



# Cooling studies in the US

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MUON Collider Collaboration Meeting

12 October 2022

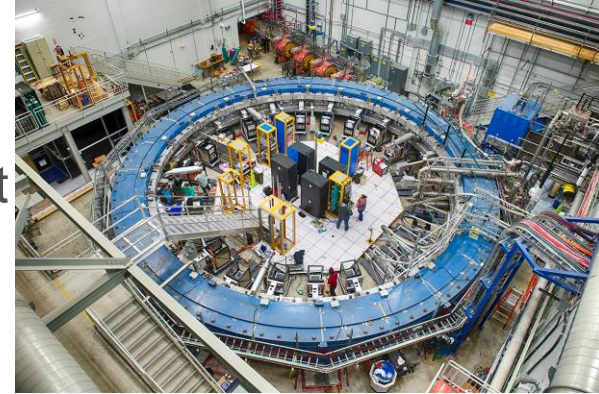
# Outline

- Experimental studies on muon cooling in the US
  - Motivation
  - Concept
  - Results
  - Future studies
- Design studies on muon cooling in the US
  - Results accomplished during the MAP program
  - Future plans

# Fermilab Muon g-2 Experiment

- Goal

- Measure the muon anomalous magnetic moment (g-2) with 0.14 ppm uncertainty - a fourfold improvement of the BNL measurement (0.54 ppm)



- Approach

- Circulate polarized muons in a uniform magnetic field and measure the precession frequency
- 3.1 GeV/c muons to simplify Thomas-BMT

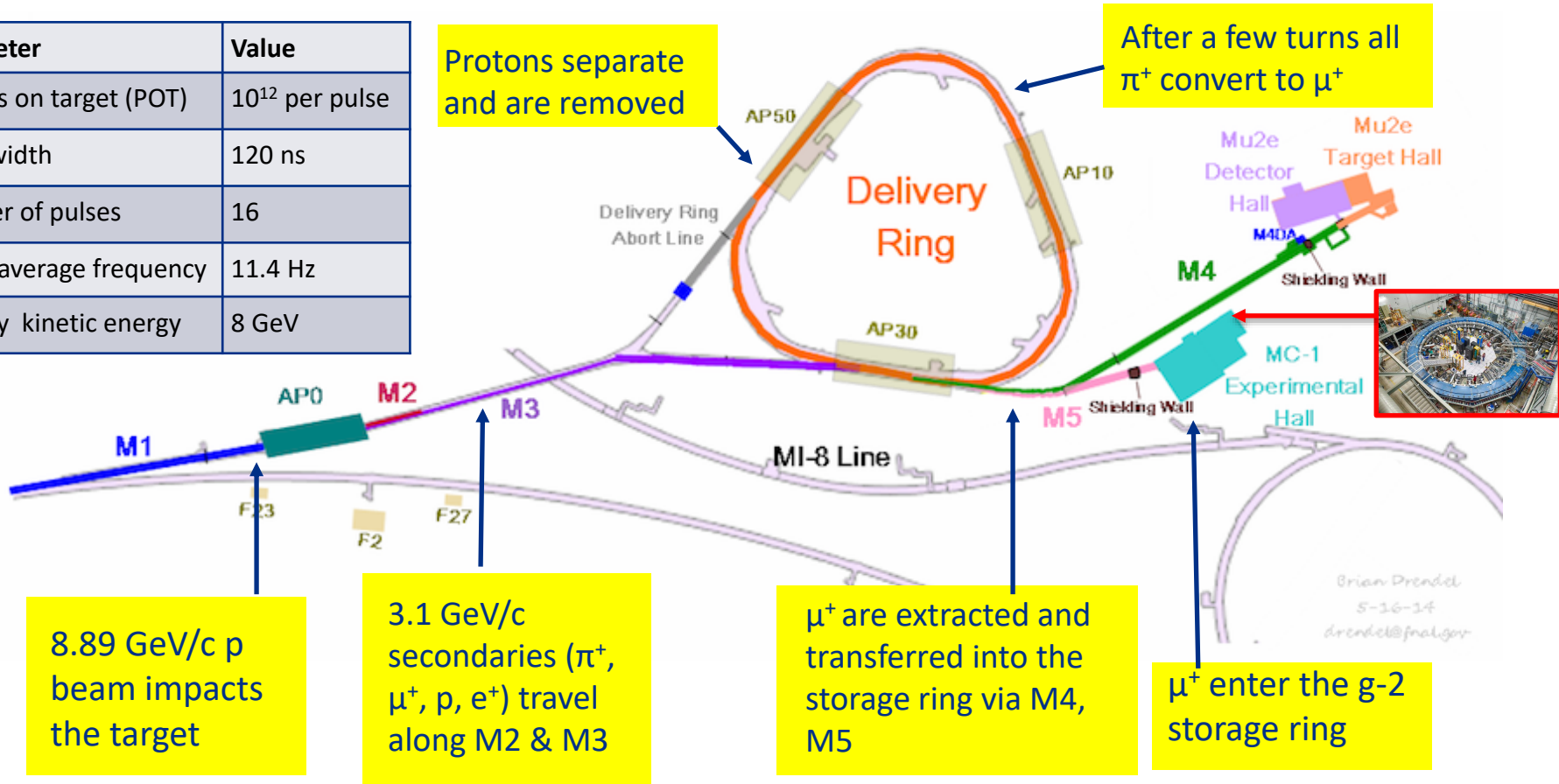
equation:  $\vec{\omega}_a = \frac{e}{mc} \left[ a_\mu \vec{B} - \left( a_\mu - \frac{1}{\gamma^2 - 1} \right) \vec{\beta} \times \vec{E} \right]$

- Requirement

- Requires delivery of  $1.4 \times 10^{14}$  muons in the ring which is x21 the statistics of the BNL experiment

# Muon Campus layout

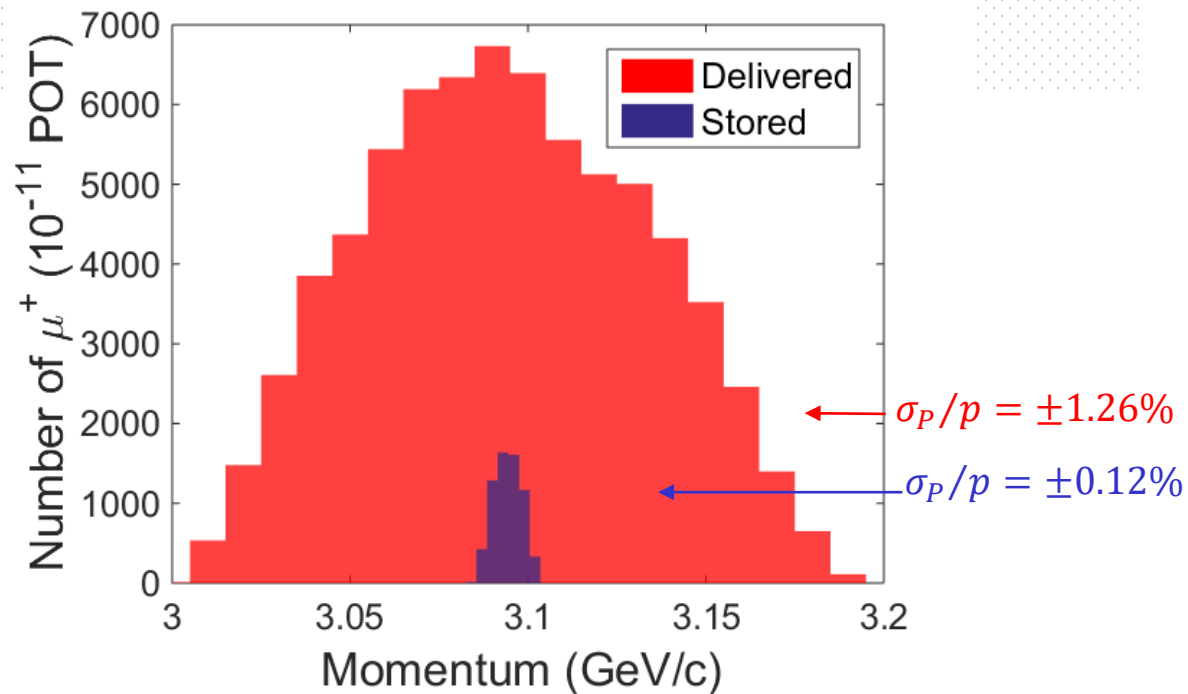
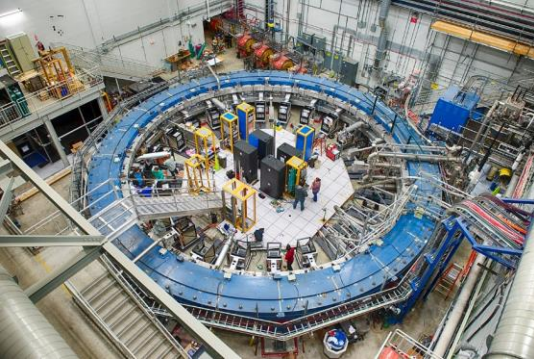
Parameter	Value
Protons on target (POT)	$10^{12}$ per pulse
Pulse width	120 ns
Number of pulses	16
Bunch average frequency	11.4 Hz
Primary kinetic energy	8 GeV



