


# The Advanced Muon Facility at Fermilab: Physics and Relationship to the Muon Collider



R. Bernstein, FNAL  
ENIGMA Collaboration

IMCC Meeting  
October 2022

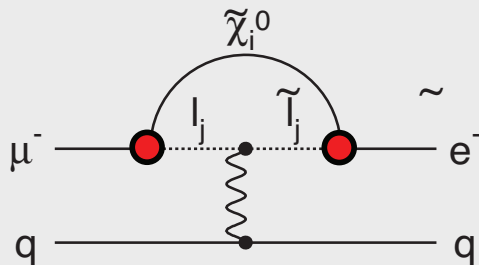
# Charged Lepton Flavor Violation

- Transitions among  $\mu \leftrightarrow e \leftrightarrow \tau$  without neutrinos
  - cannot be weak interaction: non-SM process
- Directly linked to questions of flavor and generations
  - we observe mixing in quarks and neutral leptons: why not charged?
- Muon CLFV has been under study since the discovery of the muon; taus are also important

# Contributions to Muon CLFV

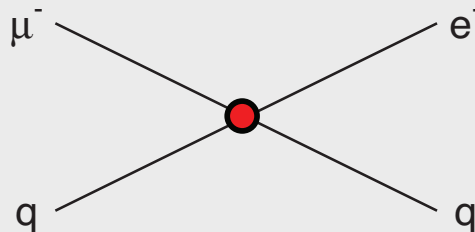
## Supersymmetry

$$\text{rate} \sim 10^{-15}$$



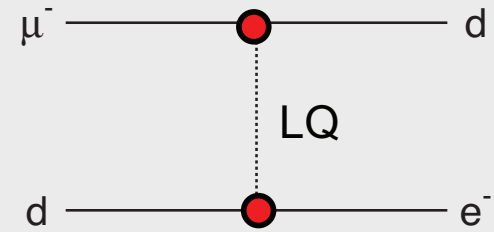
## Compositeness

$$\Lambda_c \sim 3000 \text{ TeV}$$



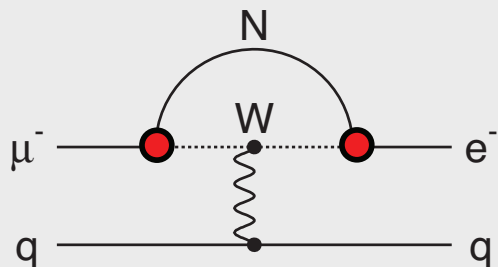
## Leptoquark

$$M_{LQ} = 3000 (\lambda_{\mu d} \lambda_{e d})^{1/2} \text{ TeV}/c^2$$



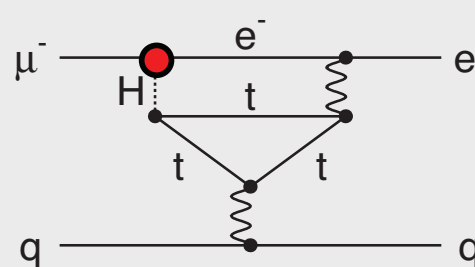
## Heavy Neutrinos

$$|U_{\mu N} U_{e N}|^2 \sim 8 \times 10^{-13}$$



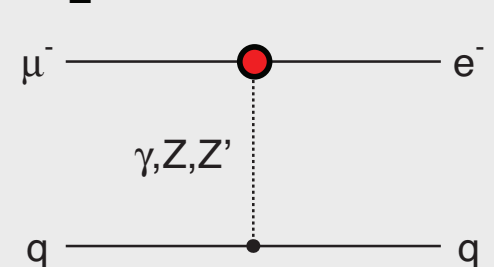
## Second Higgs Doublet

$$g(H_{\mu e}) \sim 10^{-4} g(H_{\mu\mu})$$



## Heavy Z' Anomal. Z Coupling

$$M_{Z'} = 3000 \text{ TeV}/c^2$$



also see Flavour physics of leptons and dipole moments, [arXiv:0801.1826](https://arxiv.org/abs/0801.1826) ;  
 Marciano, Mori, and Roney, Ann. Rev. Nucl. Sci. 58, doi:[10.1146/annurev.nucl.58.110707.171126](https://doi.org/10.1146/annurev.nucl.58.110707.171126) ;

# CLFV Muon Processes

- $\mu \rightarrow e\gamma$

- oldest studied, most powerful limits, and the best experiment so far: MEG at PSI

- $\mu N \rightarrow eN$

- muon to electron conversion: muon converts in field of nucleus, leaving nucleus unchanged

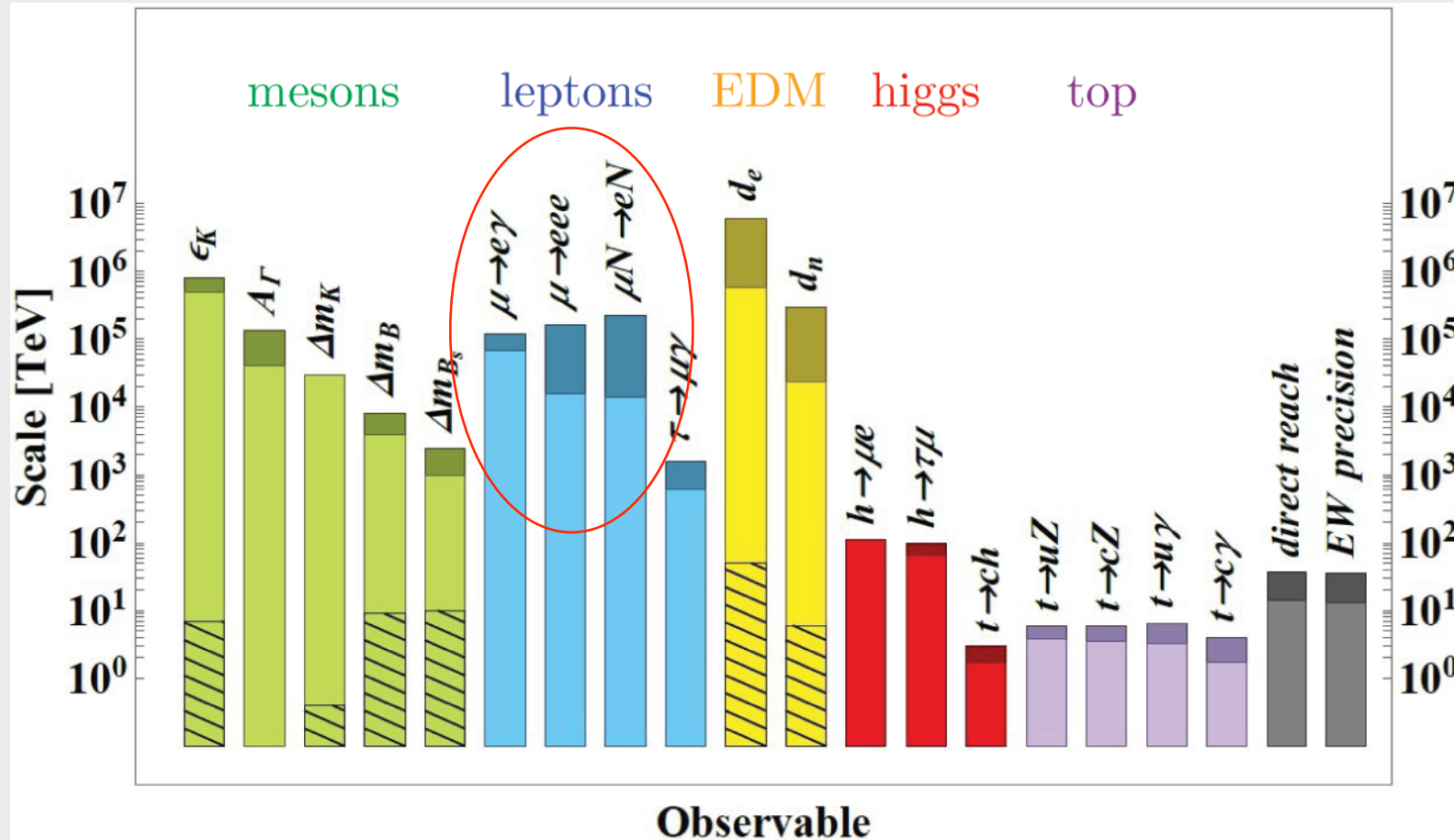
$$R_{\mu e} = \frac{\Gamma(\mu^- + N(A,Z) \rightarrow e^- + N(A,Z))}{\Gamma(\mu^- + N(A,Z) \rightarrow \text{all muon captures})}$$

