

The direct photon puzzle and the weak magnetic photon emission from QGP

arXiv: [2302.07696](https://arxiv.org/abs/2302.07696)

Jing-An Sun and Li Yan
Fudan University
jasun22@m.fudan.edu.cn



復旦大學



Outline

○ Introduction:

- direct photon puzzle
- the magnetic field in heavy-ion collisions.

○ Methodology:

- an external weak magnetic field +
- a “tilted” fireball configuration.

○ Results:

- the elliptic flow of direct photon
- the magnetic field at early stages.

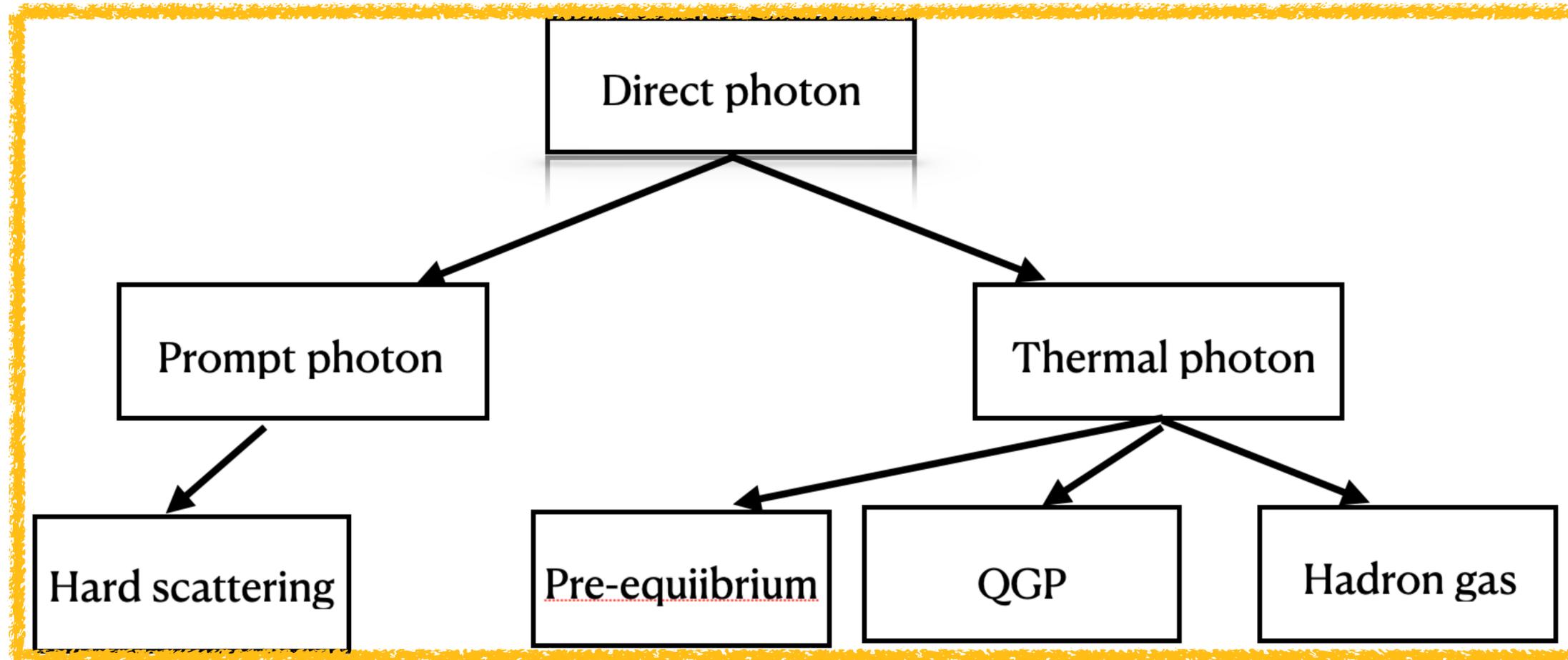
○ Summary and Outlook



Direct photon

○ Direct photons

- **directly from a particle collision**



- **Large mean free path.**
- A perfect **“historian”**.
- A **“clean”** probe.

Gabor David, arXiv:1907.08893v2 [nucl-ex]

Chapline G F, Kerman A K. 1978.

Chin S A. Phys. Lett. B, 1978, 78: 552-555.

Anishetty R, Koehler P, McLerran L. Physical Review D, 1980,22(11): 2793

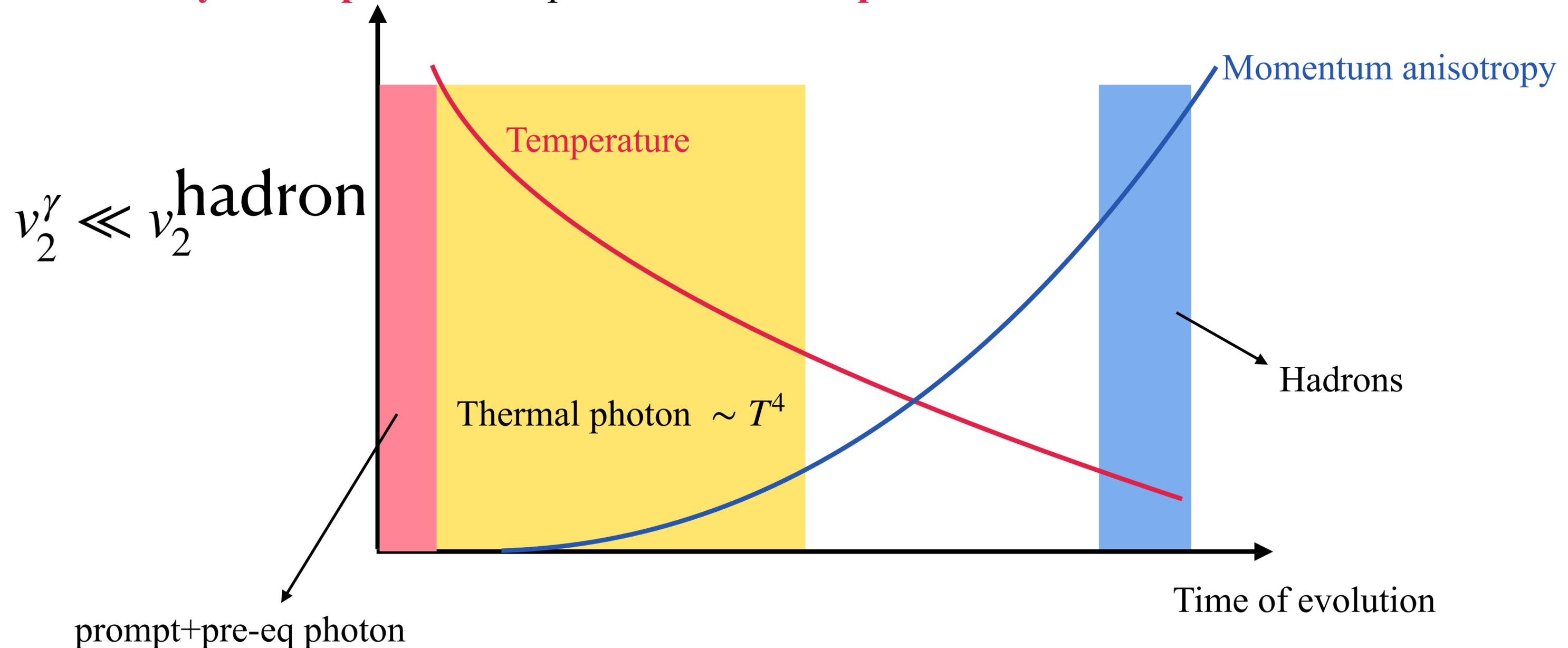
Escobar C. Nuclear Physics B, 1975, 98(1): 173-188.

Feinberg E L. Nuovo Cim. A, 1976, 34: 391.

