

Extracting phi meson properties in nuclear matter from pA reactions

Philipp Gubler
Japan Atomic Energy Agency (JAEA)



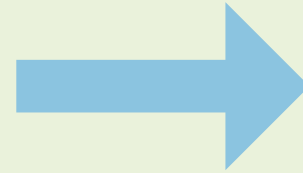
Talk at the “9th Asian Triangle Heavy-Ion Conference (ATHIC 2023)”
Hiroshima, Japan
April 24, 2023

Based on work done in collaboration with
Elena Bratkovskaya (Frankfurt/GSI),
Taesoo Song (GSI)

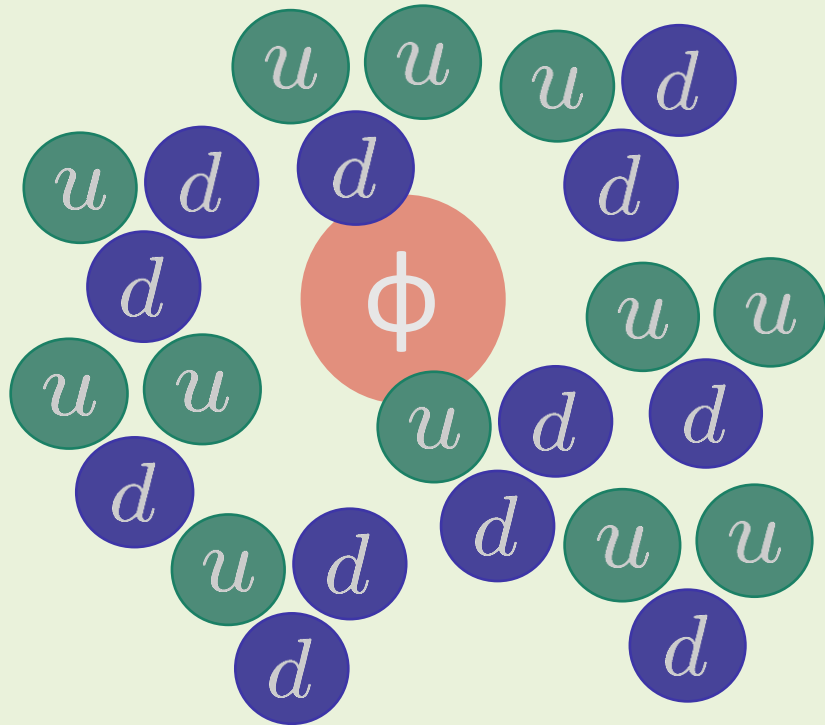
Why should we be interested?

The ϕ meson mass in nuclear matter probes the strange quark condensate at finite density!

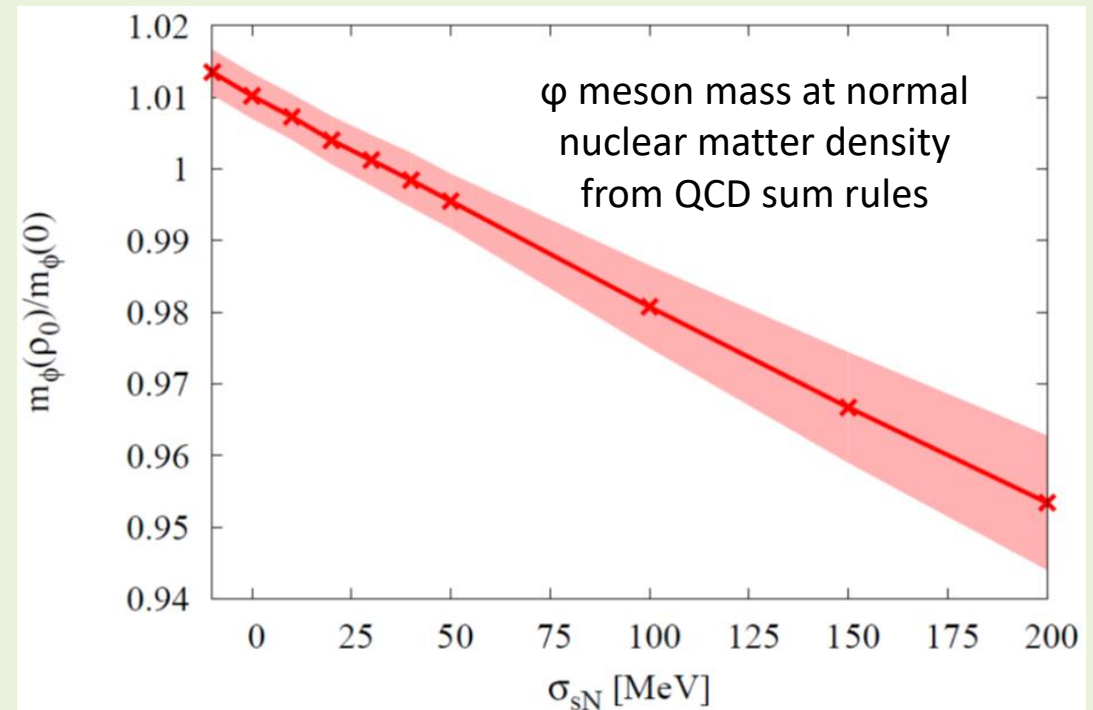
$$|\langle \bar{s}s \rangle_\rho| \quad \rightarrow$$



$$m_\phi \quad \rightarrow \quad ?$$



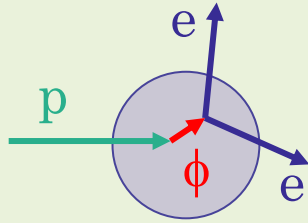
P. Gubler and K. Ohtani, Phys. Rev. D **90**, 094002 (2014).



$$|\langle \bar{s}s \rangle_\rho| = |\langle \bar{s}s \rangle_0| - \frac{\rho}{m_s} \sigma_{sN} + \dots$$

Previous experimental results

KEK
E325



12 GeV
pA-reaction

slow ϕ s

Pole mass:

$$\frac{m_\phi(\rho)}{m_\phi(0)} = 1 - k_1 \frac{\rho}{\rho_0}$$

0.034 ± 0.007

intermediate
 ϕ s

Pole width:

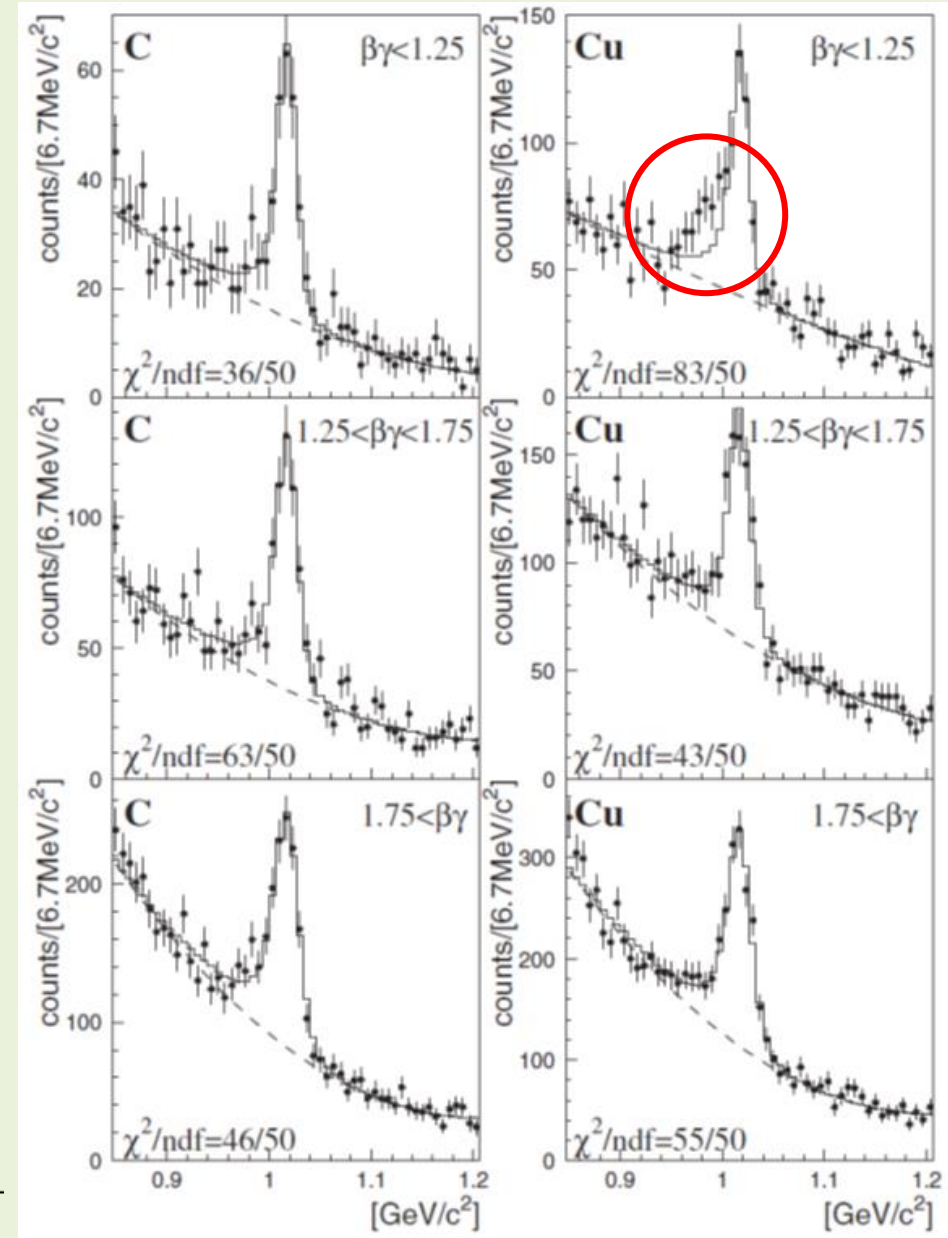
$$\frac{\Gamma_\phi(\rho)}{\Gamma_\phi(0)} = 1 + k_2 \frac{\rho}{\rho_0}$$

2.6 ± 1.5

fast ϕ s

Measurement is being repeated with
 $\sim 100x$ increased statistics at the
J-PARC E16 experiment!

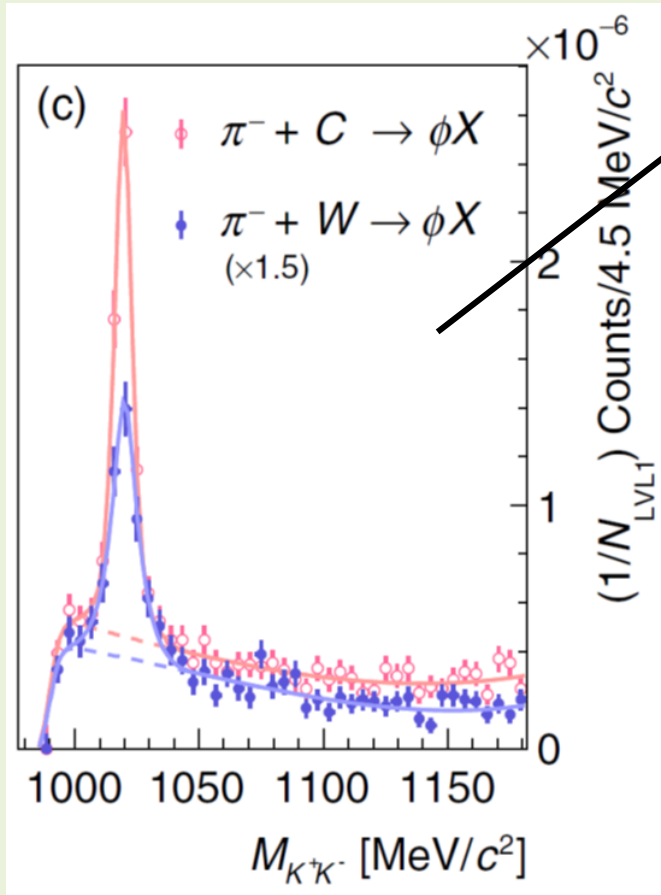
$$\beta\gamma = \frac{|\vec{p}|}{m_\phi}$$



More recent results

HADES: 1.7 GeV π^- -A-reaction

K^+K^- - invariant mass spectrum



J. Adamczewski-Musch et al. (HADES Coll.),
 Phys. Rev. Lett. **123**, 022002 (2019).

Theoretical analysis of the
 of the total ϕ meson
 production cross section:



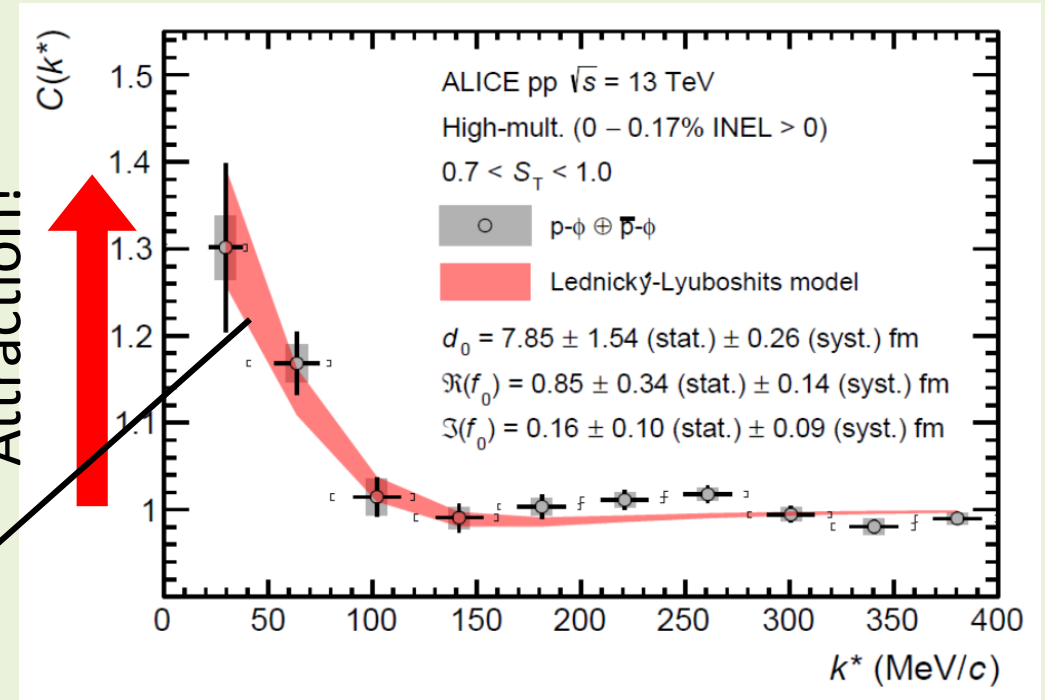
**Attractive ϕ -nucleus potential
 of -(50 - 100) MeV**

E. Ya. Paryev, Nucl. Phys. A
1032, 122624 (2023).

Negative
 mass shift

ALICE: pp

Measurement of ϕ N correlation



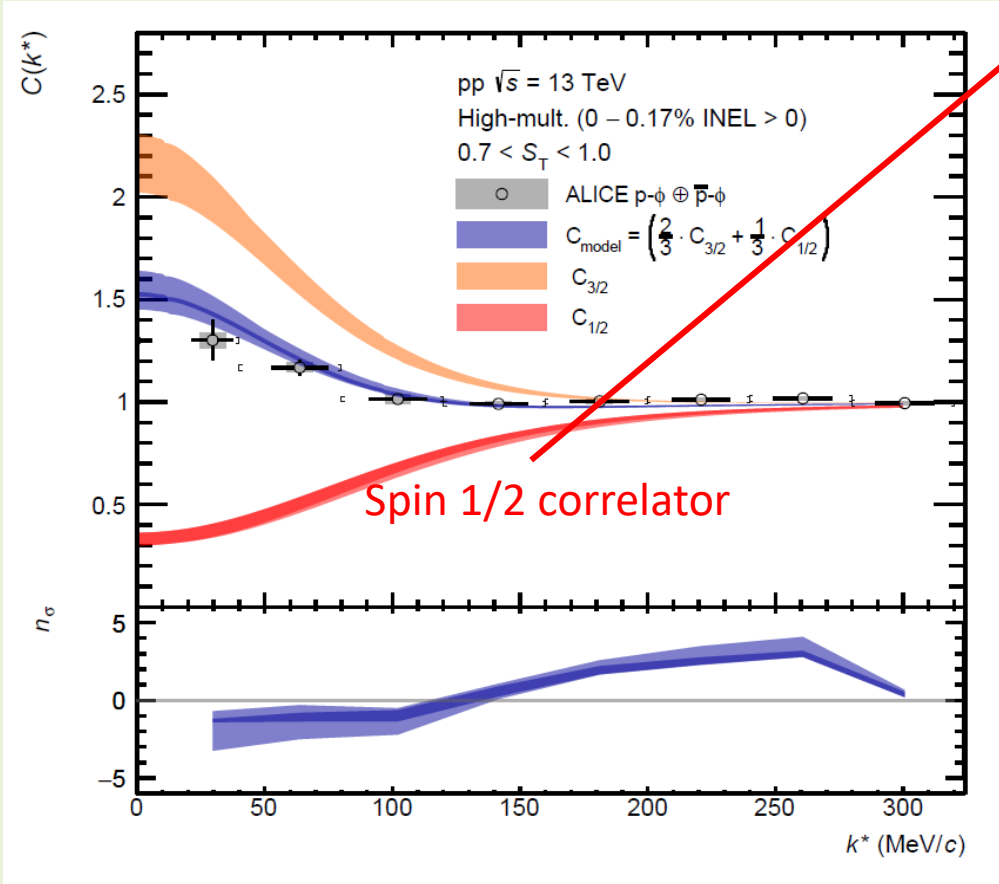
S. Acharya et al. (ALICE Coll.),
 Phys. Rev. Lett. **127**, 172301 (2021).

