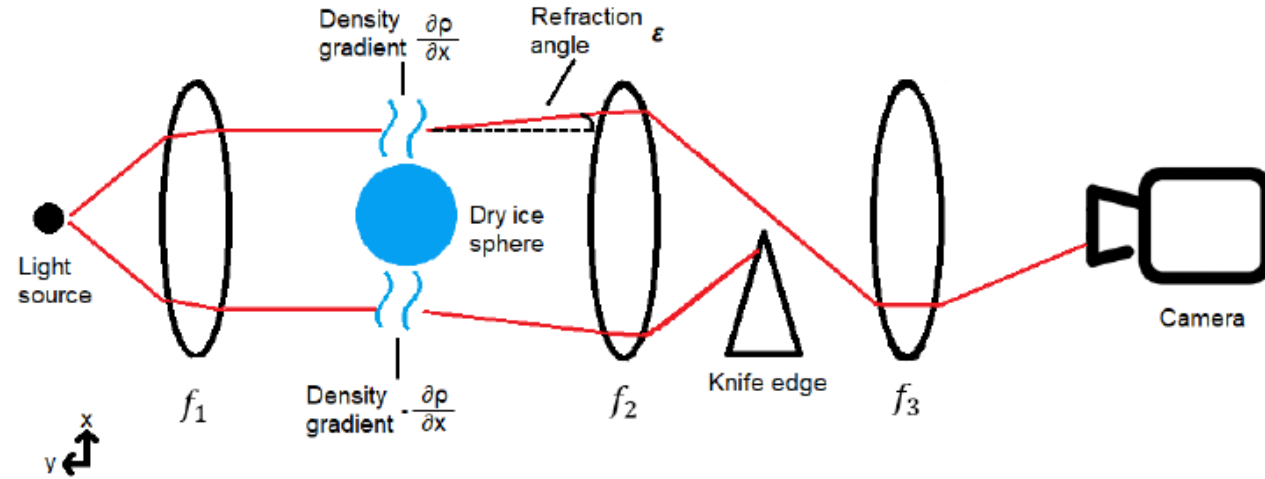
Experimental results

- What does such an experiment look like?



Extended phase diagram – results





Quantifying Leidenfrost vapor layer

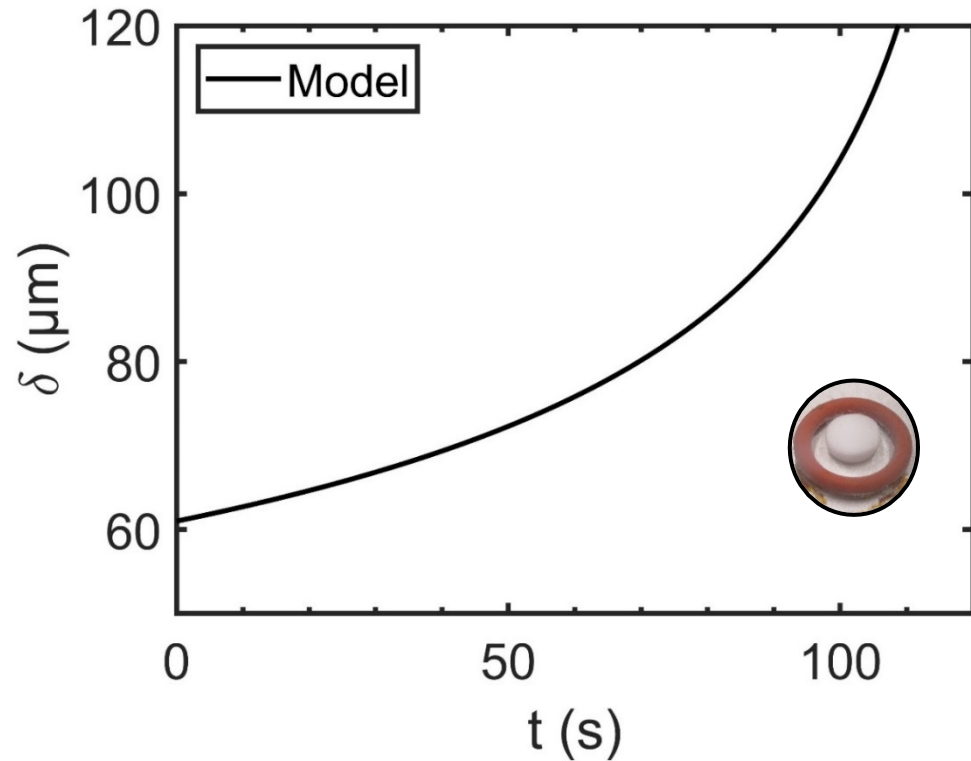


"Leidenfrost Effect - Hot pan + Water", Youtube, uploaded by LaserFloyd, 30-05-2014

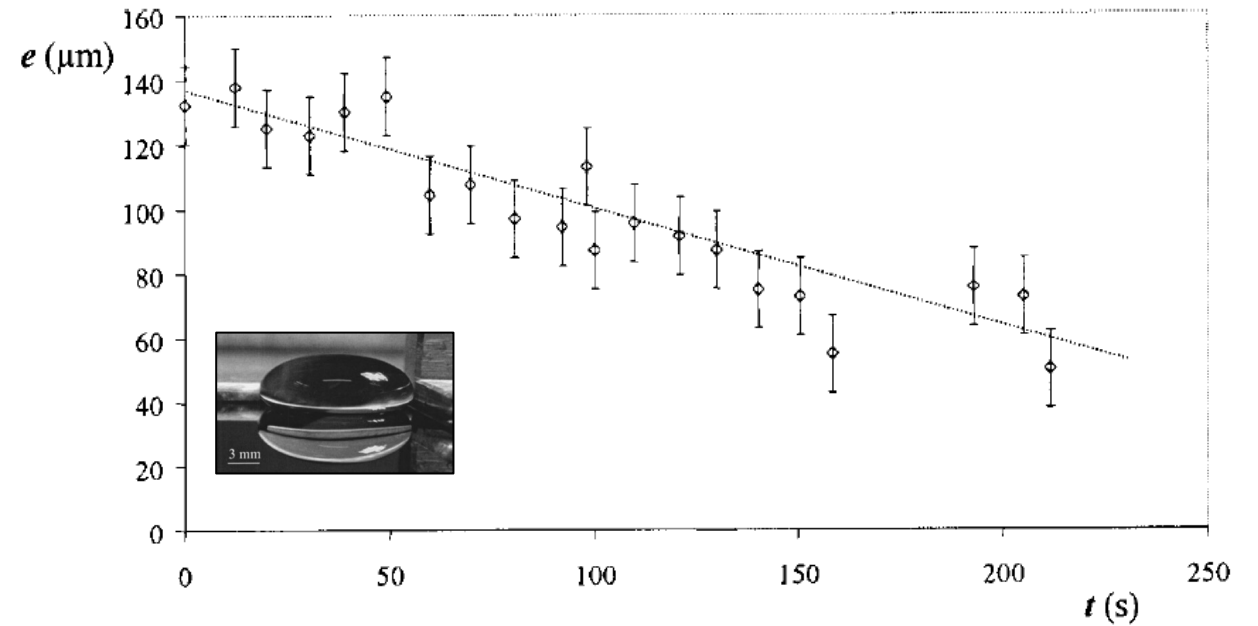


#4 Heat transfer





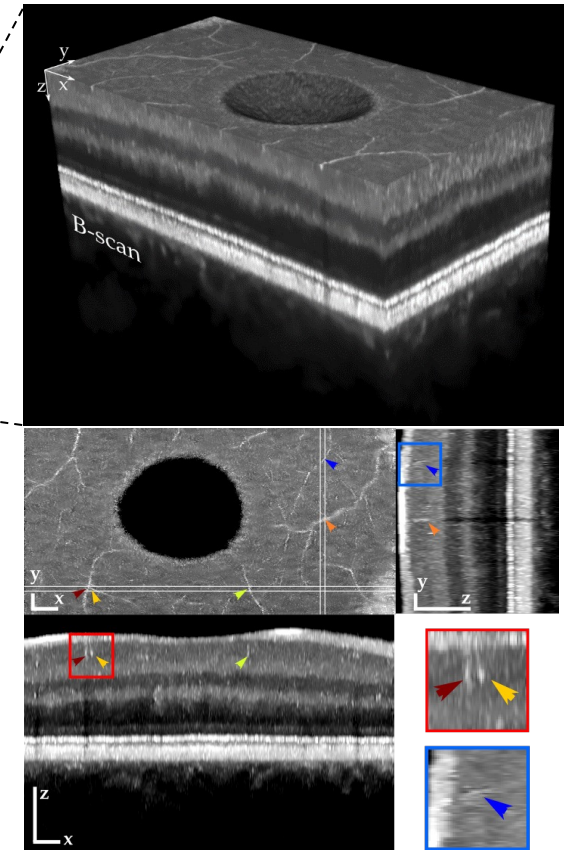
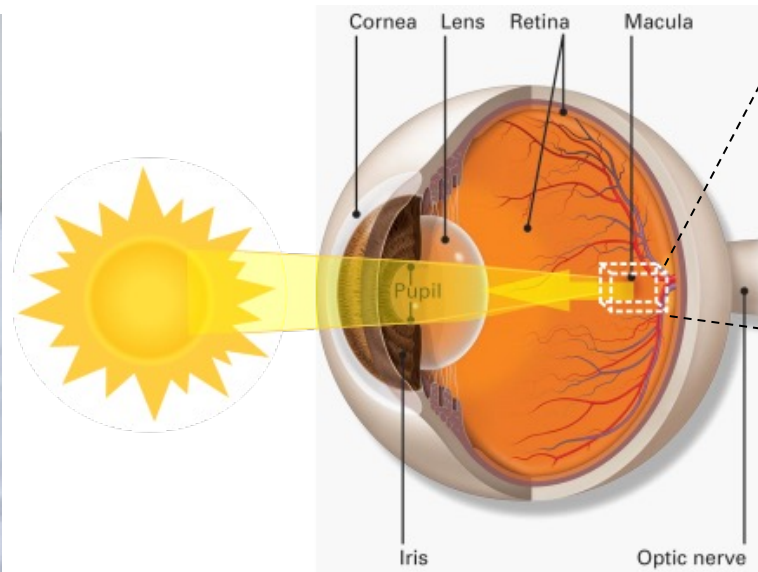
Predicted time variation of vapor layer thickness for dry ice pellet ($h_i = 5 \text{ mm}$; $d_{ci} = 10 \text{ mm}$) placed on a hot substrate



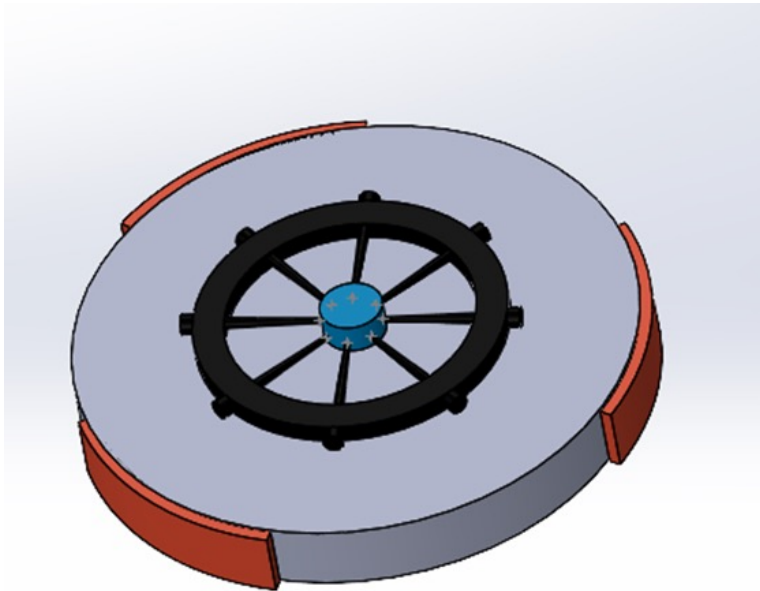
Predicted and measured time variation of vapor layer thickness for water drop ($d_{ci} = 20 \text{ mm}$) placed on a hot substrate*

Optical Coherence Tomography (OCT)

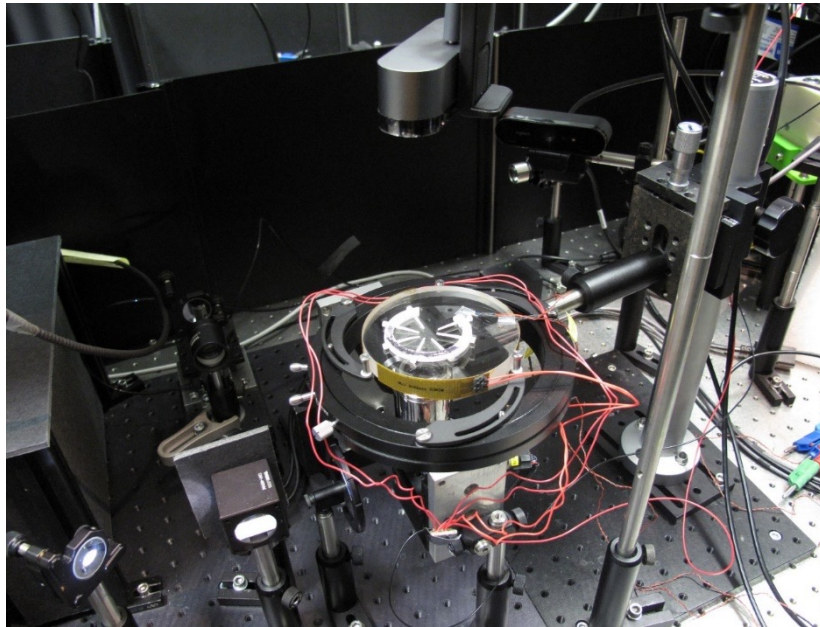
Medical **imaging technique** based on low-coherence **interferometry** which produces **high-resolution images** of scattering media such as tissue.