Direct photon puzzle

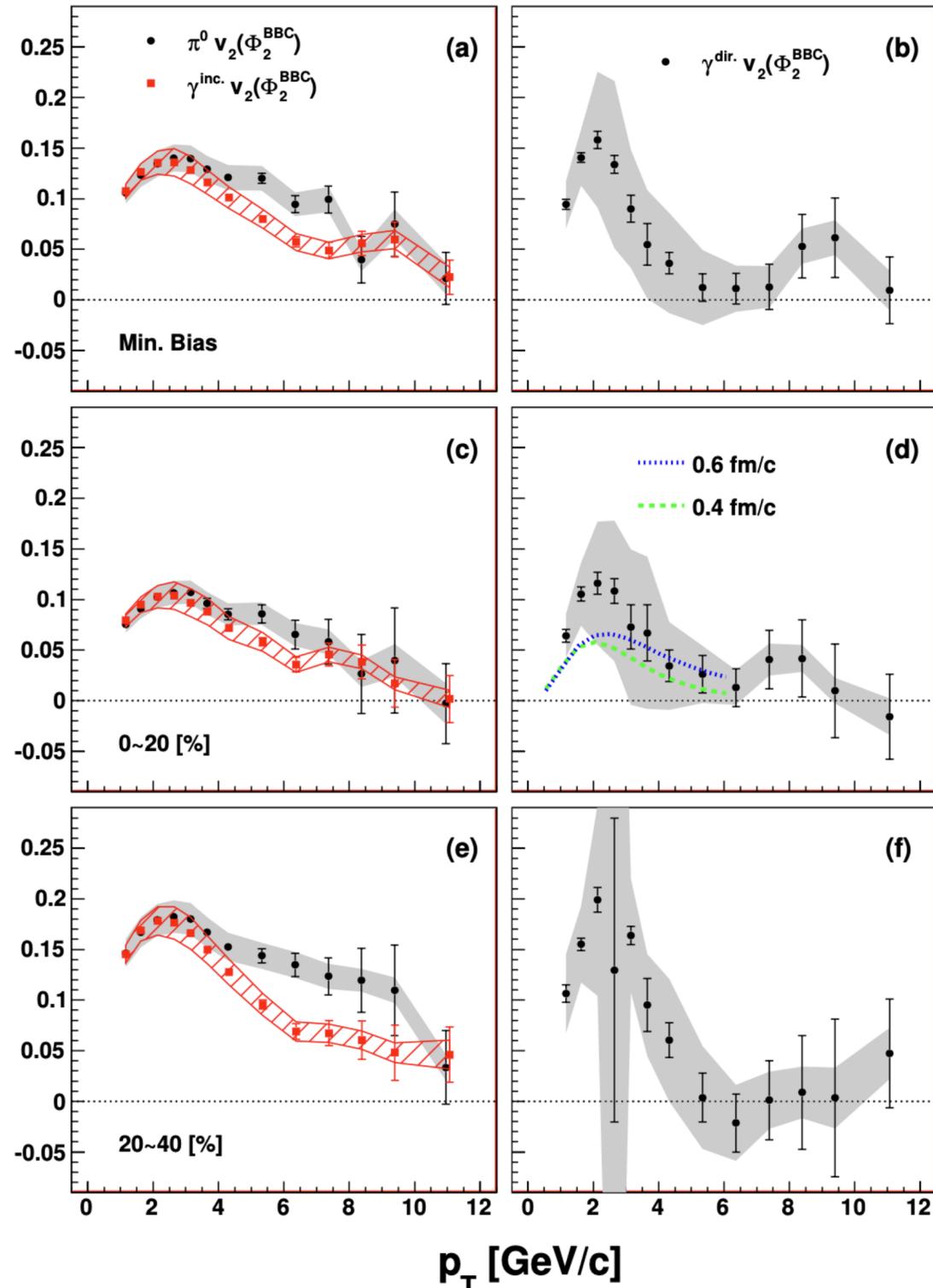
Theoretical expectations

- **Hadrons** inherit the anisotropy of QGP, leading to **large v_2 naturally**.
- The **photons** are dominantly thermal photons, where **momentum anisotropy has not been fully developed**. It is expected to be **isotropic**.



Direct photon puzzle

Experimental observation



$$v_2^\gamma \approx v_2^{\text{hadron}}$$

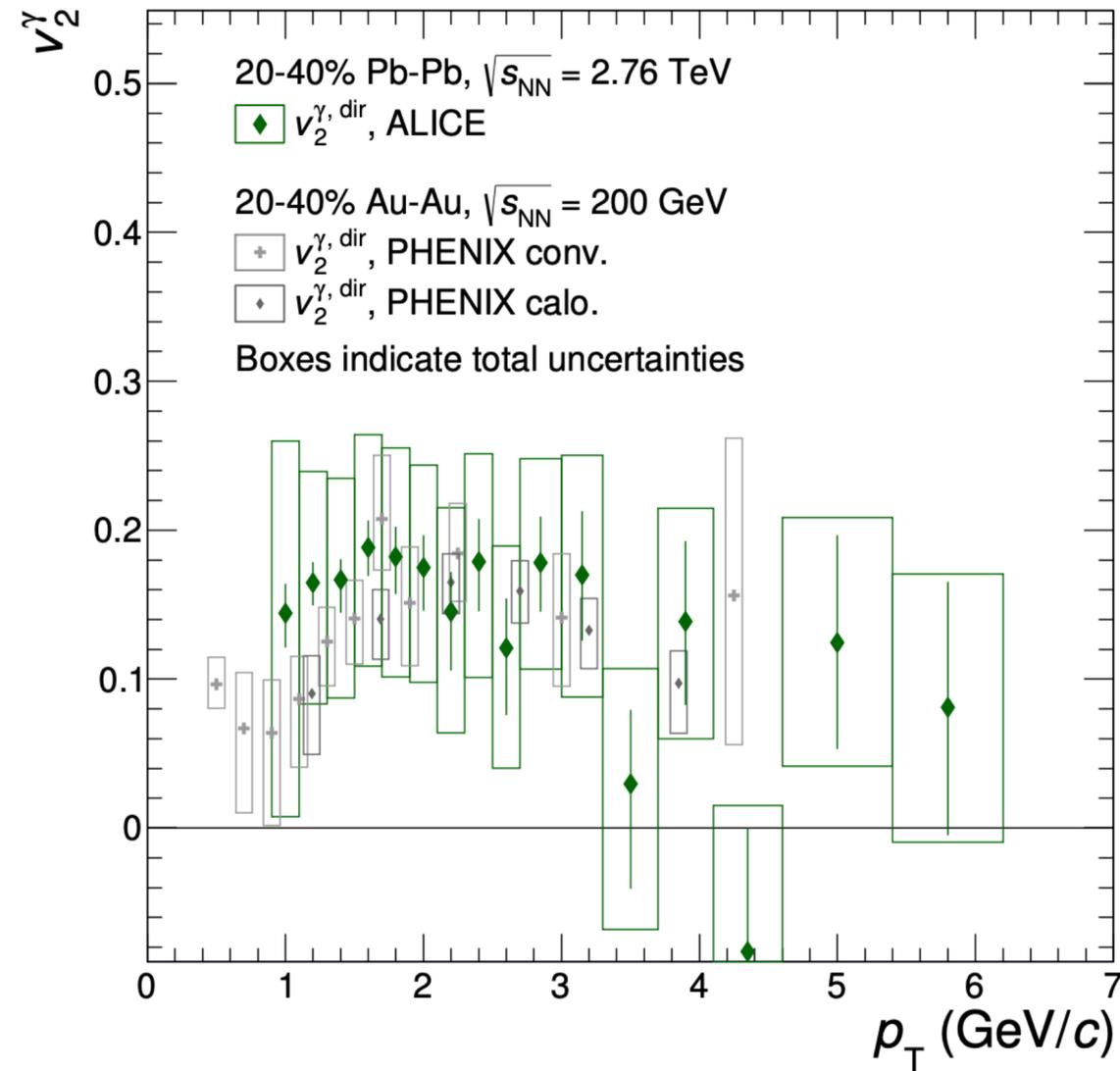
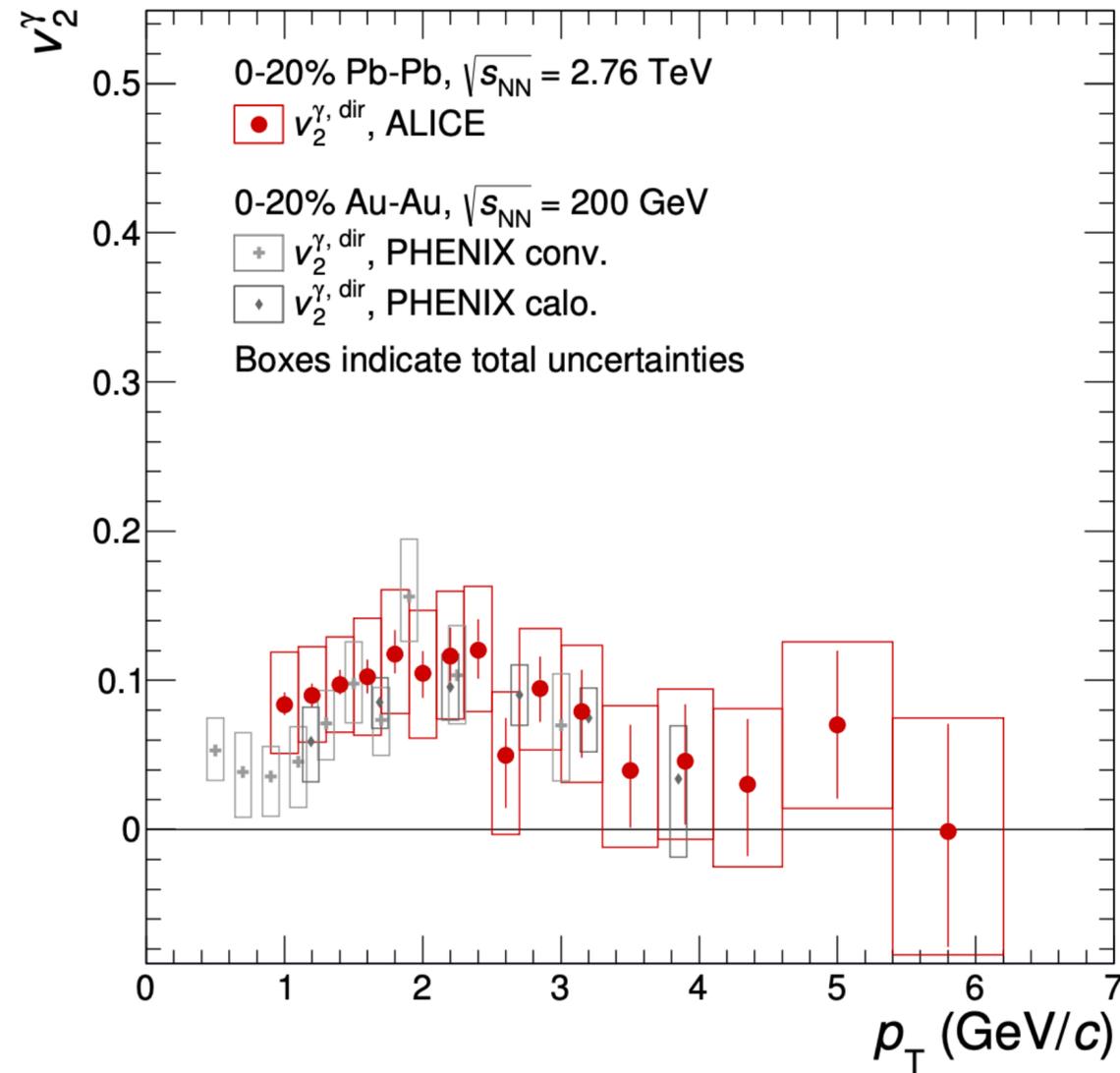
Puzzle!