- two experiments upcoming at FNAL and JPARC

- $\mu \rightarrow eee$

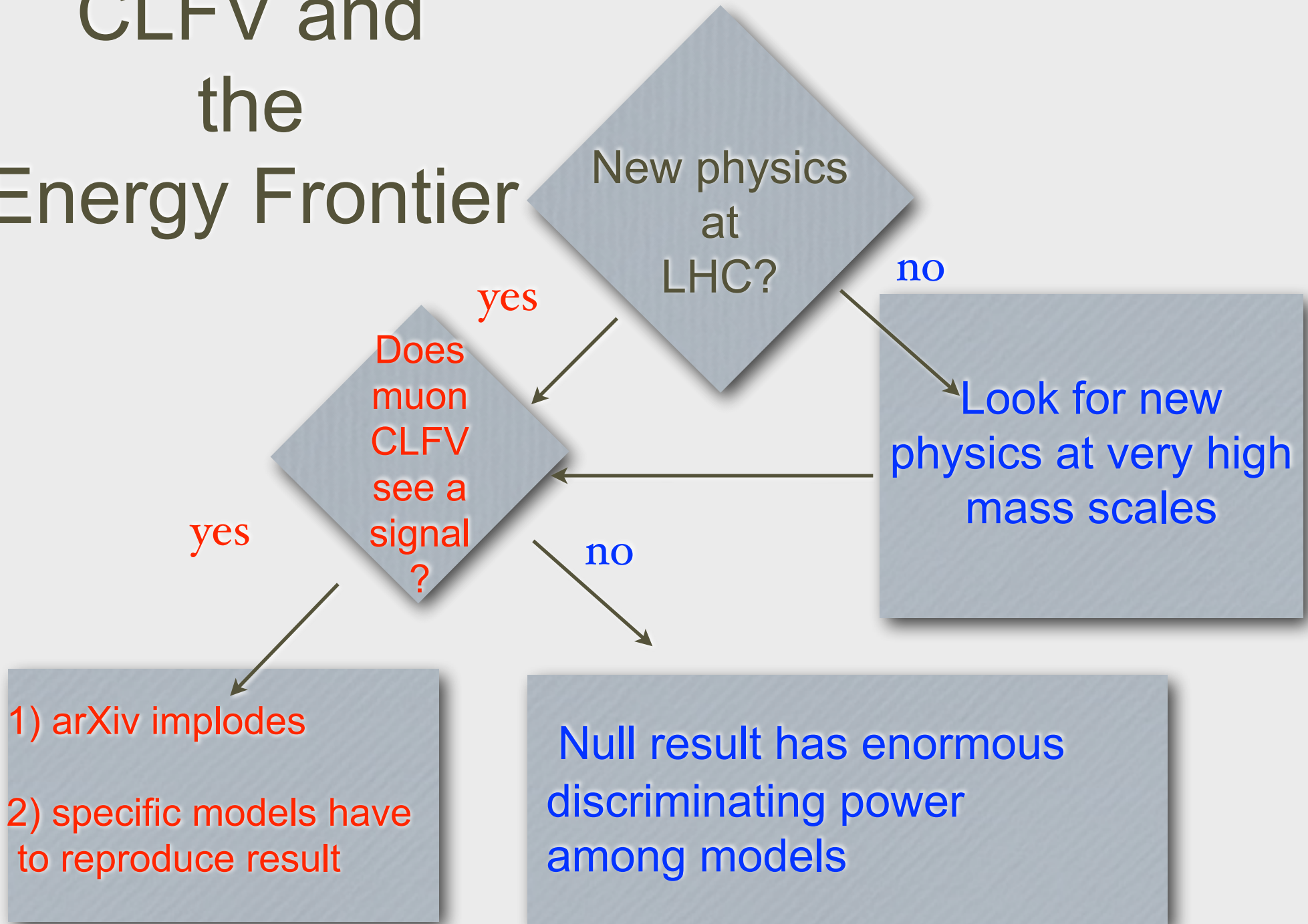
- ambitious and unique, excellent partner to other two (at PSI)

# Mass Scales of Muon CLFV Searches



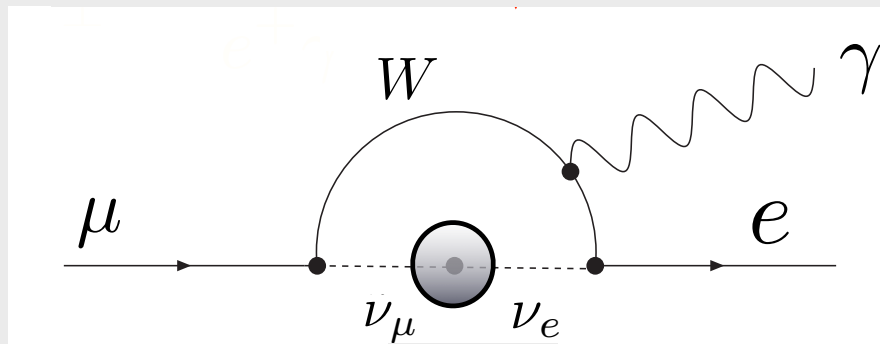
operator coefficients =1, from Physics Briefing Book, 1910.11775

# CLFV and the Energy Frontier



# Neutrino Oscillations and Muon CLFV

- $\nu$ 's have mass! *individual lepton numbers are not conserved*
- Therefore Lepton Flavor Violation occurs in Charged Leptons as well

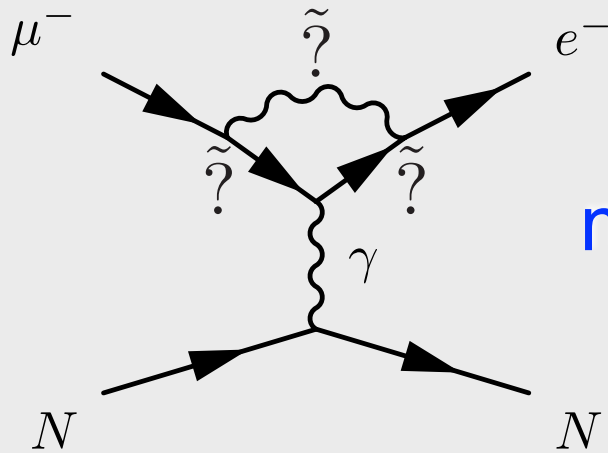


$$\text{BR}(\mu \rightarrow e \gamma) = \frac{3\alpha}{32\pi} \left| \sum_{i=2,3} U_{\mu i}^* U_{ei} \frac{\Delta m_{1i}^2}{M_W^2} \right|^2 < 10^{-54}$$

# Toy Lagrangian

$$\mathcal{L}_{\text{CLFV}} = \frac{m_\mu}{\Lambda^2} \bar{\mu}_R \sigma_{\mu\nu} e_L F^{\mu\nu} + \frac{1}{\Lambda^2} \bar{\mu}_L \gamma^\mu e_L (\bar{u}_L \gamma_\mu u_L + \bar{d}_L \gamma_\mu d_L)$$

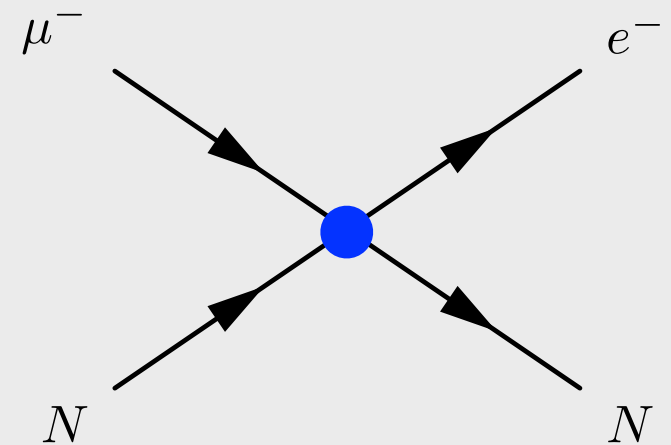
“Loops”



Supersymmetry and Heavy Neutrinos

mass scale  $\Lambda$

“Contact Terms”



New Particles at High Mass Scale (leptoquarks, heavy Z,...)

