



Istituto Nazionale di Fisica Nucleare



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Physics results with full sim and comparison with fast sim

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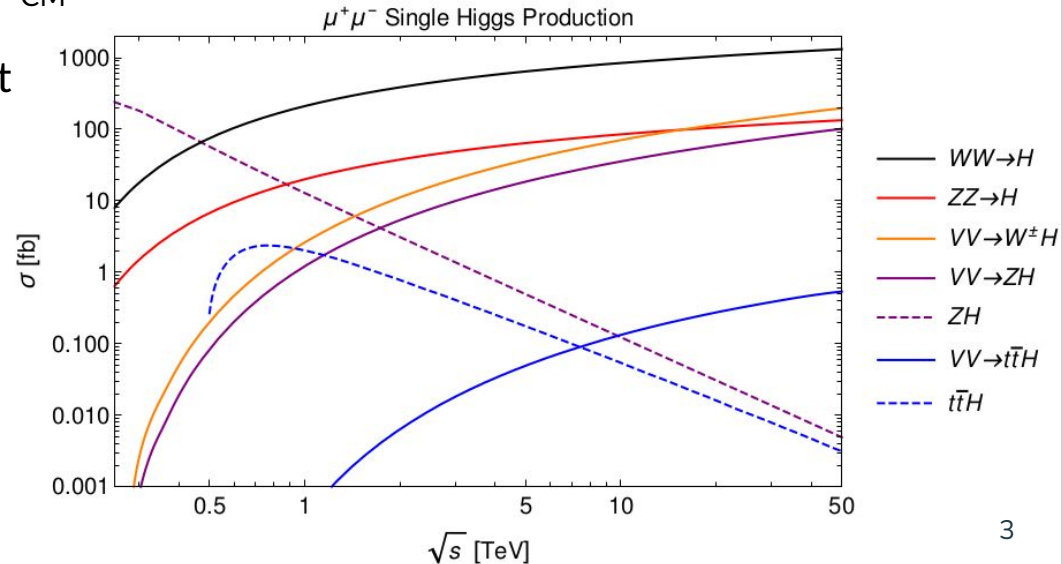
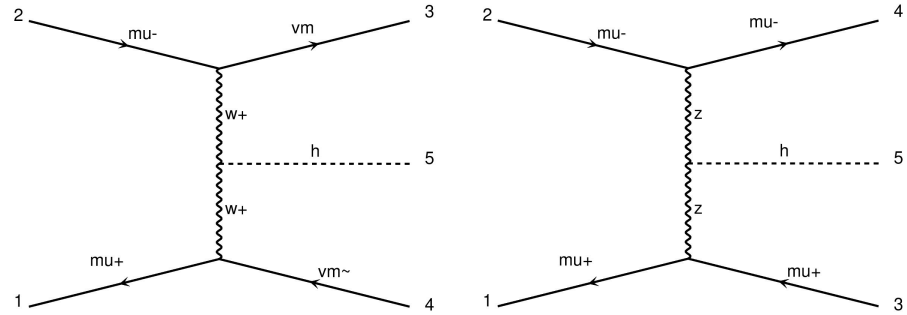
Outlook

- **1 ab⁻¹ @ 3 TeV Muon Collider** considered in this presentation
- Higgs physics results with full simulation compared with studies based on Delphes fast sim
- Full simulation studies include Beam Induced Background (BIB), unless otherwise specified
 - One BIB event superimposed on each physics event
 - BIB simulated for 1.5 TeV Muon Collider
 - Conservative approach: BIB is expected to be more forward at higher E_{CM}
 - 3 TeV BIB preliminary studies show that it's not worse than the 1.5 TeV one

Higgs production

Dominant Higgs production modes:

- WBF: $\mu\mu^- \rightarrow \nu\nu H$, ~ 500 fb
- ZBF: $\mu\mu^- \rightarrow \mu\mu H$, ~ 50 fb
- Both increases logarithmically with E_{CM}
- With ZBF, final state muons are forward, therefore difficult to detect
- In both full and fast sim studies both diagrams are considered



Full Simulation

3 TeV Muon Collider detector used for full sim studies

hadronic calorimeter

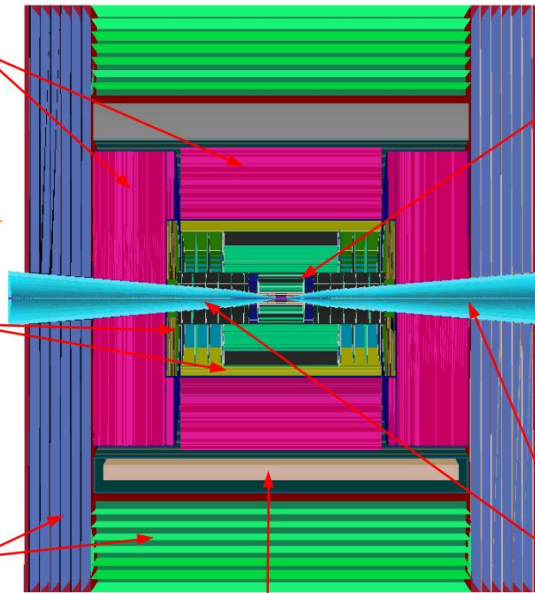
- ◆ 60 layers of 19-mm steel absorber + plastic scintillating tiles;
- ◆ 30x30 mm² cell size;
- ◆ 7.5 λ_I .