- Since 2018, Muon Campus has delivered  $\sim 19$ x BNLS and is expected to deliver the desired goal by the end of FY23

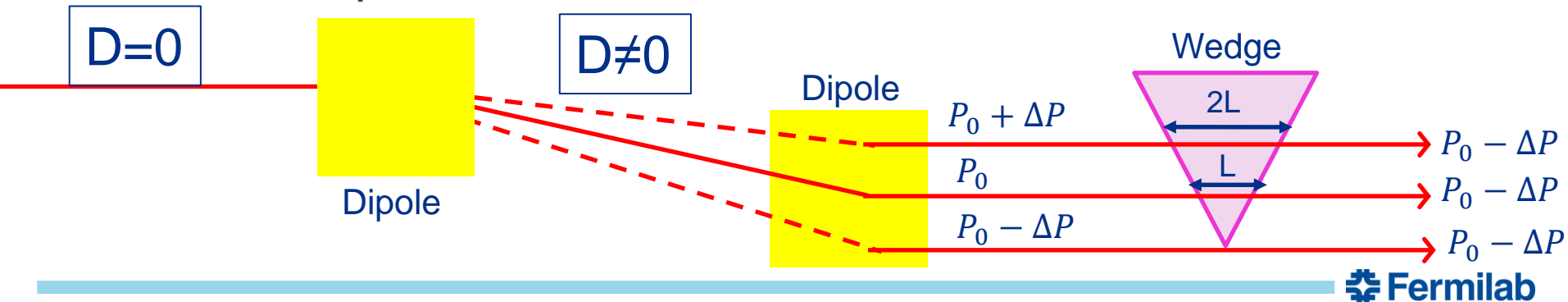
# Motivation for beam cooling

- The beam delivered to the storage ring of the Muon g-2 Experiment has a rms momentum spread of  $\sim 1.3\%$
- The ring accepts muons within  $\sim 0.1\%$  of the magic momentum ( $\sim 3.1$  GeV/c) only. Nearly 90% of the incoming beam is lost.



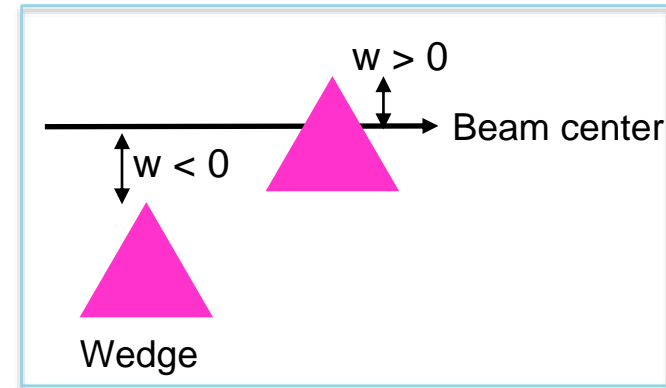
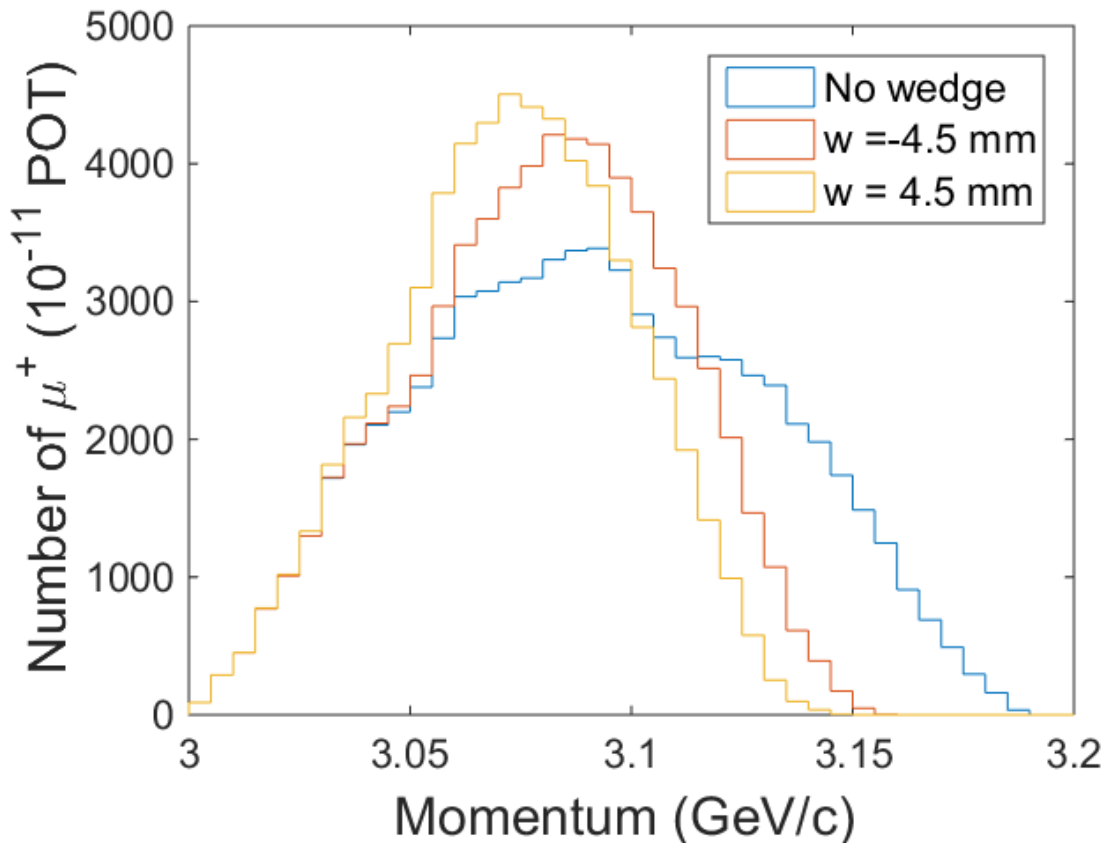
# Proposed improvement strategy

- First separate particles by momentum by guiding them into a dispersive area
- Then, pass the beam through a wedge absorber
- With a properly designed wedge, high-energy muons will lose more energy than low-energy ones. As a result, the overall energy spread of the beam is reduced
- Through Fermilab's LDRD program, in 2017, we have been awarded a grant to design, install and test a wedge in the Muon Campus



# Simulation of the concept

- Simulations of the wedge concept along the Fermilab Muon Campus revealed that a wedge can increase the number of stored muons for the Muon g-2 Experiment