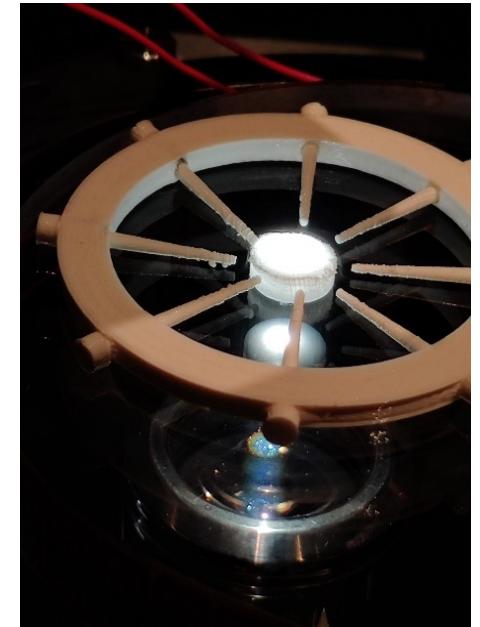
Test section assembly

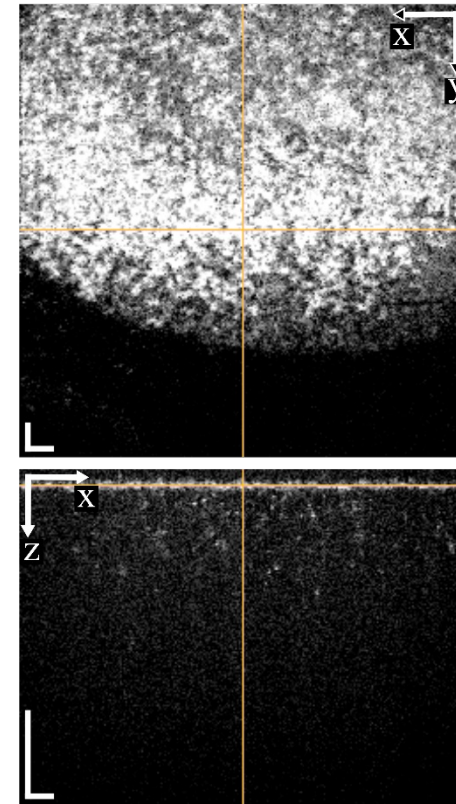
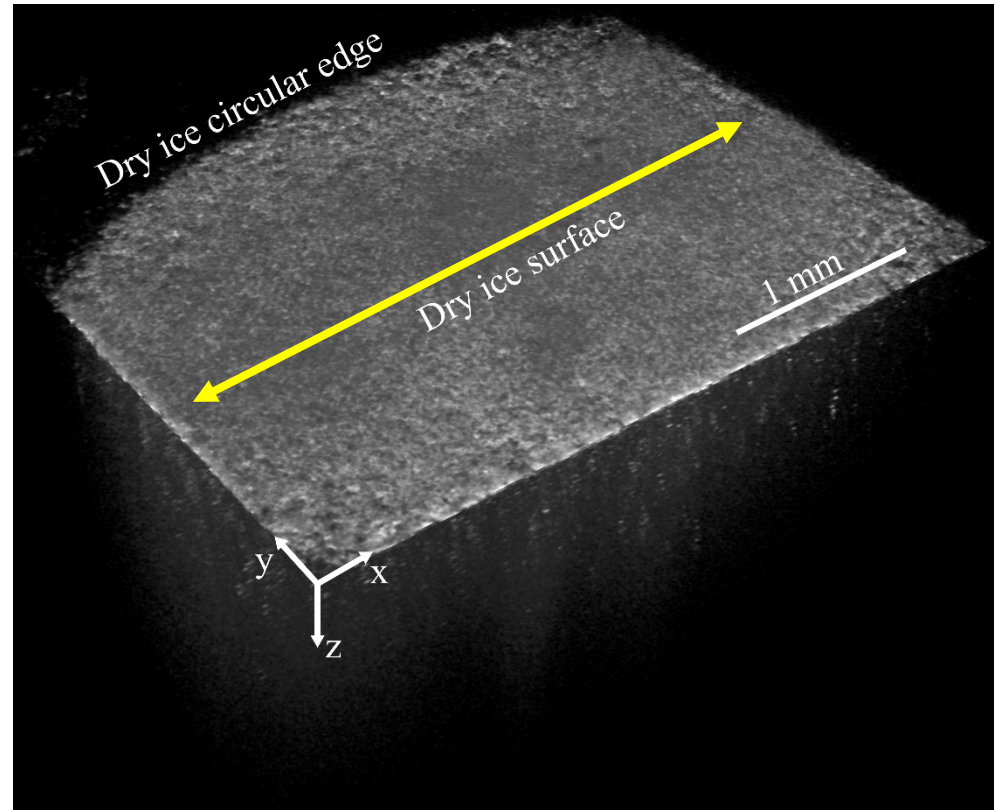
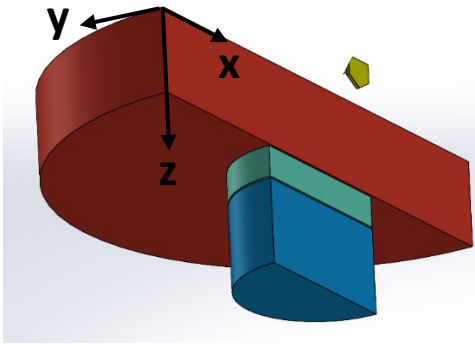


Test section in setup

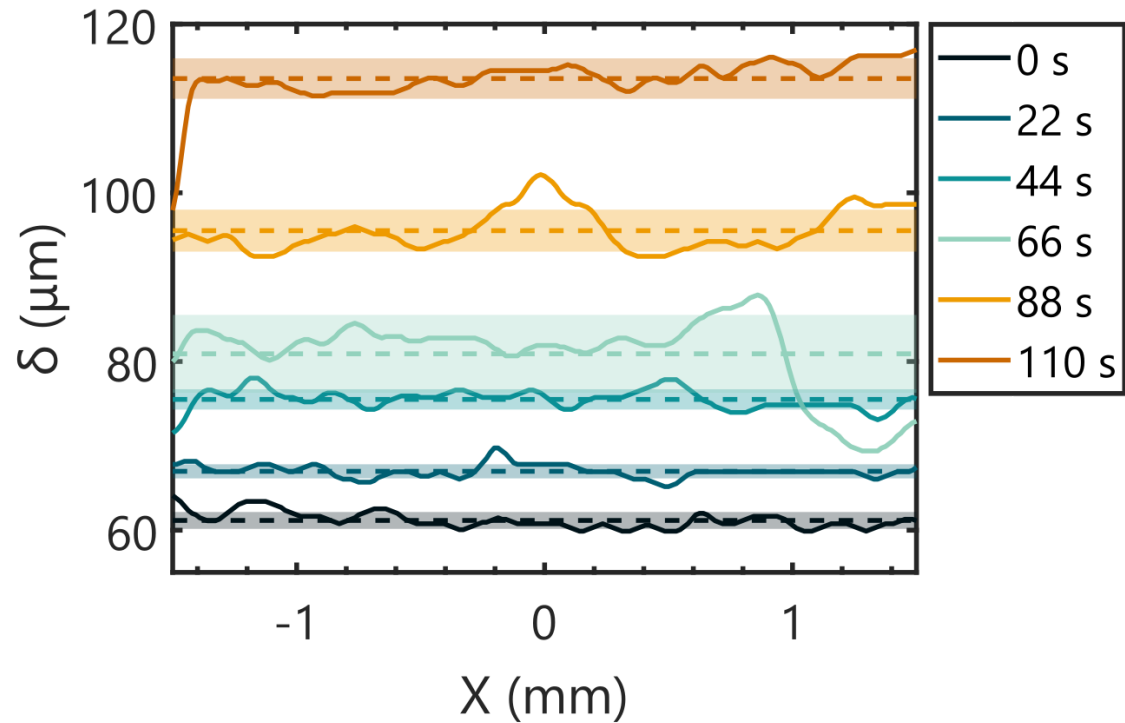


Retaining ring + dry ice



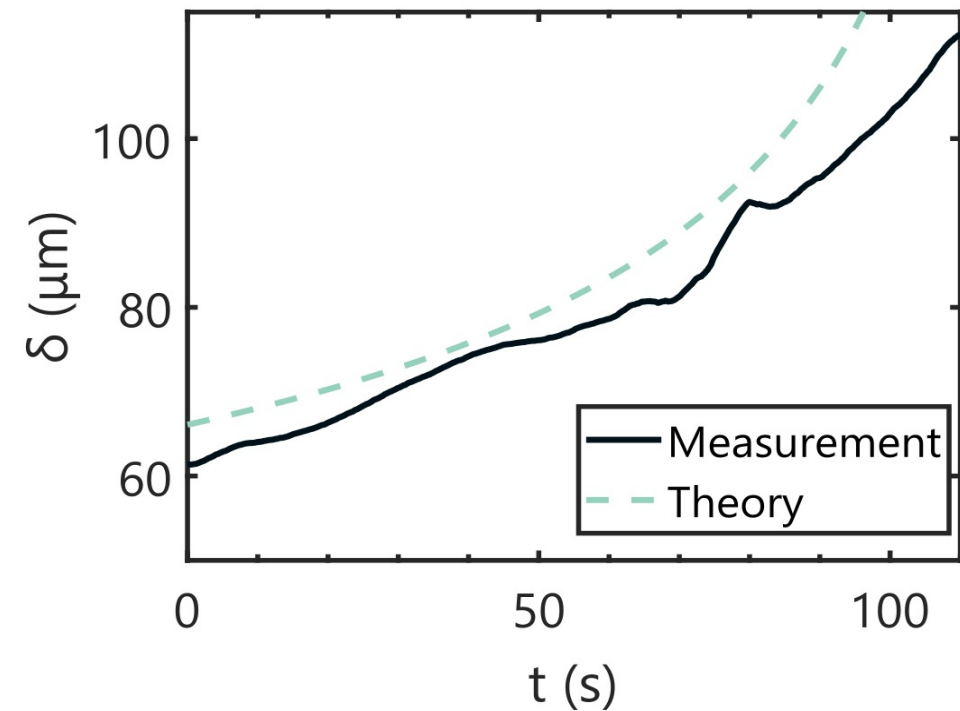


$T_p = 343 \text{ K}$

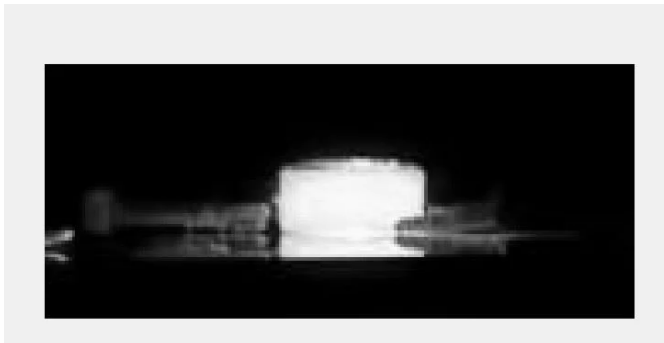


Measured vapor layer profile for dry ice pellet ($h_i = 5 \text{ mm}$; $d_{ci} = 10 \text{ mm}$) placed on a hot substrate

