

Measuring $\pi_{e3(\gamma)}$, the pion beta decay

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Topics discussed in this talk

PiBeta (and PEN) goals and design

Experimental method: PiBeta

Apparatus and measurement method

Calorimeter genesis

Calorimeter triggers

Active target

Detector performance and measurements

Radiative decays

Invariant mass and pileup suppression

Photoneutron reactions

More on pileup suppression



Summary of PiBeta and PEN goals

Goals of the **PiBeta** experiment (data runs 1999-2004):

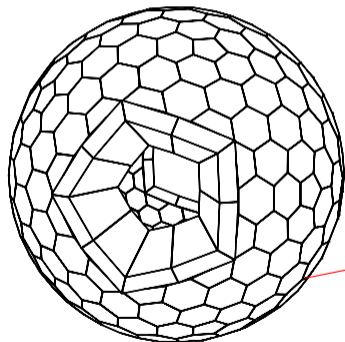
Decay	$\mathcal{O}(\text{B.R.})$	Goal $\delta R/R$	Attendant SM limits
$\pi_{e3(\gamma)} : \pi^+ \rightarrow \pi^0 e^+ \nu_e(\gamma)$	$R_{e3(\gamma)}^\pi \sim 10^{-8}$	$\sim 5 \times 10^{-3}$	CKM V_{ud} & related
$\pi_{e2\gamma} : \pi^+ \rightarrow e^+ \nu_e \gamma$	$R_{e2\gamma}^\pi \sim 10^{-7}$	$\leq 1 \times 10^{-2}$	$F_A^\pi, F_V^\pi, F_T^\pi$; χ PT l.e.c.
RMD: $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu \gamma$	$R_{e2\gamma}^\pi \sim 10^{-3}$	$\leq 1 \times 10^{-2}$	Michel param.: $\bar{\eta}$

Goals of the **PEN** experiment (data runs 2008-2010):

Decay	$\mathcal{O}(\text{B.R.})$	Goal $\delta R/R$	Attendant SM limits
$\pi_{e2(\gamma)} : \pi^+ \rightarrow e^+ \nu_e(\gamma)$	$R_{e2(\gamma)}^\pi \sim 10^{-4}$	$\sim 5 \times 10^{-4}$	lept. univ.; non- $V-A$, ...
$\pi_{e2\gamma} : \pi^+ \rightarrow e^+ \nu_e \gamma$	$R_{e2\gamma}^\pi \sim 10^{-7}$	$\sim 1 \times 10^{-2}$	improve F_V^π & limit on F_T^π
RMD: $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu \gamma$	$R_{e2\gamma}^\pi \sim 10^{-6}$	$\sim 1 \times 10^{-2}$	improve $\bar{\eta}$

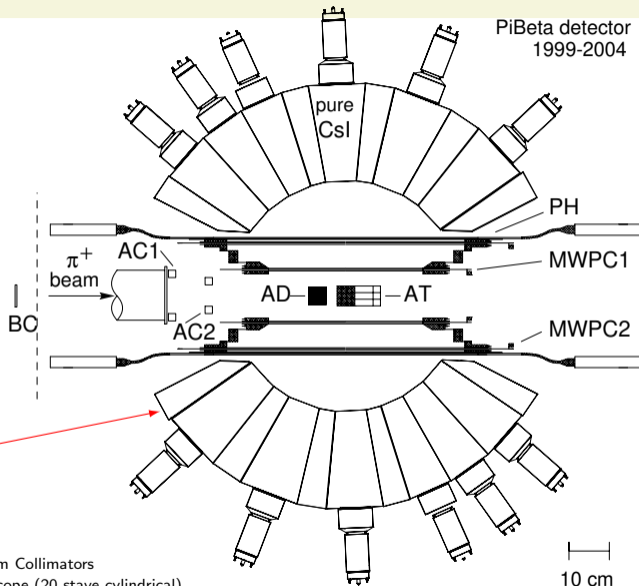
The PiBeta apparatus

- π E1 beam at PSI
- stopped π^+ beam
- 9-elem. active tgt
- 240-elem. $12X_0$ spherical pure-CsI calo.
- tightly controlled temp/humidity/gains
- central tracking
- beam tracking
- fast-digitized wf's

