

Triple high energy nuclear collisions - a new method to study QCD phase diagram at high baryonic densities

Oleksandr Vitiuk [September 24th, 2022](#)

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Colliding and Fixed Target Mode in a Single Experiment—A Novel Approach to Study the Matter under New Extreme Conditions

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Borys E. Grinyuk ⁴, Violetta Sagun ^{7,*} and Oleksii Ivanytskyi ¹

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⁵ National Research Nuclear University (MEPhI), Kashirskoe Shosse 31, 115409 Moscow, Russia; zhrebtsova.lisa@gmail.com

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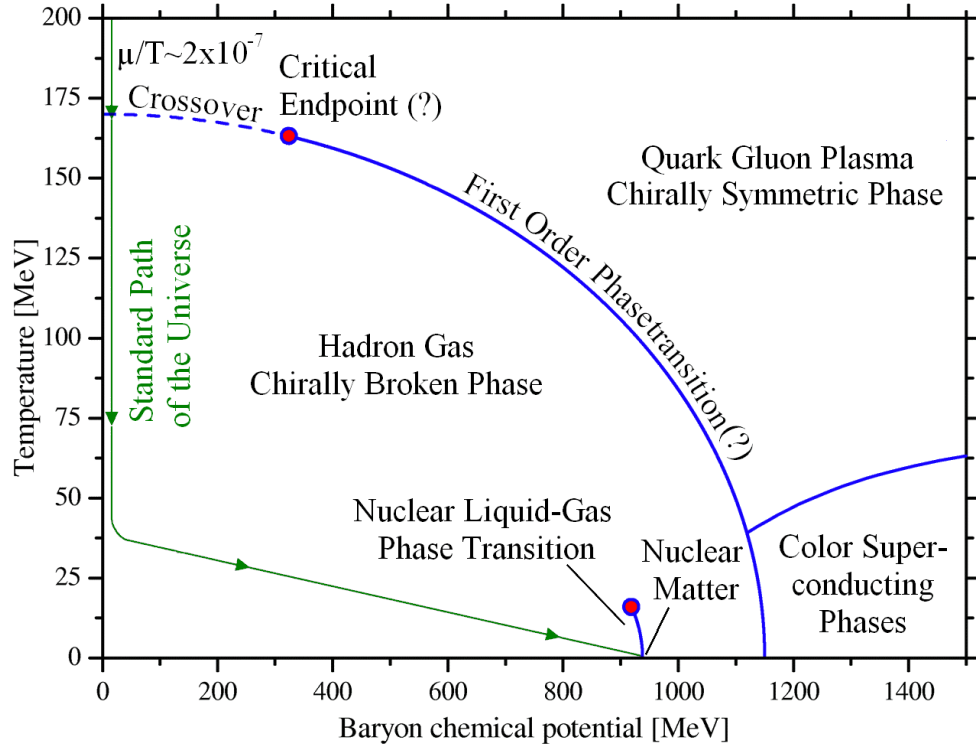
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Introduction

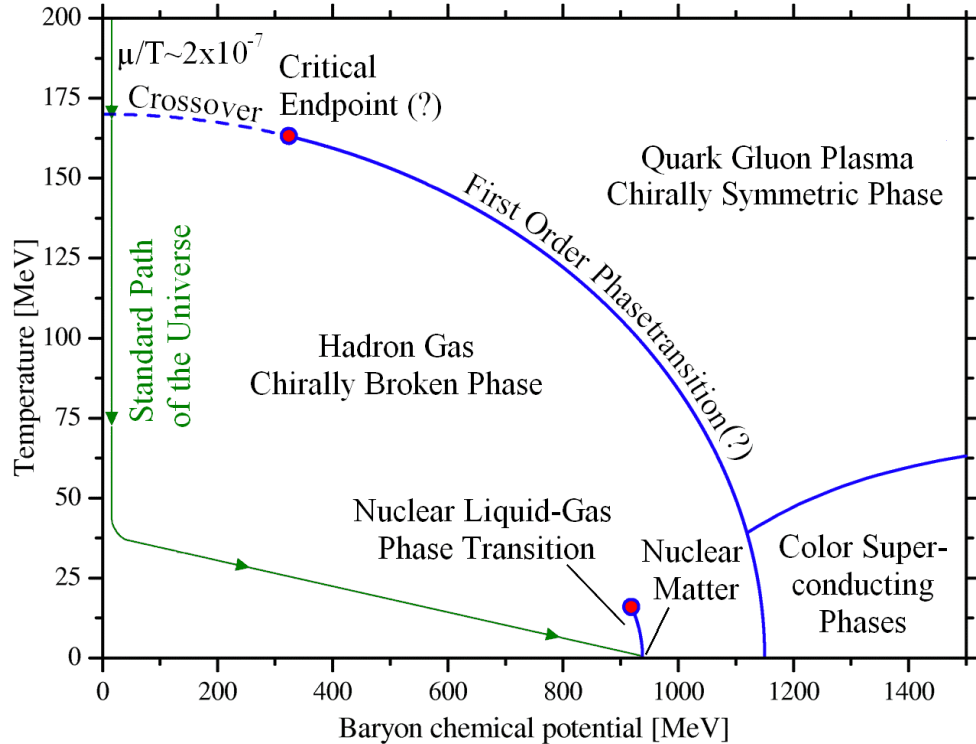


The main goal of heavy-ion collisions experiments is the understanding theory of strong interactions - QCD.

Exploring of the QCD phase diagram:

- Detect signals of deconfinement PT
- Detect signals of (partial) chiral symmetry restoration
- Locate (tri)critical endpoint(s) if such exists

