



ALMA MATER STUDIORUM  
UNIVERSITÀ DI BOLOGNA

# Resistive magnets design studies

Marco Breschi<sup>1</sup>, Rebecca Miceli<sup>1</sup>, Pier Luigi Ribani<sup>1</sup>  
Fulvio Boattini<sup>2</sup>, Luca Bottura<sup>2</sup>

<sup>1</sup>Alma Mater Studiorum – Università di Bologna, Italy

<sup>2</sup>CERN, Geneva, Switzerland

**Muon Collider Collaboration Annual Meeting**

CERN, Geneva, October 12<sup>th</sup> 2022

# Outline

- Resistive dipole magnets specifications
- Analysis methodology
- Results of the three analyzed magnet configurations
  - Windowframe magnet
  - H-type magnet
  - 'Hourglass' magnet from the US study
- Comparison of the three configurations
- Summary and perspectives



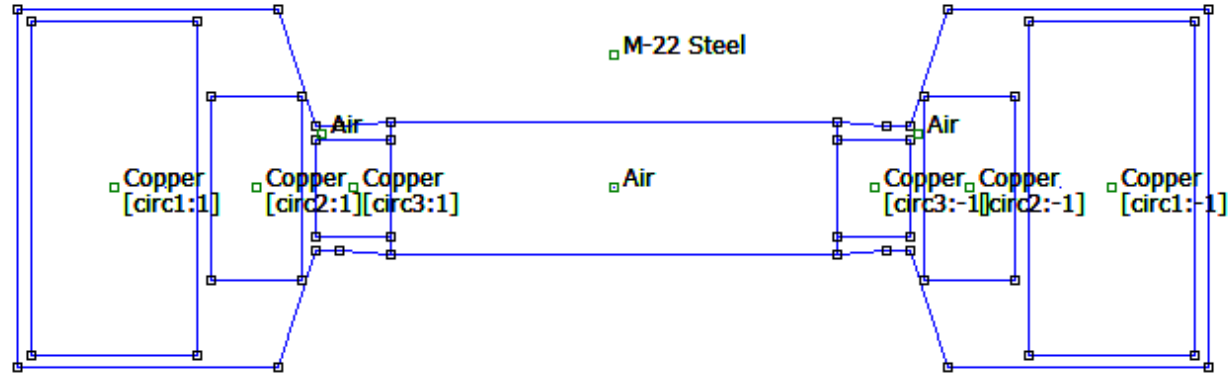
# Resistive dipole magnets main specifications

- The **resistive dipole magnets** to be designed for the Muon Collider accelerator are characterized by the following main specifications:
  - 1) Magnetic field in the aperture about **1.8 T**
  - 2) Magnetic field homogeneity within  $10 \times 10^{-4}$  in the good field region (**30 mm \* 100 mm**)
  - 3) Ramps from  $-B_{max}$  to  $+B_{max}$  in **1 ms**. The objective for the value of  $B_{max}$  is 2.0 T
  - 4) Limit the **magnet stored energy** (crucial design specification to limit the supplied power)
  - 5) Limit the **total losses (iron + copper)**

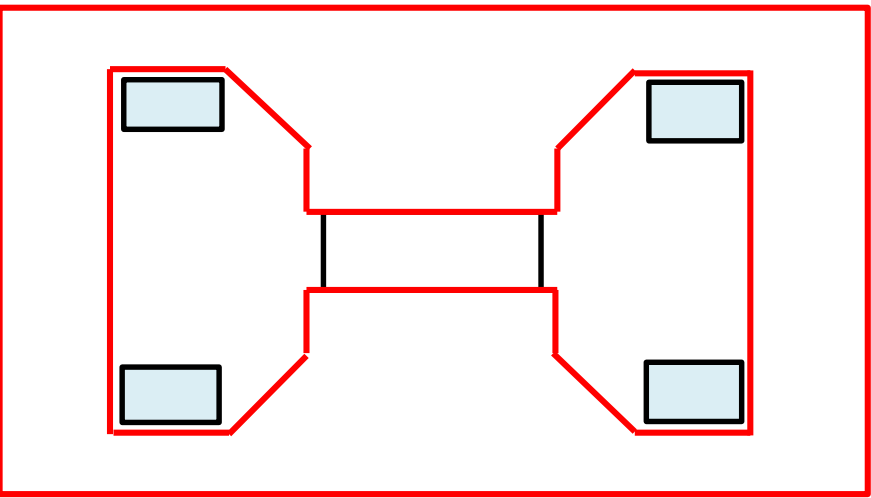


# Analysed magnet configurations

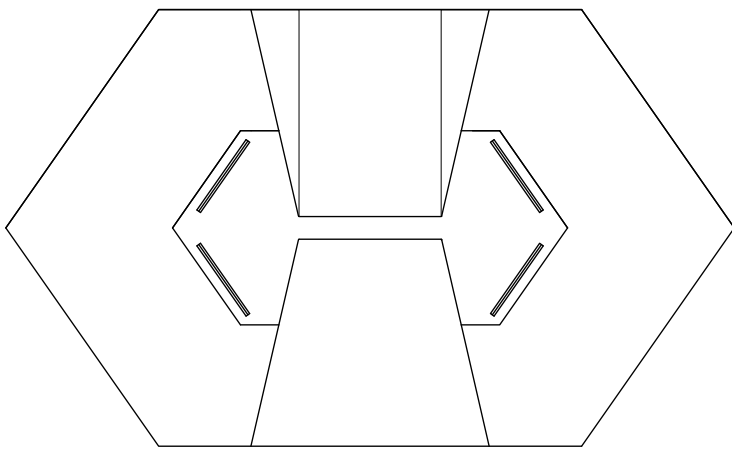
- In this preliminary study 3 main configurations are analyzed: **Windowframe magnet**, **H magnet**, **Hourglass magnet** (from the US study)



1) Windowframe magnet



2) H magnet



3) 'Hourglass' magnet

J. Scott Berg and Holger Witte, "Pulsed synchrotrons for very rapid acceleration", AIP Conference Proceedings 1777, 100002 (2016); <https://doi.org/10.1063/1.496568>.

# Study methodology: DC optimization

- The analysis is performed both in **DC and AC conditions**, in the frame of a 2D electromagnetic software (FEMM).
- A first optimization is performed in DC conditions, aimed at improving the field homogeneity in the good field region. The **objective function** to be optimized is the following:

$$\text{Field goodness} = \frac{1}{B_{des}} \sqrt{\frac{1}{A_{gap}} \iint_{A_{gap}} \{[By(x, y) - B_{des}]^2 + [Bx(x, y)]^2\} dA_{gap}}$$

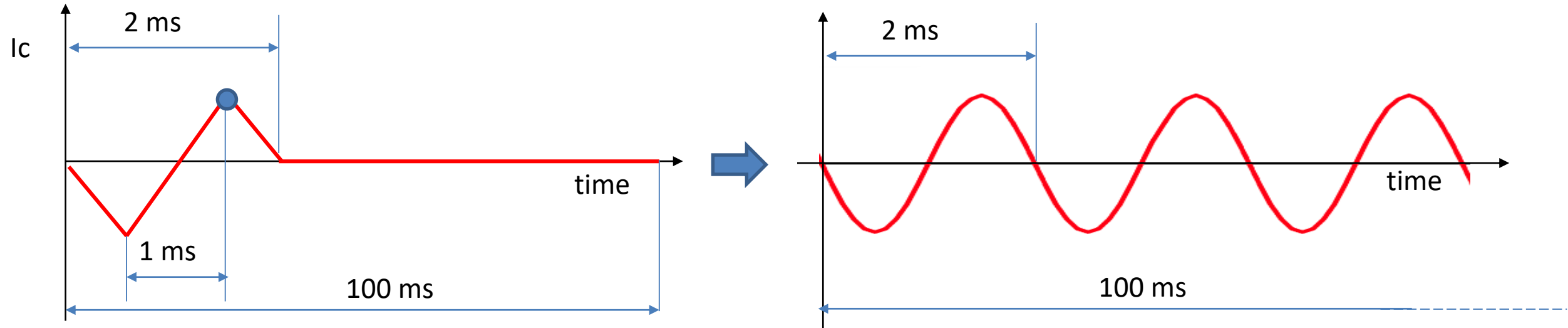
where  $B_{des}$  is the design value of the magnetic field in the center of the gap.