Contributes to  $\mu \rightarrow e\gamma$

(just imagine the photon is real)

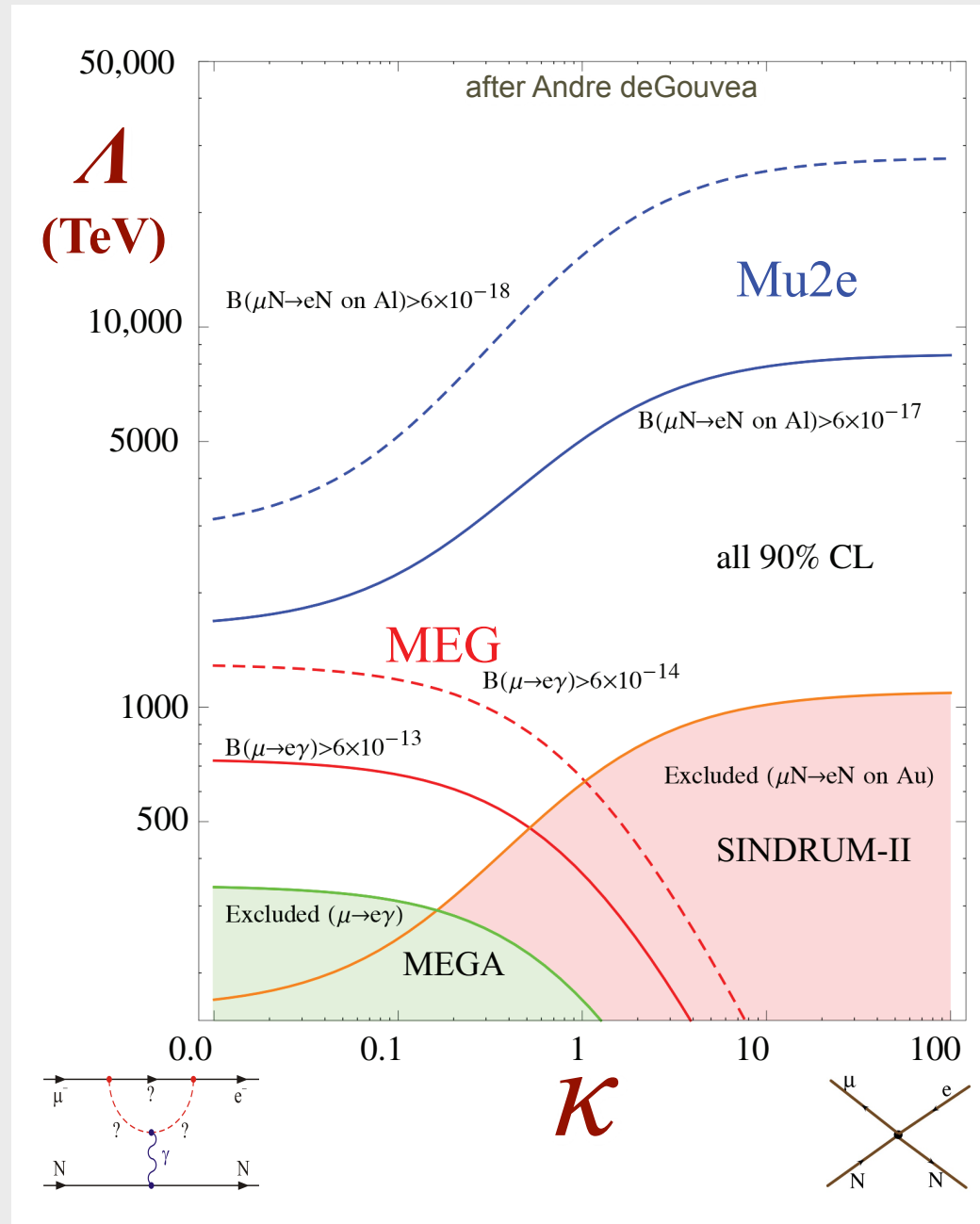
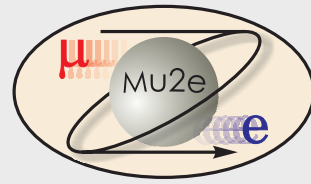
Does not produce  $\mu \rightarrow e\gamma$

A. DeGouvêa and P. Vogel, [1303.4097v2](#) [hep-ph]

for EFT treatment see S. Davidson and B. Echenard, [2010.00317](#) [hep-ph]



# “DeGouvea Plot: 2013”



↑  
higher mass scale

de Gouvêa and Vogel, 1303.4097

# EFT: Beyond $\Lambda$ and $\kappa$

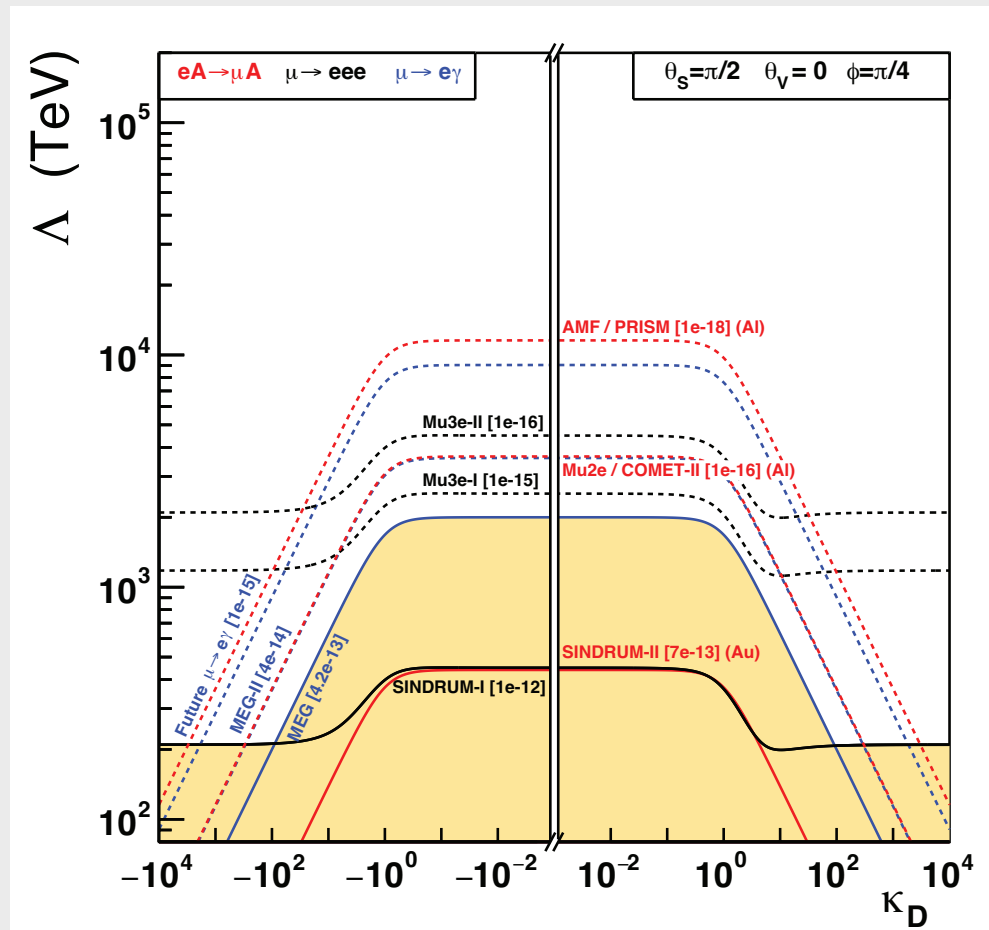
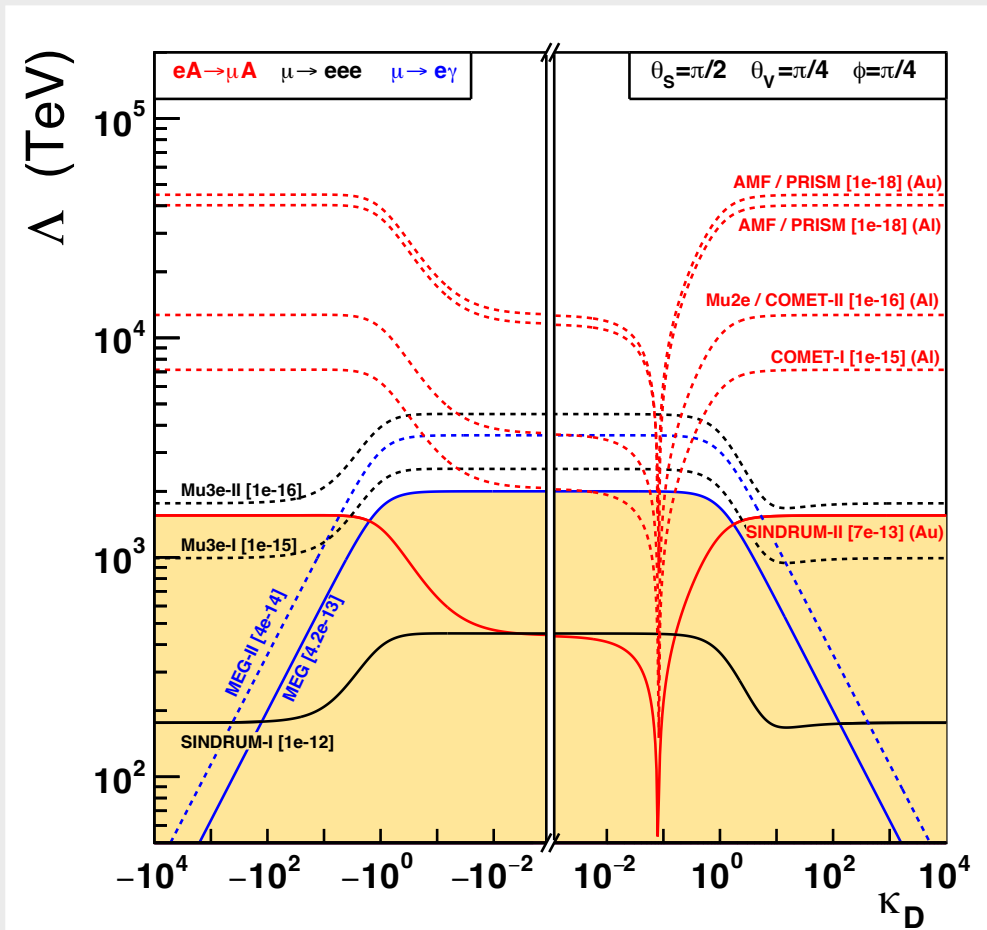
S. Davidson and B. Echenard, [2010.00317](#) [hep-ph]