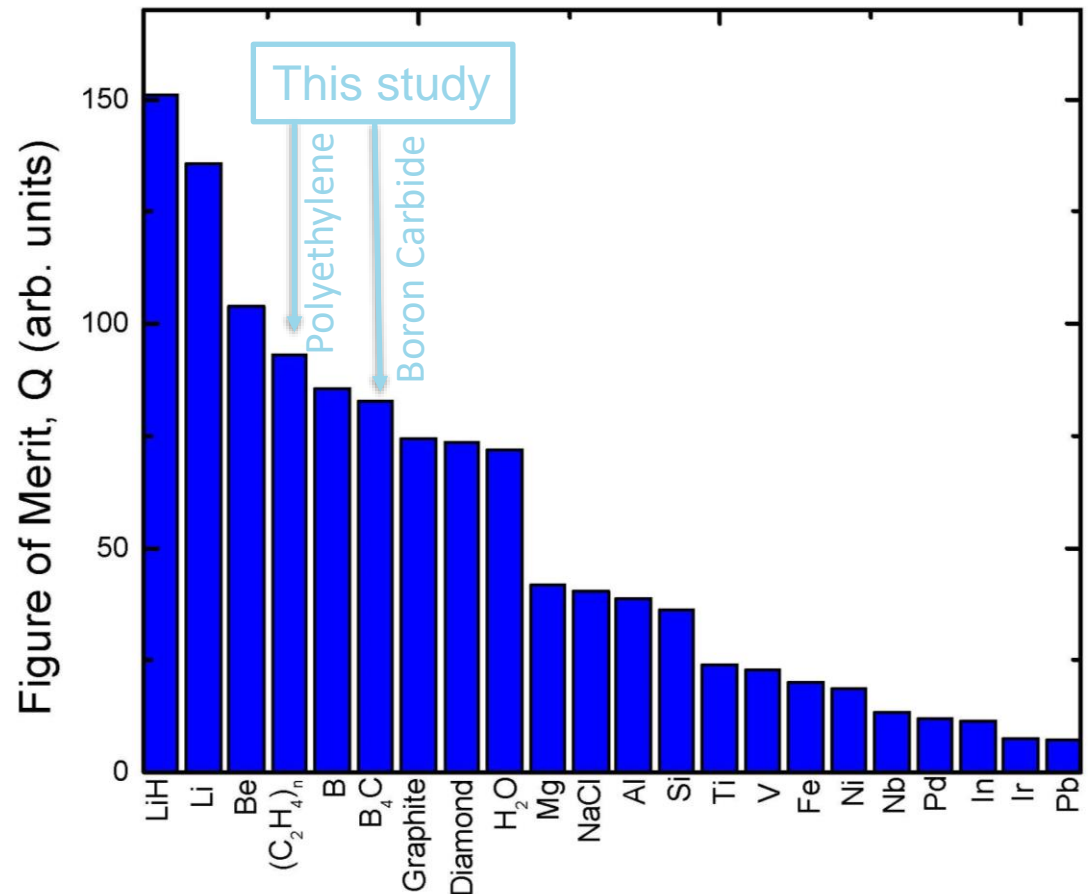


# Choice of material

- A figure of merit for each material can be obtained by taking the product of it's energy-loss and radiation length terms

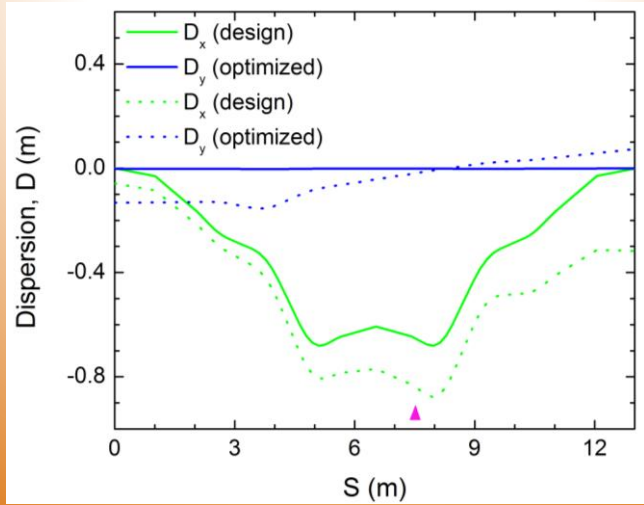
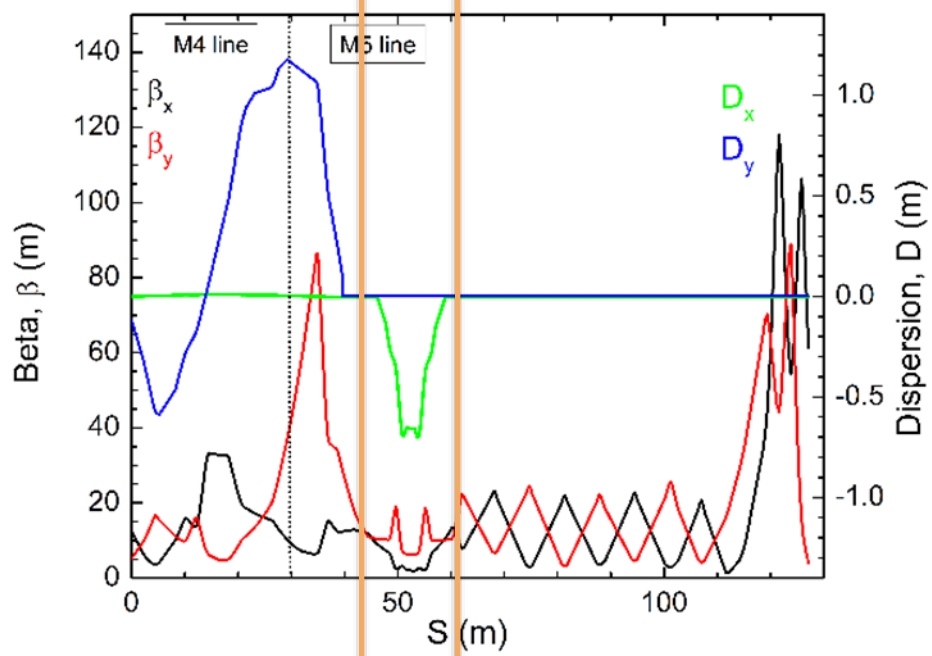
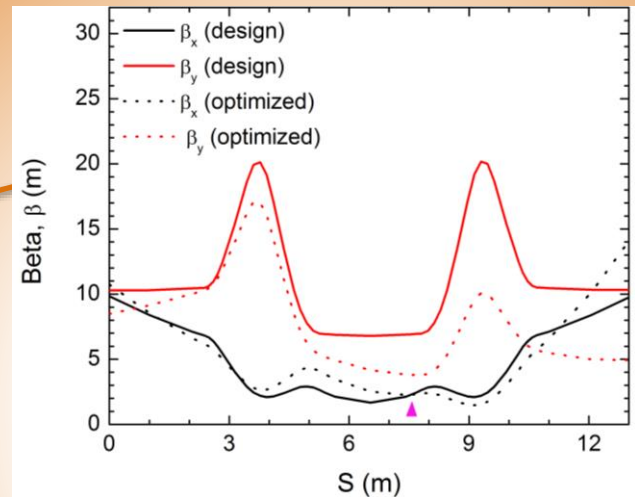
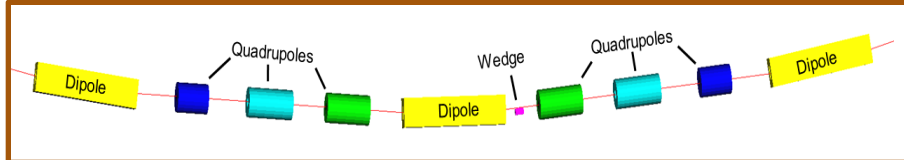
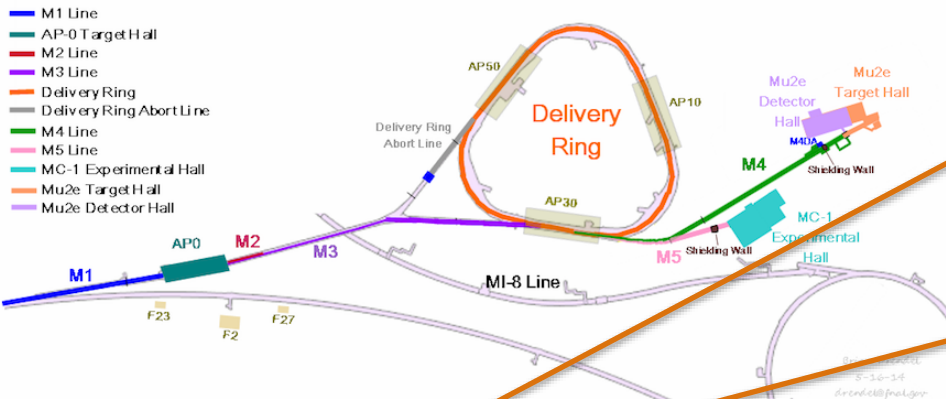
## Boron Carbide ( $B_4C$ )

