#### FORWARD-BACKWARD ASYMMETRY OF TOP QUARK IN UNPARTICLE PHYSICS

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# Outline

Motivation  $\rightarrow$  Observation at Tevatron henomenon & History over Q-FBA **ossib**le Models & Mechanisms ur results in Unparticle Physics Summary (a) 1000000000

### **1. Observations at Tevatron** DØ PRL100, 142002 (2008)





Njet	DØ data	MC@NLO	
≥4	$12\pm$ 8(stat) $\pm$ 1(sys)	0.8±0.2(stat)±1.0(acc)	
= 4	$19\pm$ 9(stat) $\pm$ 2(sys)	2.3±0.2(stat)±1.0(acc)	
$\geq$ 5	$-16^{+15}_{-17}$ (stat) $\pm 3$ (sys)	-4.9±0.4(stat)±1.0(acc)	







Δ Υ

# 2. Phenomenon

### Asymmetry If CP is invariant, Integral charge asymmetry $N_{\overline{t}}(p) = N_t(\overline{p}) \rightarrow A_C = A_{FB}$ $N_t(p) - N_{\overline{t}}(p)$ $N_t(p) + N_{\overline{t}}(p)$ :# of particle i observed in the direction of particle j Forward-backward asymmetry p $A_{FB} = \frac{N_t(p) - N_t(\overline{p})}{N_t(p) + N_t(\overline{p})}$

