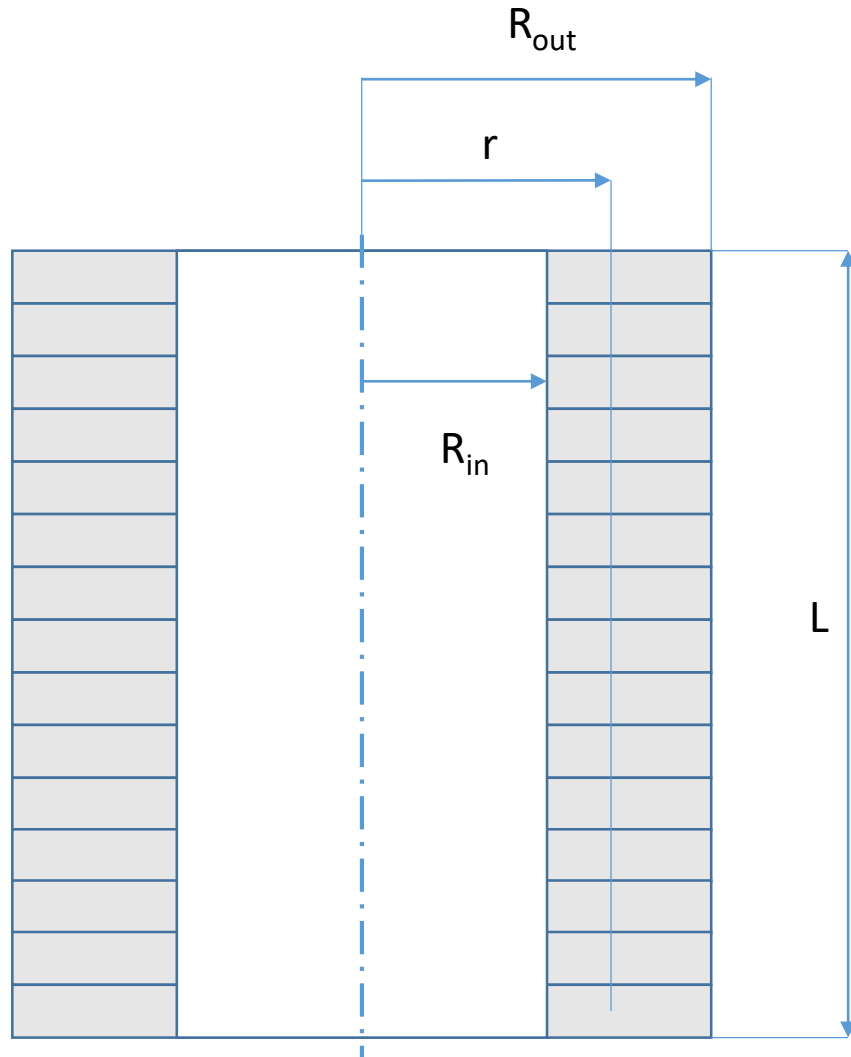


For Discussions on Maximum Field of HTS Solenoid

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For very long solenoid with constant current density J



Magnetic Flux Density is:

$$B_{\text{bore}} = \mu_0 \cdot J \cdot (R_{\text{out}} - R_{\text{in}}), \quad r < R_{\text{in}}$$

$$B(r) = \mu_0 \cdot J \cdot (R_{\text{out}} - r), \quad R_{\text{in}} < r < R_{\text{out}}$$

JBr stress may be calculated

$$\sigma = J \cdot B(r) \cdot r = \mu_0 \cdot J^2 \cdot (R_{\text{out}} - r) \cdot r$$

Its maximum found

$$\text{If } R_{\text{in}} < R_{\text{out}} / 2 \quad \sigma_{\text{max}} \text{ is at } r = R_{\text{out}} / 2 \quad \sigma_{\text{max}} = \mu_0 \cdot J^2 \cdot (R_{\text{out}} / 2)^2$$

And limit of current density defined

$$J_{\text{max}} = 2 / R_{\text{out}} \cdot \sqrt{\sigma_{\text{max}} / \mu_0}$$

For smallest possible solenoid with no bore ($R_{in}=0$) maximum field is

$$B_{\max} = 2 \cdot \sqrt{\sigma_{\max} \cdot \mu_0}$$

$$B_{\text{bore}} = \mu_0 \cdot J \cdot (R_{\text{out}} - R_{\text{in}}) = \mu_0 \cdot J \cdot R_{\text{out}}$$

$$J_{\max} = 2/R_{\text{out}} \cdot \sqrt{\sigma_{\max}/\mu_0}$$

Assuming that stress level of 600 Mpa is not degrading HTS

$$B_{\max} \approx 55 \text{ T}$$

But is such stress level achievable in the **real** coil package ????????

Some numbers to get an idea of magnet dimensions and material budget:

- inner radius $R_{in} = 26$ mm
- tape thickness $t = 0.05$ mm
- tape width $w = 4$ mm
- solenoid length $L = 500$ mm

$$R_{out} = R_{in} / (1 - B_0 / B_{max})$$

$$J_{max} = 2 / R_{out} \cdot \sqrt{\sigma_{max} / \mu_0}$$

Magnetic Field (T)	Coil Thickness (mm)	Current (A)	Stored Energy (MJ)	Tape Length (km)
27.5	26	168	1.1	16
30	31	153	1.4	21
35	46	122	2.5	35
40	70	91	4.7	67
45	118	61	10.4	157
50	264	30	35.7	655

What to choose !? Let's see presentation of Bernardo.