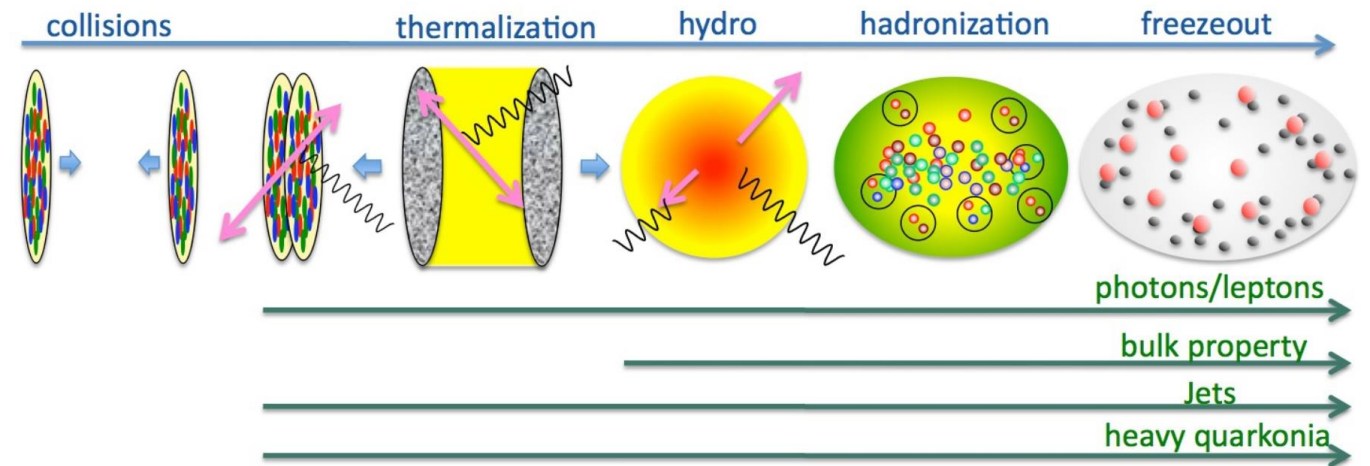
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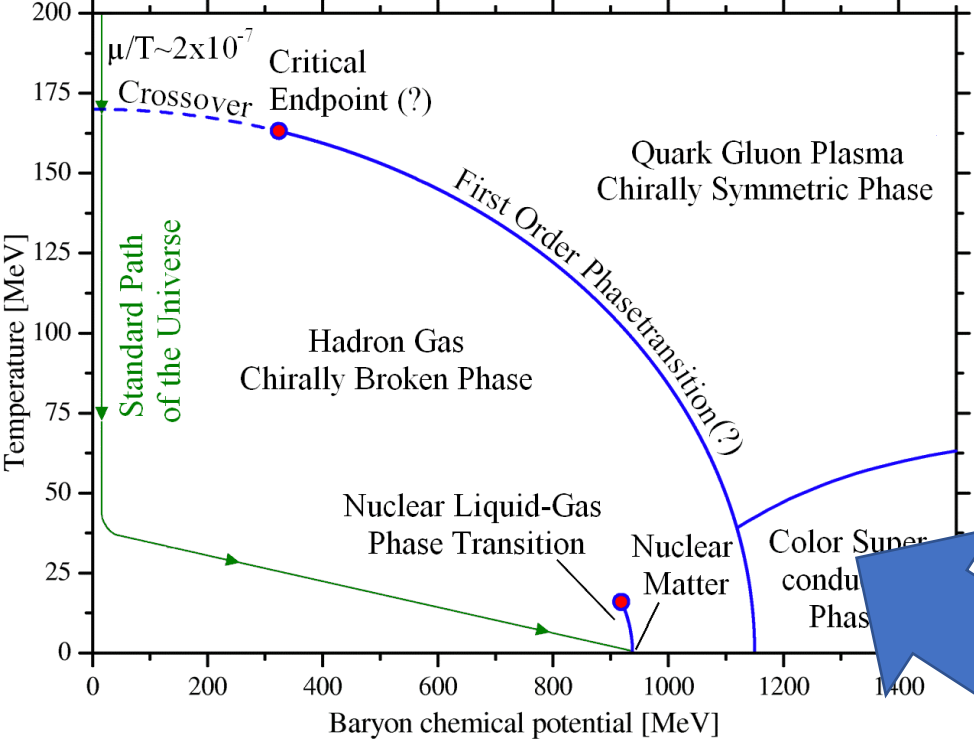
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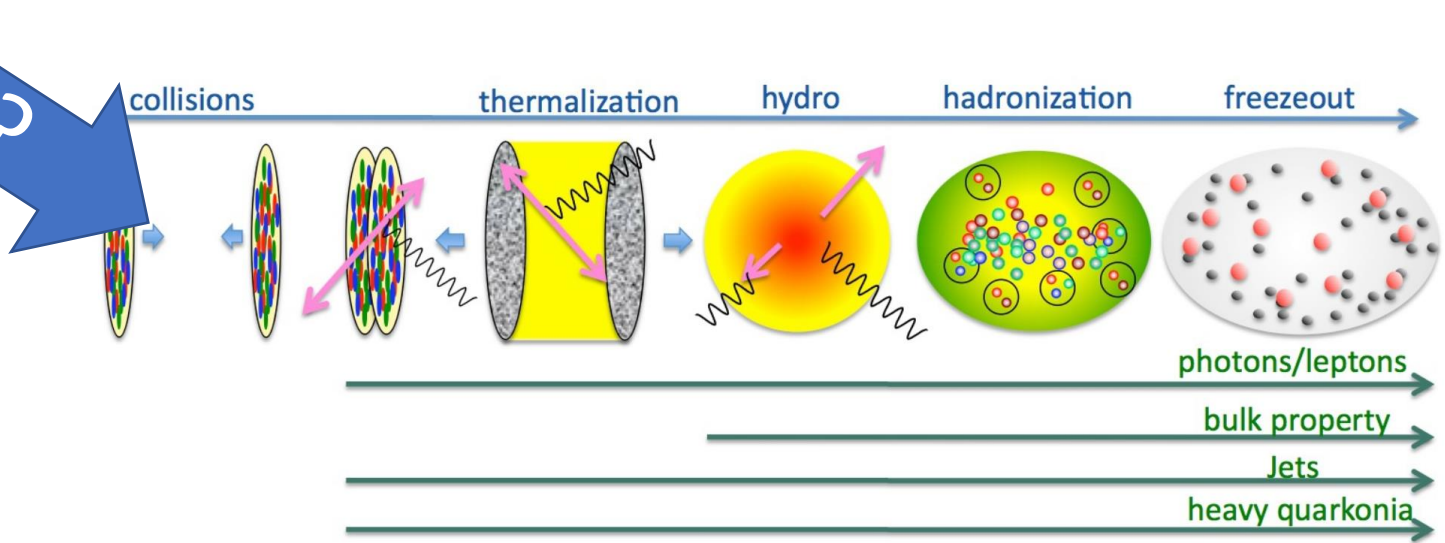
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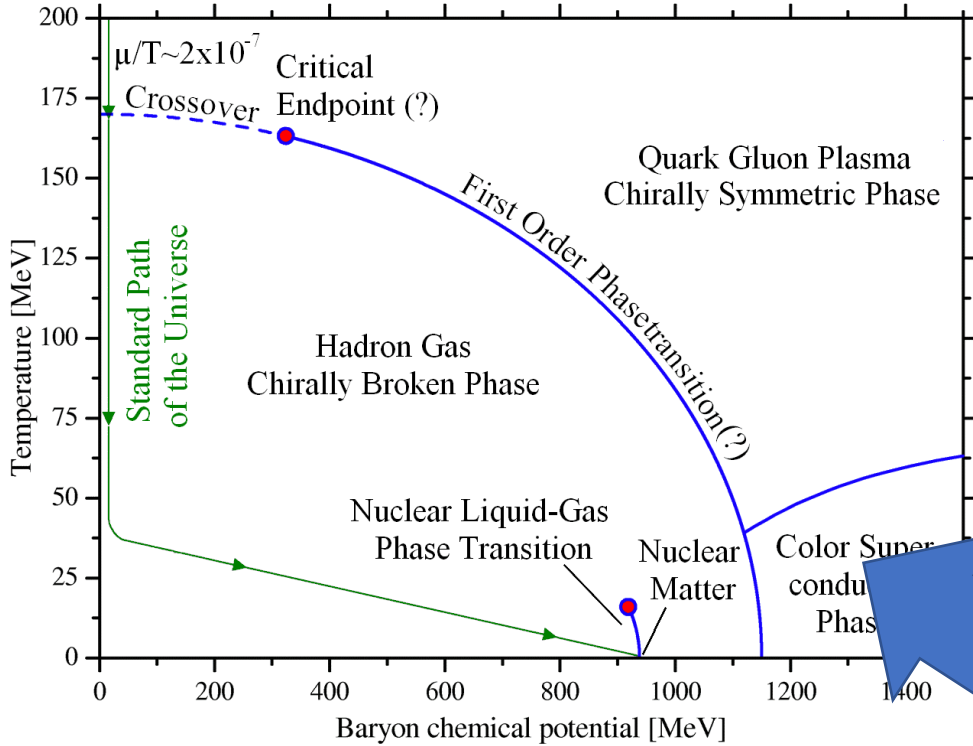
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[Credit: Universe 4 (2018) 52 & PoS (KMI 2013) 025]

Introduction

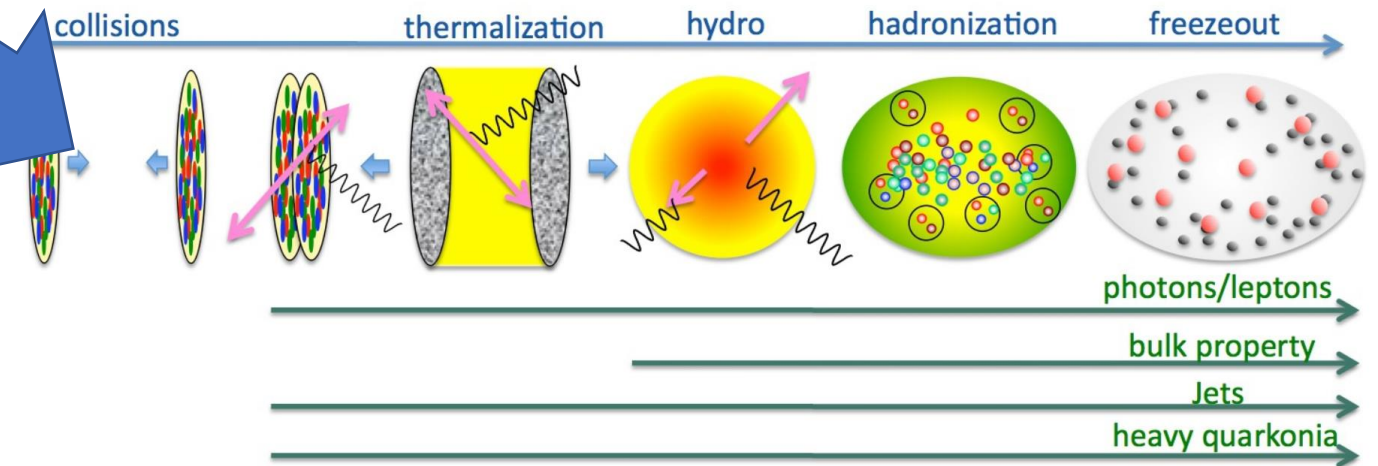


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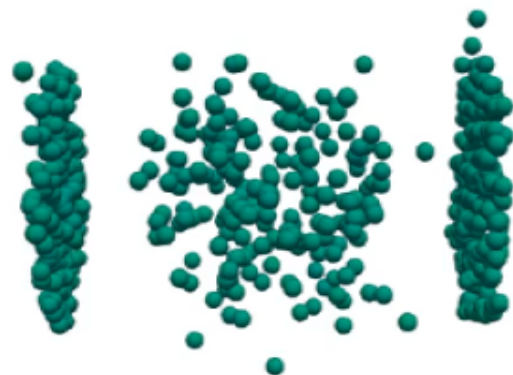
In order to resolve these tasks we need a very good observables and tools to analyse the data!