No theory predict or could readily accommodate the simultaneous observation of **large yields** and **large v_2** for “thermal” photons

A. Adare et al. (PHENIX), Phys. Rev. Lett. 109, 122302 (2012)

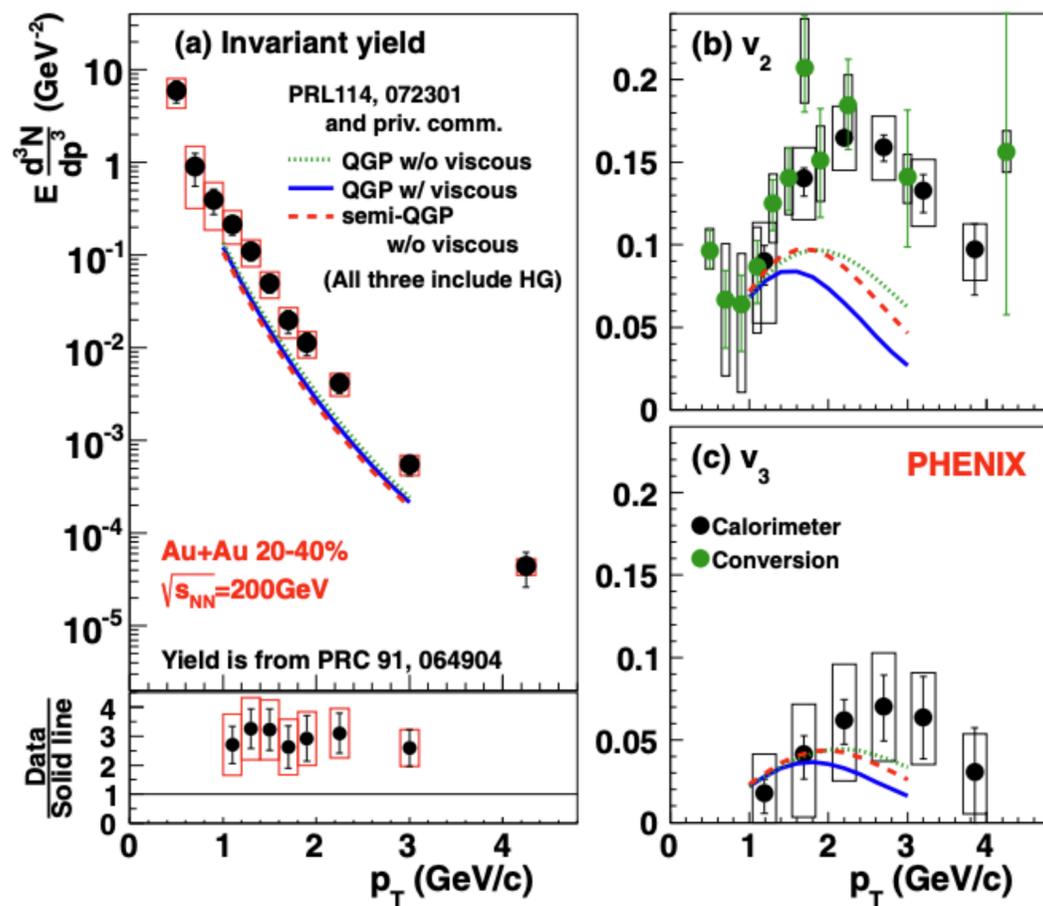
Direct photon puzzle

Experimental observation

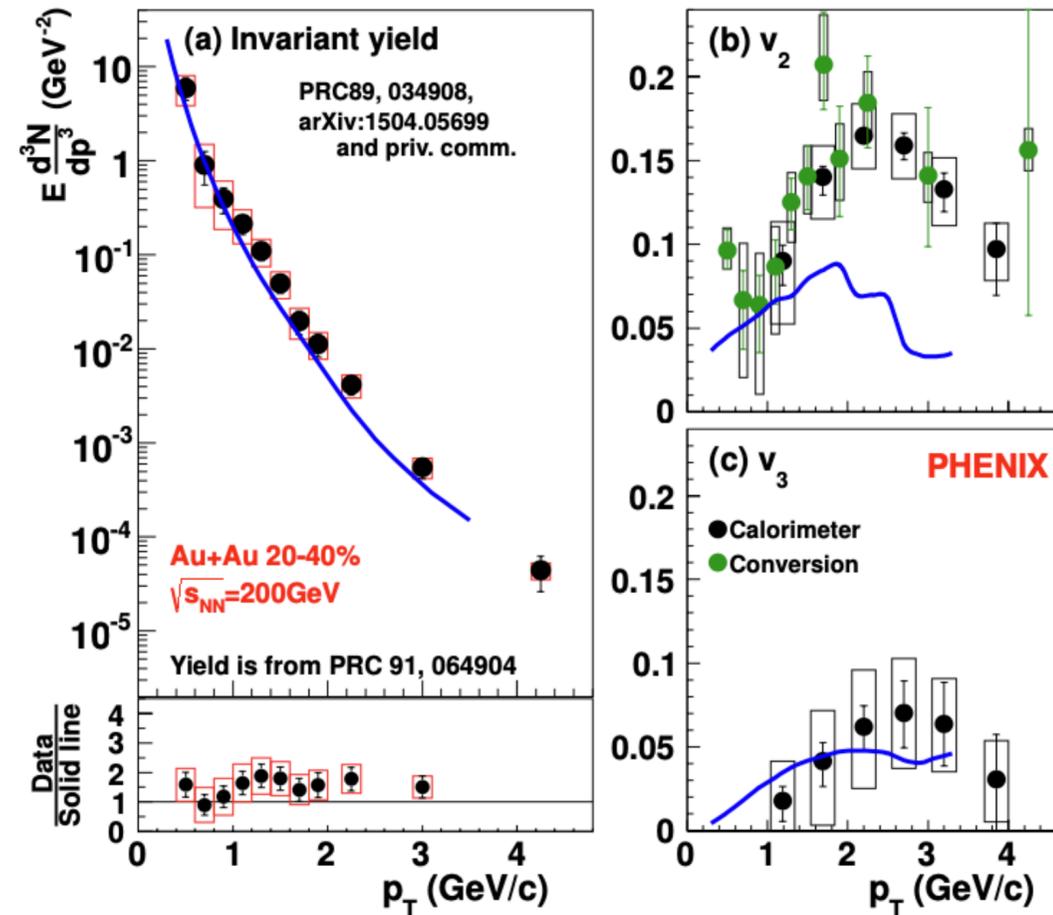


Experiment vs theories

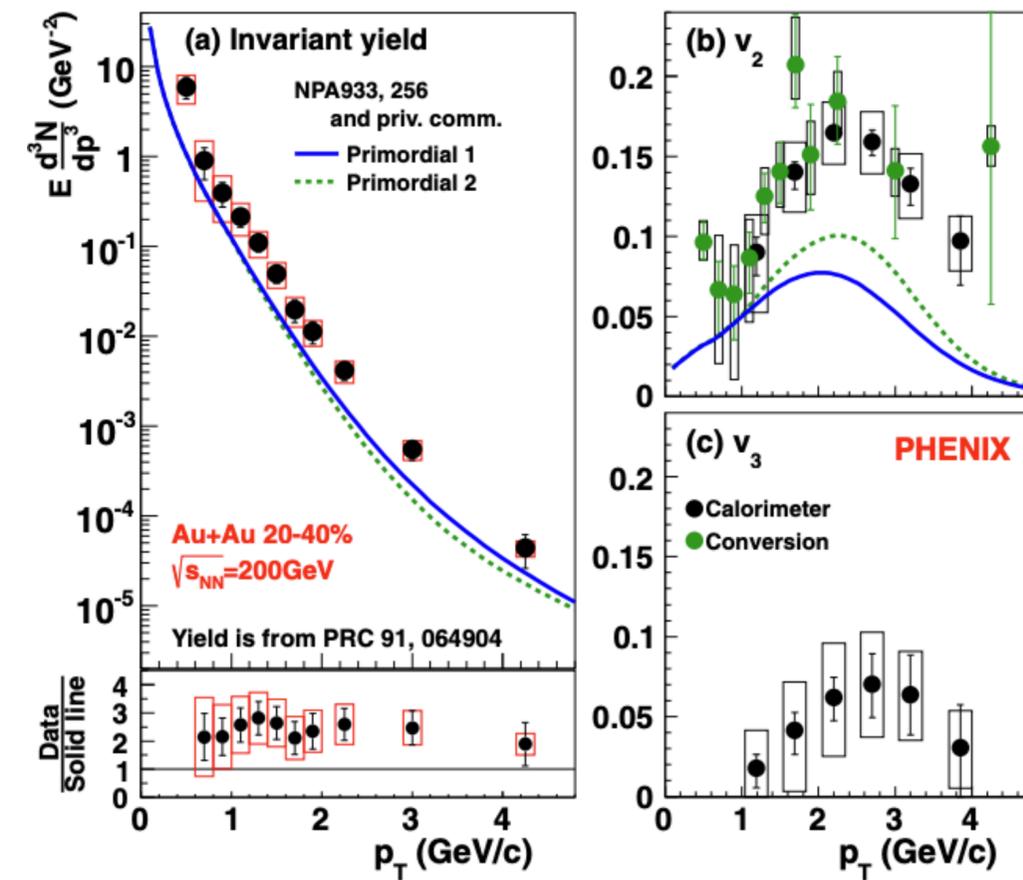
Hydrodynamical models



Transport calculations



Fireball model



○ “Not too much of a puzzle left for yields.”

[K. Reygers, Quark Matter 2022 plenary talk]

○ The present models are being challenged.