See also: Y. Lyu et al. (Lattice QCD, HAL QCD Collaboration),
 Phys. Rev. D **106**, 074507 (2022).

$\rightarrow a_0^{3/2} = 1.43(23)_{\text{stat.}} \left(\begin{smallmatrix} +36 \\ -06 \end{smallmatrix} \right)_{\text{syst.}} \text{ fm}$

Even more recent results

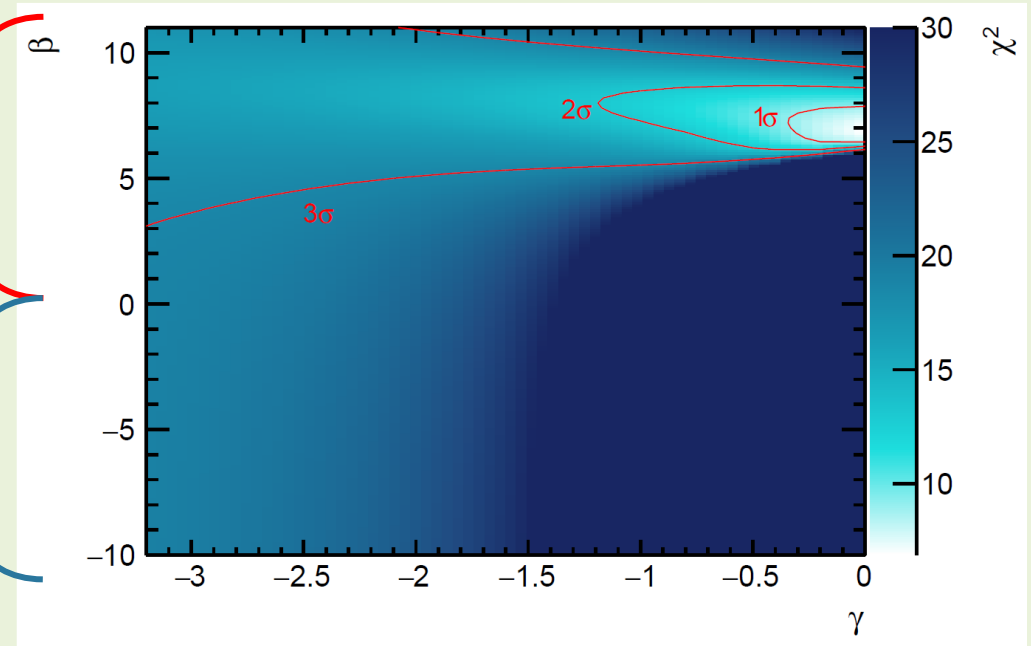
Combination of ALICE pp-data and HAL QCD (spin 3/2) calculation



Bound state?
 Repulsive?

Bound state

Repulsive



E. Chizzali et al., arXiv:2212.12690 [nucl-ex].

➔ Evidence for ϕ -N bound state!

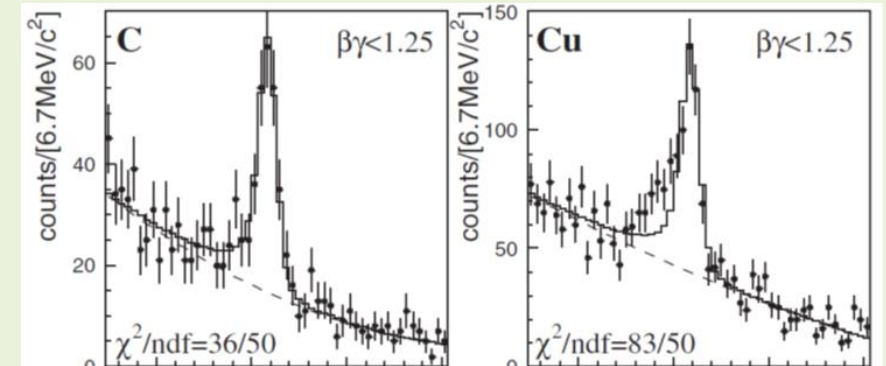
How compare theory with experiment?

Information useful for theory

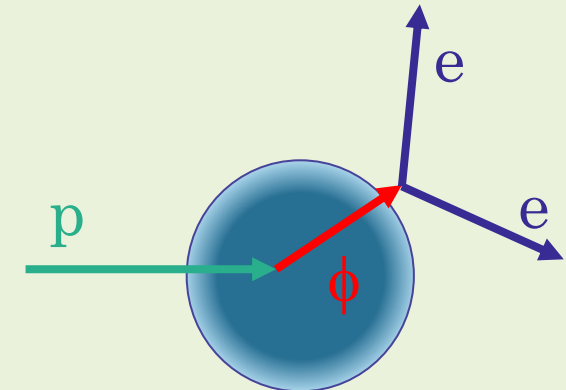
- ★ Spectral function as a function of density
- ★ Mass at normal nuclear matter density
- ★ Decay width at normal nuclear matter density



Experimental data



Realistic simulation of pA reaction is needed!



Our tool: transport simulation PHSD (Parton Hadron String Dynamics)

E.L. Bratkovskaya and W. Cassing, Nucl. Phys. A **807**, 214 (2008).
W. Cassing and E.L. Bratkovskaya, Phys. Rev. C **78**, 034919 (2008).

Off-shell dynamics of vector mesons and kaons
(dynamical modification of the mesonic spectral function during the simulated reaction)

Used spectral function:

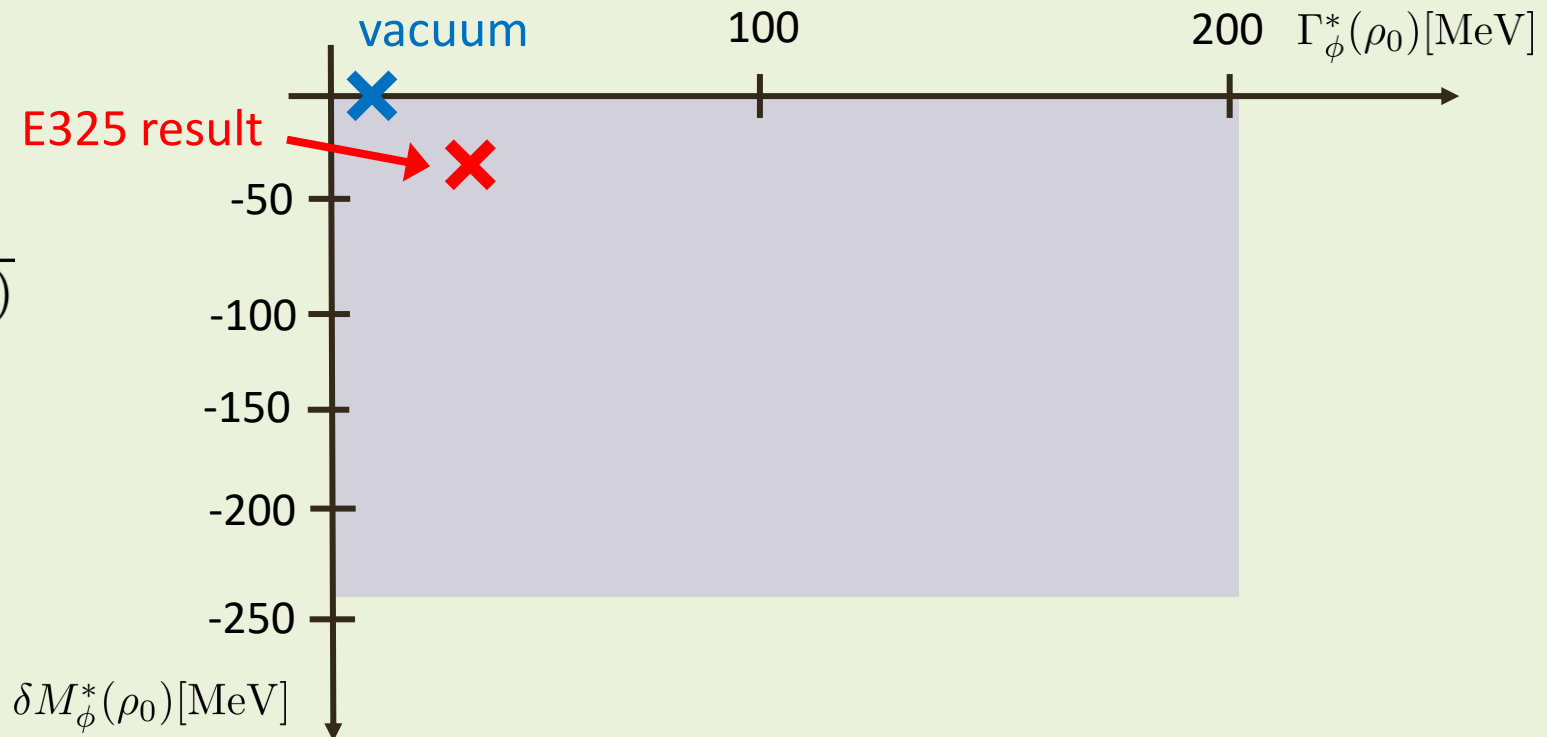
Relativistic Breit-Wigner with density dependent mass and width

$$C \frac{2}{\pi} \frac{M^2 \Gamma_\phi^*(M, \rho)}{[M^2 - M_\phi^{*2}(\rho)]^2 + M^2 \Gamma_\phi^{*2}(M, \rho)}$$

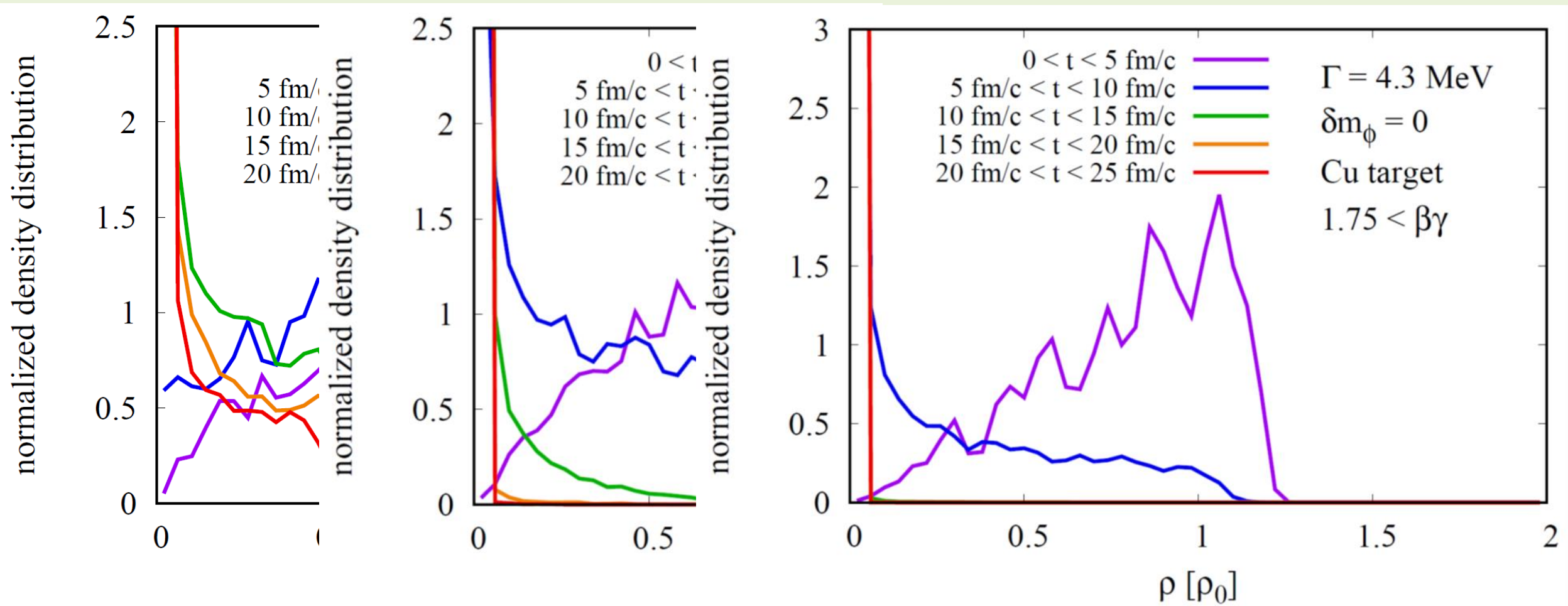
with

$$\begin{cases} M_\phi^*(\rho) = M_\phi^{\text{vac}} \left(1 - \alpha^\phi \frac{\rho}{\rho_0}\right), \\ \Gamma_\phi^*(M, \rho) = \Gamma_\phi^{\text{vac}} + \alpha_{\text{coll}}^\phi \frac{\rho}{\rho_0} \end{cases}$$

Simulated scenarios:



What density does the ϕ feel in the reaction (p+Cu at 12 GeV)?

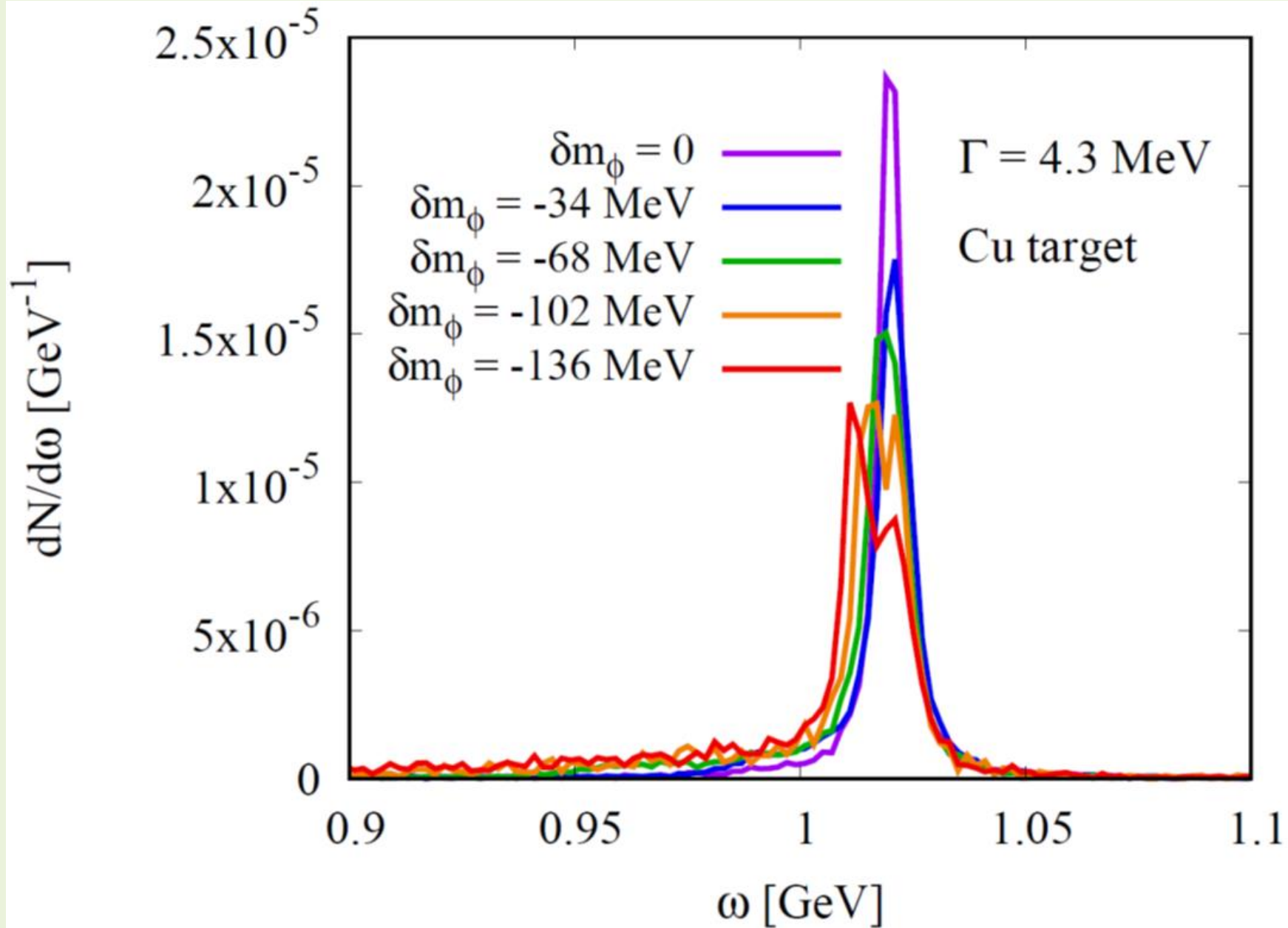


slow ϕ s

intermediate ϕ s

fast ϕ s

The dilepton spectrum in the ϕ meson region



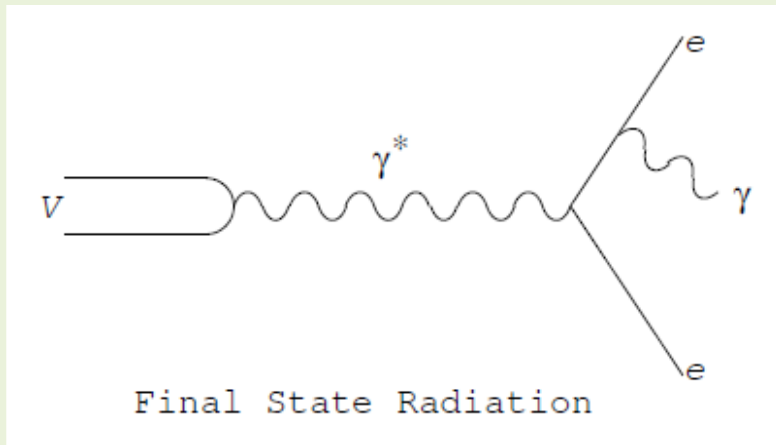
p + Cu at 12 GeV

No acceptance
corrections!