- Represents a Monte Carlo method for the time evolution of the various phase space densities of particle species
- Based on the covariant propagation of all hadrons on classical trajectories, stochastic binary scatterings, resonance and string formation with their subsequent decay
- Provides the solution of the relativistic Boltzmann equation
- The collision criterion is a black disk approximation: $d < d_0 = \sqrt{\sigma(\sqrt{s}, type)/\pi}$
- 55 baryons and 32 mesons are included. All antiparticles and isospin-projected states are implemented
- Cross sections are taken from PDG where possible + additive quark model
- Resonances are implemented in Breit–Wigner form

[S. A. Bass et al, Prog. Part. Nucl. Phys. 41 (1998) 255-369,
M. Bleicher et al, J. Phys. G: Nucl. Part. Phys. 25 (1999) 1859-1896]

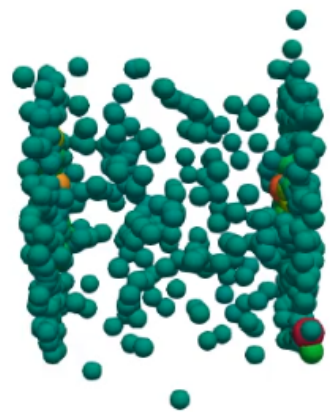
UrQMD-3.4, $\sqrt{s} = 20$ GeV, $b = 0$ fm, $t = 0.0$ fm/c
Pb+Pb+Pb



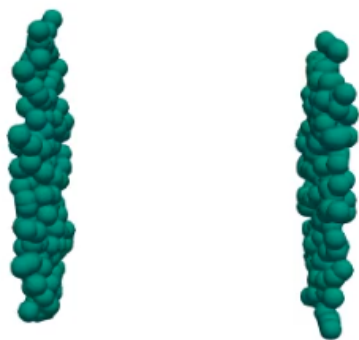
Pb+Pb



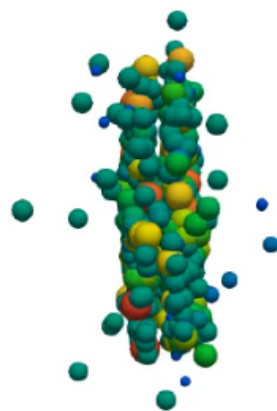
UrQMD-3.4, $\sqrt{s} = 20$ GeV, $b = 0$ fm, $t = 5.0$ fm/c
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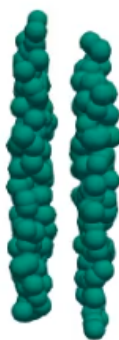
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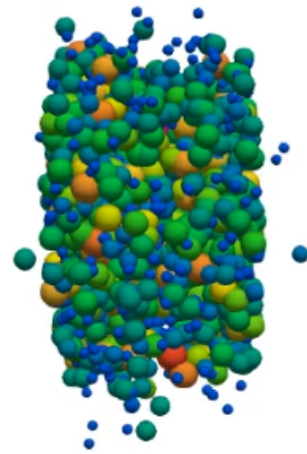
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Pb+Pb+Pb



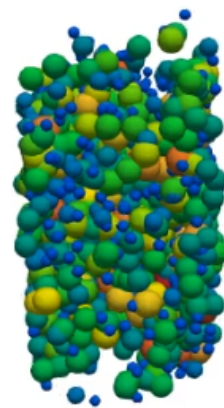
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UrQMD-3.4, $\sqrt{s} = 20$ GeV, $b = 0$ fm, $t = 15.0$ fm/c
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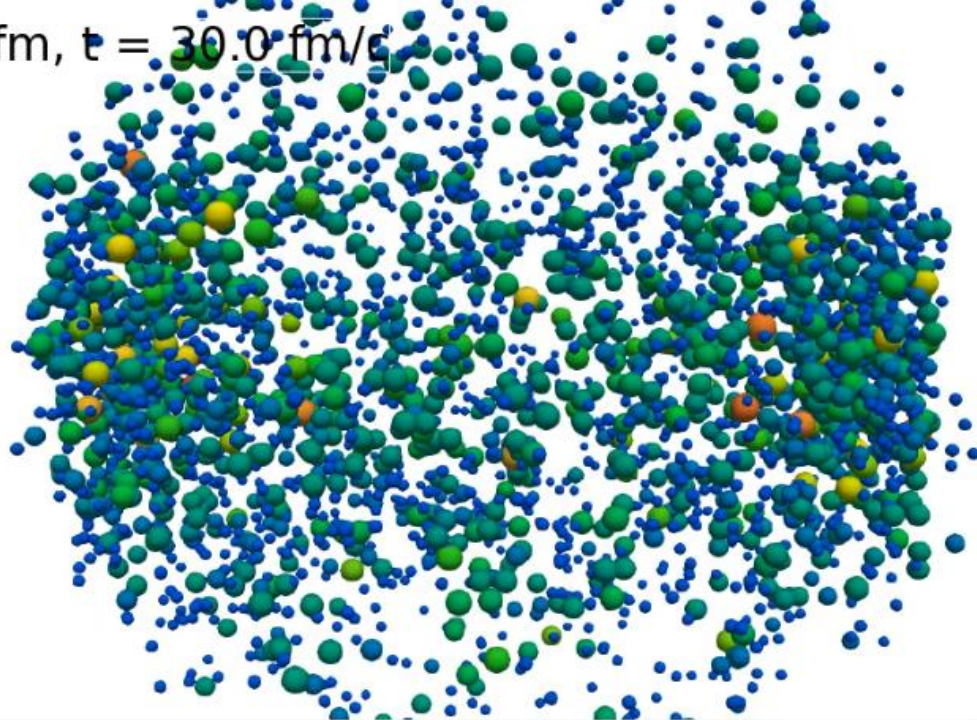
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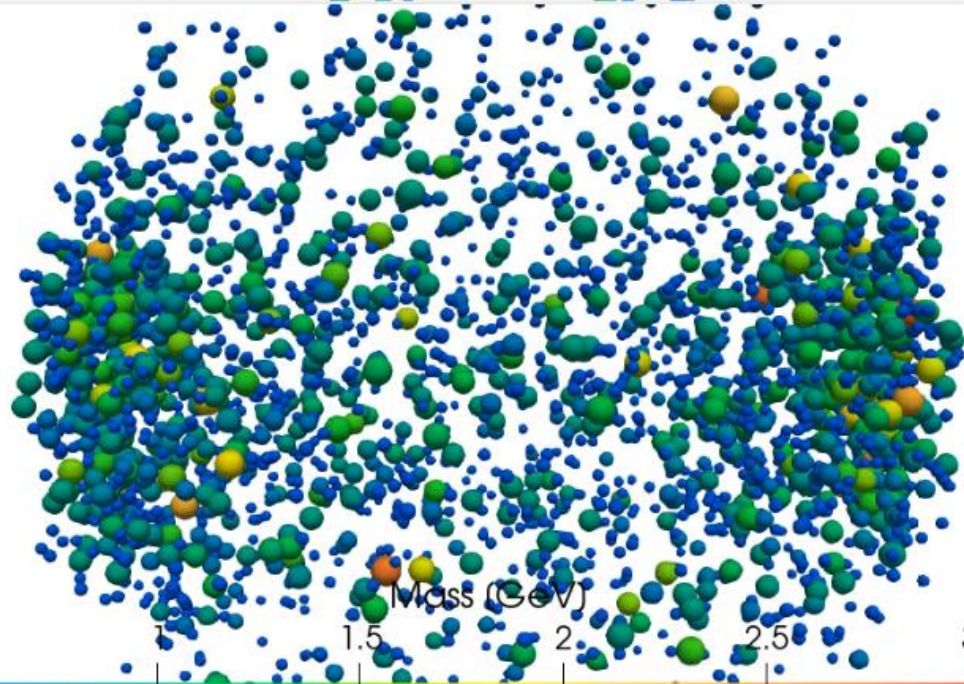
Mass (GeV)



