

# The Half-lives of $^{90\text{m}}\text{Y}$ and $^{97}\text{Ru}$

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| Nuclide | ADNDT 2003 | ENSDF 10/5/09 | % uncert | Remarks                        |
|---------|------------|---------------|----------|--------------------------------|
| 71Zn    | 2.45 min   | 2.45 10 min   | 4.1%     | uncertainty too high           |
| 97Ru    | 2.9 d      | 2.9 1 d       | 3.4%     | uncertainty too high           |
| 175Hf   | 70 d       | 70 2 d        | 2.9%     | uncertainty too high           |
| 90mY    | 3.19 h     | 3.19 6 h      | 1.9%     | uncertainty too high           |
| 111mPd  | 5.5 h      | 5.5 1 h       | 1.8%     | uncertainty too high           |
| 205Hg   | 5.2 min    | 5.14 9 min    | 1.8%     | diff, signif, uncert. too high |
| 161Gd   | 3.66 min   | 3.66 5 min    | 1.4%     | uncertainty too high           |
| 77mGe   | 52.9 s     | 52.9 6 s      | 1.1%     | uncertainty too high           |
| 75mGe   | 47.7 s     | 47.7 5 s      | 1.0%     | uncertainty too high           |
| 97Nb    | 72.1 min   | 72.1 7 min    | 1.0%     | uncertainty too high           |
| 104Rh   | 42.3 s     | 42.3 4 s      | 0.9%     | uncertainty too high           |
| 110Ag   | 24.6 s     | 24.6 2 s      | 0.8%     | uncertainty too high           |
| 131mTe  | 30 h       | 33.25 25 h    | 0.8%     | different, significant         |
| 180mHf  | 5.5 h      | 5.47 4 h      | 0.7%     | uncertainty too high           |
| 20F     | 11.16 s    | 11.07 6 s     | 0.5%     | different, significant         |
| 176mLu  | 3.635 h    | 3.664 19 h    | 0.5%     | different, significant         |
| 159Gd   | 18.56 h    | 18.479 h      | 0.4%     | different, significant         |
| 87mSr   | 2.803 h    | 2.815 12 h    | 0.4%     | different, significant         |
| 117mSn  | 13.60 d    | 13.76 4 d     | 0.3%     | different, significant         |
| 233Th   | 22.3 min   | 21.83 4 min   | 0.2%     | different, significant         |
| 42K     | 12.36 h    | 12.360 12 h   | 0.1%     | different, not significant     |
| 24Na    | 14.96 h    | 14.997 12 h   | 0.1%     | different, not significant     |
| 134mCs  | 2.903 h    | 2.912 2 h     | 0.1%     | different, not significant     |
| 134Cs   | 2.065 y    | 2.0652 4 y    | 0.02%    | different, not significant     |
| 109Pd   | 13.46 h    | 13.7012 24 h  | 0.02%    | different, significant         |
| 187W    | 23.72 h    | 24.000 4 h    | 0.02%    | different, significant         |