$T_p = 343 \text{ K}$

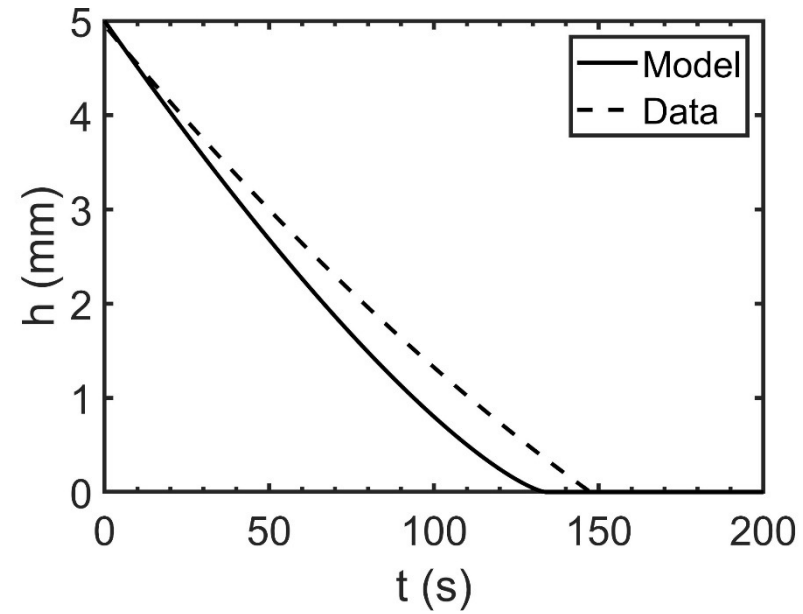


Measured and predicted time variation of vapor layer thickness for dry ice pellet ($h_i = 5 \text{ mm}$; $d_{ci} = 10 \text{ mm}$) placed on a hot substrate

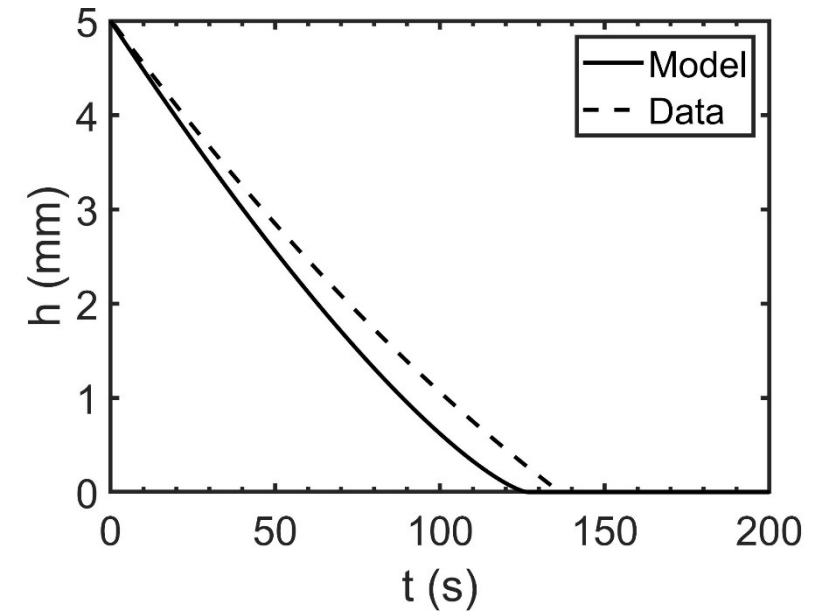


Height variation of dry ice pellet ($h_i = 5 \text{ mm}$; $d_{ci} = 10 \text{ mm}$) placed on a hot sapphire substrate

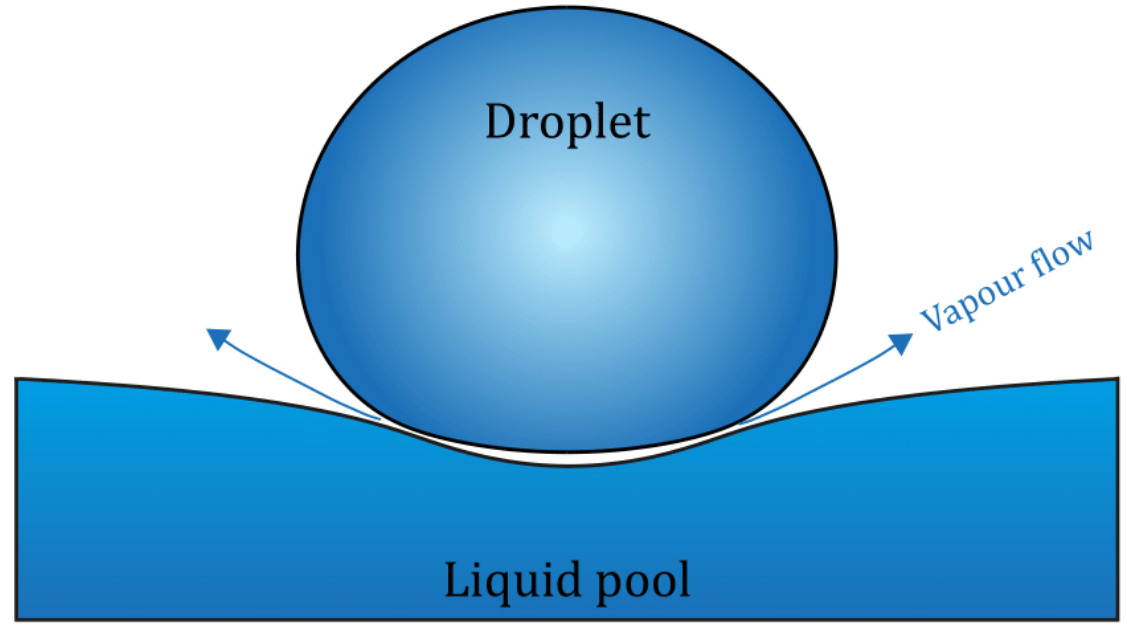
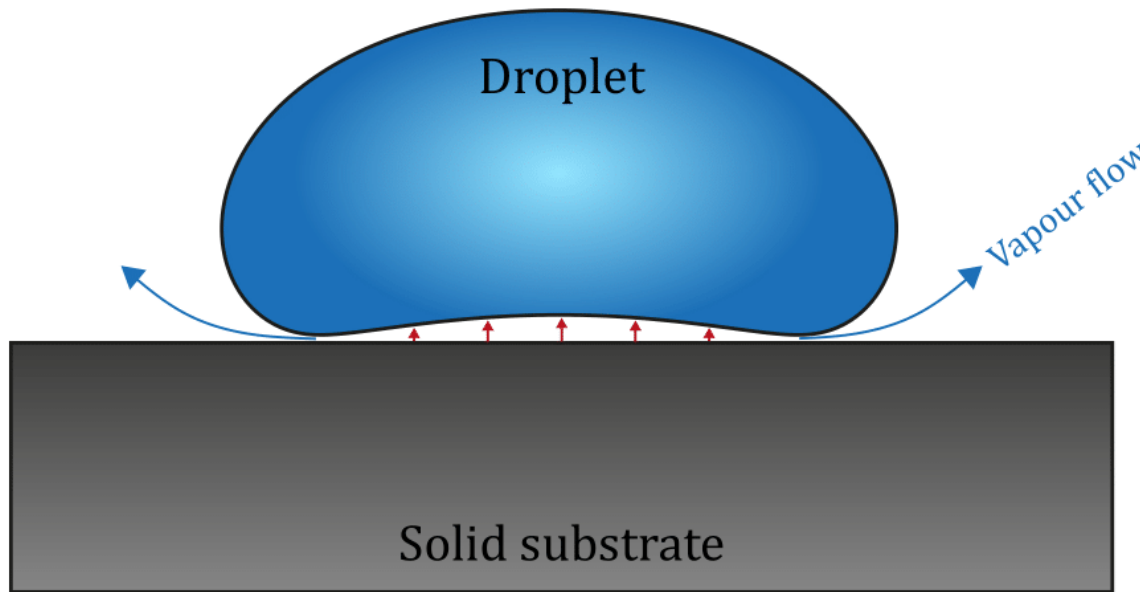
$T_p = 323 \text{ K}$




$T_p = 333 \text{ K}$



Liquid nitrogen droplets



Liquid nitrogen jet/drop dispenser



$t = 0.00$ s "LN2 jet"

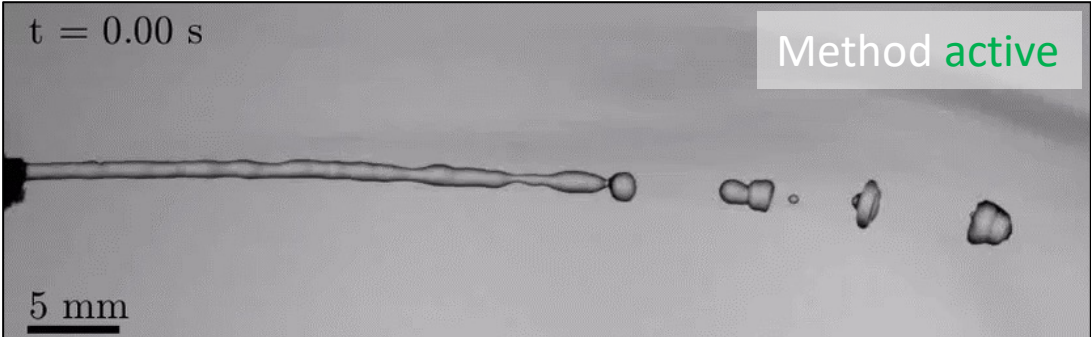
Method **inactive**

5 mm

Ambient atmosphere

Common case for a needle tube supplied from a pressurized dewar with liquid nitrogen:
Multiphase flow at nozzle exit due to evaporation in hose

New method prevents evaporation in the hose resulting in jet of pure liquid nitrogen