- The optimization is performed by using the MATLAB optimization toolbox and is based on the **interior point method** (function *fmincon*).
- The variables of the optimization are **geometric parameters**, while the current density is kept fixed
- Convergence is reached when the relative variation of all components of the vector of unknowns is less than  $10^{-10}$ . The **typical number of iterations** to reach convergence is **100**.



# Study methodology: AC analysis

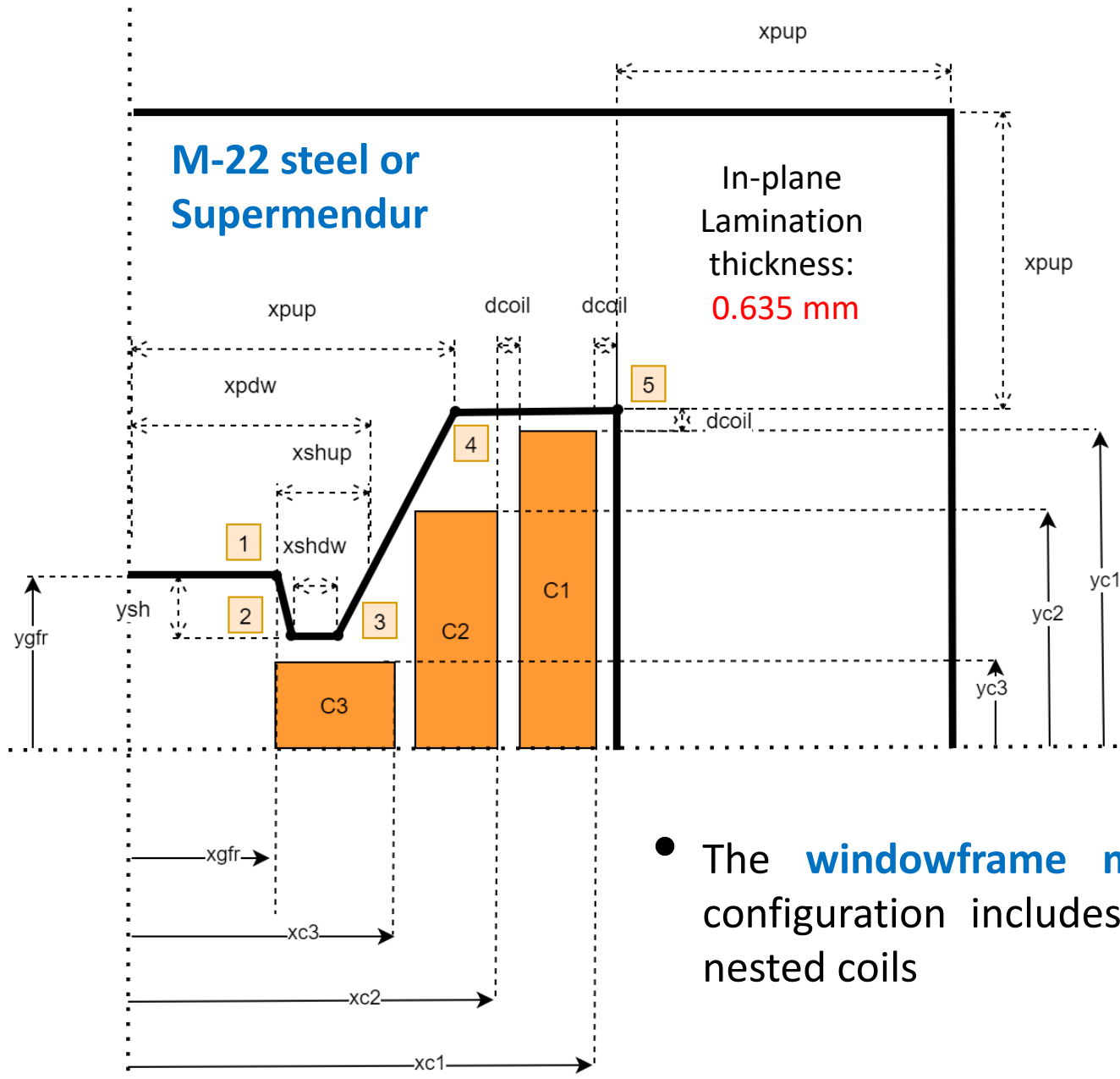
- The **design current profile** consists of a ramp from  $-B_{max}$  to  $+B_{max}$  in 1 ms. It is foreseen that this current profile will be provided by the power supply through the superposition of sinusoidal waves.



- The study in AC conditions starts from the geometric parameters defined in the DC optimization. The AC study is performed in the frequency domain: the coil currents are assumed **sinusoidal**, with a frequency of 500 Hz.
- Two approximations are made with the AC study:
  - 1) the **linear ramp** is approximated as a **sinusoid**
  - 2) the AC stationary conditions are assumed, which differ from the pulse followed by a standby time.



# Windowframe magnet: geometry



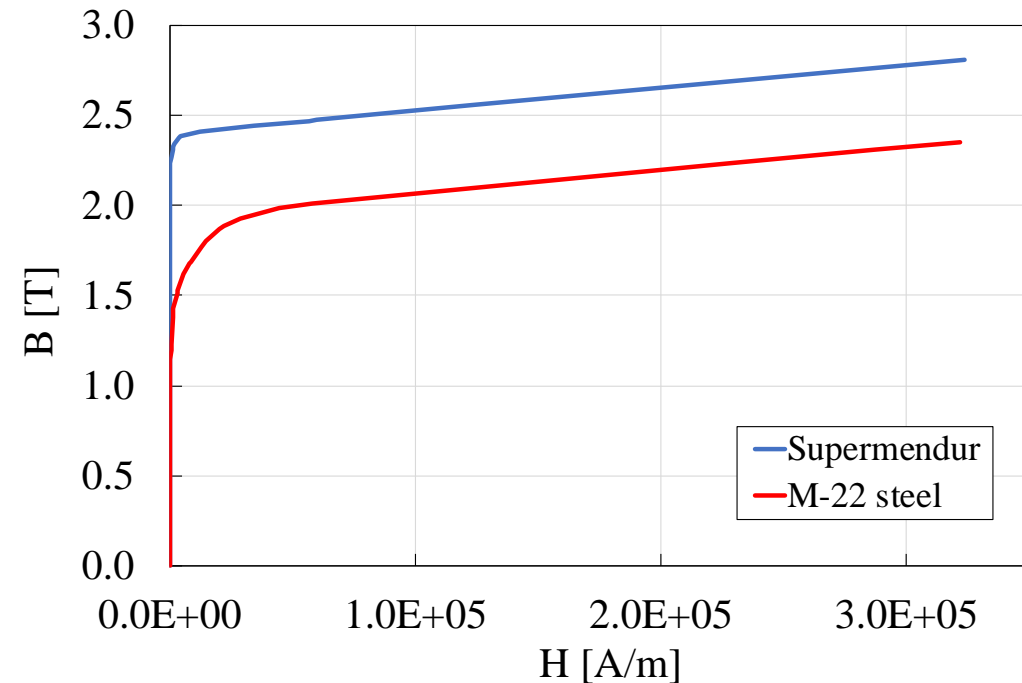
- The **windowframe magnet** configuration includes three nested coils