## Nuclide issues

3-h  $^{90\text{m}}\text{Y}$  activity is only 1/60 of 3-d  $^{90}\text{Y}$

But  $^{90}\text{Y}$  is a pure  $\beta$  emitter; use low-Z absorber

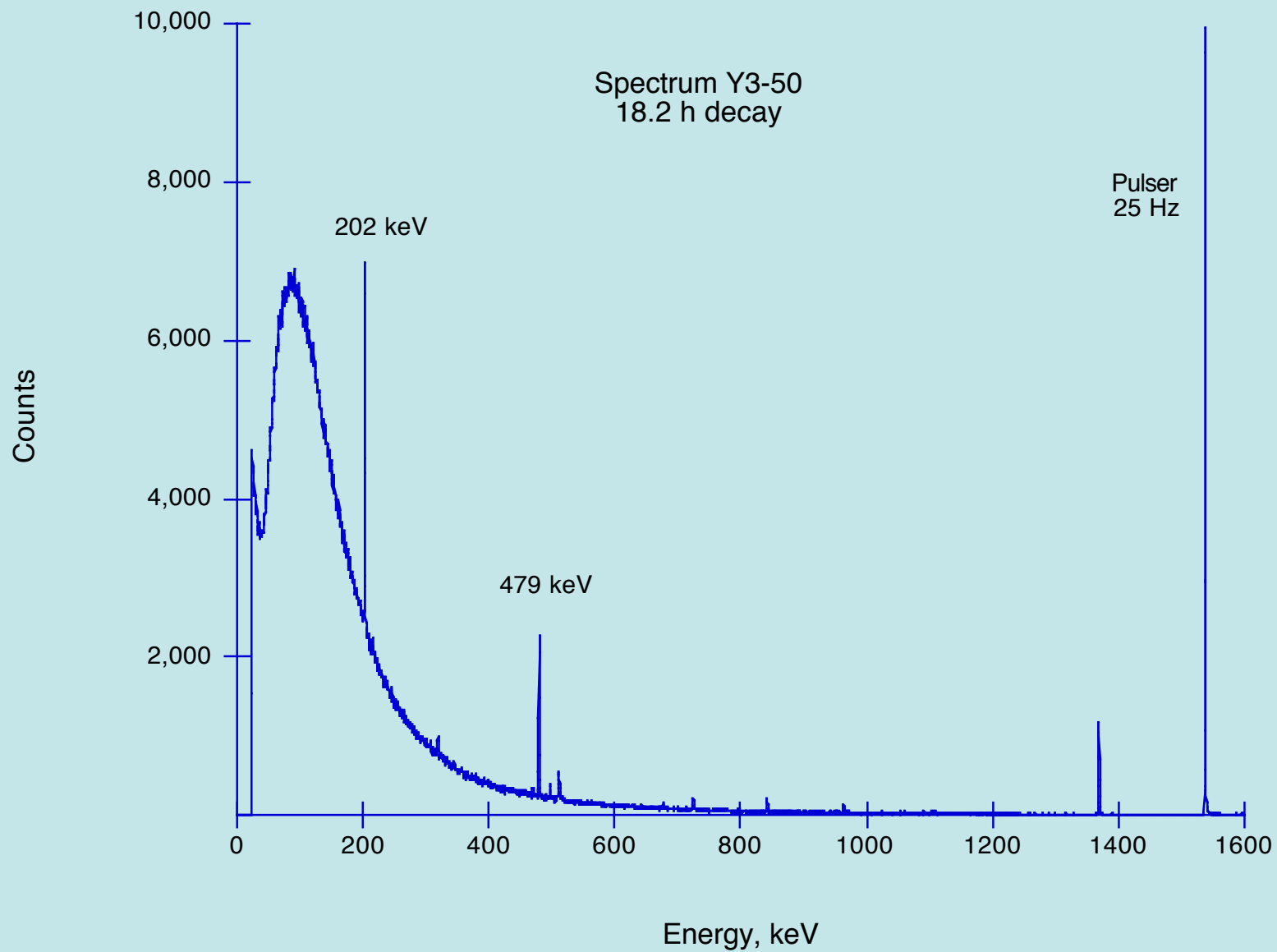
Two clean gammas at 202 and 479 keV

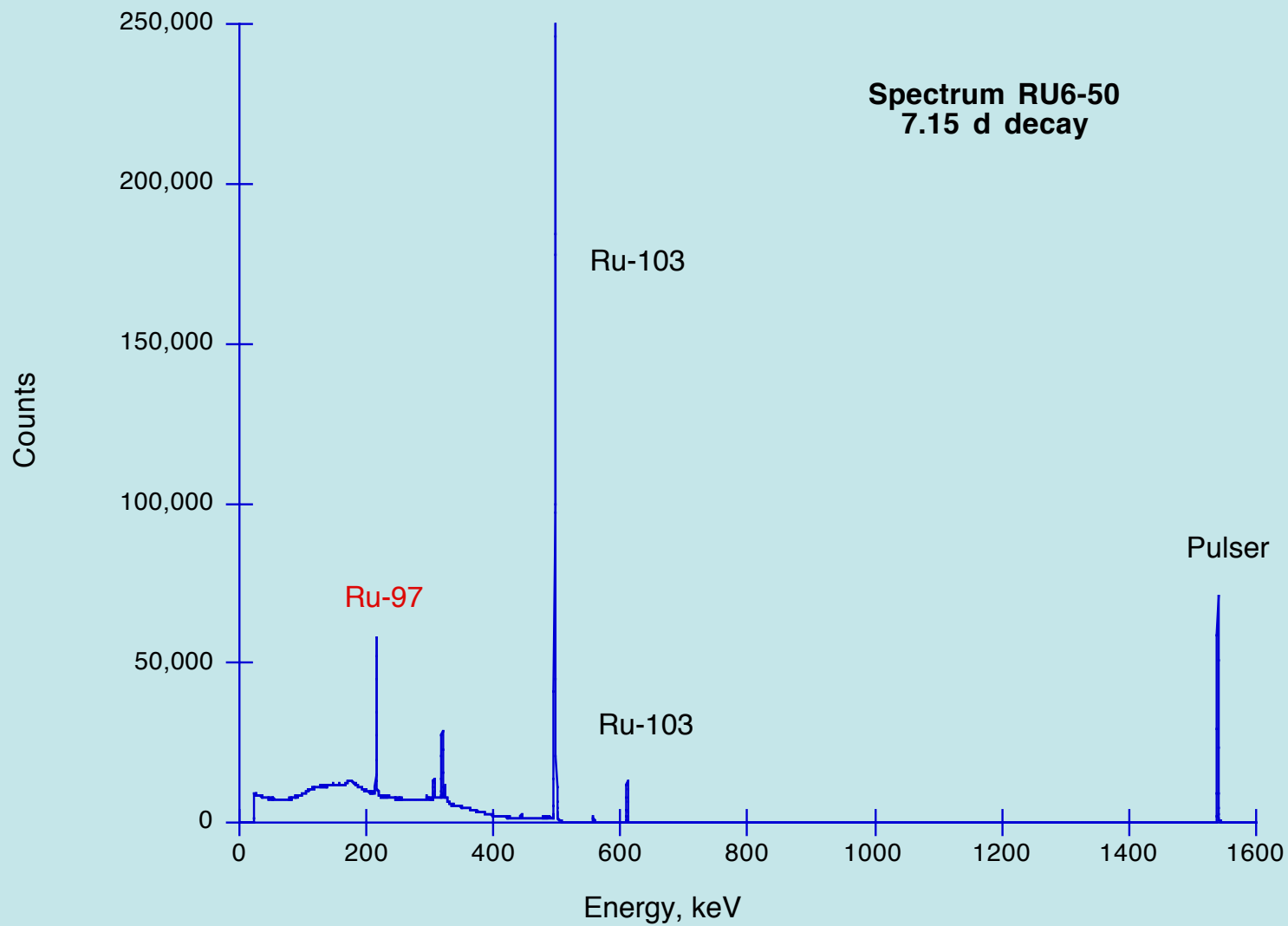
3-d  $^{97}\text{Ru}$  dominated by 4-h  $^{105}\text{Ru}$  and 39-d  $^{103}\text{Ru}$