UrQMD-3.4, $\sqrt{s} = 20$ GeV, $b = 0$ fm, $t = 30.0$ fm/c
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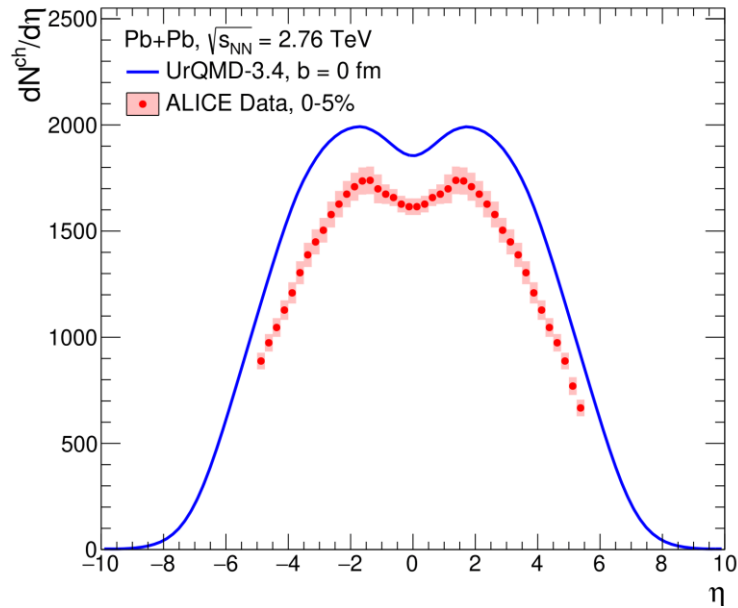
Pb+Pb



Model vs A+A data

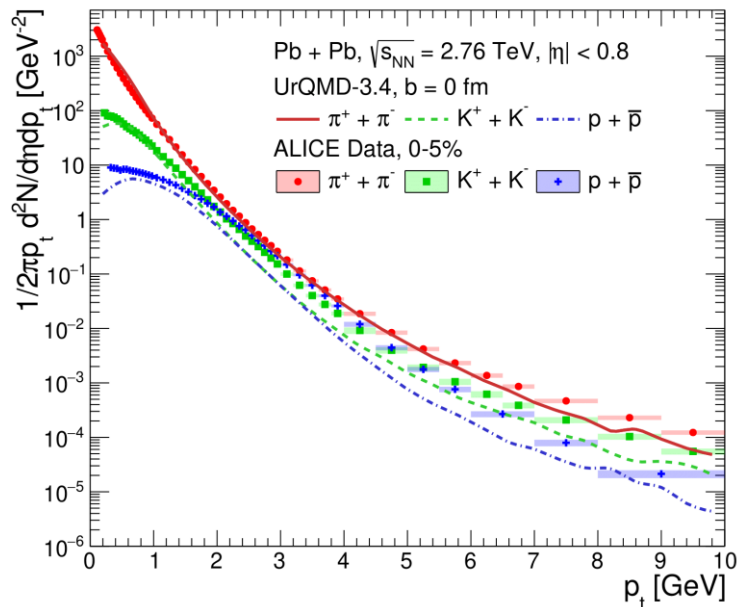
- Main task is to study the properties of hadron production in TNC
- Main interest is the baryon production in most central collisions
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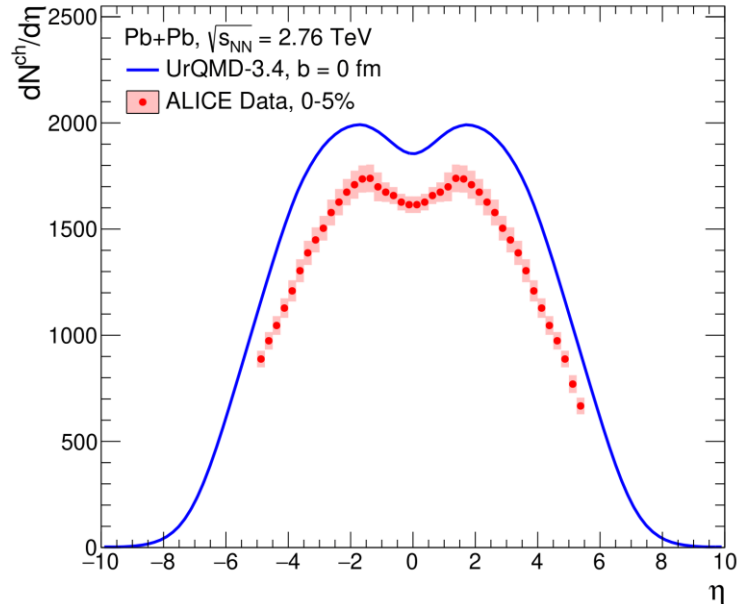


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ALICE, 0-5%	669.5 ± 48	668 ± 47	100 ± 8	99.5 ± 8.5	31 ± 2.5	30.5 ± 2.5
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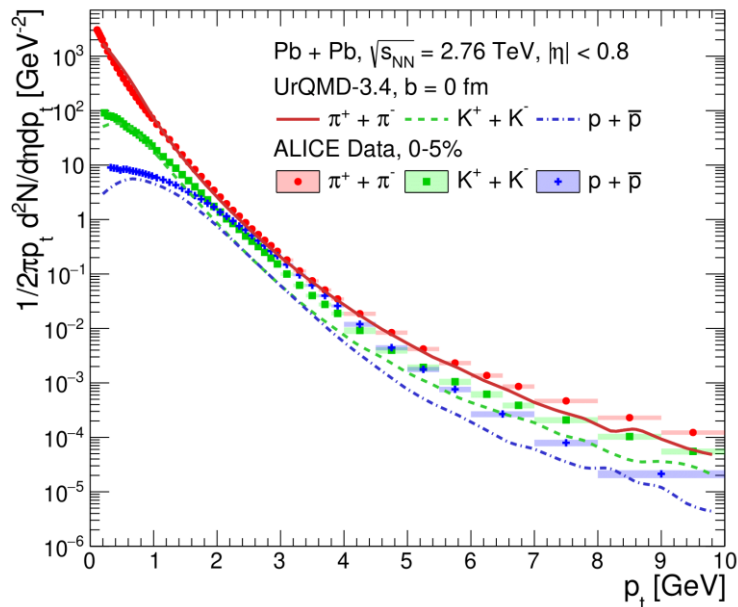
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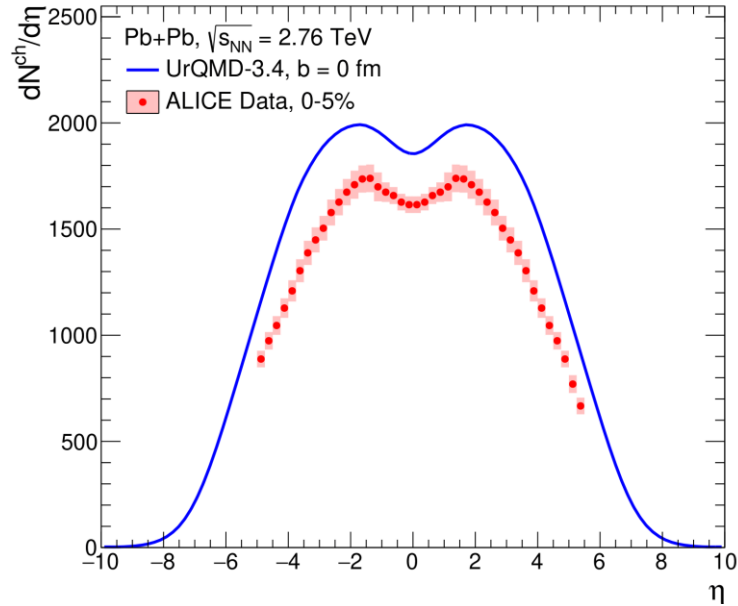
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±OK