## Optimized variables (M-22 steel):

### Parameters:

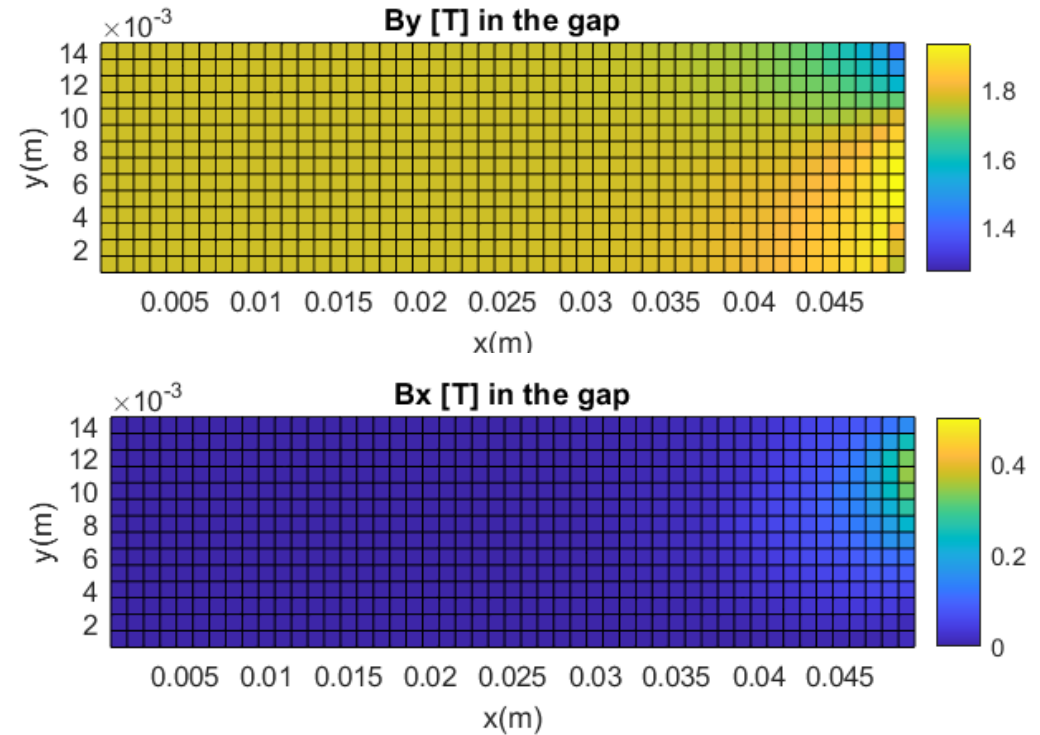
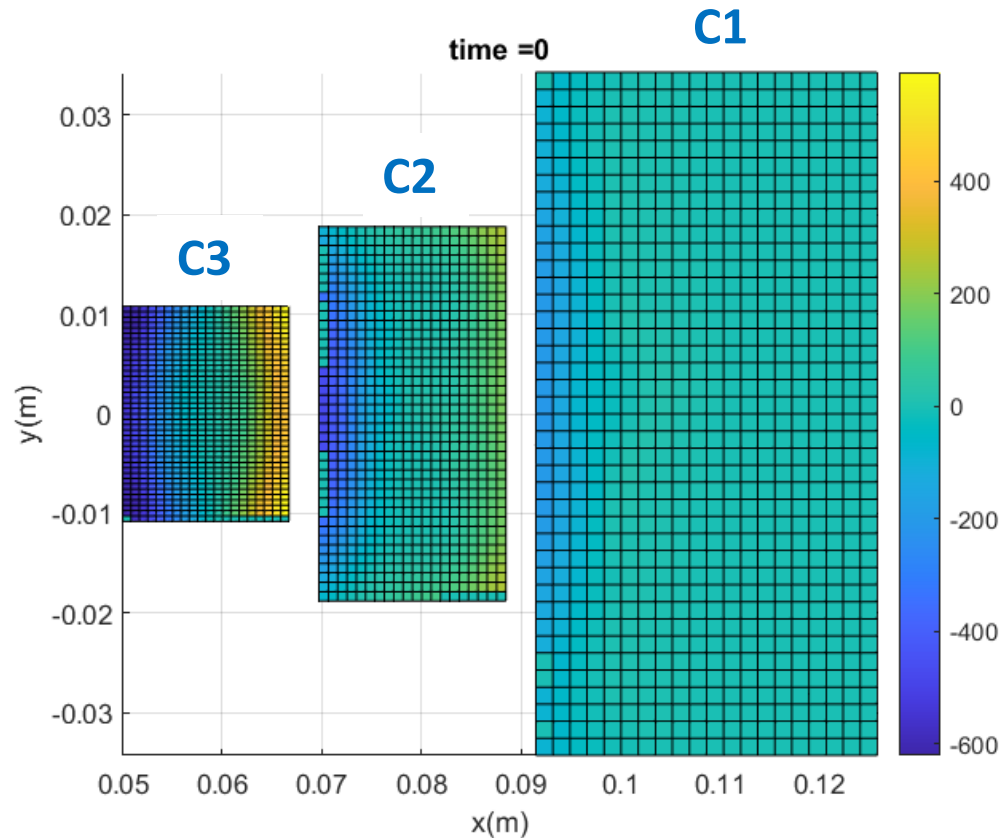
- Curatio = 0.8
- $y_{gap} = 0.03$  [m]
- $x_{gap} = 0.1$  [m]
- $x_{gfr} = x_{gap}/2$
- $y_{gfr} = y_{gap}/2$
- $d_{coil} = 0.003$  [m]

- $I_{c1} = 35000$  A
- $I_{c2} = 10500$  A
- $I_{c3} = 4500$  A
- $y_{sh} = 0.0012$  [m]
- $x_{shup} = 0.0167$  [m]
- $x_{shratio} = x_{shup}/x_{shdown} = 0.3$



# Windowframe magnet: results with Supermendur in AC

- With Supermendur, having a **high saturation field**, a good agreement is found between the computed DC field (1.77 T) and AC field (1.76 T)