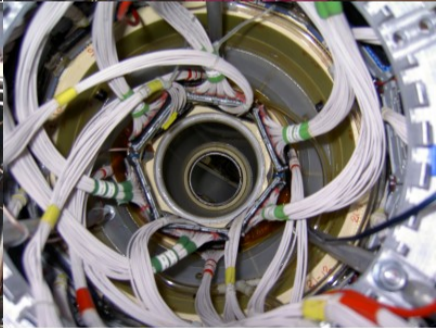
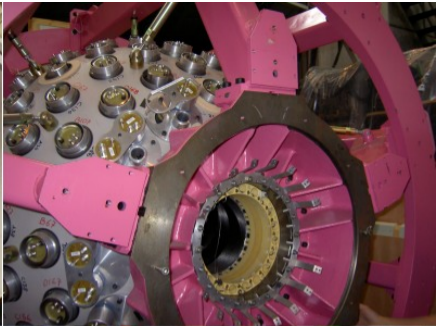
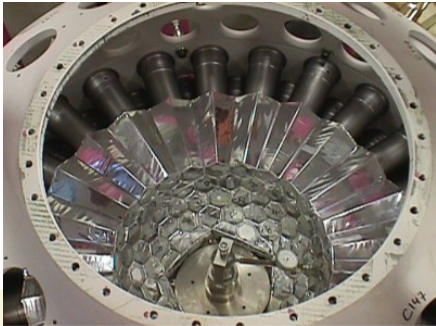


BC: Beam Counter
AD: Active Degradar
AT: Active Target

AC1,2: Active beam Collimators
PH: Plastic Hodoscope (20 stave cylindrical)
MWPC: Multi-Wire Proportional Chamber (cylindrical)



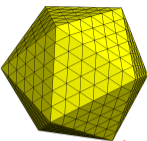
A few photos of the PiBeta apparatus:



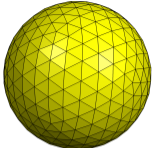
PiBeta Calo shapes: geodesic polyhedra & triangulation of the sphere



Icosahedron

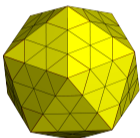


6-frequency subdivision

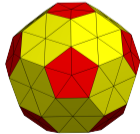


Vertices projected onto sphere

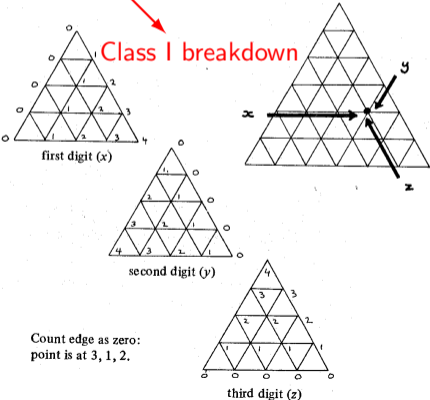
But, we don't want triangular pyramids (sharp corners \Rightarrow nonuniform light collection) — merge triangles into hexagons and pentagons.



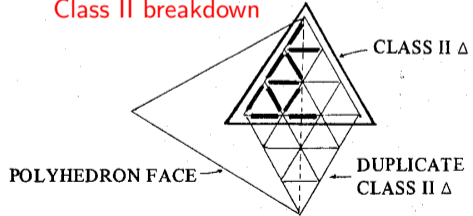
subdivided



truncated icosahedron



Class II breakdown

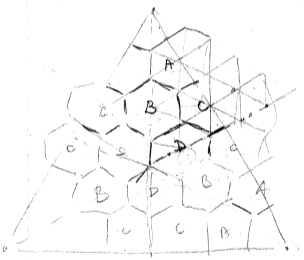


Selected subdivision: 10-frequency Class II

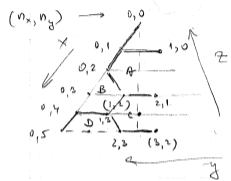
SELECTED

25 Nov 1990

The last option ICOSA 10 → Class II Meth I



12 Pentagons	12
20x Hex A x 3	60
20x Hex B x 3	60
20x Hex C x 3	60
20x Hex D x 3	60
<u>Total</u>	<u>252</u>
ns. 272 for 90 Class I	



(0,1 - 1,0)	0.1366
(0,1 - 0,2)	0.1271
(0,2 - 1,2)	0.1311
(1,2 - 2,1)	0.1479
(1,2 - 1,3)	0.1410
(1,3 - 0,4)	0.1438
(0,4 - 0,5)	0.1359
(1,3 - 2,3)	0.1428
(2,3 - 3,2)	0.1523

Remove:

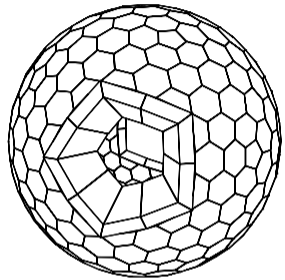
pentag x 1	.00255
A x 5	.01830
B x 5	.01980
C x 2,5	.02135
<u>Σ</u>	<u>.0517</u>
Veto: D 10	.041
+ C 5	.02135
<u>Σ</u>	<u>.0623</u>