Quantity	Value	Units
$\langle Z/A \rangle$		
Specific gravity		
Mean excitation energy		
Minimum ionization	4.157	MeV $cm^{-1}$
Nuclear collision length	23.12	cm
Nuclear interaction length	33.27	cm
Pion collision length	33.92	cm
Pion interaction length	46.04	cm
Radiation length	19.89	cm
Critical energy	88.08	MeV (for $e^+$ )
Molière radius	4.659	cm
Plasma energy $\hbar\omega_p$		
Muon critical energy		





# Choice of location: M5 line



# Fabrication and installation progress (1)

Polyethylene wedge

Boron Carbide wedge

80 mm

130 mm

New power supplies for downstream optical matching

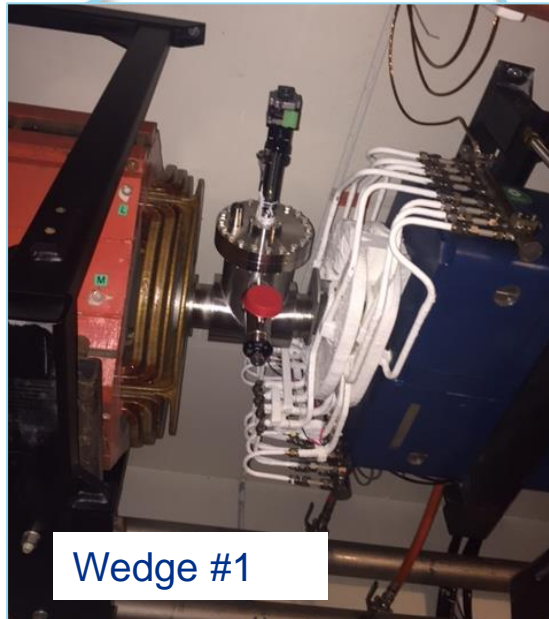
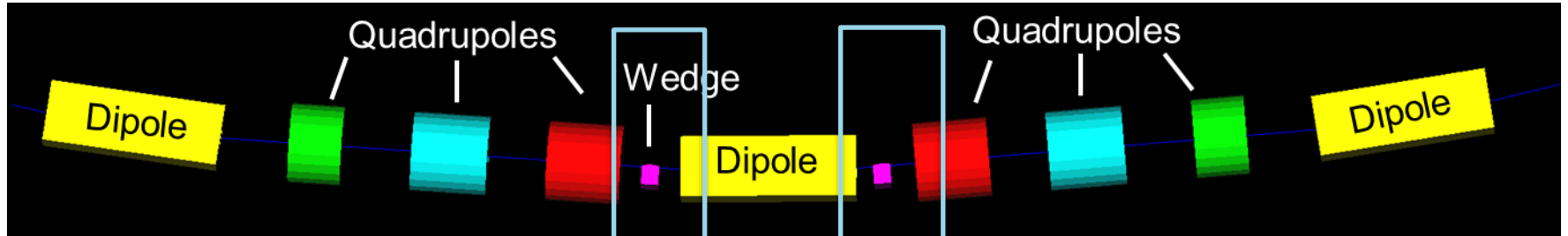
Wedge housing

Wedge insertion actuator with submillimeter precision

Motion-control tests

Design of complete mechanical assembly

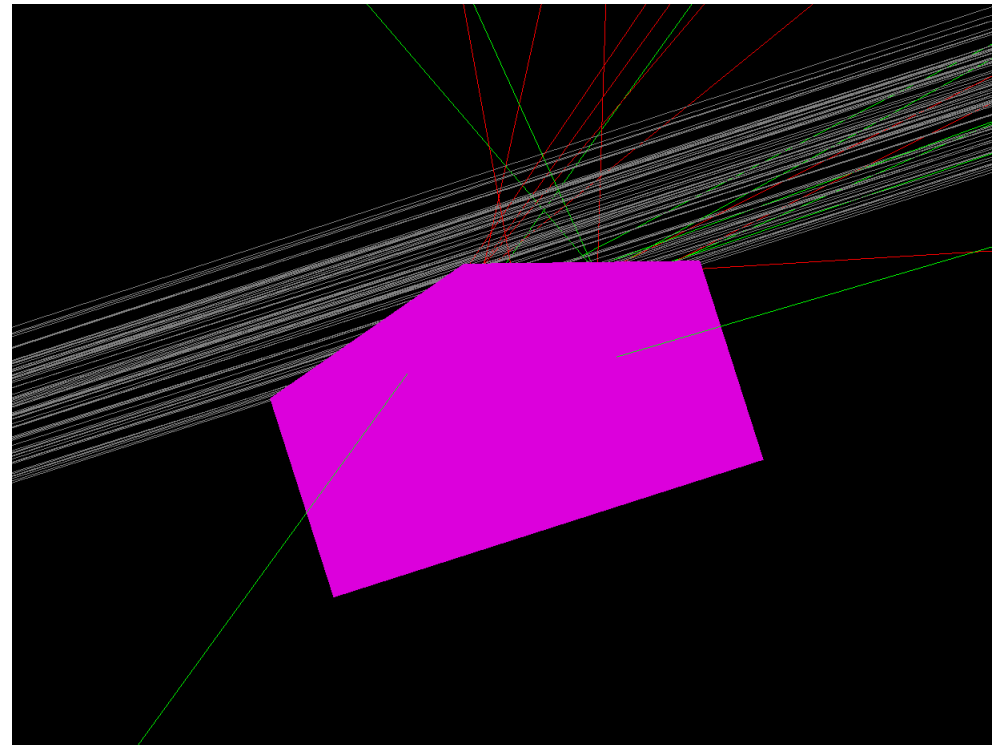
# Fabrication and installation progress (2)



# Simulated trajectories

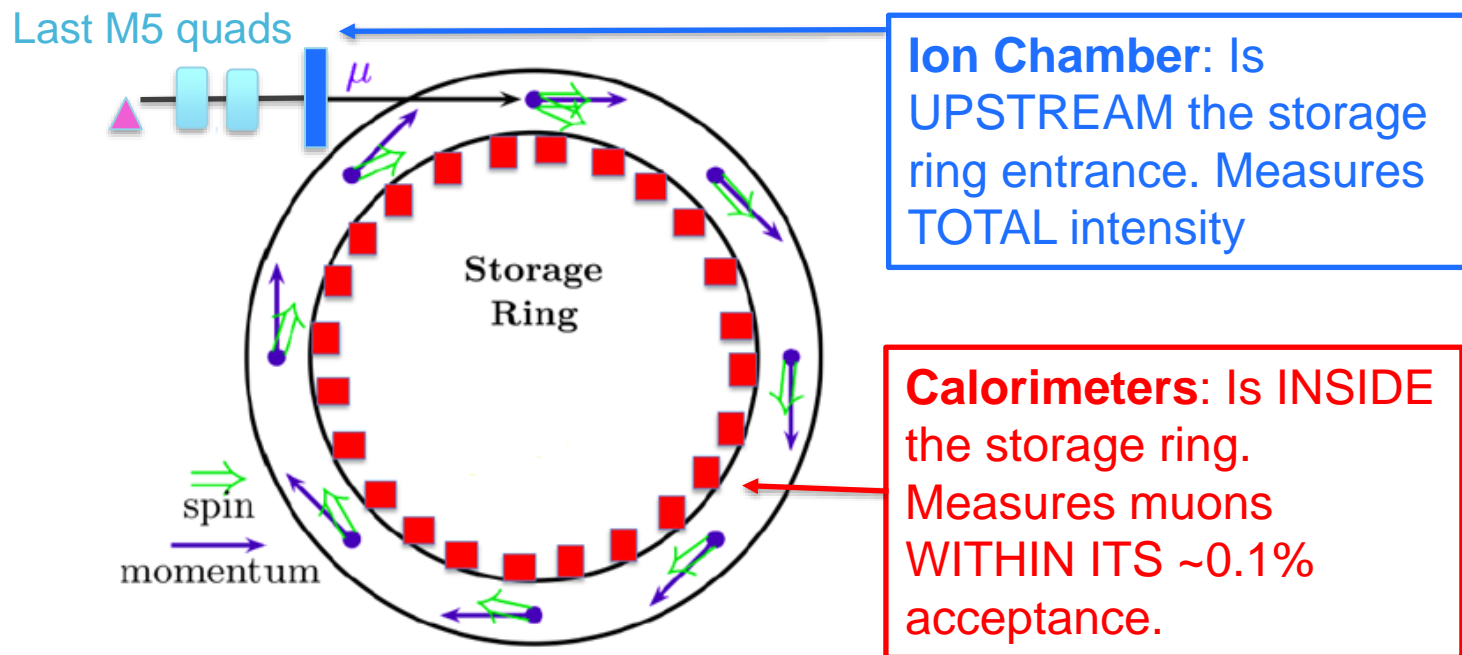
- Beam wedge covers roughly half of the beam
- The majority of beam-material interaction happens near the wedge apex

