

Using $2 \rightarrow 3$ exclusive processes as a channel to probe generalised parton distributions

QCD Master Class 2023

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IJCLab



Gluodynamics

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Based on 2212.00655, 2302.12026 and work in progress with S. Wallon, L. Szymanowski, B. Pire, G. Duplančić, K. Passek-Kumerički, N. Crković

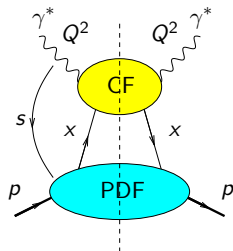
Introduction

From DIS to DVCS

- **DIS**: inclusive process (*forward amplitude*)

$x \Rightarrow$ 1-dimensional structure

Coefficient Function (hard) \otimes **Parton Distribution Function** (soft)



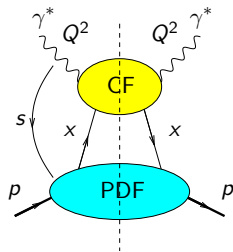
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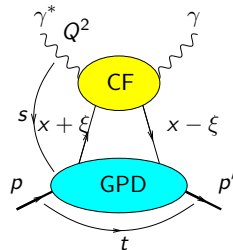
- ▶ **DVCS**: exclusive process (*non-forward amplitude*)

(DVCS: Deeply Virtual Compton Scattering)

Fourier transf.: $t \leftrightarrow$ impact parameter

$(x, t) \Rightarrow$ 3-dimensional structure

Coefficient Function (hard) \otimes Generalized Parton Distribution (soft)



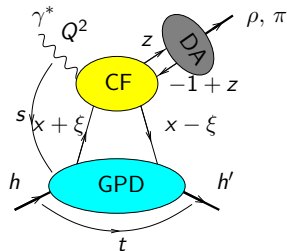
Müller et al. '91 - '94; Radyushkin '96; Ji '97

Introduction

From DVCS to meson production

- **Meson production:** γ replaced by ρ, π, \dots

GPD (soft) \otimes **CF** (hard) \otimes **Distribution Amplitude** (soft)

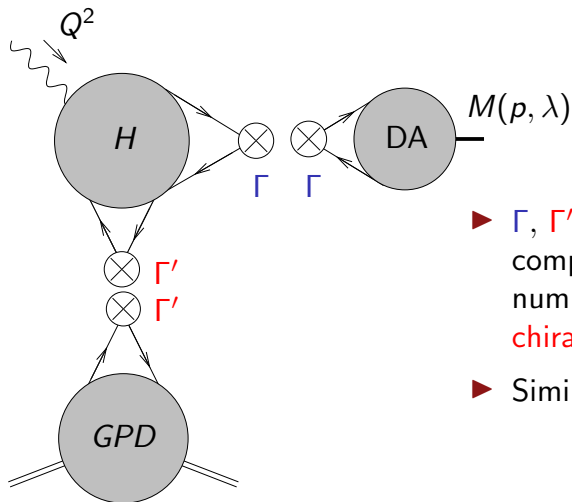


Collins, Frankfurt, Strikman '97; Radyushkin '97

proof of factorisation valid only for some restricted cases

Introduction

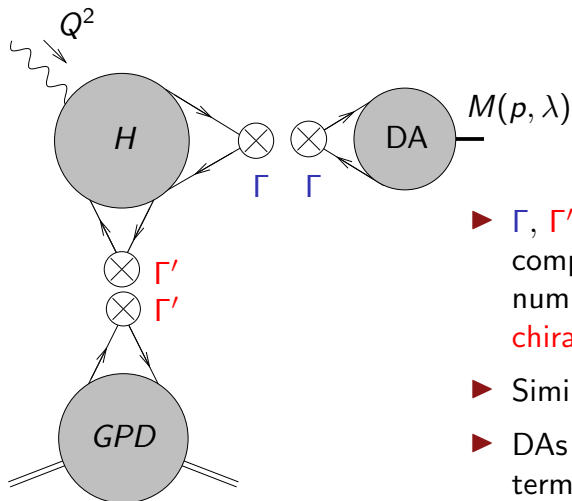
Schematic of collinear factorisation



- ▶ Γ, Γ' : Dirac matrices compatible with quantum numbers: C, P, T , chirality
- ▶ Similar structure for colour

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Schematic of collinear factorisation



- ▶ Γ, Γ' : Dirac matrices compatible with quantum numbers: C, P, T , chirality
- ▶ Similar structure for colour
- ▶ DAs and GPDs ordered in terms of twist

Introduction

Definition of Quark GPDs: twist 2 Chiral-even

Quark GPDs at twist 2 [Diehl: hep-ph/0307382]

without helicity flip (chiral-even Γ matrices): 4 chiral-even GPDs:
(Note: $\Delta = p' - p$)

$$\begin{aligned} F^q &= \frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p' | \bar{q}(-\frac{1}{2}z) \gamma^+ q(\frac{1}{2}z) | p \rangle \Big|_{z^+=0, z_\perp=0} \\ &= \frac{1}{2P^+} \left[H^q(x, \xi, t) \bar{u}(p') \gamma^+ u(p) + E^q(x, \xi, t) \bar{u}(p') \frac{i \sigma^{+\alpha} \Delta_\alpha}{2m} u(p) \right], \end{aligned}$$

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$H^q \xrightarrow{\xi=0, t=0} \text{PDF } q$

$\tilde{H}^q \xrightarrow{\xi=0, t=0} \text{polarised PDF } \Delta q$

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$H_T^q \xrightarrow{\xi=0, t=0}$ quark transversity PDFs δq

Note: $\tilde{E}_T^q(x, -\xi, t) = -\tilde{E}_T^q(x, \xi, t)$

Why consider a gamma-meson pair?

Understanding quark transversity

- ▶ Transverse spin content of the proton:

$$\begin{array}{lcl} |\uparrow\rangle_{(x)} & \sim & |\rightarrow\rangle + |\leftarrow\rangle \\ |\downarrow\rangle_{(x)} & \sim & |\rightarrow\rangle - |\leftarrow\rangle \\ \text{spin along } x & & \text{helicity states} \end{array}$$

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- ▶ Transversity GPDs can thus be accessed through **chiral-odd Γ** matrices.
- ▶ Since (in the massless limit) QCD and QED are chiral-even ($\gamma^\mu, \gamma^\mu\gamma^5$), **the chiral-odd quantities $(1, \gamma^5, [\gamma^\mu, \gamma^\nu])$ which one wants to measure should appear in pairs.**

Why consider a gamma-meson pair?

Can we probe quark transversity GPDs in DVMP?

- ▶ the leading DA (twist 2) of ρ_T is **chiral-odd** ($\sigma^{\mu\nu}$ coupling)

Why consider a gamma-meson pair?

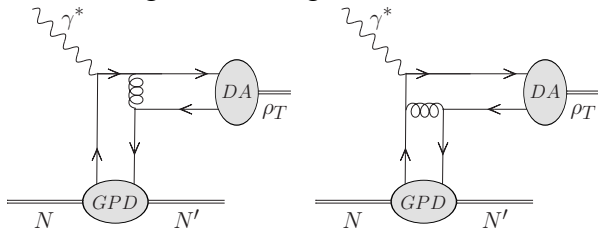
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- ▶ the leading DA (twist 2) of ρ_T is **chiral-odd** ($\sigma^{\mu\nu}$ coupling)
- ▶ unfortunately $\gamma^* N \rightarrow \rho_T N' = 0$, since such a process would require a helicity transfer of 2 from a photon. [Diehl, Gousset, Pire: hep-ph/9808479], [Collins, Diehl: hep-ph/9907498]

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- ▶ lowest order diagrammatic argument:



$$\gamma^\alpha [\gamma^\mu, \gamma^\nu] \gamma_\alpha = 0$$

Why consider a gamma-meson pair?

Go to higher twist?