Remains 0.77 of 4π

Total # of elem:	252
	<u>- 32</u>
	220
Detector	190
Veto elem	<u>30</u>

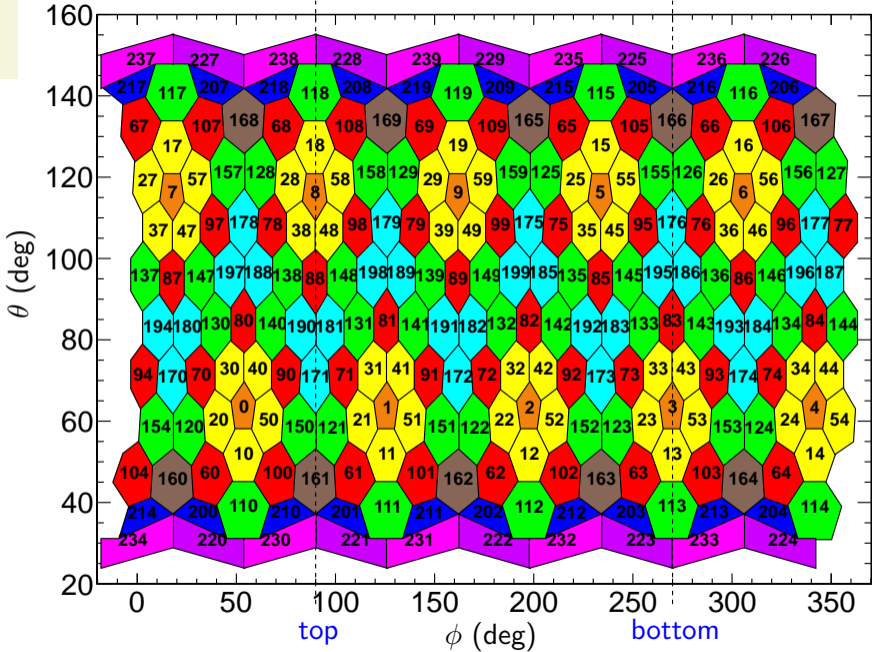


PiBeta Calo map in the Mercator projection



Accepted crystals met minimum criteria for pion beta decay measurement.

Csl module calibration details posted on PiBeta website.



Pion beta decay kinematics

The $\pi^0 \rightarrow \gamma\gamma$ signal is well separated from all backgrounds;

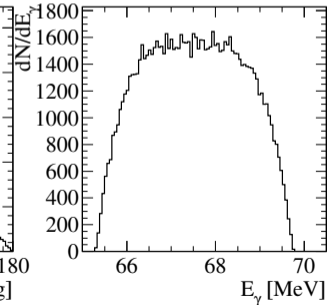
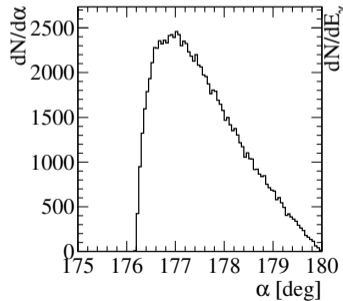
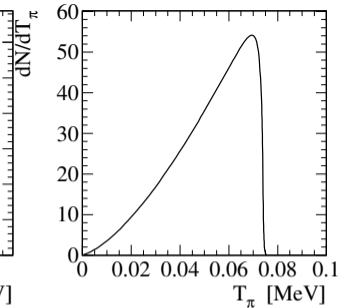
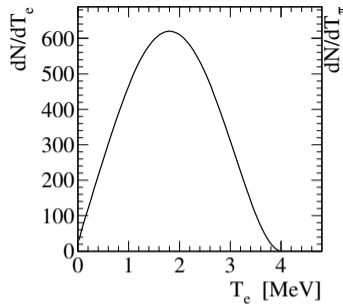
Even so, impossible to isolate without significant calo segmentation!

Challenge: detect the decay positron!

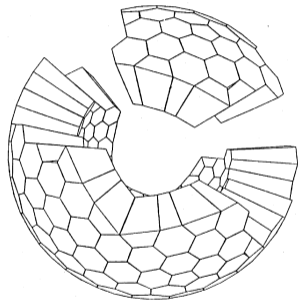
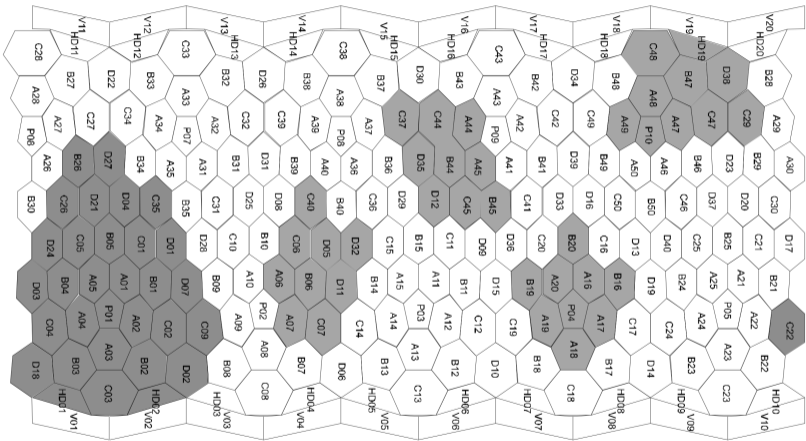
This has led to evolution in the design of PiBeta targets.