Parameter	Value at wedge
Dispersion, $D_x$	0.85 m
Beta, $\beta_x$	2.3 m
Beta, $\beta_y$	3.8 m
Emittance rms, $\varepsilon$	12.0 $\mu\text{m}$
Sigma, $\sigma_x$	10.0 mm



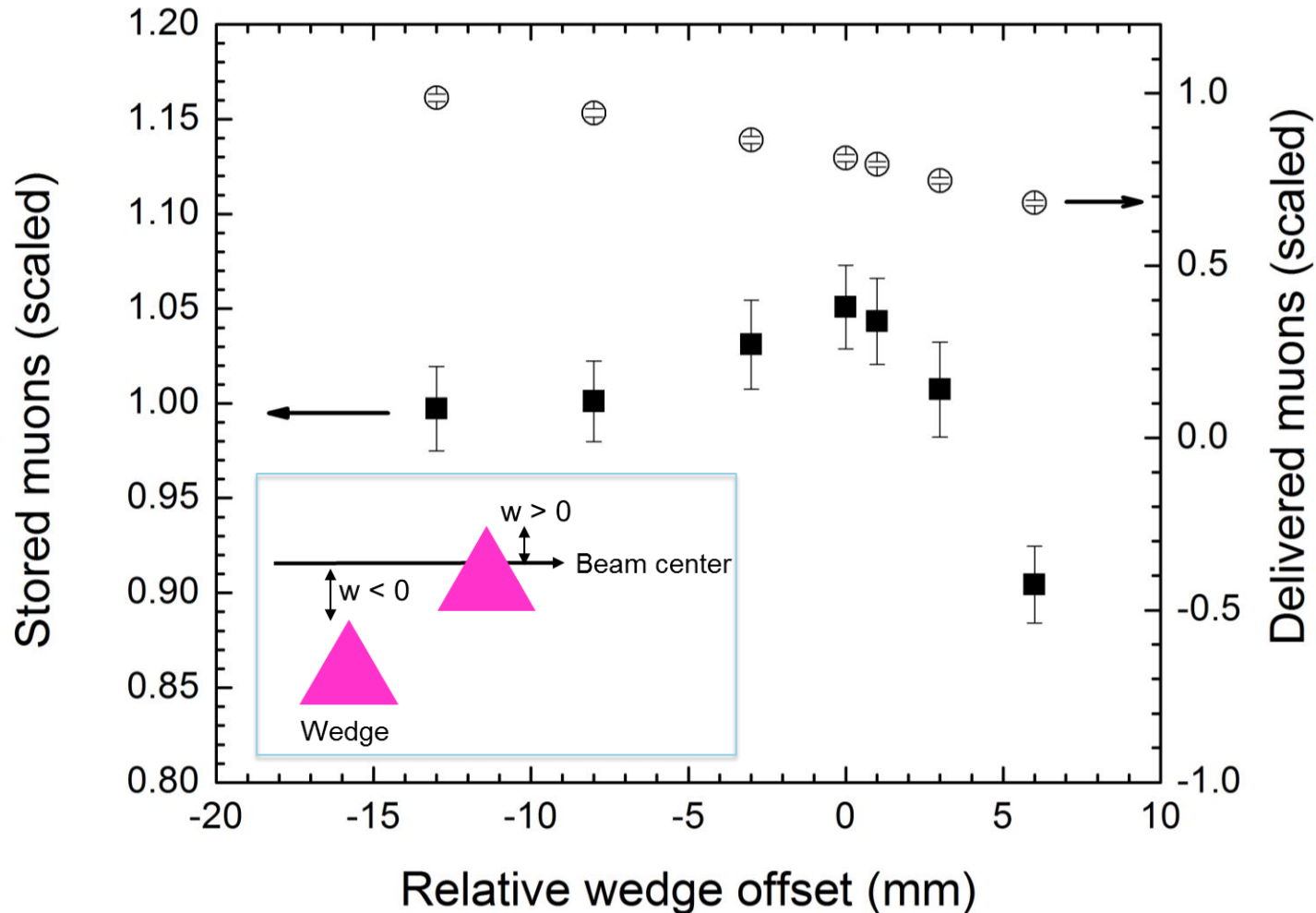
# Measuring Technique

- We measure beam intensity at two locations: (1) upstream of ring injection, and (2) inside the ring after thousand of turns
- Calorimeters measure only muons that fit within the ring's momentum acceptance. As a result this value provides a key parameter that governs the wedge performance.