# History over Heavy Quark FBA

1. Brown et al, PRL43(1979)1069; FBA of c-quak production in analogy to QED.

[1] F. Halzen, P. Hoyer, C.S. Kim, PLB195(1987)74;
 FBA of b,t-quark in QCD from (i) radiative corrections to q-qbar annihilation,
 (ii) interference between different contributions to qg → t+tbar+q, (and its CP conj.)

~~~ no more progress about 10 years

2] J.H. Kuhn, G. Rodrigo, PRL81(1998)49; detailed QCD calculation



Fig. 4. QCD asymmetries of Q=b and t production in  $p\bar{p} \rightarrow Q\bar{Q}g(q)$  at (a)  $\sqrt{s} = 630$  GeV; (b)  $\sqrt{s} = 1800$  GeV with  $|y(Q,\bar{Q} \text{ and } g(q))| < 2.5$ ,  $p_T(\bar{Q} \text{ or } g(q)) > 10$  GeV and  $[(\Delta \eta)^2 + (\Delta \phi)^2] > 0.5$  for any jet pair using the DO1 structure function [10].

[3] O. Antunano, J.H. Kuhn, G. Rodrigo, PRD77(2008)014003;
 → FBA of t-quak within the SM = 0.050 +- 0.015

5. D0 and CDF measured FBA ~ 20%
 → Now so many works beyond the SM

3.

### **SM prediction** Kuhn& Rodrigo PRD59(99); Antunano etal PRD77(08);

Leading order (d): charge asymmetry vanishes

Next-to-leading order: nonzero A<sub>C</sub> will be induced by the interference between (a) and (b) and the interference/between (c) and (d)  $N_t(y) - N_{\bar{t}}(y) = 0.051(6)$  $N_t(y) + N_{\overline{t}}(y)$ Since the measurements of D $\varnothing$  and DF have  $2\sigma$  deviation from the SM, the observed large FBA strongly indicate the new Physics

 $= 0.193 \pm 0.065 \pm 0.024$ 



### **3. Models by s-channel** Ferrario & Rodrigo PRD80(09); Frampton etal, arXiv:0911.2955







 $\alpha_X$ 



### **Model-independent approach** D.W. Jung, P. Ko, J.S. Lee, S.H. Nam, arXiv:0912.1105



| New particles                             | couplings                  | $C_1$  | $C_2$  | 1 $\sigma$ favor |
|-------------------------------------------|----------------------------|--------|--------|------------------|
| $V_8$ (spin-1 FC octet)                   | $g^{L,R}_{8q,8t}$          | indef. | indef. | $\checkmark$     |
| $\tilde{V}_1$ (spin-1 FV singlet)         | $\tilde{g}_{1q}^{L,R}$     | _      | 0      | ×                |
| $\tilde{V}_8$ (spin-1 FV octet)           | $\widetilde{g}^{L,R}_{8q}$ | +      | 0      | $\checkmark$     |
| $\tilde{S}_1$ (spin-0 FV singlet)         | $	ilde{\eta}^{L,R}_{1q}$   | 0      | _      | $\checkmark$     |
| $\tilde{S}_8$ (spin-0 FV octet)           | $\tilde{\eta}^{L,R}_{8q}$  | 0      | +      | ×                |
| $S_2^{\alpha}$ (spin-0 FV triplet)        | $\eta_3$                   | _      | 0      | ×                |
| $S_{13}^{\alpha\beta}$ (spin-0 FV sextet) | $\frac{\eta_6}{\eta_6}$    | +      | 0      | $\checkmark$     |

$$\mathcal{L} = g_s \left[ \frac{\eta_3}{2} \epsilon_{\alpha\beta\gamma} \epsilon^{ijk} u^{\alpha}_{iR} u^{\beta}_{jR} S^{\gamma}_k + \eta_6 u^{\alpha}_{iR} u^{\beta}_{jR} S^{\alpha\beta}_{ij} + h.c. \right]$$

$$\mathcal{L}_{\text{int}} = g_s V_8^{a\mu} \sum_A \left[ g_{8q}^A (\bar{q}_A \gamma_\mu T^a q_A) + g_{8t}^A (\bar{t}_A \gamma_\mu T^a t_A) \right]$$

$$+g_{s}\left[\tilde{V}_{1}^{\mu}\sum_{A}\tilde{g}_{1q}^{A}(\bar{t}_{A}\gamma_{\mu}q_{A})+\tilde{V}_{8}^{a\mu}\sum_{A}\tilde{g}_{8q}^{A}(\bar{t}_{A}\gamma_{\mu}T^{a}q_{A})+\text{h.c.}\right]$$
$$+g_{s}\left[\tilde{S}_{1}\sum_{A}\tilde{\eta}_{1q}^{A}(\bar{t}Aq)+\tilde{S}_{8}^{a}\sum_{A}\tilde{\eta}_{8q}^{A}(\bar{t}AT^{a}q)+\text{h.c.}\right], \qquad (6)$$



## **Diquark models**

Shu, Tait, Wang :0911.3237, Arhrib, Benbrik, Chen:0911.4875, Dorsner etal :0912.0972