- ▶ This vanishing only occurs at [twist 2](#)
- ▶ At twist 3 this process does not vanish [[Ahmad, Goldstein, Liuti: 0805.3568](#)], [[Goloskokov, Kroll: 1106.4897, 1310.1472](#)]

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- ▶ However processes involving **twist 3 DAs** may face problems with factorisation (end-point singularities)

⇒ can be made safe in the high-energy k_T -factorisation approach

[Anikin, Ivanov, Pire, Szymanowski, Wallon: 0909.4090]

Why consider a gamma-meson pair?

A convenient alternative solution

Circumvent this using 3-body final states:

▶ $\gamma N \rightarrow MMN'$:

El Beiyad, Enberg, Ivanov, Pire, Segond, Szymanowski, Teryaev, Wallon:
[1001.4491, hep-ph/0601138, hep-ph/0209300]

▶ $\gamma N \rightarrow \gamma MN'$:

Boussarie, Duplančić, SN, Passek-Kumerički Pire, Szymanowski, Wallon:
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▶ $\gamma N \rightarrow \gamma\gamma N'$:

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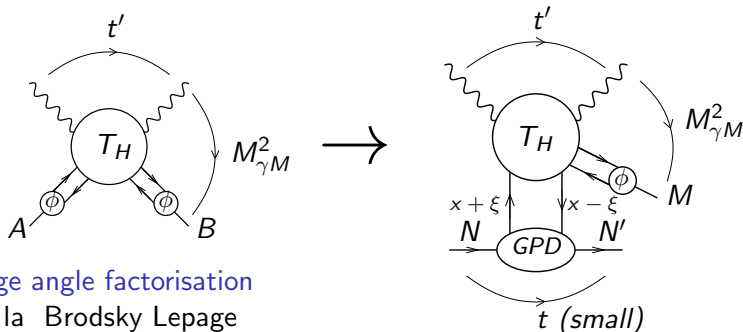
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In above cases, richer kinematics allows one to probe the sensitivity of GPDs wrt x (unlike in DVCS etc) [Qiu, Yu: 2305.15397]

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- ▶ Consider the process $\gamma N \rightarrow \gamma M N'$, M = meson. Collinear factorisation of the amplitude at large $M_{\gamma M}^2$, t' , and small t .

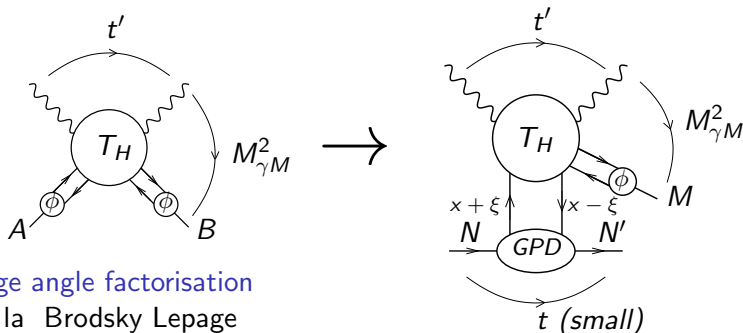


large angle factorisation
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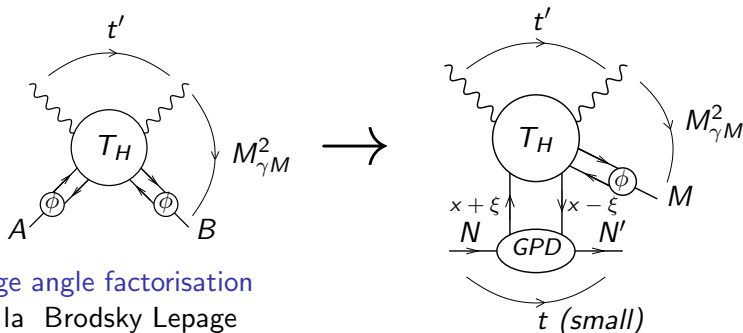
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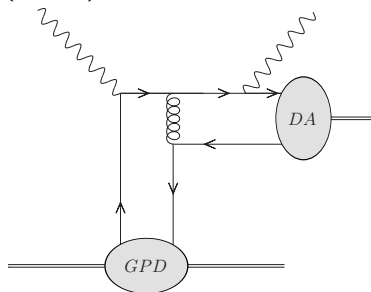
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- ▶ Mesons considered in the final state: π^\pm , $\rho_{L,T}^\pm, 0$.
- ▶ Leading order and leading twist

Why consider a gamma-meson pair?

Chiral-odd GPDs using $\rho_T \gamma$ production

How does it work (at LO)?



Typical non-zero diagram for a **transverse** ρ meson

the σ matrices (from either the DA or the GPD) do not kill it anymore!

Is QCD factorisation really justified?

- ▶ Recently, factorisation has been proved for the process $\pi^\pm N \rightarrow \gamma\gamma N'$ by Qiu, Yu [2205.07846].
- ▶ This was extended to a wide range of $2 \rightarrow 3$ exclusive processes by Qiu, Yu [2210.07995]

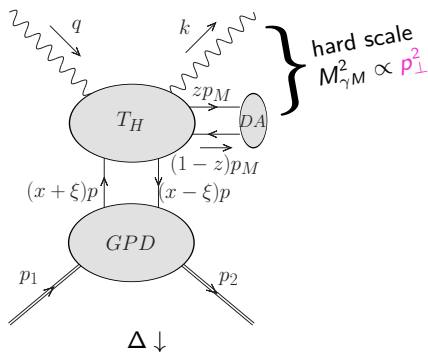
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- ▶ This was extended to a wide range of $2 \rightarrow 3$ exclusive processes by Qiu, Yu [2210.07995]
- ▶ The proof relies on having **large p_T** , rather than large invariant mass (e.g. photon-meson pair).
- ▶ In fact, NLO computation has been performed for $\gamma N \rightarrow \gamma\gamma N'$ by Grocholski, Pire, Sznajder, Szymanowski, Wagner [2110.00048].
- ▶ Also, NLO computation for $\gamma\gamma \rightarrow \pi^+\pi^-$ by crossing symmetry (but involves DAs only) by Duplancic, Nizic [hep-ph/0607069].

$$\gamma(q) + N(p_1) \rightarrow \gamma(k) + M(p_M, \varepsilon_M) + N'(p_2)$$



Useful Mandelstam variables:

$$t = (p_2 - p_1)^2$$

$$u' = (p_M - q)^2$$

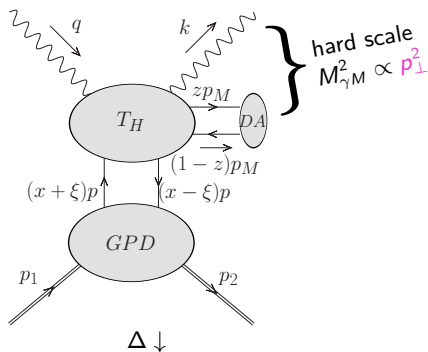
$$t' = (k - q)^2$$

► Factorisation requires:

$$-u' > 1 \text{ GeV}^2, \quad -t' > 1 \text{ GeV}^2 \quad \text{and} \quad (-t)_{\min} \leq -t \leq .5 \text{ GeV}^2$$

⇒ sufficient to ensure **large** p_T .

