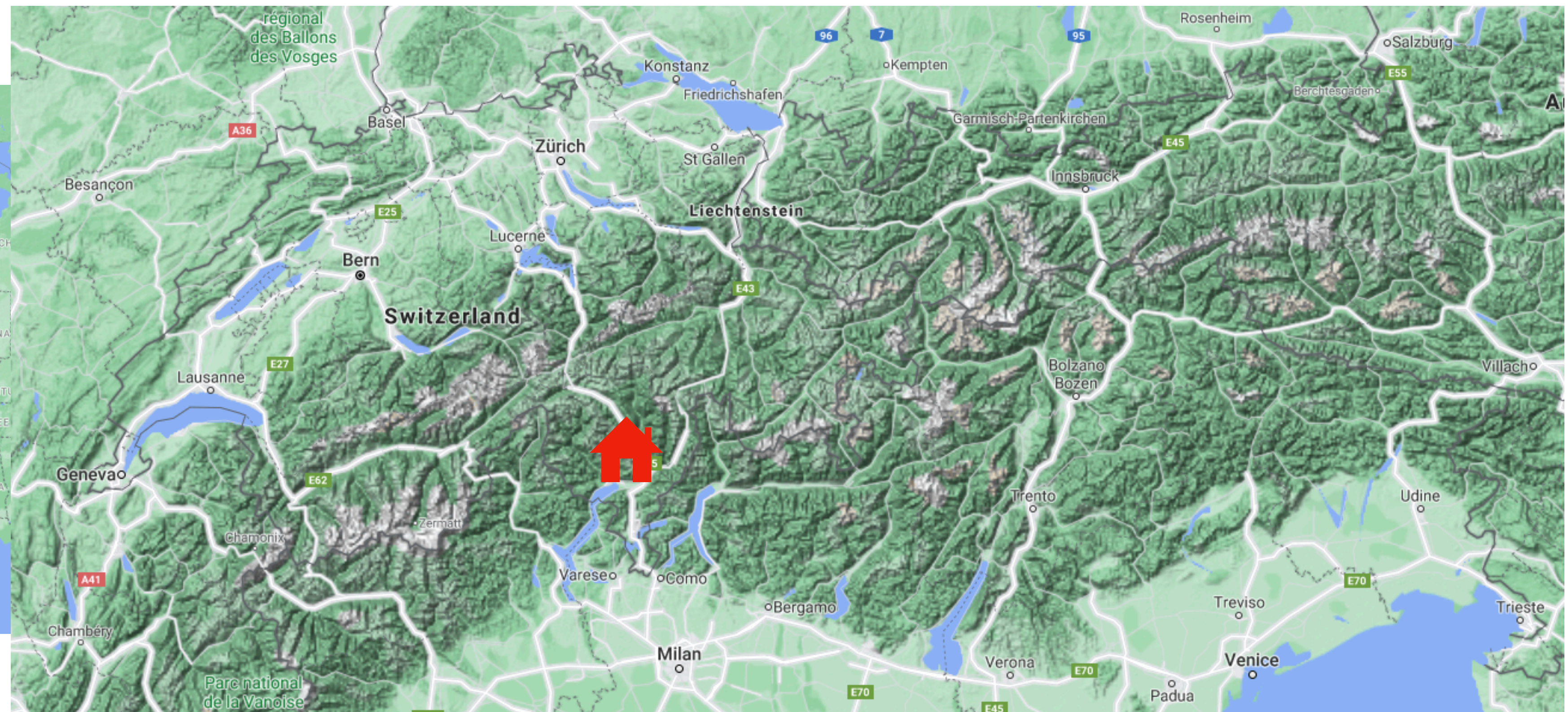


CERN Theory Group Retreat 2022

Enea Di Dio



CERN Theory Group Retreat 2022

Enea Di Dio



2005-2010

CERN Theory Group Retreat 2022

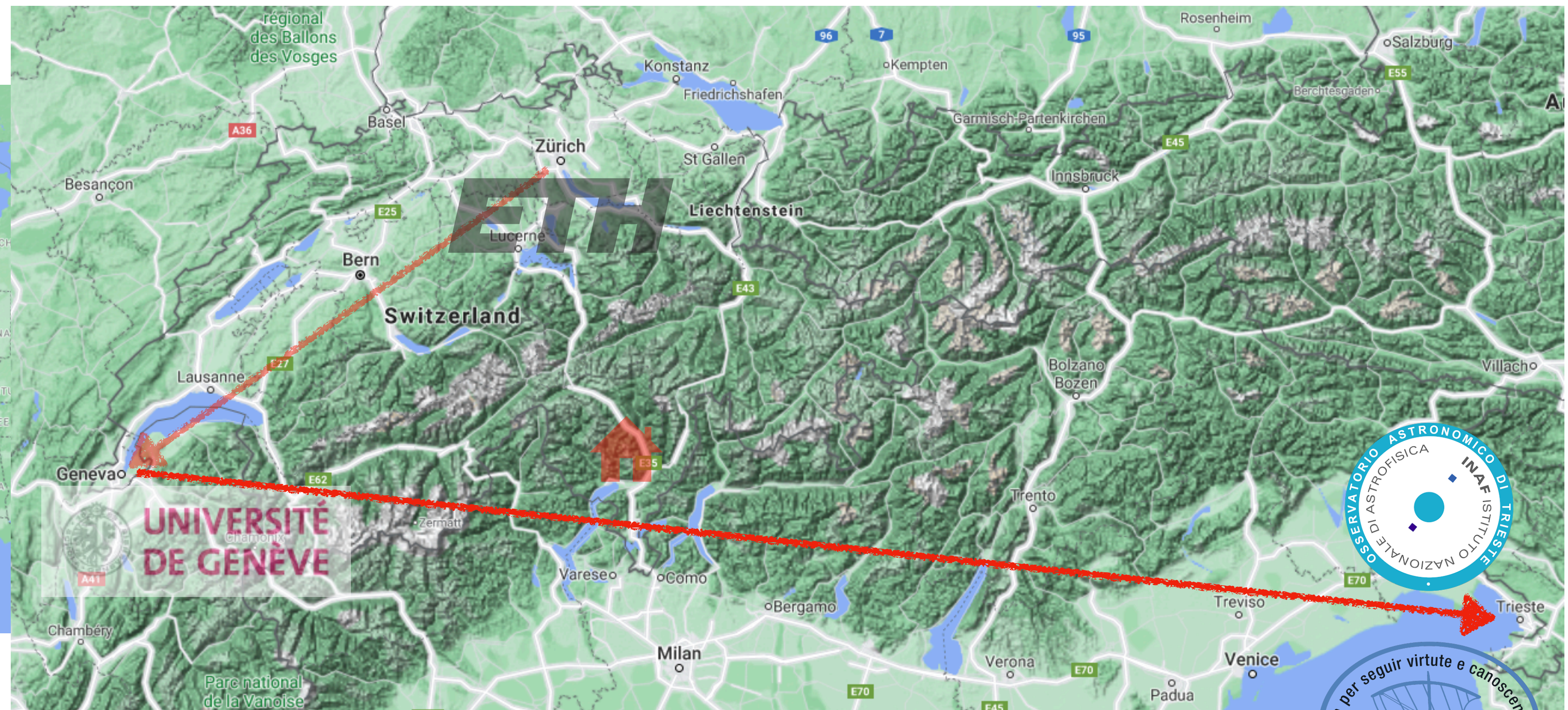
Enea Di Dio



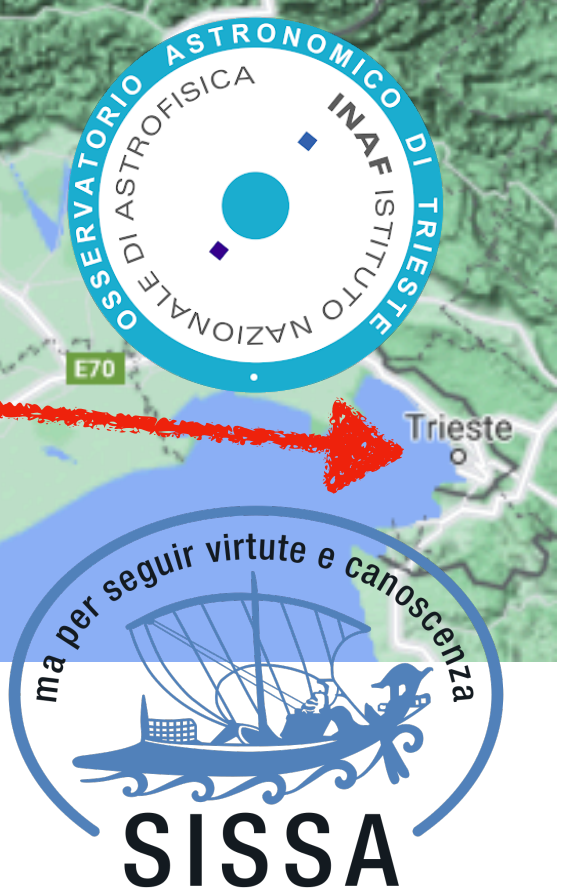
2010-2014

CERN Theory Group Retreat 2022

Enea Di Dio

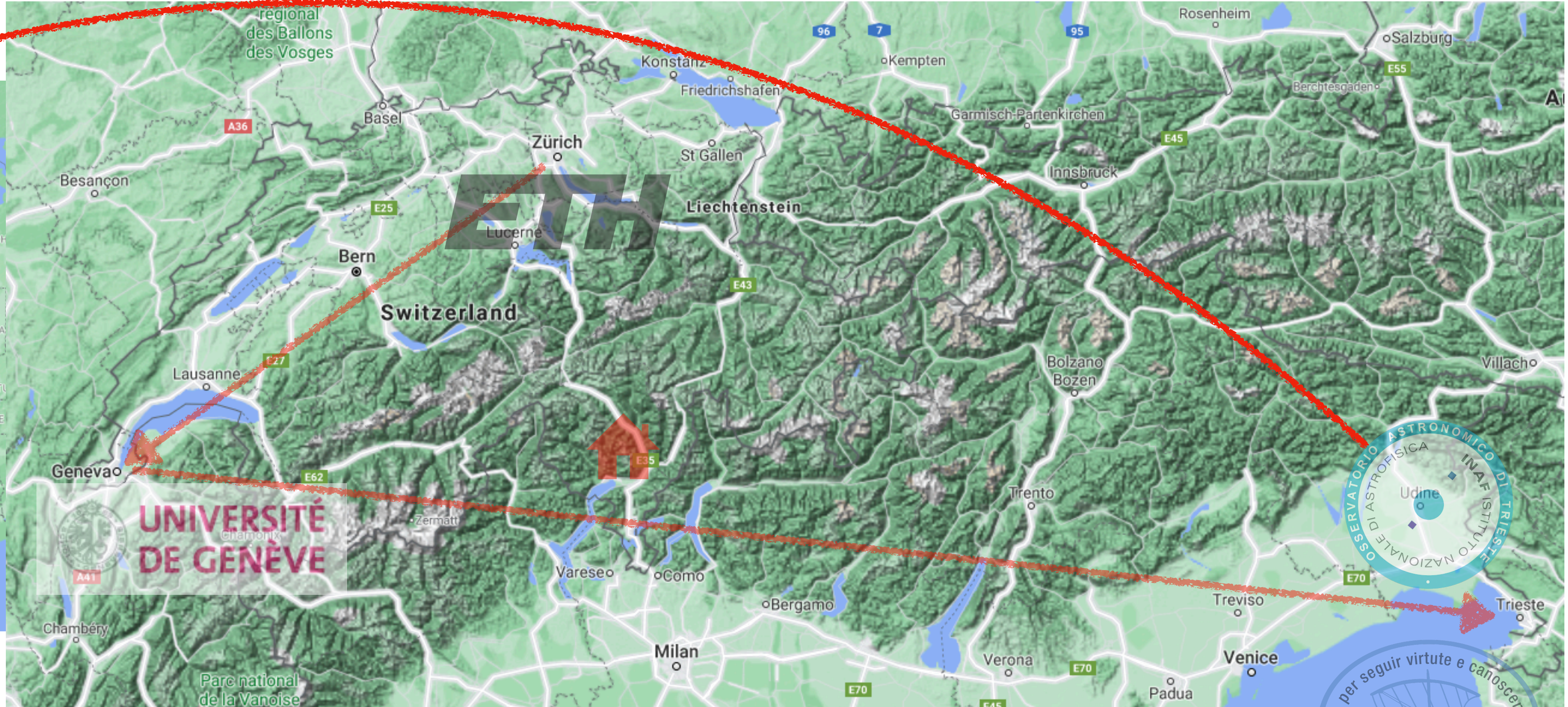


2014-2017



CERN Theory Group Retreat 2022

Enea Di Dio