Minimize passive material!

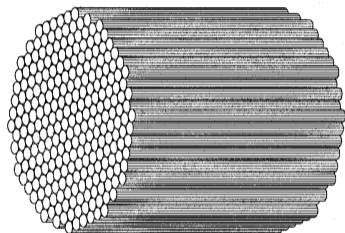
Enlarge AT components to optimize energy resolution.



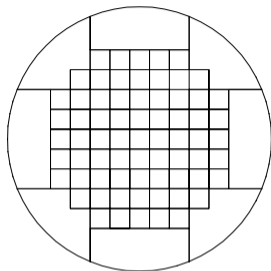
Clustering for the 2-arm HI trigger



Active target evolution

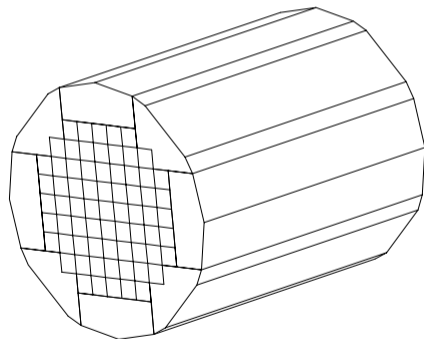


Concept 0.5



0 6mm

Diameter: 40 mm;
Length: 50 mm.



AT 1.0: 69 fibers $2.76 \text{ mm} \times 2.76 \text{ mm}^2$; 0.12 mm acrylic cladding

The PiBeta 9-element AT

Minimum segmentation to handle the rate.

Ultrafast \varnothing 10 mm Hamamatsu PMTs and custom made dividers at UVA (also for calo PMTs).

Radiation damaged; replaced after \sim 3 months in beam.

Single piece in PEN:

$$\sigma \simeq 4.5\% \text{ for } 4.1 \text{ MeV } \mu \text{ line}$$

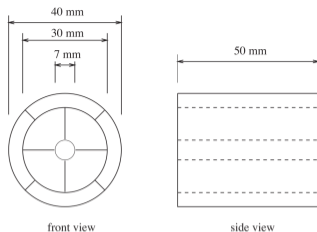


Fig. 12. A sketch of the regular PIBETA active target, composed of nine detectors. The segment sizes are chosen to balance the scaler counting rate.



Fig. 13. A photograph of the regular PIBETA active target. Acrylic tapered light guides are glued to nine optically isolated target segments.

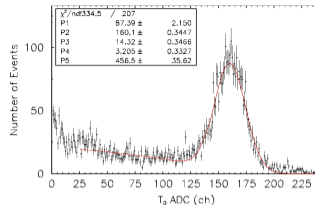


Fig. 14. The pulse-height spectrum of pions stopping in the central active target segment. The peak-to-tail area ratio depends on the beam divergence.

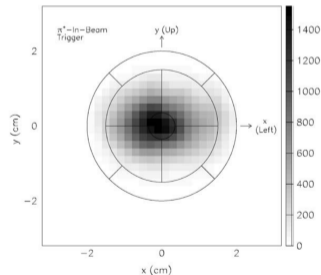
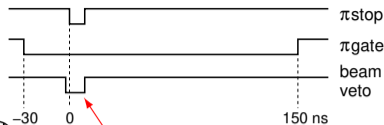
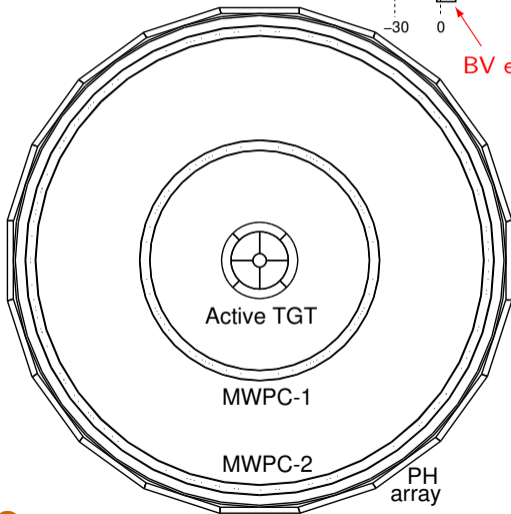


Fig. 15. Reconstructed two-dimensional shape of the π^+ beam superimposed on an outline of the segmented active target. Data for target counting rates are collected during one 48 h long series of runs.