$t = 0.00$ s

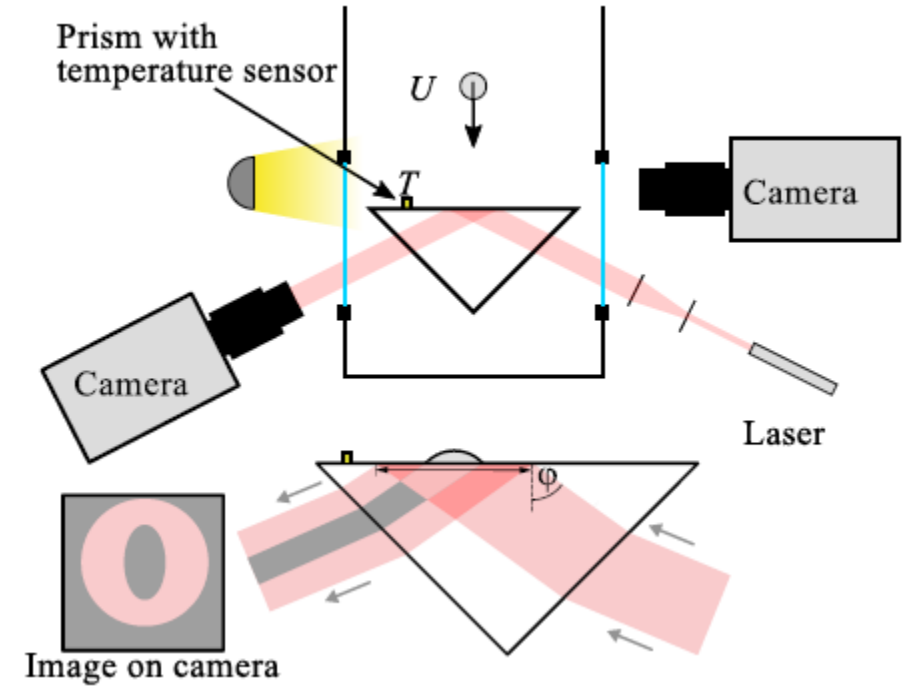
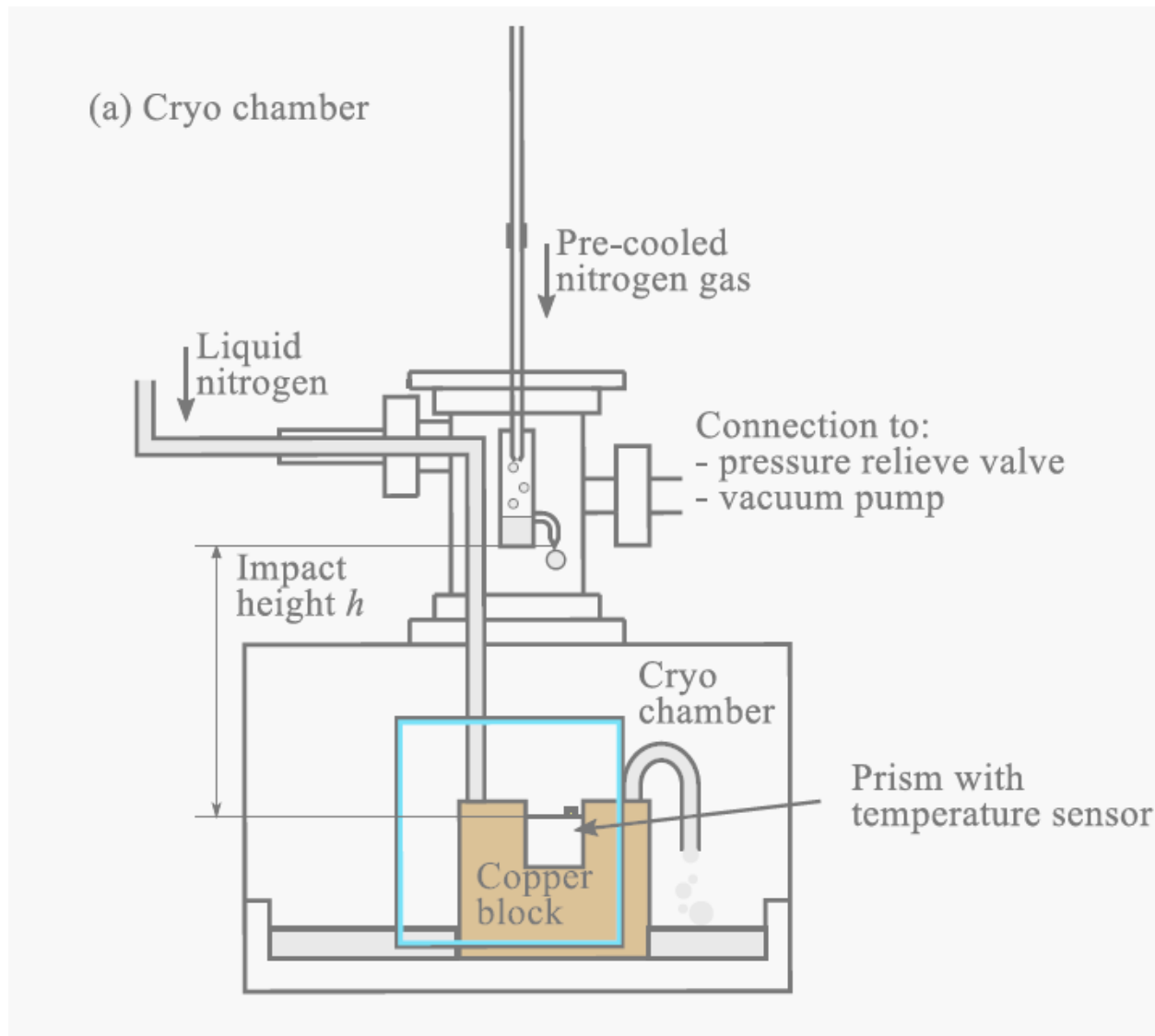
Method **active**

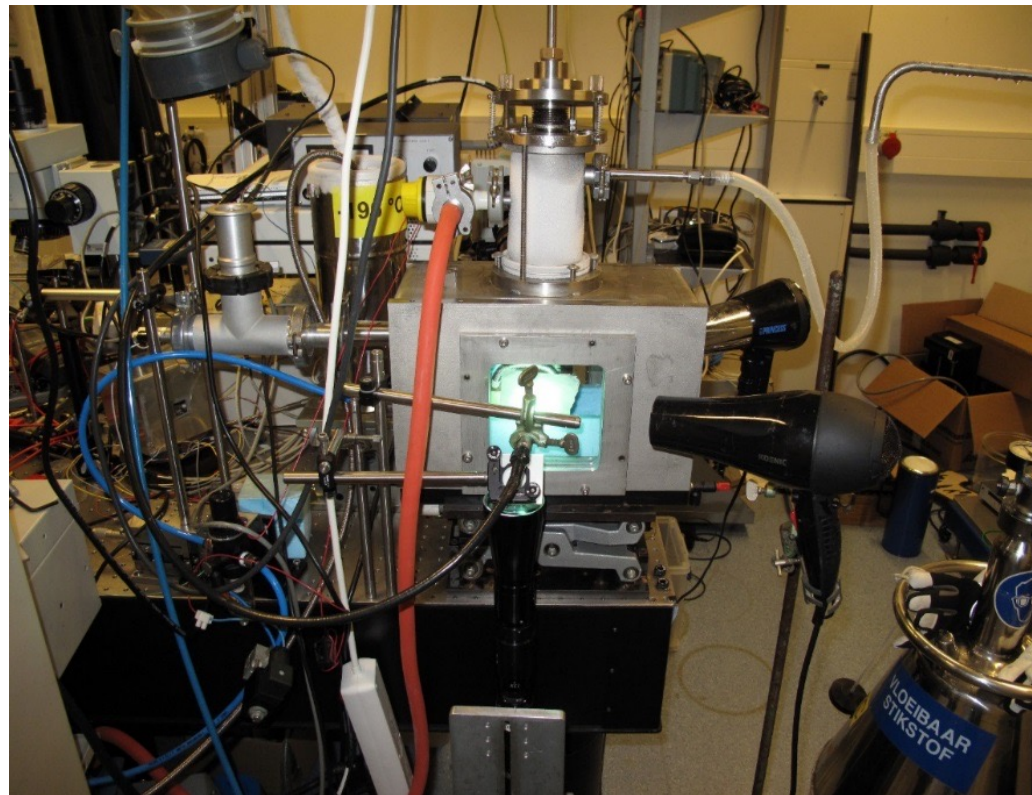
5 mm

Many opportunities for doing research with cryogenic liquid jets or single droplets

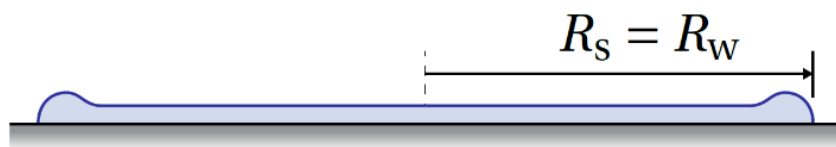
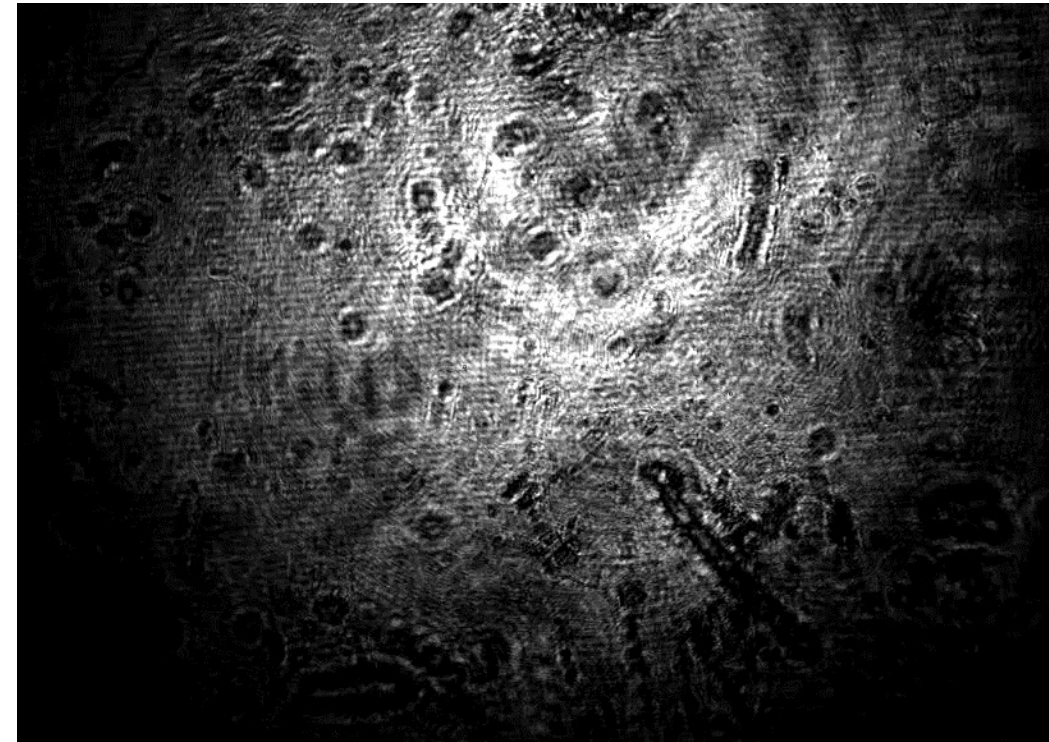


Droplet impact on a plate



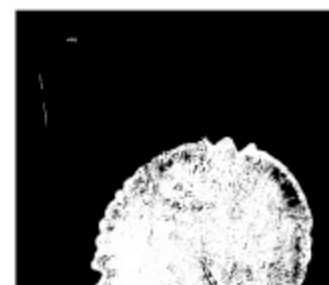
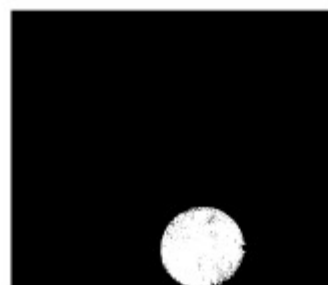
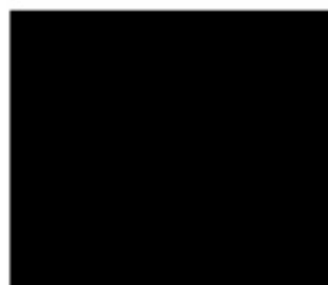
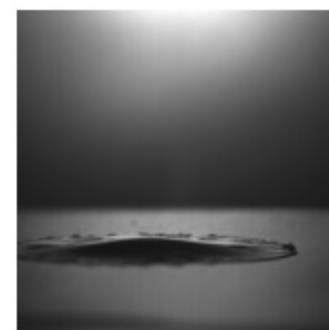
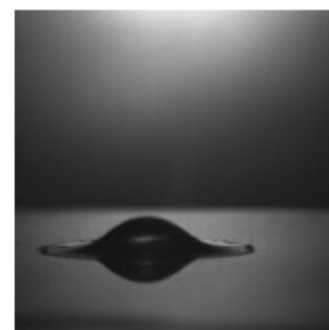
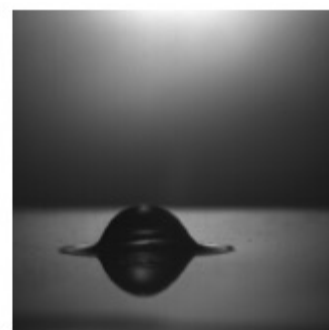
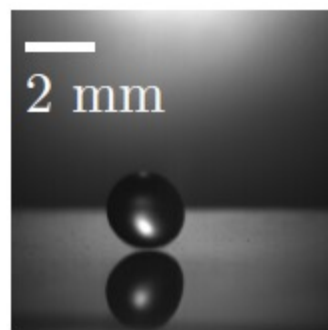