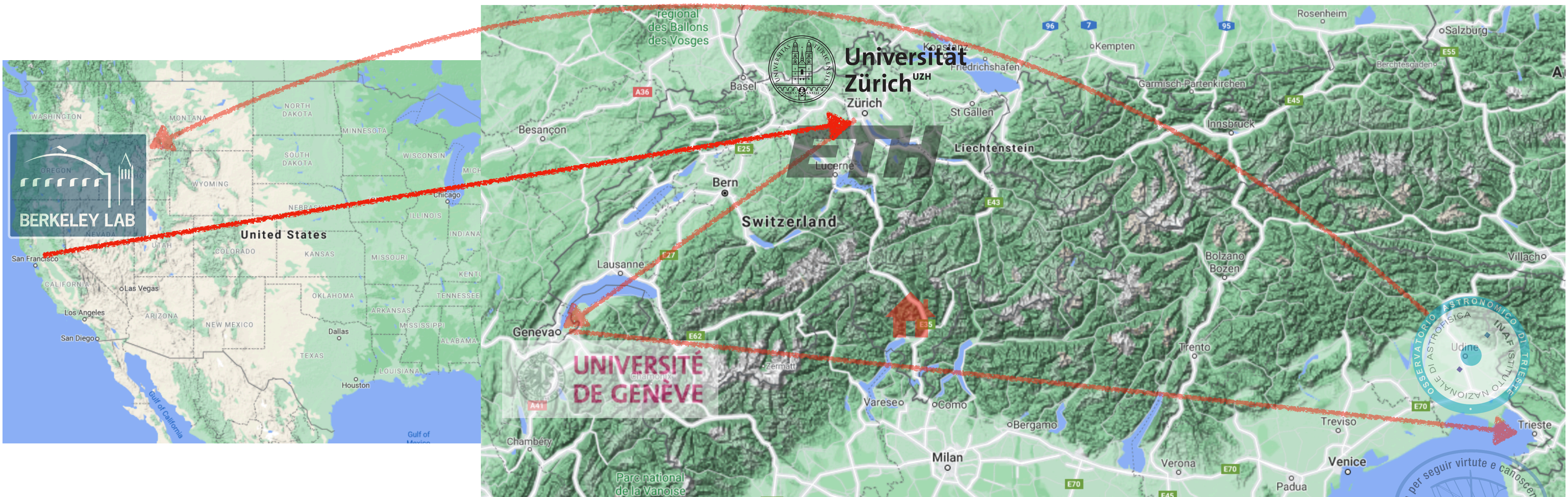


2017-2019

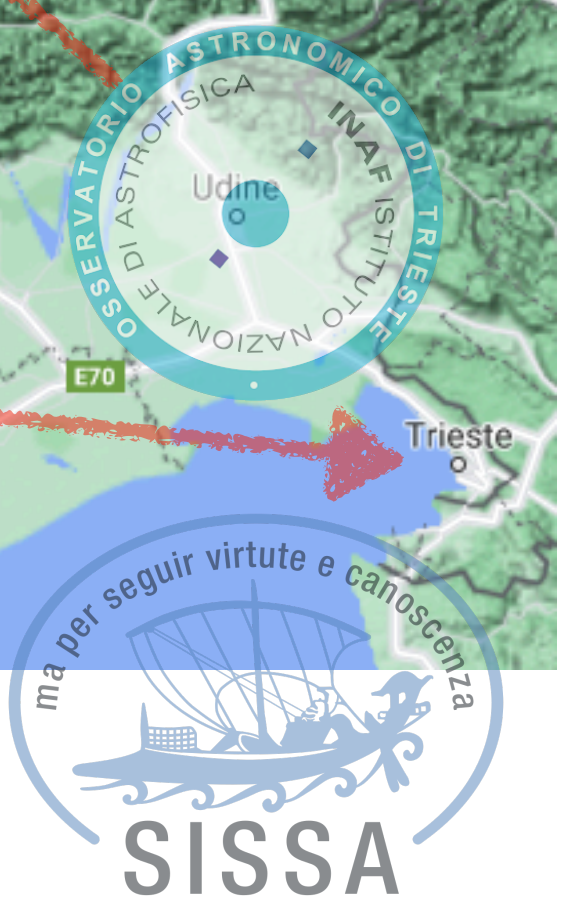


CERN Theory Group Retreat 2022

Enea Di Dio



2019-2020



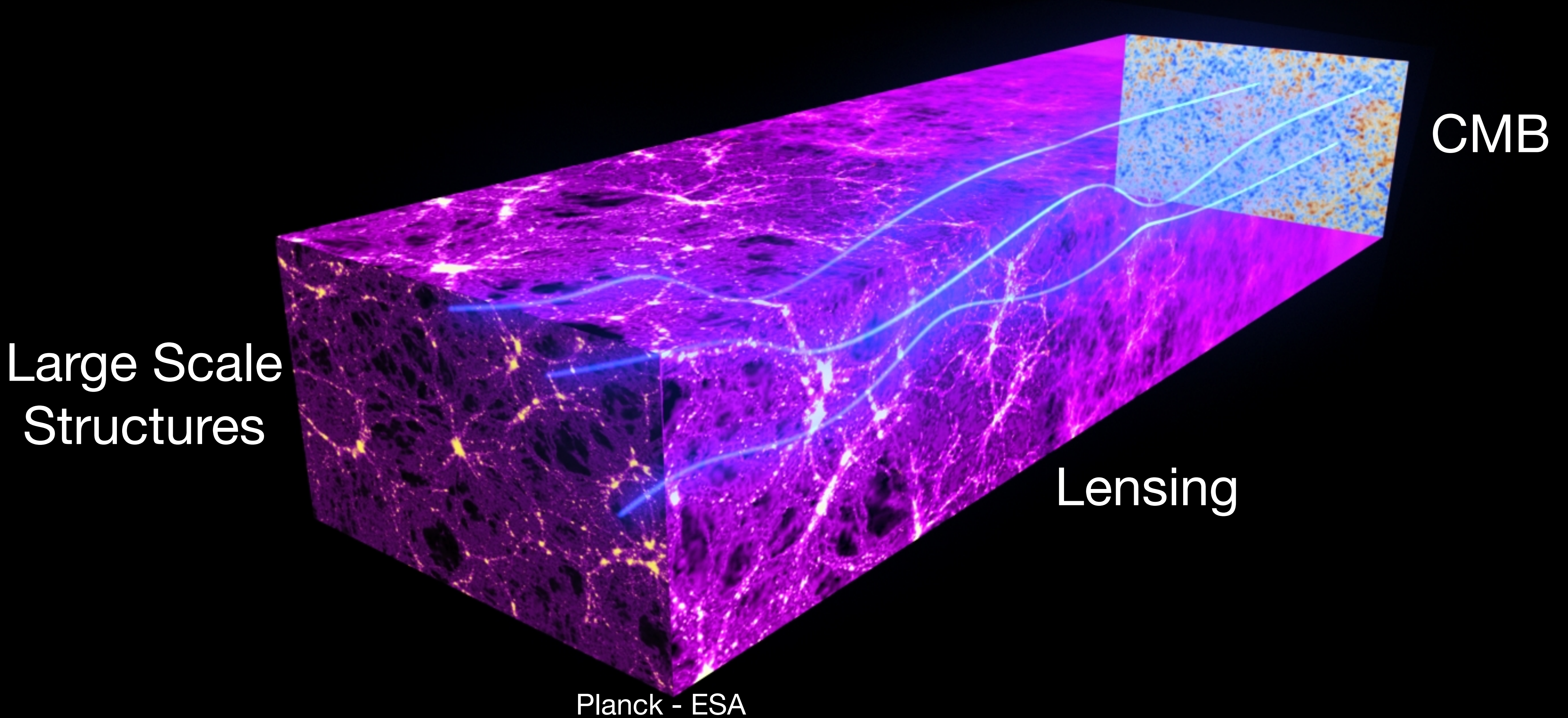
CERN Theory Group Retreat 2022

Enea Di Dio

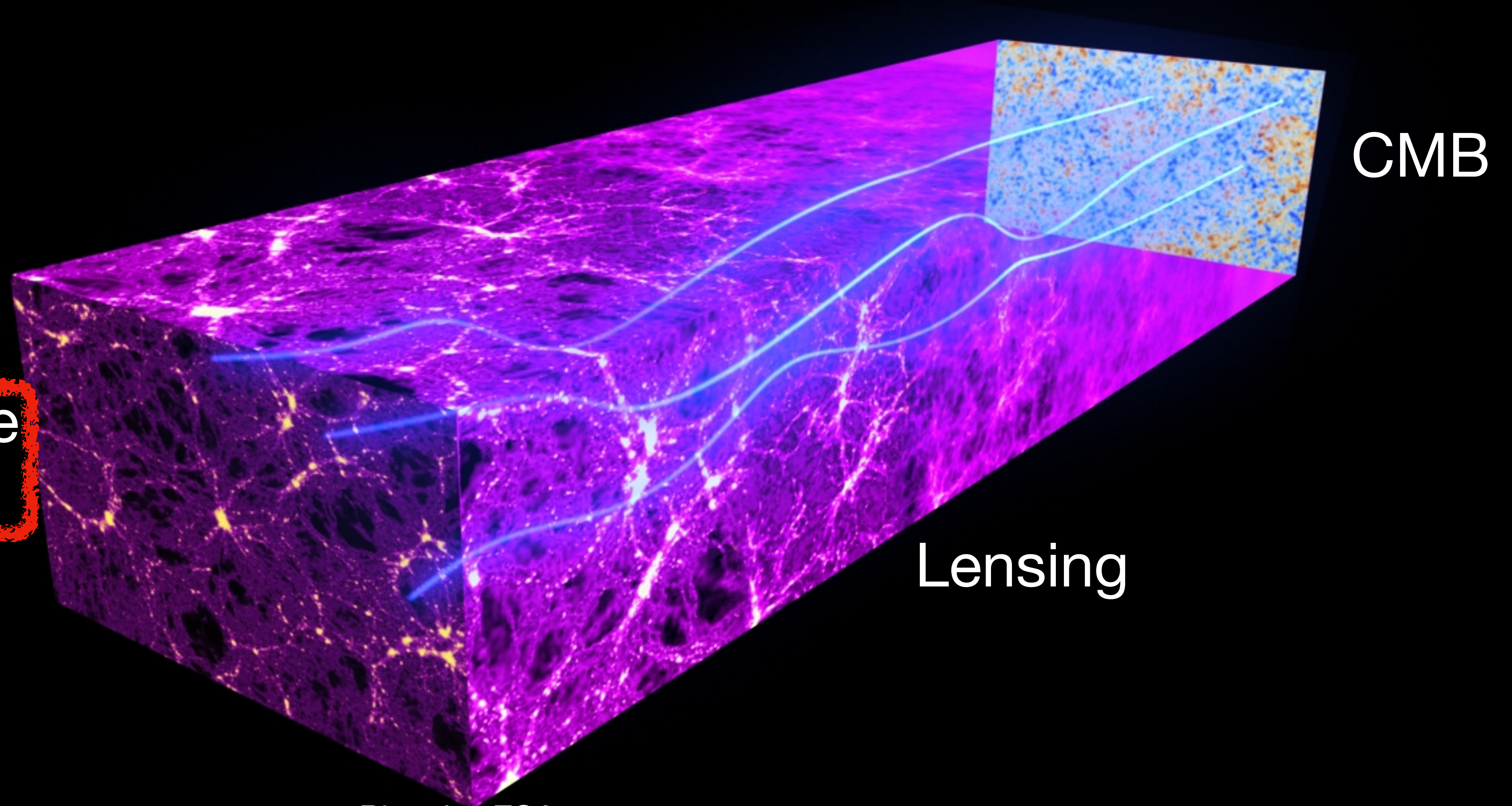


from 2020

My research interests

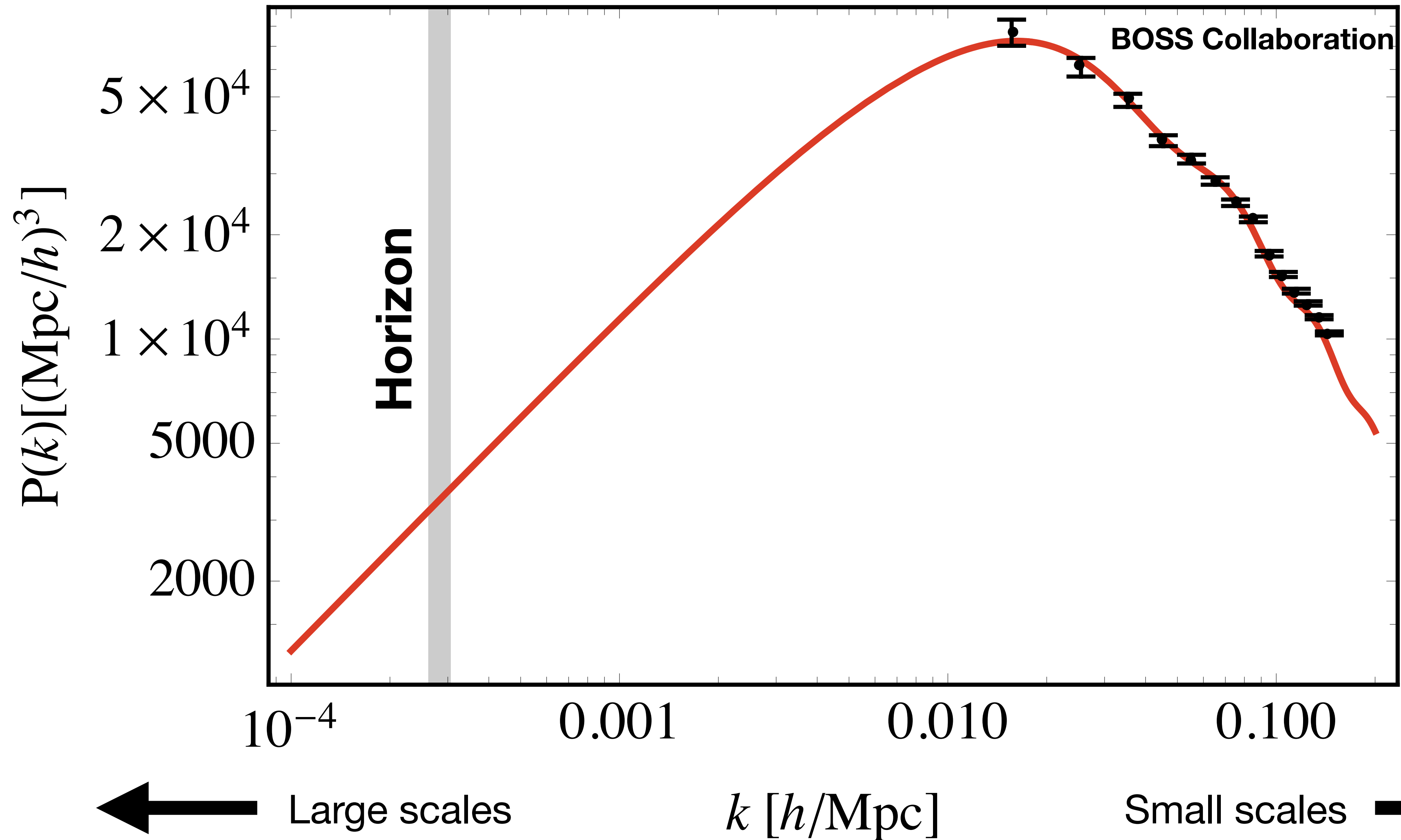


My research interests

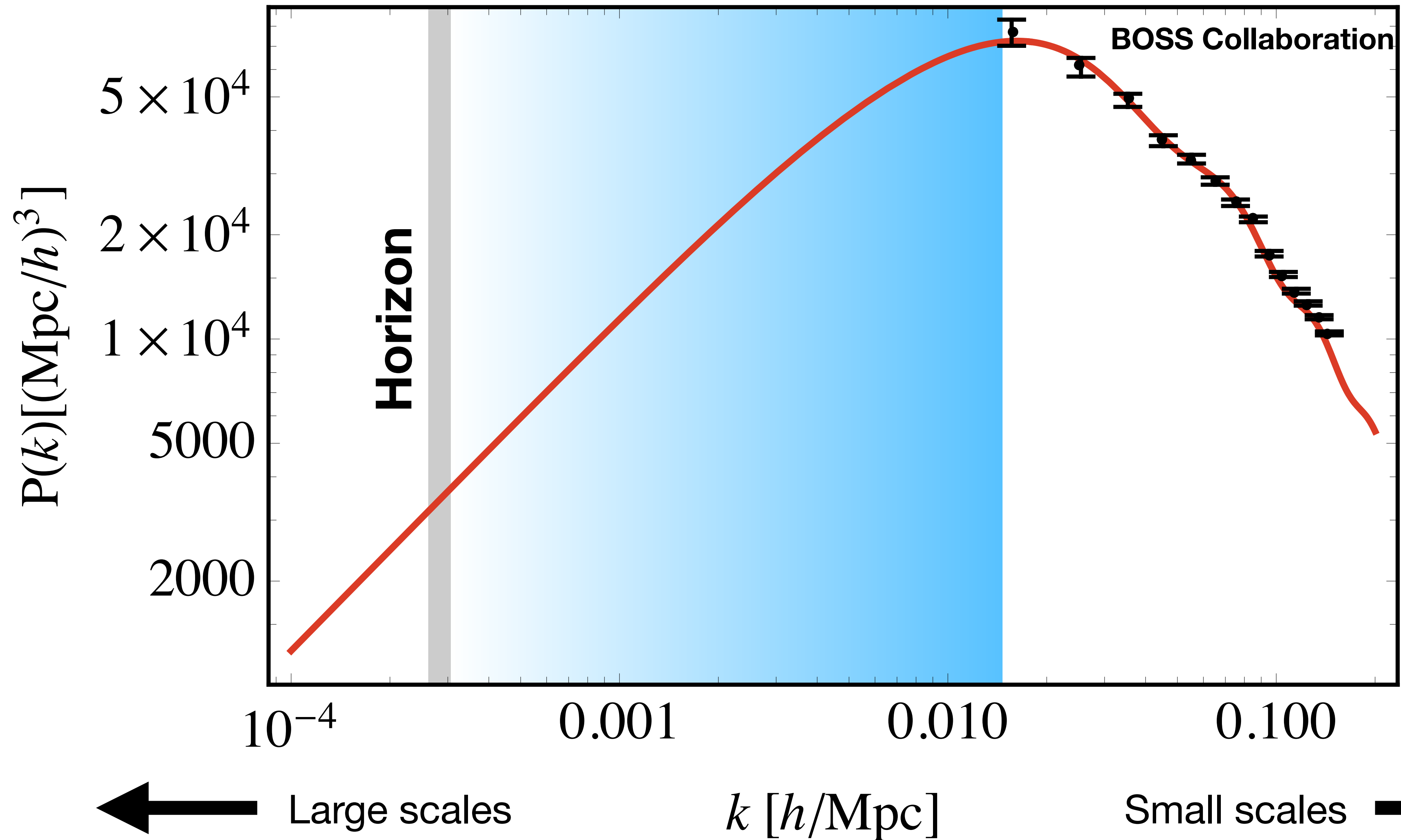