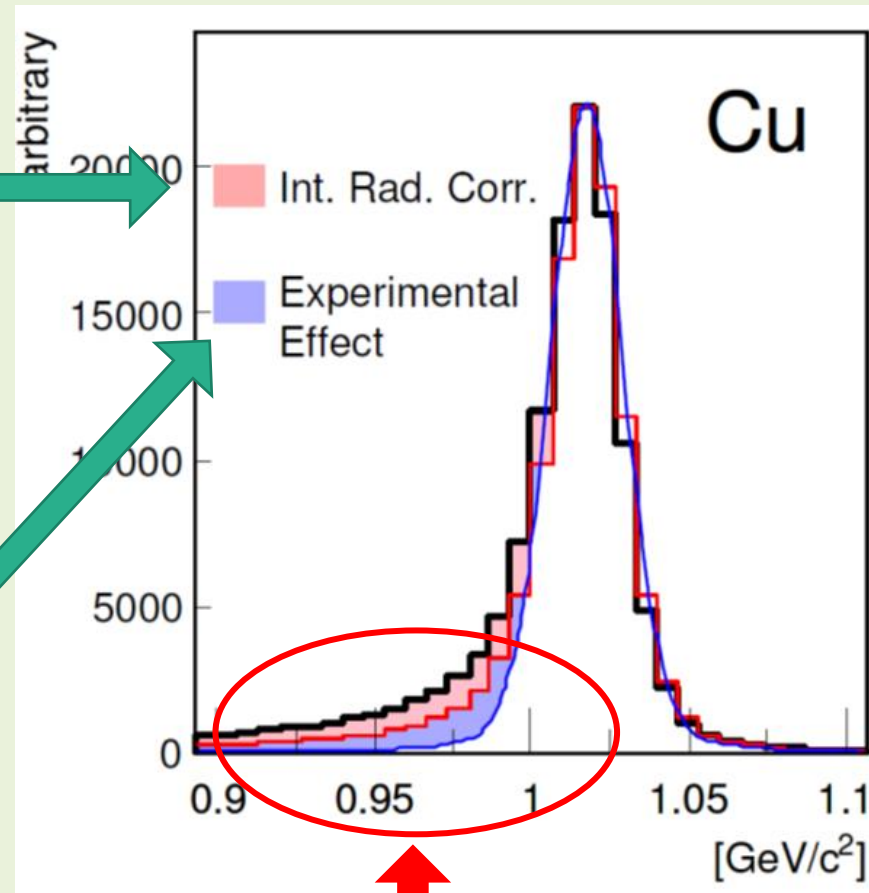
No finite
resolution effects!

No QED effects!

How do experimental rescattering and QED effects modify the dilepton spectrum?



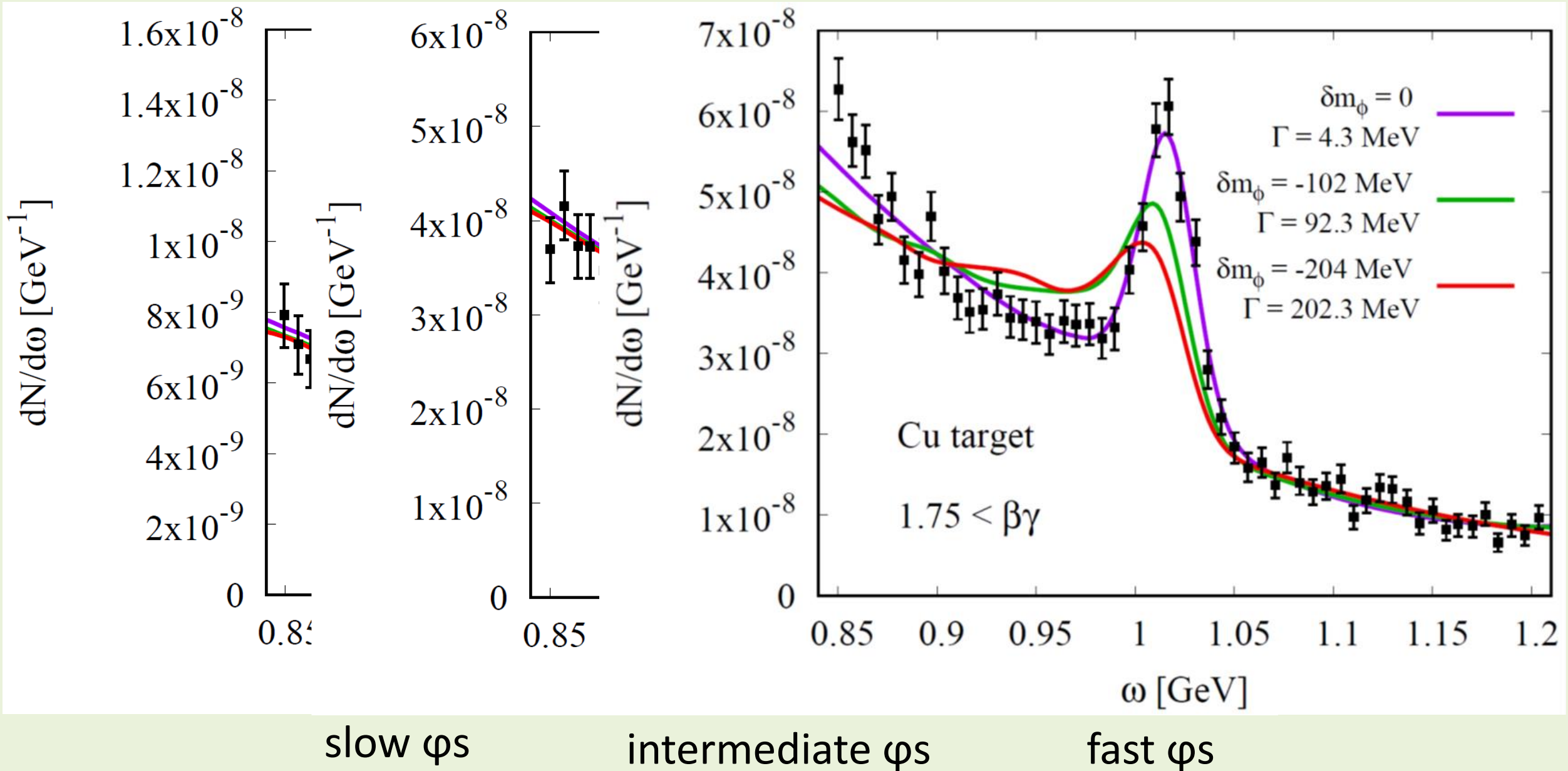
Rescattering effect
(multiple scattering,
energy loss)



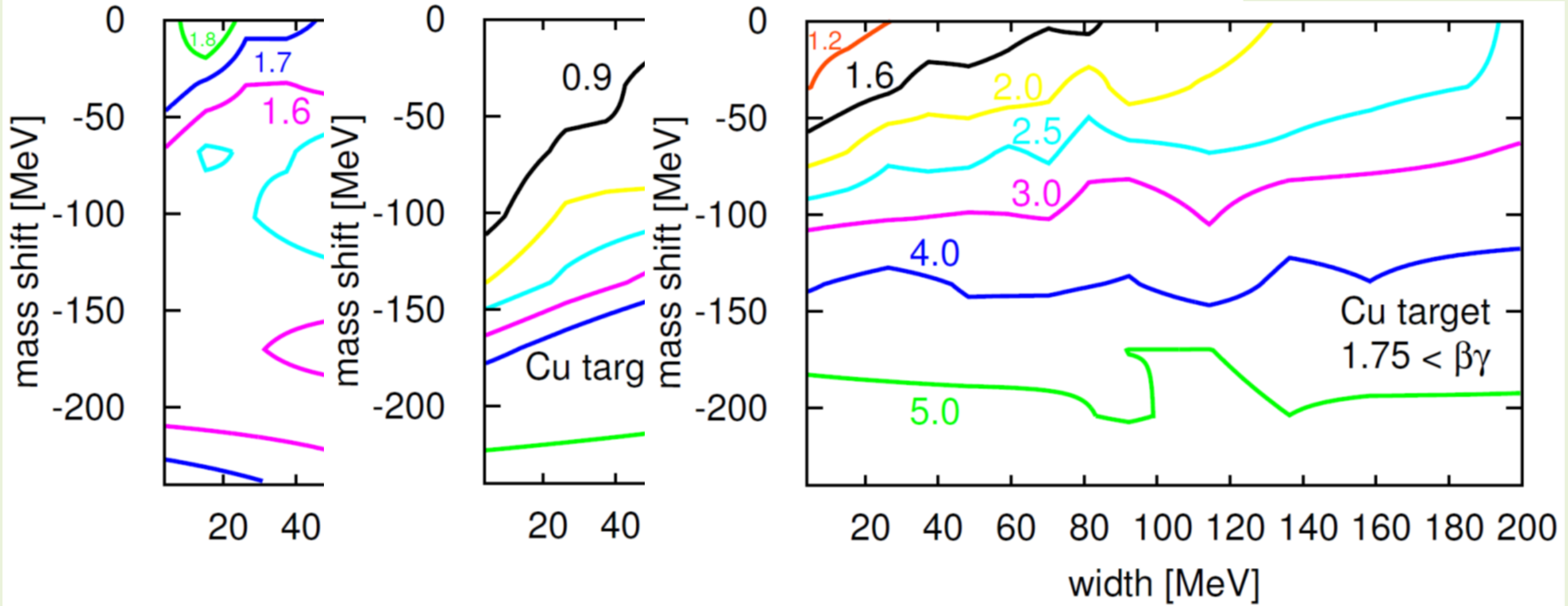
Similar to the shape expected
for a negative mass shift

PhD Thesis of R. Muto,
Kyoto U., 2007

Fits to experimental Copper target data (KEK, E325)



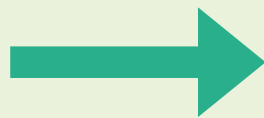
Fits to experimental Copper target data (KEK, E325)



slow ϕ s

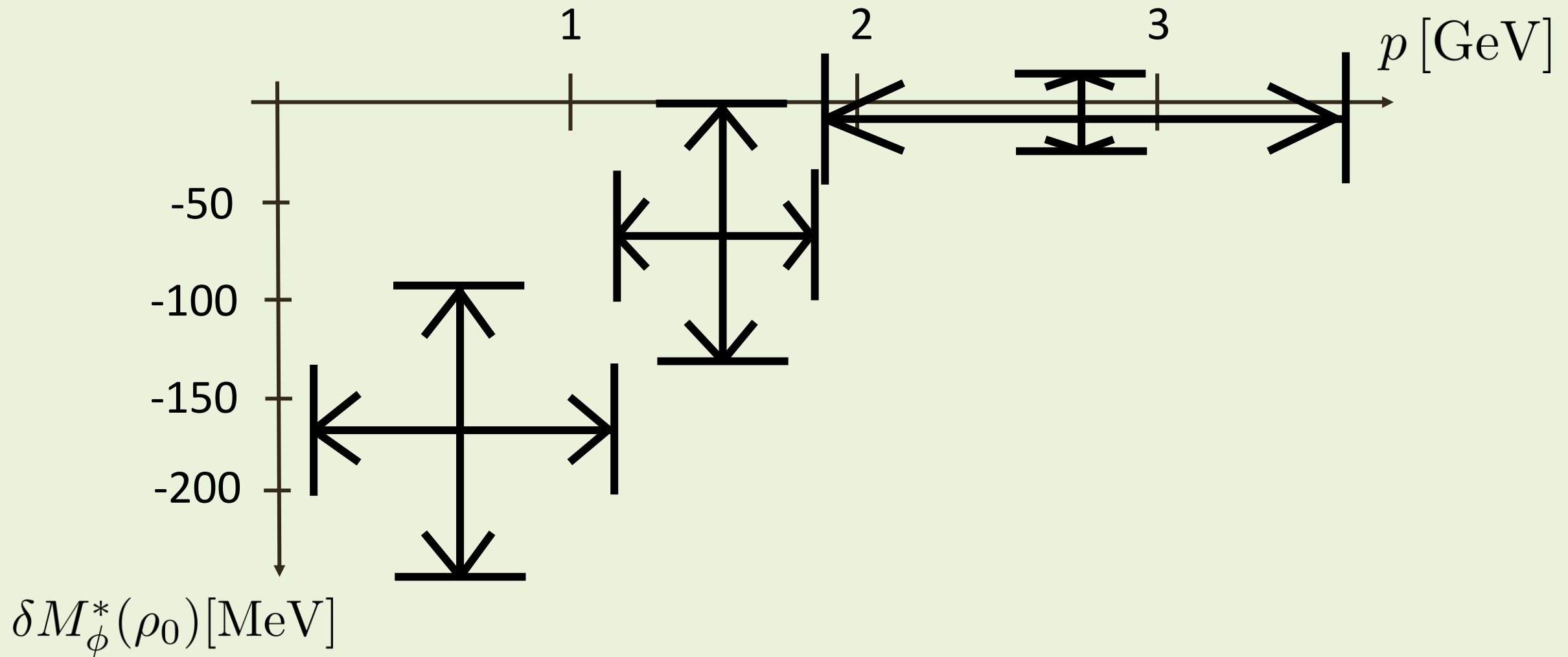
intermediate ϕ s

fast ϕ s



large momentum dependence!