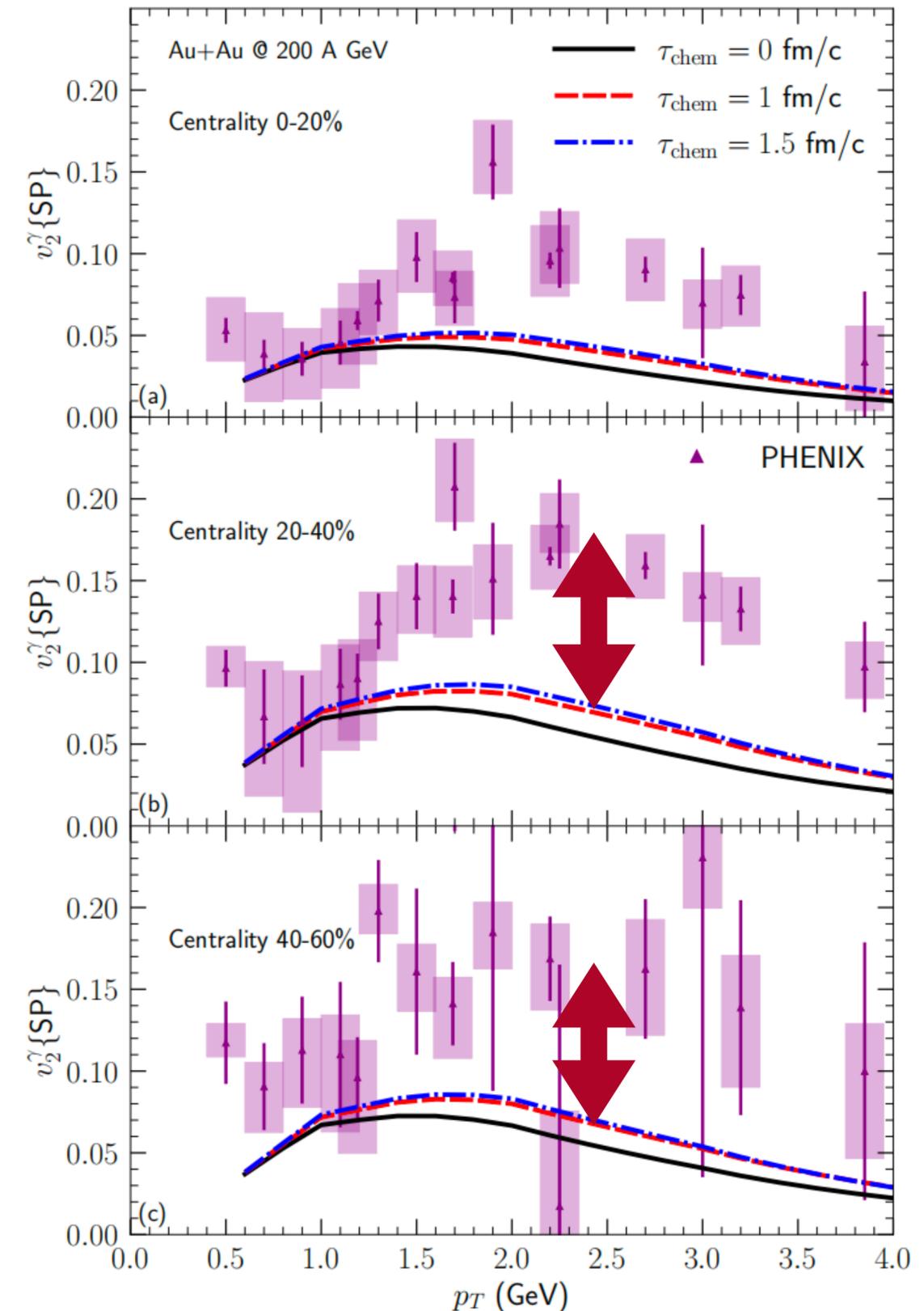
A. Adare et al. (PHENIX), Phys. Rev. C94, 064901 (2016)

The most updated calculation

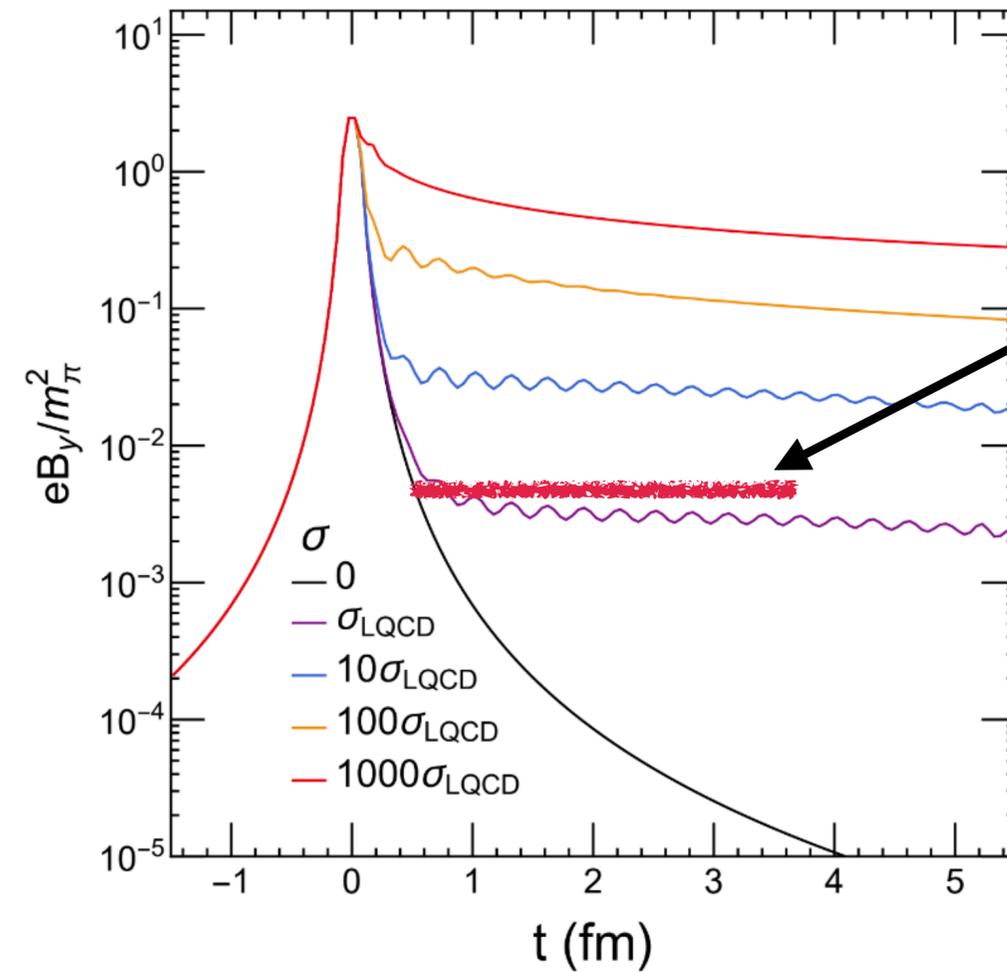
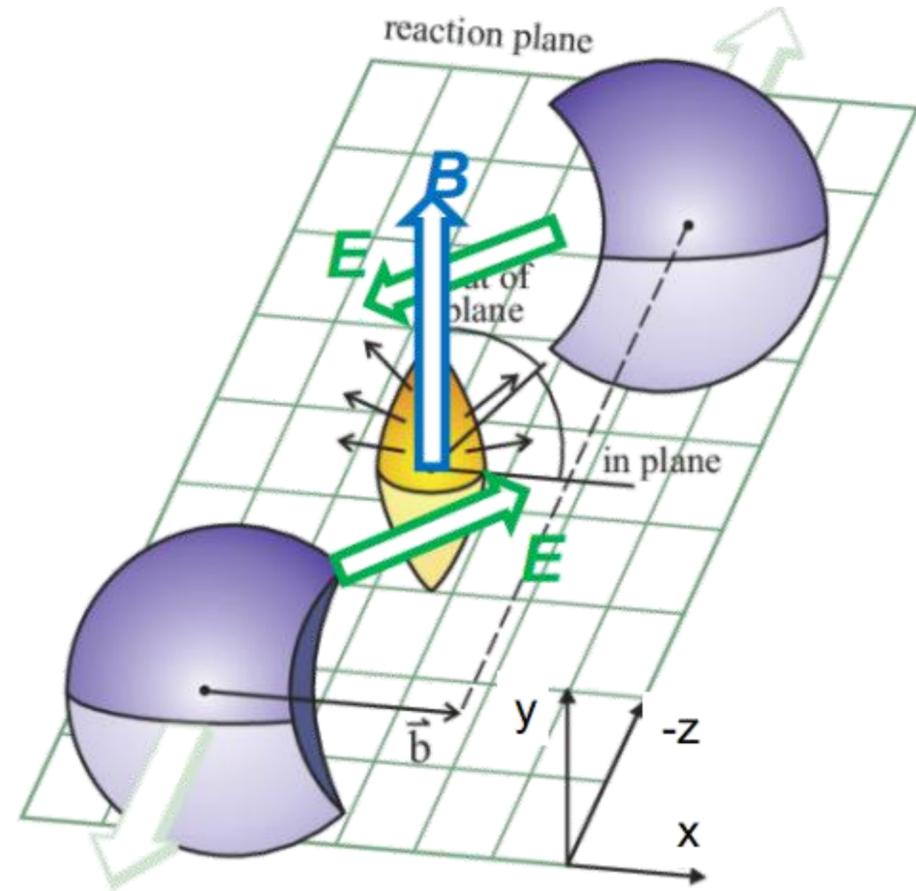
- oPre-equilibrium dynamics (KoMPost)
- oChemical equilibration in QGP
- oNNLO pQCD for prompt photons
- oShear and bulk viscous correction.

$$f_q = n_q + \delta f$$

The v_2 of direct photon is still **under-predicted**.



Magnetic Field in RHIC



Deng W T, Huang X G. Phys. Rev. C, 2012, 85: 044907.

L. Yan and X.-G. Huang (2021), 2104.00831

A. Huang et.al (2022),2212.08579.

J.-J. Zhang, et.al , Phys. Rev. Res. 4, 033138 (2022)

○ B field is dominated out of plane, $\vec{B} \parallel \hat{y}$.

○ Strong initial magnetic field, $\propto \sqrt{s}$.

○ **The lifetime of B** is determined by **the electrical conductivity** of medium, **but unknown**.

Magnetic field may be responsible for the “direct photon puzzle”?