Large Scale Structures

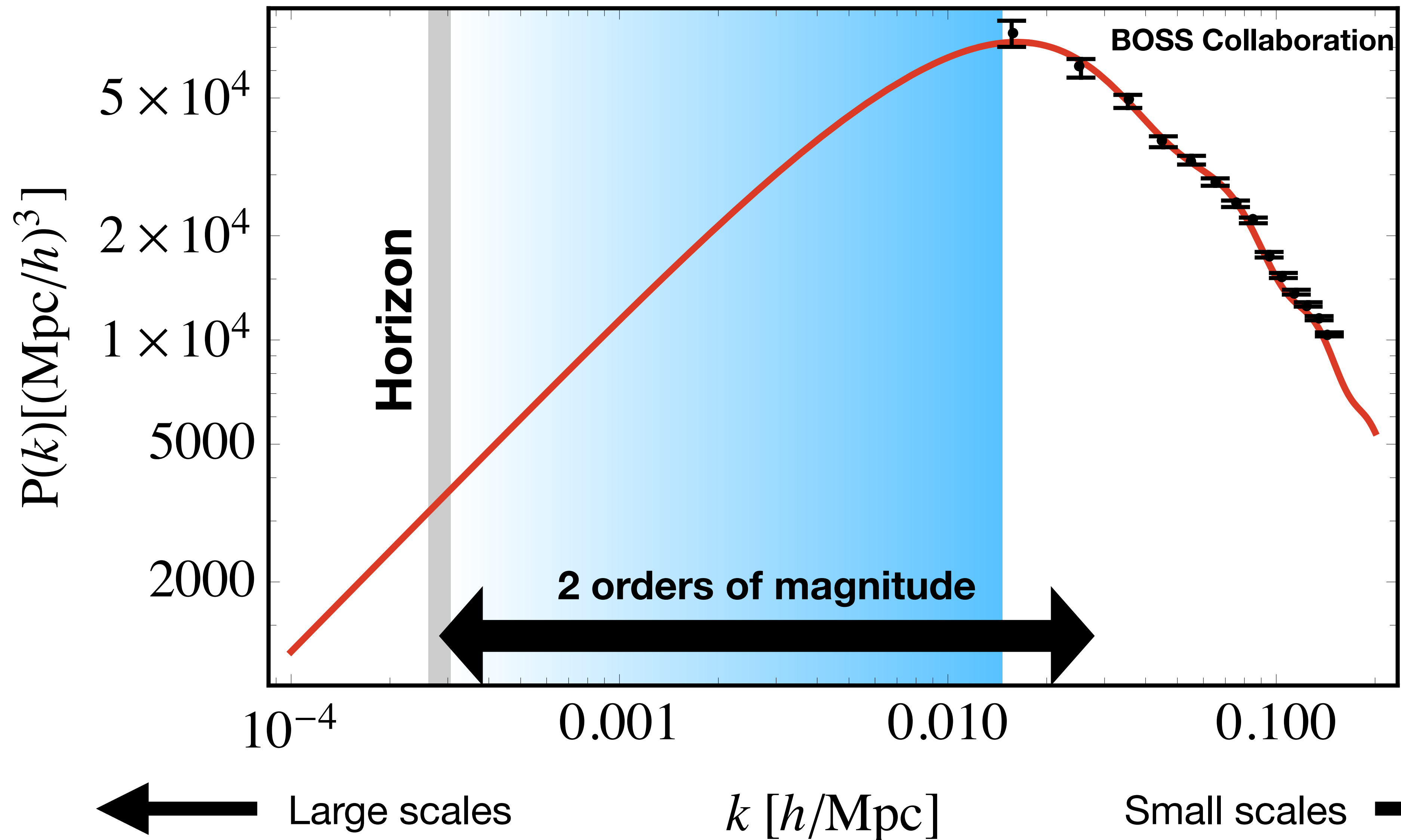
Upcoming Galaxy Surveys



Upcoming Galaxy Surveys



Upcoming Galaxy Surveys



Galaxy Surveys

Observation

Theory

$$\Delta(\mathbf{n}, z) = \frac{N(\mathbf{n}, z) - \langle N \rangle(z)}{\langle N \rangle(z)}$$

Galaxy Surveys

Observation

Theory

$$\Delta(\mathbf{n}, z) = \frac{N(\mathbf{n}, z) - \langle N \rangle(z)}{\langle N \rangle(z)} = b_1 \delta_M$$