Summary of results for Copper target data (E325)

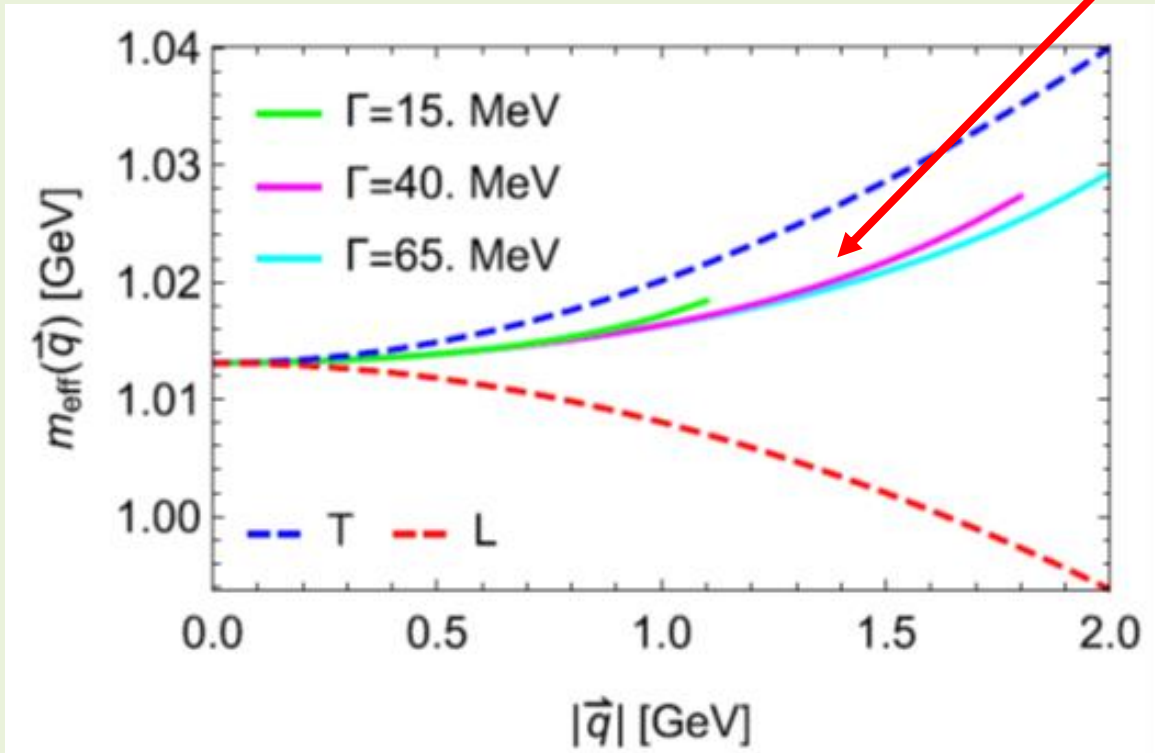


Most natural interpretation of our results



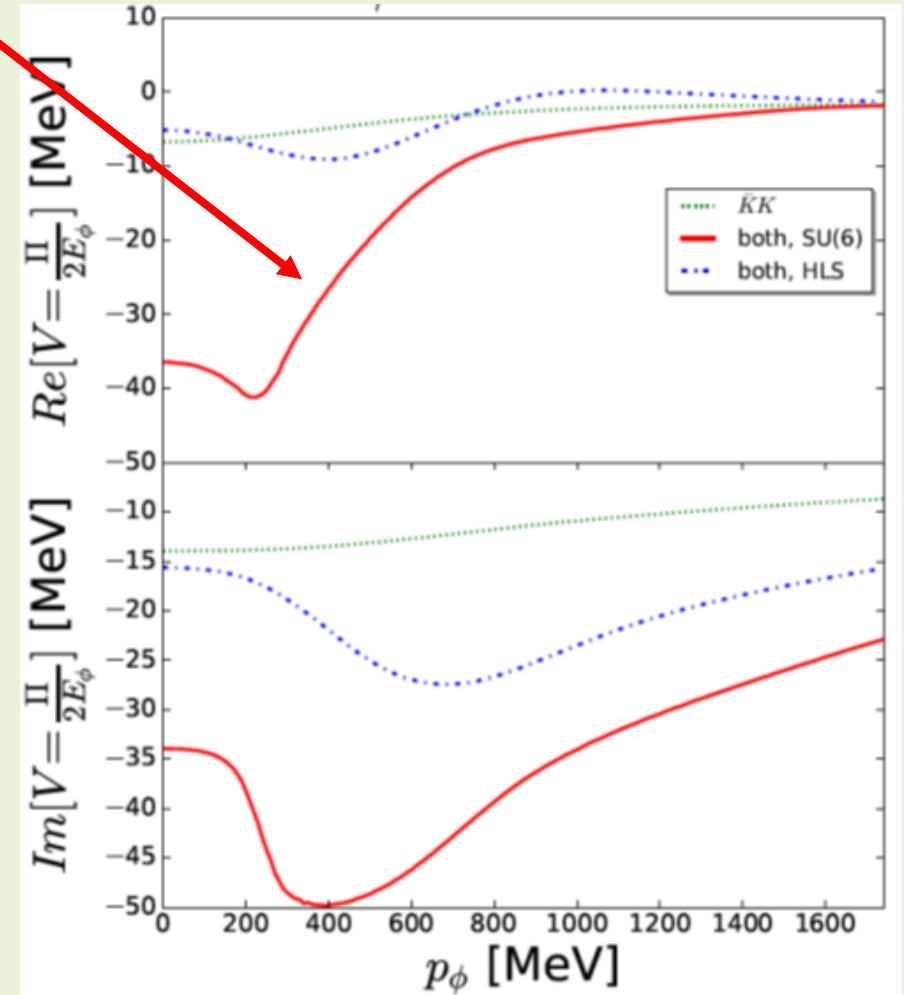
Momentum dependent mass shift

QCD sum rules



H.J. Kim and P. Gubler, Phys. Lett. B **805**, 135412 (2020).

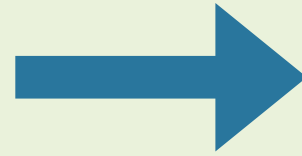
Hadronic effective theory



D. Cabrera *et al.*, Phys. Rev. C **95**, 015201 (2017).

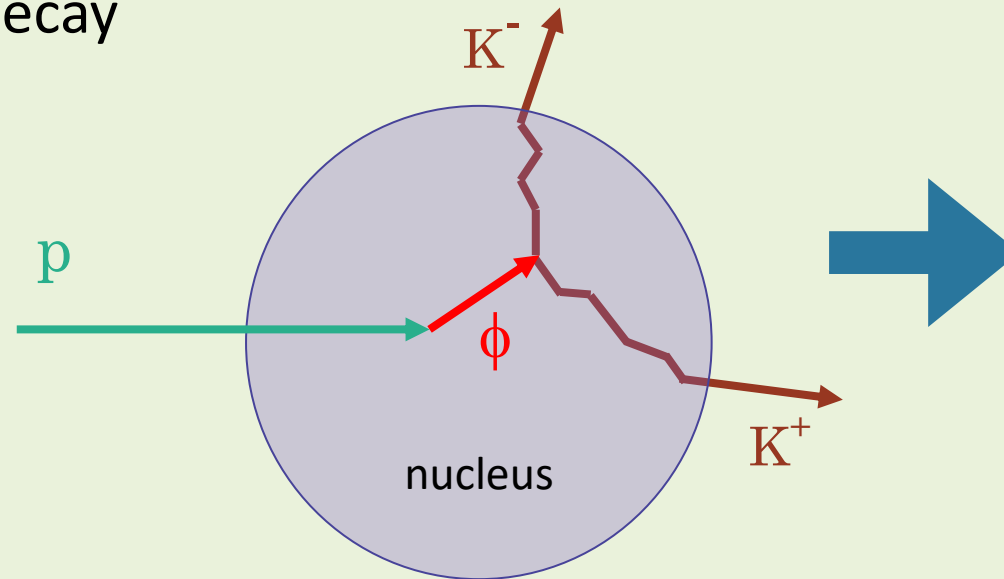
Outlook

- ★ A lot of new experimental information about the ϕ N interaction is becoming available (LHC, J-PARC, HADES)



Many opportunities for theorists!

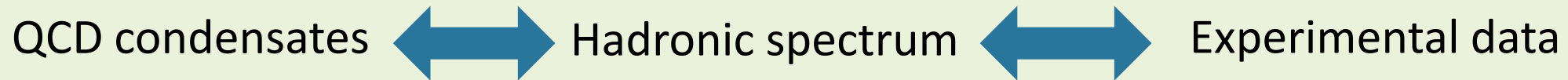
- ★ New proposal at J-PARC to measure the $K^+ + K^-$ decay



**Accurate
information about
the KN interaction
will be essential**

Summary and Conclusions

- ★ Relating modification of QCD condensates with hadron properties in nuclear matter is a non-trivial multi-step process



- ★ For studying the modification of the φ meson spectral function experimentally at finite density, a good understanding of the underlying reactions is needed

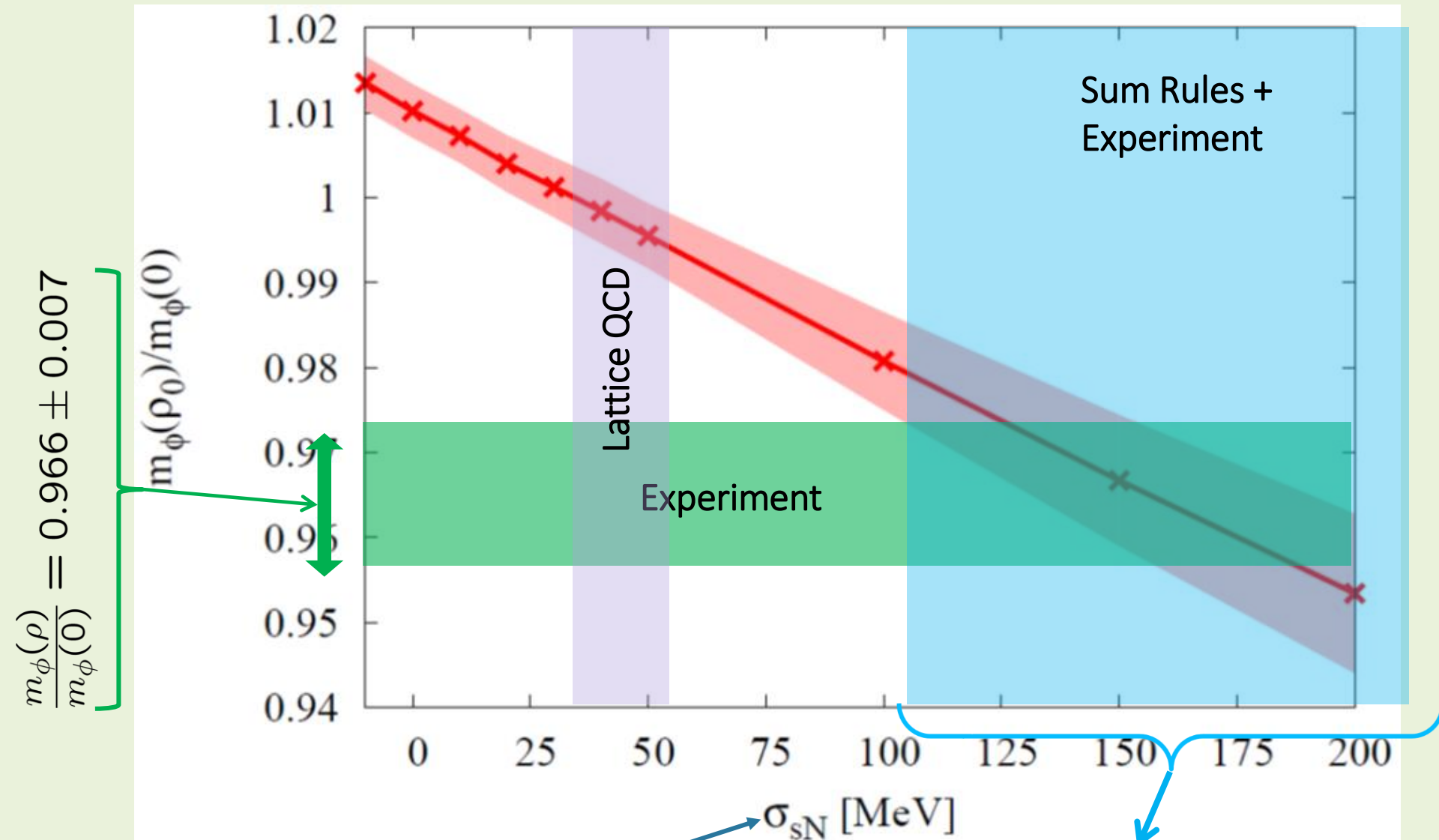
- ★ We conducted numerical simulations of the pA reactions measured at the E325 experiment at KEK, using the HSD transport code



Momentum-dependent mass shift is needed to explain the data

Backup slides

Consistency with QCD sum rules and lattice calculations?



Consistency would get much worse if the ϕ meson mass shift is about -100 MeV!!



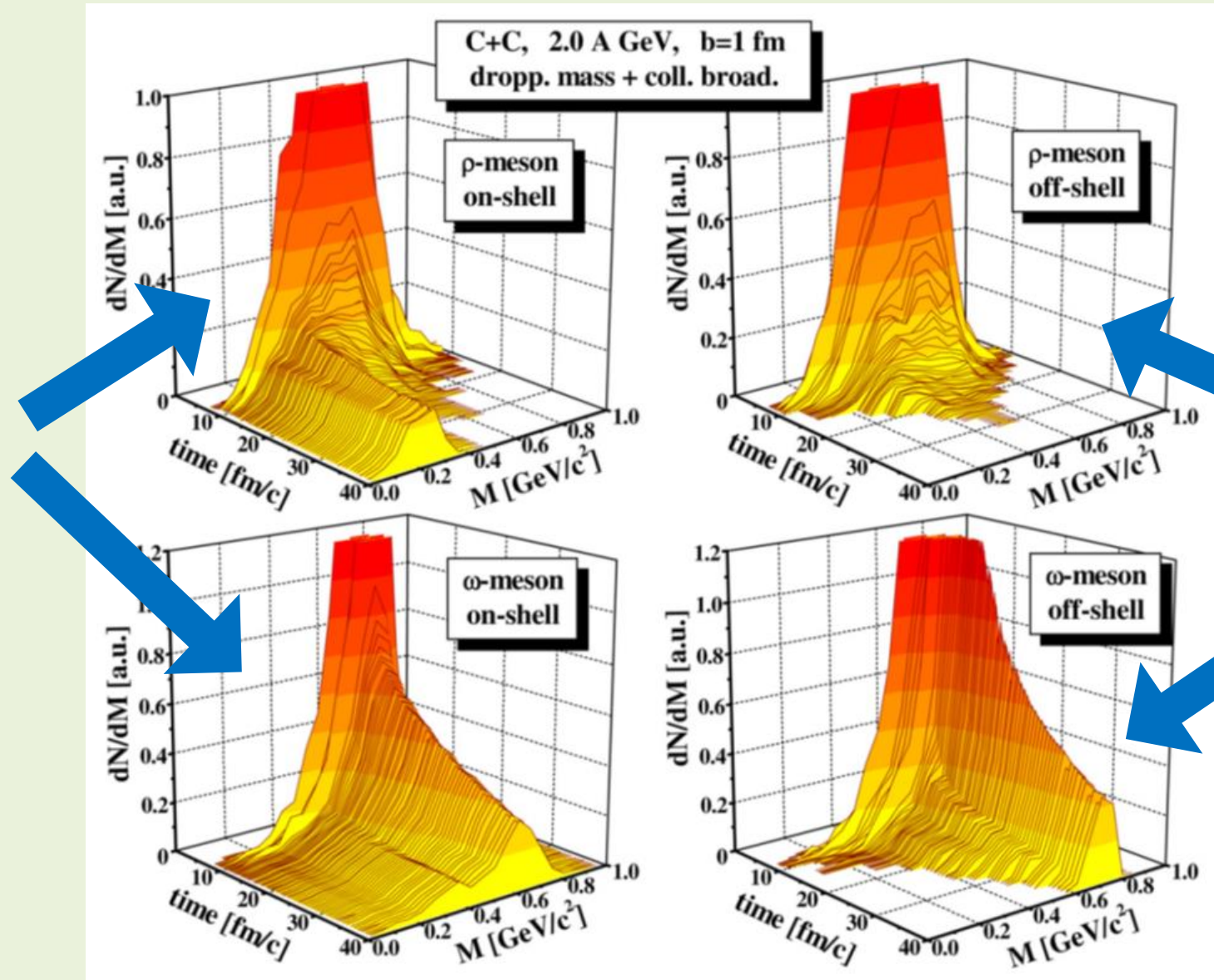
Big puzzle!!

$$\sigma_{sN} = m_s \langle N | \bar{s}s | N \rangle$$

$$\sigma_{sN} \sim 160 \pm 50 \text{ MeV}$$

The importance of off-shell contributions

Only on-shell contributions:
Vacuum spectral function
are not recovered at late
time of the reaction