$U=1.3$ m/s $T=89$ K



Contact boiling

Slowed down 500x



$t = 0$ ms

0.4 ms

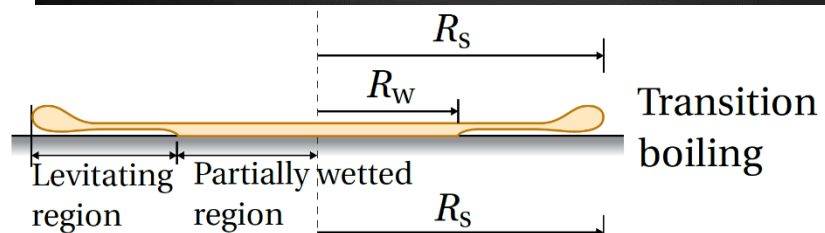
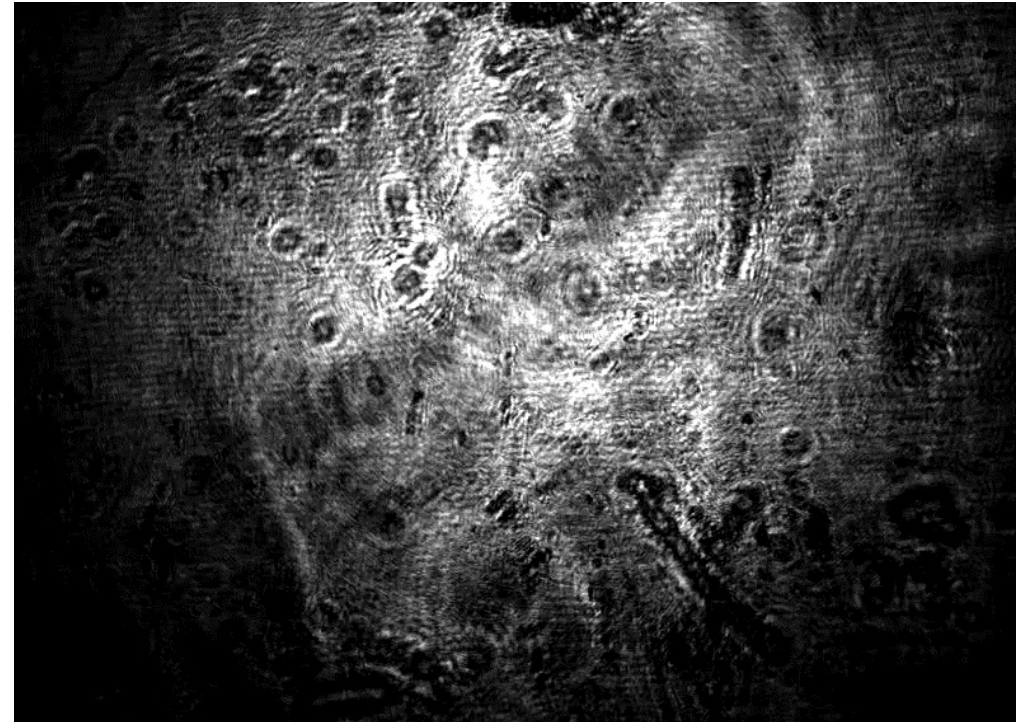
0.8 ms

1.2 ms

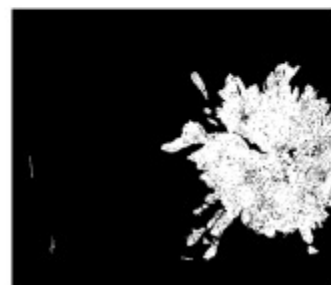
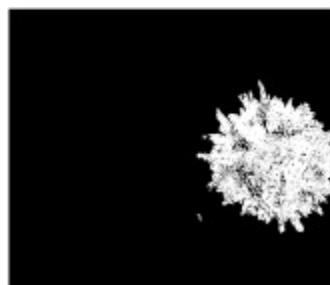
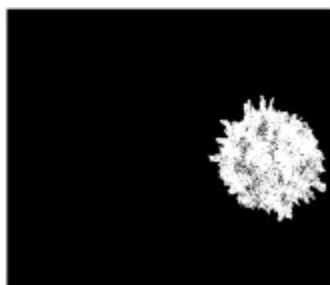
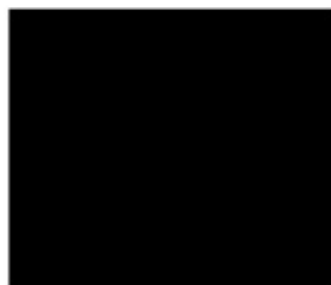
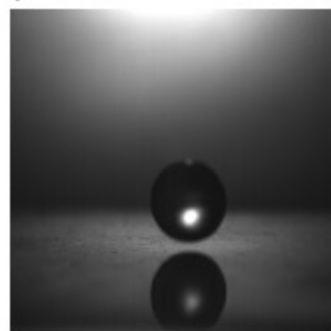
2.4 ms

Results: Increasing prism temperature

$U=1.3$ m/s $T=92$ K



Slowed down 500x



$t = 0$ ms

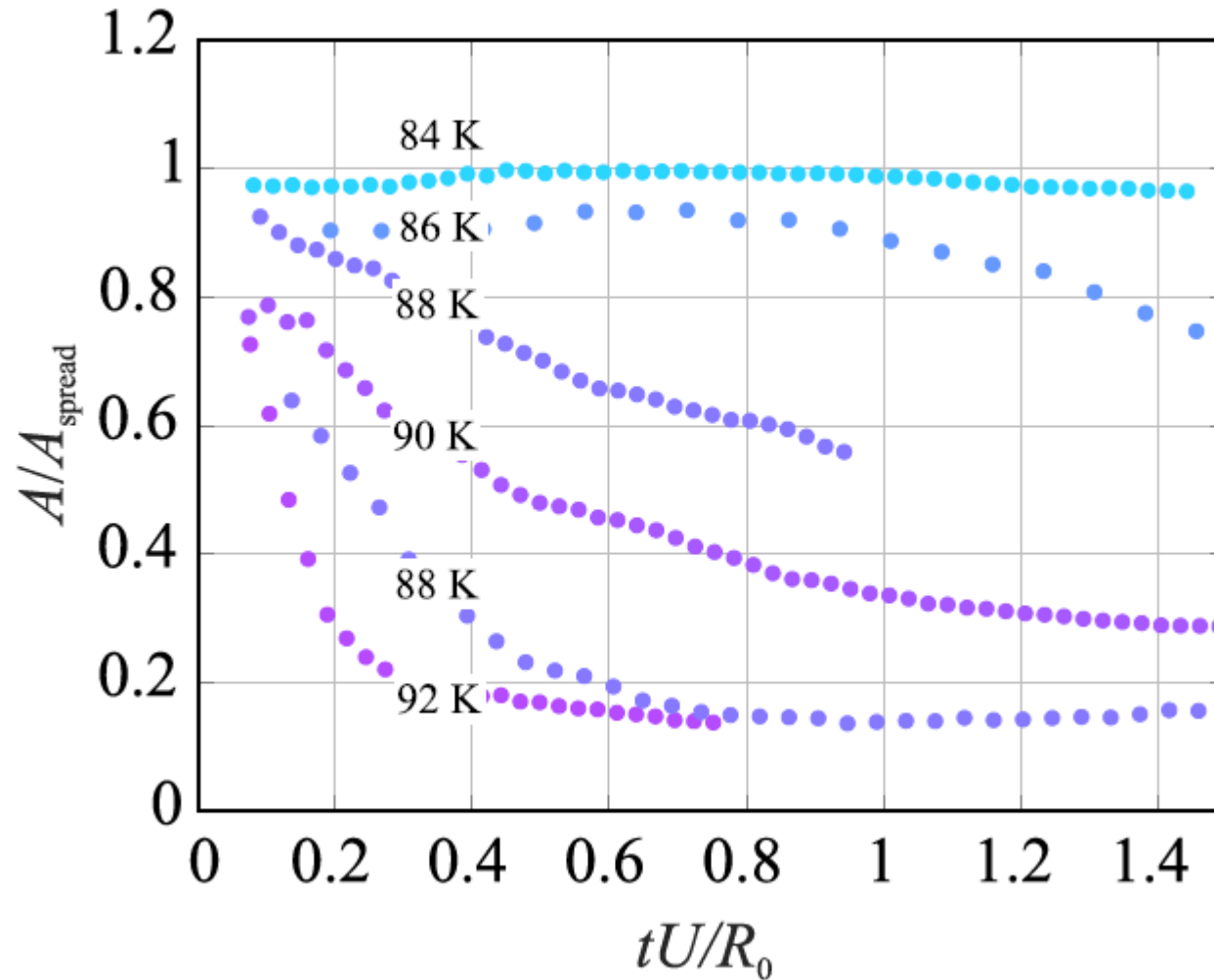
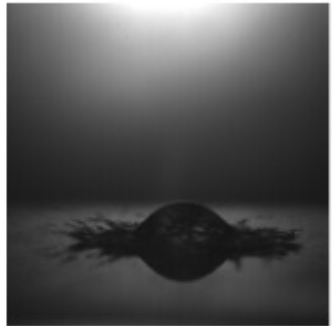
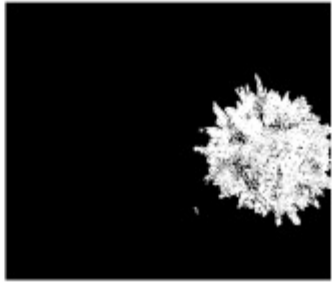
0.4 ms

0.8 ms

1.2 ms

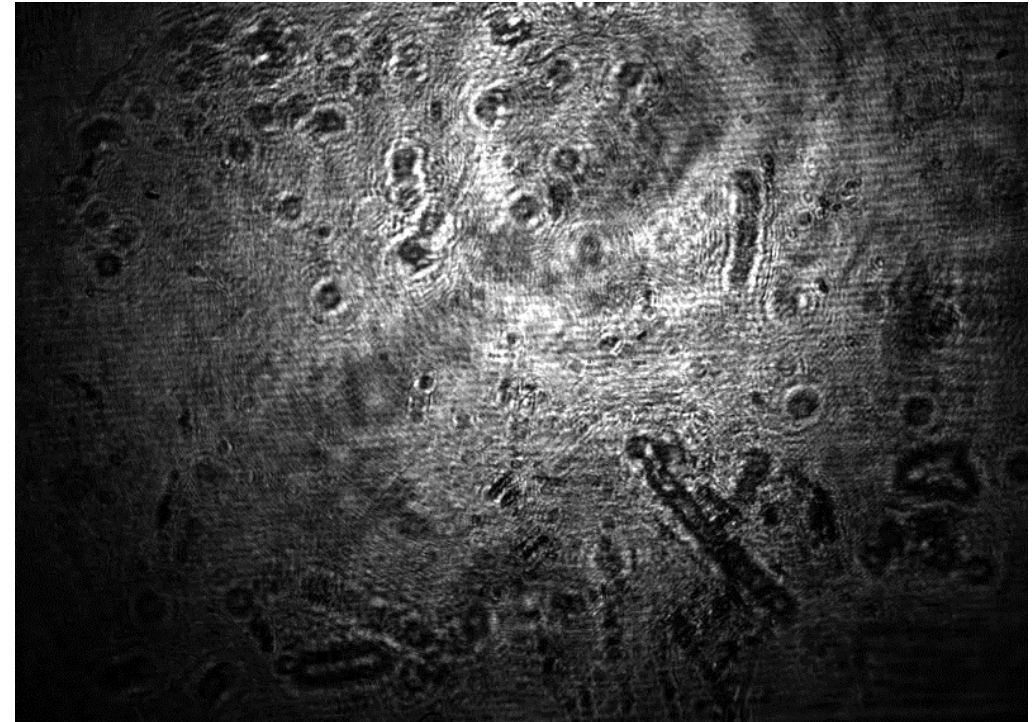
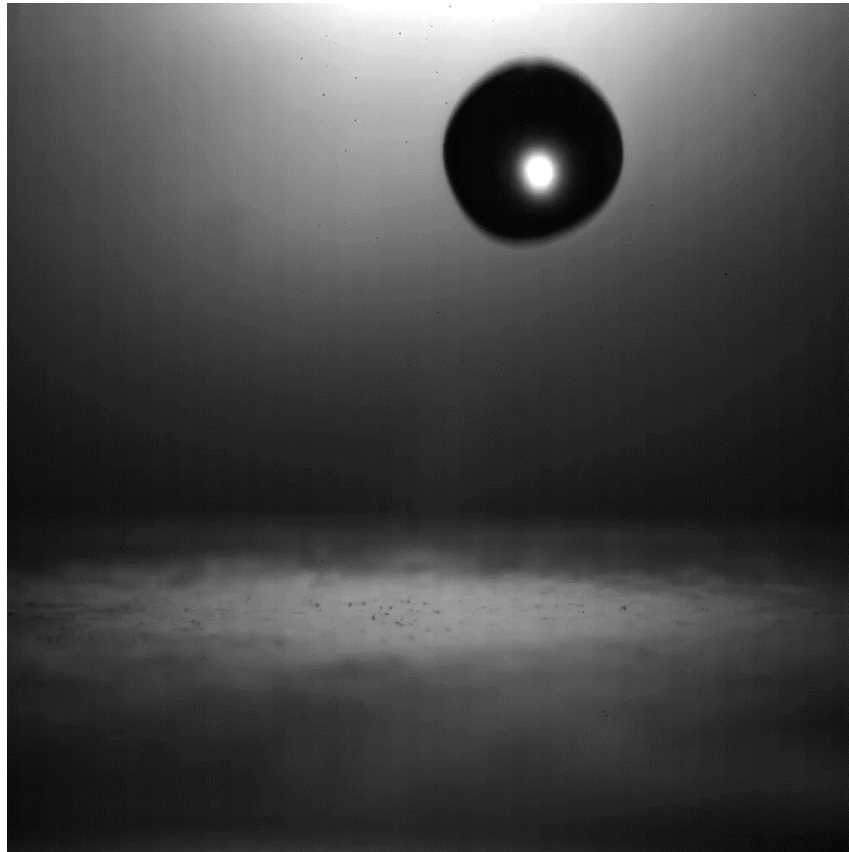
2.4 ms