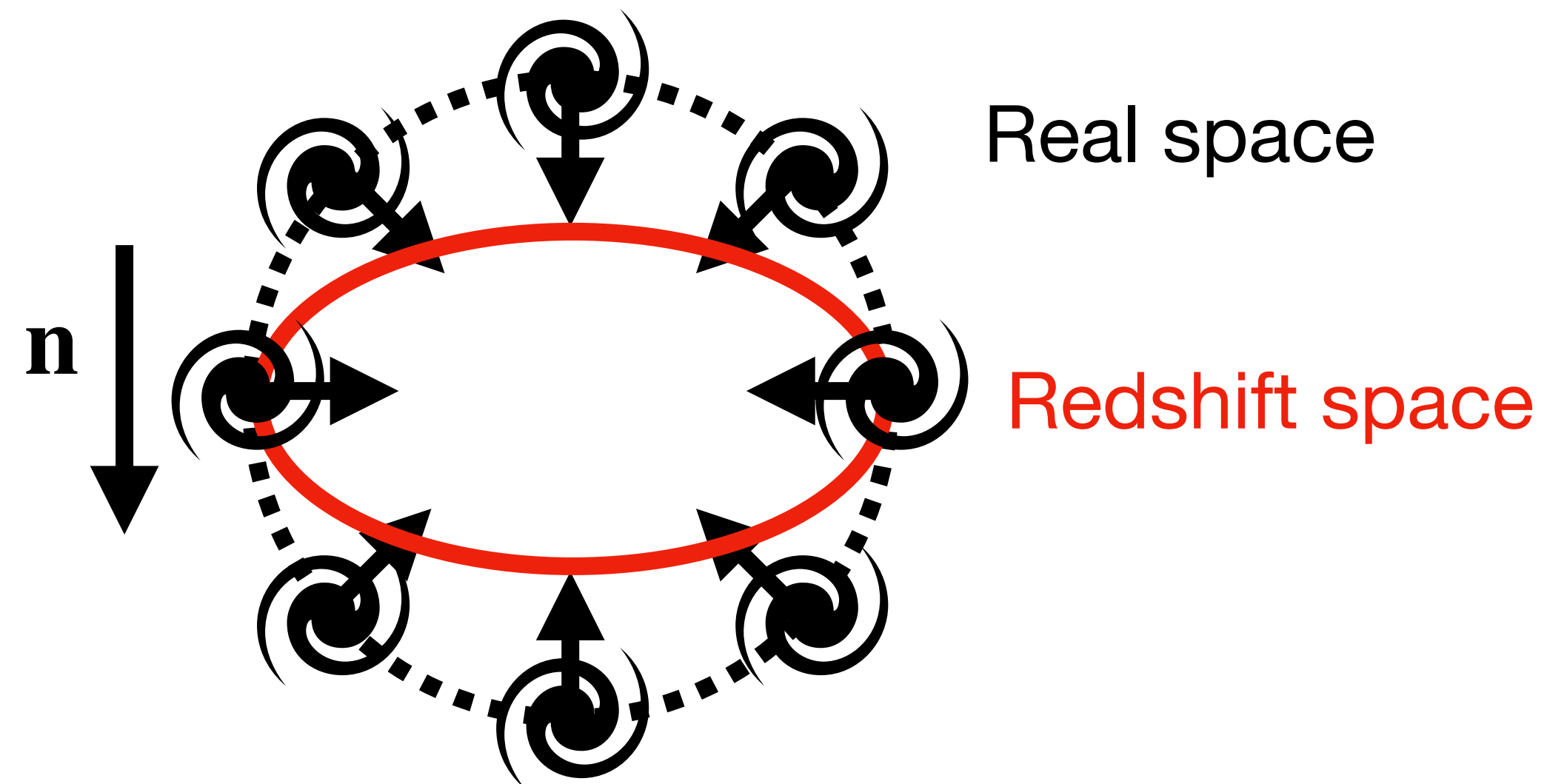
Galaxy Surveys

Observation

Theory

$$\Delta(\mathbf{n}, z) = \frac{N(\mathbf{n}, z) - \langle N \rangle(z)}{\langle N \rangle(z)} = b_1 \delta_M + \mathcal{H}^{-1} \partial_r \mathbf{v}_{\parallel}$$

Redshift perturbation $z = \bar{z} + \delta z \simeq \bar{z} - (1 + \bar{z}) \mathbf{n} \cdot \mathbf{v}$



Galaxy Surveys

Observation

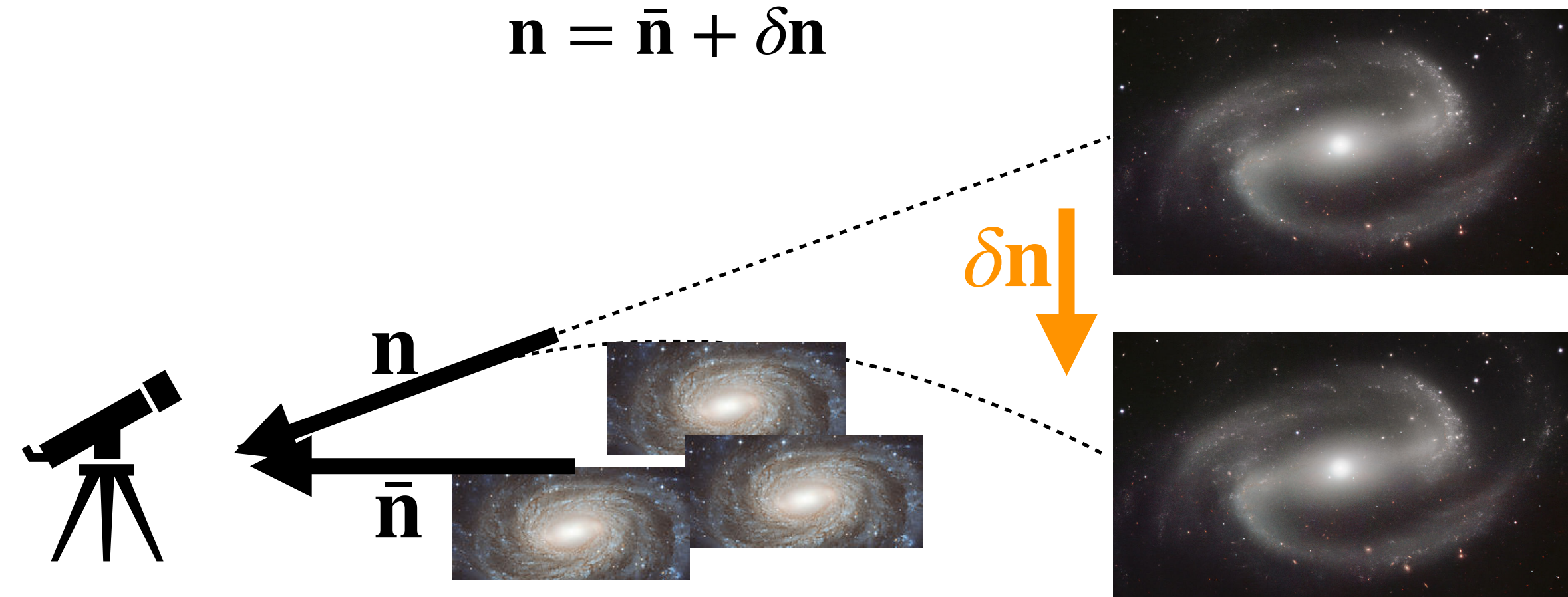
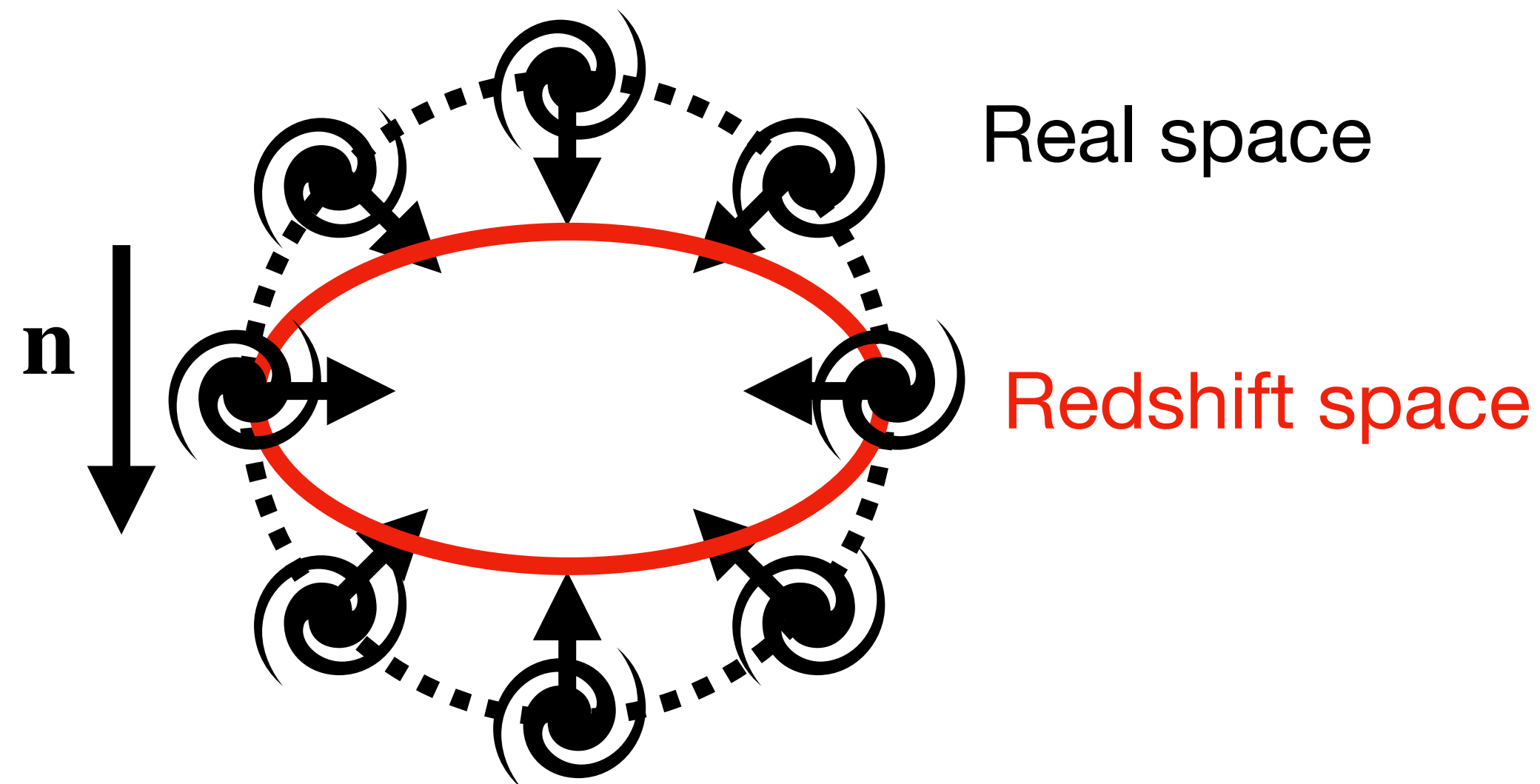
$$\Delta(\mathbf{n}, z) = \frac{N(\mathbf{n}, z) - \langle N \rangle(z)}{\langle N \rangle(z)} = b_1 \delta_M + \mathcal{H}^{-1} \partial_r \mathbf{v}_{\parallel} - 2\kappa$$

Theory

Redshift perturbation $z = \bar{z} + \delta z \simeq \bar{z} - (1 + \bar{z}) \mathbf{n} \cdot \mathbf{v}$