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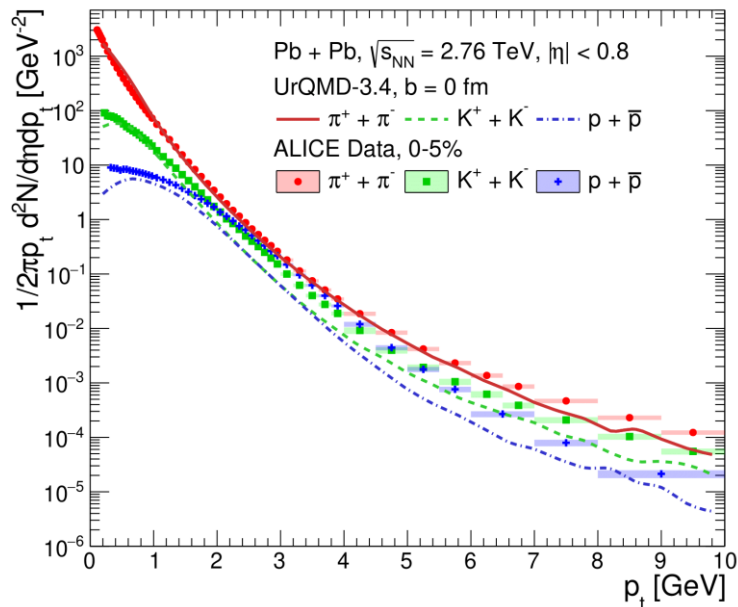
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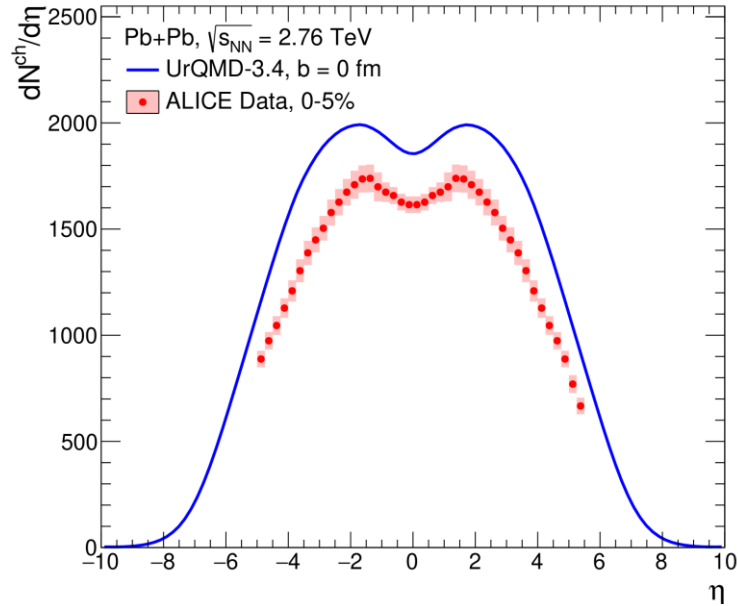
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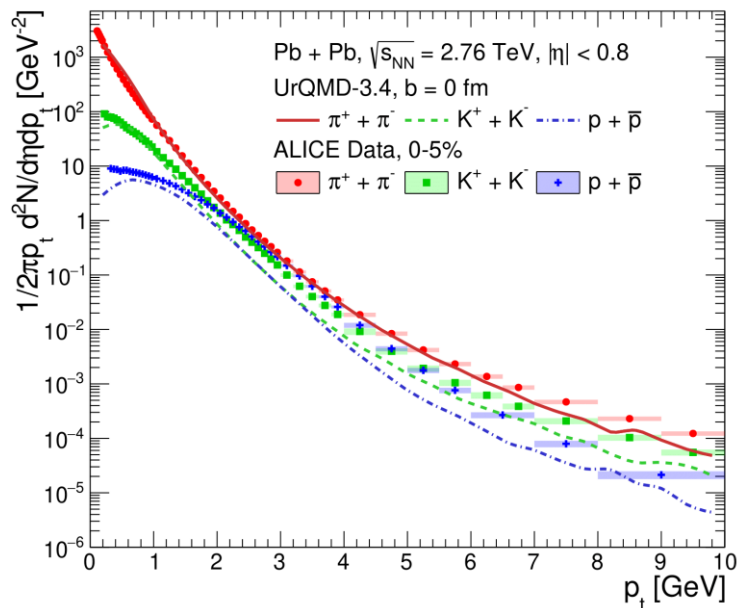
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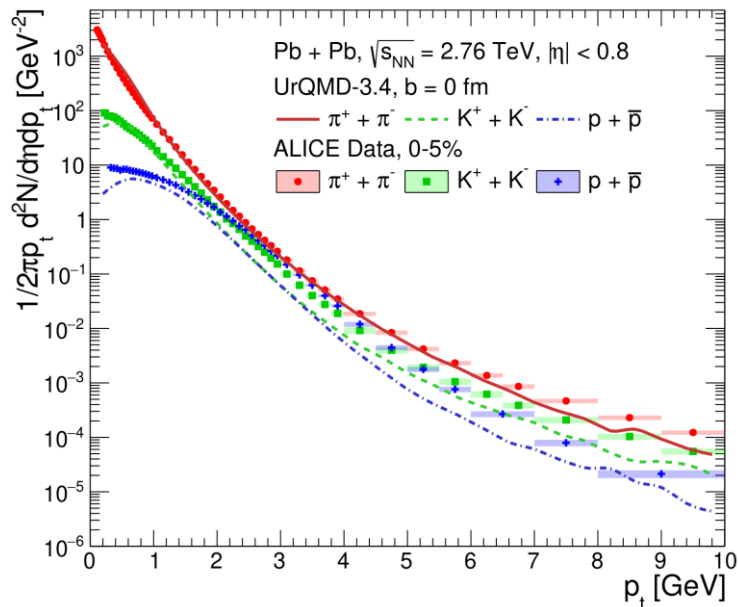
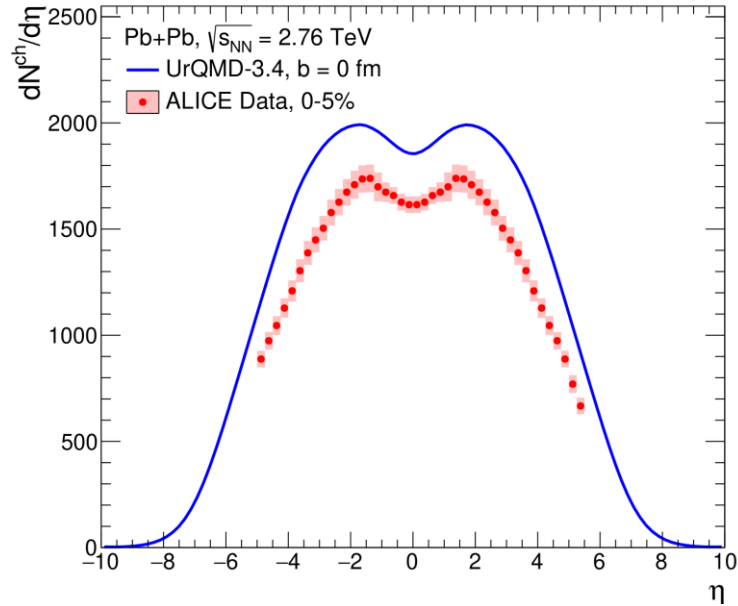
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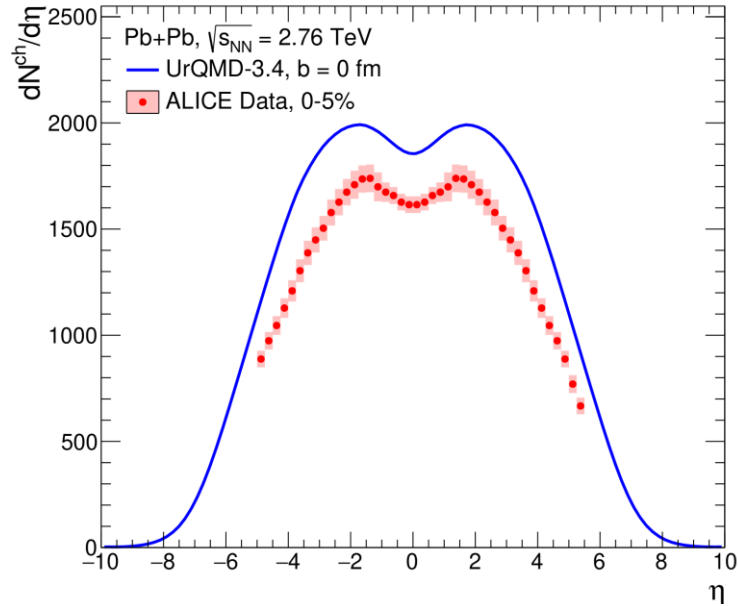