Off-shell
contributions
included:
correct behavior

Example of a transport calculation

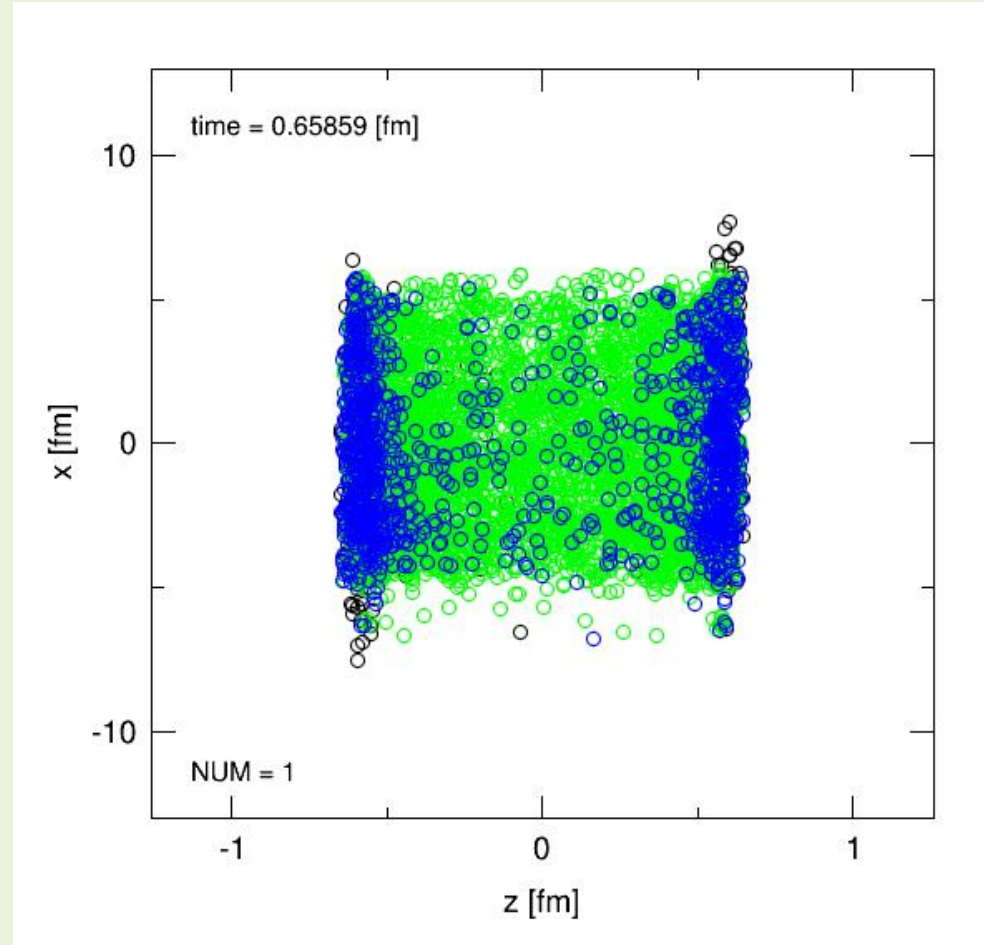
Au+Au collision at $s^{1/2} = 200$ GeV, $b = 2$ fm

nucleons

quarks

gluons

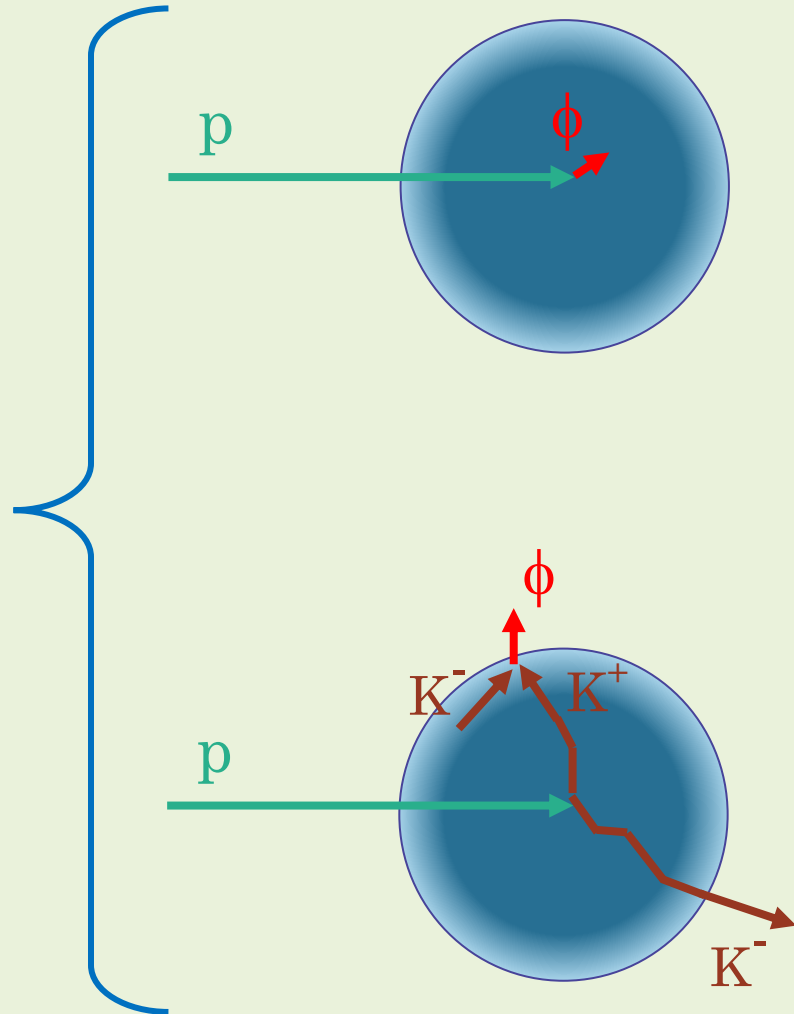
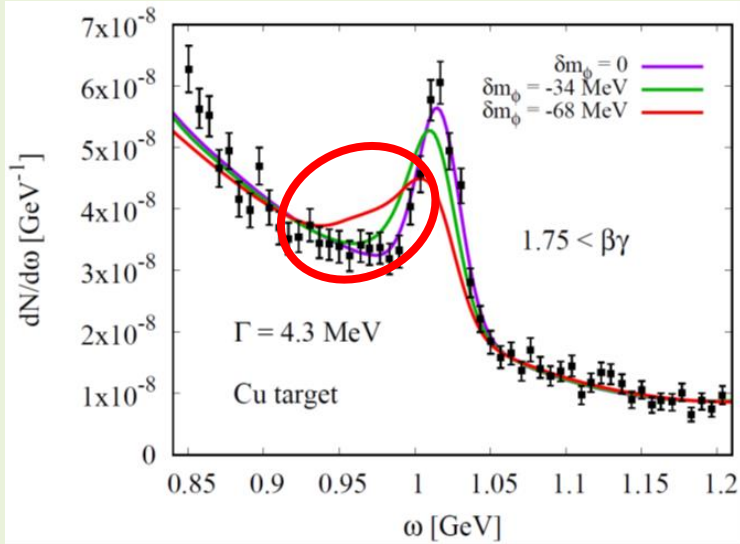
will not be included in the
simulations shown in this talk



Reason for large modification for fast ϕ mesons



Initial stage of ϕ meson production?



ϕ mesons are generated from high energy collisions (via strings)

→ large momentum

→ high density

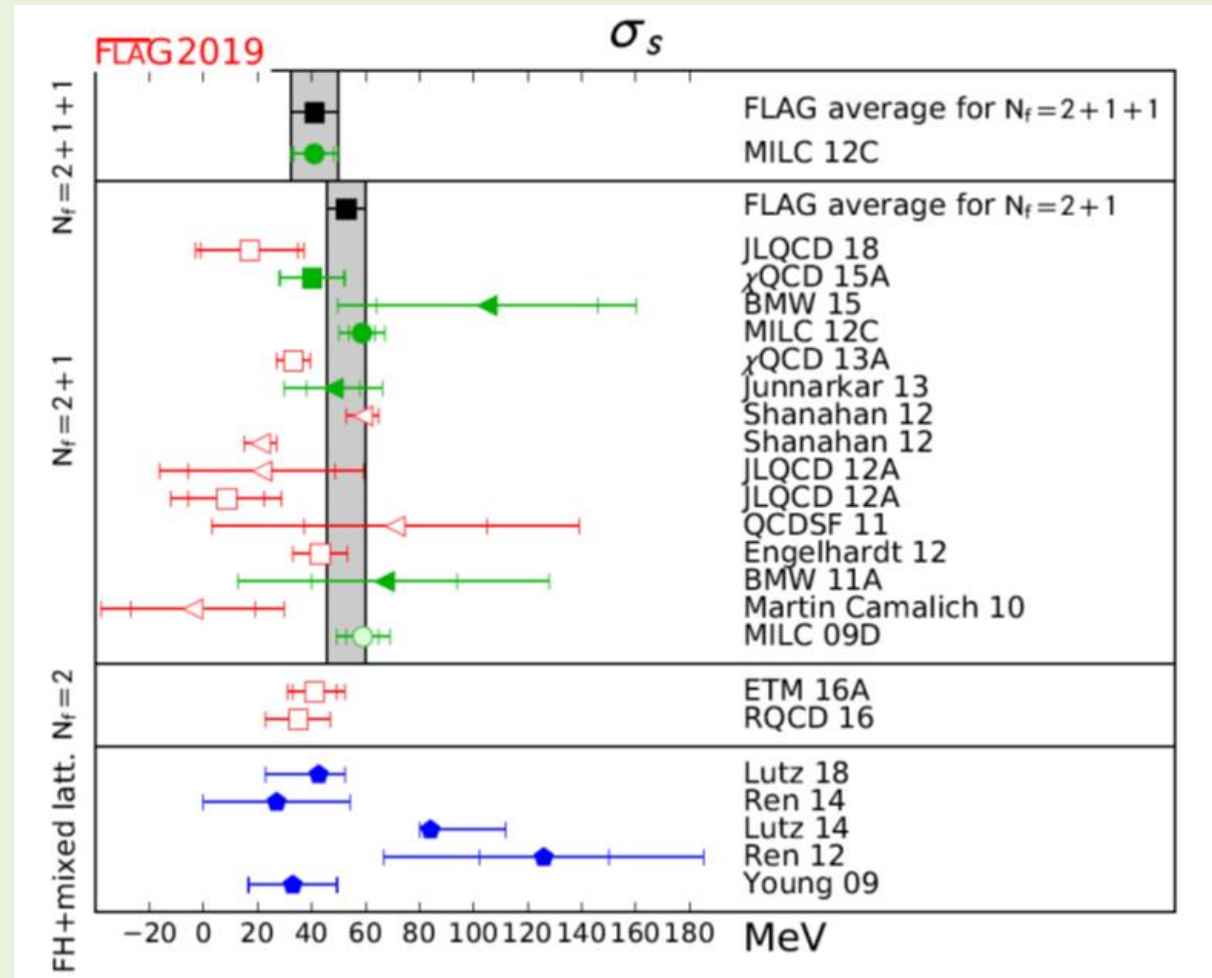
ϕ mesons are generated from low energy hadronic collisions

→ small momentum

→ low density

What does lattice QCD say about the strange sigma term?

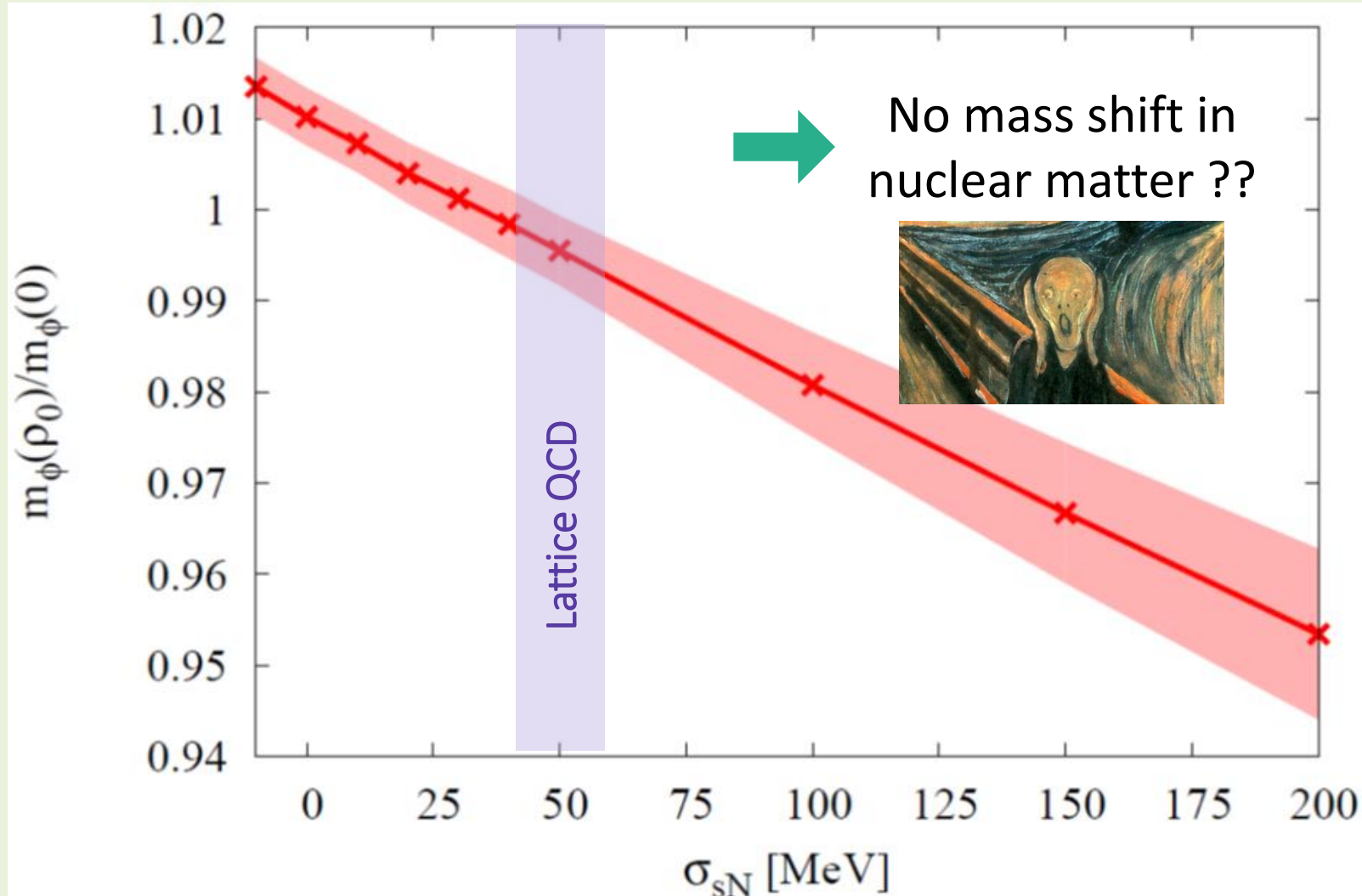
$$\sigma_{sN} = m_s \langle N | \bar{s}s | N \rangle$$



<http://flag.unibe.ch/2019/>

See also the most recent result of the BMW collaboration: Sz. Borsanyi et al., arXiv:2007.03319 [hep-lat].

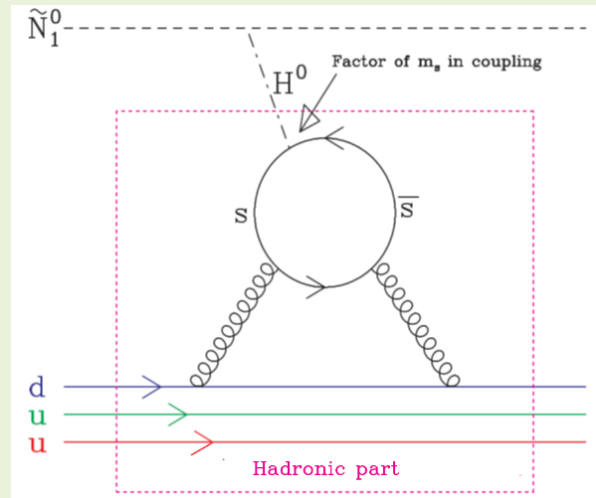
Combine QCD sum rules with lattice QCD



The strangeness content of the nucleon: $\sigma_{sN} = m_s \langle N | \bar{s}s | N \rangle$

Important parameter for dark-matter searches!