- Write EFT Lagrangian:
  - Dipole ( $\mu \rightarrow e\gamma$ ) +
  - Contact Scalar ( $\mu \rightarrow 3e$ )<sub>L</sub> +
  - Contact Vector ( $\mu \rightarrow 3e$ )<sub>R</sub> +
  - Contact  $\mu N \rightarrow eN$  (light nuclei) +
  - Contact  $\mu N \rightarrow eN$  (heavy nuclei)
- Parameterize coefficient space with spherical coordinates: *lets you express constraints on all three processes simultaneously*
- Will show you “slices” in the multi-dimensional space

# Complementarity

S. Davidson and B. Echenard, [2010.00317](#) [hep-ph]

- All three channels have strengths; we need the combination



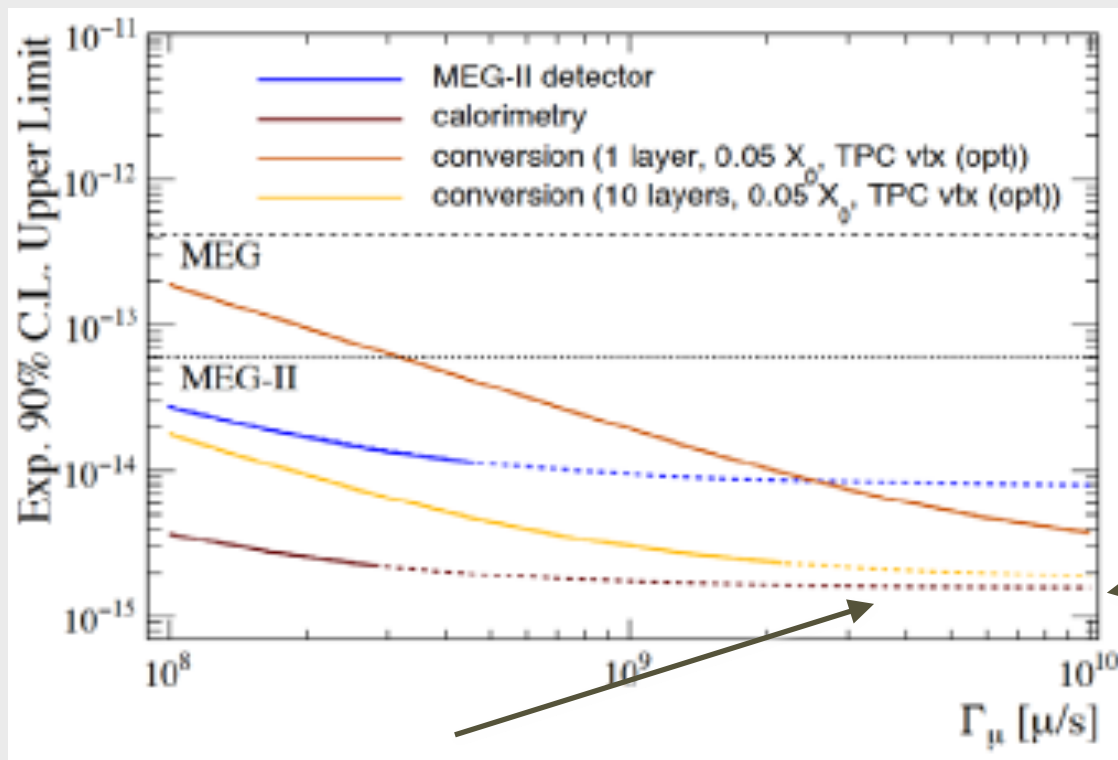
- $\mu \rightarrow e\gamma$  and  $\mu \rightarrow 3e$  at  $\mathcal{O}(10^{-15})$  are a next-gen target

# Decay Experiments

- $\mu^+ \rightarrow e^+ \gamma$  and  $\mu^+ \rightarrow e^+ e^+ e^-$ 
  - these bring low energy ( $\sim 30$  MeV)  $\mu^+$  to rest in material and observe the decay (surface muon)
  - in  $\mu^+ \rightarrow e^+ \gamma$ , accidentals scaling as  $I^2$  are the limit; accidentals come from multiple muon decays and resolution limits
    - since accidentals drive the background, we want as continuous a beam as possible
  - in  $\mu^+ \rightarrow e^+ e^+ e^-$ , additional bkg from radiative muon decay,  $\mu^+ \rightarrow e^+ e^+ e^- \nu_e \bar{\nu}_\mu$  with small  $E_\nu$

# $\mu \rightarrow e\gamma$ Limits

- $\mu^+ \rightarrow e^+\gamma$  as in MEG, but convert the photon for improved resolution (have a vertex from tracks)
- lowers statistics by  $\sim x100$  but improves background rejection



levels out at  
 $10^{10} \mu/\text{sec}$ ,  
 about HiMB  
 PSI upgrade

Renga et al., 1811.12324[hep-ex]

next-gen  $10^{-15}$  goal for  $\mu \rightarrow e\gamma$  and  $\mu \rightarrow 3e$

# New Ideas in Decay Experiments

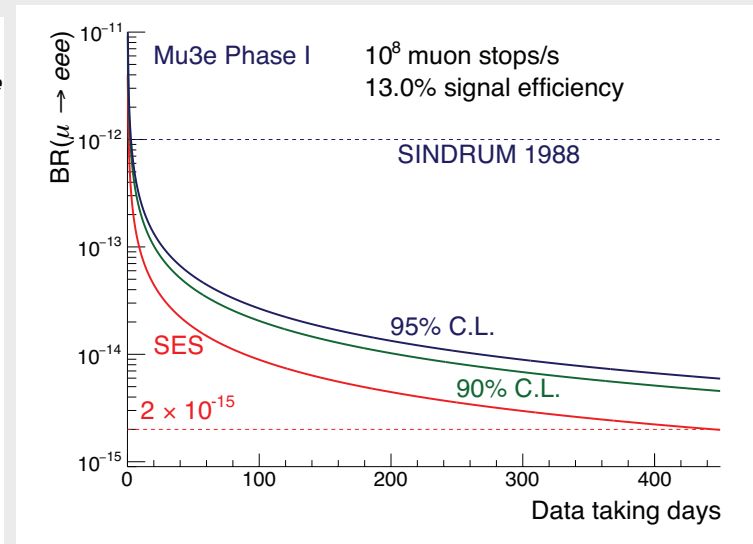
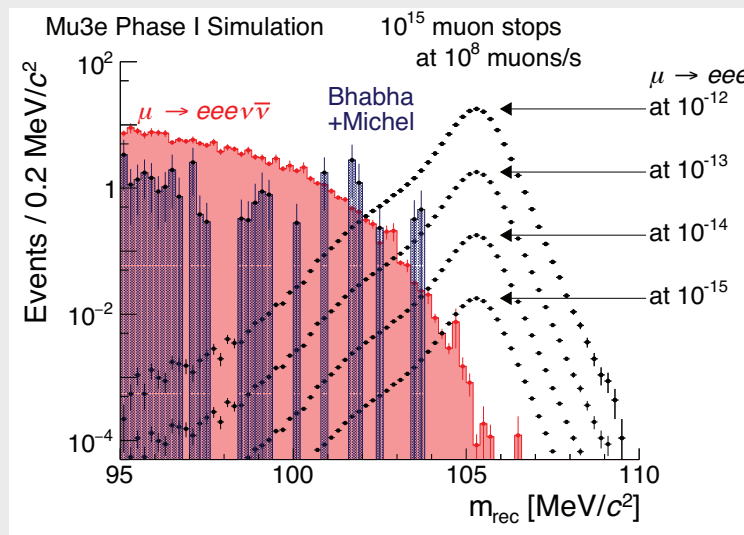
- $\mu \rightarrow e\gamma$ : back-to-back electron and photon
  - $B \propto \Gamma_{\mu}^2 \cdot \delta E_e \cdot (\delta E_{\gamma}^2) \cdot \delta T_{e\gamma} \cdot (\delta \theta_{e\gamma}^2)$
  - converting  $\gamma \rightarrow e^+e^-$  improves resolutions but there are limits: converters imply straggling in  $dE/dx$ , etc.
  - active target for vertex? fundamentally new approach?