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$$R_{32}(y) = \left(\frac{dN}{dy} \right)_{TNC} / \left(\frac{dN}{dy} \right)_{BC}$$

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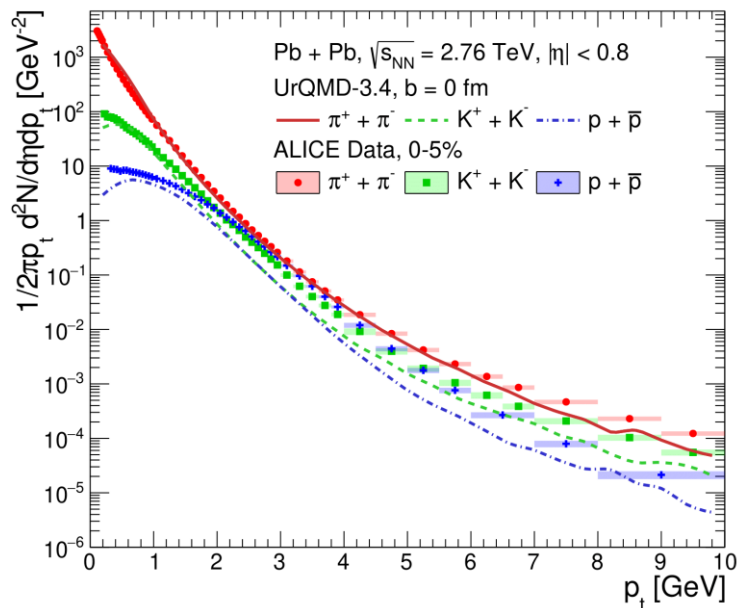
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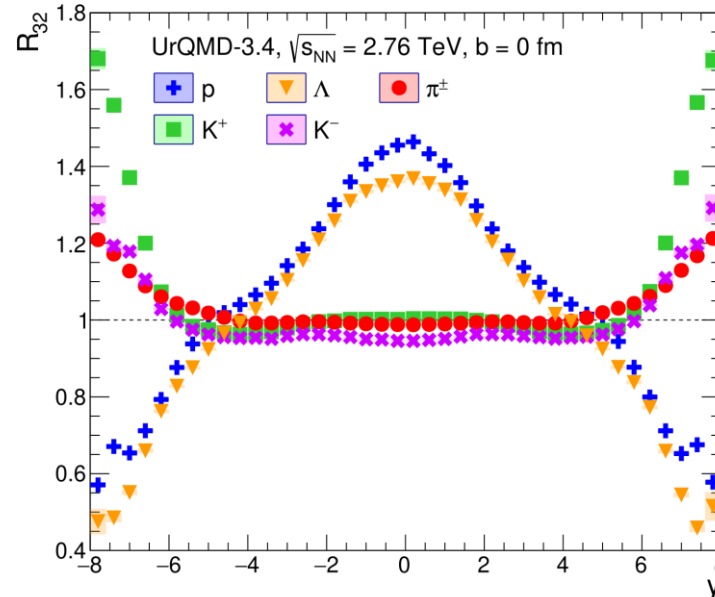
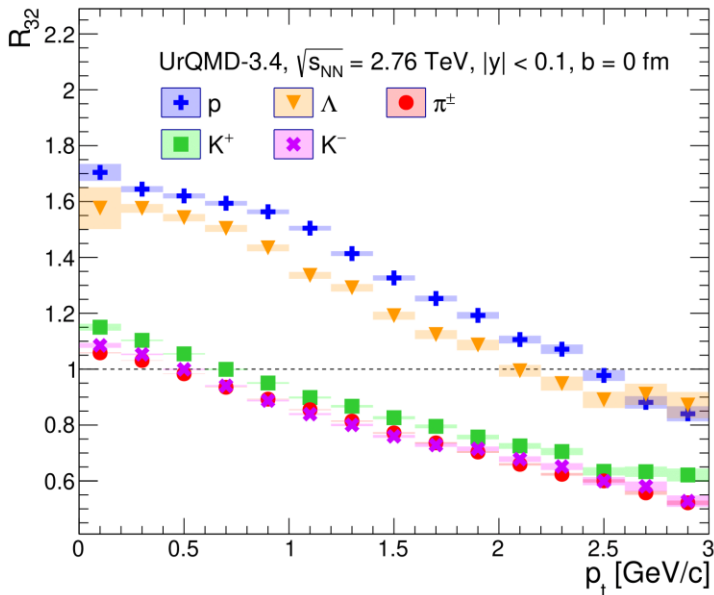
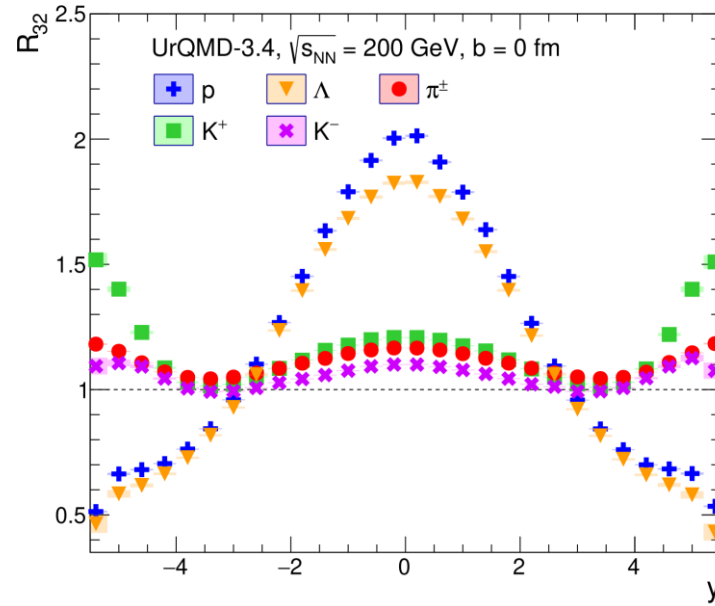
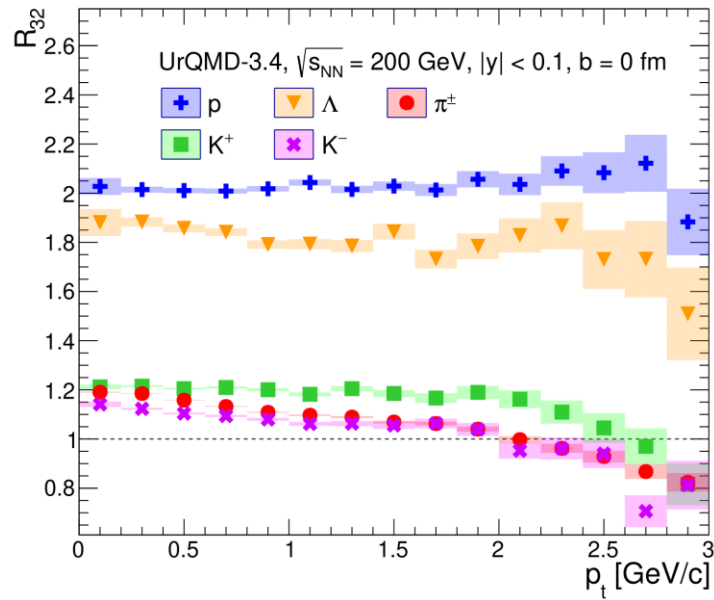


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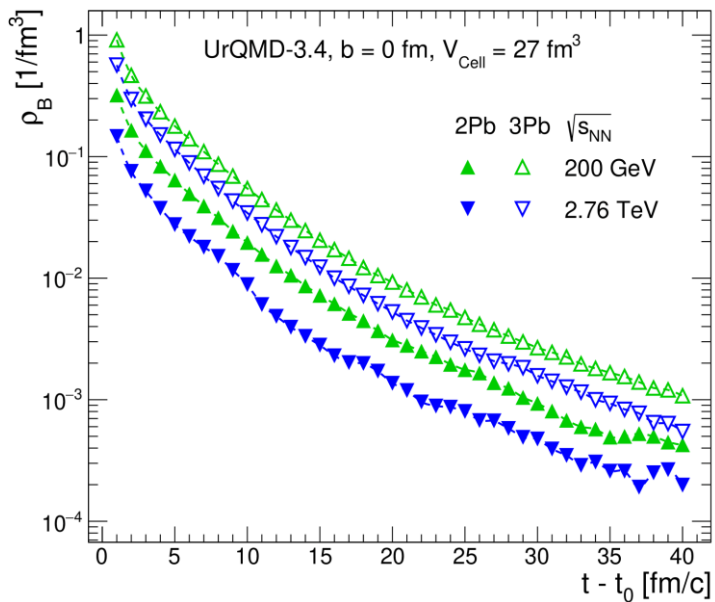
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Results: $R_{32}(y)$ & $R_{32}(p_t)$