Diquark is the particle that couples to quarks by q<sup>aT</sup> C q<sup>b</sup> H<sub>ab</sub>, where a, b are the color indices The possible representations under  $SU(3)_{C} \times SU(2)_{L} \times U(1)_{Y}$ :  $(6,3)_{1/3}, (6,1)_{4/3,1/3,-2/3},$  $(3, 3)_{-1/3}, (3, 1)_{2/3, -1/3, -4/3}$ 

We would like to pay attention to (3,1,-4/3) and (6,1,4/3)

#### The relevant interaction

$$\mathcal{L} = 2f_{ut}^{\mathbf{3}}\bar{u}_{\alpha}P_{L}t_{\beta}^{c}\epsilon^{\alpha\beta\gamma}H_{\mathbf{3}\gamma}^{\dagger} + 2f_{ut}^{\mathbf{6}}\bar{u}_{\alpha}P_{L}t_{\beta}^{c}H_{\mathbf{6}}^{\alpha\beta} + h.c.$$

$$f_{ij}^{3} = -f_{ji}^{3}, f_{ij}^{6} = f_{ji}^{6}$$

The correspondingFeynman diagram



# **4. Unparticle Physics, s-channel C.H. Chen, Gorazd Cvetic, C.S Kim, PLB694(2011)393** A stuff dictated by scale invariance, proposed by Georgi Phys.Rev.Lett.98:221601,2007 Phys.Lett.B650:275-278,2007

interactions to quarks are proposed to be

$$(\lambda_V^q \gamma_\mu + \lambda_A^q \gamma_\mu \gamma_5) T^a q O_U^{a\mu}$$

$$g_{\mathcal{J}}^{d-1} = g_{\chi}^{q}, \chi = VorA$$

Cacciapaglia, Marandella, Terning, JHEP0801:070,2008

Due to nonintegral scale dimension and no mass scale in the

propagator, it will be interesting to see the unparticle effects on the top-quark FBA

The propagator of colored vector unparticle is given by

$$-iC_V \frac{1}{(-p^2 - i\epsilon)^{3-d}} \left[ p^2 g_{\mu\nu} - \frac{2(d-2)}{d-1} p_\mu p_\nu \right]$$

$$C_V = \frac{A_{d_U}}{2\sin d_U \pi},$$
  

$$A_{d_U} = \frac{16\pi^{5/2}}{(2\pi)^{2d_U}} \frac{\Gamma(d_U + 1/2)}{\Gamma(d_U - 1)\Gamma(2d_U)}$$

Then, the scattering amplitude for  $q\bar{q} \rightarrow t\bar{t}$  by unparticle exchange in the s-channel is

$$A_{\mathcal{U}} = \bar{q} \left( g_V^q \gamma_\mu + g_A^q \gamma_\mu \gamma_5 \right) T^a q \frac{C_V}{(-p^2 - i\epsilon)^{3-d_{\mathcal{U}}}} \left[ p^2 g_{\mu\nu} - \frac{2(d_{\mathcal{U}} - 2)}{d_{\mathcal{U}} - 1} p_\mu p_\nu \right] \\ \times \bar{t} \left( g_V^t \gamma_\nu + g_A^t \gamma_\nu \gamma_5 \right) T^a t$$

Scattering amplitude combined with the SM becomes

with

$$\begin{split} &= A_{\rm SM} + A_{\mathcal{U}} \\ &= \frac{g_s^2}{\hat{s}} \bar{q} \gamma_\mu T^a q \bar{t} \gamma^\mu T^a t \\ &+ \frac{\hat{s} C_V}{\hat{s}^{3-d_{\mathcal{U}}}} e^{-i\pi(3-d_{\mathcal{U}})} \bar{q} \left( g_V^q \gamma_\mu + g_A^q \gamma_\mu \gamma_5 \right) T^a q \bar{t} \left( g_V^t \gamma^\mu + g_A^t \gamma^\mu \gamma_5 \right) T^a t \end{split}$$

explicitly showing the differential cross section in  $t\bar{t}$  invariant mass frame, relevant coordinates of particle momenta as

$$\begin{split} p_{u,\bar{u}} &= \frac{\sqrt{\hat{s}}}{2}(1,0,0,\pm 1) ,\\ p_{t,\bar{t}} &= \frac{\sqrt{\hat{s}}}{2}(1,\pm\beta_t\sin\hat{\theta},0,\pm\beta_t\cos\hat{\theta}) , \end{split}$$

with 
$$\beta_t^2 = 1 - 4m_t^2/\hat{s}$$
.

Spin and color averaged amplitude-square is

$$\begin{split} |\bar{A}|^{2} &= \frac{1}{2^{2}} \frac{1}{N_{C}^{2}} |A|^{2}, \\ &= \frac{N_{C}^{2} - 1}{16N_{C}^{2}} \left\{ 4(4\pi\alpha_{s})^{2} \left( 1 + \beta_{t}^{2}\cos^{2}\hat{\theta} + 4\frac{m_{t}^{2}}{\hat{s}} \right) \right. \\ &+ 8(C_{V}4\pi\alpha_{s})\cos\pi(3 - d_{\mathcal{U}}) \frac{\hat{s}^{2}}{\hat{s}^{3-d_{\mathcal{U}}}} \left[ g_{V}^{q}g_{V}^{t} \left( 1 + \beta_{t}^{2}\cos^{2}\hat{\theta} + 4\frac{m_{t}^{2}}{\hat{s}} \right) + 2g_{A}^{q}g_{A}^{t}\beta_{t}\cos\hat{\theta} \right] \\ &+ 4\hat{s}^{2} \left( \frac{\hat{s}C_{V}}{\hat{s}^{3-d_{\mathcal{U}}}} \right)^{2} \left[ (g_{V}^{t})^{2} \left( (g_{V}^{q})^{2} + (g_{A}^{q})^{2} \right) \left( 1 + \beta_{t}^{2}\cos^{2}\hat{\theta} + \frac{4m_{t}^{2}}{\hat{s}} \right) \\ &+ \left. (g_{A}^{t})^{2} \left( (g_{V}^{q})^{2} + (g_{A}^{q})^{2} \right) \left( 1 + \beta_{t}^{2}\cos^{2}\hat{\theta} - \frac{4m_{t}^{2}}{\hat{s}} \right) + 8g_{V}^{q}g_{V}^{t}g_{A}^{q}g_{A}^{t}\beta_{t}\cos\hat{\theta} \right] \right\}. \end{split}$$