Results: Transition boiling



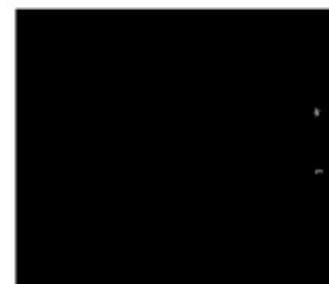
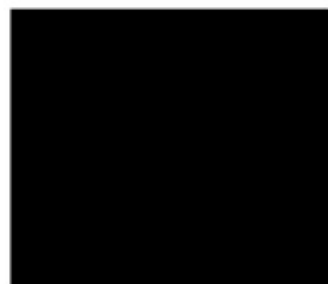
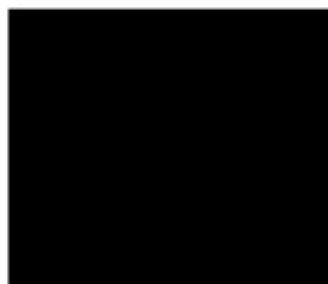
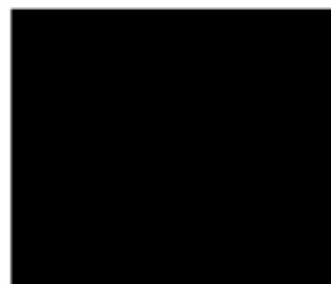
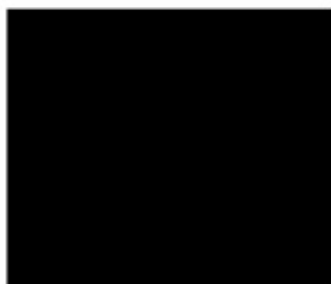
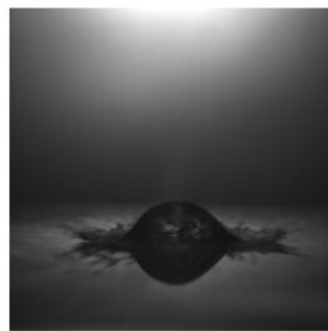
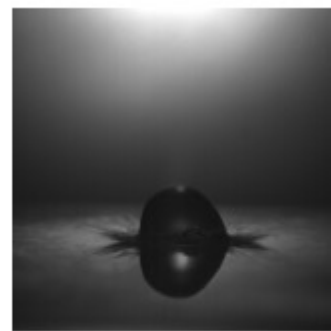
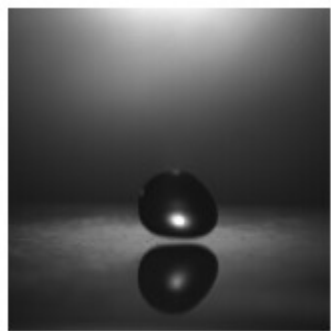
Results: Increasing plate temperature

$U=1.3$ m/s $T=102$ K



Slowed down 500x





$t = 0$ ms

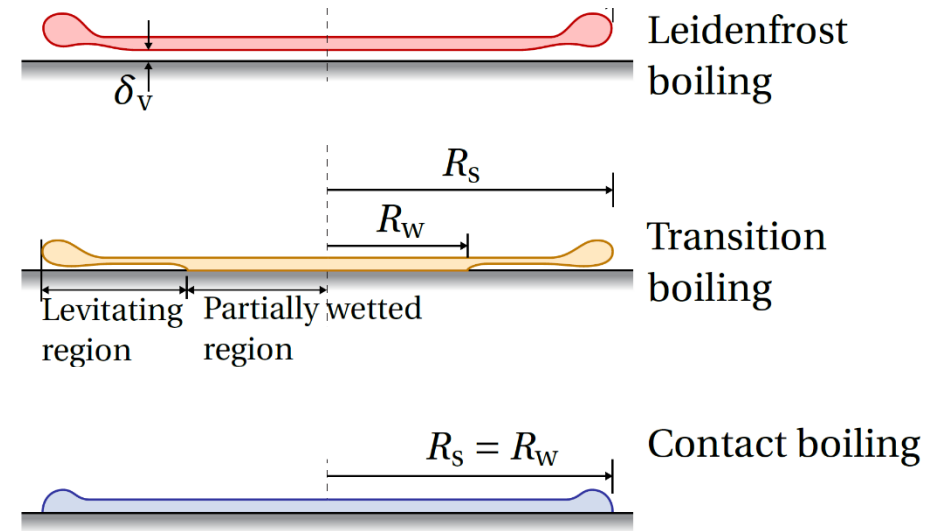
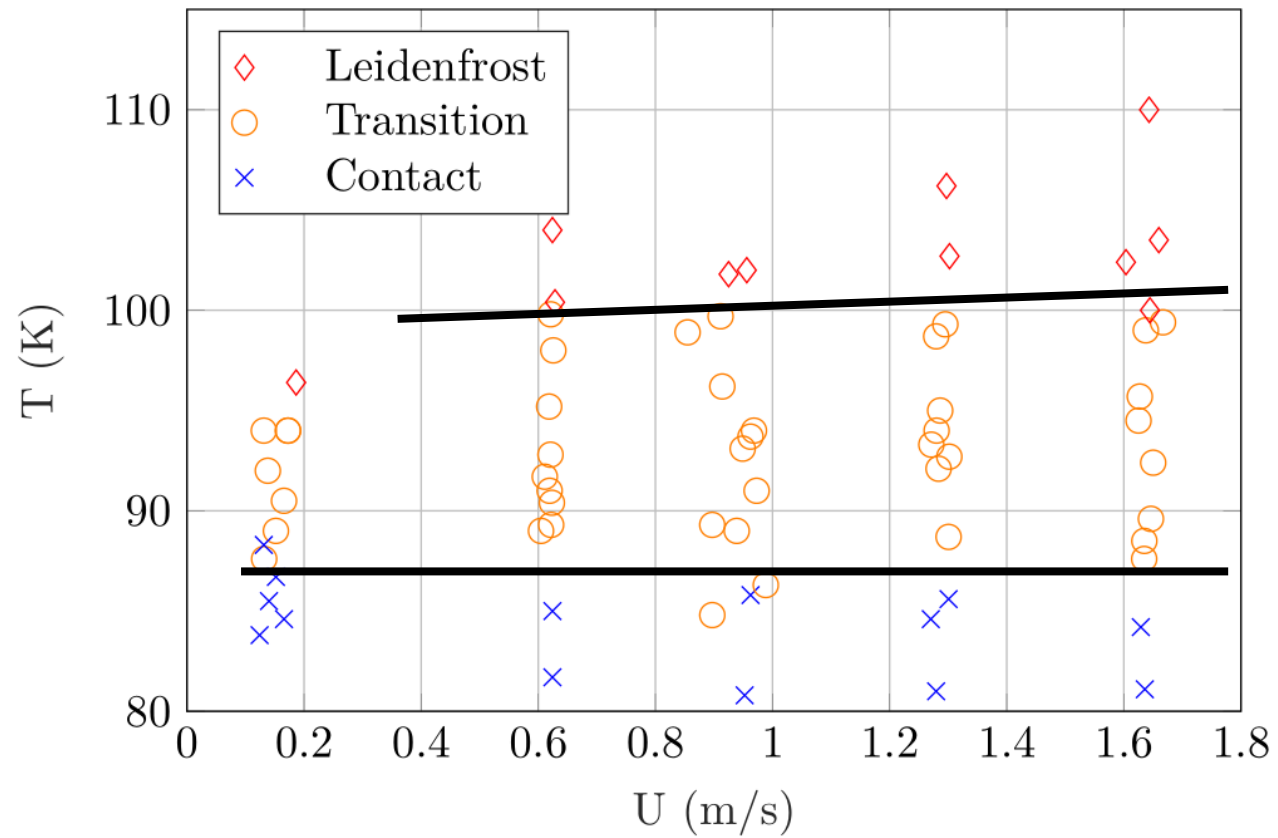
0.4 ms

0.8 ms

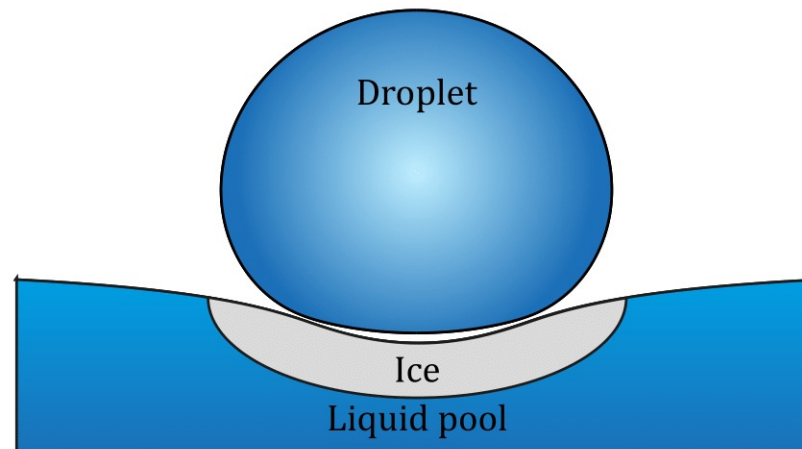
1.2 ms

2.4 ms

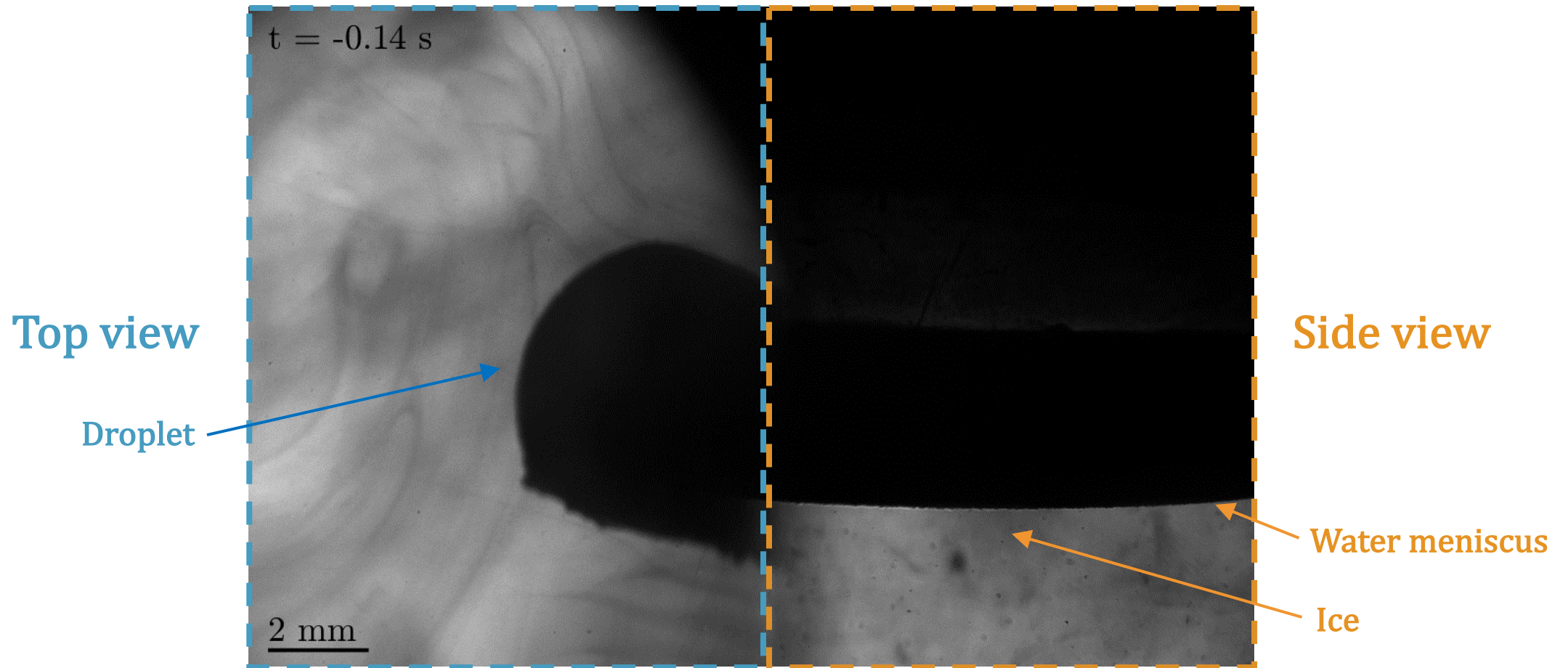
Phase diagram



Investigate both theoretically and experimentally
the dynamics of a Leidenfrost droplet
(liquid nitrogen) on a liquid pool (water)