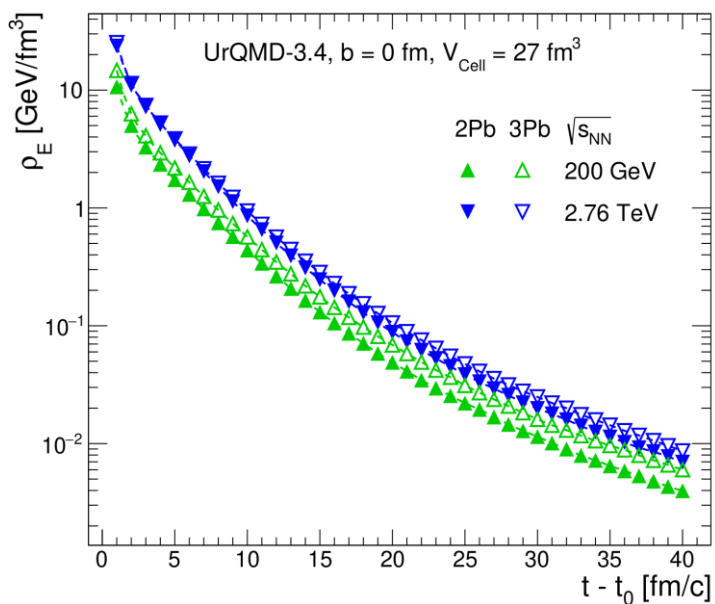
- Baryon yields are strongly enhanced in the midrapidity region
- p_t -spectra show enhancement of slow hadrons and deficit of fast ones
 1. Density trap
 2. Transverse momentum redistribution effect
- Different p_t behavior of 3-to-2 nuclei enhancement factor at RHIC and LHC energies
 1. $\approx \text{const.}$ at RHIC energy for particles with $p_t \leq 2$ GeV/c
 2. Decreasing function of p_t at LHC energy

Results: Central Cell Evolution

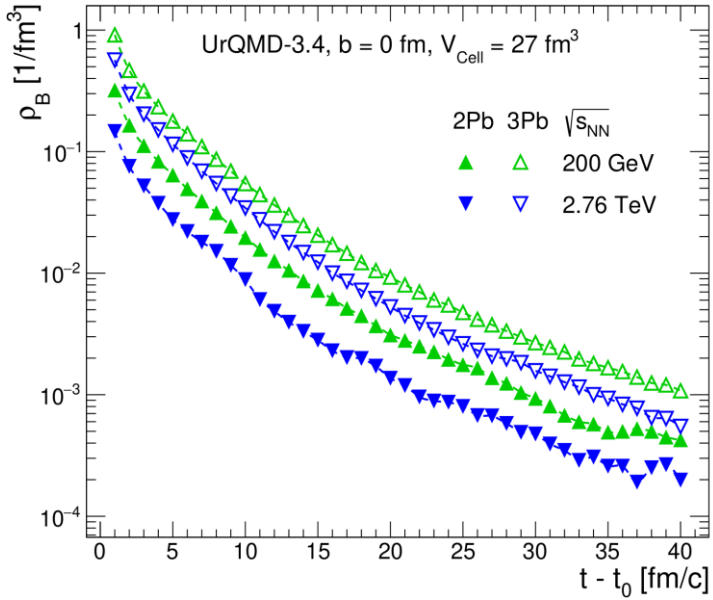


UrQMD

$$n_B = \frac{1}{V} \sum_{\vec{r}_k \in V} B_k$$
$$\varepsilon = \frac{1}{V} \sum_{\vec{r}_k \in V} E_k$$



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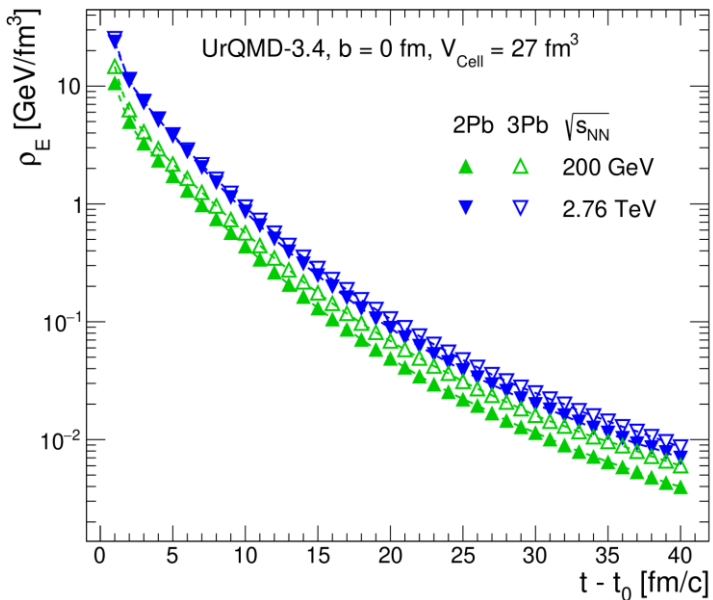
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Bag Model EoS

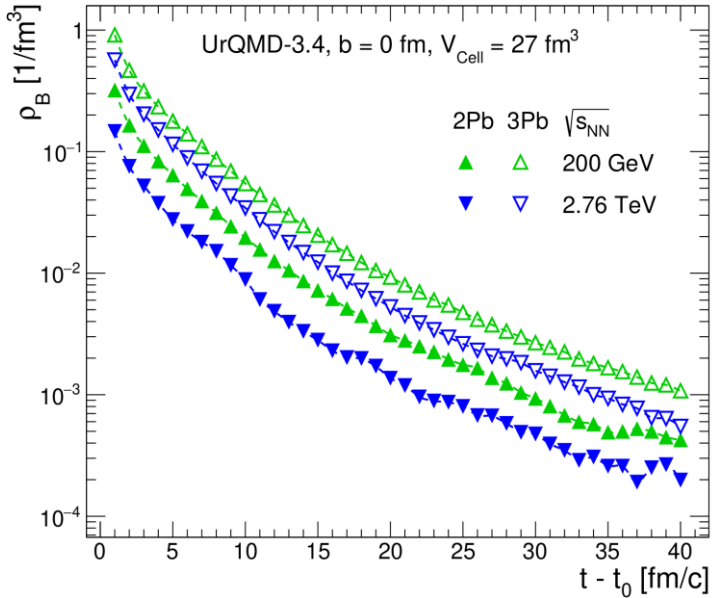
$$p = \frac{19}{36} \pi^2 T^4 + \frac{1}{6} \mu_B^2 T^2 + \frac{\mu_B^4}{108 \pi^2} - B_{vac}$$

$$\varepsilon = \frac{19}{12} \pi^2 T^4 + \frac{1}{2} \mu_B^2 T^2 + \frac{\mu_B^4}{36 \pi^2} + B_{vac}$$

$$n_B = \frac{\mu_B}{3} \left(T^2 + \frac{\mu_B^2}{9 \pi^2} \right), B_{vac}^{1/4} = 206 \text{ MeV}$$



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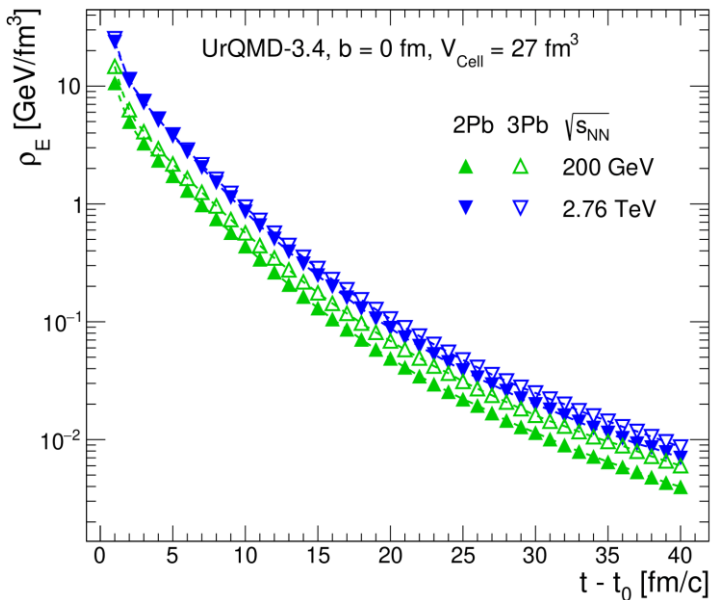