$$\begin{aligned} \frac{d\hat{\sigma}^{q\bar{q} \to t\bar{t}}}{d\cos\hat{\theta}} &= \frac{N_C^2 - 1}{128N_C^2 \pi \hat{s}} \beta_t \left\{ (4\pi\alpha_s)^2 \left( 1 + \beta_t^2 \cos^2\hat{\theta} + 4\frac{m_t^2}{\hat{s}} \right) \right. \\ &+ 2C_V (4\pi\alpha_s) \cos\pi (3 - d_{\mathcal{U}}) \frac{\hat{s}^2}{\hat{s}^{3-d_{\mathcal{U}}}} \left[ g_V^q g_V^t \left( 1 + \beta_t^2 \cos^2\hat{\theta} + 4\frac{m_t^2}{\hat{s}} \right) + 2g_A^q g_A^t \beta_t \right] \\ &+ \left( \frac{\hat{s}^2 C_V}{\hat{s}^{3-d_{\mathcal{U}}}} \right)^2 \left[ (g_V^t)^2 \left( (g_V^q)^2 + (g_A^q)^2 \right) \left( 1 + \beta_t^2 \cos^2\hat{\theta} + \frac{4m_t^2}{\hat{s}} \right) \right. \\ &+ \left. (g_A^t)^2 \left( (g_V^q)^2 + (g_A^q)^2 \right) \left( 1 + \beta_t^2 \cos^2\hat{\theta} - \frac{4m_t^2}{\hat{s}} \right) + 8g_V^q g_V^t g_A^q g_A^t \beta_t \right] \right\}. \end{aligned}$$

3 physical observables are: 
$$\sigma(p\bar{p} \to t\bar{t}) = \int_{-1}^{1} d\cos\theta \, \frac{d\sigma(p\bar{p} \to t\bar{t})}{d\cos\theta}$$

$$A_{FB}^{p\bar{p}} = \left(\int_{0}^{1} d\cos\theta \, \frac{d\sigma(p\bar{p} \to t\bar{t})}{d\cos\theta} - \int_{0}^{-1} d\cos\theta \, \frac{d\sigma(p\bar{p} \to t\bar{t})}{d\cos\theta}\right) / \sigma(p\bar{p} \to t\bar{t})$$

$$\frac{d\sigma(p\bar{p} \to t\bar{t})}{dM_{t\bar{t}}} = 2 \, \frac{M_{t\bar{t}}}{s} \int_{M_{t\bar{t}}^{2}/s}^{1} \frac{dx_{1}}{x_{1}} \sum_{i,j} f_{i}(x_{1})f_{j}(x_{2}) \int_{-1}^{1} d\cos\theta \, \frac{\partial\sigma^{q,q_{j} \to t\bar{t}}(\theta, x_{1}, x_{2})}{\partial\cos\theta}\Big|_{x_{2}=M_{t\bar{t}}^{2}/(sx_{1})}$$
1 den the tractmeters:  $(\Lambda_{\mathcal{U}}, \lambda \text{ and } d_{\mathcal{U}})$ 
1 first we set  $\Lambda_{\mathcal{U}} = 1 \text{ TeV}$ 
2 remaining dimensionless parameters are  $\lambda$  from  $g = \lambda/\Lambda_{\mathcal{U}}^{d_{i-1}}$  assuming flavor blind (colored) unparticle and finally the scale dimension  $d_{\mathcal{U}}$ 
 $g_{V}^{t} = g_{A}^{t} = g_{V}^{q} = g_{A}^{q} = g$ 
i.e. the flavor blind and chirality-independent couplings
$$\sigma(p\bar{p} \to t\bar{t})^{exp} = 7.50 \pm 0.31 \, (\text{stat}) \pm 0.34 \, (\text{syst}) \pm 0.15 \, (\text{th}) \text{ pb}$$
 $= 7.50 \pm 0.48 \, \text{pb}$ .
the SM prediction is  $\sigma(p\bar{p} \to t\bar{t})^{\text{SM}} = 6.73_{-0.79}^{-0.71} \text{ pb}$ 
 $M_{cacciati \ et \ d., \text{HEP 0809, 127 (2008); N. Kidonakis and R. Vogr. Phys. Rev. D 78, 074005 (2008); S. Moch and P. Uver, Phys. Rev. D 78, 074005 (2008); S. Moch and P. Uver, Phys. Rev. D 78, 074005 (2008); S. Moch and P. Uver, Phys. Rev. D 78, 074005 (2008); S. Moch and P. Uver, Phys. Rev. D 78, 074005 (2008); S. Moch and P. Uver, Phys. Rev. D 78, 074005 (2008); S. Moch and P. Uver, Phys. Rev. D 78, 074005 (2008); S. Moch and P. Uver, Phys. Rev. D 78, 074005 (2008); S. Moch and P. Uver, Phys. Rev. D 78, 074005 (2008); S. Moch and P. Uver, Phys. Rev. D 78, 074005 (2008); S. Moch and P. Uver, Phys. Rev. D 78, 074005 (2008); S. Moch and P. Uver, Phys. Rev. D 78, 074005 (2008); S. Moch and P. Uver, Phys. Rev. D 78, 074005 (2008); S. Moch and P. Uver, Phys. Rev. D 78, 074005 (2008); S. Moch and P. Uver, Phys. Rev. D 78, 074005 (2008); S. Moch and P. Uver, Phys. Rev. D 78, 074005 (2008); S. Moch and P. Uver, Phys. Rev. D 78, 074005 (2008); S. Moch and P. Uver, Phys. Rev. D 78, 074005 (2008); S. Moch and P. Uver, Phys$ 