# New Ideas in Decay Experiments

- $\mu \rightarrow 3e$ :

2204.00001

- $\mu \rightarrow 3e\bar{\nu}_e\nu_\mu$  is main background



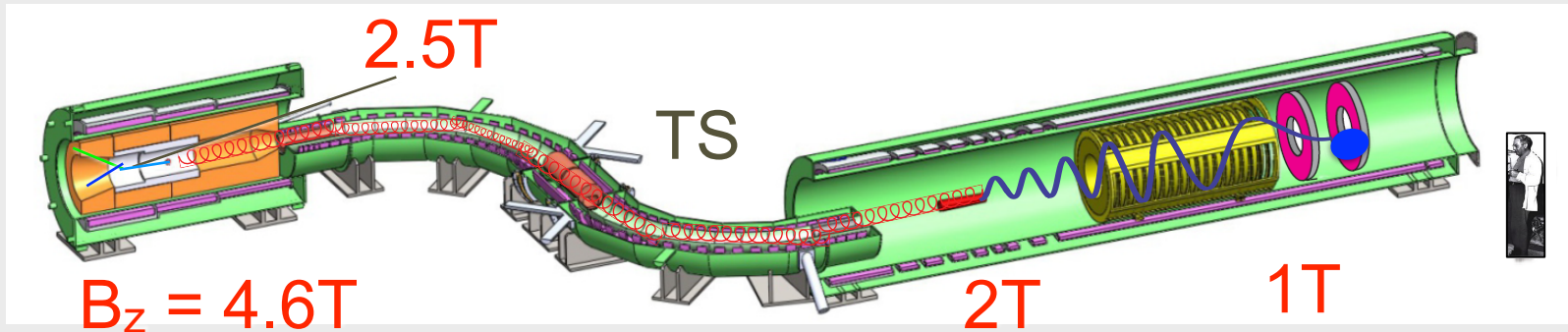
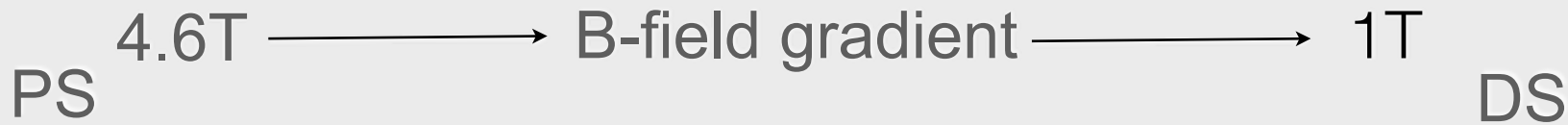
- target sensitivity of  $10^{-16}$  at HiMB,  $2e9 \mu/s$
- with more rate, harder cuts? new detector ideas?

# Capture Experiment

- $\mu^- N \rightarrow e^- N$  ( $N = {}^{27}\text{Al}_{13}$  for Mu2e)
- brings a muon near an atomic nucleus where it falls into a muonic 1s state: monoenergetic electron just below  $m_\mu$
- for several generations of experiments, including Mu2e/COMET, the beam design was driven by radiative pion capture (RPC):
  - $\pi^- N \rightarrow \gamma N', \gamma \rightarrow e^+ e^-$  at the signal energy
  - Mu2e/COMET use a *pulsed* beam and use the 26 ns pion lifetime vs  $2.2 \mu\text{s}$  muon lifetime to “wait out” RPC



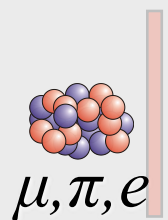
# Mu2e Muon Beam: Three Solenoids and Gradient



8 kW

- Target protons at 8 GeV inside superconducting solenoid
- Capture muons and guide through S-shaped region to Al stopping target
- Gradient fields used to collect and transport muons

Al

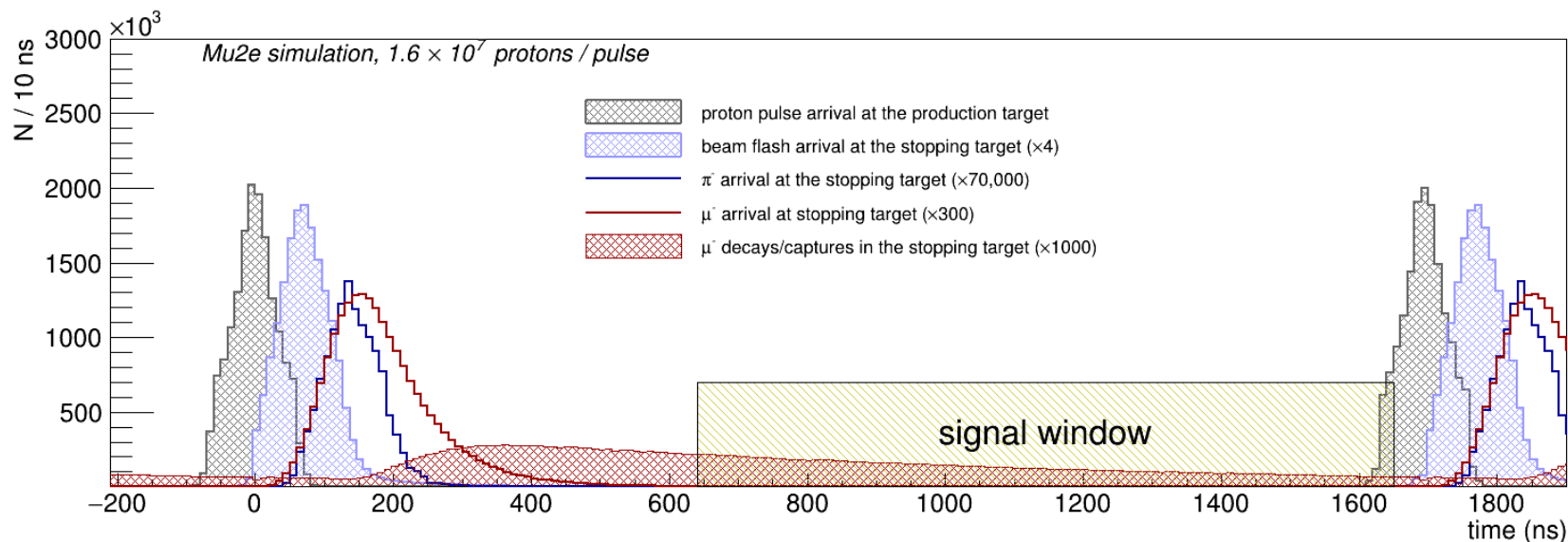


Muon K.E ~ 7 MeV  
muons range out by  $dE/dx$   
in Aluminum

# Mu2e/COMET timing scheme

- Complicated plot, but similar for Mu2e/COMET
  - pulse at beginning
  - wait for pions to decay
  - open a signal window

Mu2e is  $\mu^-Al \rightarrow e^-Al$

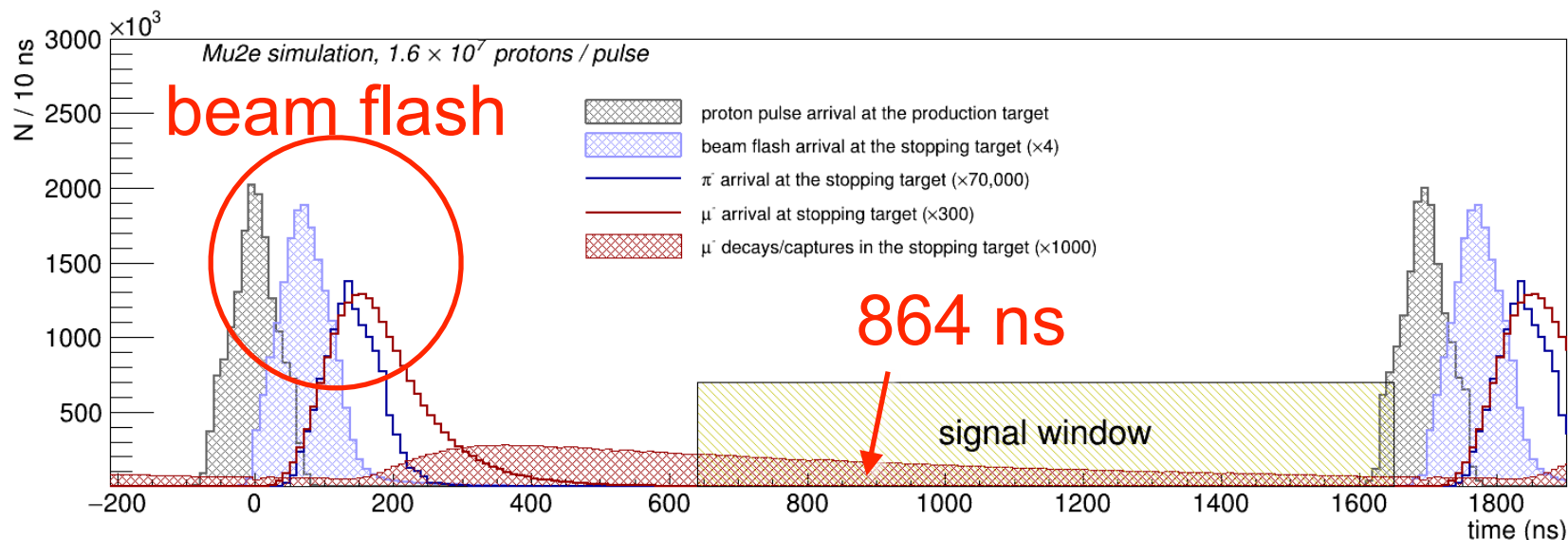


# Mu2e/COMET timing scheme

- Complicated plot, but for both Mu2e/COMET
  - pulse at beginning
  - wait for pions to decay
  - open a signal window

