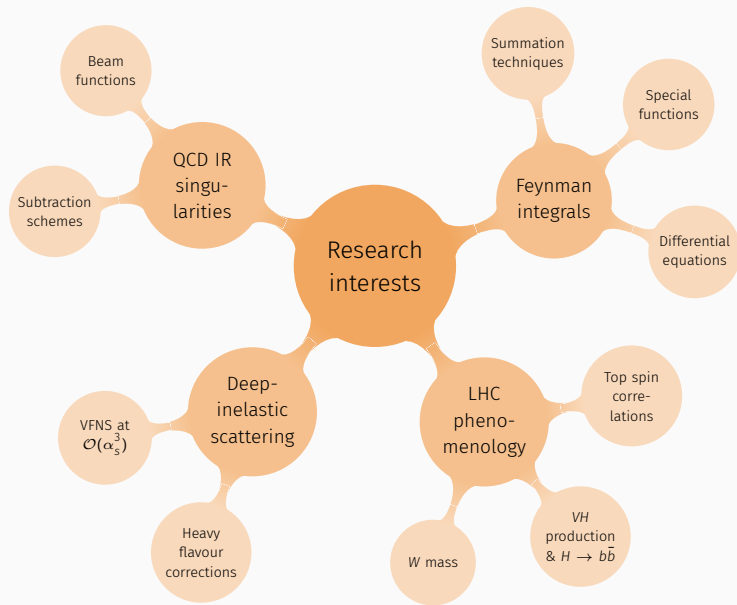




Arnd Behring

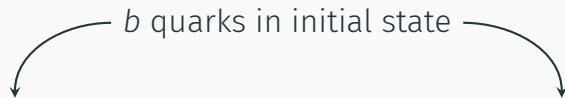
Particle physics on
long-distance trains

My research interests



Variable flavour number scheme at $O(\alpha_s^3)$

b quarks in initial state



massless u, d, s, c and massive b

- u, d, s, c PDFs
- b only produced perturbatively
- potentially large $\ln(Q^2/m_b^2)$

massless u, d, s, c and b

- u, d, s, c and b PDFs
- DGLAP equations resum collinear singularities

- Appropriate description depends on relevant scales of the process
- Match PDFs in both schemes at a matching scale, e.g.,

$$f_Q(n_f + 1) + f_{\bar{Q}}(n_f + 1) = A_{Qq}^{\text{PS}} \otimes \sum_k [f_k(n_f) + f_{\bar{k}}(n_f)] + A_{Qg} \otimes G(n_f)$$

Variable flavour number scheme at $O(\alpha_s^3)$ (cont.)

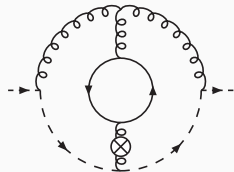
Matching coefficients A_{ij} can be calculated perturbatively:

Massive operator matrix elements (OMEs)

$$A_{ij} \sim \langle j|O_i|j\rangle$$

Until recently: 5 of 7 OMEs known to $O(\alpha_s^3)$

→ Important, e.g., for N³LO PDFs



Variable flavour number scheme at $O(\alpha_s^3)$ (cont.)

Matching coefficients A_{ij} can be calculated perturbatively:

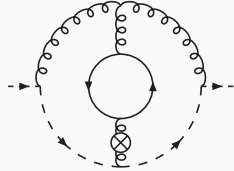
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Many of the results in this project were obtained while on the train between Berlin ↔ Dortmund/Bielefeld during my PhD



Variable flavour number scheme at $O(\alpha_s^3)$ (cont.)