FIG. 1:  $t\bar{t}$  production cross section (the lower) and top-quark FBA (the upper figure) as a function of the scale dimension  $d_{\mathcal{U}}$ , where the solid, dashed, dotted and dash-dotted lines represents  $\lambda=1.4$ , 1.6, 1.8, 2.0, respectively. The band in the plot represents the measured values with  $1\sigma$ uncertainties.



#### → d\_U=1.28+-0.22, lambda=2.05+-0.45



FIG. 2: As Fig. 1, but as a function of the parameter  $\lambda$ . The solid, dashed, dotted and dash-dotted lines represents  $d_{\mathcal{U}}=1.1, 1.15, 1.2, 1.25$ , respectively.



FIG. 4:  $d\sigma/dM_{t\bar{t}}$  as a function of invariant mass of top-pair  $M_{t\bar{t}}$ , where the solid, dash-dotted and dashed lines represent the SM result and colored unparticle with  $(\lambda, d_{\mathcal{U}}) = (2.05, 1.28)$  and (1.70, 1.175), respectively. The vertical bars are the data from CDF measurement with an integrated luminosity of 2.5 fb<sup>-1</sup>, Ref. [32]. (CDF).



- (i) The chosen scales of renormalization  $(\mu_R)$  and factorization  $(\mu_F)$  for which the usual possible values could be taken between  $m_t/2$  and  $2m_t$ . Here we adopted  $\mu_R = \mu_F = m_t$ .
- (ii) The  $M_{t\bar{t}}$ -dependent NLO effects which include the NLO parton distribution function (PDF). Here for simplicity we just use a  $M_{t\bar{t}}$ -independent scale factor value of K=1.36 (*i.e.*, the factor  $\sqrt{K} = \sqrt{1.36}$  for the tree-level SM amplitude  $A_{\rm SM}$ ) to fit the  $t\bar{t}$ production cross section with LO calculations.

#### For detailed analysis, cosider Mtt-restricted FBA,

restricted by  $M_{t\bar{t}} < M_{t\bar{t}}^{edge}$  (the quantity  $A_{FB}^{t,low}$ ) or by  $M_{t\bar{t}} > M_{t\bar{t}}^{edge}$  (the quantity  $A_{FB}^{t,high}$ )  $A_{FB}^{t,X} = A_{FB}^{X}(exp) - A_{FB}^{X}(SM)$  (X = low, high)  $A_{FB}^{t,0} = A_{FB}^{X}(exp) - A_{FB}^{X}(SM)$  (X = low, high)  $A_{FB}^{t,0} = A_{FB}^{t,0}(exp) - A_{FB}^$ 

 $M_{t\bar{t}}$  edge [GeV]

FIG. 5: Restricted forward-backward asymetries  $A_{\rm FB}^{t,\rm low}$  and  $A_{\rm FB}^{t,\rm high}$  as functions of the threshold ("edge")  $M_{t\bar{t}}$  values, for  $(\lambda, d_{\mathcal{U}}) = (2.05, 1.28)$  (circles) and (1.70, 1.175) (squares). Included are also the corresponding CDF measured values [37] (their 8th and 9th figure) subtracted by the SM values [38], as bars with triangles.

 $M_{t\bar{t}}$  edge [GeV]

This issue remains inconclusive because of: (i) the aforementioned very large experimental uncertainties of  $A_{\rm FB}^{\rm high}$  at high  $M_{t\bar{t}}^{\rm edge}$ ; (ii) the severely restricted phase space at high  $M_{t\bar{t}}^{\rm edge}$ . Namely, our simplified approach of rescaling the tree-level SM (QCD) amplitude by a fixed factor ( $\sqrt{K} = \sqrt{1.36}$ ) for all  $M_{t\bar{t}}$  values becomes increasingly unreliable when  $M_{t\bar{t}}^{\rm edge}$  increases in  $A_{\rm FB}^{t,\rm high}$ , because the phase space becomes so severely restricted.

## 5. Summary

An unexpected large FBA of top-quark is observed by  $D\emptyset$  and CDF: strongly indicate the new physics effects (NLO effects). Various possible solutions to the "anomaly" are proposed, like axigluon, KK excitations of gluon, Z', W', colored scalars, etc We investigated whether colored flavor-conserving unparticle can explain the measured FBA of ttbar production at Tevatron. With a natural assumption of quark flavor-blind and chiralityindependent unparticle, UP contribution can explain the deviation.