electromagnetic calorimeter

- ◆ 40 layers of 1.9-mm W absorber + silicon pad sensors;
- ◆ 5x5 mm² cell granularity;
- ◆ 22 $X_0 + 1 \lambda_I$.

muon detectors

- ◆ 7-barrel, 6-endcap RPC layers interleaved in the magnet's iron yoke;
- ◆ 30x30 mm² cell size.



superconducting solenoid (3.57T)

tracking system

- ◆ **Vertex Detector:**
 - double-sensor layers (4 barrel cylinders and 4+4 endcap disks);
 - 25x25 μm^2 pixel Si sensors.
- ◆ **Inner Tracker:**
 - 3 barrel layers and 7+7 endcap disks;
 - 50 μm x 1 mm macro-pixel Si sensors.
- ◆ **Outer Tracker:**
 - 3 barrel layers and 4+4 endcap disks;
 - 50 μm x 10 mm micro-strip Si sensors.

shielding nozzles

- ◆ Tungsten cones + borated polyethylene cladding.

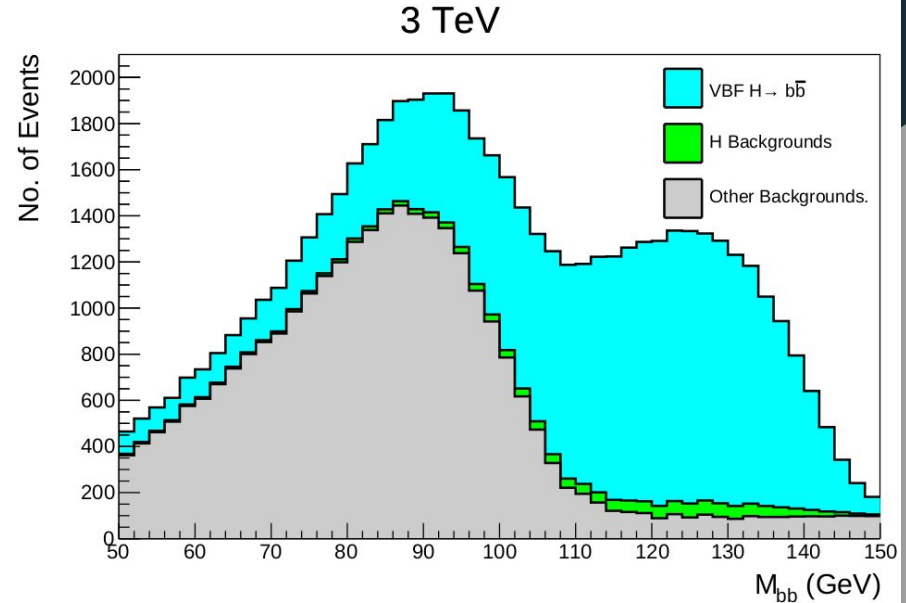
Fast Simulation

- Events generated with MG5+Pythia8, Delphes to model detector performance
https://indico.cern.ch/event/957299/contributions/4023467/attachments/2106044/3541874/delphes_card_mucol_mdi%20.pdf
- Jet p_T resolution 2% for $|\eta| < 0.76$ and 5% for $|\eta| > 0.76$
- Cut-off at $|\eta| = 2.5$ to simulate presence of nozzles
- b-tagging: 50% efficiency, flat in p_T and η
 - c-mistag: 0.07%-3%
 - light mistag: 0.02%-0.7%
- Muon efficiency close to 100%
- Photon efficiency $\sim 90\%$
- Cut based analysis, resolution estimated from event counts as $\frac{\Delta\sigma}{\sigma} = \frac{\sqrt{S+B}}{S}$
- See: *High precision Higgs from high energy muon colliders*, JHEP **08** (2022), 185

H->bb fast sim

- Part of the 2-body hadronic Higgs decay study
- Events with two b-tagged jets with $p_T > 40$ GeV and invariant mass $100 \text{ GeV} < m_H < 150 \text{ GeV}$
- Main background from VBF Z->jj

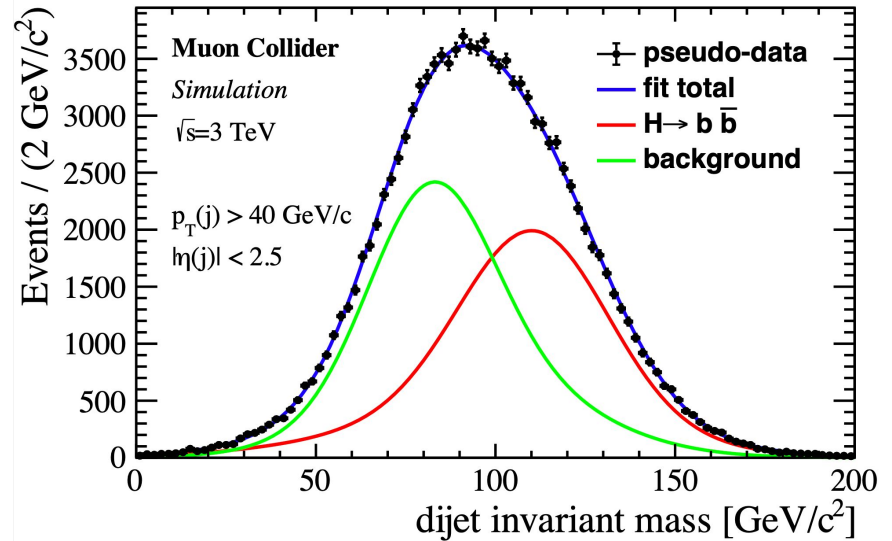
$$\frac{\Delta\sigma}{\sigma} = \frac{\sqrt{S+B}}{S} \longrightarrow 0.76\%$$