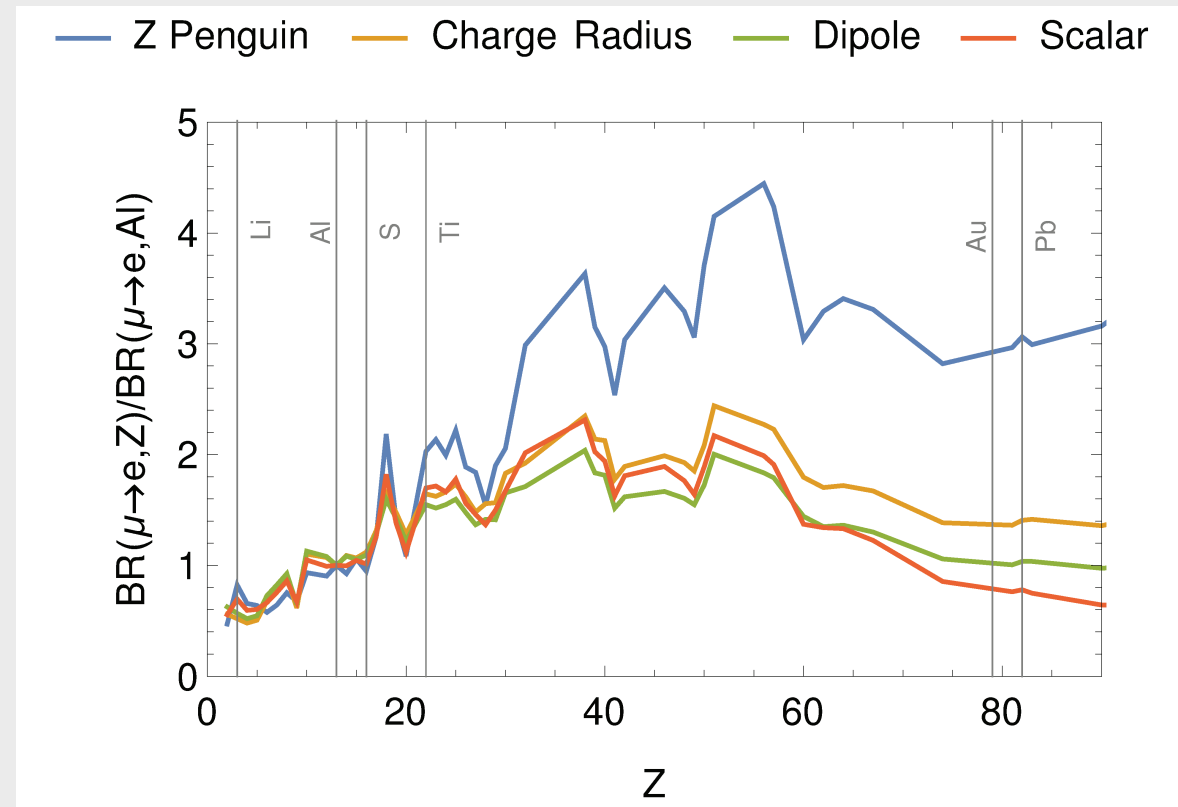
Mu2e is  $\mu^- \text{Al} \rightarrow e^- \text{Al}$

864 ns  $\mu^- \text{Al}$  atom lifetime  
well after beam flash



# Conversion at Higher Atomic Number

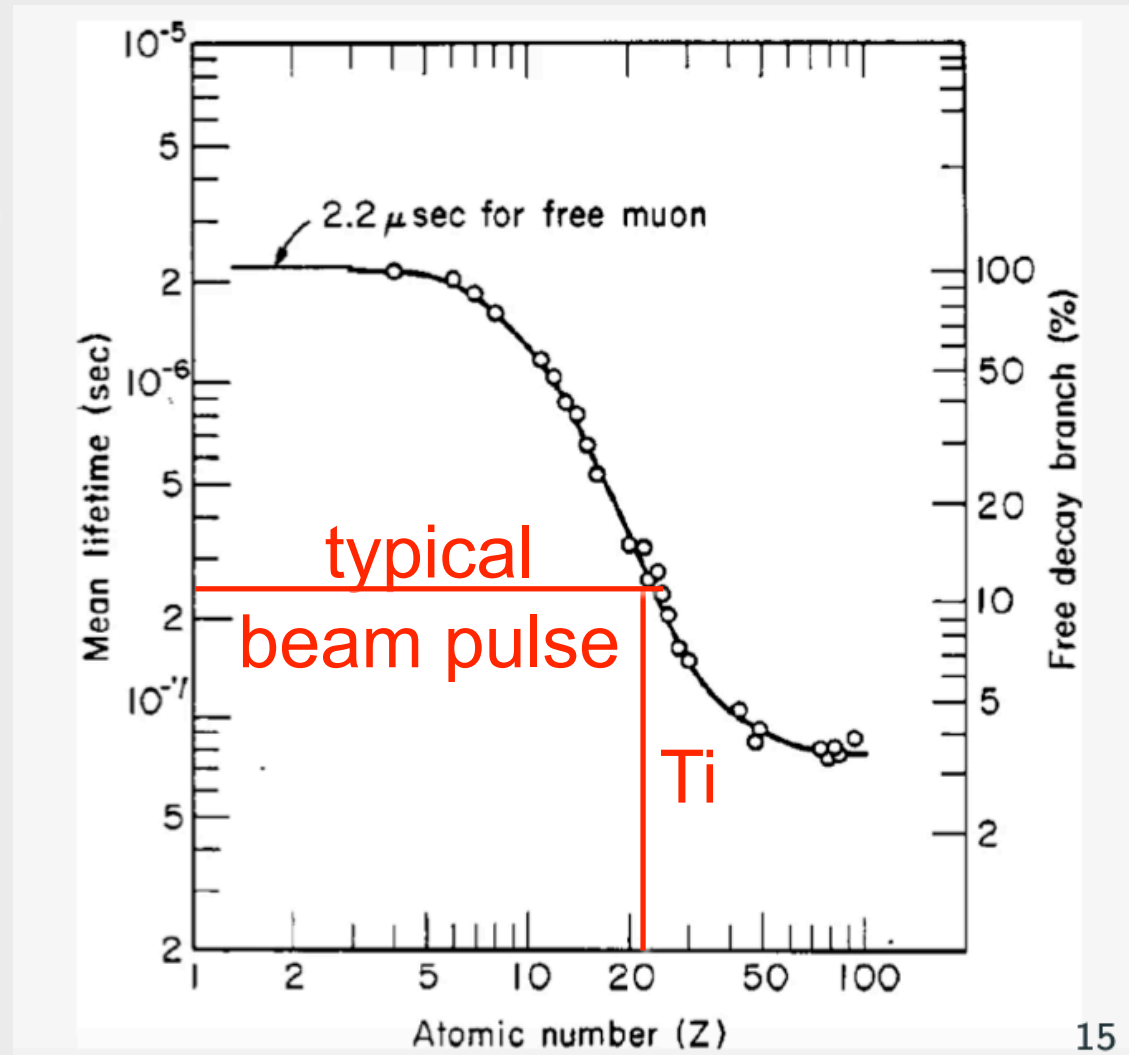
- Model Discrimination and Possibly Larger Signal at high  $Z$
- if Mu2e sees a signal, this is the obvious next step
- if not, we should try for another  $\times 10-100$  better constraints



adapted from V. Cirigliano, B. Grinstein, G. Isidori, M. Wise **Nucl.Phys.B728:121-134,2005**

# Limitation of Mu2e Method

- A beam pulse is  $\sim 250$  ns FWHM
- You can't do an experiment inside the debris from the beam pulse
- And therefore you can't go to high  $Z$ : Ti about limit



# New Facility: AMF

hep-ex 2203.08278

- The “Advanced Muon Facility” would use PIP-II to enable
  - ***CLFV in all three muon modes: world-leading facility***
    - two new small rings for  $\mu N \rightarrow eN$  at high  $Z$  and additional x100 in rate
      - with a possible DM experiment
    - x100-1000 more beam for  $\mu \rightarrow e\gamma$  and  $\mu \rightarrow 3e$  than are possible at PSI
  - Possible muonium-antimuonium and muon EDM