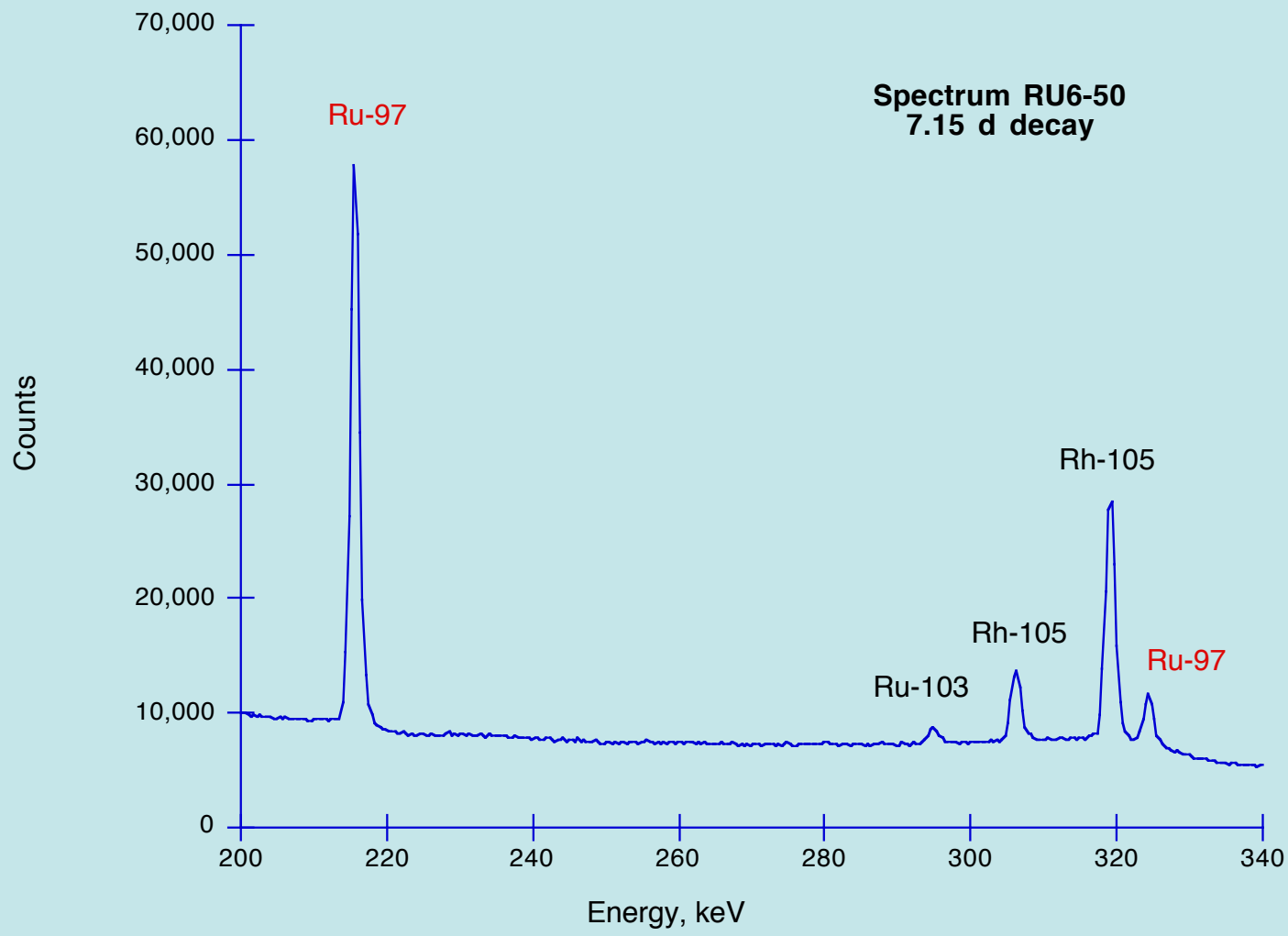
One useful gamma at 216 keV

324 keV interfered by  $^{105}\text{Ru}$  and trace  $^{105}\text{Rh}$

Long life requires weeks of measurement







# Measurements

Select pure  $Y_2O_3$  or Ru metal

Irradiate with thermal neutrons

Repackage in clean container

Fix in position near Ge detector

Count repeatedly for 4-10 half-lives

Use precision pulser to monitor losses

$$\Delta\nu/\nu < 2 \cdot 10^{-8}/d$$

Repeat

# Experimental conditions

| <b>Experiment</b> | <b>Geometry,<br/>cm</b> | <b>Initial dead<br/>time</b> | <b>Counting<br/>interval</b> | <b>Number of<br/>spectra</b> |
|-------------------|-------------------------|------------------------------|------------------------------|------------------------------|
| Y1                | 20                      | 15.4%                        | 20 m                         | 50                           |
| Y2                | 30                      | 8.7%                         | 20 m                         | 100                          |
| Y3                | 20                      | 16.1%                        | 20 m                         | 100                          |
| Ru1               | 30                      | 6.5%                         | 3 h                          | 42                           |
| Ru2               | 40                      | 6.3%                         | 3 h                          | 101                          |
| Ru3               | 25                      | 2.5%                         | 3 h                          | 33                           |
| Ru6               | 40                      | 10.9%                        | 3 h                          | 112                          |