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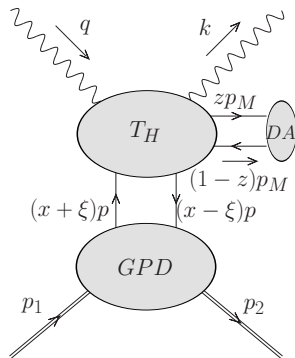
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 \implies sufficient to ensure **large** p_T .
- ▶ Cross-section differential in $(-u')$ and $M^2_{\gamma M}$, and evaluated at $(-t) = (-t)_{\min}$.

$$\mathcal{A} = \int_{-1}^1 dx \int_0^1 dz T(x, \xi, z) H(x, \xi, t) \Phi_M(z)$$

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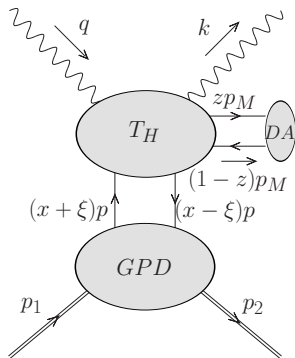
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- Kinematic parameters: $S_{\gamma N}$, $M_{\gamma M}^2$, $-t$, $-u'$
- Useful dimensionless variables (hard part):

$$\alpha = \frac{-u'}{M_{\gamma M}^2},$$

$$\xi = \frac{M_{\gamma M}^2}{2(S_{\gamma N} - m_N^2) - M_{\gamma M}^2}.$$



Computation

Parametrising the GPDs: 2 scenarios for polarised and transversity PDFs

Quark GPDs are parametrised in terms of **Double Distributions**
[Radyushkin: [hep-ph/9805342](https://arxiv.org/abs/hep-ph/9805342)]

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For **polarised** PDFs (and hence **transversity** PDFs), two scenarios are proposed for the parameterization:

- ▶ “**standard**” scenario, with flavor-symmetric light sea quark and antiquark distributions.
- ▶ “**valence**” scenario with a completely flavor-asymmetric light sea quark densities.

- ▶ We take the simplistic **asymptotic** form of the DAs

$$\phi_{\text{as}}(z) = 6z(1 - z).$$

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- ▶ We also investigate the effect of using a **holographic** DA:

$$\phi_{\text{hol}}(z) = \frac{8}{\pi} \sqrt{z(1 - z)}.$$

Suggested by

- ▶ AdS/QCD correspondence [Brodsky, de Teramond: hep-ph/0602252],
- ▶ dynamical chiral symmetry breaking on the light-front [Shi, Chen, Chang, Roberts, Schmidt, Zong: 1504.00689],
- ▶ recent lattice results. [Gao, Hanlon, Karthik, Mukherjee, Petreczky, Scior, Syritsyn, Zhao: 2206.04084]

Exclusive photoproduction of $\pi^0\gamma$

Gluonic GPD contributions

- ▶ Because of the quantum numbers of π^0 ($J^{PC} = 0^{-+}$), the exclusive photoproduction of $\pi^0\gamma$ is also sensitive to gluonic GPD contributions.

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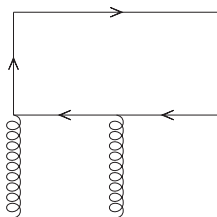
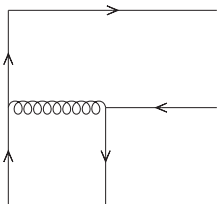
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- ▶ A total of 24 diagrams contribute in this case (compared to 20 diagrams from quark GPD contributions), with 6 groups of 4 related by symmetries ($x \rightarrow -x$ and $z \rightarrow 1 - z$ separately).

Exclusive photoproduction of $\pi^0\gamma$

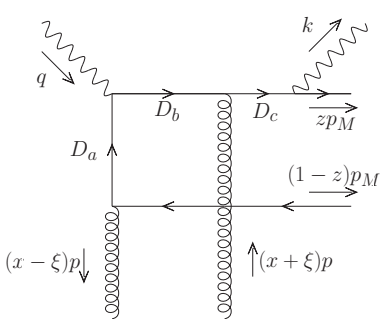
Gluonic GPD contributions

- ▶ Because of the quantum numbers of π^0 ($J^{PC} = 0^{-+}$), the exclusive photoproduction of $\pi^0\gamma$ is also sensitive to gluonic GPD contributions.
- ▶ A total of 24 diagrams contribute in this case (compared to 20 diagrams from quark GPD contributions), with 6 groups of 4 related by symmetries ($x \rightarrow -x$ and $z \rightarrow 1 - z$ separately).
- ▶ Diagrams amount to connecting photons to the following two topologies.



Exclusive photoproduction of $\pi^0\gamma$

Gluonic GPD contributions



$$D_a = ((x - \xi)p + \bar{z}p_M)^2 + i\epsilon$$

$$= s\bar{\alpha}\bar{z} \left[x - \xi + i\epsilon \right],$$

$$D_b = (k + zp_M - (x + \xi)p)^2 + i\epsilon$$

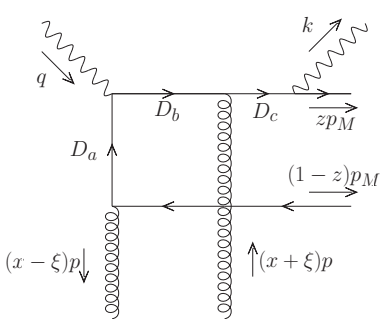
$$= -s \left[z \left(x - \xi - i\epsilon \right) + \alpha\bar{z} \left(x + \xi - i\epsilon \right) \right],$$

$$D_c = (k + zp_M)^2 + i\epsilon$$

$$= 2s\xi z + i\epsilon$$

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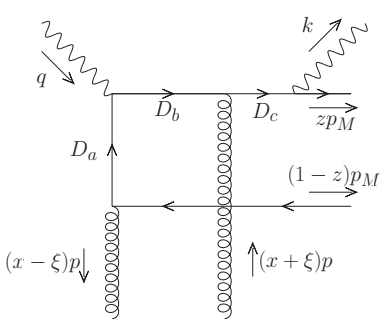
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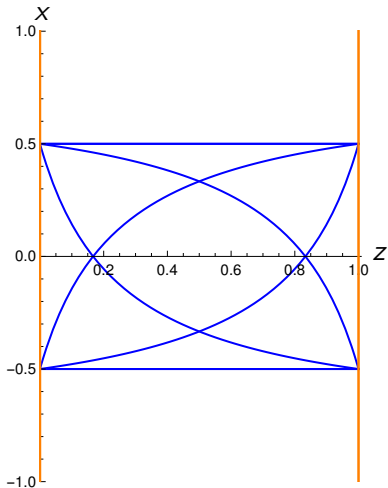
\implies *pinching of poles in the propagators in the limit of $z \rightarrow 1$*

Assuming an asymptotic form of the DA, they manifest themselves (*as a purely imaginary part*) in terms of

- ▶ $\int_0^1 \frac{dz}{z\bar{z}}$ contributions, when the x integration is performed first,
- ▶ $\int_1^1 dx \frac{\ln(x-\xi-i\epsilon)}{(x-\xi+i\epsilon)}$ contributions, when the z integration is performed first.

Exclusive photoproduction of $\pi^0\gamma$

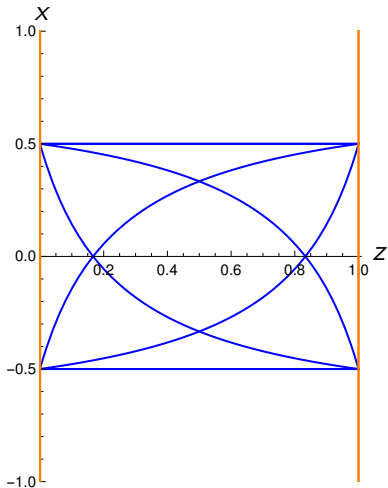
Gluonic GPD contributions: Singularity structure of the full amplitude