# Conversion Experiment

- Like Mu2e, target beam inside a solenoid, but at 100 kW - 1MW vs. Mu2e's 8 kW
  - Mu2e-II at 100 kW, but not high Z
- Rebunch PIP-II beam in a “compressor ring”
- next, bring to proton target
- Transfer to a fixed-field alternating (FFA) gradient ring
  - phase rotates to slow higher momentum muons, accelerate lower momentum muons.
  - pion contamination from RPC greatly reduced while muons are circulating in ring
  - Extract pure, cold muon beam to detector

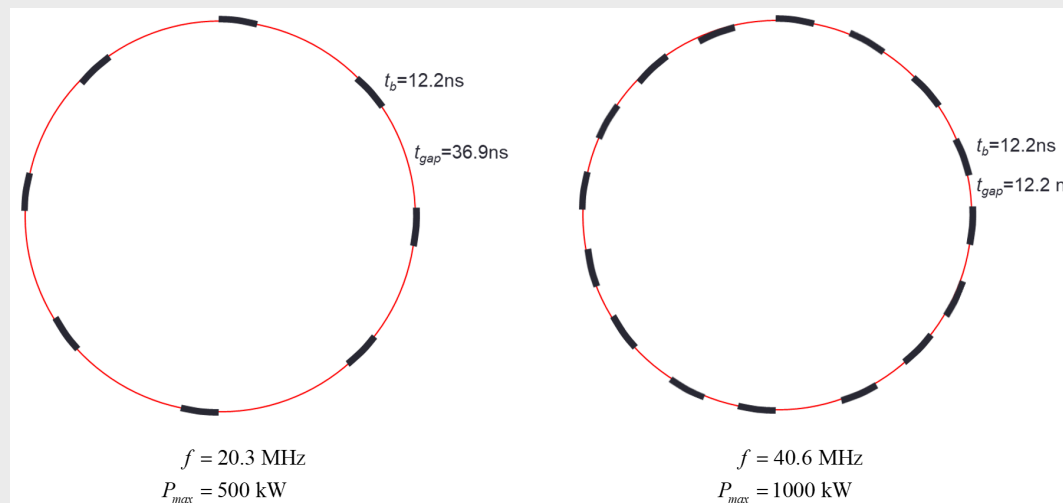
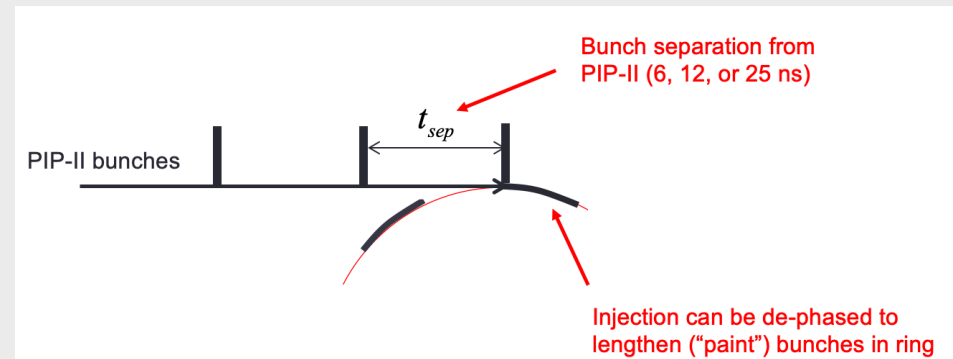
the FFA for conversion from Japan:

<https://indico.fnal.gov/event/46669/contributions/203147/attachments/138314/173082/>

PRISM\_CLFV\_10122020\_Pasternak.pdf

# Beam for Conversion

- Compressor Ring:
  - 500 kW achievable;
    - 12 ns kickers are the limit for 1 MW



| Description | Protons-Per-Pulse    | Pulse Spacing (ns) | Repetition Rate (Hz) |
|-------------|----------------------|--------------------|----------------------|
| AMF         | $7.8 \times 10^{13}$ | 24                 | 100                  |
| Dark Matter | $6.2 \times 10^{14}$ | 196                | 100                  |



# Production Solenoid

- Mu2e at 8 kW requires a complicated heat and radiation shield to keep superconductor from quenching; COMET (Japanese version) proposes 56 kW
- Mu2e-II Conceptual designs exist for 100 kW
  - “moving mass” target and thicker shield
- AMF would provide world-class physics at high-Z; 100 kW is just the first step
- Various ideas for 1MW have been promoted
  - $\nu$  targets for DUNE get to 1MW...why so hard?
  - *not inside a superconductor: MuCol is working on this*

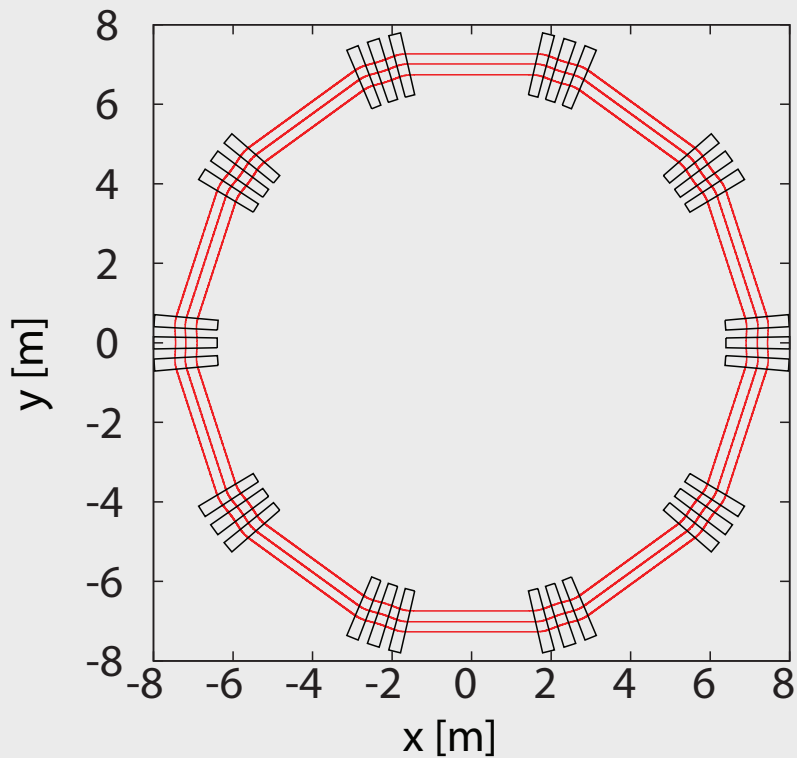
# FFA

- PRISM (Phase Rotated Intense Source of Muons)

(arXiv:1310.0804 [physics.acc-ph])