Matching coefficients A_{ij} can be calculated perturbatively:

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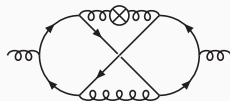
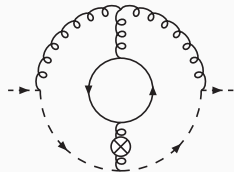
New progress in past few weeks: Finished $A_{gg,Q}^{(3)}$

Enters matching relation for gluons:

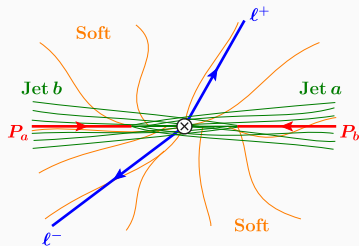
$$G(n_f + 1) = A_{gq,Q}(n_f) \otimes \sum_k [f_k(n_f) + f_{\bar{k}}(n_f)] + A_{gg,Q} \otimes G(n_f)$$

Paper (CERN-TH-2022-179) on arXiv later this week:

[J. Ablinger, AB, J. Blümlein, A. De Freitas, A. Goedicke, A. von Manteuffel, C. Schneider, K. Schönwald '22]



Beam functions for N -jettiness at $N^3\text{LO}$



Long-running project to calculate the beam functions for N -jettiness (τ_N) at $N^3\text{LO}$

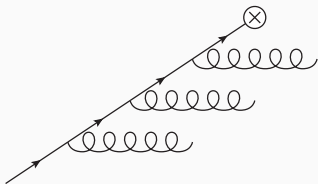
[Melnikov, Rietkerk, Tancredi, Wever '18] [Melnikov, Rietkerk, Tancredi, Wever '19]

[AB, Melnikov, Rietkerk, Tancredi, Wever '19]

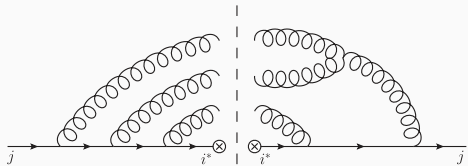
- Appear in factorisation theorem for $\tau_0 \rightarrow 0$

$$\lim_{\tau_0 \rightarrow 0} \sigma = B \otimes B \otimes S \otimes H \otimes \sigma_{\text{LO}} + O(\tau)$$

- Describe collinear emissions off the initial state
- Building block for
 - Slicing scheme \rightarrow differential description of colour singlet production at $N^3\text{LO}$
 - Resummation

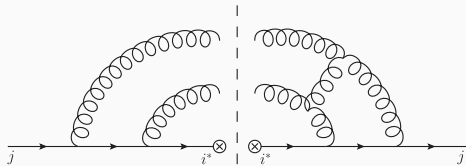


Beam functions for N -jettiness at $N^3\text{LO}$ (cont.)



Axial gauge calculation

$$D^{\mu\nu}(k) = \frac{1}{k^2} \left(-g^{\mu\nu} + \frac{k^\mu \bar{p}^\nu + k^\nu \bar{p}^\mu}{k \cdot \bar{p}} \right)$$



Partial fraction rel. between MI

$$\frac{1}{(k_1 \cdot \bar{p})(k_2 \cdot \bar{p})} = \frac{2}{s\bar{z}} \left[\frac{1}{k_1 \cdot \bar{p}} + \frac{1}{k_2 \cdot \bar{p}} \right]$$

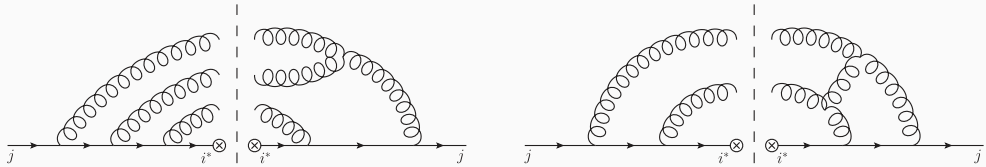
Canonical bases with square roots

$$\frac{d}{dz} \begin{pmatrix} l_1 \\ l_2 \\ \vdots \end{pmatrix} = \varepsilon \begin{pmatrix} \blacksquare & & & \\ \blacksquare & \blacksquare & & \\ \blacksquare & \blacksquare & \blacksquare & \\ \blacksquare & & \blacksquare & \ddots \end{pmatrix} \begin{pmatrix} l_1 \\ l_2 \\ \vdots \end{pmatrix}$$

Iterated integrals with square roots

$$\int_0^z \frac{dz'}{\sqrt{z'}\sqrt{4-z'}} \int_0^{z'} \frac{dz''}{\sqrt{4+z''}} \int_0^{z''} \dots$$

Beam functions for N -jettiness at $N^3\text{LO}$ (cont.)