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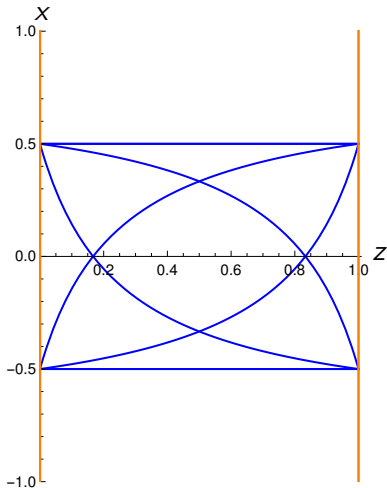
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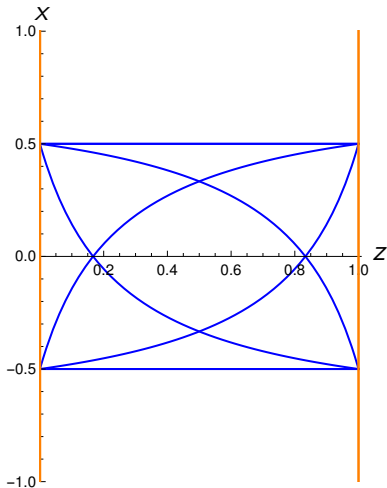
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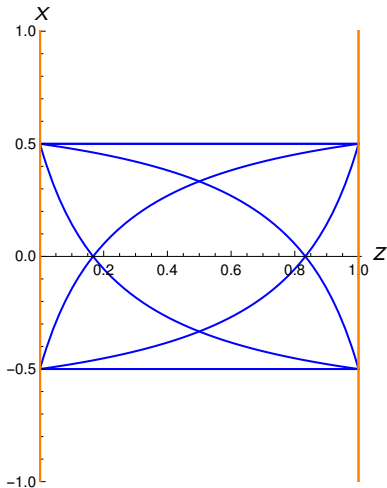
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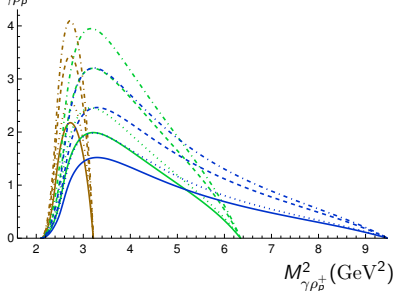
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 - ▶ As far as we know, this represents the first indication of violation of factorisation at leading order and twist-2.
- ▶ Problem happens only if **both** limits are taken, since singularity is a **point** in the integration region of momentum fractions.

Results

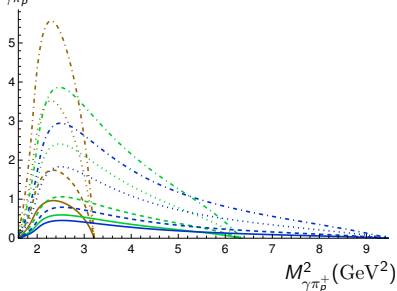
Single differential cross-section: $\gamma\rho_p^+$ vs $\gamma\pi_p^+$

[Details of phase space integration in backup]

$$\frac{d\sigma^{\text{even}}_{\gamma\rho_p^+}}{dM^2_{\gamma\rho_p^+}} \text{ (pb} \cdot \text{GeV}^{-2}\text{)}$$



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$$S_{\gamma N} = 8, 14, 20 \text{ GeV}^2$$

Dashed: Holographic DA

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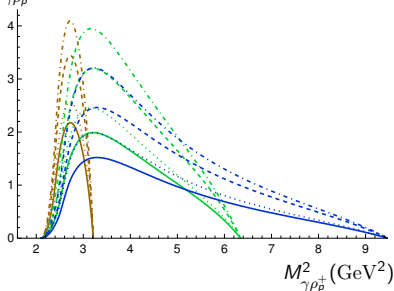
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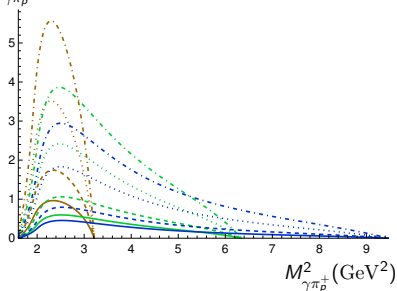
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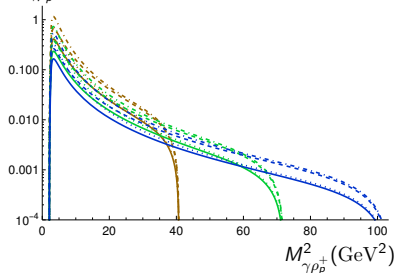
Dotted: standard scenario non-dotted: valence scenario

⇒ Effect of GPD model more important on π_p^+ than on ρ_p^+

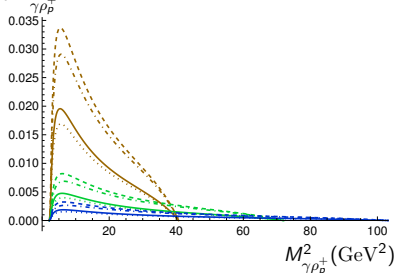
Results

Single differential cross-section: $\gamma\rho_{pL}^+$ vs $\gamma\rho_{pT}^+$

$$\frac{d\sigma^{\text{even}}}{dM^2} \frac{\gamma\rho_{pL}^+}{\gamma\rho_p^+} \text{ (pb} \cdot \text{GeV}^{-2}\text{)}$$



$$\frac{d\sigma^{\text{odd}}}{dM^2} \frac{\gamma\rho_{pT}^+}{\gamma\rho_p^+} \text{ (pb} \cdot \text{GeV}^{-2}\text{)}$$



$$S_{\gamma N} = 80, 140, 200 \text{ GeV}^2$$

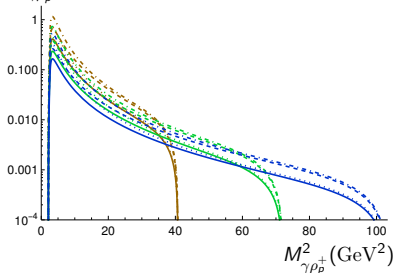
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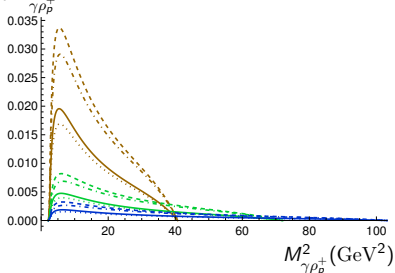
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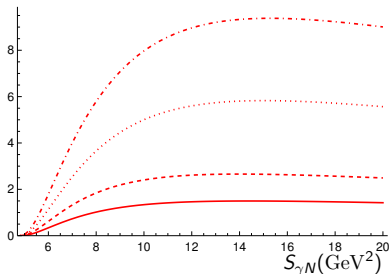
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CO cross-section is suppressed by a factor of ξ^2 ($\xi \approx \frac{M_{\gamma\rho}^2}{2S_{\gamma N}}$):
Measurable at small $S_{\gamma N}$, but drops rapidly with increasing $S_{\gamma N}$.

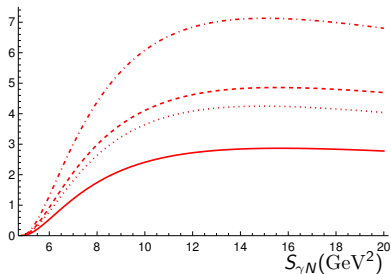
Results

Integrated cross-section: $\gamma\pi_p^+$ vs $\gamma\pi_n^-$

$\sigma_{\gamma\pi_p^+}^{even}$ (pb)



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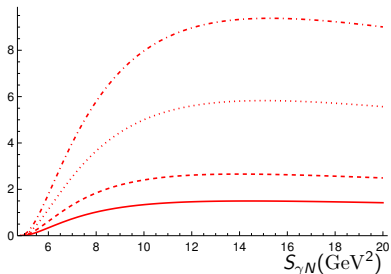
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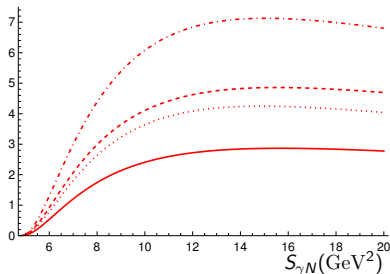
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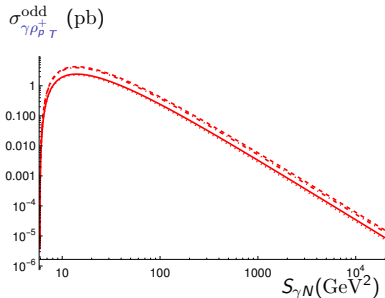
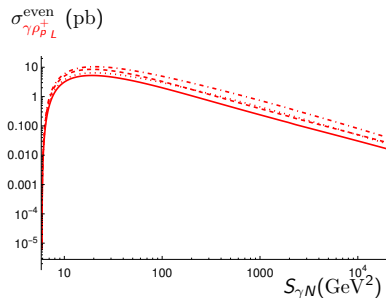
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⇒ Huge effect from GPD model in π_p^+ case.