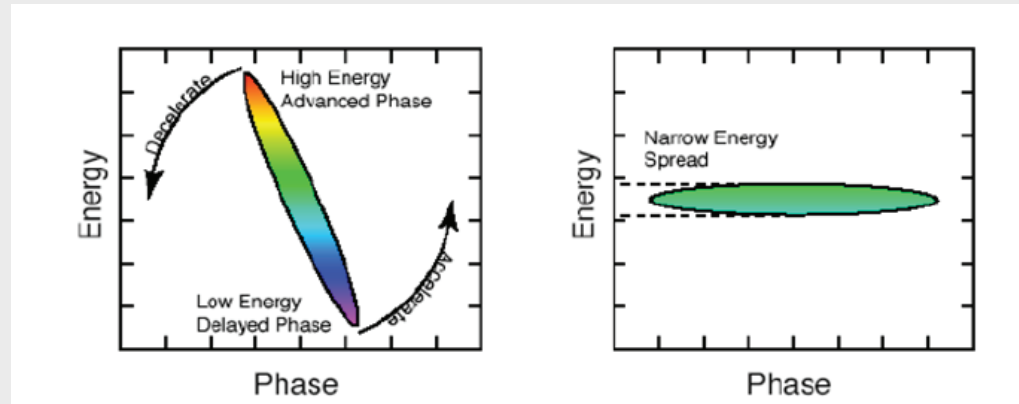
- EMMA, MuCol studies at higher momenta

<https://indico.psi.ch/event/7313>



~ 40 MeV/c central momentum; we actually want lower, ~15 MeV/c

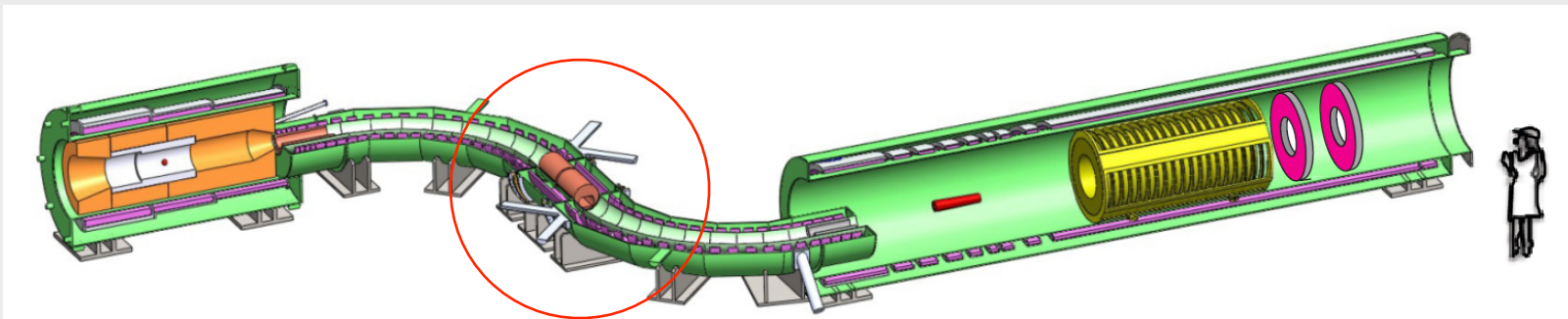
R. Bernstein, FNAL



6 cell  
demonstrator  
at Osaka

# Beam for Decay Experiments

- Two Options:
  - a conventional stopped muon beam at 1MW based on PSI but a new, dedicated facility for CLFV.
  - use same production system as for capture experiments, but flip sign of selected muons; rotate central collimator and get  $\mu^-$  (charged particles traveling around a curved solenoidal field see effective centrifugal force)
  - will require detailed MCs to choose



# Other ideas: Beam for Decay Experiments

- Reversing sign of solenoids not easy; initial proton beam doesn't reverse charge and therefore follows a different trajectory inside solenoid, misses target, and then other "bad things". But we could take beam out other end of solenoid...
- But is it possible to select muon momentum by "waiting?" Slowest, lowest energy muons are last and those are best.
  - enough beam to make this work, preliminary simulations indicate could work
- Active muon channel: *cooling ideas used in MuCol designs*
- Many ideas and will take a lot of work to sort through. Surface muons are conceptually simplest but we should be able to do better




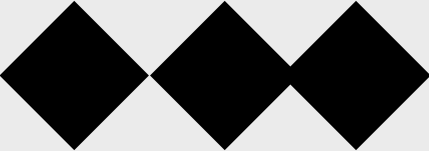
# Existing Attempts on Targeting

<https://aip.scitation.org/doi/pdf/10.1063/1.3399332>

- Problem with a long history and a lot of thought:
  - liquid Hg in 1990's, moving away from that
  - MERIT experiment
- Tues AM session on Targeting:
  - Mori, Ximenes, Densham, Carrelli talks at this meeting

Calviani: [https://indico.cern.ch/event/1016248/contributions/4282384/attachments/2215324/3752155/MCa\\_MUC\\_Targetry\\_25Mar2021\\_v1.pdf](https://indico.cern.ch/event/1016248/contributions/4282384/attachments/2215324/3752155/MCa_MUC_Targetry_25Mar2021_v1.pdf)

# Beam Technical Challenges

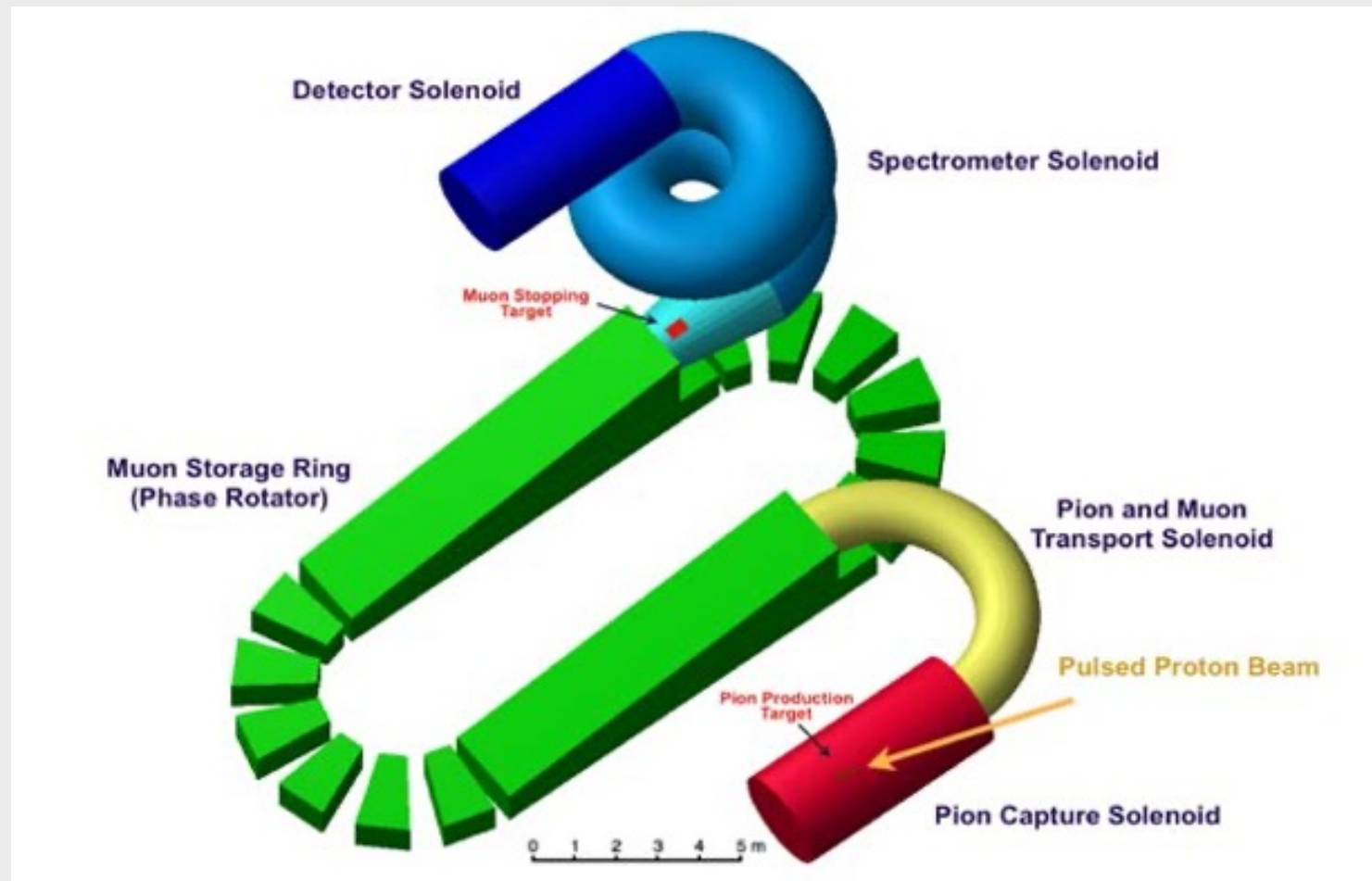
- Things that are very hard that we know how to do:
  - stopped muon beam at 1MW 
  - compressor ring 
  - FFA 
- Things that are very hard that we don't know how to do
  - 1MW target inside a solenoid 

# Detector Technical Challenges

- $\mu^- N \rightarrow e^- N$ 
  - halving momentum resolution on signal  $e^-$ 
    - not just making Mu2e straws thinner
    - rethink detector design
  - dominant background (we think) will be cosmic ray production of electrons in signal region
    - a CRV x100-x1000 better than Mu2e

# One Concept for $\mu^- N \rightarrow e^- N$

- Spiral Detector Solenoid greatly reduces rate seen by detector, opens up new detector designs (from PRISM/PRIME)



ENIGMA  
experiment



# Overlaps

- Targeting inside a solenoid at up to 1MW
  - Does it make sense to use MuCol ideas about resistive/superconducting solenoids for this program?
- Is an FFA the right answer, or are there cooling ideas to provide a better muon beam?
  - are there other ideas? PRISM is a large emittance beam in an FFA, is that the best option?
    - FFA solves a lot of problems: serves as a storage ring to let  $\pi$ 's decay and we never see the beam flash
- Can this program either be a demonstrator for or a customer of a muon collider facility?

# Summary

- Muon-based Charged Lepton Flavor Violation provides powerful searches and constraints for BSM physics
- A new facility at FNAL could provide all three muon channels,  $\mu \rightarrow e\gamma$ ,  $\mu \rightarrow 3e$ , and  $\mu N \rightarrow eN$  with orders of magnitude more data and open new possibilities in  $\mu N \rightarrow eN$  at high  $Z$ 
  - plus a dark matter experiment and other muon measurements not discussed.
  - technical challenges directly related to muon collider R&D:
    - solenoid, targeting, and FFA are common
    - We hope for P5 to recommend design of the program with submission to next P5