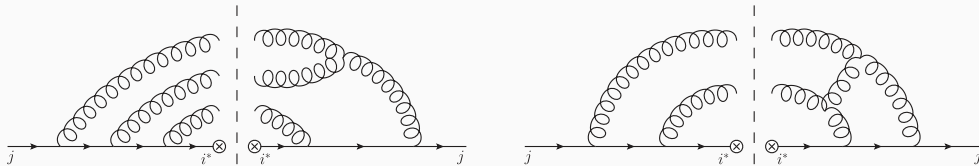


There are 5 independent matching coefficients:

- $q_j \rightarrow q_i$: Finished in Karlsruhe
- $g \rightarrow q$:
- $q \rightarrow g$:
- $g \rightarrow g$:
- $\bar{q}_j \rightarrow q_i$:



Beam functions for N -jettiness at $N^3\text{LO}$ (cont.)

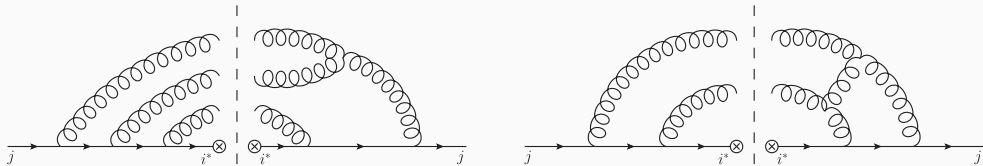


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- $\bar{q}_j \rightarrow q_i$:



Beam functions for N -jettiness at $N^3\text{LO}$ (cont.)

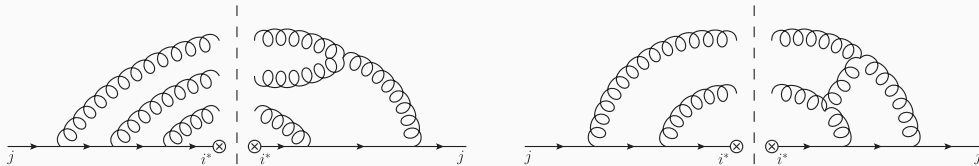


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- $g \rightarrow g$: Finished at CERN
- $\bar{q}_j \rightarrow q_i$:



Beam functions for N -jettiness at $N^3\text{LO}$ (cont.)

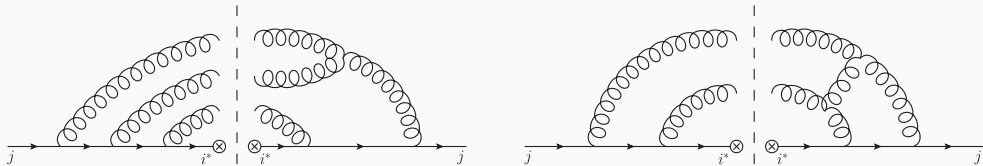


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- $\bar{q}_j \rightarrow q_i$: Finished on the train in Karlsruhe Hbf



Beam functions for N -jettiness at $N^3\text{LO}$ (cont.)



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Paper (CERN-TH-2022-178) on arXiv later this week:

[D. Baranowski, AB, K. Melnikov, L. Tancredi, C. Wever '22]

Future directions

VBF & $h \rightarrow b\bar{b}$ @ NNLO with $m_b \neq 0$

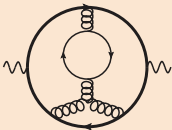
with K. Asteriadis, F. Caola,
K. Melnikov, R. Röntsch



Effects from $m \neq 0$?
Flavour jet alg.?

Four-loop ρ parameter

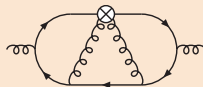
with S. Abreu, A. McLeod, B. Page



Two-mass contributions (m_b & m_t)
New functions?

Massive OME $A_{Qg}^{(3)}$

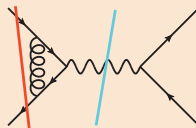
with J. Blümlein, A. De Freitas,
C. Schneider, K. Schönwald



Last missing OME
New functions?

Local unitarity for the LHC

with V. Hirschi, B. Ruijl, Z. Capatti



Deal with hadronic
initial states