Deflection angle

$$\mathbf{n} = \bar{\mathbf{n}} + \delta \mathbf{n}$$



Galaxy Surveys

Observation

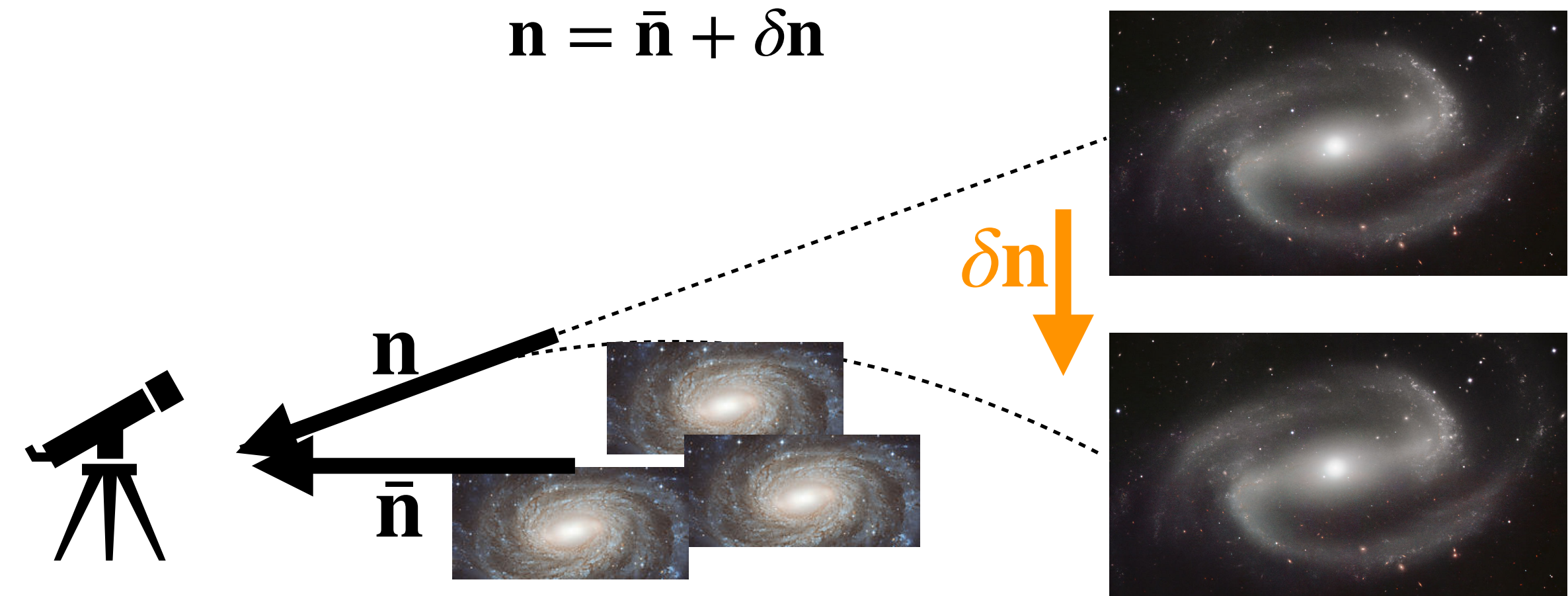
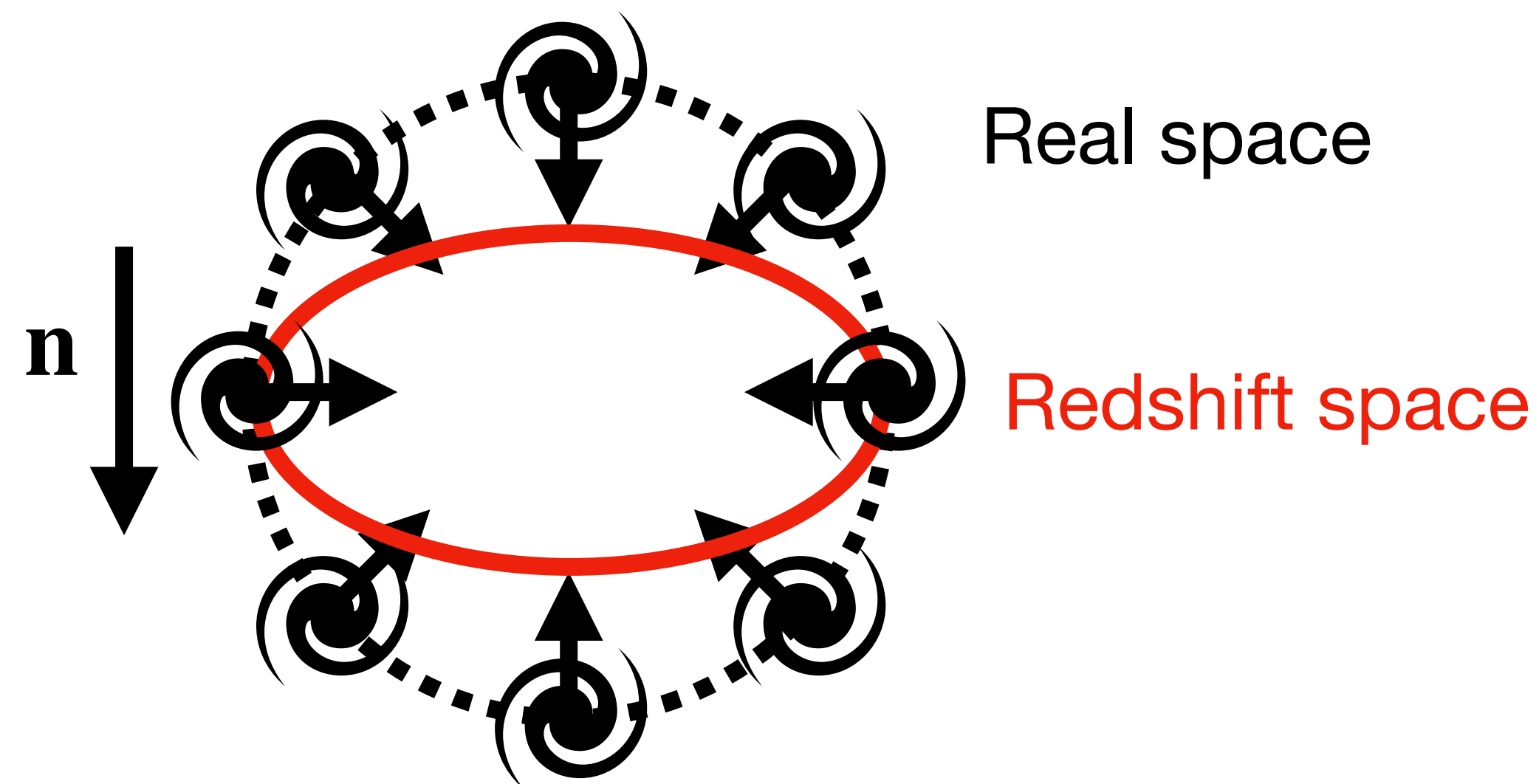
$$\Delta(\mathbf{n}, z) = \frac{N(\mathbf{n}, z) - \langle N \rangle(z)}{\langle N \rangle(z)} = b_1 \delta_M + \mathcal{H}^{-1} \partial_r \mathbf{v}_{\parallel} - 2\kappa + \mathcal{O}(\mathbf{v}_{\parallel}) + \mathcal{O}(\Phi)$$

Theory

Redshift perturbation $z = \bar{z} + \delta z \simeq \bar{z} - (1 + \bar{z}) \mathbf{n} \cdot \mathbf{v}$

Deflection angle

$$\mathbf{n} = \bar{\mathbf{n}} + \delta \mathbf{n}$$



Galaxy Surveys

Observation

Theory

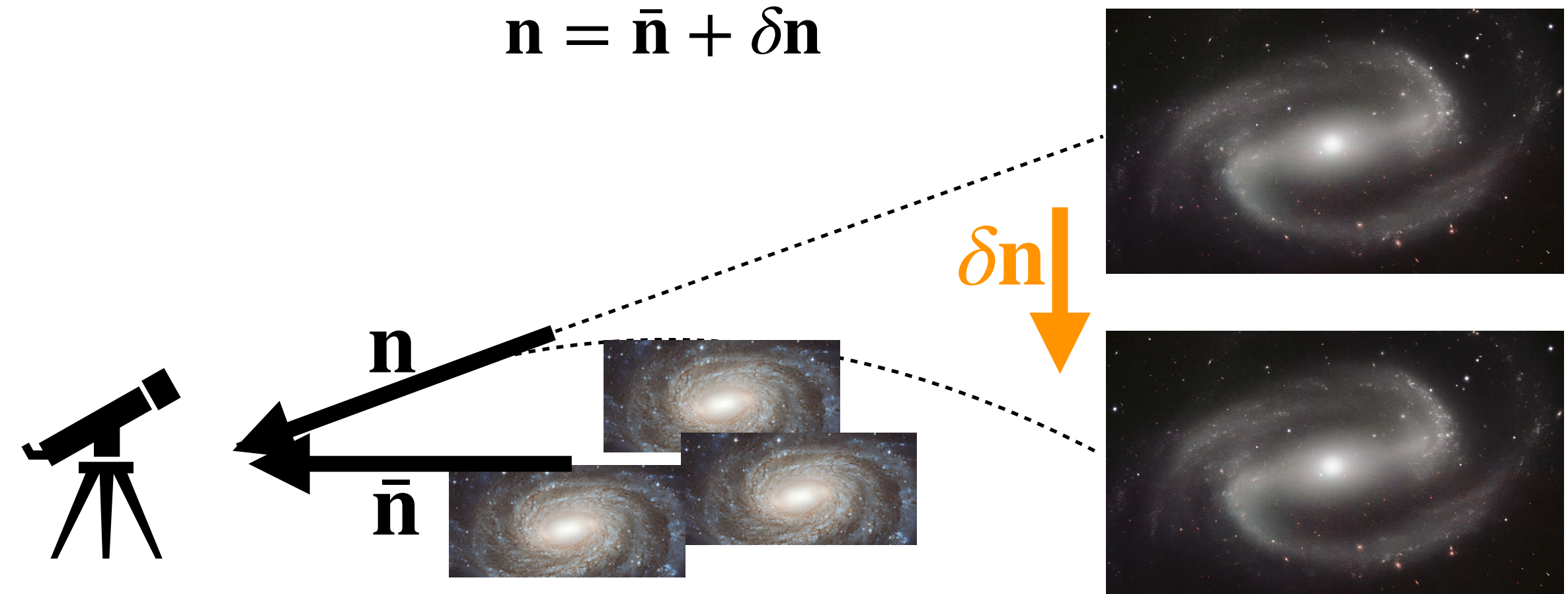
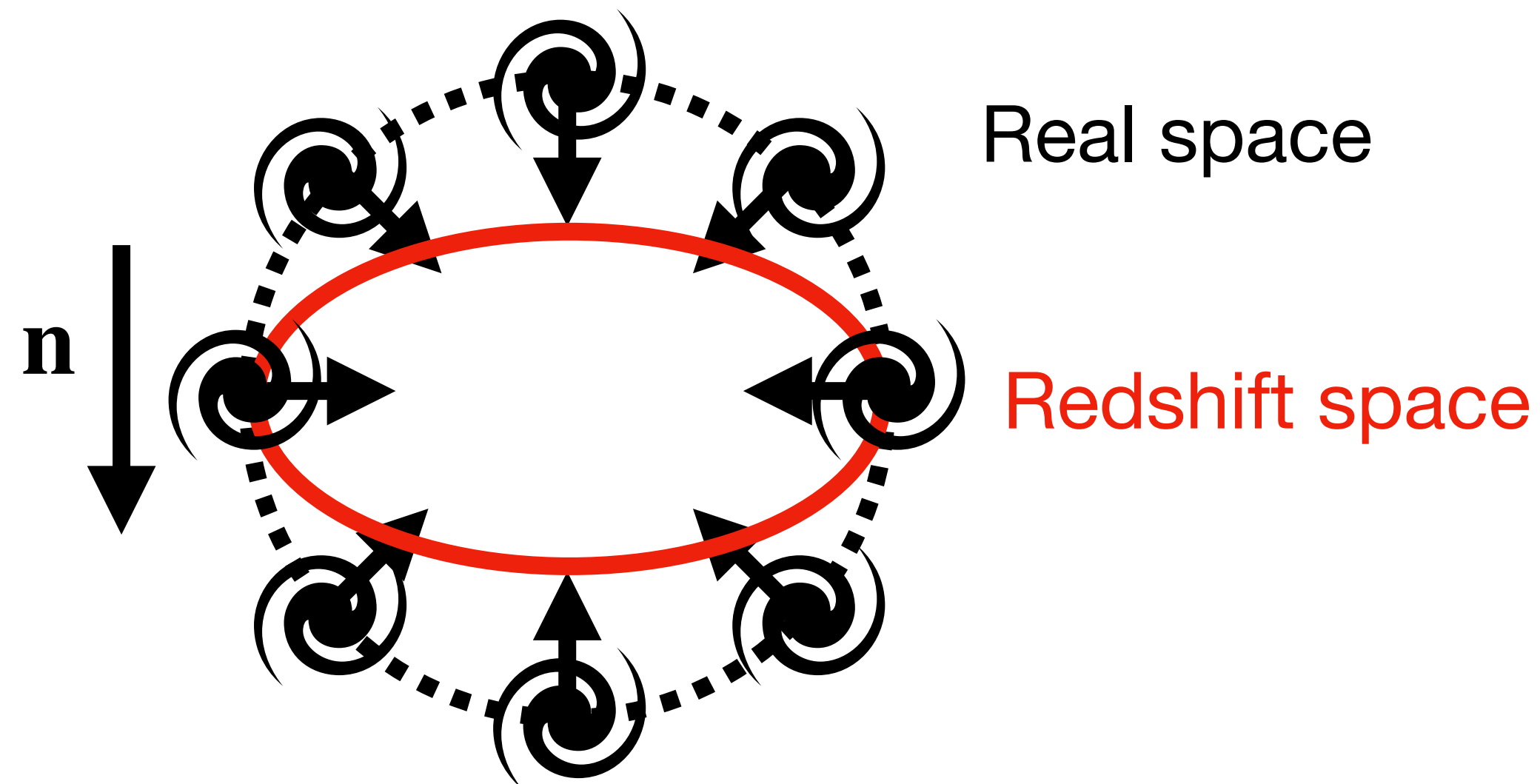
$$\Delta(\mathbf{n}, z) = \frac{N(\mathbf{n}, z) - \langle N \rangle(z)}{\langle N \rangle(z)} = \boxed{b_1 \delta_M + \mathcal{H}^{-1} \partial_r \mathbf{v}_{\parallel}} - 2\kappa + \mathcal{O}(\mathbf{v}_{\parallel}) + \mathcal{O}(\Phi)$$