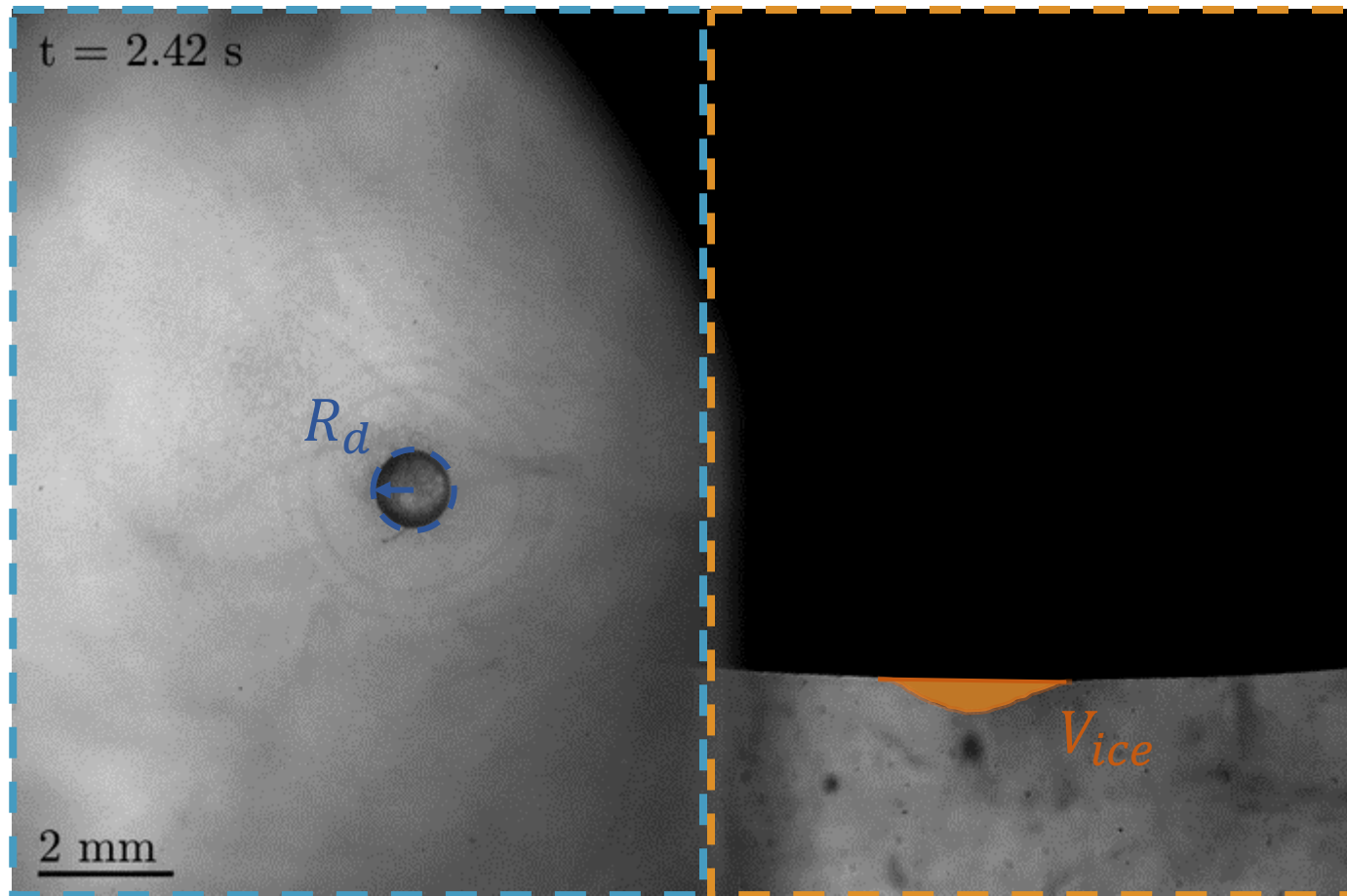


Leidenfrost droplet on a liquid pool



Leidenfrost droplet on a liquid pool

Top view



Side view

Outer part droplet

- Laplace pressure equals hydrostatic pressure

$$\gamma_d \kappa = -\rho_d g z$$

- Let κ_{top} be the input variable to determine the size

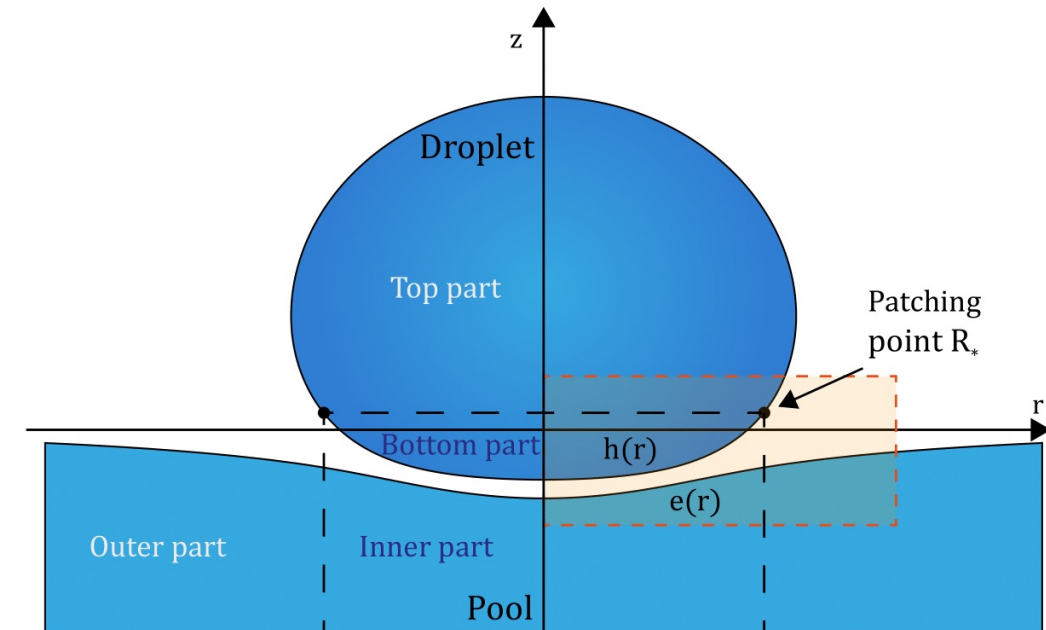
$$\tilde{\kappa}_{top} + \tilde{z}_{top} = \tilde{\kappa} + \tilde{z}$$

- Write in terms of arclength s

$$\frac{\partial \theta}{\partial s} = -\frac{\sin(\theta)}{r} - h + \kappa_{top}$$

$$\frac{\partial s}{\partial h} = \sin(\theta), \quad \frac{\partial r}{\partial s} = \cos(\theta)$$

- Integrate from $s = 0$ to $s = s_t$ with $\theta(0) = 0, h(0) = z_{top}, r(0) = 0, \theta(s_t) = -\pi$



Inner part droplet

- Excess pressure in vapour film p_v can be found by balancing all forces normal to the drop surface

$$\tilde{p}_v + \tilde{\kappa} = \tilde{\kappa}_{top} + (\tilde{z}_{top} - \tilde{h})$$

- This pressure drives a lubrication flow with no-slip conditions on both sides

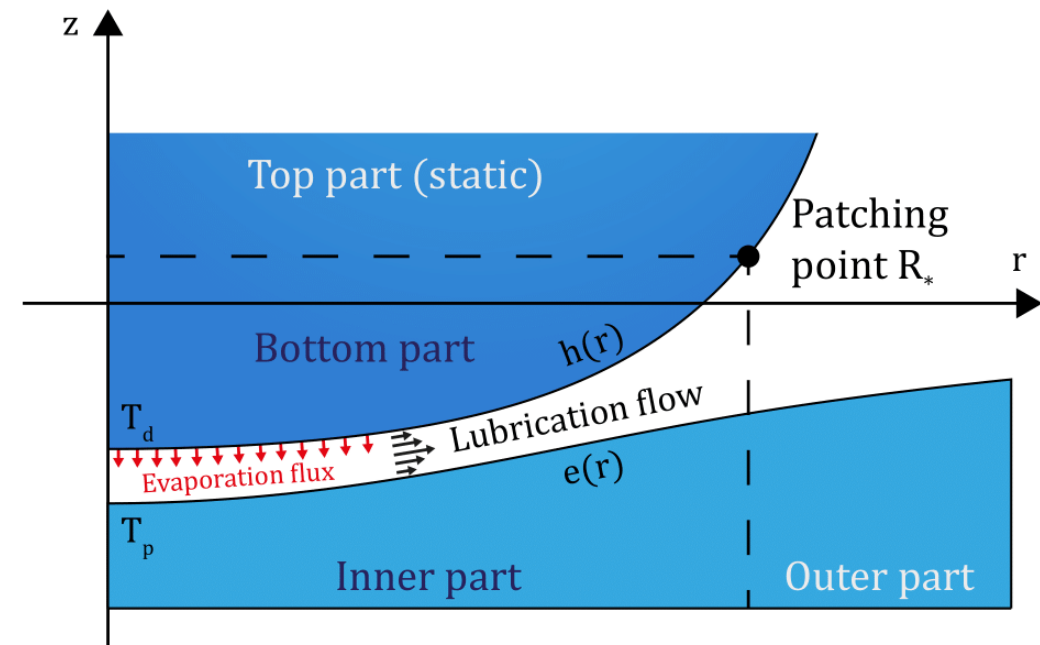
$$\vec{q}_v = -\frac{\nabla p_v}{12\mu_v} (h - e)^3$$

- The local evaporation flux is equal to

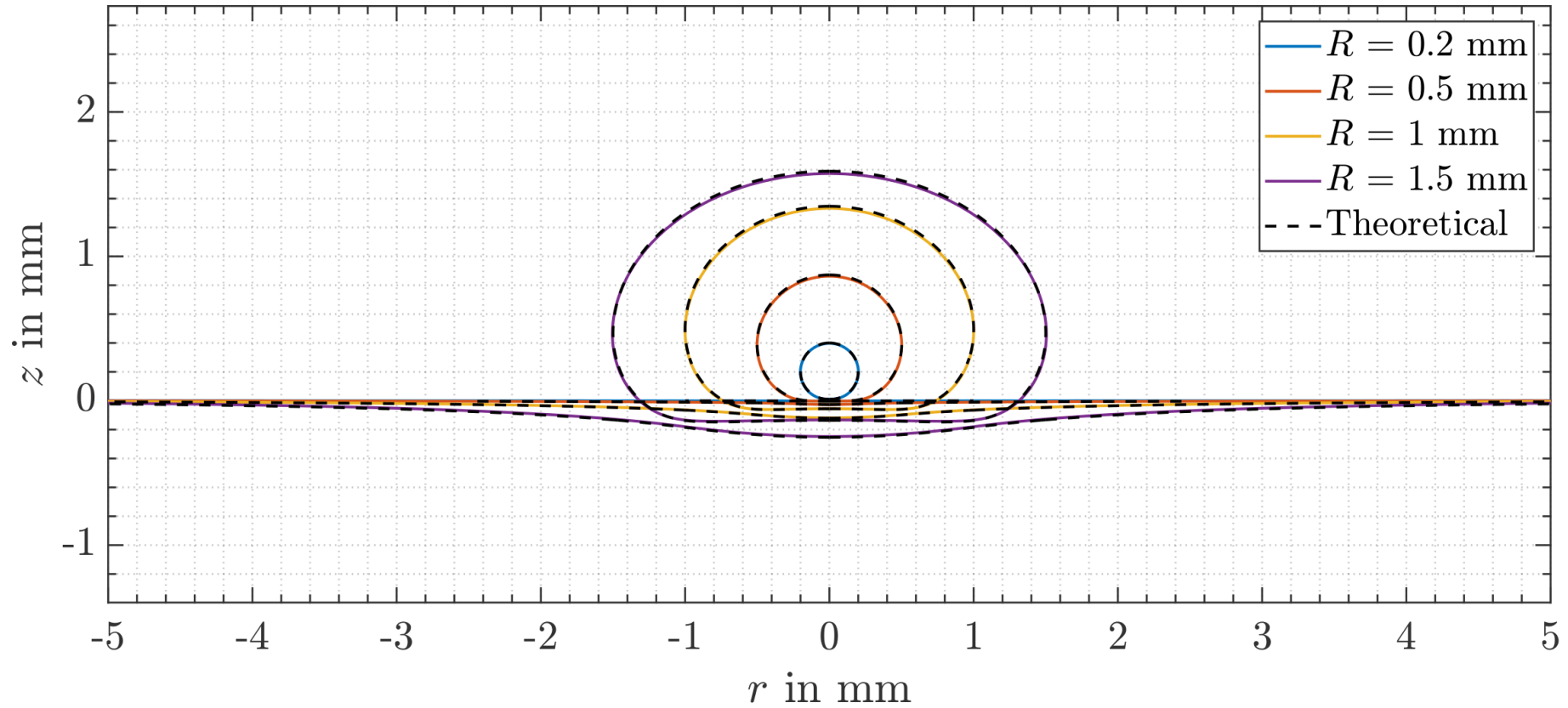
$$J = \frac{q}{L} = \frac{1}{L} \frac{\lambda_v (T_p - T_d)}{(h - e)}$$