PiBeta central detector region

TGT stopping rate: $\geq 10^6 \pi/s$;
9-pc. AT: 5 inner (fiducial stop)
4 guard/tracking ring;



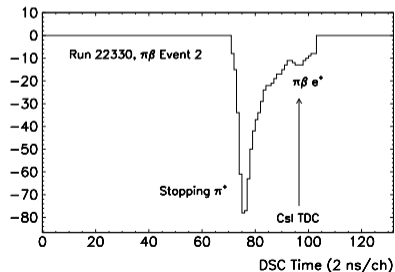
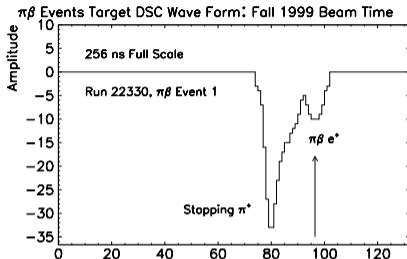
BV eliminated in PEN!

Beam $p \simeq 113 \text{ MeV}/c$
(to achieve π_{stop} rate)

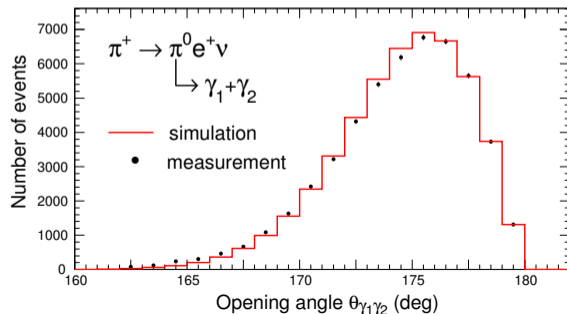
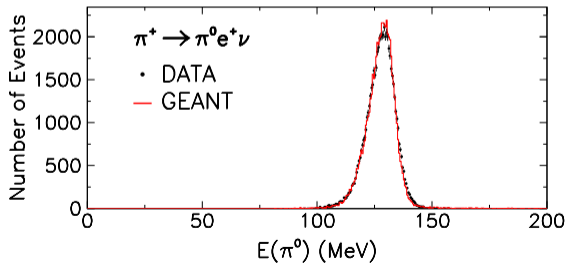
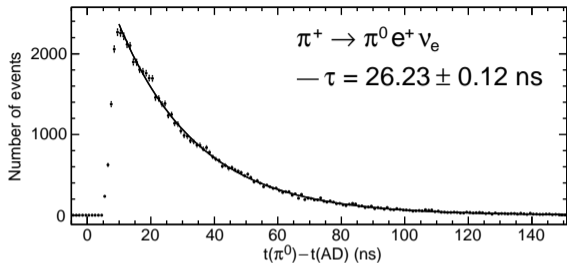
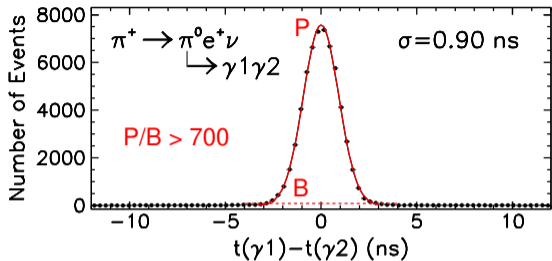
9-piece AT provides rudimentary beam stop tracking

Note: AT was replaced for each annual run due to radiation damage.

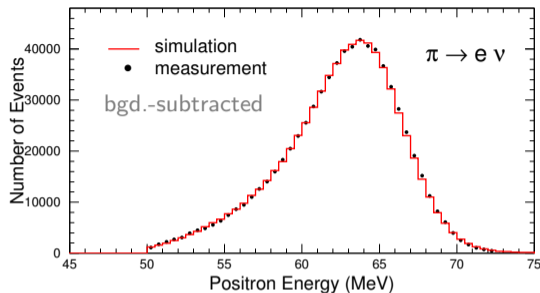
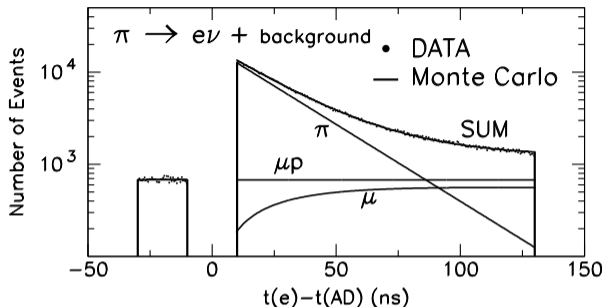
Digitized AT signal waveforms:



Key PiBeta spectra: π_{e3} decay (2004)

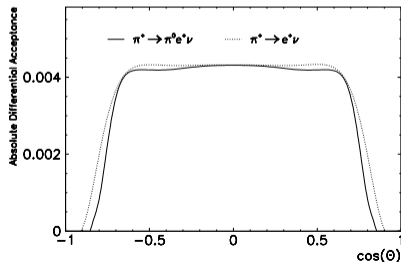


PiBeta normalization spectra: π_{e2} decay (2004)



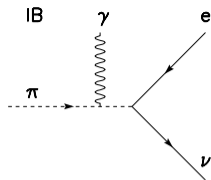
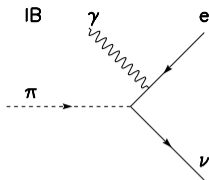
Notes:

- π_{e3} signals are clean, w/low bgd. levels (previous slide);
- large background in π_{e2} from $\pi \rightarrow \mu \rightarrow e$ decay chain,
- ... also from **pile-up** μ 's in target;
- ~ 15 ns vetoed around $t = 0$ to suppress prompt hadr. bgd.;
- excellent agreement with Geant3 MC simulations;
- π_{e2} : large subtraction of $\pi \rightarrow \mu \rightarrow e$ events below ~ 55 MeV;
- well matched acceptances for π_{e3} , π_{e2} decays (shown);
- even closer for π_{e2} and $\pi \rightarrow \mu \rightarrow e$ channels (not shown).



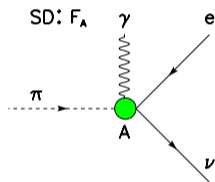
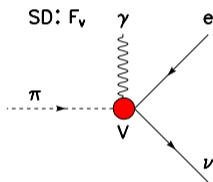
Physics of $\pi^+ \rightarrow e^+ \nu \gamma$
(RPD):

QED IB terms:

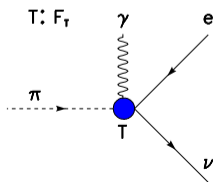


and SD V, A terms:

SM



A tensor interaction, too?



Exchange of $S=0$ leptoquarks
P Herczeg, PRD 49 (1994) 247



The $\pi \rightarrow e\nu\gamma$ amplitude and FF's

The IB amplitude (QED **uninteresting!**):

$$M_{\text{IB}} = -i \frac{eG_F V_{ud}}{\sqrt{2}} f_\pi m_e \epsilon^{\mu*} \bar{e} \left(\frac{k_\mu}{kq} - \frac{p_\mu}{pq} + \frac{\sigma_{\mu\nu} q^\nu}{2kq} \right) \times (1 - \gamma_5) \nu.$$

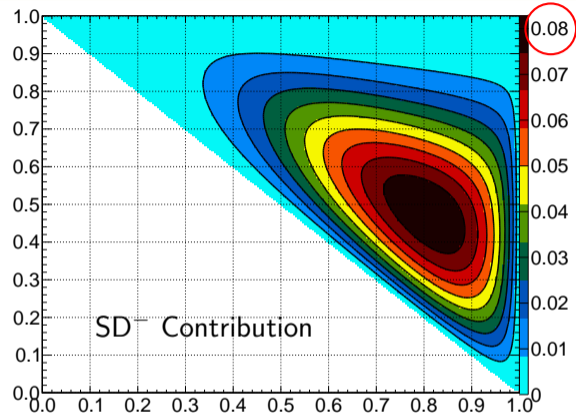
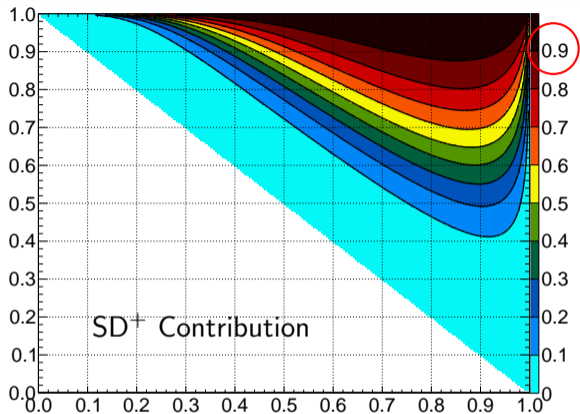
The structure-dependent amplitude (**interesting!**):

$$M_{\text{SD}} = \frac{eG_F V_{ud}}{m_\pi \sqrt{2}} \epsilon^{\nu*} \bar{e} \gamma^\mu (1 - \gamma_5) \nu \times [F_V \epsilon_{\mu\nu\sigma\tau} p^\sigma q^\tau + iF_A (g_{\mu\nu} pq - p_\nu q_\mu)].$$