Newtonian

Redshift perturbation $z = \bar{z} + \delta z \simeq \bar{z} - (1 + \bar{z}) \mathbf{n} \cdot \mathbf{v}$

Deflection angle

$$\mathbf{n} = \bar{\mathbf{n}} + \delta \mathbf{n}$$



Galaxy Surveys

Observation

$$\Delta(\mathbf{n}, z) = \frac{N(\mathbf{n}, z) - \langle N \rangle(z)}{\langle N \rangle(z)}$$

$$b_1 \delta_M + \mathcal{H}^{-1} \partial_r \mathbf{v}_{\parallel}$$

Newtonian

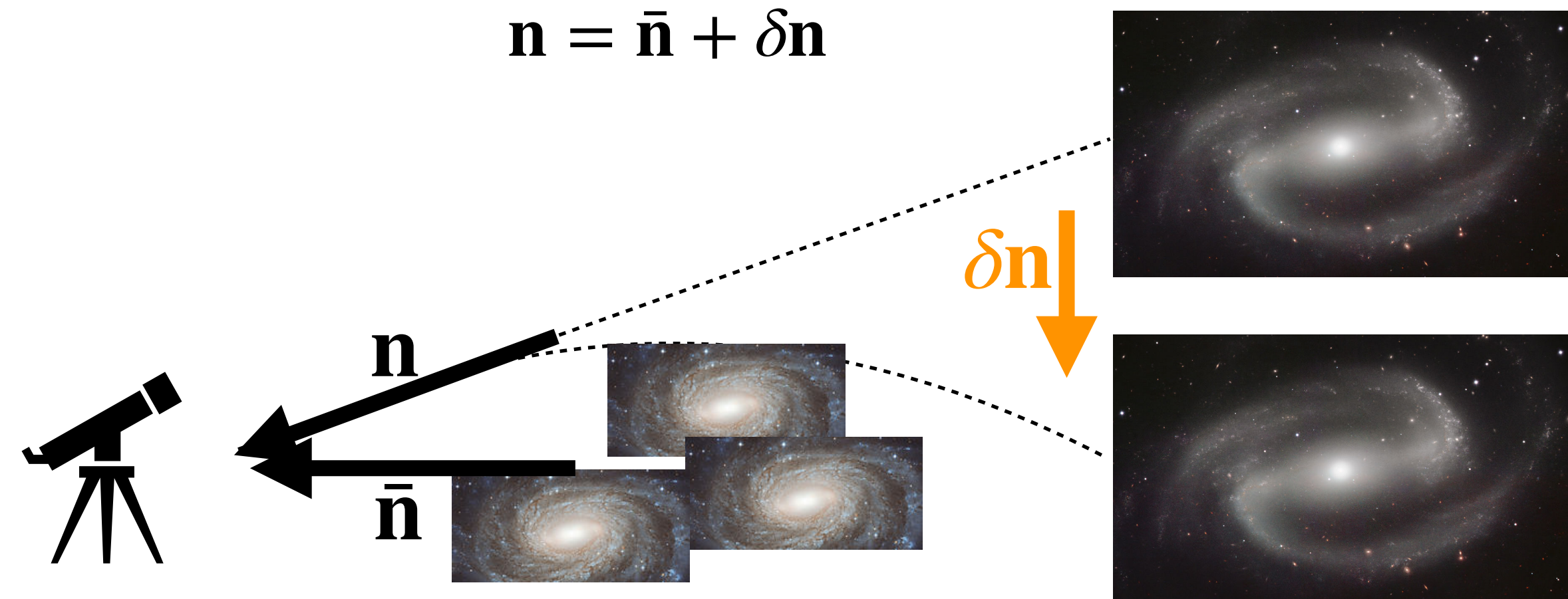
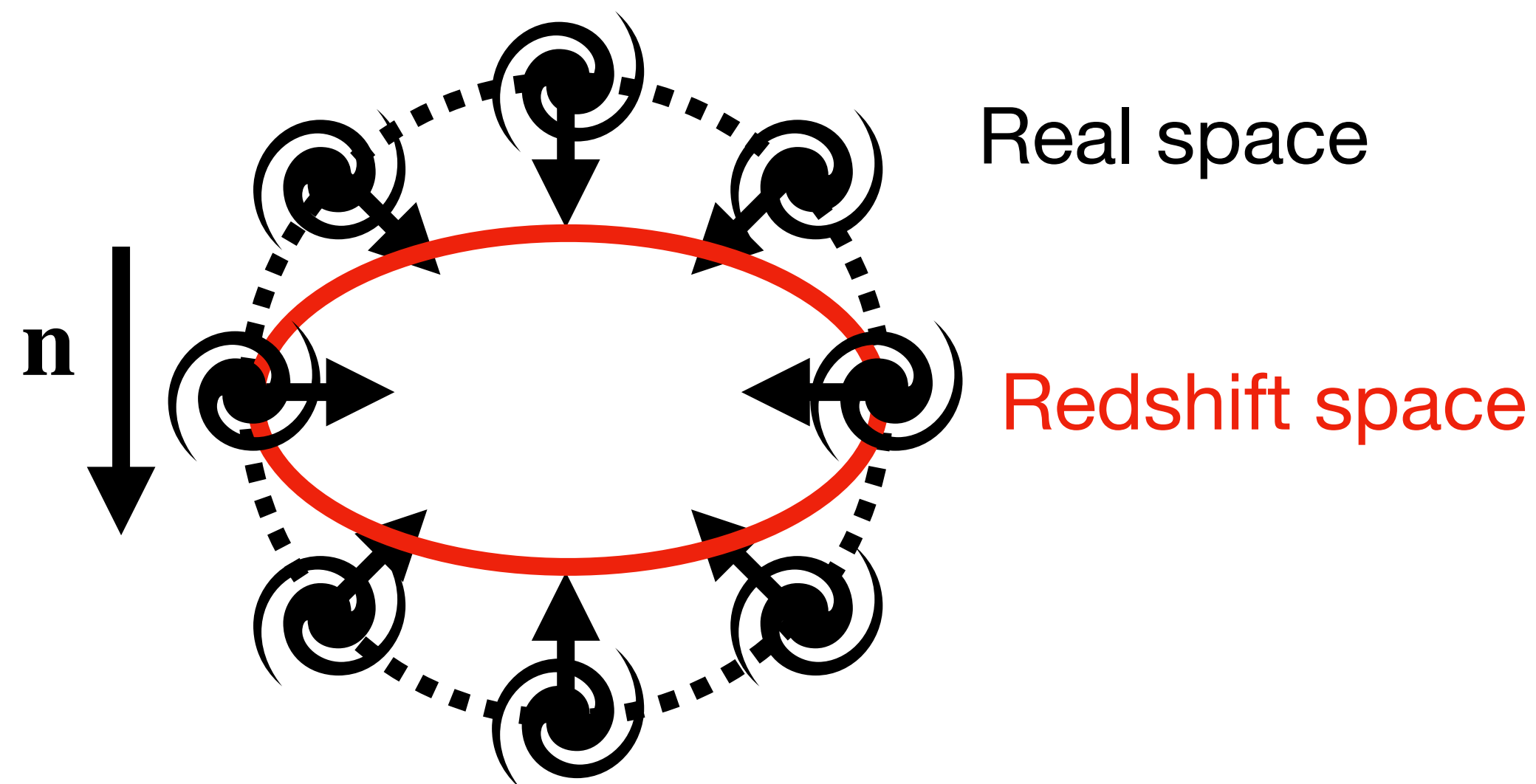
$$-2\kappa + \mathcal{O}(\mathbf{v}_{\parallel}) + \mathcal{O}(\Phi)$$

Relativistic

Redshift perturbation $z = \bar{z} + \delta z \simeq \bar{z} - (1 + \bar{z}) \mathbf{n} \cdot \mathbf{v}$

Deflection angle

$$\mathbf{n} = \bar{\mathbf{n}} + \delta \mathbf{n}$$



Galaxy Surveys

$$\begin{aligned}
 \Delta(\mathbf{n}, z) = & bD_m + \mathcal{H}^{-1} \partial_r v_{\parallel} \\
 & + \frac{5s_b - 2}{2} \int_0^r dr' \frac{r - r'}{rr'} \Delta_{\Omega} (\Psi + \Phi) \\
 & + \mathcal{R} (v_{\parallel} - v_{\parallel o}) - (2 - 5s_b) v_{\parallel o} \\
 & + \left\{ \left(\mathcal{R} - \frac{2 - 5s_b}{\mathcal{H}_0 r} \right) \mathcal{H}_0 V_o + (\mathcal{R} + 1) \Psi - \mathcal{R} \Psi_o + (5s_b - 2) \Phi + \dot{\Phi} \mathcal{H}^{-1} \right. \\
 & \quad \left. + (f_{\text{evo}} - 3) \mathcal{H} V \right\} \\
 & + \frac{2 - 5s_b}{r} \int_t^{t_o} (\Psi + \Phi) dt' + \mathcal{R} \int_t^{t_o} (\dot{\Psi} + \dot{\Phi}) dt'.
 \end{aligned}$$

Galaxy Surveys

$$\begin{aligned}
 \Delta(\mathbf{n}, z) = & \underbrace{bD_m + \mathcal{H}^{-1}\partial_r v_{\parallel}}_{\text{Newtonian}} \\
 & + \frac{5s_b - 2}{2} \int_0^r dr' \frac{r - r'}{rr'} \Delta_{\Omega} (\Psi + \Phi) \\
 & + \mathcal{R} (v_{\parallel} - v_{\parallel o}) - (2 - 5s_b) v_{\parallel o} \\
 & + \left\{ \left(\mathcal{R} - \frac{2 - 5s_b}{\mathcal{H}_0 r} \right) \mathcal{H}_0 V_o + (\mathcal{R} + 1) \Psi - \mathcal{R} \Psi_o + (5s_b - 2) \Phi + \dot{\Phi} \mathcal{H}^{-1} \right. \\
 & \quad \left. + (f_{\text{evo}} - 3) \mathcal{H} V \right\} \\
 & + \frac{2 - 5s_b}{r} \int_t^{t_o} (\Psi + \Phi) dt' + \mathcal{R} \int_t^{t_o} (\dot{\Psi} + \dot{\Phi}) dt'.
 \end{aligned}$$

Galaxy Surveys

$$\Delta(\mathbf{n}, z) = bD_m + \mathcal{H}^{-1} \partial_r v_{\parallel} \quad \text{Newtonian}$$

Relativistic

$$\begin{aligned}
 & + \frac{5s_b - 2}{2} \int_0^r dr' \frac{r - r'}{rr'} \Delta_{\Omega} (\Psi + \Phi) \\
 & + \mathcal{R} (v_{\parallel} - v_{\parallel o}) - (2 - 5s_b) v_{\parallel o} \\
 & + \left\{ \left(\mathcal{R} - \frac{2 - 5s_b}{\mathcal{H}_0 r} \right) \mathcal{H}_0 V_o + (\mathcal{R} + 1) \Psi - \mathcal{R} \Psi_o + (5s_b - 2) \Phi + \dot{\Phi} \mathcal{H}^{-1} \right. \\
 & \quad \left. + (f_{\text{evo}} - 3) \mathcal{H} V \right\} \\
 & + \frac{2 - 5s_b}{r} \int_t^{t_o} (\Psi + \Phi) dt' + \mathcal{R} \int_t^{t_o} (\dot{\Psi} + \dot{\Phi}) dt'.
 \end{aligned}$$