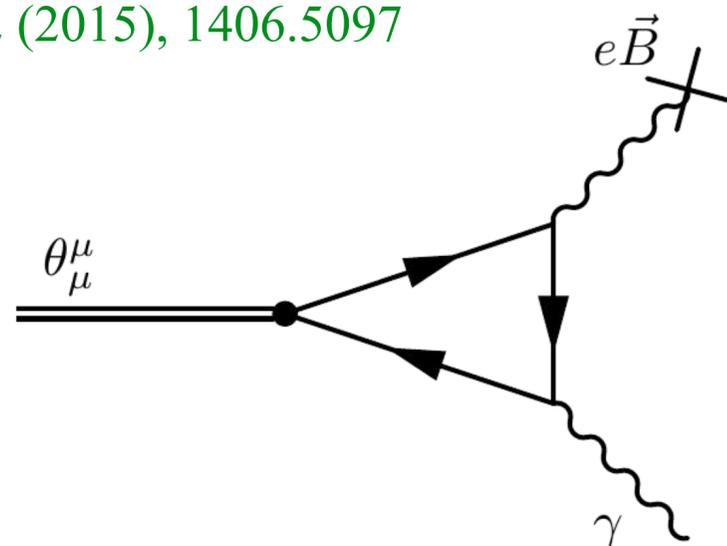
- Magnetic field is **large and highly anisotropic.** → Maybe a natural source of the photons’ anisotropy.
- **Be maximal at the early stage** of a collision. → Large yield of thermal photon.

A. Bzdak et.al, Phys. Rev. Lett. 110, 192301(2013), 1208.5502.

Strong magnetic field and direct photon ν_2

- Synchrotron radiation

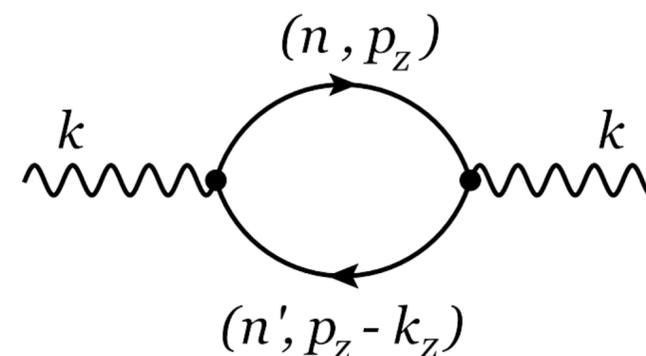
K. Tuchin, Phys. Rev. C 91, 014902 (2015), 1406.5097



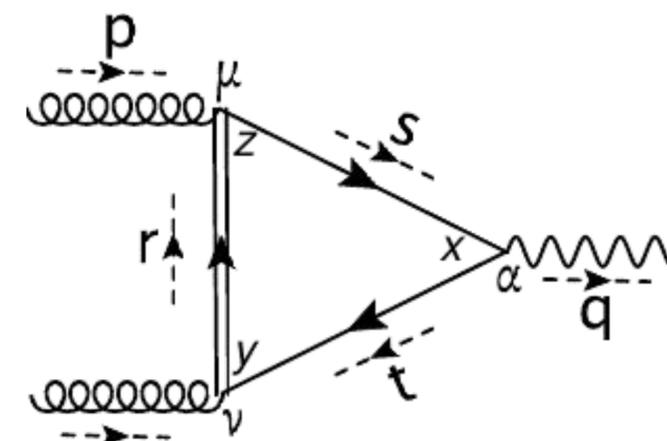
- Conformal anomaly

G. Basar, et.al, Phys. Rev. Lett. 109, 202303 (2012), 1206.1334.

- Quark with Landau level excitations



Ayala et al, 1704.02433,
X. Wang et al, 2006.16254



Weak magnetic field

○ Scales of magnetic field

$eB \gg g^2 T^2$ The quantization of Landau level.

$T^2 \gg eB \gg T \nabla$ Magnetohydrodynamics (MHD).

$eB \ll T \nabla \sim m_\pi^2$ **Weak magnetic non-equilibrium correction.**

$$f_q = n_q + \delta f + f_{EM}$$

$$f_{EM} = \frac{c}{8\alpha_{EM}} \frac{\sigma_{el} n_{eq} (1 - n_{eq})}{T^3 p \cdot u} e Q_f F^{\mu\nu} p_\mu u_\nu$$

An additional **cos ϕ** term !

$$[\dots \cos \phi + \dots \cos 2\phi + \dots] \cos \phi$$

v_1^{hadron}

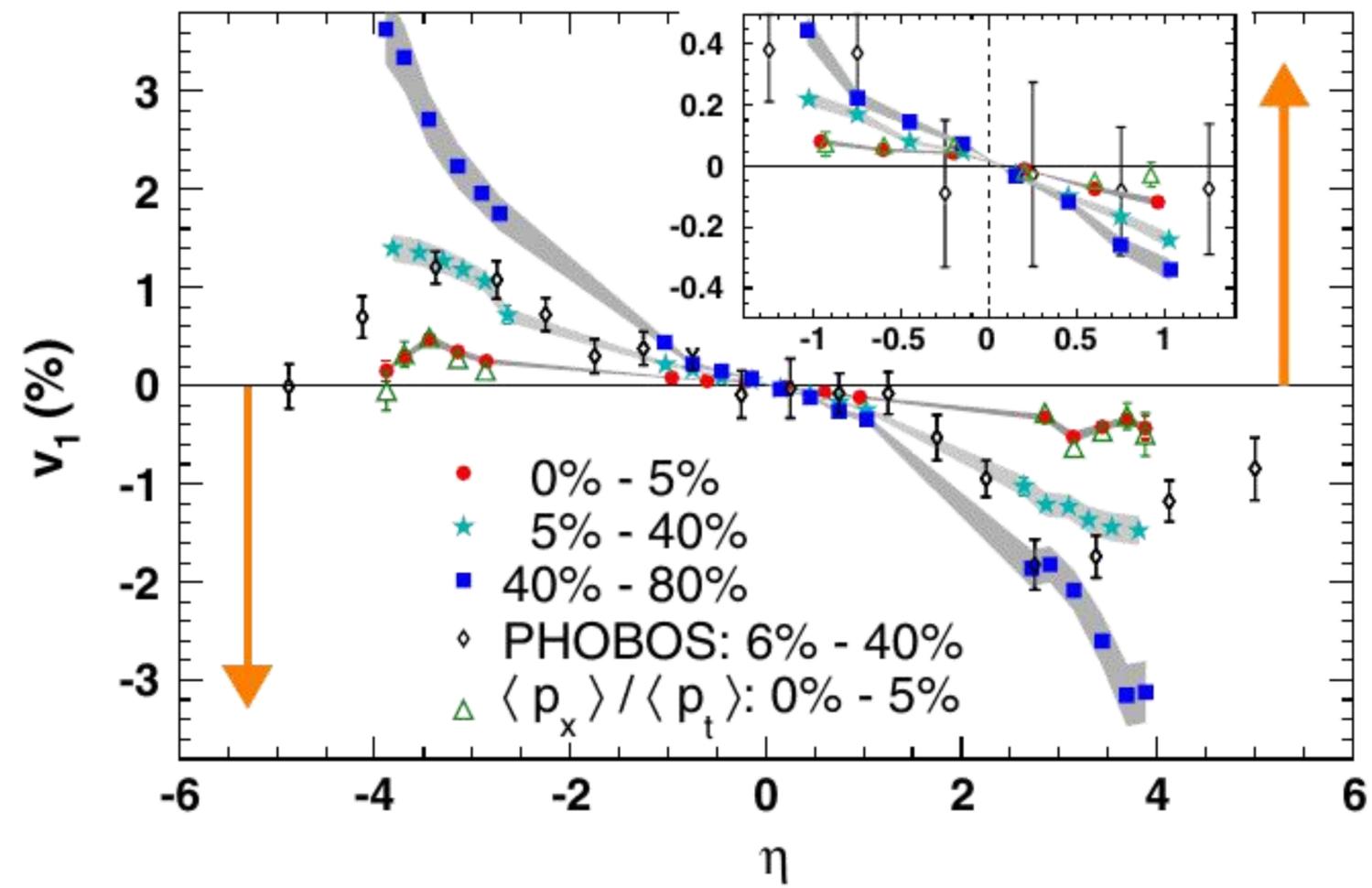
v_2^{hadron}

A Rapidity-odd directed flow for background medium is required !