H->bb full sim

- Signal $\mu\mu \rightarrow (H \rightarrow b\bar{b})X$ and background $\mu\mu \rightarrow qqX$ ($q=b,c$) generated with Whizard+Pythia8. X is a pair of neutrinos or muons
- Required 2 jets with a secondary vertex each
- $S = 59\,500$, $B = 65\,400$ in 1 ab^{-1}
- Signal yield from template fit to pseudo-experiments using invariant mass
- Statistical relative uncertainty on

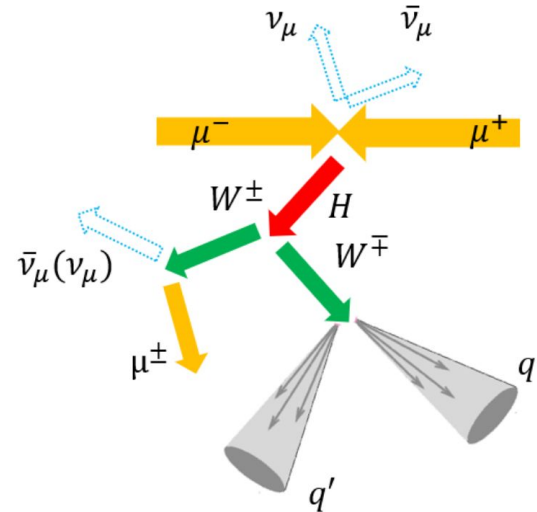
$$\sigma \times \text{BR} = 0.75\%$$



H \rightarrow WW* fast sim

- Semileptonic decay: full Higgs reconstruction not possible
- Events with 2 R=0.5 jets + 1 isolated lepton, all with $p_T > 20$ GeV
 - **Note:** electron and muon decays used together
- Dominant backgrounds:
 - On-shell diboson production
 - $\mu^+\mu^- \rightarrow \nu\nu\ell\ell jj$
 - $\mu^+\mu^- \rightarrow \ell\ell\nu\ell jj$
- $5 \text{ GeV} < m_{jj} < 90 \text{ GeV}$, $20 \text{ GeV} < m_{jjl} < 110 \text{ GeV}$
- $40 \text{ GeV} < E_{jj} < 700 \text{ GeV}$, $85 \text{ GeV} < E_{jjl} < 800 \text{ GeV}$

$$\frac{\Delta\sigma}{\sigma} = \frac{\sqrt{S+B}}{S} \longrightarrow 1.7\%$$

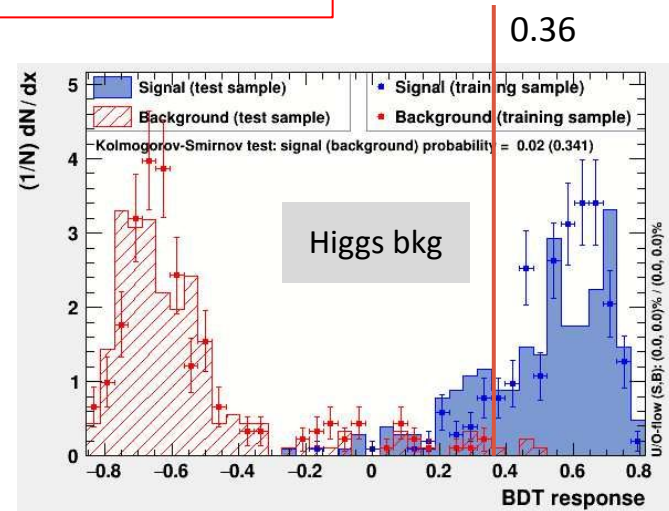
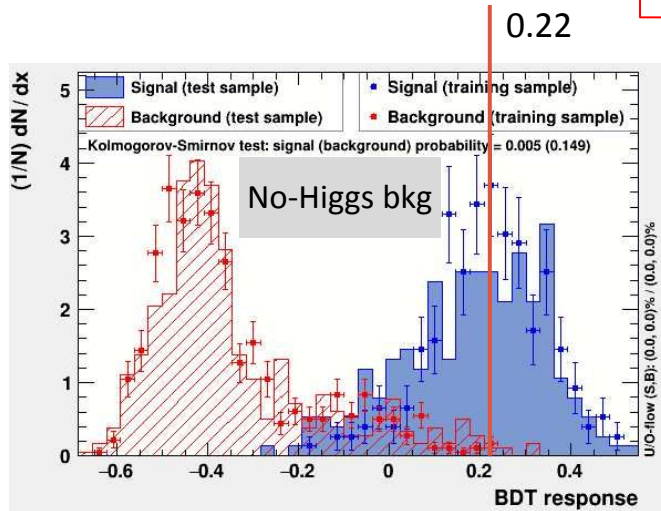