- Finally, mass conservation gives us

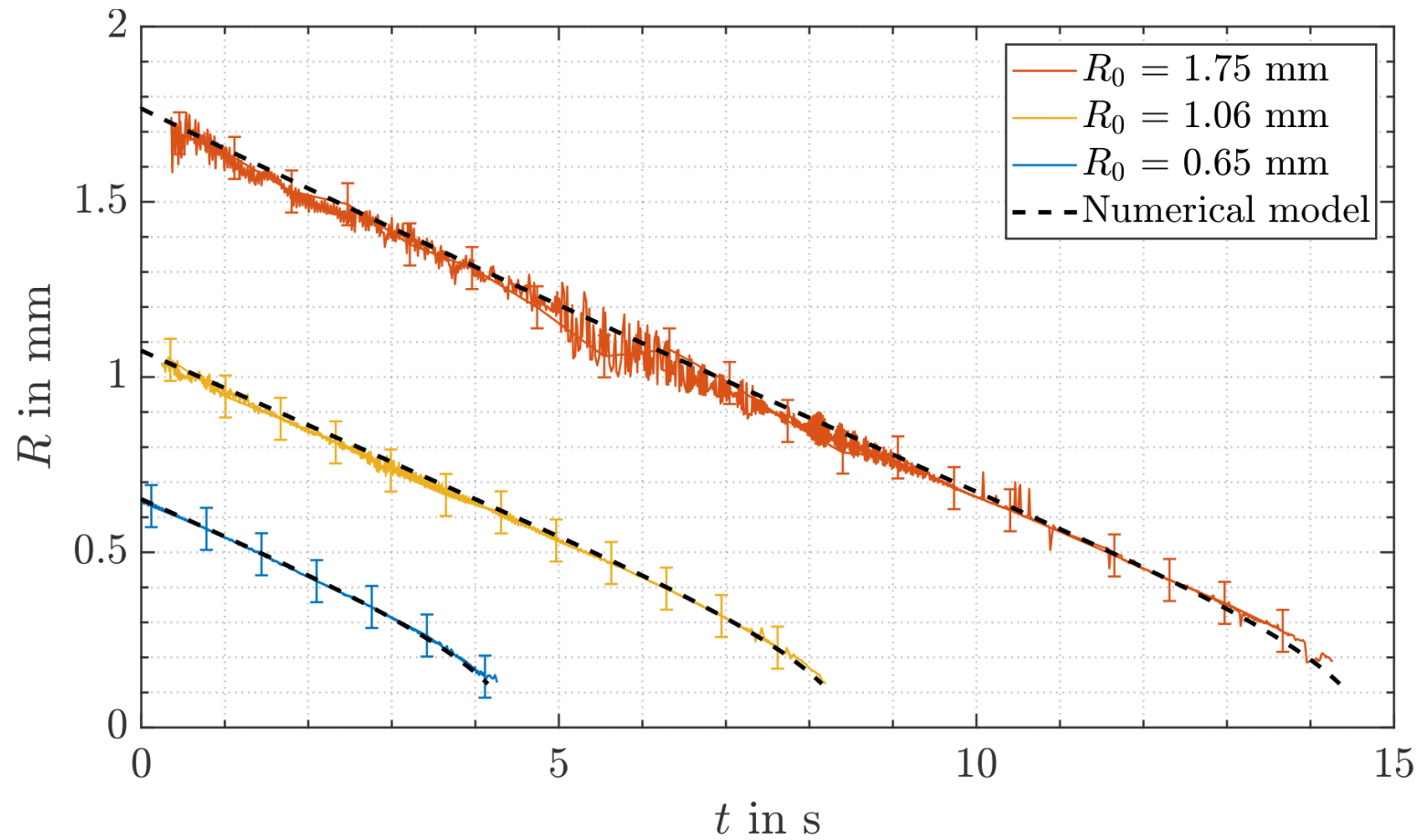
$$\vec{\nabla} \cdot q_v = \frac{J}{\rho_v}$$

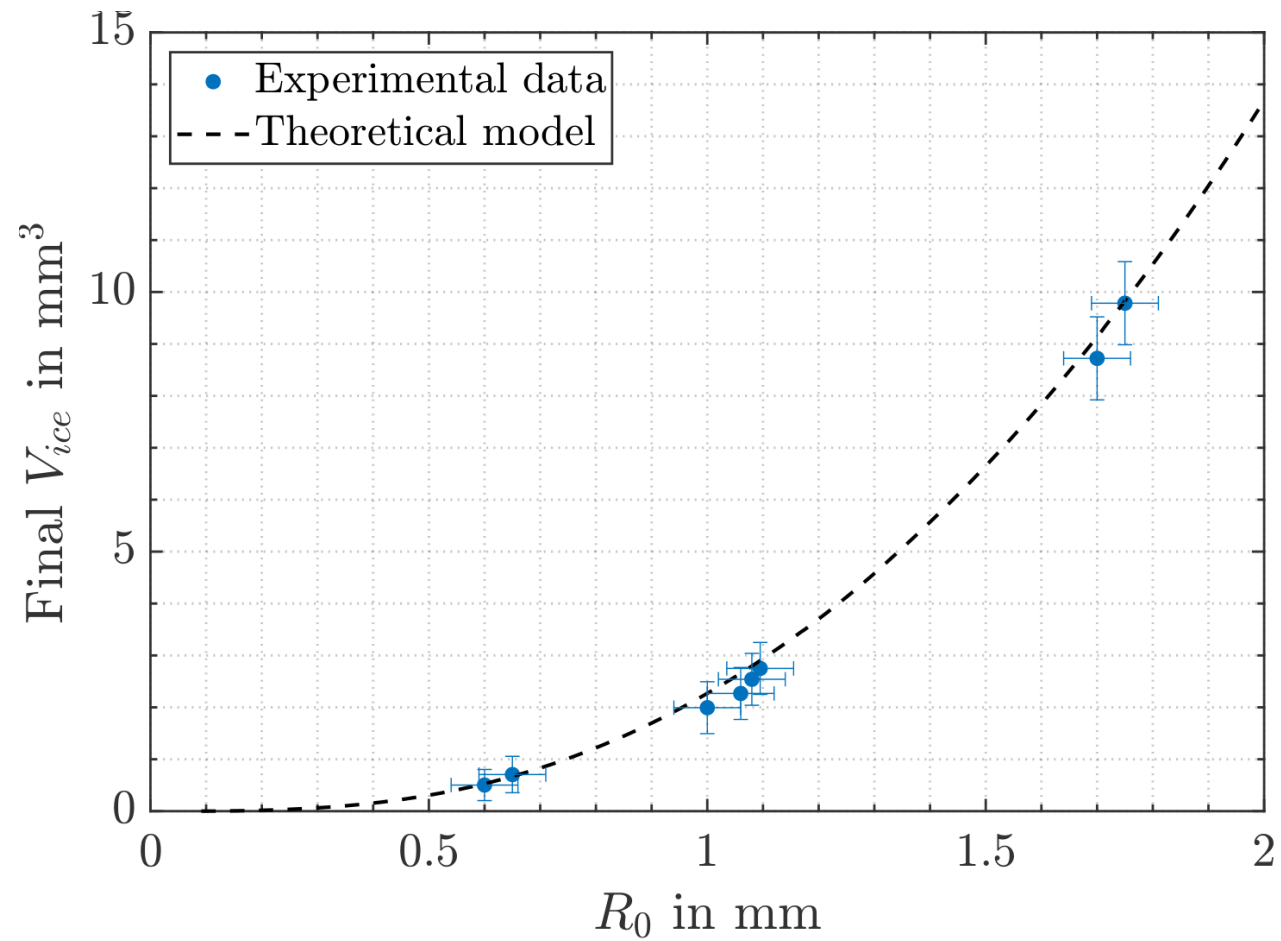


Numerical model shape



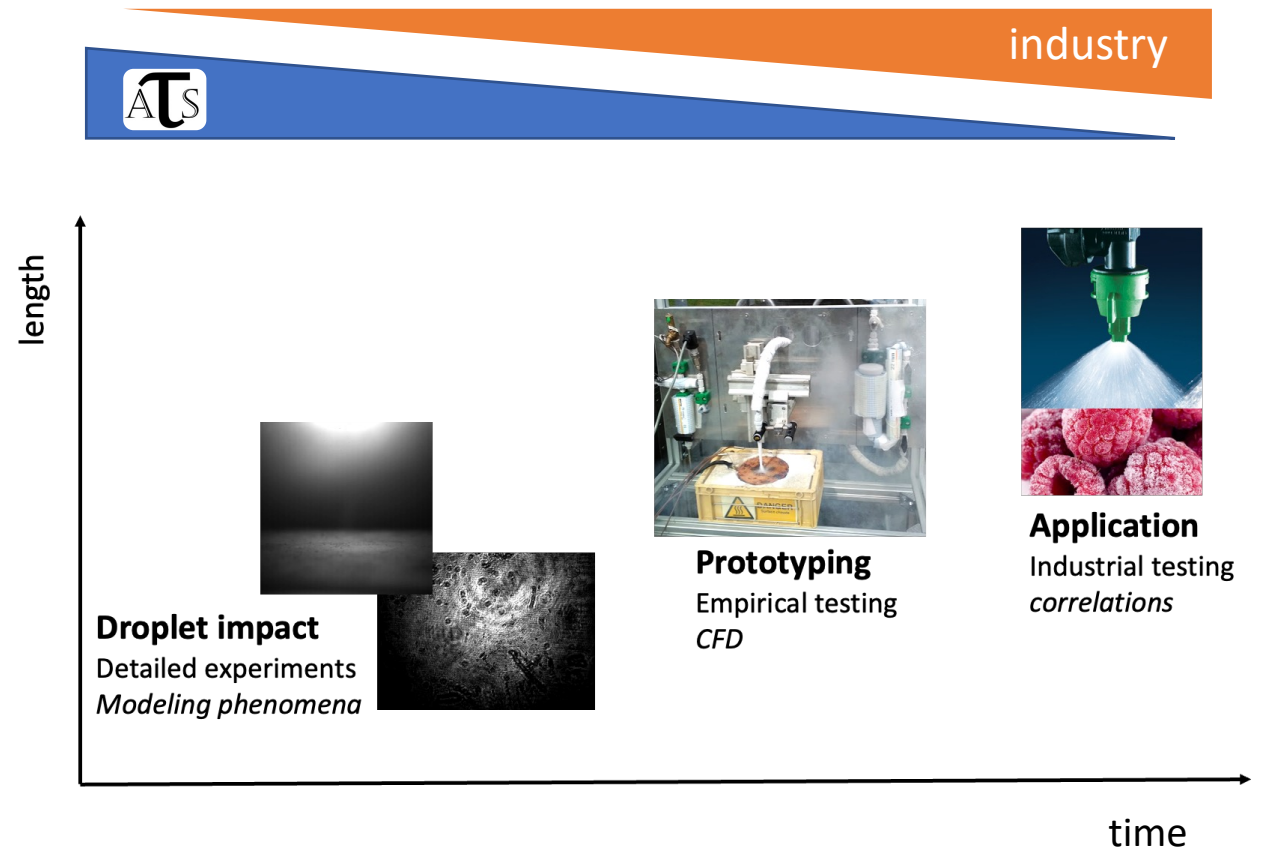
Experimental results $R(t)$ ($T_{(p,0)}=273.15$ K)





MISSION & APPROACH

to identify specific phenomena and mechanisms that are key in understanding the cryogenic cooling processes and propose engineering models.



Wouter



Pankaj



Marijn

Daniel



Jan-Willem



Jenny



Ruben



Markus



Harry