Neutralino:
Linear superposition of the
Super-partners of the Higgs, the
photon and the Z-boson



Adapted from:
W. Freeman and D. Toussaint (MILC Collaboration),
Phys. Rev. D **88**, 054503 (2013).

$$\sigma_{\text{scalar}}^{(\text{nucleon})} = \frac{8G_F^2}{\pi} M_Z^2 m_{\text{red}}^2 \left[\frac{F_h I_h}{m_h^2} + \frac{F_H I_H}{m_H^2} \frac{M_Z}{2} \sum_q \langle N | \bar{q}q | N \rangle \sum_i P_{\tilde{q}_i} (A_{\tilde{q}_i}^2 - B_{\tilde{q}_i}^2) \right]^2$$

most important contribution

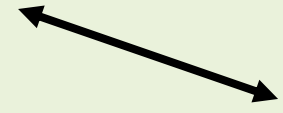
$$I_{h,H} = k_{u\text{-type}}^{h,H} g_u + k_{d\text{-type}}^{h,H} g_d$$

dominates

$$g_d = \frac{2}{27} \left(m_N + \frac{23}{4} \sigma_{\pi N} + \frac{25}{2} \sigma_{sN} \right)$$

Structure of QCD sum rules for the φ meson channel

(after application of the Borel transform)

$$\chi(x) = \bar{s}(x)\gamma_\mu s(x)$$


$$\frac{1}{M^2} \int_0^\infty ds e^{-\frac{s}{M^2}} \rho(s) = c_0(\rho) + \frac{c_2(\rho)}{M^2} + \frac{c_4(\rho)}{M^4} + \frac{c_6(\rho)}{M^6} + \dots$$

In Vacuum

$$\text{Dim. 0: } c_0(0) = 1 + \frac{\alpha_s}{\pi}$$

$$\text{Dim. 2: } c_2(0) = -6m_s^2$$

$$\text{Dim. 4: } c_4(0) = \frac{\pi^2}{3} \langle 0 | \frac{\alpha_s}{\pi} G^2 | 0 \rangle + 8\pi^2 m_s \langle 0 | \bar{s}s | 0 \rangle$$

$$\text{Dim. 6: } c_6(0) = -\frac{448}{81} \kappa \pi^3 \alpha_s \langle 0 | \bar{s}s | 0 \rangle^2$$

Structure of QCD sum rules for the φ meson

$$\frac{1}{M^2} \int_0^\infty ds e^{-\frac{s}{M^2}} \rho(s) = c_0(\rho) + \frac{c_2(\rho)}{M^2} + \frac{c_4(\rho)}{M^4} + \frac{c_6(\rho)}{M^6} + \dots$$

At finite density

(within the linear density approximation)

Dim. 0: $c_0(\rho) = c_0(0)$

$$\langle \bar{s}s \rangle_\rho = \langle 0 | \bar{s}s | 0 \rangle + \langle N | \bar{s}s | N \rangle \rho + \dots$$

Dim. 2: $c_2(\rho) = c_2(0)$

Dim. 4: $c_4(\rho) = c_4(0) + \rho \left[-\frac{2}{27} M_N + \frac{56}{27} m_s \langle N | \bar{s}s | N \rangle \right. \\ \left. + \frac{4}{27} m_q \langle N | \bar{q}q | N \rangle + A_2^s M_N - \frac{7}{12} \frac{\alpha_s}{\pi} A_2^g M_N \right]$

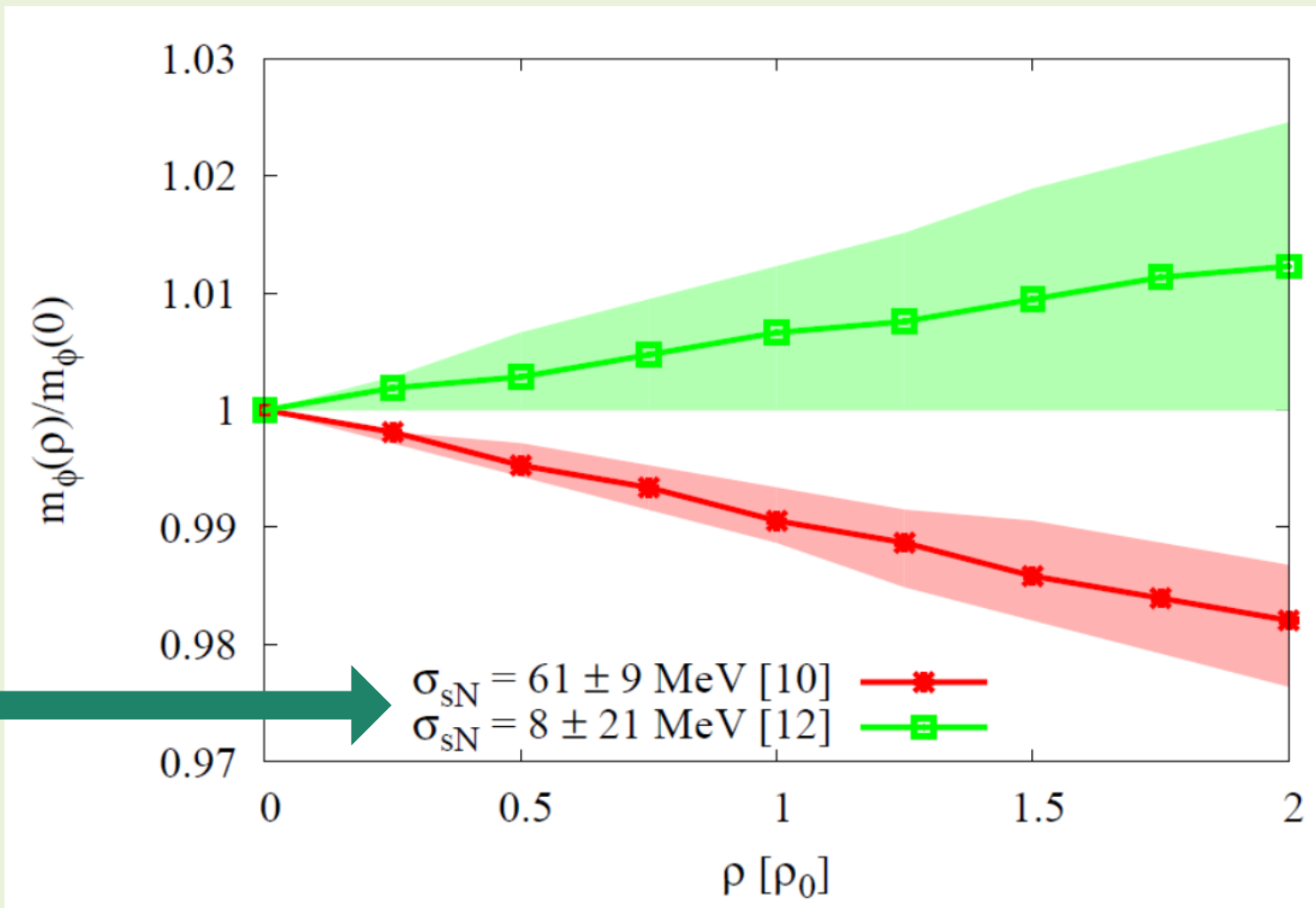
Dim. 6: $c_6(\rho) = c_6(0) + \rho \left[-\frac{896}{81} \kappa_N \pi^3 \alpha_s \langle \bar{s}s \rangle \langle N | \bar{s}s | N \rangle - \frac{5}{6} A_4^s M_N^3 \right]$

Results for the ϕ meson mass at rest

Most important parameter, that determines the behavior of the ϕ meson mass at finite density:


Strangeness content of the nucleon

$$\sigma_{sN} = m_s \langle N | \bar{s}s | N \rangle$$

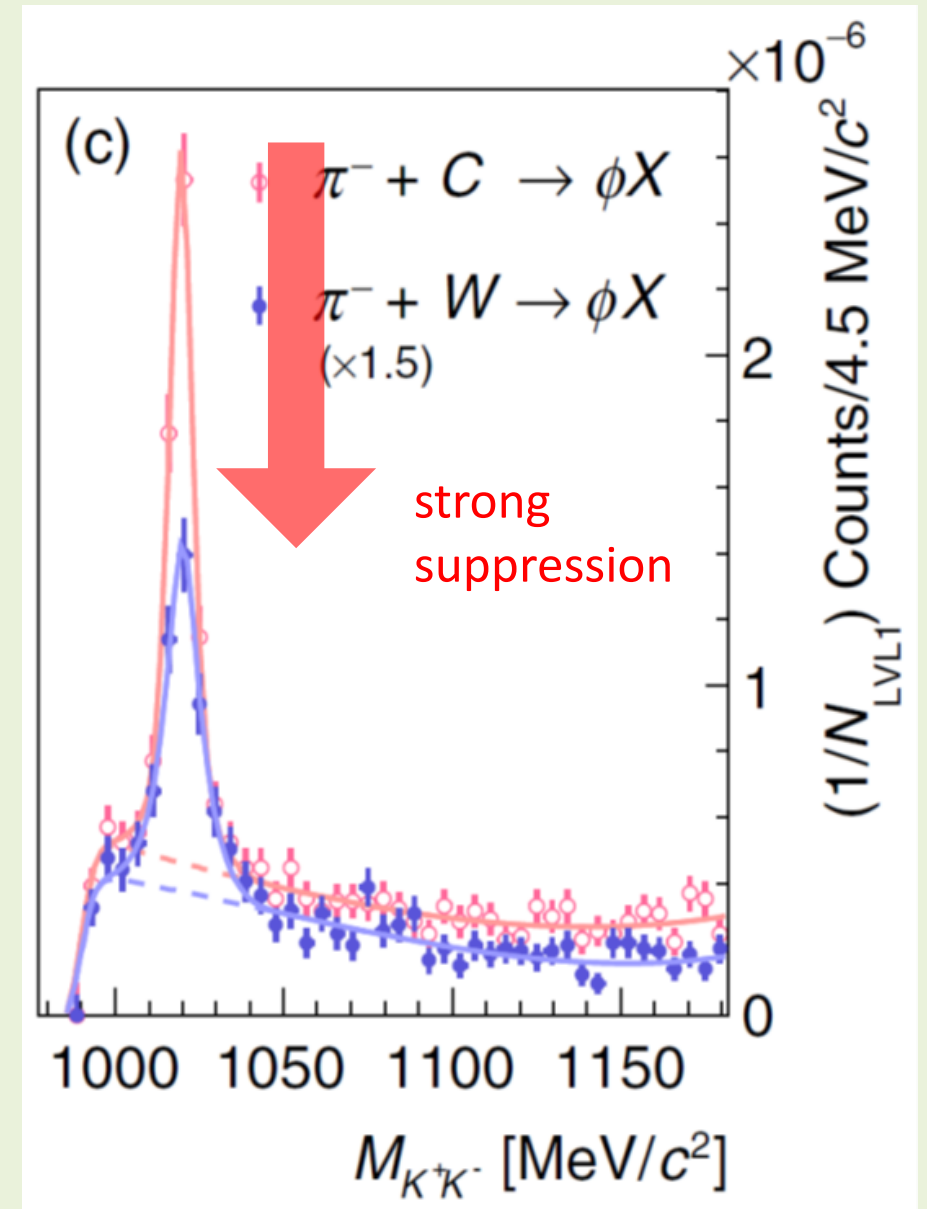


Recent experimental results

HADES: 1.7 GeV π^- -A-reaction

- ★ Larger suppression of K^- in the Tungsten target compared to the Carbon target
 - ★ K^-/ϕ ratio is similar for both Tungsten and Carbon targets
- 
- ★ Observation of large suppression (broadening?) of the ϕ meson in large nuclei

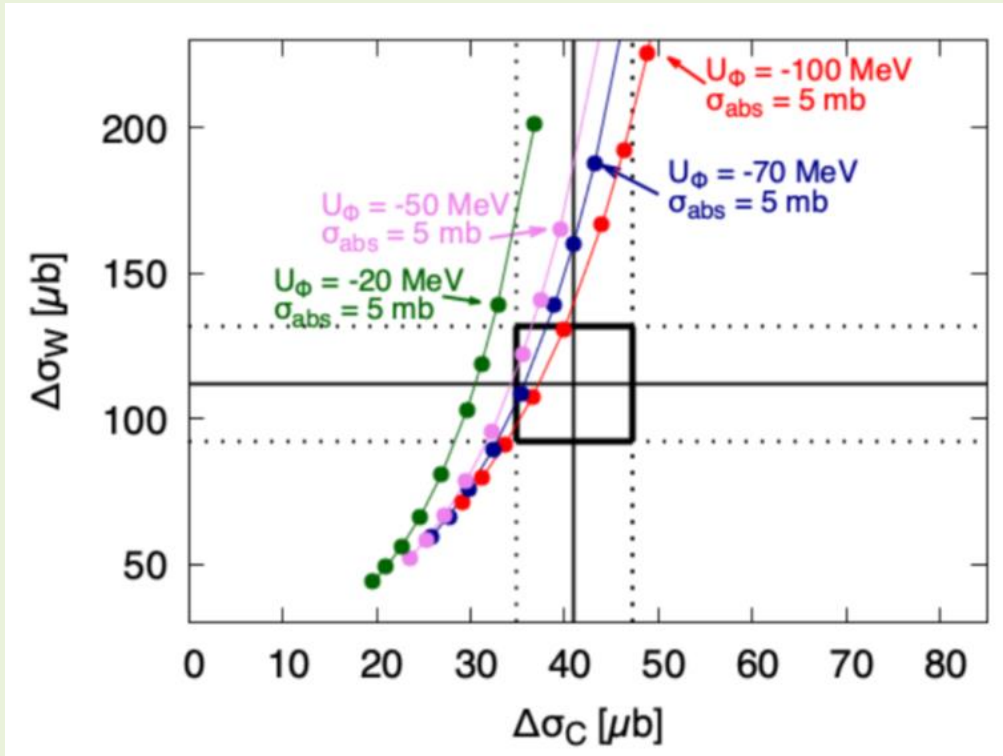
K^+K^- - invariant mass spectrum



Even more recent results

HADES: 1.7 GeV π^- A-reaction

K^+K^- - invariant mass spectrum

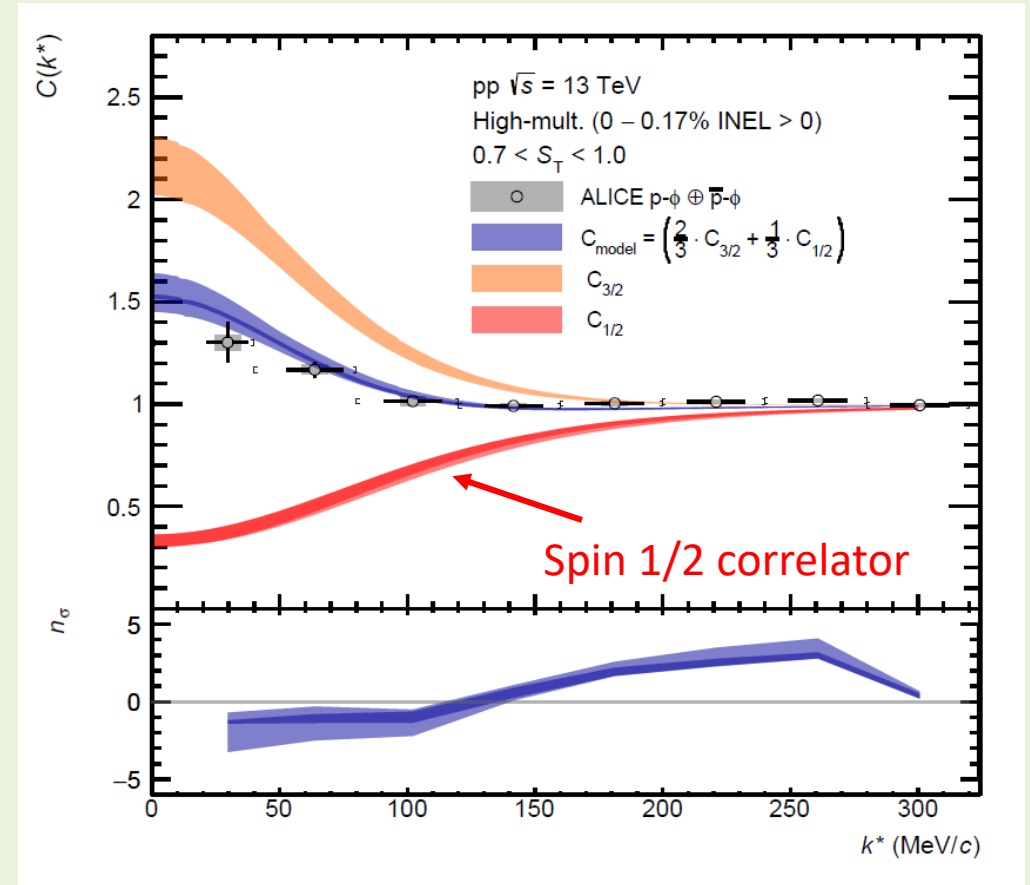


Theoretical calculation by E. Ya. Paryev:
E. Ya. Paryev, Nucl. Phys. A **1032**, 122624 (2023).