Results

Integrated cross-section: $\gamma\rho_{pL}^+$ vs $\gamma\rho_{pT}^+$



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$\implies \xi^2$ suppression in the chiral-odd case causes the cross-section to drop rapidly with $S_{\gamma N}$.

Results

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We consider an **unpolarised target**, and determine polarisation asymmetries wrt the incoming photon.

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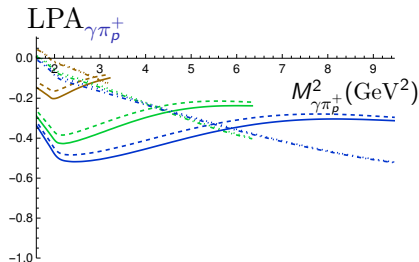
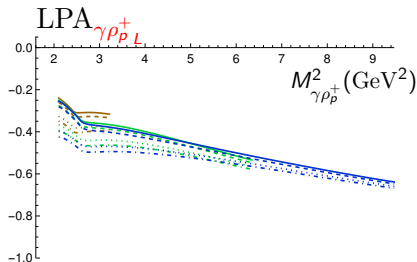
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- ▶ **Kleiss-Sterling** spinor techniques used to obtain expressions.
- ▶ **Both asymmetries zero in chiral-odd case!**

Results

LPA wrt incoming photon: Single-differential level: $\gamma\rho_p^+$ vs $\gamma\pi_p^+$



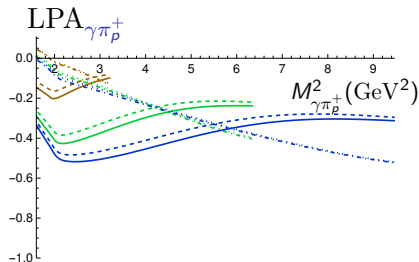
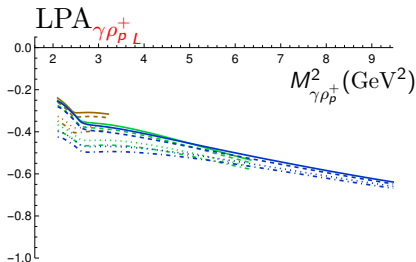
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⇒ GPD model changes the behaviour of the LPA completely in the π_p^+ case!

Prospects at experiments

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Good statistics: For example, at [JLab Hall B](#):

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- ▶ No problem in detecting outgoing photon at JLab [\[backup\]](#).

At COMPASS:

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- ▶ Lower numbers due to low luminosity (factor of 10^3 less than JLab!)

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- ▶ Small ξ study:
 $300 < S_{\gamma N} / \text{GeV}^2 < 20000$ ($5 \cdot 10^{-5} < \xi < 5 \cdot 10^{-3}$):
 - ρ_L^0 (on p) : $\approx 1.2 \times 10^3$
 - ρ_T^0 (on p) : ≈ 6.5 (Chiral-odd) (tiny)
 - ρ_L^+ : $\approx 9.3 \times 10^2$
 - π^+ : $\approx 5.0 \times 10^2$

For p-Pb UPCs at LHC (integrated luminosity of 1200 nb^{-1}):

► With future data from runs 3 and 4,

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- ▶ $300 < S_{\gamma N} / \text{GeV}^2 < 20000$ ($5 \cdot 10^{-5} < \xi < 5 \cdot 10^{-3}$):
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- ▶ **Good statistics** in various experiments, particularly at JLab.
- ▶ **Small ξ limit** of GPDs can be investigated by exploiting high energies available in collider mode such as EIC and UPCs at LHC.

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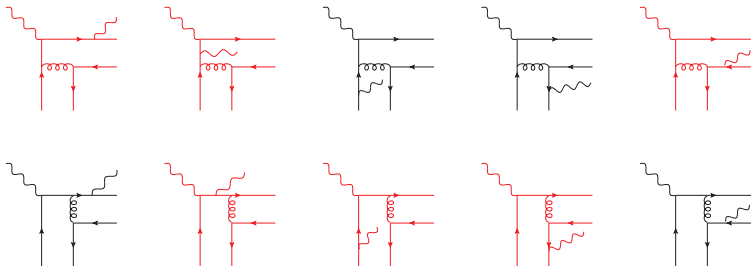
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 - Quark GPD contribution only involves 422 diagrams!
 - Also, double integration over momentum fractions: Very hard!
- ▶ Generalise to **electroproduction** ($Q^2 \neq 0$).
- ▶ Add **Bethe-Heitler** component (photon emitted from incoming lepton)
 - zero in chiral-odd case.
 - suppressed in chiral-even case.

BACKUP SLIDES

Computation

Hard Part: Diagrams

A total of 20 diagrams to compute



- ▶ Need to compute 10 diagrams: Other half related by $q \leftrightarrow \bar{q}$ (anti)symmetry.
- ▶ In fact, by choosing the **right gauge**, **only 4 diagrams** can be used to generate all the others by various symmetries (eg. photon exchange).
- ▶ **Red** diagrams **cancel** in the chiral-odd case

Computation

Parametrising the GPDs: ρ_L and π case, Chiral-even

$$\int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p_2, \lambda_2 | \bar{\psi}_q \left(-\frac{1}{2}z^- \right) \gamma^+ \psi \left(\frac{1}{2}z^- \right) | p_1, \lambda_1 \rangle$$
$$= \frac{1}{2P^+} \bar{u}(p_2, \lambda_2) \left[H^q(x, \xi, t) \gamma^+ + E^q(x, \xi, t) \frac{i\sigma^{\alpha+} \Delta_\alpha}{2m} \right] u(p_1, \lambda_1)$$

$$\int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p_2, \lambda_2 | \bar{\psi}_q \left(-\frac{1}{2}z^- \right) \gamma^+ \gamma^5 \psi \left(\frac{1}{2}z^- \right) | p_1, \lambda_1 \rangle$$
$$= \frac{1}{2P^+} \bar{u}(p_2, \lambda_2) \left[\tilde{H}^q(x, \xi, t) \gamma^+ \gamma^5 + \tilde{E}^q(x, \xi, t) \frac{\gamma^5 \Delta^+}{2m} \right] u(p_1, \lambda_1)$$

- ▶ Take the limit $\Delta_\perp = 0$.
- ▶ In that case and for small ξ , the dominant contributions come from H^q and \tilde{H}^q .

Computation

Parametrising the GPDs: ρ_T case, Chiral-odd

$$\begin{aligned} & \int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p_2, \lambda_2 | \bar{\psi}_q \left(-\frac{1}{2}z^- \right) i\sigma^{+i} \psi \left(\frac{1}{2}z^- \right) | p_1, \lambda_1 \rangle \\ &= \frac{1}{2P^+} \bar{u}(p_2, \lambda_2) \left[H_T^q(x, \xi, t) i\sigma^{+i} + \tilde{H}_T^q(x, \xi, t) \frac{P^+ \Delta^i - \Delta^+ P^i}{m_N^2} \right. \\ &+ \left. E_T^q(x, \xi, t) \frac{\gamma^+ \Delta^i - \Delta^+ \gamma^i}{2m_N} + \tilde{E}_T^q(x, \xi, t) \frac{\gamma^+ P^i - P^+ \gamma^i}{m_N} \right] u(p_1, \lambda_1) \end{aligned}$$

- ▶ Take the limit $\Delta_\perp = 0$.
- ▶ In that case and for small ξ , the dominant contributions come from H_T^q .