H → WW* full sim

- 1 Muon + 2 jets final state (no electron)
- Signal and backgrounds (with and without Higgs) simulated with Whizard+Pythia8
- Cuts on two BDTs to select signal vs backgrounds
- S=2 430, B=2 600 in 1 ab⁻¹

| Event | Expected Events |
|---|------------------|
| $\mu^+\mu^- \rightarrow H\nu\bar{\nu} \rightarrow WW^*\nu\bar{\nu} \rightarrow qq\mu\nu\bar{\nu}$ | 2430 ± 150 |
| $\mu^+\mu^- \rightarrow qq\mu\nu$ | 2600 ± 1300 |
| $\mu^+\mu^- \rightarrow qqll$ | < 100 C.L. = 68% |
| $\mu^+\mu^- \rightarrow qq\nu\nu$ | < 100 C.L. = 68% |
| $\mu^+\mu^- \rightarrow H \rightarrow WW^* \rightarrow qqqq$ | < 10 C.L. = 68% |
| $\mu^+\mu^- \rightarrow H \rightarrow bb$ | < 150 C.L. = 68% |
| $\mu^+\mu^- \rightarrow H \rightarrow \tau\tau$ | < 4 C.L. = 68% |

$$\frac{\Delta\sigma}{\sigma} = \frac{\sqrt{S+B}}{S} \longrightarrow 2.9\%$$



H->ZZ* fast sim

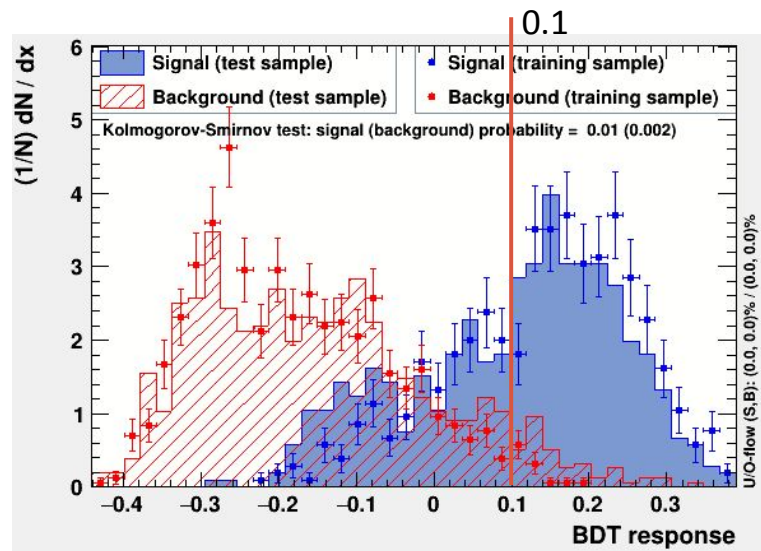
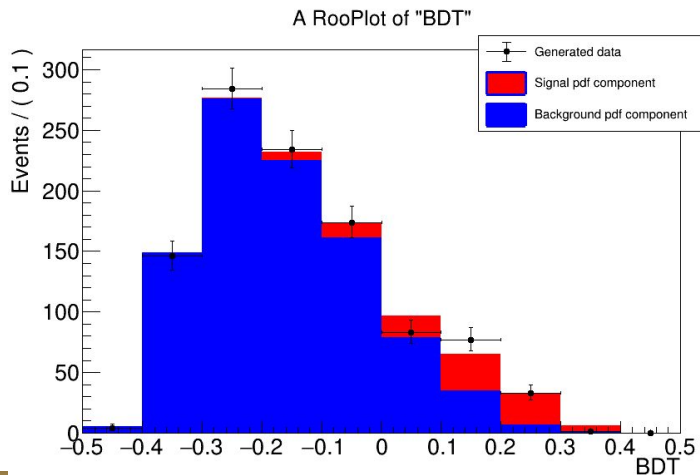
- Events with 2 leptons and 2 R=0.5 jets, all with $p_T > 20$ GeV
 - **Note:** electron and muon decays used together
- The pair of either leptons or jets with invariant mass closer to m_Z is assigned to the on-shell Z
- Main backgrounds:
 - $\mu^+\mu^- \rightarrow \nu\nu jj$
 - $\mu^+\mu^- \rightarrow \nu l jj$
- $20 \text{ GeV} < m_Z < 100 \text{ GeV}$ for on-shell Z
- $5 \text{ GeV} < m_{Z^*} < 60 \text{ GeV}$ for off-shell Z
- $100 \text{ GeV} < m_H < 130 \text{ GeV}$ if lepton pair reconstruct the on-shell Z,
 $80 \text{ GeV} < m_H < 135 \text{ GeV}$ otherwise

| | 4j | 2j2l | 4l |
|---|------|------|----|
| $\mu^+\mu^- \rightarrow \nu_\mu\bar{\nu}_\mu H; H \rightarrow ZZ^* \rightarrow X$ | 124 | 103 | 5 |
| $\mu^+\mu^- \rightarrow \mu^+\mu^- H; H \rightarrow ZZ^* \rightarrow X$ | 3 | 9 | 0 |
| Backgrounds | 6700 | 50 | 0 |