The SM branching ratio (with $x = 2E_\gamma/m_\pi$; $y = 2E_e/m_\pi$),

$$\begin{aligned} \frac{d\Gamma_{\pi e 2\gamma}}{dx dy} = & \frac{\alpha}{2\pi} \Gamma_{\pi e 2} \left\{ IB(x, y) + \left(\frac{m_\pi^2}{2f_\pi m_e} \right)^2 \right. \\ & \times [(F_V + F_A)^2 SD^+(x, y) + (F_V - F_A)^2 SD^-(x, y)] \\ & \left. + \frac{m_\pi}{f_\pi} [(F_V + F_A) S_{\text{int}}^+(x, y) + (F_V - F_A) S_{\text{int}}^-(x, y)] \right\}. \end{aligned}$$

Best sensitivity for SD terms



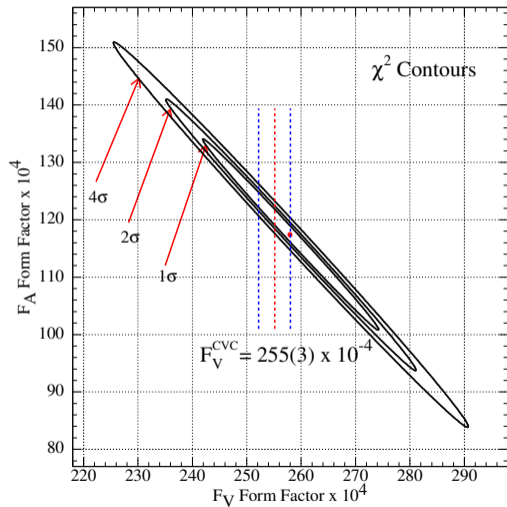
SD⁺ region favors high energy e⁺ and γ 's.

High energy track pairs occur with large opening angles.

Large solid angle coverage required \Rightarrow good match to PEN!

SD⁻ is notoriously hard to measure directly.

Pion FF values and precision improvement factors (pif) over previous work:



Observable	(pif)
$F_V = 0.0258(17)$	$(8\times)$
$F_A = 0.0119(1)_{(F_V^{CVC})}^{\text{exp}}$	$(16\times)$
$a = 0.10(6)^*$	(∞)
$-5.2 < 10^4 \cdot F_T < 4.0$	90% c.l.
$B_{\pi e 2\gamma} = 73.86(54) \times 10^{-8} \dagger$	$(17\times)$

* $a \dots q^2$ dependence of F_V

† for $(E_\gamma > 10 \text{ MeV}, \text{ and } \theta_{e\gamma} > 40^\circ)$

[Bychkov et al., PRL 103, 051802 (2009)]

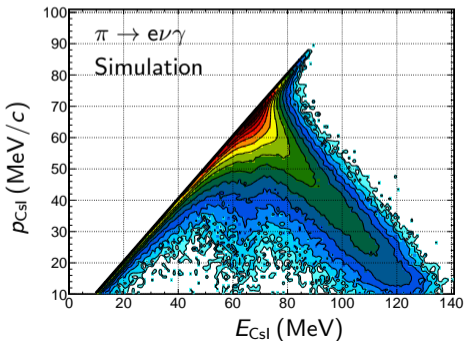
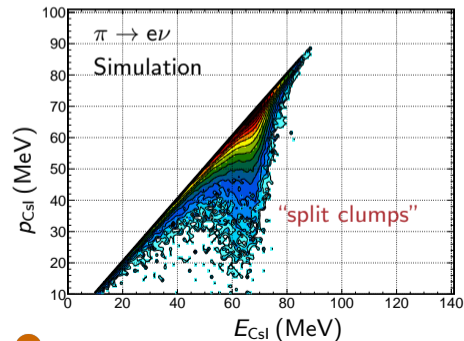
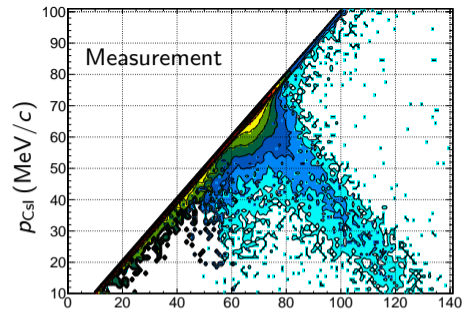
Identifying hard radiative decays in PEN

PEN indirectly measures p_ν in $\pi \rightarrow e\nu\gamma$

$$\vec{p}_e + \vec{p}_\gamma = -\vec{p}_\nu \equiv \vec{p}_{\text{obs}}; \text{ with:}$$