$v_1^{\text{odd}}(\eta)$ of hadrons

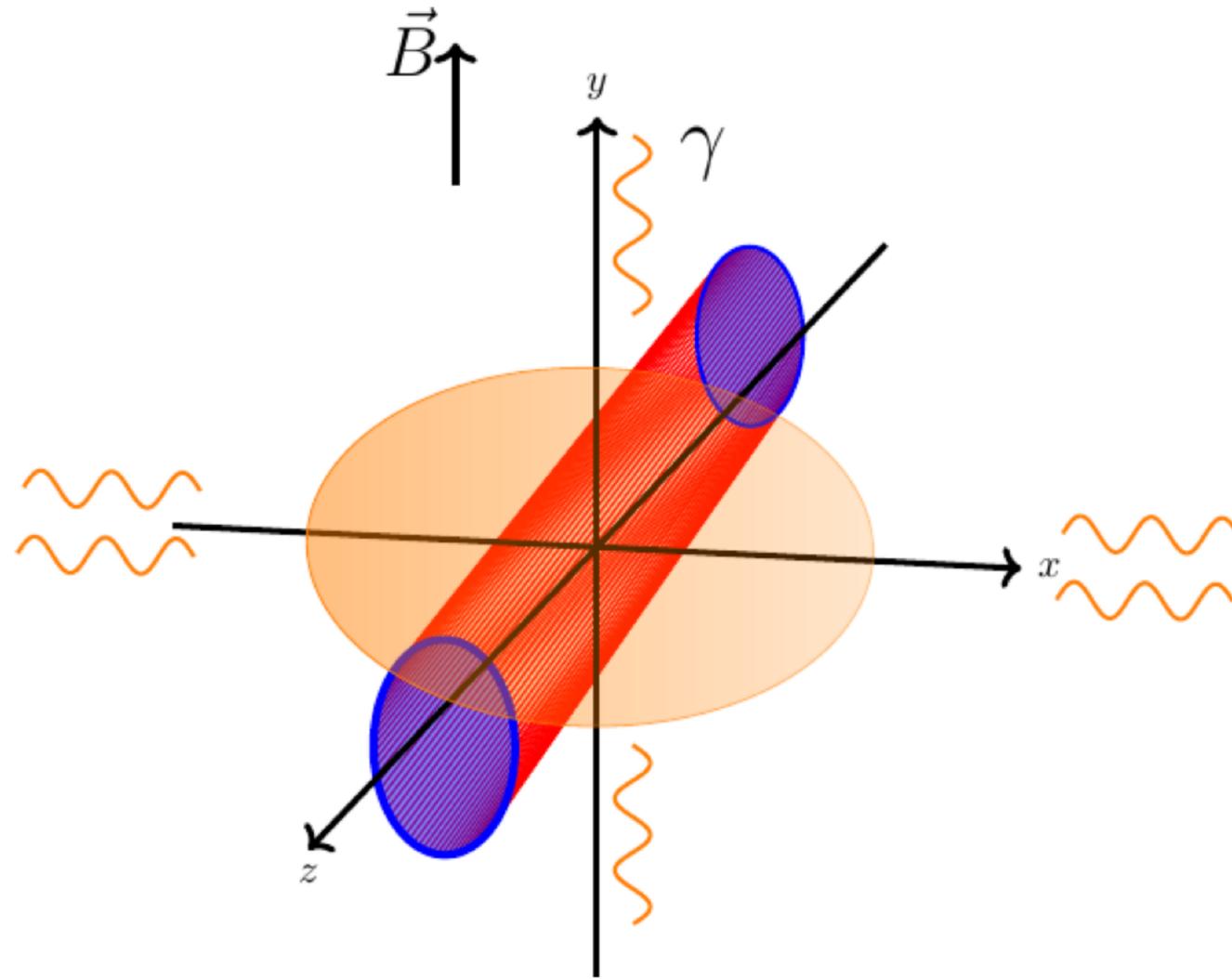
○ Rapidity-odd directed flow

The **rapidity-odd directed flow** of charge hadrons is **experimentally observed!**

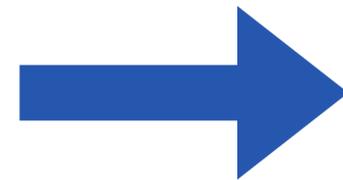


[STAR collaboration, PRL 101, 252301 (2008)]

Weak magnetic photon emission:



An external magnetic field
+ a “tilted” fireball



Elliptic flow of photons

For rapidity-odd v_1^{hadron}

Hydrodynamic simulation

- A “tilted” fireball : single-shot simulation

S. Chatterjee and P. Bozek, Phys. Rev. Lett. 120, 192301 (2018)

Use a tilted fireball configuration to capture the rapidity-odd v_1 of charged hadrons

- Trento3D initial condition : event-by-event simulation

PRC 92 011901, PRC 96 044912.

Realistic conditions !

JETSCAPE framework, arxiv 1903.07706

Magnetic field profile

- LO pQCD evaluation (AMY) is used for Electrical conductivity, to be consistent with background photon results.
- Space-time dependence of external B field as in vacuum: “worst-case”

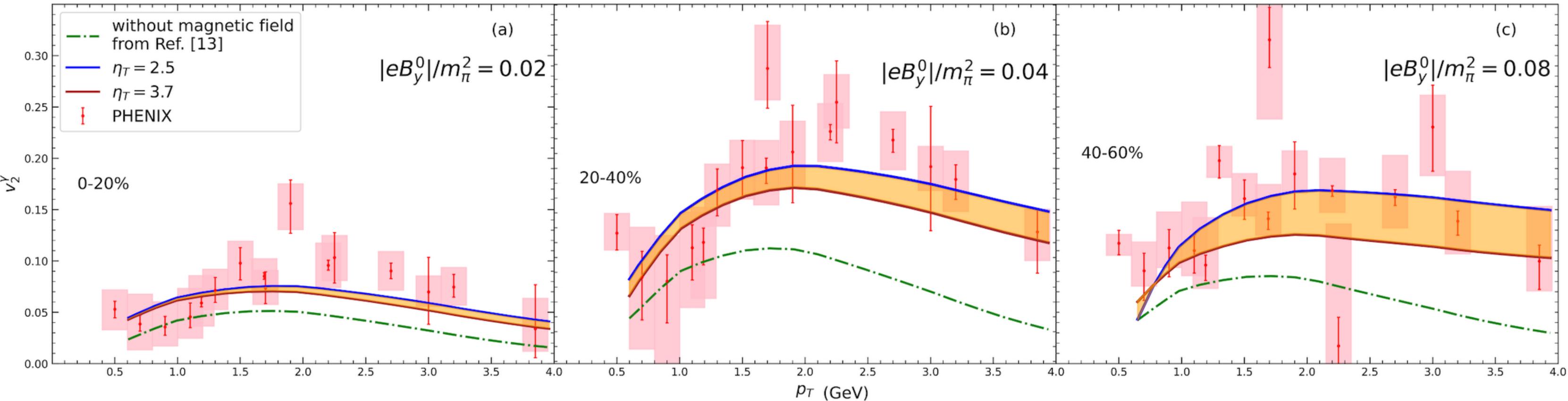
$$eB_y(\tau, \eta_s) = eB_y^0 \Gamma(\tau, \eta_s)$$

K. Hattori and X. Huang, 1609.00747

here eB_y^0 is the initial field strength when QGP evolves hydrodynamically

Single shot for RHIC

○ Confronts experiment at RHIC AuAu@200 GeV

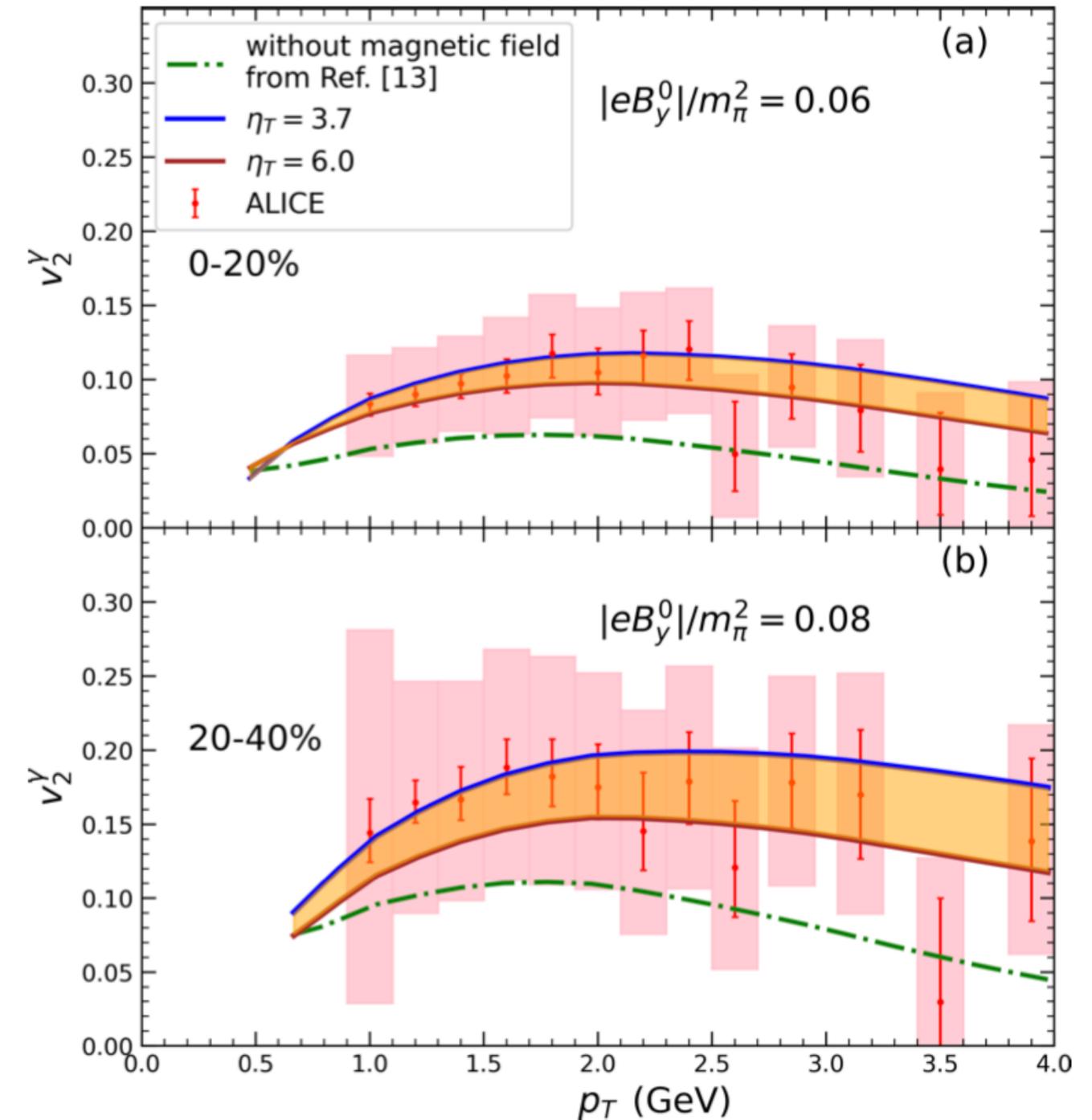


- The **experimental data are reproduced** excellently for all centralities.
- Initial field strength is extracted and is **under weak magnetic assumption**.
- More “tilted”, weaker magnetic field.
- The B field magnitude grows as centrality increases: **correct trend!**