$$\frac{\Delta\sigma}{\sigma} = \frac{\sqrt{S+B}}{S} \longrightarrow 11\%$$

H->ZZ* full sim

- 2 muons + 2 jets final state
- Signal generated with MG5+Pythia8
- Inclusive $\mu^+\mu^- \rightarrow \nu\nu \mu^+\mu^- jj$ background (excluding signal) generated with Whizard+Pythia8
- BDT used to select signal vs background
- Resolution obtained with cut-based approach and with fit of BDTs, giving the same result



$$\frac{\Delta\sigma}{\sigma} = \frac{\sqrt{S+B}}{S} \longrightarrow 17\%$$

H \rightarrow $\mu^+ \mu^-$ fast sim

- Events with two muons with opposite charge and $p_T > 20$ GeV
- Two main backgrounds: $\mu^+ \mu^- \rightarrow \mu^+ \mu^- \nu \bar{\nu}$ and $\mu^+ \mu^- \rightarrow \mu^+ \mu^- \mu^+ \mu^-$
- $124 < m_H < 126$ GeV

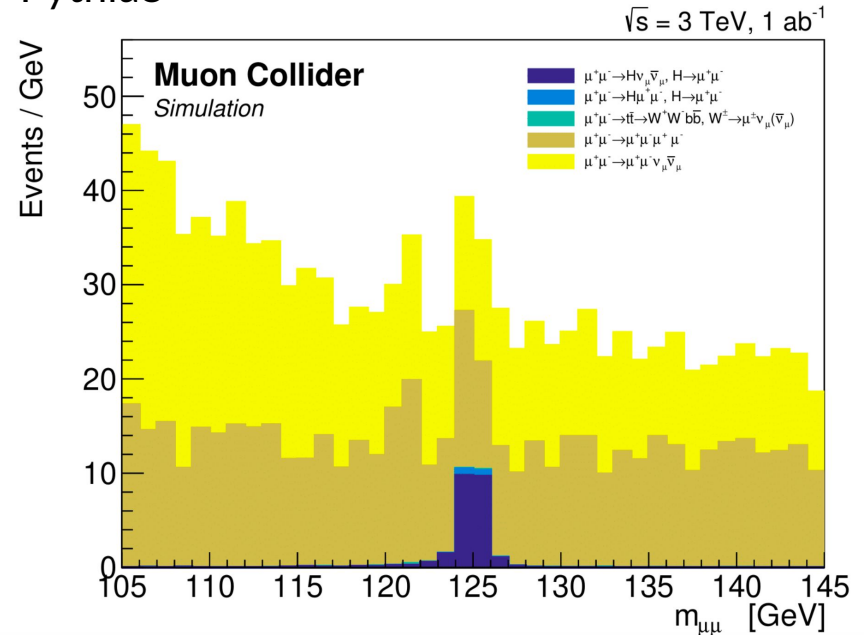
| | σ (fb) | ϵ (%) | N |
|--|---------------|----------------|-----|
| $\mu^+ \mu^- \rightarrow \nu_\mu \bar{\nu}_\mu H; H \rightarrow \mu^+ \mu^-$ | 0.11 | 52 | 57 |
| $\mu^+ \mu^- \rightarrow \mu^+ \mu^- H; H \rightarrow \mu^+ \mu^-$ | 0.011 | 43 | 5 |
| $\mu^+ \mu^- \rightarrow \nu_\mu \bar{\nu}_\mu \mu^+ \mu^-$ | 67.2 | 0.30 | 198 |
| $\mu^+ \mu^- \rightarrow \mu^+ \mu^- \mu^+ \mu^-$ | 211 | 0.16 | 345 |

$$\frac{\Delta\sigma}{\sigma} = \frac{\sqrt{S+B}}{S} \longrightarrow 40\%$$

H \rightarrow $\mu^+ \mu^-$ full sim

- Signal and backgrounds generated with MG5+Pythia8
- BIB not used (low impact in muon chambers)
- Selection cuts on two BDTs trained to discriminate signal from the backgrounds
- Uncertainty on signal yield obtained from unbinned maximum likelihood fit to dimuon invariant mass

| Process | Expected events with $105 < m_{\mu\mu} < 145 \text{ GeV}$ 1 ab^{-1} |
|---|---|
| [1] $\mu^+ \mu^- \rightarrow H \nu_{\mu} \bar{\nu}_{\mu}$, $H \rightarrow \mu^+ \mu^-$ | 24.2 |
| [1] $\mu^+ \mu^- \rightarrow H \mu^+ \mu^-$, $H \rightarrow \mu^+ \mu^-$ | 1.6 |
| $\mu^+ \mu^- \rightarrow \mu^+ \mu^- \nu \bar{\nu}_{\mu}$ | 636.5 |
| $\mu^+ \mu^- \rightarrow \mu^+ \mu^- \mu^+ \mu^-$ | 476.4 |
| [t \bar{t}] $\mu^+ \mu^- \rightarrow t \bar{t} \rightarrow W^+ W^- b \bar{b}$, $W^{\pm} \rightarrow \mu^{\pm} \nu_{\mu} (\bar{\nu}_{\mu})$ | 1.1 |