- ▶ GPDs can be represented in terms of **Double Distributions**
[Radyushkin: hep-ph/9805342]

$$H^q(x, \xi, t = 0) = \int_{-1}^1 d\beta \int_{-1+|\beta|}^{1-|\beta|} d\alpha \delta(\beta + \xi\alpha - x) f^q(\beta, \alpha)$$

- ▶ ansatz for these Double Distributions:

- ▶ chiral-even sector:

$$\begin{aligned} f^q(\beta, \alpha, t = 0) &= \Pi(\beta, \alpha) q(\beta) \Theta(\beta) - \Pi(-\beta, \alpha) \bar{q}(-\beta) \Theta(-\beta), \\ \tilde{f}^q(\beta, \alpha, t = 0) &= \Pi(\beta, \alpha) \Delta q(\beta) \Theta(\beta) + \Pi(-\beta, \alpha) \Delta \bar{q}(-\beta) \Theta(-\beta). \end{aligned}$$

- ▶ chiral-odd sector:

$$f_T^q(\beta, \alpha, t = 0) = \Pi(\beta, \alpha) \delta q(\beta) \Theta(\beta) - \Pi(-\beta, \alpha) \delta \bar{q}(-\beta) \Theta(-\beta).$$

- ▶ $\Pi(\beta, \alpha) = \frac{3}{4} \frac{(1-\beta)^2 - \alpha^2}{(1-\beta)^3}$: profile function

- ▶ simplistic factorised ansatz for the t -dependence:

$$H^q(x, \xi, t) = H^q(x, \xi, t = t_{\min}) \times F_H(t)$$

with $F_H(t) = \frac{(t_{\min} - C)^2}{(t - C)^2}$ a standard **dipole form factor**
($C = 0.71 \text{ GeV}^2$)

Sets of PDFs used to model GPDs

- ▶ $q(x)$: unpolarised PDF:
 - GRV-98 [Glück, Reya, Vogt: hep-ph/9806404]
 - MSTW2008lo [Martin, Stirling, Thorne, Watt: 0901.0002]
 - MSTW2008nnlo [Martin, Stirling, Thorne, Watt: 0901.0002]
 - ABM11nnlo [Alekhin, Blumlein, Moch: 1202.2281]
 - CT10nnlo [Gao, Guzzi, Huston, Lai, Li, Nadolsky, Pumplin, Stump, Yuan: 1302.6246]
- ▶ $\Delta q(x)$ polarised PDF
 - GRSV-2000 [Glück, Reya, Stratmann, Vogelsang: hep-ph/0011215]
- ▶ $\delta q(x)$: transversity PDF:
 - Based on parameterisation for TMDs from which transversity PDFs obtained as limiting case [Anselmino, Boglione, D'Alesio, Melis, Murgia, Prokudin: 1303.3822]

Effects are not significant! But relevant for NLO corrections!

- Helicity conserving (vector) DA at twist 2: ρ_L

$$\langle 0 | \bar{u}(0) \gamma^\mu u(x) | \rho_L^0(p) \rangle = \frac{p^\mu}{\sqrt{2}} f_\rho \int_0^1 du e^{-iup \cdot x} \phi_\rho(u)$$

- Helicity flip (tensor) DA at twist 2: ρ_T

$$\langle 0 | \bar{u}(0) \sigma^{\mu\nu} u(x) | \rho_T^0(p, s) \rangle = \frac{i}{\sqrt{2}} (\epsilon_\rho^\mu p^\nu - \epsilon_\rho^\nu p^\mu) f_\rho^\perp \int_0^1 du e^{-iup \cdot x} \phi_\rho(u)$$

- Helicity conserving (axial) DA at twist 2: π^\pm

$$\langle 0 | \bar{u}(0) \gamma^\mu \gamma^5 d(x) | \pi(p) \rangle = ip^\mu f_\pi \int_0^1 du e^{-iup \cdot x} \phi_\pi(u)$$

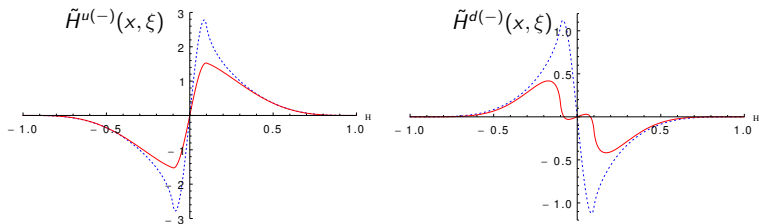
Computation

Valence vs Standard scenarios in \tilde{H} (Chiral-even, Axial)

Typical kinematic point (for JLab kinematics):

$$\xi = .1 \leftrightarrow S_{\gamma N} = 20 \text{ GeV}^2 \text{ and } M_{\gamma\rho}^2 = 3.5 \text{ GeV}^2$$

$$\tilde{H}^{q(-)}(x, \xi, t) = \tilde{H}^q(x, \xi, t) - \tilde{H}^q(-x, \xi, t) \quad [C = -1]$$



“valence” and “standard”: two GRSV Ansätze for $\Delta q(x)$

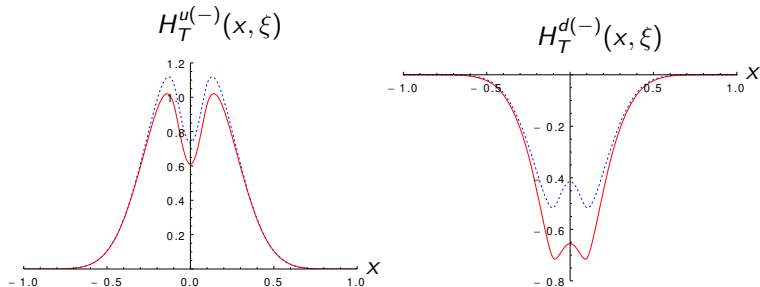
Computation

Valence vs Standard scenarios in H_T (Chiral-odd)

Typical kinematic point (for JLab kinematics):

$$\xi = .1 \leftrightarrow S_{\gamma N} = 20 \text{ GeV}^2 \text{ and } M_{\gamma\rho}^2 = 3.5 \text{ GeV}^2$$

$$H_T^{q(-)}(x, \xi, t) = H_T^q(x, \xi, t) + H_T^q(-x, \xi, t) \quad [C = -1]$$



“valence” and “standard”: two GRSV Ansätze for $\Delta q(x)$

\Rightarrow two Ansätze for $\delta q(x)$

- ▶ Work in the limit of:

- $\Delta_{\perp} \ll p_{\perp}$
- $m_N^2, m_M^2 \ll M_{\gamma M}^2$

- ▶ initial state particle momenta:

$$q^{\mu} = n^{\mu},$$

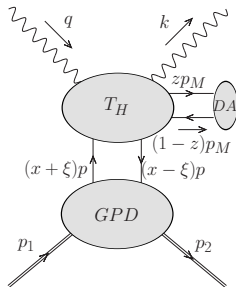
$$p_1^{\mu} = (1 + \xi) p^{\mu} + \frac{m_N^2}{s(1+\xi)} n^{\mu}$$

- ▶ final state particle momenta:

$$p_2^{\mu} = (1 - \xi) p^{\mu} + \frac{m_N^2 + \vec{p}_t^2}{s(1 - \xi)} n^{\mu} + \Delta_{\perp}^{\mu}$$

$$k^{\mu} = \alpha n^{\mu} + \frac{(\vec{p}_t - \vec{\Delta}_t/2)^2}{\alpha s} p^{\mu} + p_{\perp}^{\mu} - \frac{\Delta_{\perp}^{\mu}}{2}, \quad \Delta \downarrow$$