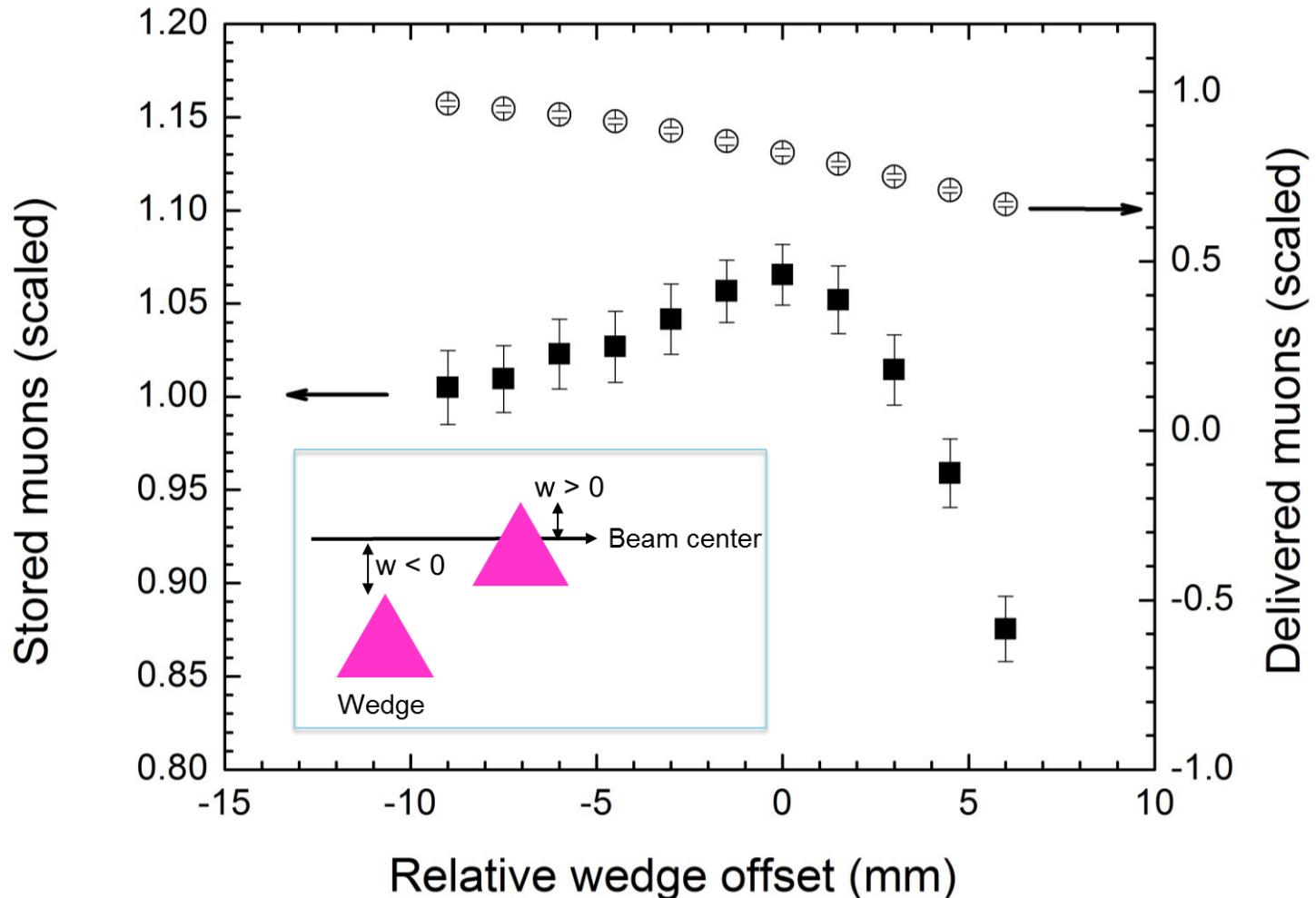
# Test with a Polyethylene wedge

- A polyethylene wedge provided a 5% gain in stored muons



# Test with a Boron Carbide wedge

- A boron carbide wedge provided a 7% gain in stored muons




# Conclusion


- The LDRD run for 3 years and finished in 2020
- Similar to MICE, demonstrated the emittance-exchange process i.e longitudinal cooling
- The novelty of our work is that it demonstrated direct applicability to an operational facility: Muon g-2 Experiment
- Showed an increase in storable muons by  $\sim 7\%$
- Showed numerically the potential to increase storable muons by 20% or more
  - Required significant change on optics/power supplies
  - Not possible given the time constraints of the experiment



# Muon g-2 cooling: Thanks to several students!




**Nick Amato (2019)**  
Master's Thesis, **NIU**  
(Syphers)  
Title: Improved momentum spread for precision experiments using wedges



**Lauren Carver (2019)**  
Fermilab Intern  
Title: Modeling a wedge absorber for the g-2 Experiment




**Jerzy Manczak (2018)**  
Fermilab Intern  
Title: Modeling a wedge absorber for the Mu2e Experiment



**Joe Bradley (2017)**  
Fermilab Intern  
Title: Material & geometry study of a wedge absorber for the g-2 Experiment



**Grace Roberts (2020)**  
Fermilab Intern  
Title: Optimizing injection for a wedge based Muon g-2 Experiment



**Ben Simons(2020)**  
**NIU** grad. student  
Title: Tuning beam optics for the Muon Campus


PHYSICAL REVIEW ACCELERATORS AND BEAMS 22, 053501 (2019)

Application of passive wedge absorbers for improving the performance of precision-science experiments

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Fermi National Accelerator Laboratory, Batavia, Illinois 60510, USA

Nuclear Inst. and Methods in Physics Research, A 962 (2020) 163704

Contents lists available at ScienceDirect

 Nuclear Inst. and Methods in Physics Research, A

journal homepage: [www.elsevier.com/locate/nima](http://www.elsevier.com/locate/nima)

Realistic modeling of a particle-matter-interaction system for controlling the momentum spread of muon beams

Lauren Carver<sup>a</sup>, Diktys Stratakis<sup>b,\*</sup>

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<sup>b</sup> Fermi National Accelerator Laboratory, Batavia, IL 60510, USA

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journal homepage: [www.elsevier.com/locate/nima](http://www.elsevier.com/locate/nima)

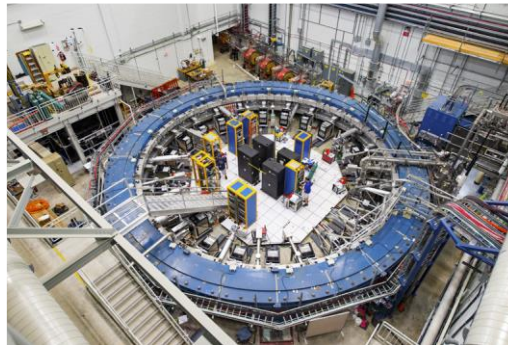
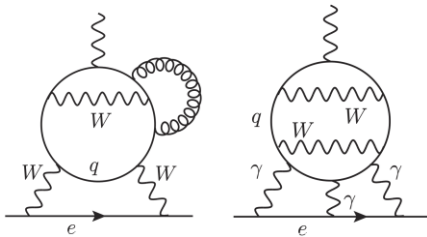
A parametric analysis for maximizing beam quality of muon-based storage ring experiments

Grace Roberts<sup>a</sup>, Diktys Stratakis<sup>b,\*</sup>

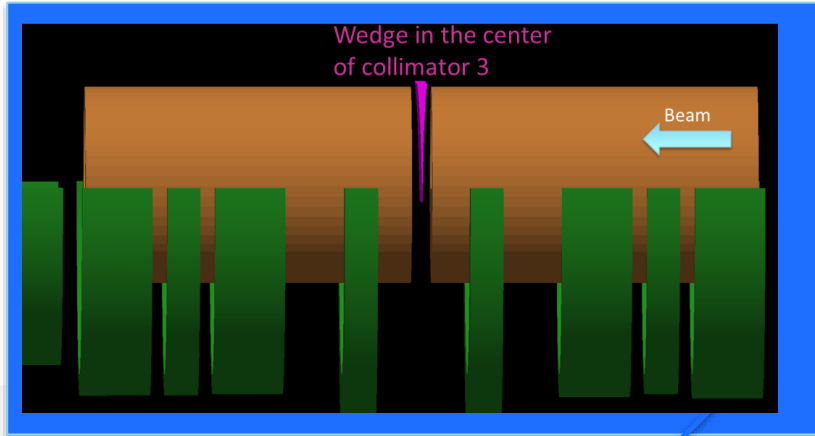
<sup>a</sup> Purdue University, Department of Physics, West Lafayette, IN 47906, USA  
<sup>b</sup> Fermi National Accelerator Laboratory, Batavia, IL 60510, USA

# Future work: EDM experiment

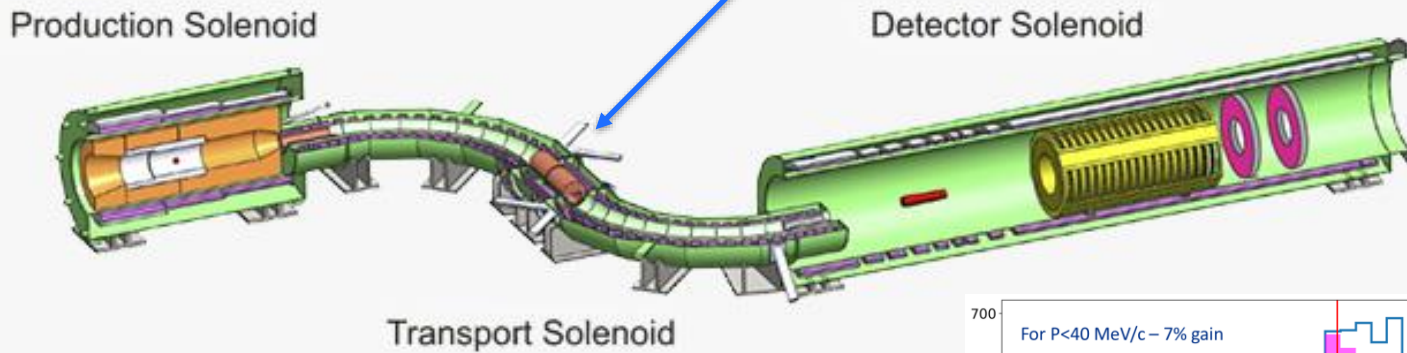
- There is considerable interest for an Electron Dipole Measurement (EDM) experiment at the Fermilab muon g-2 ring
- It will require the collection and transport of **300 MeV/c** muons along the Muon Campus
- Can open a path for wedge testing in a parameter regime that is closer to the actual cooling needed for a Muon Collider
- Simulations underway to estimate performance