Galaxy Surveys

$$\Delta(\mathbf{n}, z) = bD_m + \mathcal{H}^{-1} \partial_r v_{||}$$

Lensing

$$+ \frac{5s_b - 2}{2} \int_0^r dr' \frac{r - r'}{rr'} \Delta_{\Omega} (\Psi + \Phi)$$

$$+ \mathcal{R} (v_{||} - v_{||o}) - (2 - 5s_b) v_{||o}$$

$$+ \left\{ \left(\mathcal{R} - \frac{2 - 5s_b}{\mathcal{H}_0 r} \right) \mathcal{H}_0 V_o + (\mathcal{R} + 1) \Psi - \mathcal{R} \Psi_o + (5s_b - 2) \Phi + \dot{\Phi} \mathcal{H}^{-1} \right.$$

$$\left. + (f_{\text{evo}} - 3) \mathcal{H} V \right\}$$

$$+ \frac{2 - 5s_b}{r} \int_t^{t_o} (\Psi + \Phi) dt' + \mathcal{R} \int_t^{t_o} (\dot{\Psi} + \dot{\Phi}) dt' .$$

Galaxy Surveys

$$\begin{aligned}
 \Delta(\mathbf{n}, z) = & bD_m + \mathcal{H}^{-1} \partial_r v_{\parallel} \\
 & + \frac{5s_b - 2}{2} \int_0^r dr' \frac{r - r'}{rr'} \Delta_{\Omega} (\Psi + \Phi) \\
 \text{Velocity } & + \mathcal{R} (v_{\parallel} - v_{\parallel o}) - (2 - 5s_b) v_{\parallel o} \\
 & + \left\{ \left(\mathcal{R} - \frac{2 - 5s_b}{\mathcal{H}_0 r} \right) \mathcal{H}_0 V_o + (\mathcal{R} + 1) \Psi - \mathcal{R} \Psi_o + (5s_b - 2) \Phi + \dot{\Phi} \mathcal{H}^{-1} \right. \\
 & \quad \left. + (f_{\text{evo}} - 3) \mathcal{H} V \right\} \\
 & + \frac{2 - 5s_b}{r} \int_t^{t_o} (\Psi + \Phi) dt' + \mathcal{R} \int_t^{t_o} (\dot{\Psi} + \dot{\Phi}) dt'.
 \end{aligned}$$

Galaxy Surveys

$$\Delta(\mathbf{n}, z) = bD_m + \mathcal{H}^{-1} \partial_r v_{||} \\ + \frac{5s_b - 2}{2} \int_0^r dr' \frac{r - r'}{rr'} \Delta_{\Omega} (\Psi + \Phi) \\ + \mathcal{R} (v_{||} - v_{||o}) - (2 - 5s_b) v_{||o}$$

$$+ \left\{ \left(\mathcal{R} - \frac{2 - 5s_b}{\mathcal{H}_0 r} \right) \mathcal{H}_0 V_o + (\mathcal{R} + 1) \Psi - \mathcal{R} \Psi_o + (5s_b - 2) \Phi + \dot{\Phi} \mathcal{H}^{-1} \right. \\ \left. + (f_{\text{evo}} - 3) \mathcal{H} V \right\} \\ + \frac{2 - 5s_b}{r} \int_t^{t_o} (\Psi + \Phi) dt' + \mathcal{R} \int_t^{t_o} (\dot{\Psi} + \dot{\Phi}) dt' .$$

Gravitational
potential

Galaxy Surveys

Observation

Theory

$$\Delta(\mathbf{n}, z) = \frac{N(\mathbf{n}, z) - \langle N \rangle(z)}{\langle N \rangle(z)} = b_1 \delta_M + \mathcal{H}^{-1} \partial_r \mathbf{v}_{\parallel} - 2\kappa + \mathcal{O}(\mathbf{v}_{\parallel}) + \mathcal{O}(\Phi)$$

Lensing

$$\int_0^r dr' \frac{r-r'}{rr'} \Delta_{\Omega} \Phi \sim \int_0^r dr' \frac{r-r'}{r} r' H_0^2 \delta_{M,0} \sim (rH_0)^2 \delta_M$$

deep galaxy surveys

Velocity

$$v_{\parallel} \sim \mu \frac{H}{k} \delta_M$$

non-zero dipole

Gravitational Potential

$$\Phi \sim \left(\frac{H}{k} \right)^2 \delta_M$$

search of primordial
non-gaussianity

The IR behaviour

$$\begin{aligned}
 \Delta(\mathbf{n}, z) = & bD_m + \mathcal{H}^{-1} \partial_r v_{||} \\
 & + \frac{5s_b - 2}{2} \int_0^r dr' \frac{r - r'}{rr'} \Delta_{\Omega} (\Psi + \Phi) \\
 & + \mathcal{R} (v_{||} - v_{||_o}) - (2 - 5s_b) v_{||_o} \\
 & + \left\{ \left(\mathcal{R} - \frac{2 - 5s_b}{\mathcal{H}_0 r} \right) \mathcal{H}_0 V_o + (\mathcal{R} + 1) \Psi - \mathcal{R} \Psi_o + (5s_b - 2) \Phi + \dot{\Phi} \mathcal{H}^{-1} \right. \\
 & \quad \left. + (f_{\text{evo}} - 3) \mathcal{H} V \right\} \\
 & + \frac{2 - 5s_b}{r} \int_t^{t_o} (\Psi + \Phi) dt' + \mathcal{R} \int_t^{t_o} (\dot{\Psi} + \dot{\Phi}) dt' .
 \end{aligned}$$

Gravitational
potential

$$\xi \supset \langle \Phi \Phi \rangle \sim \int \frac{dq}{2\pi^2} q^2 P(q) \frac{j_0(qs)}{(qs)^4}$$

IR divergence

The IR behaviour

$$\begin{aligned} \Delta(\mathbf{n}, z) = & bD_m + \mathcal{H}^{-1} \partial_r v_{||} \\ & + \frac{5s_b - 2}{2} \int_0^r dr' \frac{r - r'}{rr'} \Delta_\Omega (\Psi + \Phi) \\ & + \mathcal{R} (v_{||} - v_{||_o}) - (2 - 5s_b) v_{||_o} \\ & + \left\{ \left(\mathcal{R} - \frac{2 - 5s_b}{\mathcal{H}_0 r} \right) \mathcal{H}_0 V_o + (\mathcal{R} + 1) \Psi - \mathcal{R} \Psi_o + (5s_b - 2) \Phi + \dot{\Phi} \mathcal{H}^{-1} \right. \\ & \quad \left. + (f_{\text{evo}} - 3) \mathcal{H} V \right\} \\ & + \frac{2 - 5s_b}{r} \int_t^{t_o} (\Psi + \Phi) dt' + \mathcal{R} \int_t^{t_o} (\dot{\Psi} + \dot{\Phi}) dt'. \end{aligned}$$

Gravitational potential

$$\xi \supset \langle \Phi \Phi \rangle \sim \int \frac{dq}{2\pi^2} q^2 P(q) \overset{\text{IR safe}}{\frac{j_0(qs) - 1}{(qs)^4}} + \int \frac{dq}{2\pi^2} q^2 P(q) \overset{\text{IR divergence}}{\frac{1}{(qs)^4}} = \left[\int \frac{dq}{2\pi^2} q^2 P(q) \frac{j_0(qs) - 1}{(qs)^4} \right] + \sigma_\Phi^2$$

By including all the terms we can show that

$$\sum_{\mathcal{O}\mathcal{O}'} (\sigma^2)_{\mathcal{O}\mathcal{O}'}^{\text{div}} = 0$$

Grimm, Scaccabarozzi, Yoo, Biern
Castorina & ED

The theoretical predictions are independent from the gravitational potential in the IR limit

Galaxy Surveys

Observation

Theory

$$\Delta(\mathbf{n}, z) = \frac{N(\mathbf{n}, z) - \langle N \rangle(z)}{\langle N \rangle(z)} = b_1 \delta_M + \mathcal{H}^{-1} \partial_r \mathbf{v}_{\parallel} - 2\kappa + \mathcal{O}(\mathbf{v}_{\parallel}) + \mathcal{O}(\Phi)$$

Lensing

$$\int_0^r dr' \frac{r-r'}{rr'} \Delta_{\Omega} \Phi \sim \int_0^r dr' \frac{r-r'}{r} r' H_0^2 \delta_{M,0} \sim (rH_0)^2 \delta_M$$