Single-shot for LHC

○ Confronts experiment at LHC PbPb@2760 GeV

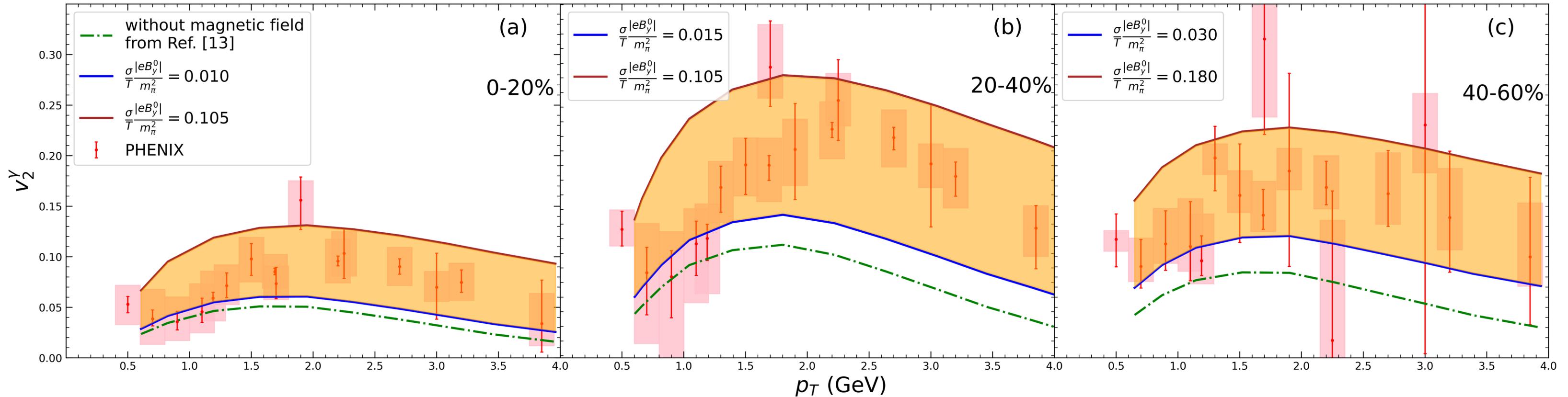
- The **experimental data are reproduced** excellently for all centralities.
- Initial field strength is extracted and is **under weak magnetic assumption**.
- More “tilted”, weaker magnetic field.
- The B field magnitude grows as centrality increases: **correct trend!**



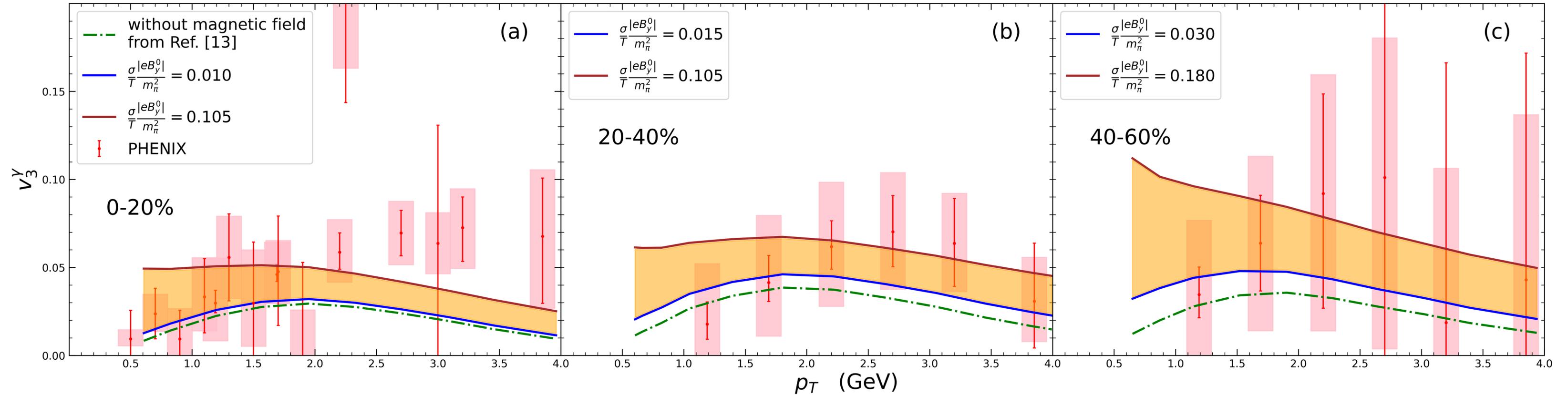
Extracting B field — ebe simulations

v_2 of direct photon

AuAu@200GeV



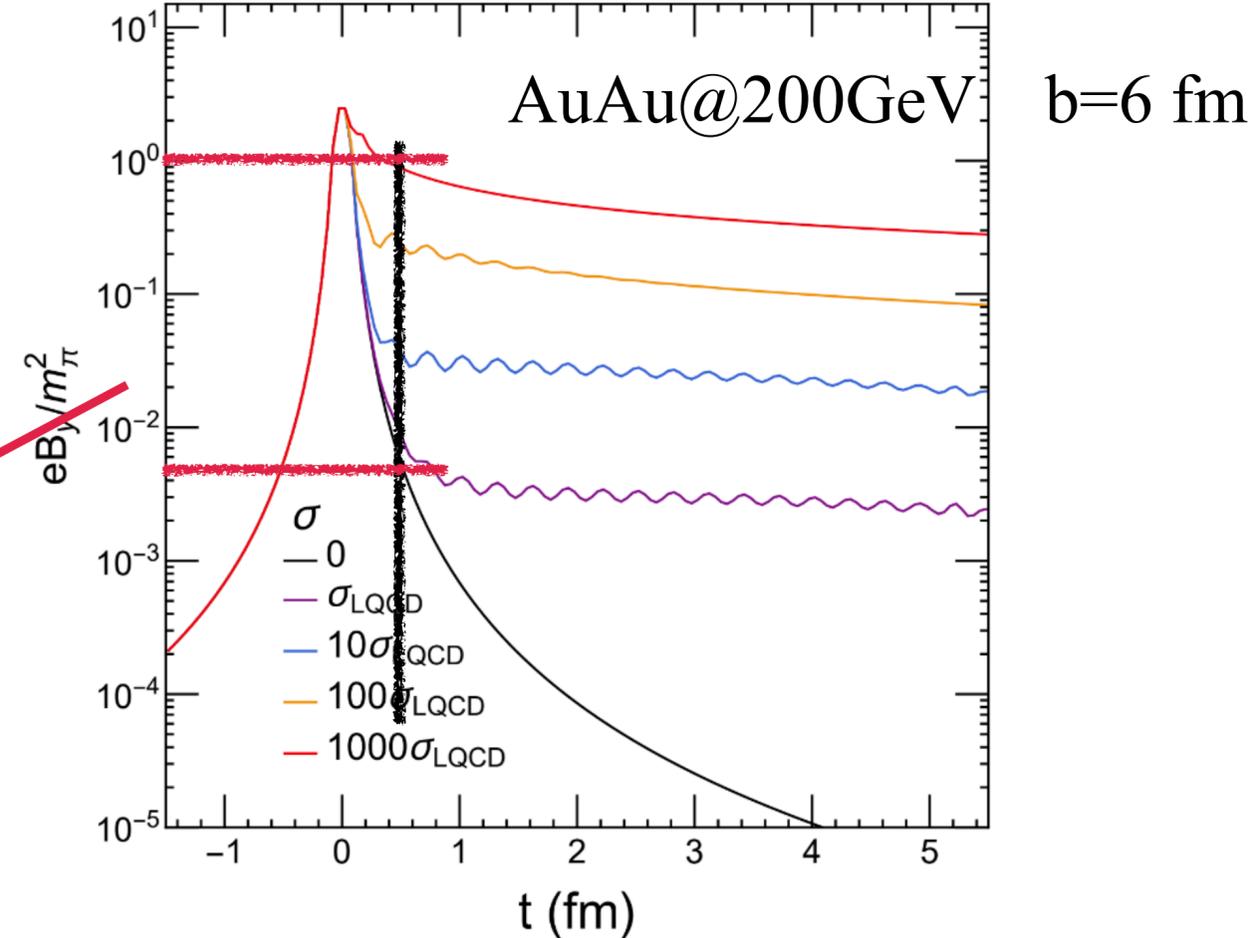
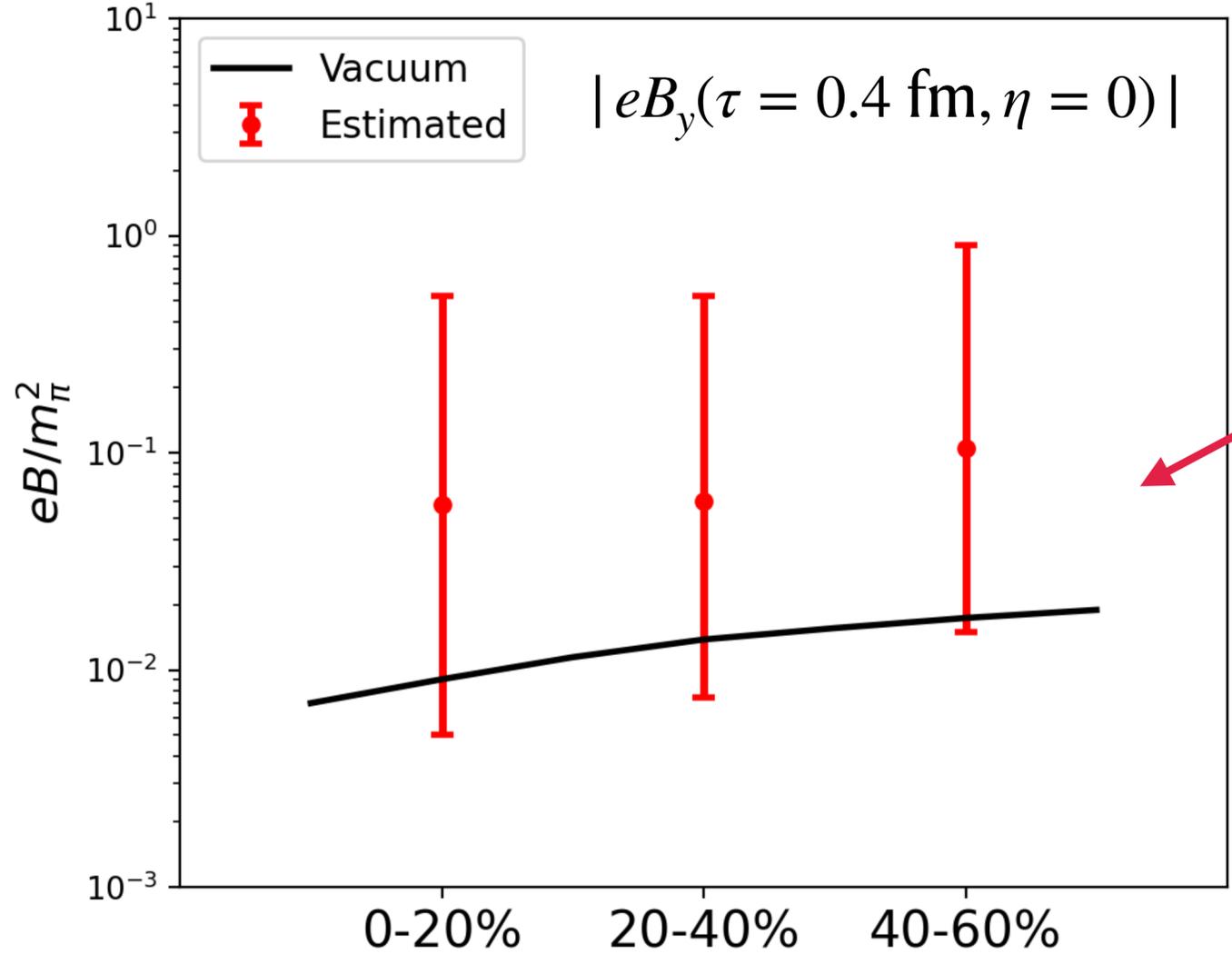
- Use the experimental measured elliptic flow to constrain the strength of B field.
- $eB^{\text{ebe}} \ll eB^{\text{Single}}$