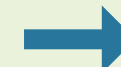


Attractive ϕ -nucleus potential:
-(50 - 100) MeV

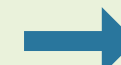
Combination of ALICE pp-data and
HAL QCD (spin 3/2) calculation



E. Chizzali et al., arXiv:2212.12690 [nucl-ex].



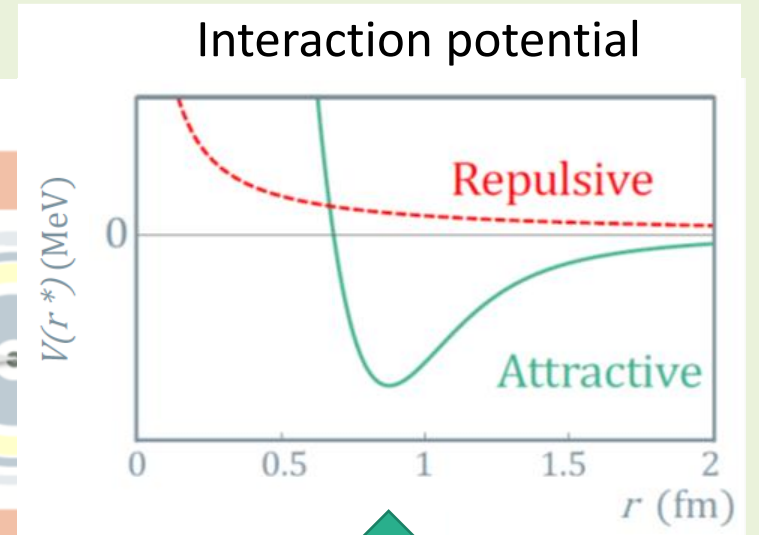
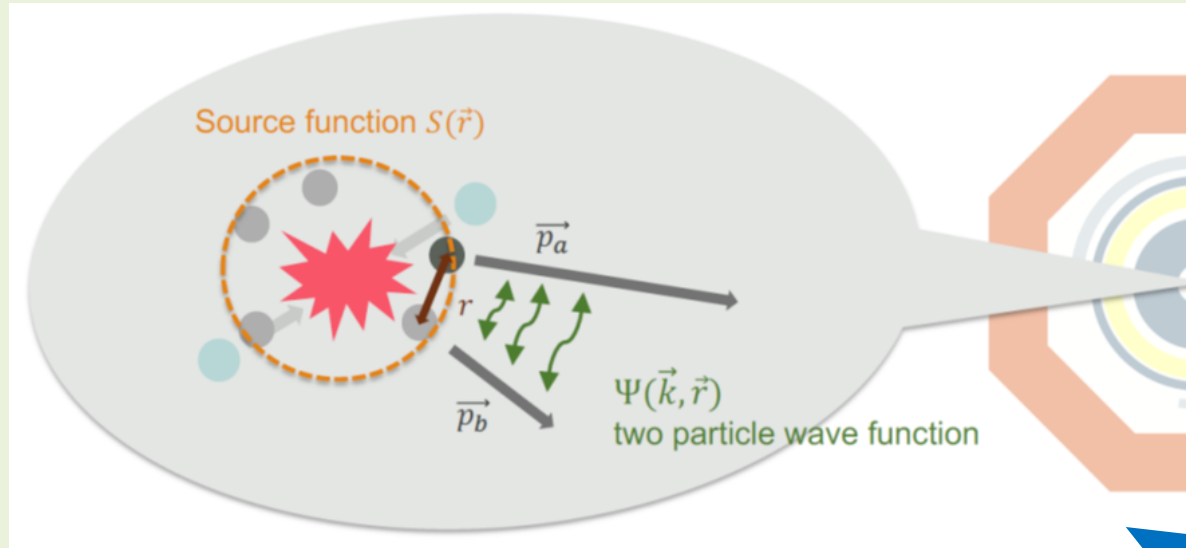
Evidence for ϕ -N bound state!



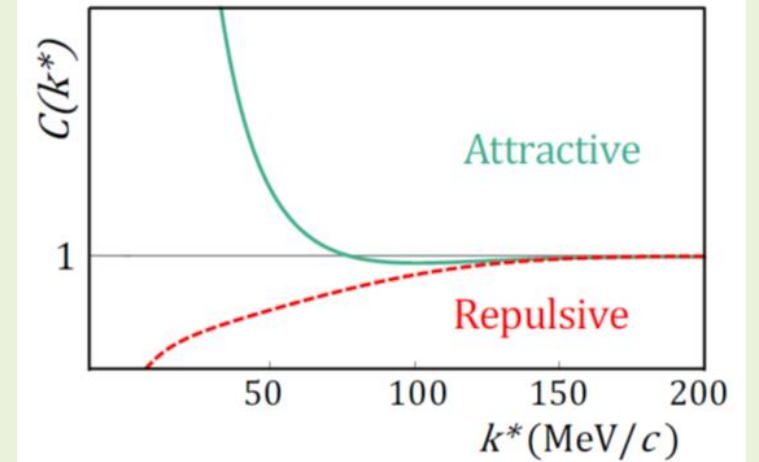
Attractive ϕ -nucleus potential \approx -100 MeV

New experimental results

ALICE (Femtoscscopy)



Correlation function



The observable to be measured: the correlation function:

$$C(k) = \mathcal{N} \frac{N_{\text{Same}}}{N_{\text{Mixed}}} = \int S(\vec{r}) |\Psi(\vec{k}, \vec{r})|^2 d^3\vec{r}$$


Emission source
(Gaussian)

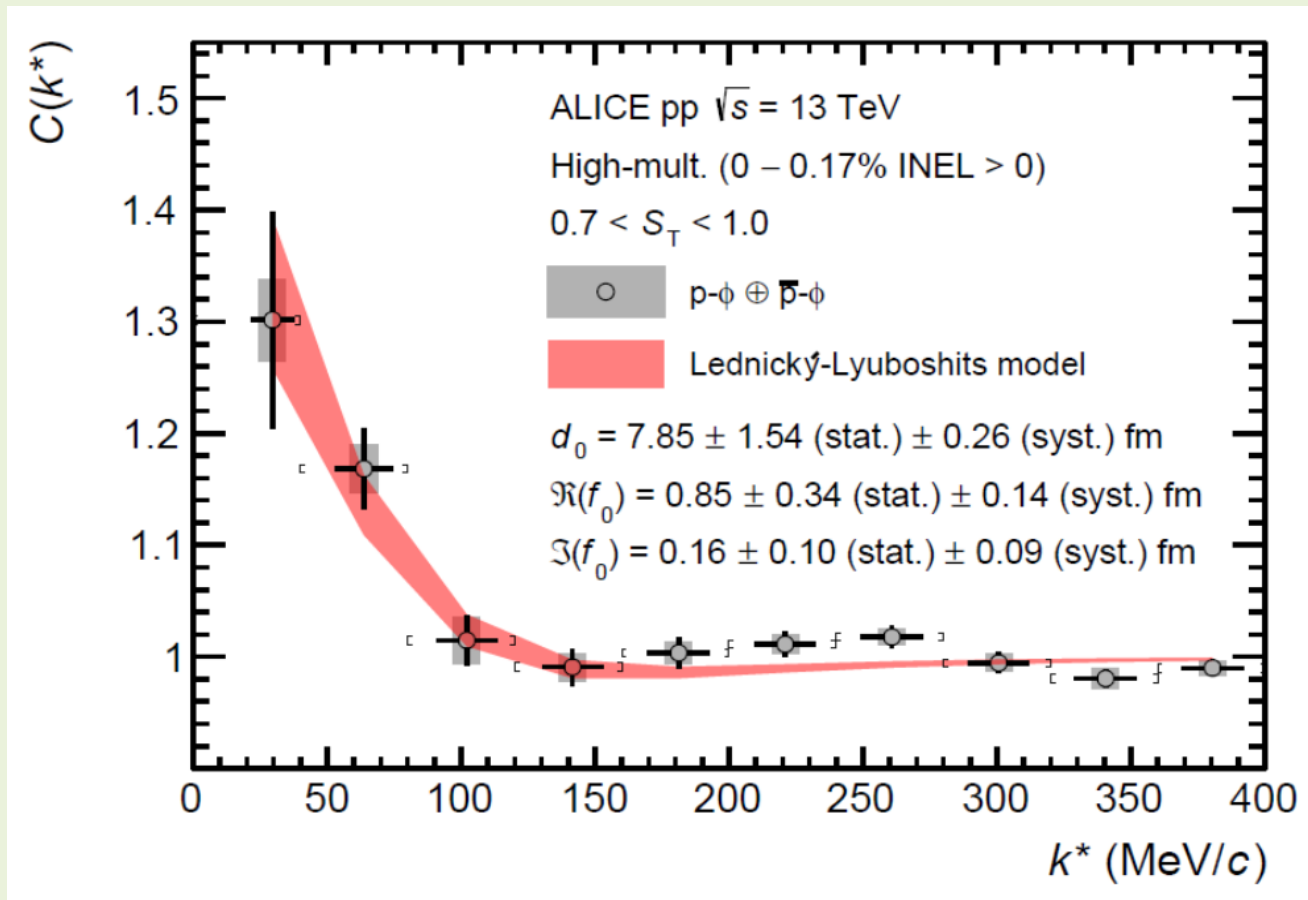
Relative momentum
of the particle pair

New experimental results

ALICE

Measurement of ϕ N correlation

Attraction!




Extracted ϕ N scattering length

Real part:

$$\Re(f_0) = 0.85 \pm 0.34(\text{stat.}) \pm 0.14(\text{syst.}) \text{ fm}$$



Attractive

Imaginary part:

$$\Im(f_0) = 0.16 \pm 0.10(\text{stat.}) \pm 0.09(\text{syst.}) \text{ fm}$$



Small
absorption/broadening ?

Our tool: a transport approach

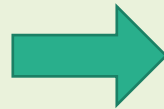
Basic Ingredient 1: Solve a Boltzmann-Uehling-Uhlenbeck (BUU) type equation for each particle type

$$\left(\frac{\partial}{\partial t} + \vec{\nabla}_p \epsilon \cdot \vec{\nabla}_r - \vec{\nabla}_r \epsilon \cdot \vec{\nabla}_p \right) f_a(\vec{r}, \vec{p}; t) = I_{\text{coll}}[f_a(\vec{r}, \vec{p}; t)]$$

Includes mean field
(tuned to reproduce
nuclear matter properties)

particle distribution
function

Basic Ingredient 2: „Testparticle“ approach



$$f_h(\mathbf{r}, \mathbf{p}; t) = \frac{1}{N_{\text{test}}} \sum_i^{N_h(t) \times N_{\text{test}}} \delta(\mathbf{r} - \mathbf{r}_i(t)) \delta(\mathbf{p} - \mathbf{p}_i(t))$$

Example of a transport calculation

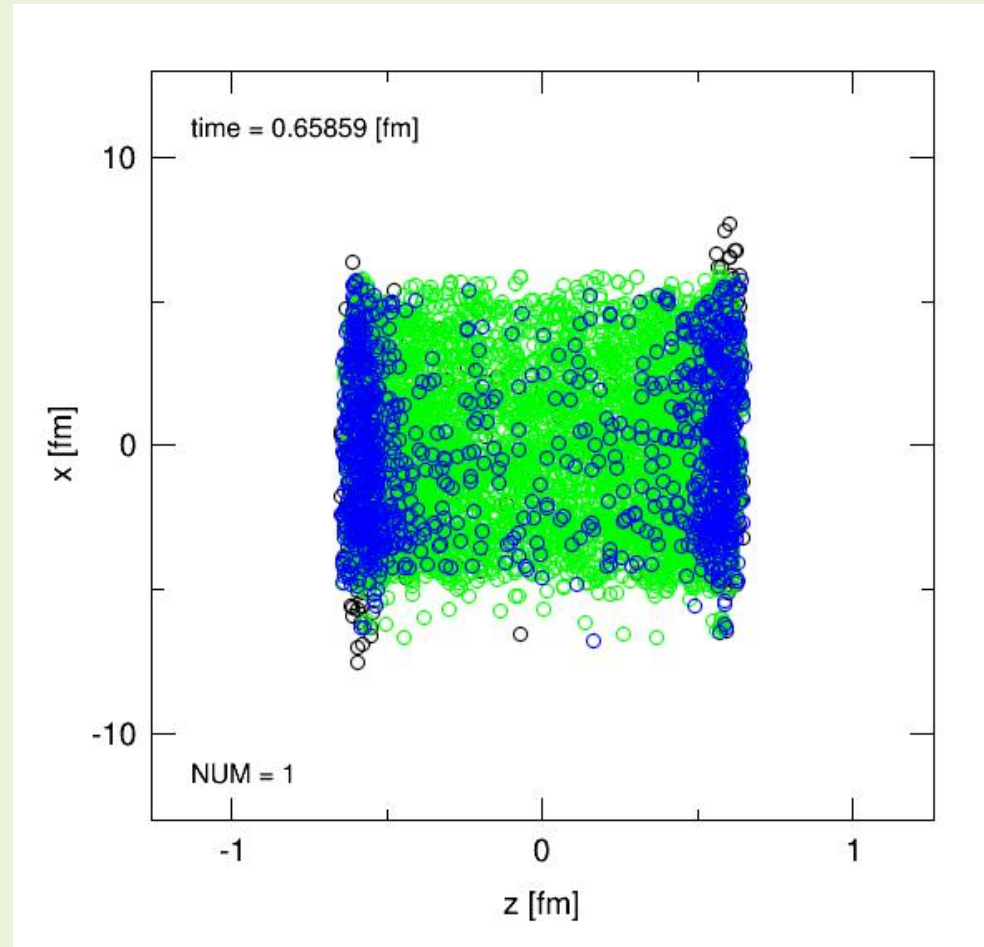
Au+Au collision at $s^{1/2} = 200$ GeV, $b = 2$ fm

nucleons

quarks

gluons

will not be included in the
simulations shown in this talk



Final step: comparison to experimental data

- Potential issues:
- ★ Experimental background is not included in the simulation
 - ★ Normalization of the experimental dilepton spectrum is not given



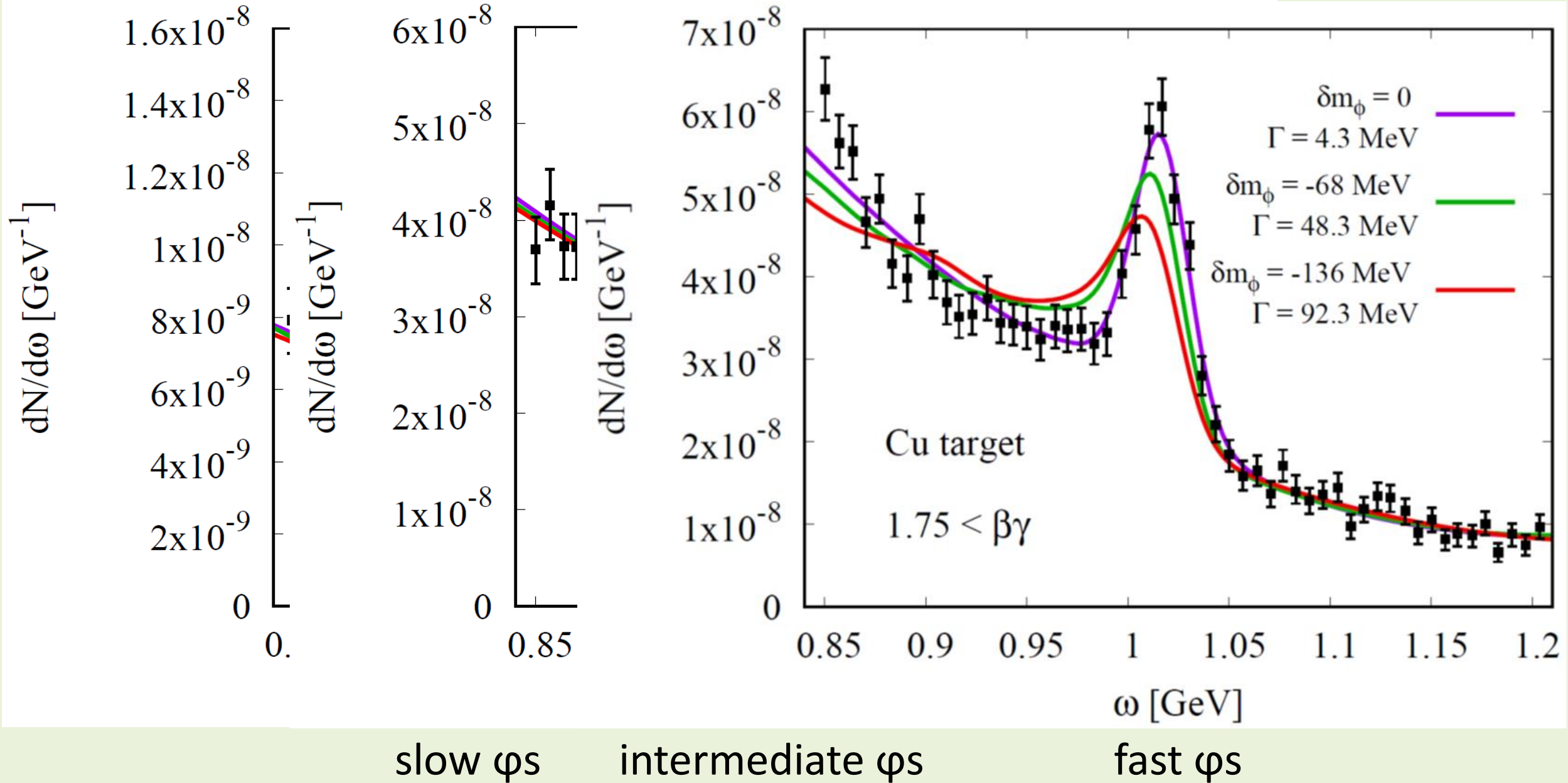
Fit to experimental data is necessary!