deep galaxy surveys

Velocity

$$v_{\parallel} \sim \mu \frac{H}{k} \delta_M$$

non-zero dipole

**Gravitational
Potential**

$$\Phi \sim \left(\frac{H}{k} \right)^2 \delta_M$$

**search of primordial
non-gaussianity**

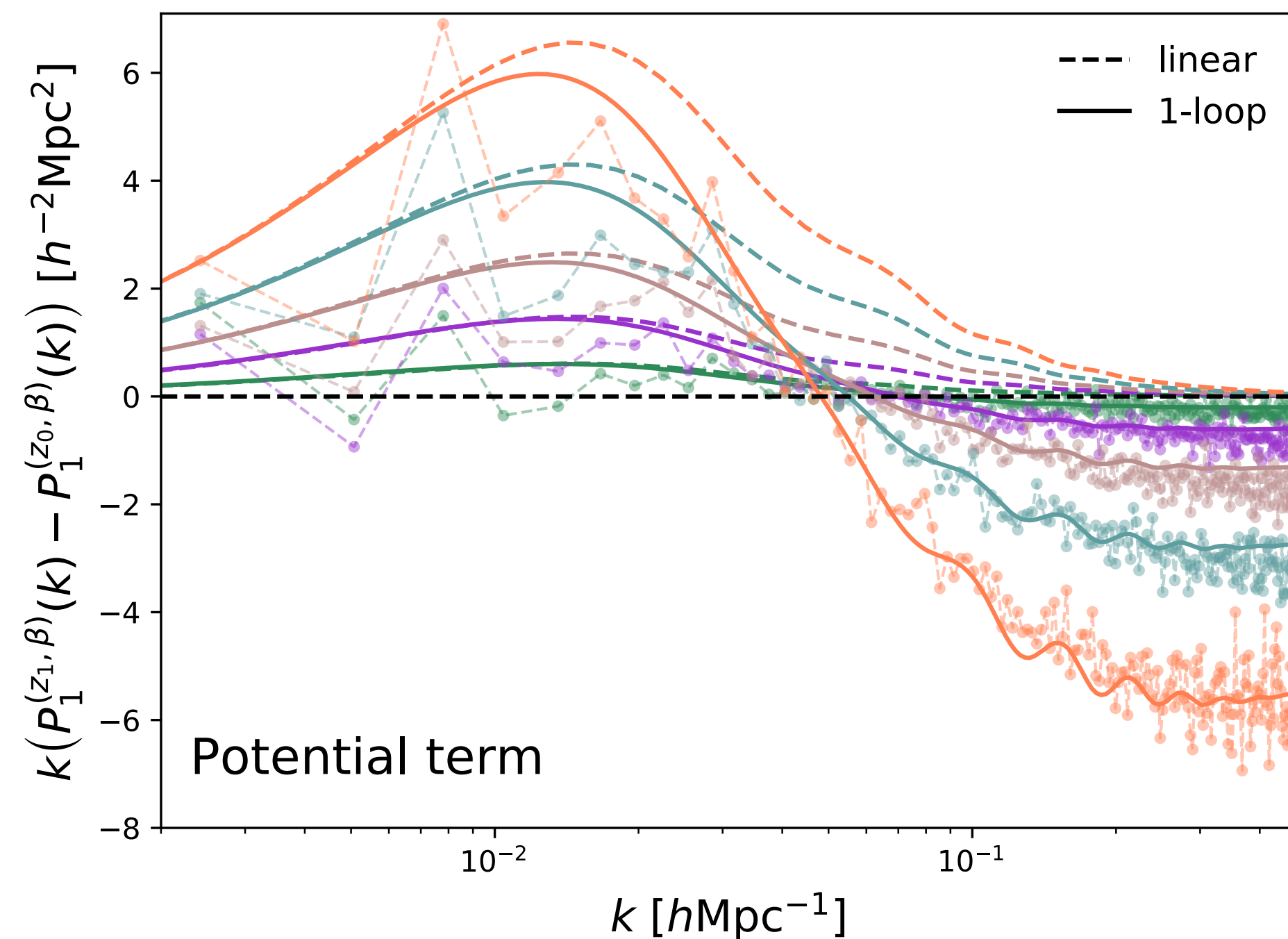
Dipole of the power spectrum

at **one loop**

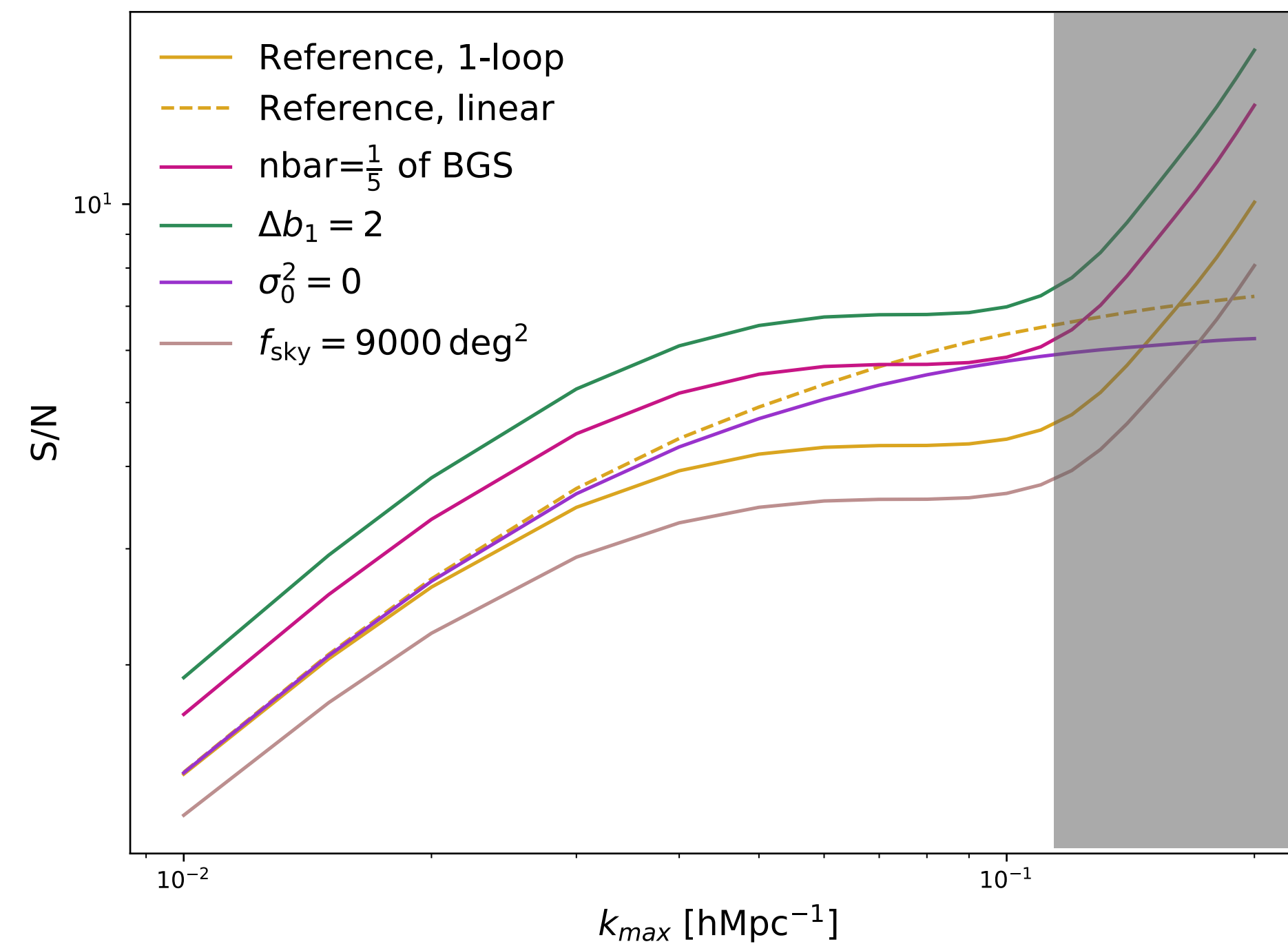
$$\longrightarrow \Delta_{\text{gal}}(\mathbf{n}, z) = \frac{N(\mathbf{n}, z) - \langle N \rangle(z)}{\langle N \rangle(z)}$$

At 3rd order in perturbation theory
ED & Seljak, ED & Beutler

Comparison with relativistic N-body sims



DESI Forecast



Galaxy Surveys

Observation

Theory

$$\Delta(\mathbf{n}, z) = \frac{N(\mathbf{n}, z) - \langle N \rangle(z)}{\langle N \rangle(z)} = b_1 \delta_M + \mathcal{H}^{-1} \partial_r \mathbf{v}_{\parallel} - 2\kappa + \mathcal{O}(\mathbf{v}_{\parallel}) + \mathcal{O}(\Phi)$$

Lensing

$$\int_0^r dr' \frac{r-r'}{rr'} \Delta_{\Omega} \Phi \sim \int_0^r dr' \frac{r-r'}{r} r' H_0^2 \delta_{M,0} \sim (rH_0)^2 \delta_M$$

deep galaxy surveys

Velocity

$$v_{\parallel} \sim \mu \frac{H}{k} \delta_M$$

non-zero dipole

**Gravitational
Potential**

$$\Phi \sim \left(\frac{H}{k} \right)^2 \delta_M$$

**search of primordial
non-gaussianity**

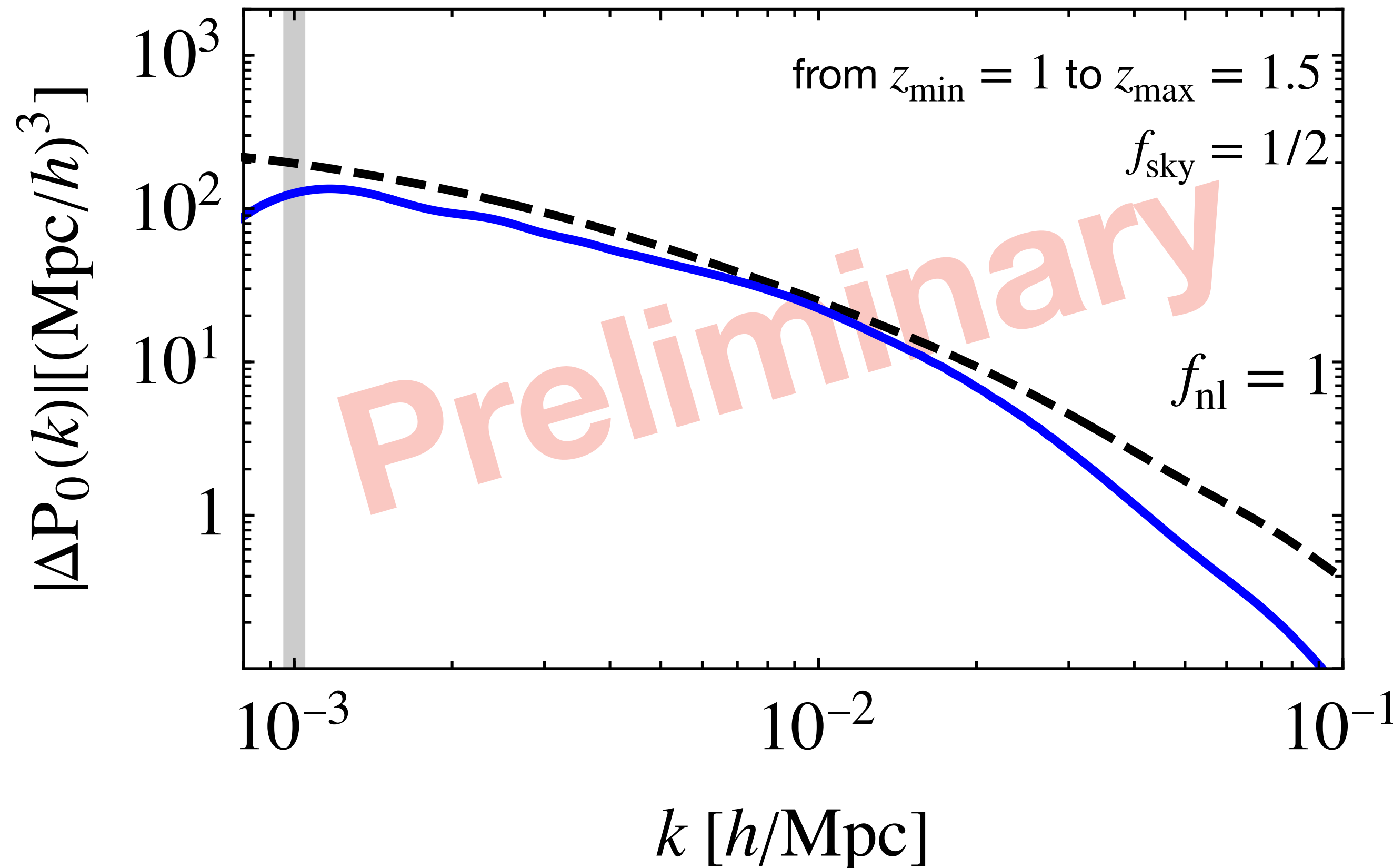
(Galaxy Power Spectrum Estimator)

soon publicly available

Fast and accurate numerical code to compute $\langle \hat{P}_L(k) \rangle$ for galaxy number counts and luminosity distance including:

- ✓ all relativistic effects
- ✓ window function
- ✓ wide-angle effects
- ✓ primordial local non-gaussianity (scale-dependent bias)

all these effects are relevant at the largest scales



Data analysis

- in full-sky
- with magnification
- without relativistic effects

Galaxy Surveys

Observation

Theory

$$\Delta(\mathbf{n}, z) = \frac{N(\mathbf{n}, z) - \langle N \rangle(z)}{\langle N \rangle(z)} = b_1 \delta_M + \mathcal{H}^{-1} \partial_r \mathbf{v}_{\parallel} - 2\kappa + \mathcal{O}(\mathbf{v}_{\parallel}) + \mathcal{O}(\Phi)$$

Lensing

$$\int_0^r dr' \frac{r-r'}{rr'} \Delta_{\Omega} \Phi \sim \int_0^r dr' \frac{r-r'}{r} r' H_0^2 \delta_{M,0} \sim (rH_0)^2 \delta_M$$

deep galaxy surveys

Velocity

$$v_{\parallel} \sim \mu \frac{H}{k} \delta_M$$

non-zero dipole

Gravitational Potential

$$\Phi \sim \left(\frac{H}{k} \right)^2 \delta_M$$

search of primordial
non-gaussianity

Galaxy Surveys

Observation

$$\Delta(\mathbf{n}, z) = \frac{N(\mathbf{n}, z) - \langle N \rangle(z)}{\langle N \rangle(z)} = b_1 \delta_M + \mathcal{H}^{-1} \partial_r \mathbf{v}_{\parallel} - 2\kappa + \mathcal{O}(\mathbf{v}_{\parallel}) + \mathcal{O}(\Phi)$$

Theory

Lensing

$$\int_0^r dr' \frac{r-r'}{rr'} \Delta_{\Omega} \Phi \sim \int_0^r dr' \frac{r-r'}{r} r' H_0^2 \delta_{M,0} \sim (rH_0)^2 \delta_M$$

deep galaxy surveys

Velocity

$$v_{\parallel} \sim \mu \frac{H}{k} \delta_M$$



non-zero dipole

Gravitational Potential

$$\Phi \sim \left(\frac{H}{k} \right)^2 \delta_M$$

search of primordial non-gaussianity

Galaxy Surveys

Observation

Theory

$$\Delta(\mathbf{n}, z) = \frac{N(\mathbf{n}, z) - \langle N \rangle(z)}{\langle N \rangle(z)} = b_1 \delta_M + \mathcal{H}^{-1} \partial_r \mathbf{v}_{\parallel} - 2\kappa + \mathcal{O}(\mathbf{v}_{\parallel}) + \mathcal{O}(\Phi)$$

Lensing

$$\int_0^r dr' \frac{r-r'}{rr'} \Delta_{\Omega} \Phi \sim \int_0^r dr' \frac{r-r'}{r} r' H_0^2 \delta_{M,0} \sim (rH_0)^2 \delta_M$$

deep galaxy surveys

Velocity

$$v_{\parallel} \sim \mu \frac{H}{k} \delta_M$$



non-zero dipole

Gravitational Potential

$$\Phi \sim \left(\frac{H}{k} \right)^2 \delta_M$$

$$f_{\text{nl}}^{\text{eff}} \sim 1$$

search of primordial non-gaussianity

Thank you