# Data reduction

Determine net peak areas with fixed ROI

Correct each datum for decay and pileup

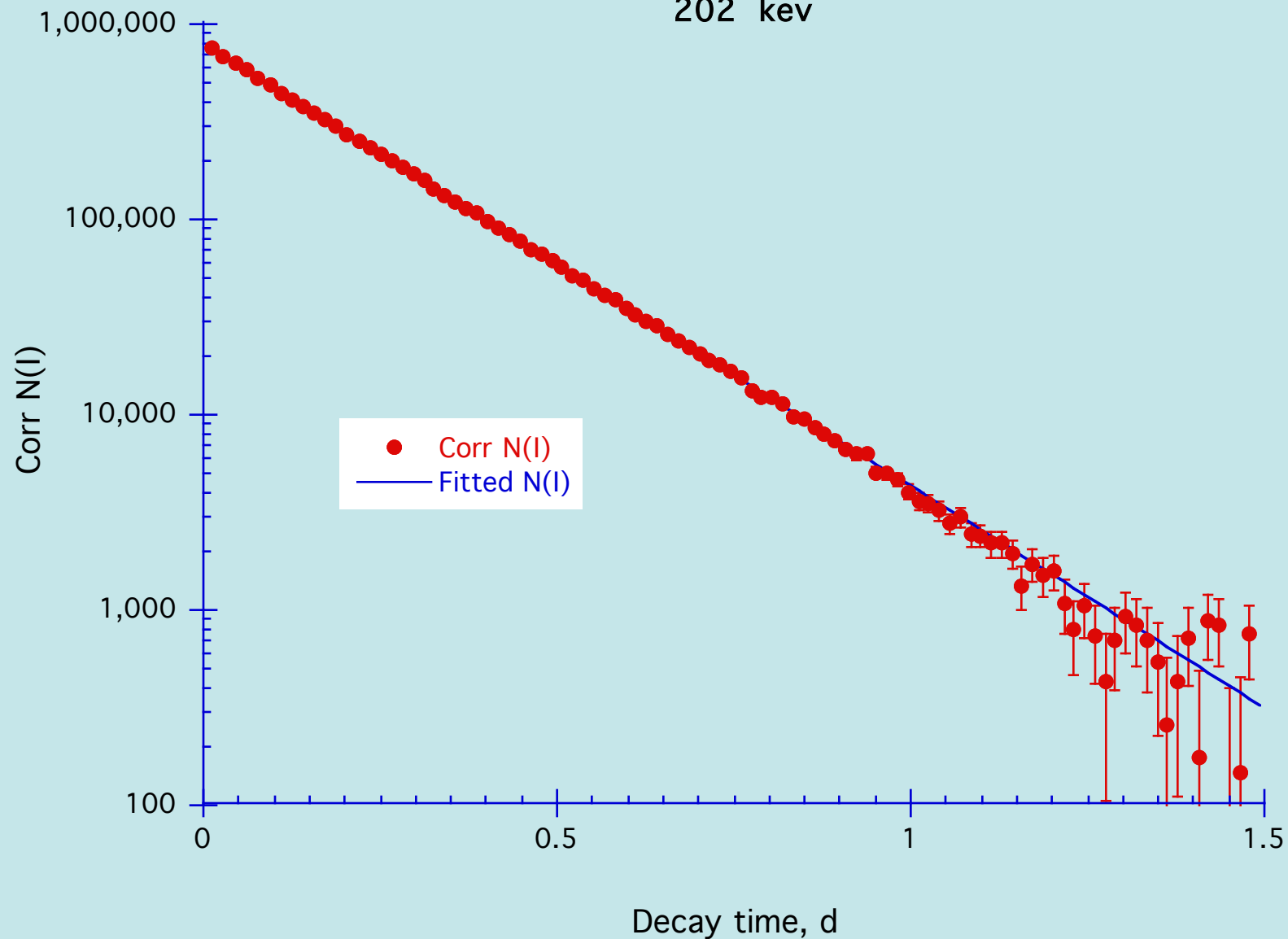
Fit to exponential by  $\chi^2$  minimization