Dilepton spectrum:

$$\rho(\omega) = \underbrace{a\omega^2 + b\omega + c}_{\text{Background}} + \underbrace{A\rho_{\phi, \text{HSD}}(\omega)}_{\phi \text{ meson signal}}$$

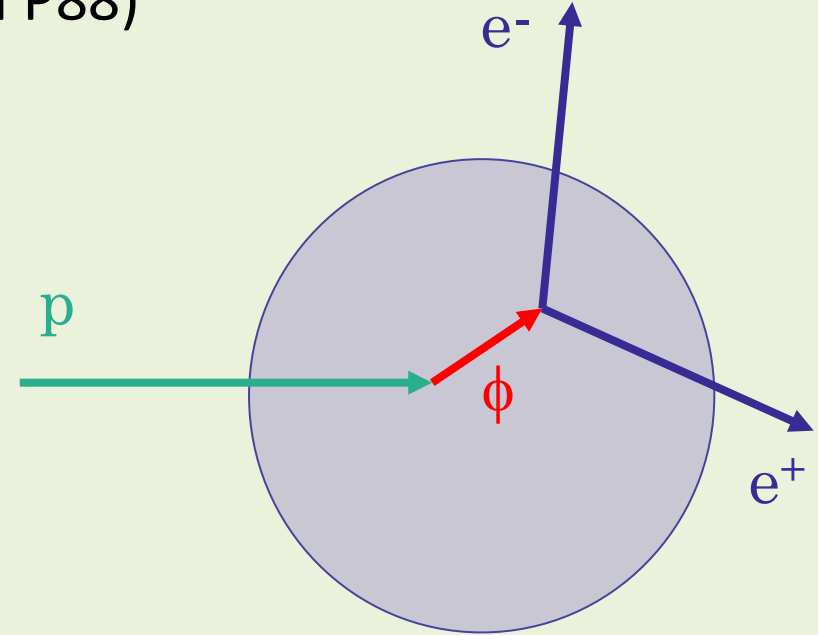
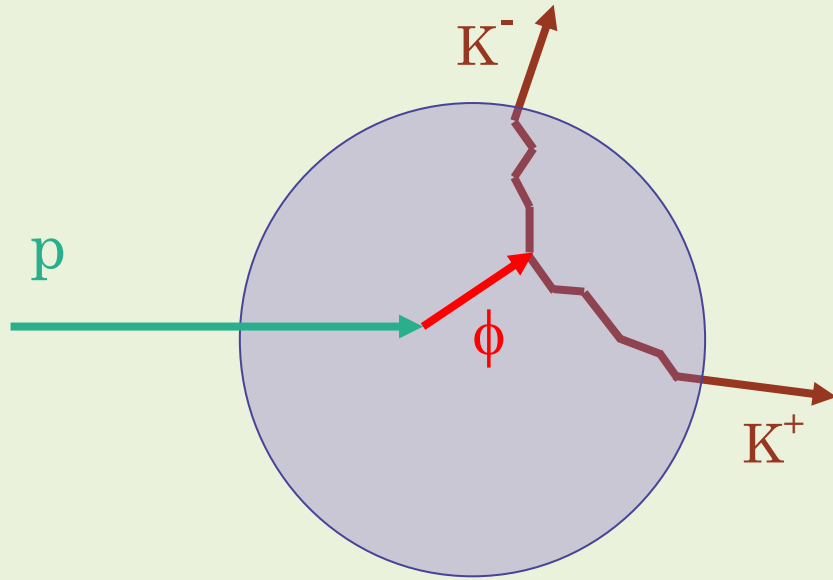
Fitted to the experimental dilepton spectrum
independently for each $\beta\gamma$ -region

Fits to experimental Copper target data (E325)



What about the K^+K^- decay channel?

(new J-PARC proposal P88)



Kaons feel the strong interaction \rightarrow Distorted in-medium ϕ meson signal \times

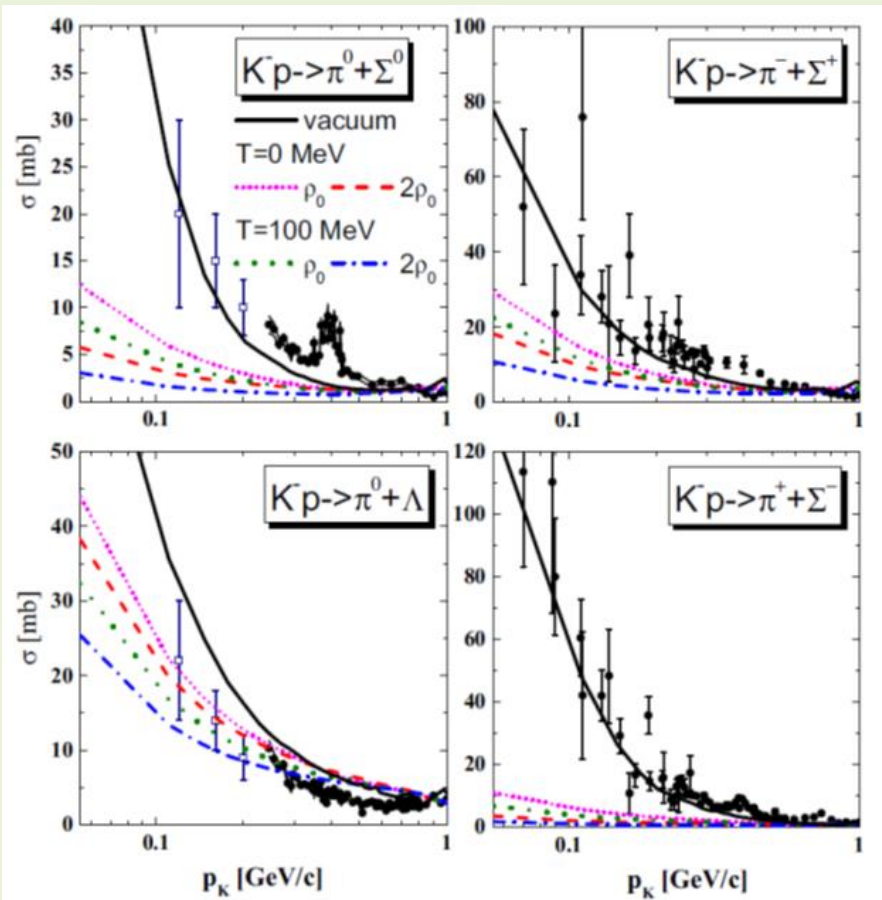
Large branching ratio \rightarrow Good statistics \bigcirc

Kaons do not feel the strong interaction \rightarrow Clear in-medium ϕ meson signal \bigcirc

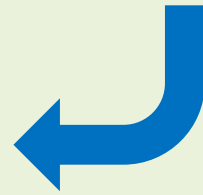
Small branching ratio \rightarrow Bad statistics \times

Treatment of KN-interactions

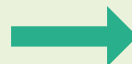
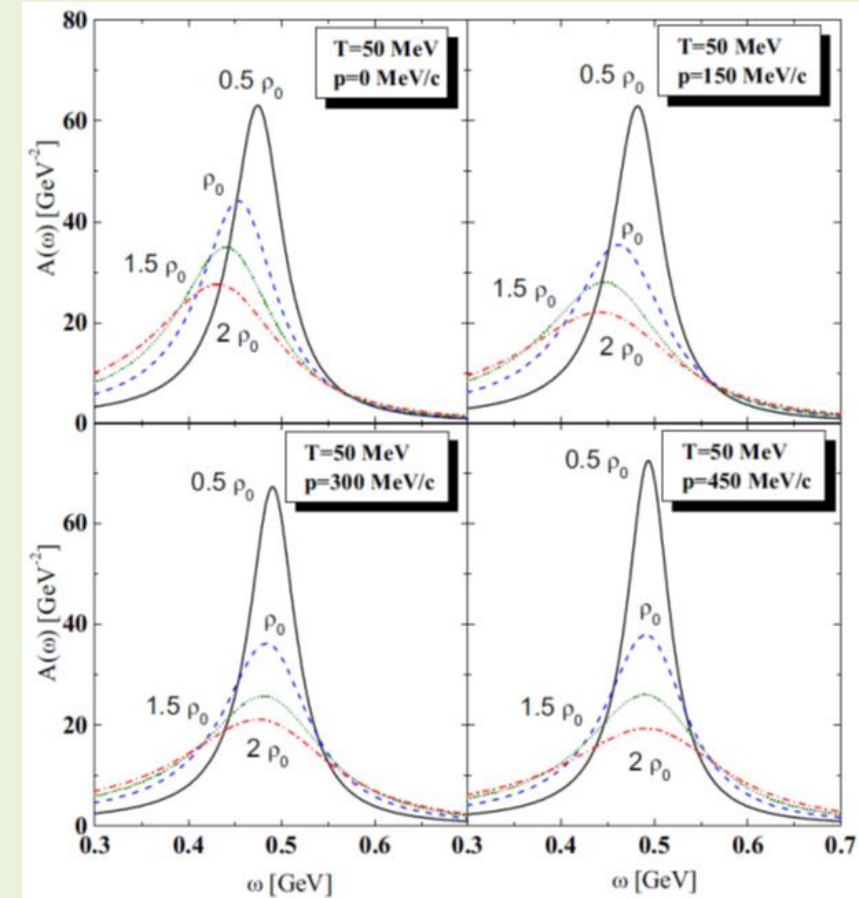
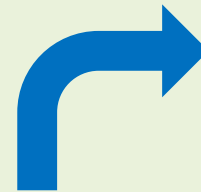
Density dependent cross sections based on the chiral unitary model
(including coupled channels and s-/p-wave of $\bar{K}N$ interactions)



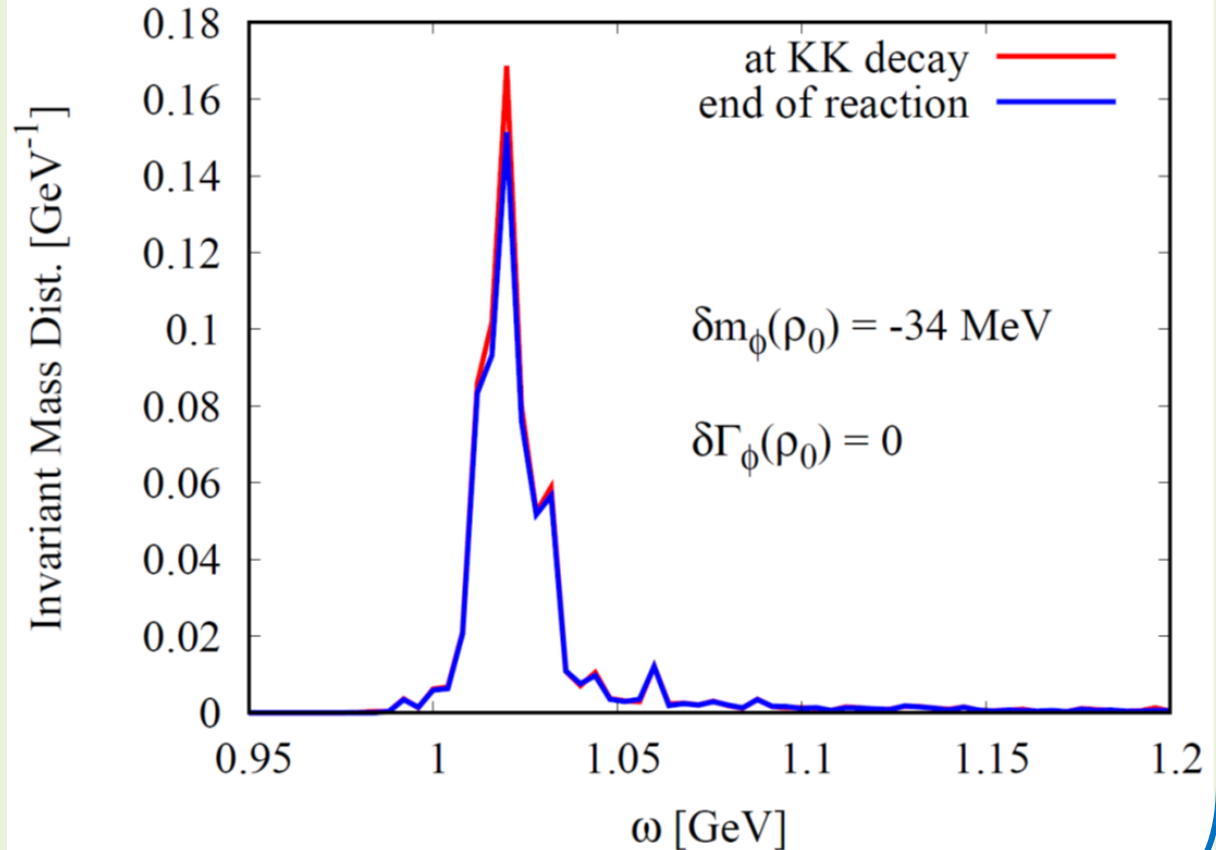
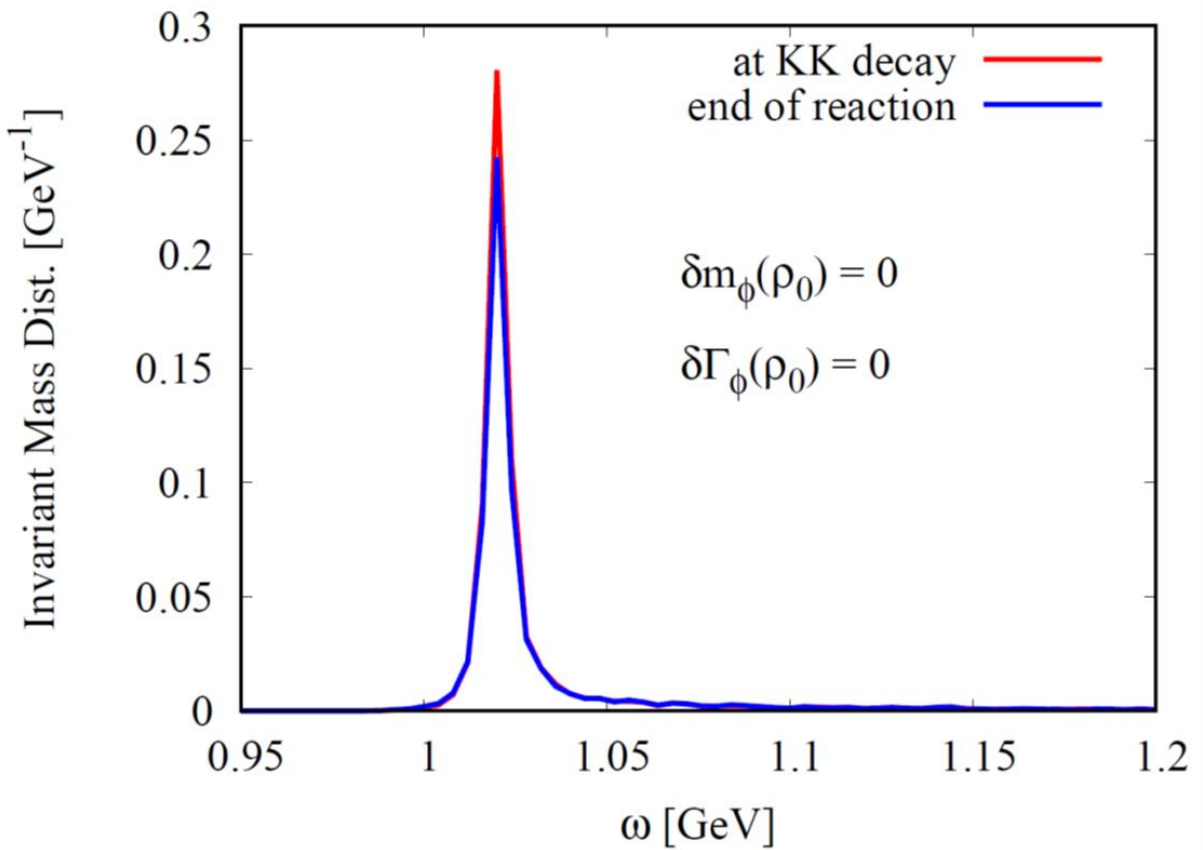
Vacuum and density dependent $\bar{K}N$ cross sections



Density dependent \bar{K} spectral functions



Distortion of the in-medium ϕ meson signal in the K^+K^- channel (p + Cu at 30 GeV)



Small distortion effect from the strong KN interaction !?