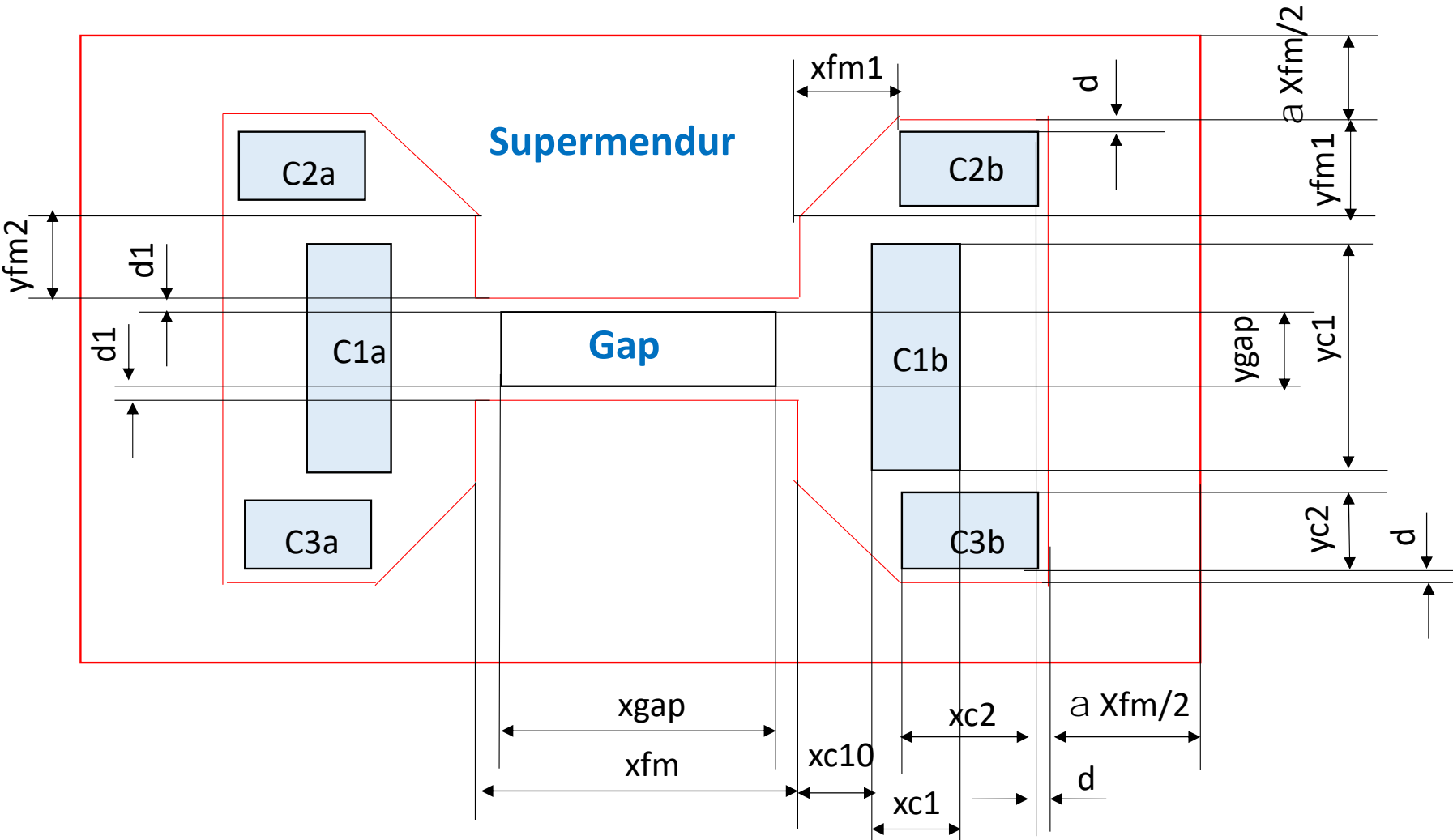
- The use of the Supermendur allows a reduction of the iron losses from **64 kW/m to 18 kW/m** with respect to M-22 steel





# H magnet 3-coils configuration: geometry

- In order to reduce the **current distribution non-uniformity**, and the mutual induction coupling between different coils, a different configuration was analyzed.



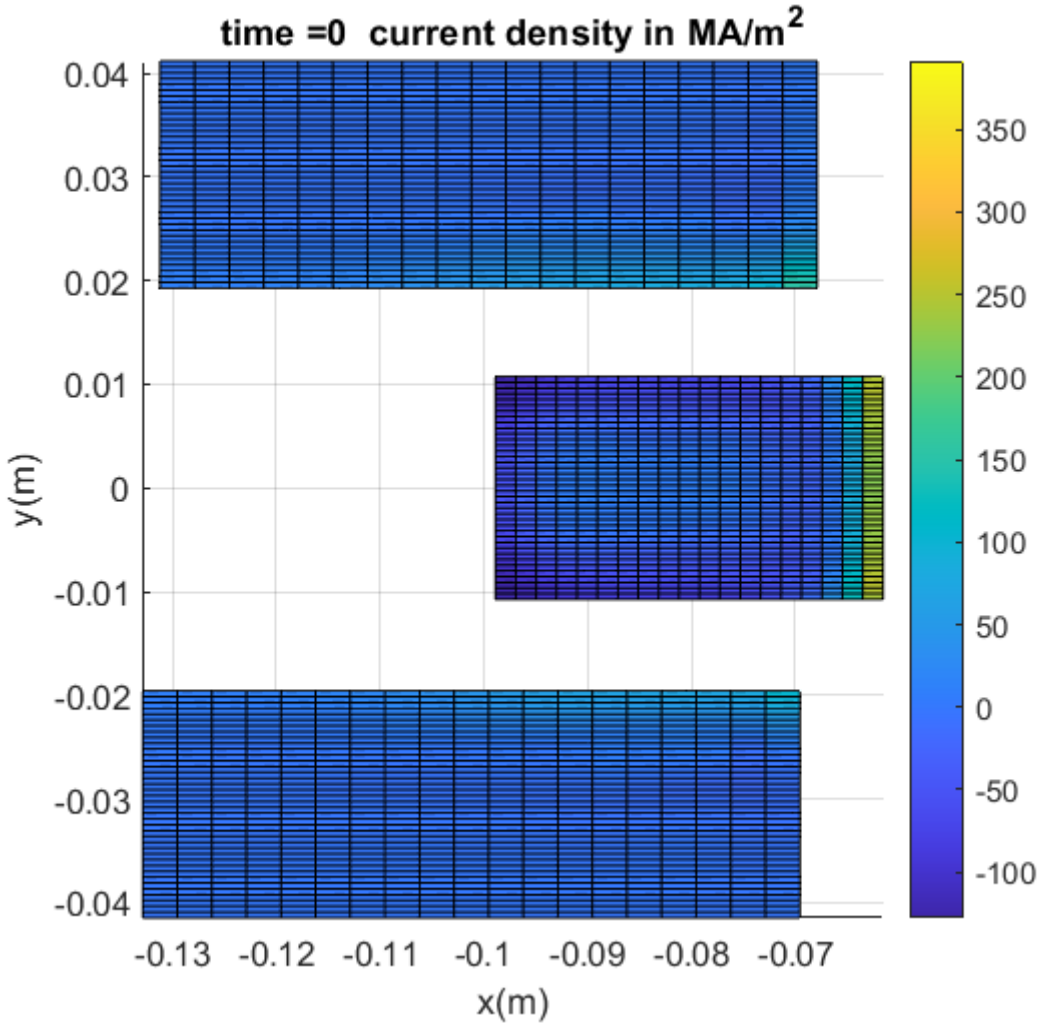
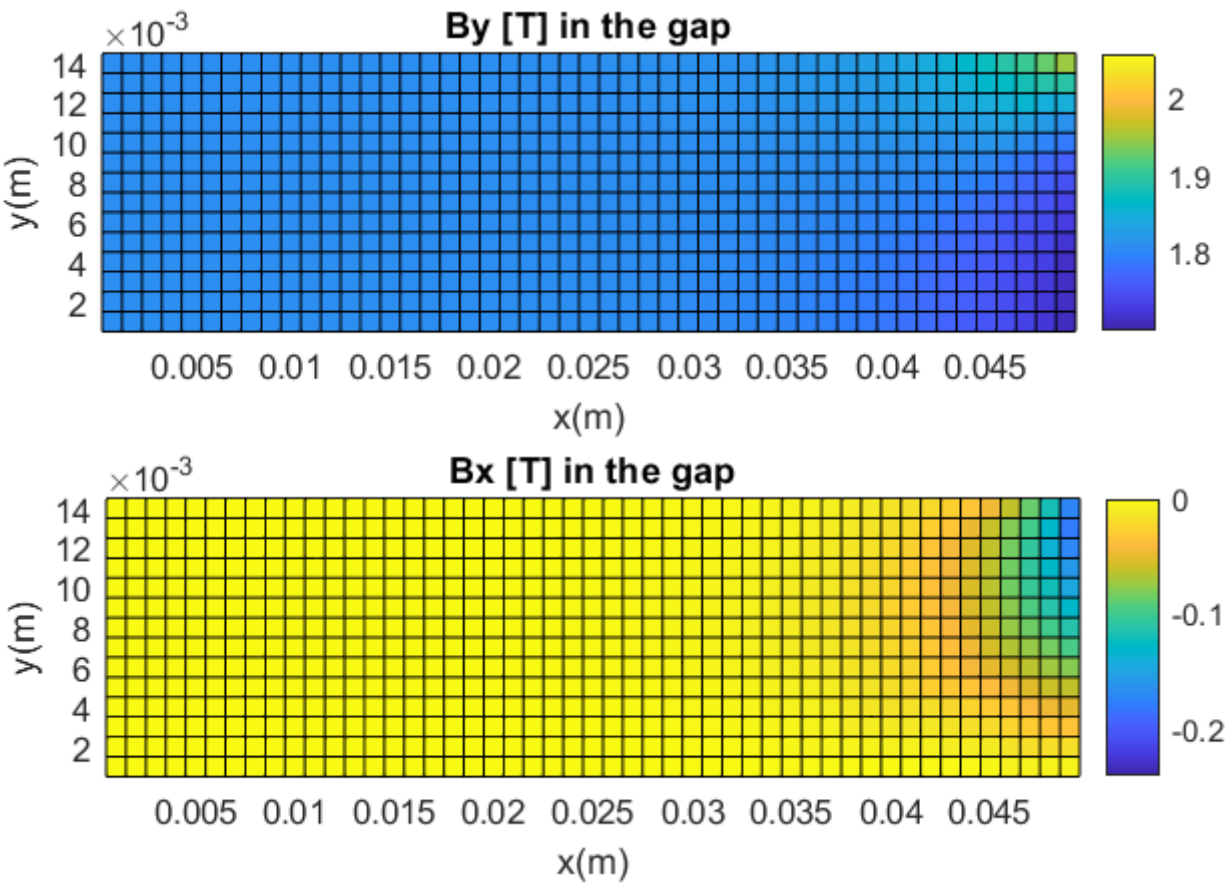
### Parameters:

- $x_{gap} = 100 \text{ mm}$
- $y_{gap} = 30 \text{ mm}$
- $d = 3 \text{ mm}$
- $\alpha = 1.3$
- $J_c = 12 \text{ A/mm}^2$

### Optimized variables:

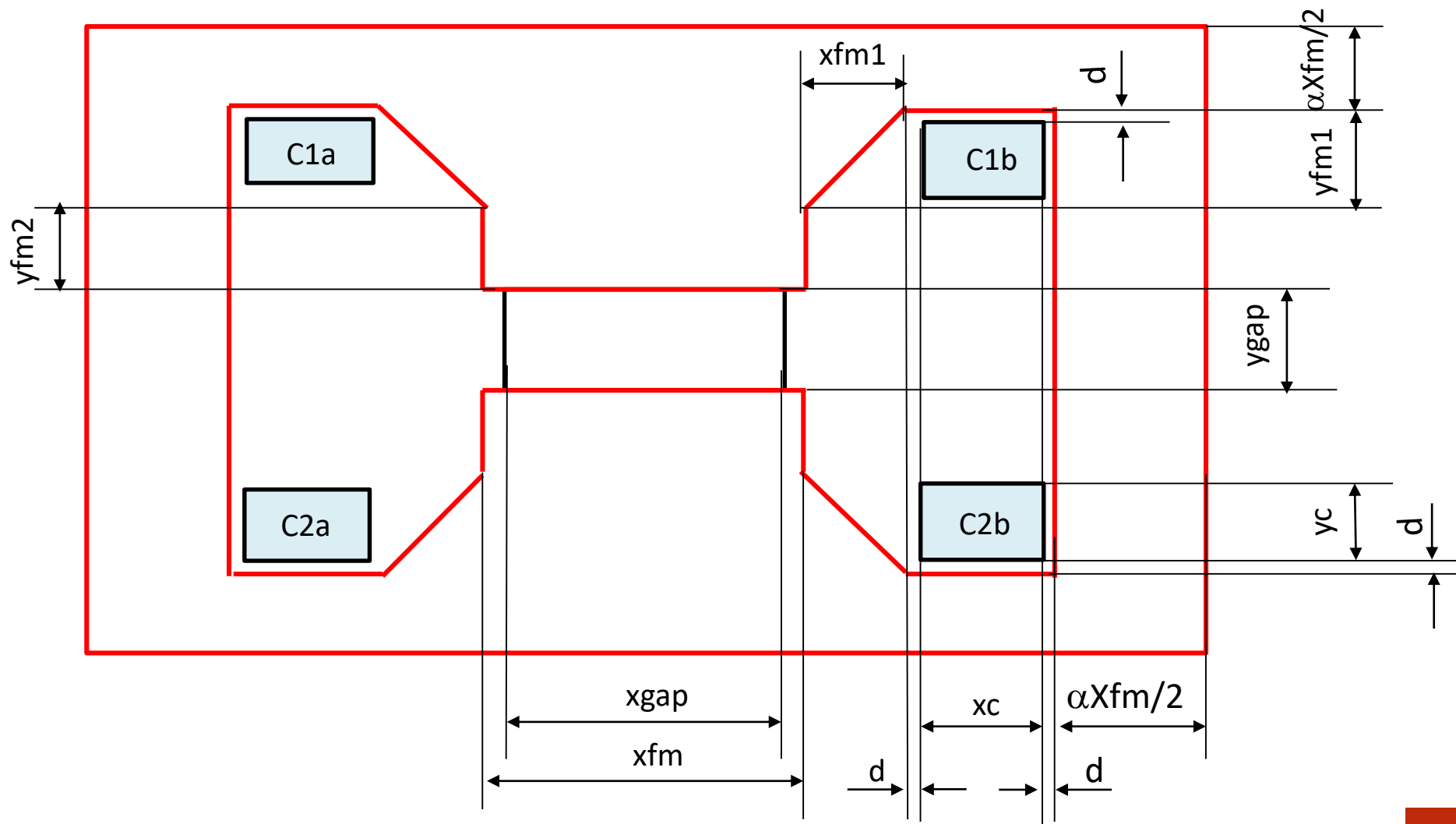
- $x_{fm}$
- $x_{fm1}$
- $y_{fm1}$
- $y_{fm2}$
- $x_{c10}$
- $x_{c1}$
- $y_{c1}$
- $x_{c2}$
- $y_{c2}$  ( $x_{c3} = x_{c2}$ ,  $y_{c3} = y_{c2}$ )

# H magnet 3-coils configuration: results in AC



- The current distribution is **more uniform** than in the windowframe magnet, which leads to lower losses in the copper
- A significant non-uniformity is still found in the **central coil**, which suggests its elimination