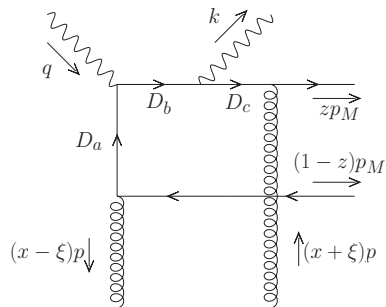
$$p_M^{\mu} = \alpha_M n^{\mu} + \frac{(\vec{p}_t + \vec{\Delta}_t/2)^2 + m_M^2}{\alpha_M s} p^{\mu} - p_{\perp}^{\mu} - \frac{\Delta_{\perp}^{\mu}}{2},$$



hard scale
 $M_{\gamma M}^2 \propto p_{\perp}^2$

Exclusive photoproduction of $\pi^0\gamma$

Gluonic GPD contributions



$$D_a = ((x - \xi)p + \bar{z}p_M)^2 + i\epsilon$$

$$= s\bar{\alpha}\bar{z}[x - \xi + i\epsilon] ,$$

$$D_b = (k + zp_M - (x + \xi)p)^2 + i\epsilon$$

$$= -s[z(x - \xi - i\epsilon) + \alpha\bar{z}(x + \xi - i\epsilon)] ,$$

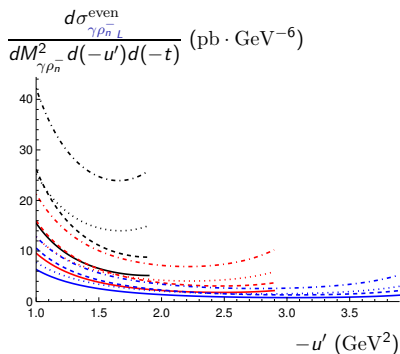
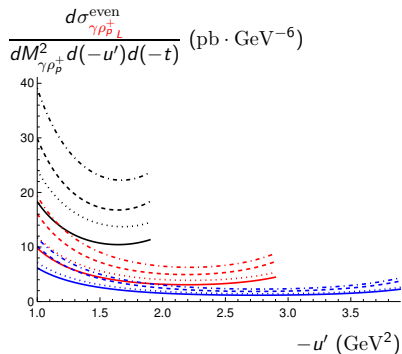
$$D_c = (zp_M - (x + \xi)p)^2 + i\epsilon$$

$$= -s\bar{\alpha}z[x + \xi - i\epsilon]$$

\implies pinching of poles in the propagators (D_a and D_b) in the limit of $z \rightarrow 1$

Results

Fully-differential cross-sections: $\gamma\rho_{pL}^+$ vs $\gamma\rho_{nL}^-$



$$S_{\gamma N} = 20 \text{ GeV}^2, \quad -t = (-t)_{\text{min}}, \quad M_{\gamma\rho}^2 = 3, 4, 5 \text{ GeV}^2$$

Dashed: Holographic DA non-dashed: Asymptotical DA

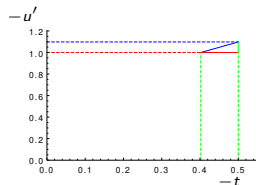
Dotted: standard scenario non-dotted: valence scenario

Results

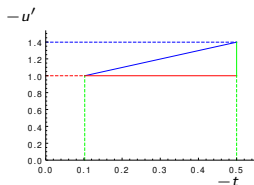
Phase space integration: Evolution in $(-t, -u')$ plane

large angle scattering: $M_{\gamma\rho}^2 \sim -u' \sim -t'$ ($S_{\gamma N} = 20 \text{ GeV}^2$)

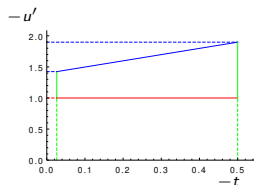
$\implies -u' > 1 \text{ GeV}^2$ and $-t' > 1 \text{ GeV}^2$ and $(-t)_{\min} \leq -t \leq .5 \text{ GeV}^2$



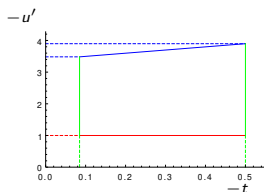
$M_{\gamma\rho} = 2.2 \text{ GeV}^2$



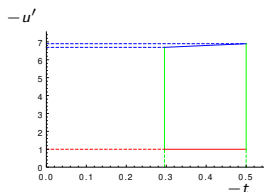
$M_{\gamma\rho} = 2.5 \text{ GeV}^2$



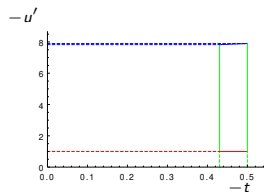
$M_{\gamma\rho} = 3 \text{ GeV}^2$



$M_{\gamma\rho} = 5 \text{ GeV}^2$



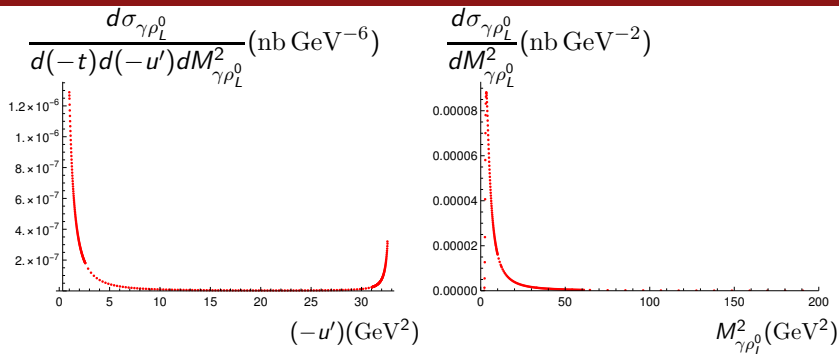
$M_{\gamma\rho} = 8 \text{ GeV}^2$



$M_{\gamma\rho} = 9 \text{ GeV}^2$

Results

Necessity for Importance Sampling



- ▶ Need enough points at boundaries for distribution in $(-u')$
- ▶ Need enough points to resolve peak (at low $M_{\gamma\rho_L^0}^2$) for distribution in $M_{\gamma\rho_L^0}^2$

Results

Explaining the difference between chiral-even and chiral-odd plots

▶ $\xi = \frac{M_{\gamma M}^2}{2S_{\gamma N} - M_N^2} \approx \frac{M_{\gamma M}^2}{2S_{\gamma N}}$ for $M_{\gamma M}^2 \ll S_{\gamma N}$

▶ Chiral-even (unpolarised) cross-section:

$$|\overline{\mathcal{M}}_{\text{CE}}|^2 = \frac{2}{s^2} (1 - \xi^2) C_{\text{CE}}^2 \left\{ 2 |N_A|^2 + \frac{p_{\perp}^4}{s^2} |N_B|^2 + \frac{p_{\perp}^2}{s} (N_A N_B^* + \text{c.c.}) + \frac{p_{\perp}^4}{4s^2} |N_{A_5}|^2 + \frac{p_{\perp}^4}{4s^2} |N_{B_5}|^2 \right\}.$$

▶ Chiral-odd (unpolarised) cross-section:

$$|\overline{\mathcal{M}}_{\text{CO}}|^2 = \frac{2048}{s^2} \xi^2 (1 - \xi^2) C_{\text{CO}}^2 \left\{ \alpha^4 |N_{TA}|^2 + |N_{TB}|^2 \right\}.$$

▶ Note: $\alpha = \frac{-u'}{M_{\gamma M}^2}$.

Results

Integrated cross-section: Mapping procedure for different values of $S_{\gamma N}$

To obtain distribution in $S_{\gamma N}$, we exploit non-trivial mapping between 1 set of data at a fixed $S_{\gamma N}$ to other values $\tilde{S}_{\gamma N}$ *lower* than it.

$$\tilde{M}_{\gamma M}^2 = M_{\gamma M}^2 \frac{\tilde{S}_{\gamma N} - m_N^2}{S_{\gamma N} - m_N^2},$$
$$- \tilde{u}' = \frac{\tilde{M}_{\gamma M}^2}{M_{\gamma M}^2} (-u').$$

Implementing **importance sampling** \implies careful consideration of the various limits involved are needed.