Use Solver to determine  $T_{1/2}$  and  $A_0$

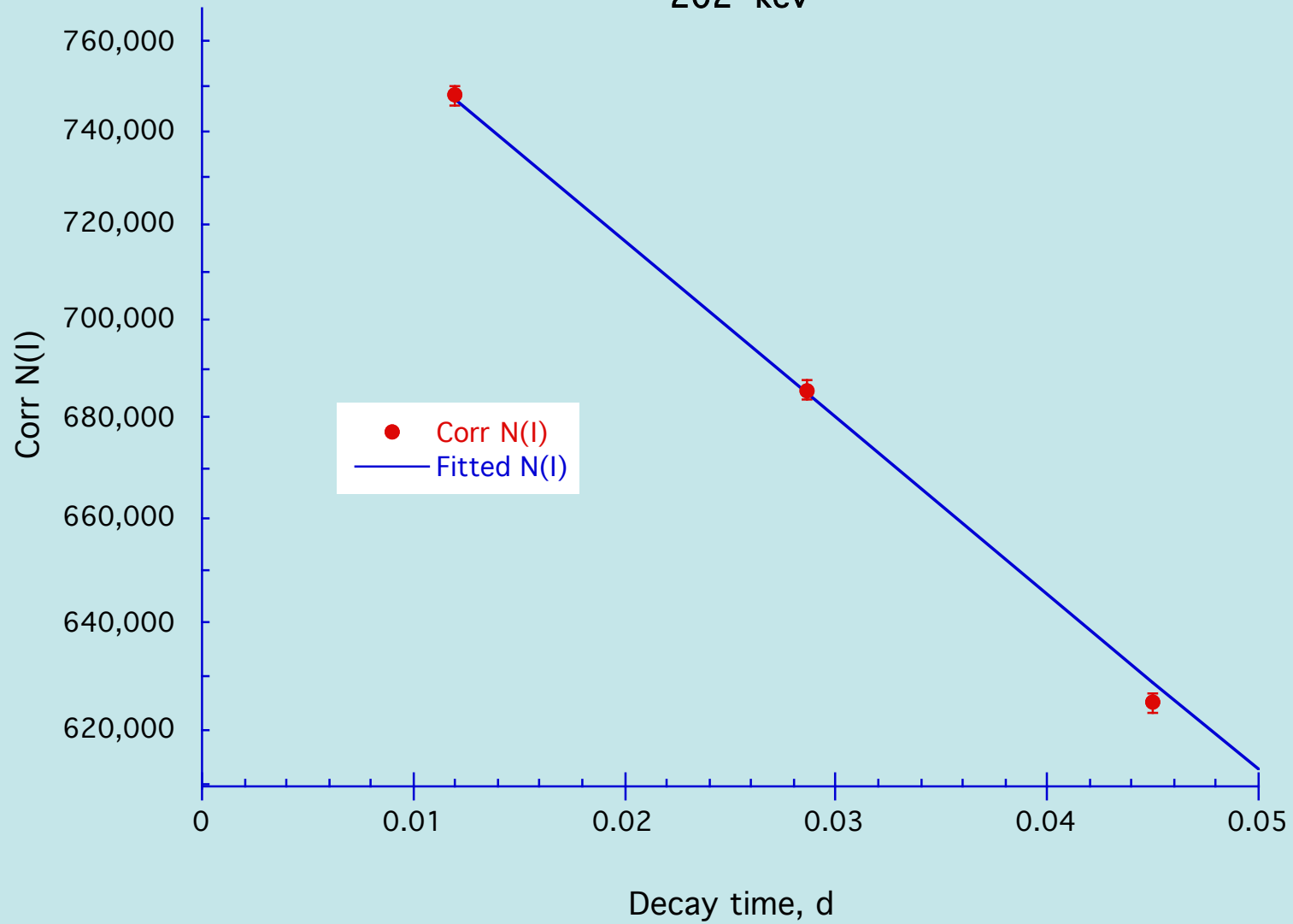
Repeat

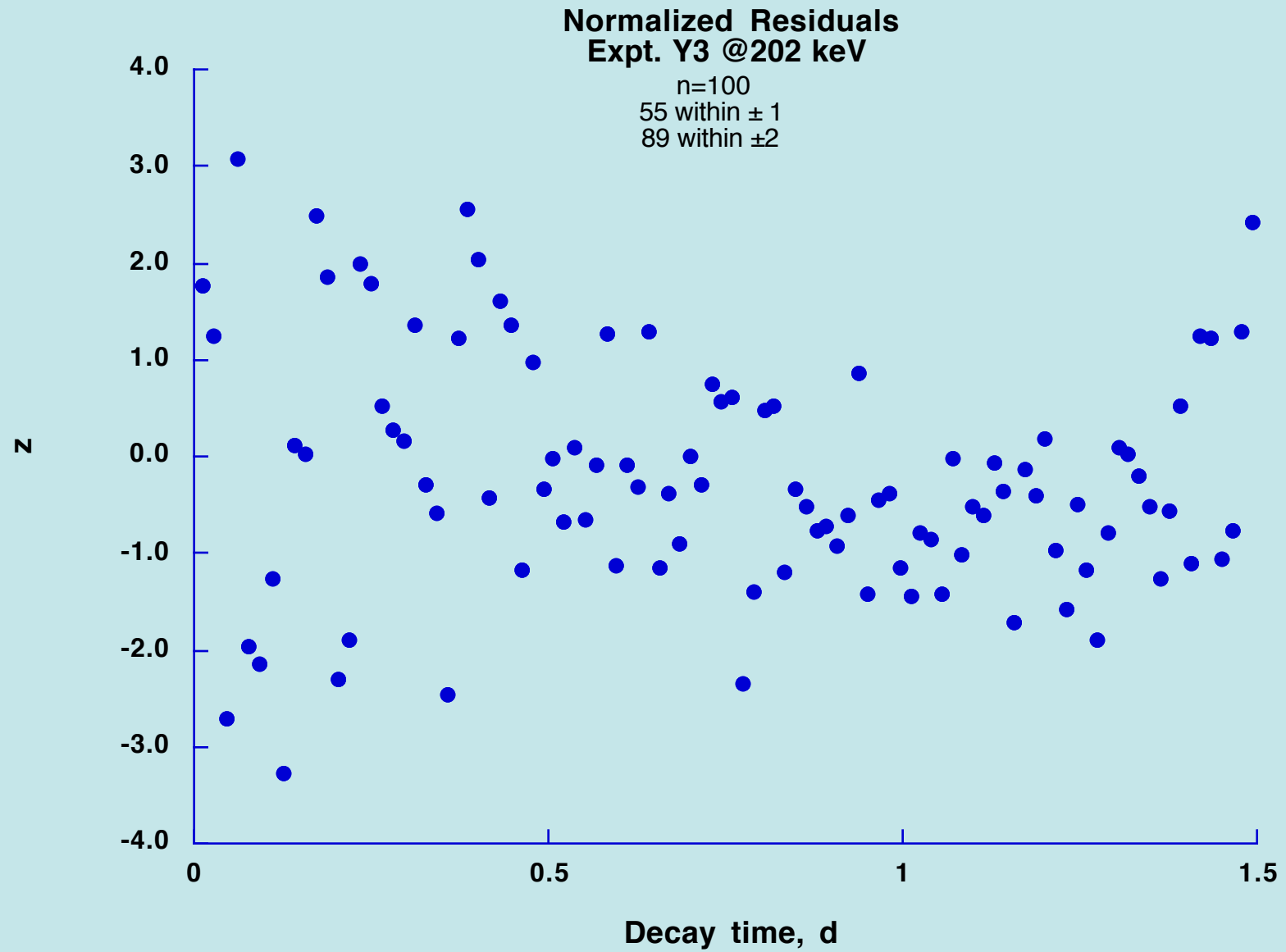
Evaluate best values and uncertainties

Experiment Y3  
202 keV



Experiment Y3  
202 kev





## 90mY Results

| <b>Expt, E<sub>γ</sub></b> | <b>Half-lives</b> | <b>Net counts</b> | <b>T<sub>1/2</sub>, hr</b> | <b>±</b> | <b>χ<sup>2</sup>/df</b> |
|----------------------------|-------------------|-------------------|----------------------------|----------|-------------------------|
| Y1 202                     | 5.7               | 7,275,017         | 3.211                      | 0.003    | 1.58                    |
| Y2 202                     | 10.8              | 5,015,603         | 3.206                      | 0.003    | 1.41                    |
| Y3 202                     | 11.2              | 8,568,738         | 3.194                      | 0.002    | 1.61                    |
| Y1 479                     | 5.7               | 3,647,243         | 3.202                      | 0.003    | 1.69                    |
| Y2 479                     | 10.8              | 2,653,289         | 3.215                      | 0.003    | 1.07                    |
| Y3 479                     | 11.2              | 4,616,720         | 3.203                      | 0.002    | 1.59                    |

## <sup>97</sup>Ru Results

| <b>Expt, E<sub>γ</sub></b> | <b>Half-lives</b> | <b>Net counts</b> | <b>T<sub>1/2</sub>, da</b> | <b>±</b> | <b>χ<sup>2</sup>/df</b> |
|----------------------------|-------------------|-------------------|----------------------------|----------|-------------------------|
| Ru1 216                    | 3.8               | 14,254,210        | 2.837                      | 0.002    | 1.46                    |
| Ru2 216                    | 4.9               | 16,715,849        | 2.847                      | 0.002    | 1.21                    |
| Ru3 216                    | 1.5               | 8,290,780         | 2.836                      | 0.005    | 1.08                    |
| Ru6 216                    | 6.1               | 29,738,916        | 2.826                      | 0.001    | 1.10                    |

"We demand guaranteed rigidly defined areas of  
doubt and uncertainty." – Vroomfondel

D.N. Adams, *Hitchhiker's Guide to the Galaxy*, Pan, London (1979)

# Realistic uncertainty assignment

The goodness-of-fit to the decay curve is an underestimate of the true uncertainty as judged from the repeatability of measurements.