# H magnet 2-coils configuration: geometry



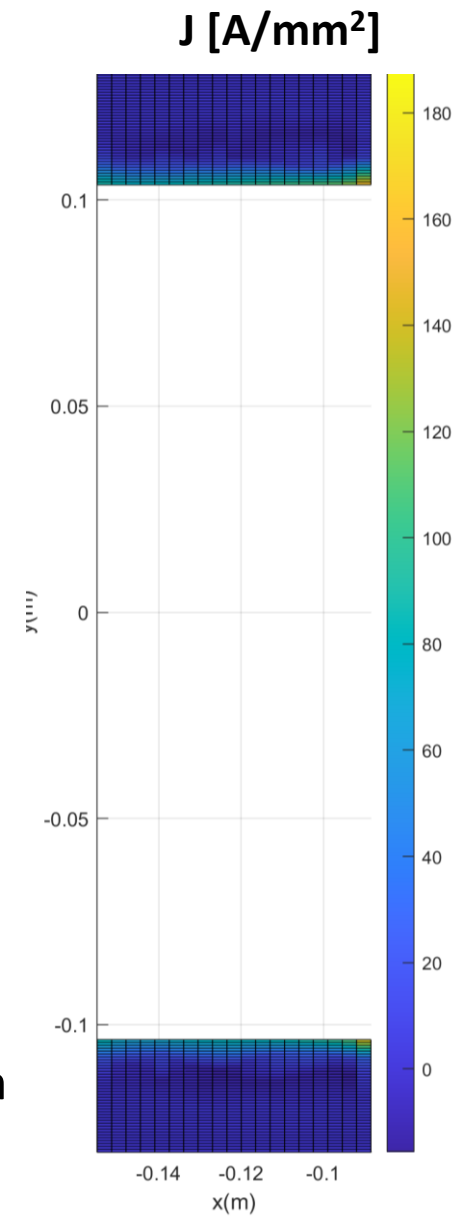
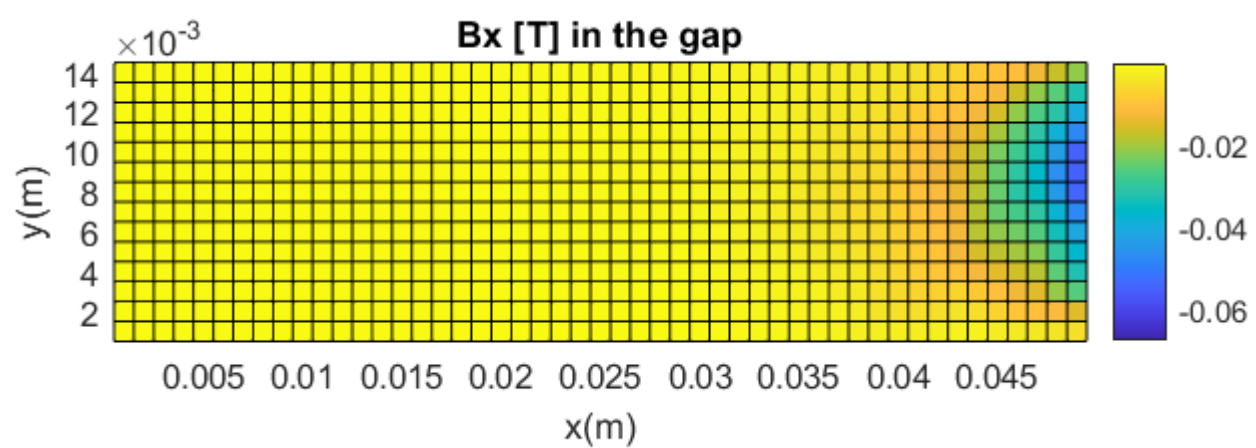
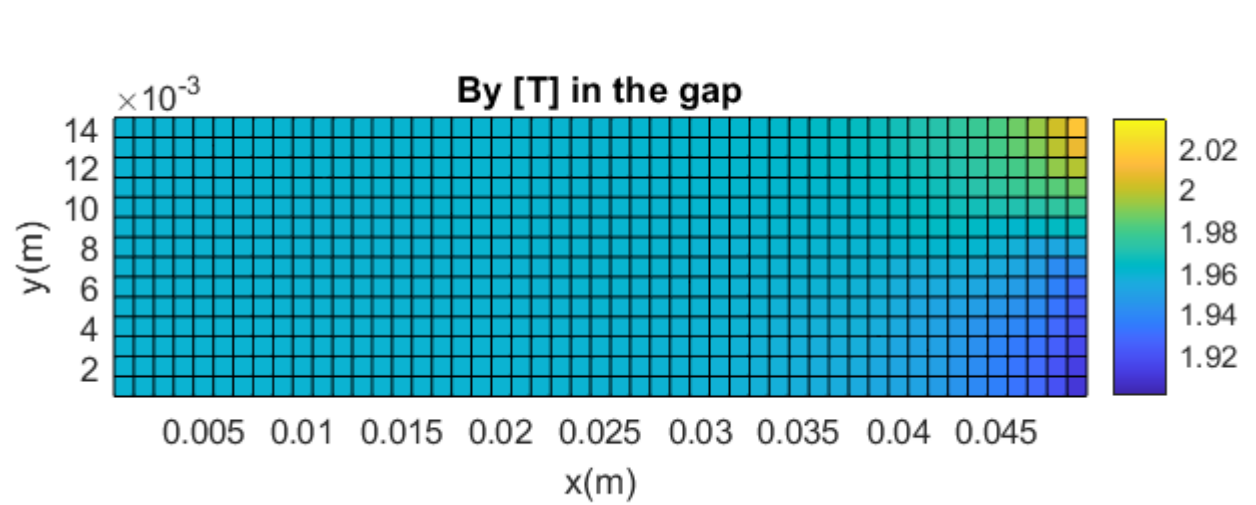
## Parameters:

1.  $x_{gap}$
2.  $y_{gap}$
3.  $d$
4.  $\alpha$
5.  $J_c$

## Optimized variables:

1.  $x_{fm}$
2.  $x_{fm1}$
3.  $y_{fm1}$
4.  $y_{fm2}$
5.  $x_c$
6.  $y_c$

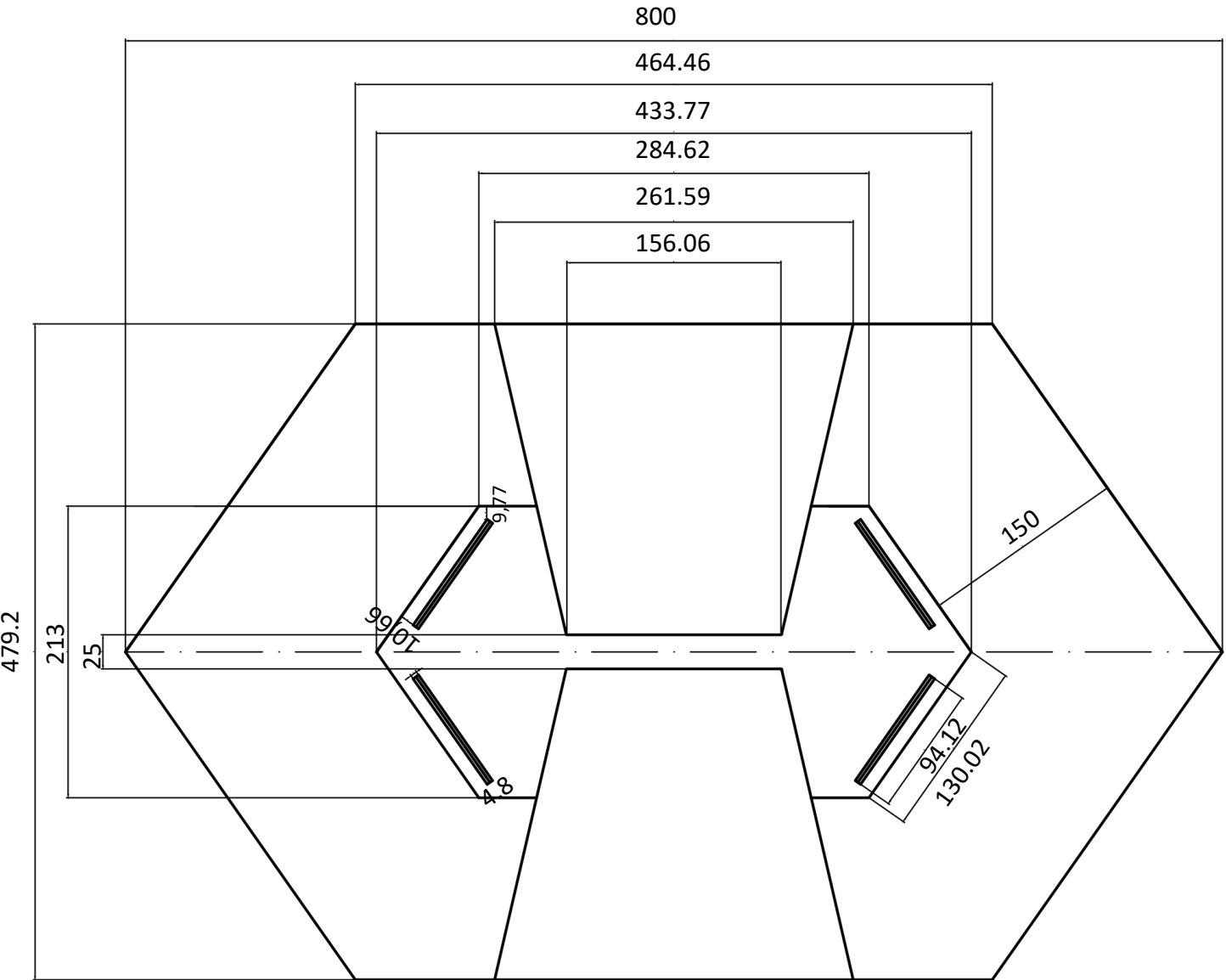
# H-Type magnet 2-coils configuration: results in AC



- A **more uniform current distribution** is obtained than in the configuration with 3 coils

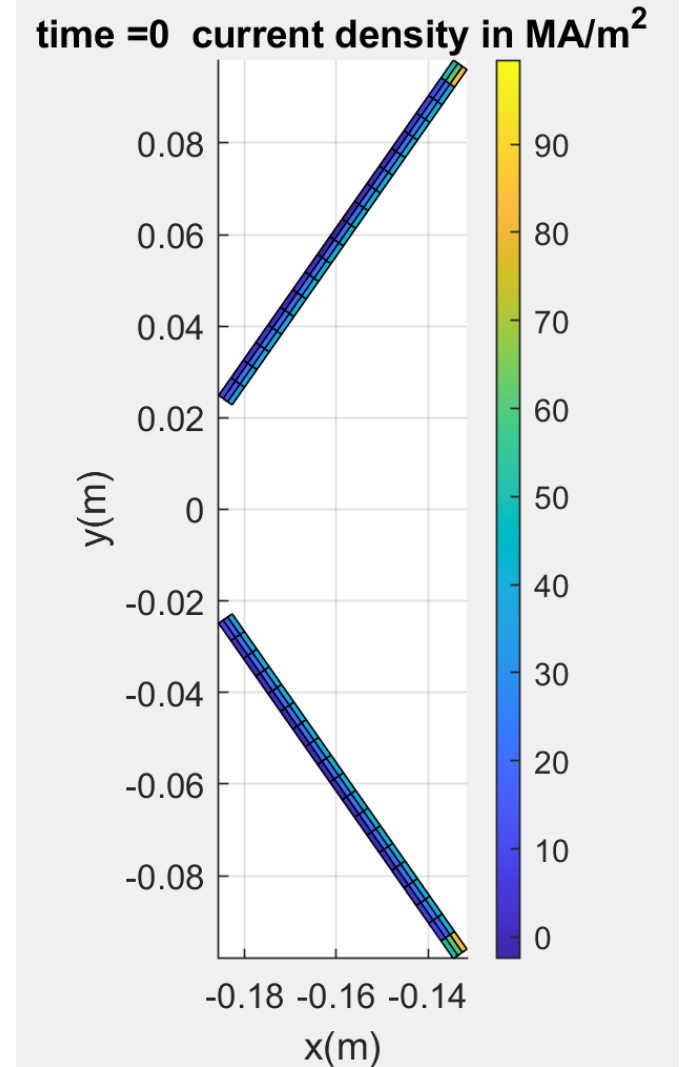
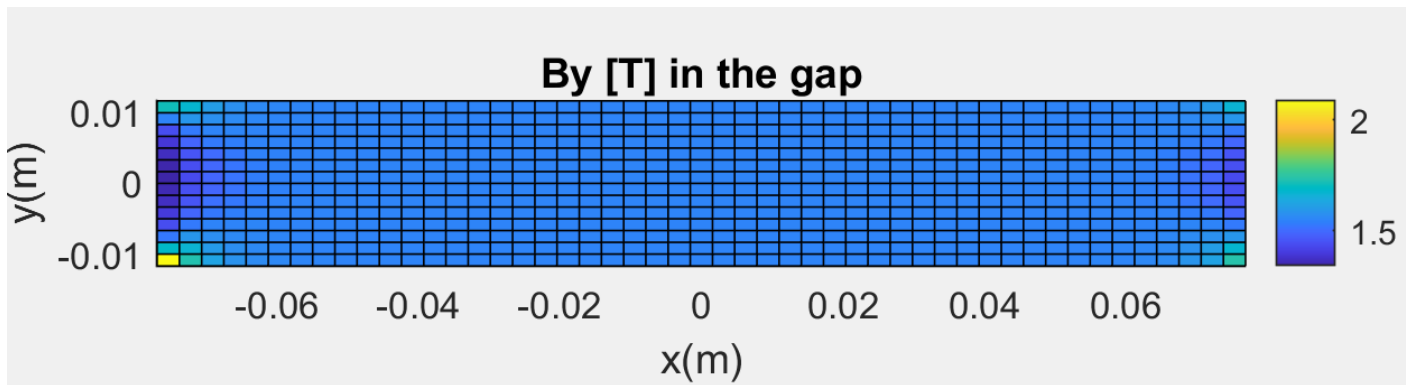
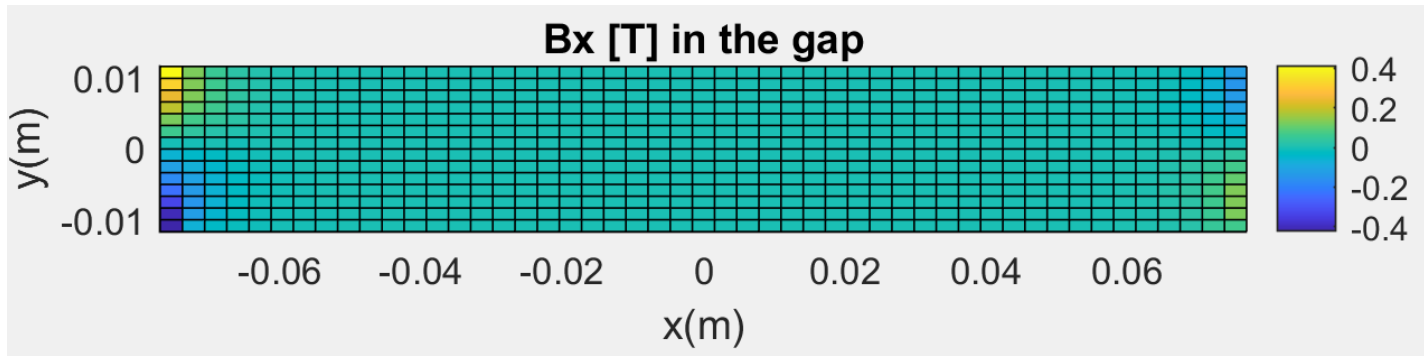
- The results reported in this plot correspond to a current density set to **12 A/mm<sup>2</sup>** in the DC optimization
- Only the total transport current is kept fixed in the AC analysis