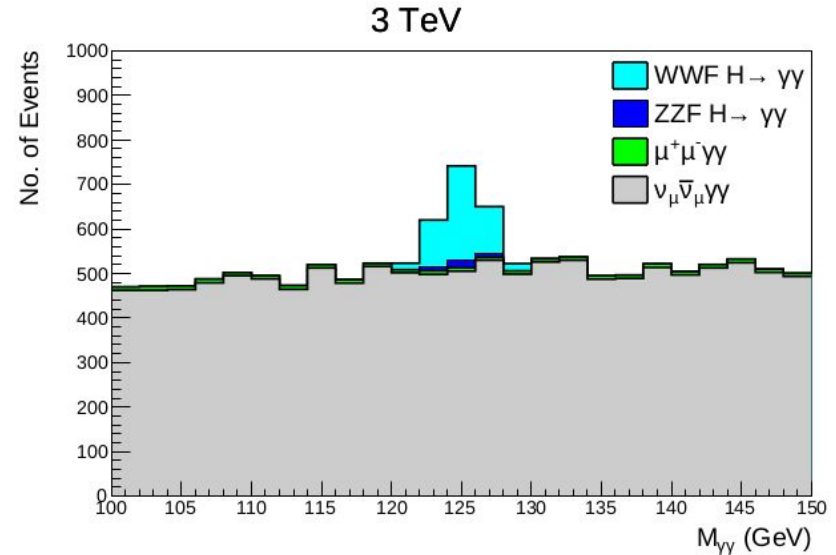


Relative uncertainty on $\sigma = 38\%$

H- $\rightarrow\gamma\gamma$ fast sim

- Events with at least two isolated photons, no jets and no leptons
- Selected two photons with largest p_T , requiring $p_T > 40$ GeV
- $122 < m_H < 128$ GeV

| | σ (fb) | ϵ (%) | N |
|---|---------------|----------------|-----|
| $\mu^+\mu^- \rightarrow \nu_\mu\bar{\nu}_\mu H; H \rightarrow \gamma\gamma$ | 1.14 | 37 | 419 |
| $\mu^+\mu^- \rightarrow \mu^+\mu^- H; H \rightarrow \gamma\gamma$ | 0.12 | 29 | 34 |
| $\mu^+\mu^- \rightarrow \nu_\mu\bar{\nu}_\mu\gamma\gamma$ | 198 | 0.16 | 311 |
| $\mu^+\mu^- \rightarrow \mu^+\mu^-\gamma\gamma$ | 297 | 0.001 | 3 |



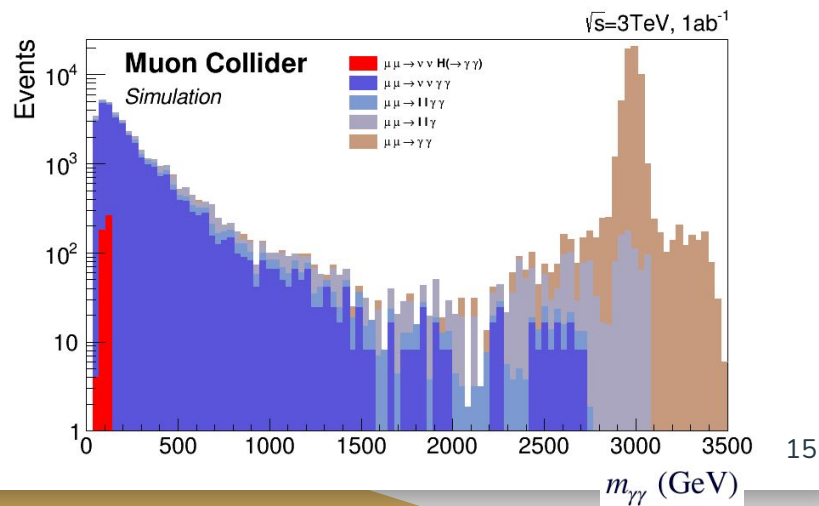
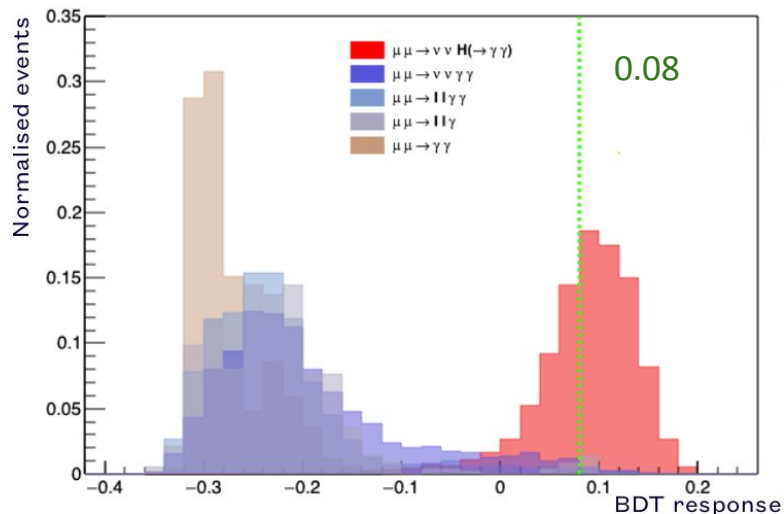
$$\frac{\Delta\sigma}{\sigma} = \frac{\sqrt{S+B}}{S} \longrightarrow 6.1\%$$