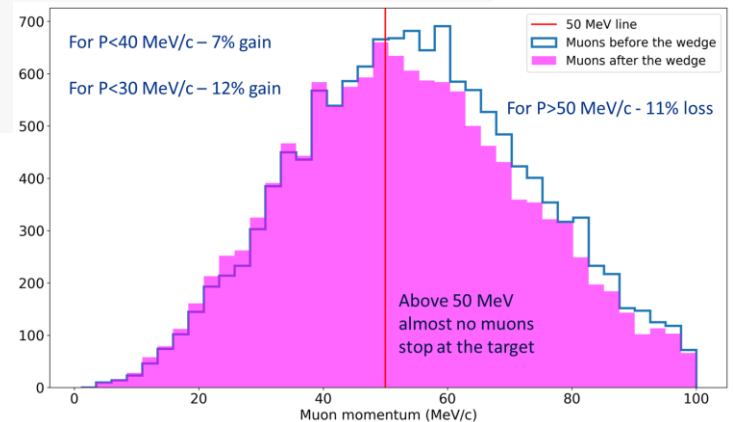
# Future work: Fermilab Mu2e-II Experiment



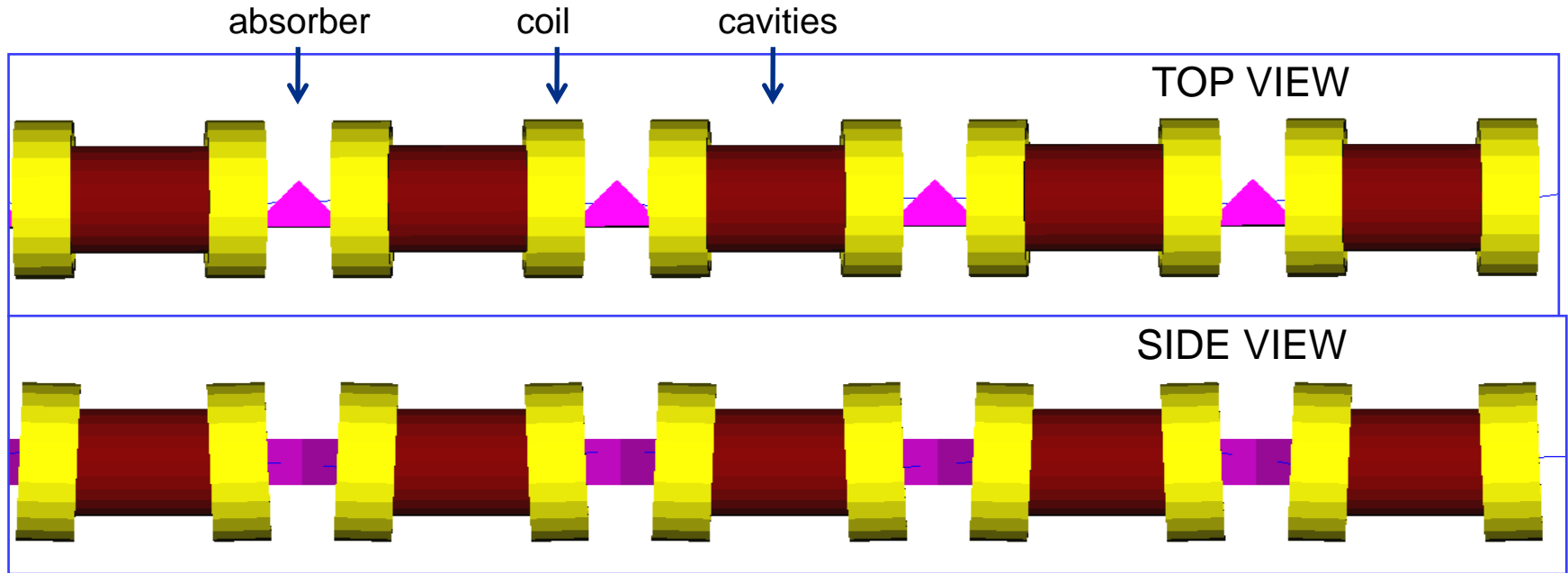
March 17, 2022  
Mu2e-II: Muon to electron conversion with PIP-II  
Contributed paper for Snowmass



- Goal is to increase muons in the 0-30 MeV/c range
- Concept works; its getting harder due to increased scattering



# Design: Rectilinear channel concept

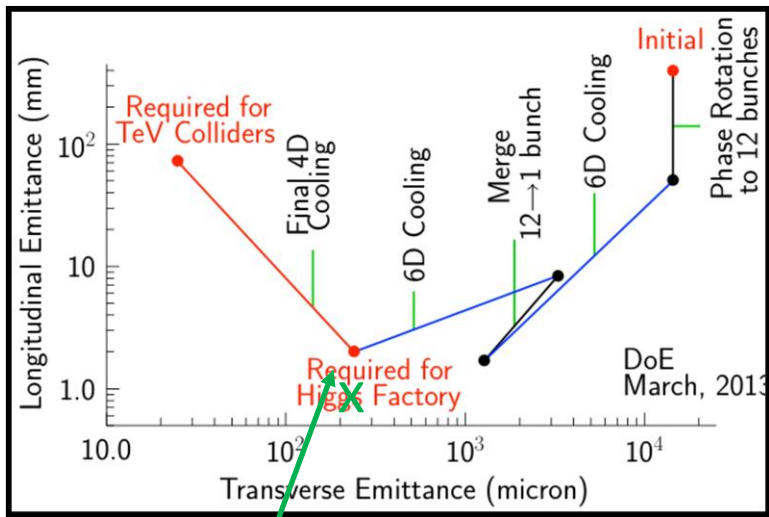


- Through the MAP program, we delivered 6D cooling designs in place with realistic assumptions
  - **Matched the desired performance goal**
  - Conservative limits on RF and magnet technology
  - Improvements expected with recent technology advancements

# Performance

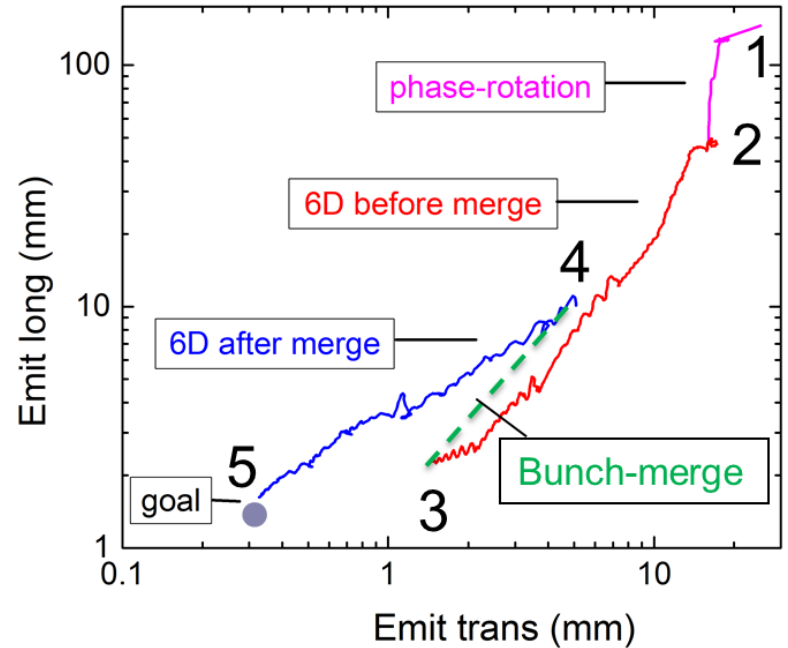
- Complete end-to-end simulation from the target (point 1)
- 6D emittance reduction by five orders of magnitude (point 5)
- Achieved emittances and transmissions specified by MAP
- Overall distance ~ 900 m