Others have found ca. 3-6x underestimate and proposed recipes to assess real uncertainty.

J. A. Becker et al, Nucl. Instrum. Methods **155**, 211 (1978).

K. F. Walz, K. Debertin, H. Schrader, Int. J. Appl. Radiat. Isot. **34**, 1191 (1983).

S. Pommé, J. Camps, R. Van Ammel, J. Paepen, J. Radioanal. Nucl. Chem. **276**, 335 (2008).

K. Nakamura (Particle Data Group), J. Phys. G: Nucl. Part. Phys. **37**, 075021 (2010).



# How good are the Y numbers?

| Experiment, energy                     | $T_{1/2}$ , d | Uncertainty, 1s | Normalized residual      | Relative weight |
|--|---------------|-----------------|--------------------------|-----------------|
| Y1 202                                 | 3.2107        | 0.0027          | 2.59                     | 0.138           |
| Y2 202                                 | 3.2061        | 0.0029          | 0.81                     | 0.117           |
| Y3 202                                 | 3.1942        | 0.0021          | -4.48                    | 0.227           |
| Y1 479                                 | 3.2017        | 0.0027          | -0.75                    | 0.141           |
| Y2 479                                 | 3.2153        | 0.0029          | 4.06                     | 0.125           |
| Y3 479                                 | 3.2026        | 0.0020          | -0.52                    | 0.252           |
| Weighted mean                          |               | <b>3.2037</b>   | hours                    |                 |
| Unweighted mean                        |               | 3.2051          |                          |                 |
| s about weighted mean                  |               | 0.0075          | (0.24% of weighted mean) |                 |
| Observed s.d. of mean ( $s/\sqrt{n}$ ) |               | 0.0030          | (0.09%)                  |                 |
| A priori s.d. of mean                  |               | 0.0010          | (0.03%)                  |                 |
| $ts/\sqrt{n}$ [P=0.05; t=2.57)         |               | <b>0.0078</b>   | (0.424%)                 |                 |
| Chi squared/d.f.                       |               | 8.95            | for 5 degrees of freedom |                 |

Present work **3.204 h  $\pm$  0.004 (1s)**; ENSDF 3.19  $\pm$  0.06

# How good are the Ru numbers?

| Experiment, energy | $T_{1/2}$ , d | Uncertainty, 1s | Normalized residual | Relative weight |
|--------------------|---------------|-----------------|---------------------|-----------------|
| Ru1 216            | 2.8372        | 0.0020          | 0.67                | 0.204           |
| Ru2 216            | 2.8474        | 0.0016          | 7.29                | 0.332           |
| Ru3 216            | 2.8356        | 0.0048          | -0.05               | 0.036           |
| Ru6 216            | 2.8262        | 0.0014          | -6.87               | 0.428           |

|  |               |                          |
|--|---------------|--------------------------|
| Weighted mean                          | <b>2.8358</b> | days                     |
| Unweighted mean                        | 2.8366        |                          |
| s about weighted mean                  | 0.0087        | (0.31% of weighted mean) |
| Observed s.d. of mean ( $s/\sqrt{n}$ ) | 0.0043        | (0.15%)                  |
| A priori s.d. of mean                  | 0.0009        | (0.03%)                  |
| $ts/\sqrt{n}$ [P=0.05; t=3.18)         | <b>0.0138</b> | (0.49%)                  |
| Chi squared/d.f.                       | 33.6          | for 3 degrees of freedom |

Present work **2.836 d  $\pm$  0.007 (1s)**; ENSDF 2.9  $\pm$  0.1

## Conclusions

Uncertainties are about an order of magnitude better than ENSDF.

These data should lead to improved accuracy in INAA.



Grazie! Domande?  
Questions?

Thanks to Menno Blaauw and Ron Fleming for constructive suggestions in earlier phases of the half-life work.

NIST