H $\rightarrow\gamma\gamma$ full sim

- Signal and backgrounds generated with MG5+Pythia8
- **Preliminary result: No BIB at the moment** and some minor bkg still missing
- Used a BDT to perform signal vs. background separation
- Cut on BDT output to maximize $S/\sqrt{(S+B)}$

| Process | σ (fb) | Events |
|--|---------------------|--------|
| $\mu\mu \rightarrow H\nu\nu, H \rightarrow \gamma\gamma$ | 0.9025 ± 0.0026 | 707 |
| $\mu\mu \rightarrow \nu\nu\gamma\gamma$ | 81.98 ± 0.27 | 30168 |
| $\mu\mu \rightarrow ll\gamma\gamma$ | 4.419 ± 0.016 | 2678 |
| $\mu\mu \rightarrow ll\gamma$ | 159.0 ± 0.6 | 4738 |
| $\mu\mu \rightarrow \gamma\gamma$ | 60.15 ± 0.03 | 59933 |

$$\frac{\Delta\sigma}{\sigma} = \frac{\sqrt{S+B}}{S} \longrightarrow \mathbf{8.9\%}$$



Trilinear coupling

- HH->4b, EFT approach, no background considered
- Acceptance cuts:

$$p_T(b) > 30 \text{ GeV}, \quad 10^\circ < \theta_b < 170^\circ, \quad \Delta R_{bb} > 0.4$$

- The four most energetic jets in the event are paired to minimize

$$(m_{j_1 j_2} - m_H)^2 + (m_{j_3 j_4} - m_H)^2$$

- Other requirements:

$$|m_{jj} - m_H| < 15 \text{ GeV}$$

$$M_{\text{recoil}} = \sqrt{(p_{\mu^+} + p_{\mu^-} - p_{H_1} - p_{H_2})^2} > 200 \text{ GeV}$$

- λ_3 obtained from likelihood fit in bins of m_{HH}

$$m_{HH} = [0, 350, 450, 550, 650, 750, 950, 1350, 5000] \text{ GeV}$$

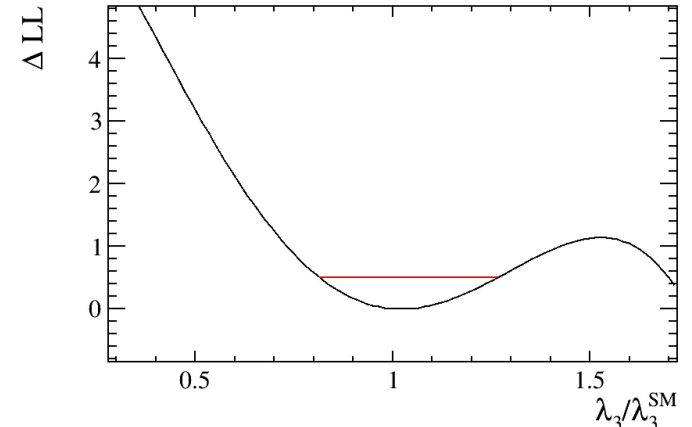
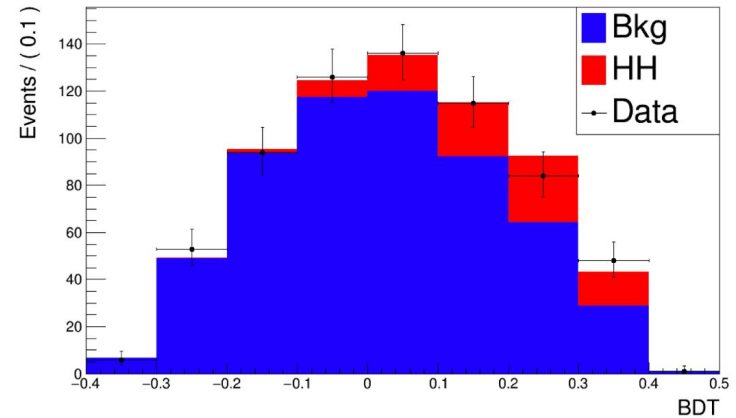
95% CL confidence interval

| | |
|-------------------------------------|-----|
| \sqrt{s} (TeV) | 3 |
| benchmark lumi (ab^{-1}) | 1 |
| $(\Delta\lambda_3)_{\text{in}}$ | 25% |

Electroweak couplings of the Higgs boson at a multi-TeV muon collider, Phys.Rev.D 103 (2021) 1, 013002

HH->bb bb and trilinear coupling

- Signal and backgrounds (H+bb and 4b) generated with Whizard+Pythia8
- Events with 4 jets, at least 2 must contain a secondary vertex
 - $S = 50, B = 432$ in 1 ab^{-1}
- BDT trained for sig-vs-bkg discrimination, fit on BDT output to find resolution
 - $\Delta\sigma/\sigma$ of **30%** is found
- Two MLPs are used: HH vs 4b and trilinear vs HH
- Simulated events with different λ_3 hypothesis, resolution on λ_3 obtained from a likelihood scan
 - **Stat. uncertainty of ~20% @ 68% CL** is found
 - CLIC: [-8%, 11%] @ 68% CL with 2.5 ab^{-1} @ $1.4 \text{ TeV} + 5 \text{ ab}^{-1}$ @ 3 TeV