# Hourglass magnet configuration: geometry



- In this analysis the same magnet dimensions adopted in the **US Muon Collider design study** have been considered
- Differently from the present configuration, the gap height is set to **25 mm instead of 30 mm**, while the gap length is set to **157 mm instead of 100 mm**
- **No further optimization** is applied to this configuration, as it results from the US study; in this analysis the coils are not subdivided into separate current sheets

# Hourglass magnet configuration: results in AC



- **Current density** and **magnetic flux density** in the gap calculated in a.c. regime with  $f = 500$  Hz, with Supermendur in the iron yoke
- A **very uniform current distribution** is found, except for the edges of the two coils

# Comparison of the three analyzed configurations

- The 'hourglass' magnet from the US study exhibits the **lowest real power (losses) and low reactive power**
- The windowframe magnet exhibits the **lowest reactive power**
- The H-magnets exhibit **lower copper losses** than the windowframe magnet

	Active power [kW/m]	Reactive power [MVar/m]	Gap energy [J/m]	Energy in air (no gap) [J/m]	Energy in coils [J/m]	Losses in iron [kW/m]
<b>Windowframe magnet</b>	1236	14.0	3697	668	1485	18
<b>H magnet - 3 coils</b>	356	16.3	3814	1305	552	26
<b>H magnet - 2 coils</b>	182	19.9	3875	3140	142	111
<b>Hourglass magnet</b>	149	15.7	3821	1165	7	122



# Summary and perspectives

- A **tool for the optimized analysis** of resistive magnets for the Muon Collider accelerator has been developed
- The **assumptions of this tool** will be carefully checked through other computation methods not requiring the AC approximation
- Three different configurations have been analyzed, namely the **windowframe magnet, the H type magnet** and **the 'hourglass' configuration** resulting from the US design study
- The **'hourglass' configuration** exhibits **low real and reactive power**, which indicates it already reached a very good level of optimization
- Further **optimization** will be applied to the newly proposed designs







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**Thank you for your kind attention !**

Marco Breschi, Rebecca Miceli, Pier Luigi Ribani  
Fulvio Boattini, Luca Bottura

[marco.breschi@unibo.it](mailto:marco.breschi@unibo.it)

# Windowframe magnet: M-22 steel vs Supermendur

## M-22 steel

Ic1max = 35.0 kA  
Vc1max = 789 V/m  
Fluxmax = 0.25 Wb/m  
Real Power = 1.35 MW/m  
Reactive Power = 13.7 MVar/m  
Cu losses = 110.6 kW/m

Ic2max = 10.5 kA  
Vc2max = 759 V/m  
Fluxmax = 0.24 Wb/m  
Real Power = 0.33 MW/m  
Reactive Power = 3.96 MVar/m  
Cu losses = 501.6 kW/m

Ic3max = 4.5 kA  
Vc3max = 680 V/m  
Fluxmax = 0.26 Wb/m  
Real Power = 0.057 MW/m  
Reactive Power = 1.53 MVar/m  
Cu losses = 1068.8 kW/m

**Fe loss = 64 kW/m**

## Supermendur

Ic1max = 29.8 [kA]  
Vc1max = 676 [V/m]  
Fluxmax = 0.22 [Wb/m]  
Real Power = 0.97 [MW/m]  
Reactive Power = 10.0 [MVar/m]  
Cu losses = 89.2 [kW/m]

Ic2max = 8.9 [kA]  
Vc2max = 648 [V/m]  
Fluxmax = 0.21 [Wb/m]  
Real Power = 0.23 [MW/m]  
Reactive Power = 2.88 [MVar/m]  
Cu losses = 371.8 [kW/m]

Ic3max = 3.8 [kA]  
Vc3max = 580 [V/m]  
Fluxmax = 0.22 [Wb/m]  
Real Power = 0.038 [MW/m]  
Reactive Power = 1.11 [MVar/m]  
Cu losses = 757.3 [kW/m]

**Fe loss = 18 [kW/m]**



# H-Type magnet 2-coils configuration: results in AC

## Nominal current density = 12 MA/m<sup>2</sup>

Ic1max = 23.5 [kA]	Ic2max = 23.5 [kA]
Vc1max = 1118 [V/m]	Vc2max = 1118 [V/m]
Fluxmax = 0.356 [Wb/m]	Fluxmax = 0.356 [Wb/m]
Real Power = 0.1006 [MW/m]	Real Power = 0.1006 [MW/m]
Reactive Power = 13.134 [Mvar/m]	Reactive Power = 13.134 [MVAR/m]
Resistive loss = 45.104 [kW/m]	Resistive loss = 45.104 [kW/m]

Fe loss = 111.009 [kW/m]  
field energy in the gap = 2.292 [kJ/m]  
field energy in iron = 40.6 [J/m]  
field energy in air-in = 1.838 [kJ/m]  
field energy in coil 1 [J/m] = 5.0 [J/m]  
field energy in coil 2 [J/m] = 5.0 [J/m]

## Nominal current density = 10 MA/m<sup>2</sup>

Ic1max = 22.7 [kA]	Ic2max = 22.7 [kA]
Vc1max = 1064 [V/m]	Vc2max = 1064 [V/m]
Fluxmax = 0.339 [Wb/m]	Fluxmax = 0.339 [Wb/m]
Real Power = 0.0904 [MW/m]	Real Power = 0.0904 [MW/m]
Reactive Power = 12.107 [Mvar/m]	Reactive Power = 12.107 [MVAR/m]
Resistive loss = 42.714 [kW/m]	Resistive loss = 42.714 [kW/m]

Fe loss = 95.434 [kW/m]  
field energy in the gap = 2.153 [kJ/m]  
field energy in iron = 40.6 [J/m]  
field energy in air-in = 1.659 [kJ/m]  
field energy in coil 1 [J/m] = 4.7 [J/m]  
field energy in coil 2 [J/m] = 4.7 [J/m]



# Comparison of the three analyzed configurations

- The **'hourglass' magnet** from the US study exhibits the **lowest real power**
- Among the newly developed designs, the windowframe magnet exhibits the **lowest value of reactive power**
- Due to a **more uniform current distribution**, the H-magnets exhibit lower copper losses than the windowframe magnet

Windowframe magnet	Real power [kW/m]	Reactive power [MVar/m]	Gap energy [J/m]	Energy in air (no gap) [J/m]	Energy in coils [J/m]	Losses in iron [kW/m]
Coil1	966.0	10.0	3697	668	1485	18
Coil2	232.0	2.9				
Coil3	38.0	1.1				
Total	1236.0	14.0				
<b>H magnet 3-coils</b>						
Coil1	62.4	3.6	3814	1305	552	26
Coil2	146.6	6.4				
Coil3	146.6	6.4				
Total	355.6	16.3				
<b>H magnet 2-coils</b>						
Coil1	90.9	10.0	3875	3140	142	111
Coil2	90.9	10.0				
Total	181.8	19.9				
<b>Hourglass magnet</b>						
Coil1	74.5	7.9	3821	1165	7	122
Coil2	74.5	7.9				
Total	149.1	15.7				