Mapping possible since **different** sets of $(S_{\gamma N}, M_{\gamma M}^2, -u')$ correspond to the **same** (α, ξ) .

$$\alpha = \frac{-u'}{M_{\gamma M}^2}, \quad \xi = \frac{M_{\gamma M}^2}{2(S_{\gamma N} - m_N^2) - M_{\gamma M}^2}.$$

Results

Why does the circular asymmetry vanish for unpolarised target?

Consider

$$\gamma(q, \lambda_q) + N(p_1, \lambda_1) \rightarrow \gamma(k, \lambda_k) + \pi^\pm(p_\pi) + N'(p_2, \lambda_2),$$

where λ_i represent the helicities of the particles.

QED/QCD **invariance under parity** implies that [Bourenly, Soffer, Leader: Phys.Rept. 59 (1980) 95-297]

$$\mathcal{A}_{\lambda_2 \lambda_k; \lambda_1 \lambda_q} = \eta (-1)^{\lambda_1 - \lambda_q - (\lambda_2 - \lambda_k)} \mathcal{A}_{-\lambda_2 - \lambda_k; -\lambda_1 - \lambda_q},$$

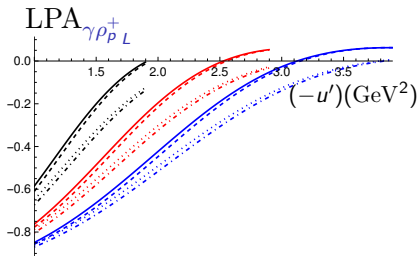
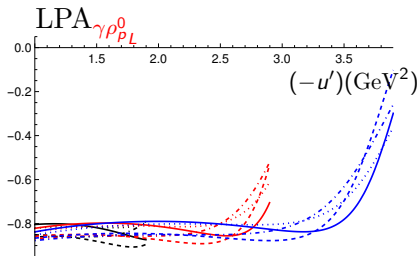
where η represents phase factors related to intrinsic spin.

Thus, at the cross-section level, it is clear that circular asymmetry will vanish, since

$$\sum_{\lambda_i, i \neq q} |\mathcal{A}_{\lambda_2 \lambda_k; \lambda_1 +}|^2 = \sum_{\lambda_i, i \neq q} |\mathcal{A}_{\lambda_2 \lambda_k; \lambda_1 -}|^2$$

Results

LPA wrt incoming photon: Fully-differential level: $\gamma\rho_{PL}^0$ vs $\gamma\rho_{PL}^+$



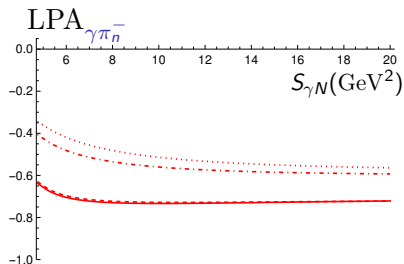
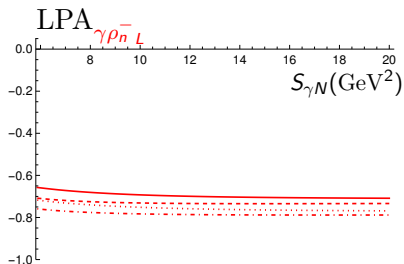
$$S_{\gamma N} = 20 \text{ GeV}^2, -t = (-t)_{\min}, M_{\gamma\rho}^2 = 3, 4, 5 \text{ GeV}^2$$

Dashed: Holographic DA non-dashed: Asymptotical DA

Dotted: standard scenario non-dotted: valence scenario

Results

LPA wrt incoming photon: Integrated level: $\gamma\rho_n^-$ vs $\gamma\pi_n^-$



Dashed: Holographic DA

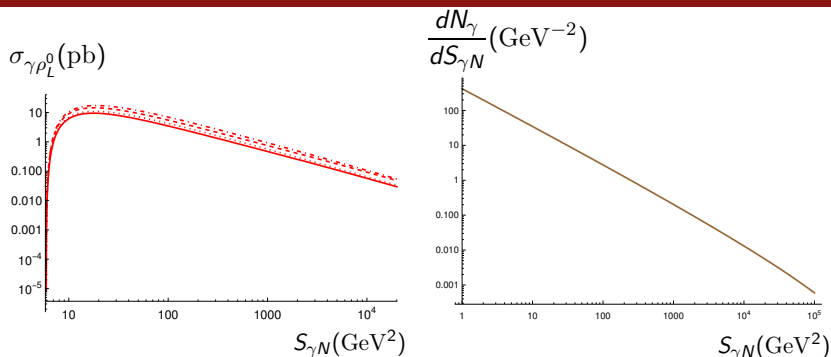
non-dashed: Asymptotical DA

Dotted: standard scenario

non-dotted: valence scenario

Prospects at experiments

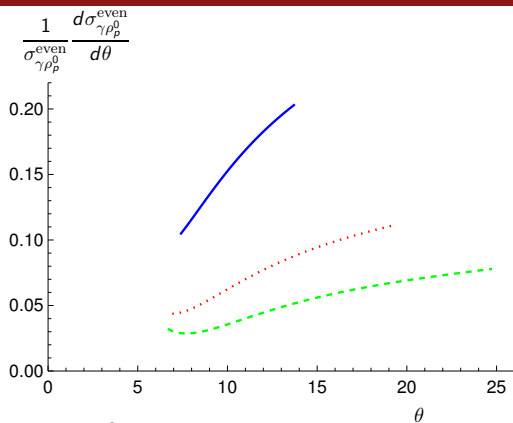
Why counting rates lower UPCs at LHC?



- ▶ Photon flux enhanced by a factor of Z^2 , but drops rapidly with $S_{\gamma N} \implies$ *Low luminosity not compensated by larger photon flux.*
- ▶ LHC great for high energy, but JLab better in terms of luminosity.
- ▶ Still, LHC gives us access to the small ξ region of GPDs!

Angular cuts on outgoing photon at JLab

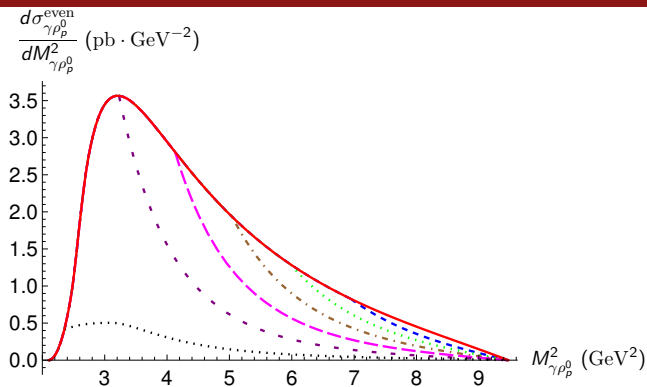
Angular distribution: $\rho_p^0 \gamma$ photoproduction at $S_{\gamma N} = 20 \text{ GeV}^2$



- ▶ $M_{\gamma\rho_p^0}^2 = 4 \text{ GeV}^2$ (solid blue)
- ▶ $M_{\gamma\rho_p^0}^2 = 6 \text{ GeV}^2$ (dotted red)
- ▶ $M_{\gamma\rho_p^0}^2 = 8 \text{ GeV}^2$ (dashed green)

Angular cuts on outgoing photon at JLab

Single differential cross-section: $\rho_p^0 \gamma$ photoproduction at $S_{\gamma N} = 20 \text{ GeV}^2$



- ▶ no angular cut (solid red)
- ▶ $\theta \leq 35^\circ$ (dashed blue)
- ▶ $\theta \leq 30^\circ$ (dotted green)
- ▶ $\theta \leq 25^\circ$ (dashed-dotted brown)
- ▶ $\theta \leq 20^\circ$ (long-dashed magenta)
- ▶ $\theta \leq 15^\circ$ (short-dashed purple)
- ▶ $\theta \leq 10^\circ$ (dotted black)