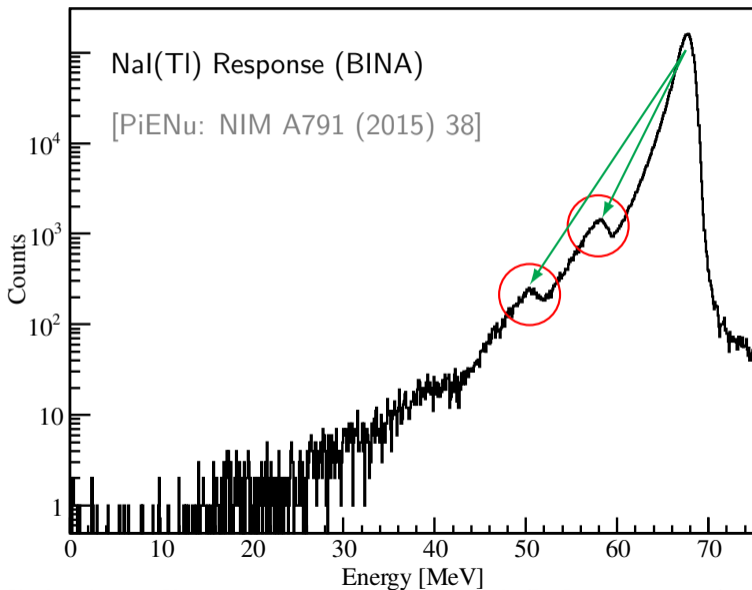
$$E_e + E_\gamma \equiv E_{\text{obs}}$$

$$E_{\text{obs}} + p_{\text{obs}}c = m_\pi c^2$$



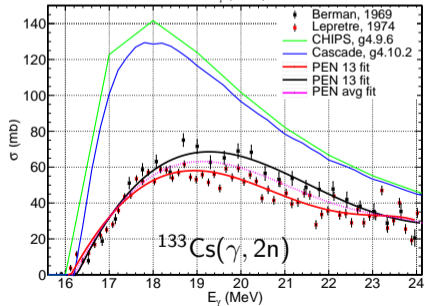
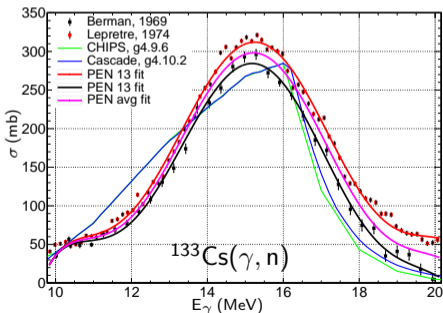
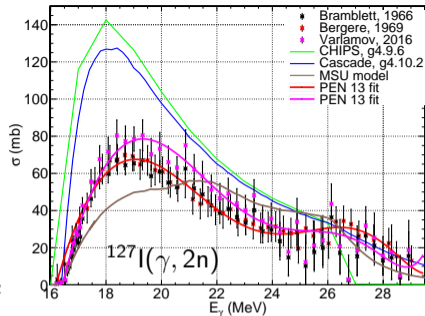
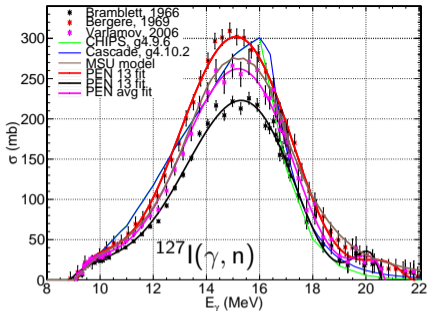
Tail fraction: photoneutron reactions

(γ, n) reactions on calorimeter nuclei, Cs and I, shift counts from the main peak to the “tail” region if the neutron is undetected.



Photoneutron cross sections, $\sigma(\gamma, xn)$

- ▶ Many inconsistencies among the data sets;
- ▶ Geant4 descriptions inadequate, often miss data by a wide margin.
- ▶ PEN was forced to implement its own parametrization in Geant4 (C. Glaser).
- ▶ This procedure works at the PEN goal precision, but would be inadequate at higher precision.



More on pileup suppression and $\pi_{e2}/\pi_{\mu2}$ discrimination

- ▶ The most potent weapon: vetoing events with prior beam pions/muons for N muon lifetimes is **not practical in the PiBeta phase** of PiONEER!
- ▶ Meaningful review of cuts and techniques used in PEN requires a separate discussion.
- ▶ We have found that a forward beam counter (BC), active degrader (AD), central tracking (MWPC), and beam tracking (mTPC) all are essential.
- ▶ We must examine how much of this ATAR can replace, and whether or not ATAR brings new compromises.
- ▶ It is important to see how some of those functions will be replaced in the PiONEER paradigm.
- ▶ Most important of all: the pion beta phase still requires precise π_{e2} normalization!