Baseline



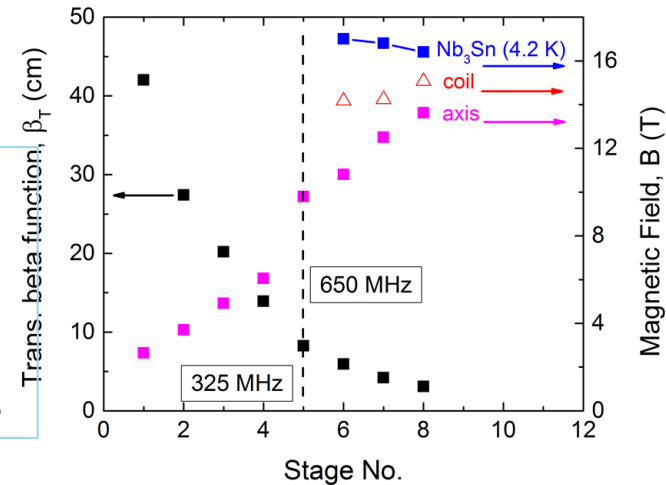
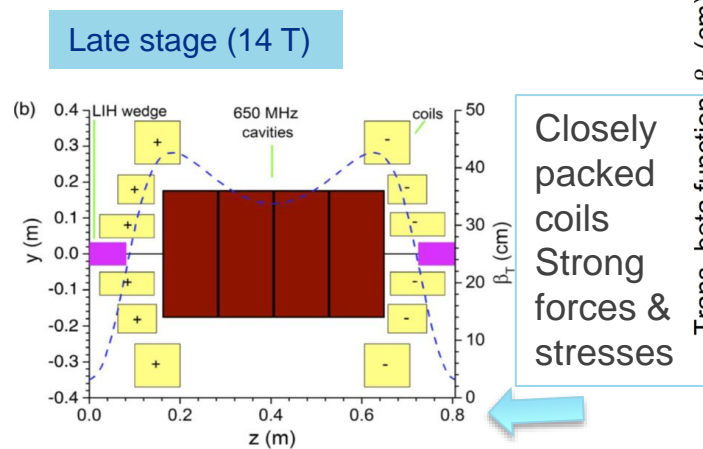
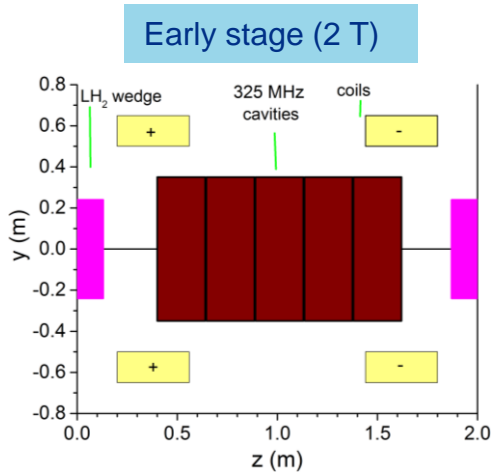
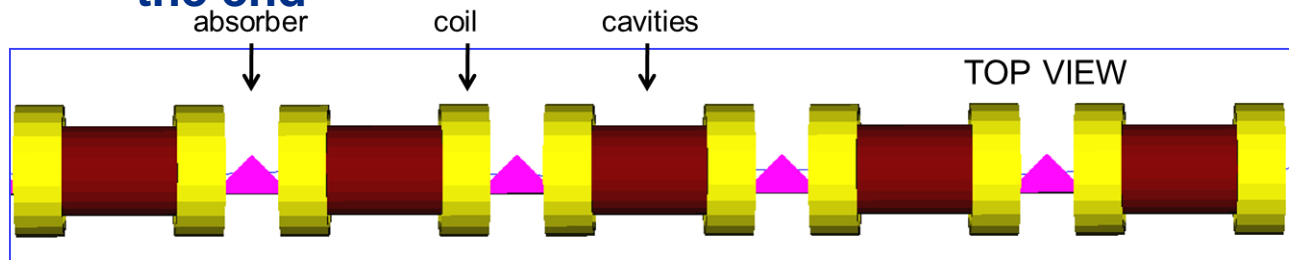
Emittances achieved

End-to-End to simulation



# Ionization cooling design for a MC – 6D cooling

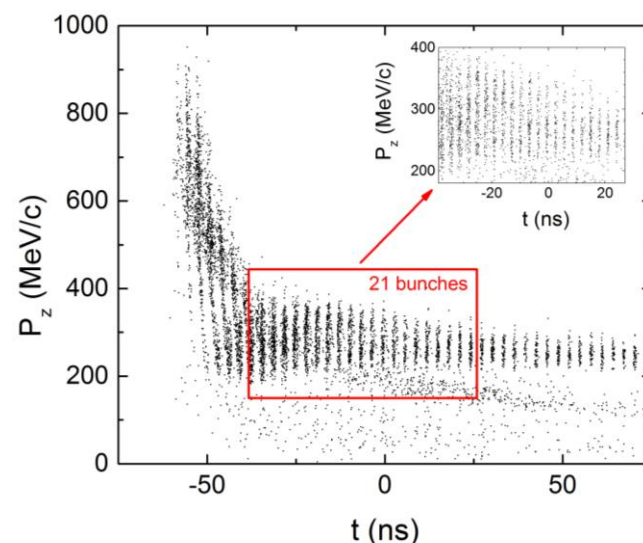
- Multiple stages that vary in magnetic strength & rf requirements
  - 8 stages: B-Field and rf gradient progressively larger from stage to stage
  - The cells are becoming more challenging in terms of engineering towards the end**



# Comments on performance

- Early stages had LH while later stages had LiH absorbers
- The starting distribution was the one delivered after phase-rotation in the front-end section
- The cooling “performance” was evaluated with the program ecalc9f based on “agreed” momentum cuts and acceptances
- Momentum cut we used to evaluate transmission was between 150 and 350 MeV/c

Stage	$\epsilon_T^{\text{sim}}$ [mm]	$\epsilon_L^{\text{sim}}$ [mm]	$P_z^{\text{sim}}$ [MeV/c]	$T$ [%]
Begin	17.00	46.00	255	
A1	6.28	14.48	238	70.6
A2	3.40	4.64	229	87.5
A3	2.07	2.60	220	88.8
A4	1.48	2.35	215	94.6
Begin	5.10	10.04	209	
B1	3.76	7.76	210	89.7
B2	2.40	6.10	208	90.6
B3	1.55	4.28	207	89.2
B4	1.10	3.40	207	89.7
B5	0.68	2.97	204	87.5
B6	0.50	2.16	202	88.0
B7	0.38	1.93	200	89.6
B8	0.28	1.57	200	89.0



# Cooling: Where are we now

- Strong participation of the MC community at Snowmass
- Best case scenario: Muon Collider activities could resume in the US after a positive outcome of P5 next year
- Under that scenario, for Summer 2023
  - Expect to have 1-2 interns to work on Muon cooling designs
- For FY24
  - Submit a proposal through Fermilab's LDRD program
  - PhD student support through the Fermilab-Joint University program?
  - DOE funding?



# Topics of interest

- Recall that cooling has significant impact on PD requirements
- Past designs were conservative in magnet and rf technology
  - Critical to understand the impact of a higher solenoidal and rf fields on the overall design. Will this improve performance?
- What are the limits of 6D cooling
  - Don Summers showed that with higher fields and more stages we can cool more with a rectilinear channel. Is this beneficial?
- Study critical processes such beam loading or beam-absorber interactions
  - What modifications are needed if this becomes a problem?
- Final cooling alternatives: Benefits of Neuffer's wedge cooler?
- Explore cooling demonstrator options in the US