Higgs couplings from full sim

- The measurement of Higgs width Γ_H is the key that allows to determine Higgs couplings from previous measurements of $\sigma \times BR$

$$\sigma(\mu^+ \mu^- \rightarrow H \nu_\mu \bar{\nu}_\mu) \times BR(H \rightarrow xx) \propto g_{HWW}^2 g_{Hxx}^2 / \Gamma_H$$

- A study for Γ_H with full simulation is ongoing
- Previous measurements combined to extract couplings assuming $\Gamma_H = \Gamma_H^{SM}$
- Results compared with CLIC

[Eur. Phys. J. C 77, 475 (2017)]

- CLIC fitted also Γ_H
- CLIC used multiple energy stages and larger integrated luminosity
- CLIC: 25 years program
- Muon Collider: 5 years 3 TeV stage

| | Muon Collider 1 ab ⁻¹ @ 3 TeV | CLIC 0.5 ab ⁻¹ @ 350 GeV + 1.5 ab ⁻¹ @ 1.4 TeV + 2 ab ⁻¹ @ 3 TeV |
|---------------------|---|--|
| Γ_H | SM | 3.5% |
| g_{HZZ} | 8.2% | 0.8% |
| g_{HWW} | 0.9% | 0.9% |
| g_{Hbb} | 0.8% | 0.9% |
| $g_{H\mu\mu}$ | 19% | 7.8% |
| $g_{H\gamma\gamma}$ | 4.5% | 3.2% |

Higgs couplings from fast sim

- Similar fit to couplings, but from results of fast simulation
- kappa-0 framework: Higgs width excluded from fit of couplings

$$\mu_i = \frac{\sigma_i \cdot \text{BR}_f}{\sigma_i^{\text{SM}} \cdot \text{BR}_f^{\text{SM}}} = \frac{\kappa_i^2 \kappa_f^2}{\kappa_H^2}, \quad \kappa_H = \sum_f \frac{\kappa_f^2 \Gamma_f^{\text{SM}}}{\Gamma_H^{\text{SM}}}$$

- Currently a fast sim study of Γ_H with only a high energy (multi-TeV) muon collider has not been done yet

| Fast sim | | Full sim | |
|-----------------|------|---------------------|------|
| κ_W | 0.55 | g_{HZZ} | 8.2% |
| κ_Z | 5.1 | g_{HWW} | 0.9% |
| κ_γ | 3.2 | g_{Hbb} | 0.8% |
| κ_b | 0.97 | $g_{H\mu\mu}$ | 19% |
| κ_μ | 20 | $g_{H\gamma\gamma}$ | 4.5% |

Results overview

| | | Full sim | Fast sim |
|---------------------------|---------------------|----------|--------------------------|
| Cross sections resolution | → H->WW | 2.9% | H->WW 1.7% |
| | H->ZZ | 17% | H->ZZ 11% |
| | H->bb | 0.75% | H->bb 0.76% |
| | H-> $\mu\mu$ | 38% | H-> $\mu\mu$ 40% |
| | H-> $\gamma\gamma$ | 8.9% | H-> $\gamma\gamma$ 6.1% |
| | HH->4b | 30% | |
| Couplings resolution | → g_{HWW} | 0.9% | g_{HWW} 0.55% |
| | g_{HZZ} | 8.2% | g_{HZZ} 5.1% |
| | g_{Hbb} | 0.8% | g_{Hbb} 0.97% |
| | $g_{H\mu\mu}$ | 19% | $g_{H\mu\mu}$ 20% |
| | $g_{H\gamma\gamma}$ | 4.5% | $g_{H\gamma\gamma}$ 3.2% |
| | λ_3 | 20% | λ_3 (95% CL) 25% |

Next steps

- Indirect measurement of Higgs width from measurement of off-shell $H \rightarrow ZZ$ and $H \rightarrow WW$
- The use of the off-shell signal alone allows to disentangle the degeneracy between couplings and width
- Approach:
 - Simulate background + off-shell Higgs in the high invariant mass region with different hypothesis of g_{HZZ} and g_{HWW}
 - Determine resolution on off-shell couplings, in both channels, from a **likelihood scan**
 - Resolution on Higgs width can be obtained later from Δg_{HZZ} and Δg_{HWW}

Summary

- Analyzed results for 5 Higgs decay channels, comparing full sim and fast sim
- Similar results in the two cases
 - Better resolution in $H \rightarrow ZZ$ and $H \rightarrow WW$ with fast sim, also because both electronic and muonic decay channels were used (unlike full sim)
- Determined resolutions on Higgs couplings, assuming for the moment $\Gamma_H = \Gamma_H^{\text{SM}}$
- Presented also measurements of $HH \rightarrow 4b$ and trilinear coupling
- Need for a measurement of Γ_H with off-shell Higgs decays to vector bosons
- Only some Higgs decay channels studied up to now \rightarrow add further channels (e.g. $H \rightarrow \tau\tau$)

Fast sim performance