o The weak magnetic photon emission also has significant effect on the triangle flow.

Non-trivial coupling effect: weak magnetic field + longitudinal dynamics!

Estimated B field at $\tau = 0.4$ fm based on event-by-event simulations



A. Huang et.al (2022),2212.08579.
 J.-J. Zhang, et.al , Phys. Rev. Res. 4, 033138 (2022)

o The error-bar contains: theoretical + experimental

$\frac{\sigma}{T} \in [0.2, 2]$ Cover the experimental elliptic flow data

F.Stefan arxiv: 2112.12497

Summary

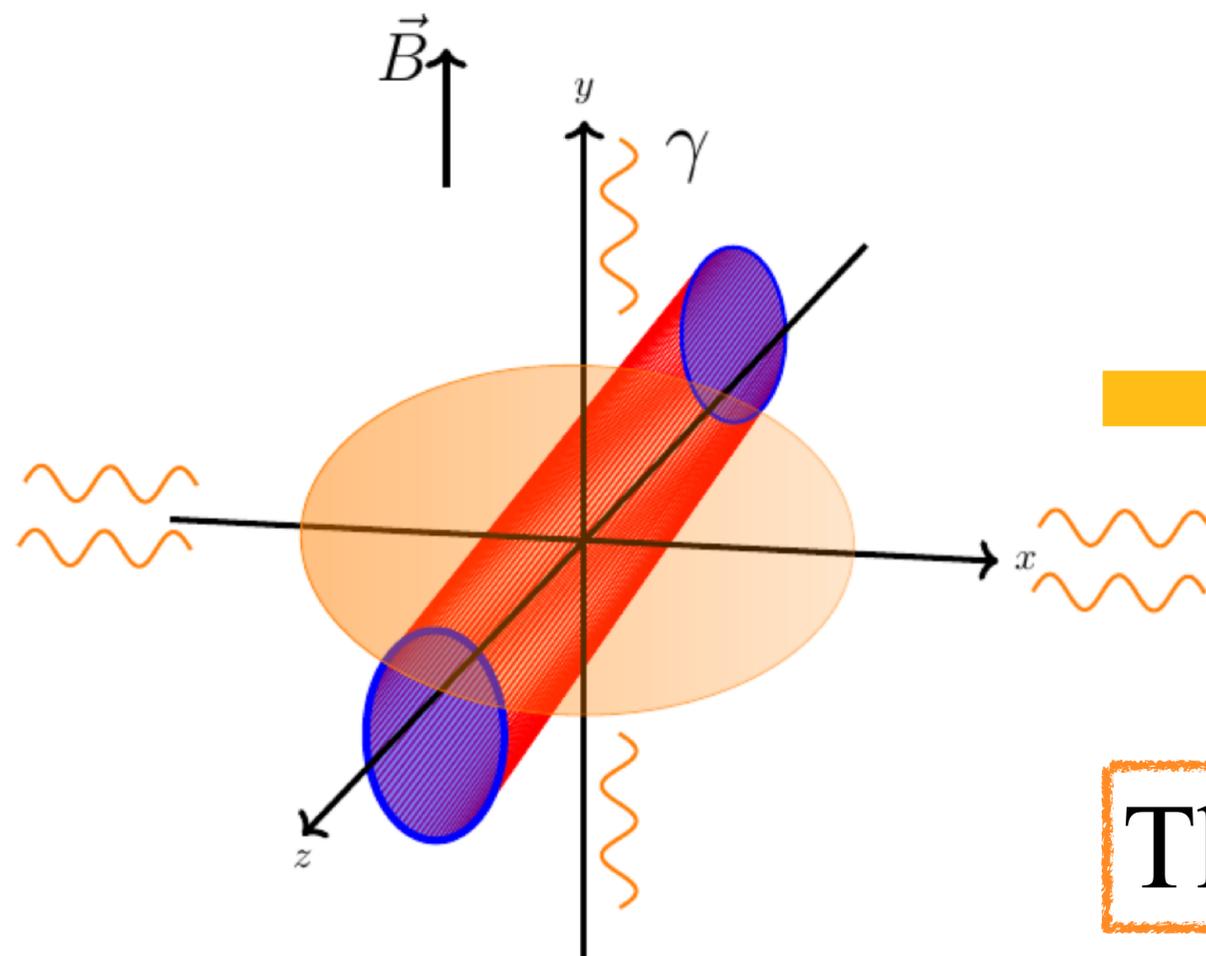
- Weak magnetic photon emission:

Weak magnetic field + the non-trivial longitudinal dynamics of fireball.

- The elliptic flow of photons at RHIC and LHC are **reproduced for the first time**.

- The initial B field** can be extracted from photon spectra.

arXiv: [2302.07696](https://arxiv.org/abs/2302.07696)



Towards direct photon puzzle.

Back up

$$\mathcal{R}^\gamma = \bar{\mathcal{R}}^\gamma + \mathcal{R}_{\text{EM}}^\gamma$$

$$E_p \frac{d^3 \bar{N}}{d^3 \mathbf{p}} = \int_V \bar{\mathcal{R}}^\gamma(P, X) = \bar{v}_0 (1 + 2\bar{v}_2 \cos 2\phi_p)$$

$$E_p \frac{d^3 N_{\text{EM}}}{d^3 \mathbf{p}} = \int_V \mathcal{R}_{\text{EM}}^\gamma(P, X) = v_0^{\text{EM}} (1 + 2v_2^{\text{EM}} \cos 2\phi_p)$$

$$v_0^\gamma = \bar{v}_0 + v_0^{\text{EM}}, \quad v_2^\gamma = \frac{\bar{v}_2 \bar{v}_0 + v_2^{\text{EM}} v_0^{\text{EM}}}{\bar{v}_0 + v_0^{\text{EM}}}$$

Small angle approximation for photon production rate

For the process $1 + 2 \longrightarrow 3 + \gamma$

$$\begin{aligned} \omega \frac{d^3 R_\gamma}{d^3 k} &= \frac{1}{2(2\pi)^3} \int \frac{d^3 p_1}{2p_1^0 (2\pi)^3} \frac{d^3 p_2}{2p_2^0 (2\pi)^3} \frac{d^3 p_3}{2p_3^0 (2\pi)^3} \times (2\pi)^4 \delta^4(P_1 + P_2 - P_3 - K) |\mathcal{M}|^2 \\ &\times f_{B/F}(p_1) f_{B/F}(p_2) [1 + \sigma_{B/F} f_{B/F}(p_3)] \\ &\propto f_q(k) \end{aligned} \quad \longrightarrow \quad R^\gamma \propto f_q = n_q + \delta f + f_{\text{EM}}$$

○ Bjorken analysis for illustration

For background medium: $n_{\text{eq}} = A_0(\tau, \eta_s, p_T, Y) + A_1(\tau, \eta_s, p_T, Y) \cos \phi_p$

$$f_{\text{EM}} \propto QB_y \frac{\tau_R}{T} \frac{\sinh \eta_s}{\cosh(y - \eta_s)} (A_0 + A_1 \cos \phi_p) \cos \phi_p$$

This $\cos \phi$ is from weak magnetic field.

$$= QB_y \frac{\tau_R}{T} \frac{\sinh \eta_s}{\cosh(y - \eta_s)} \left[\frac{A_1}{2} + A_0 \cos \phi + \frac{A_1}{2} \cos 2\phi \right] \longrightarrow v_2^{EM} \propto \int \frac{\sinh \eta_s}{\cosh(y - \eta_s)} A_1$$

Rapidity-odd!

Must be Rapidity-odd

A Rapidity-odd directed flow for background medium is required for non-zero v_2^{EM}

○ Hydrodynamic simulation

Reweight participants of the forward and backward-going nuclei in the two component Glauber model

$$s(\tau_0, x_\perp, \eta_s) \propto w(\eta_s) [\alpha N_{\text{coll}} + (1 - \alpha)(N_{\text{part}}^+ w^+(\eta_s) + N_{\text{part}}^- w^-(\eta_s))] \quad \text{S. Chatterjee and P. Bozek, Phys. Rev. Lett. 120, 192301 (2018)}$$

$$w^+(\eta_s) = \begin{cases} 0, & \eta_s < -\eta_T \\ \frac{\eta_T + \eta_s}{2\eta_T}, & -\eta_T \leq \eta_s \leq \eta_T \\ 1, & \eta_s > \eta_T \end{cases}$$

η_T determines the extent to which the fireball is tilted.

Yield of photons