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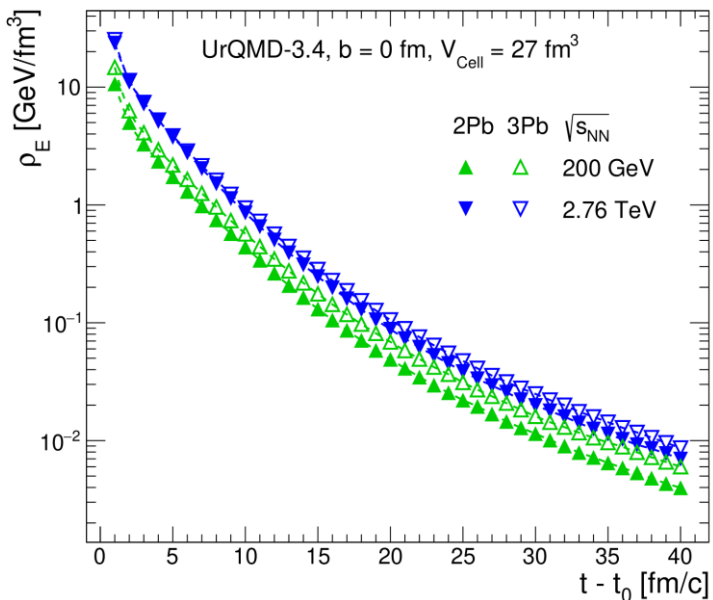
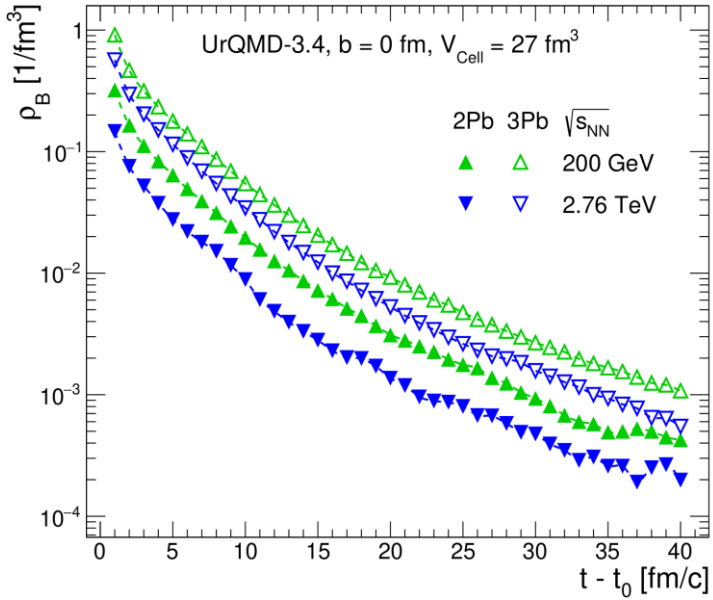
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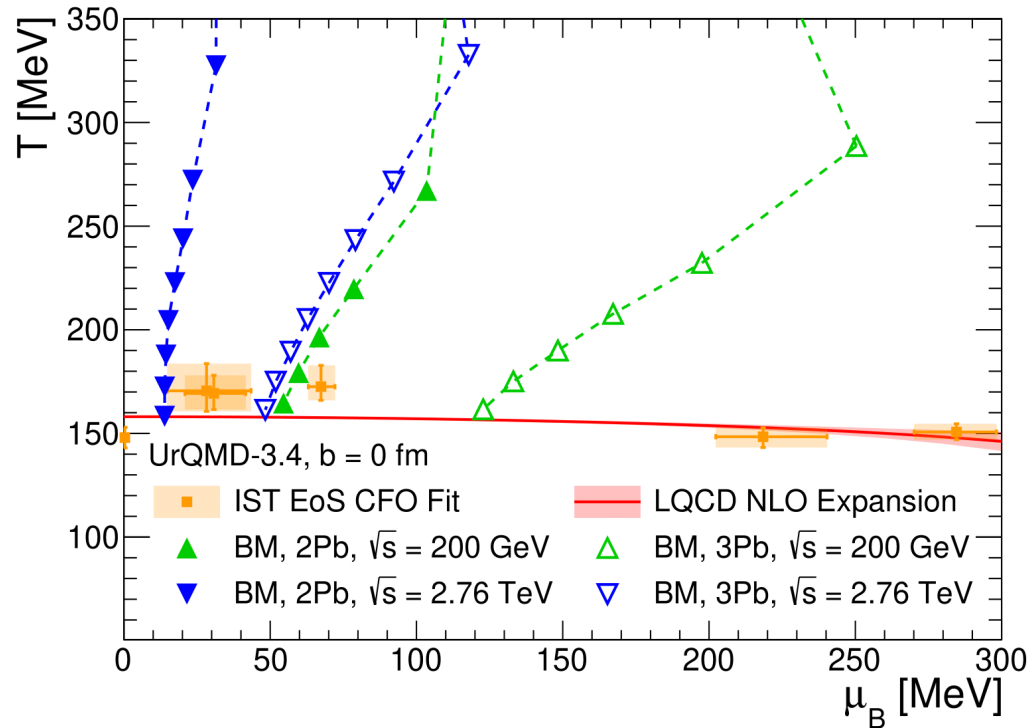


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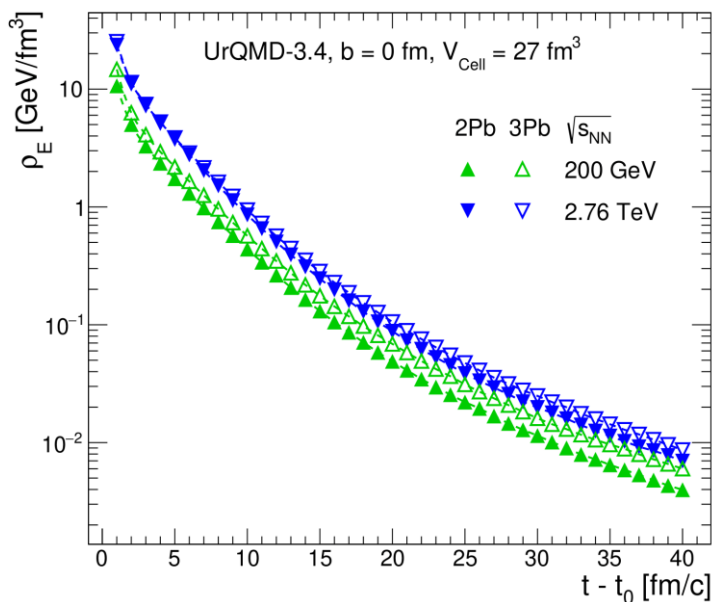
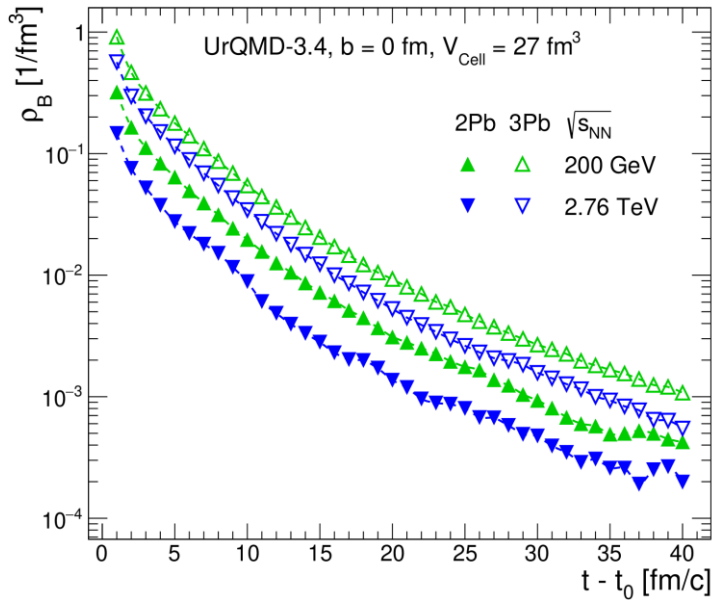
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$$\varepsilon = \frac{1}{V} \sum_{\vec{r}_k \in V} E_k$$

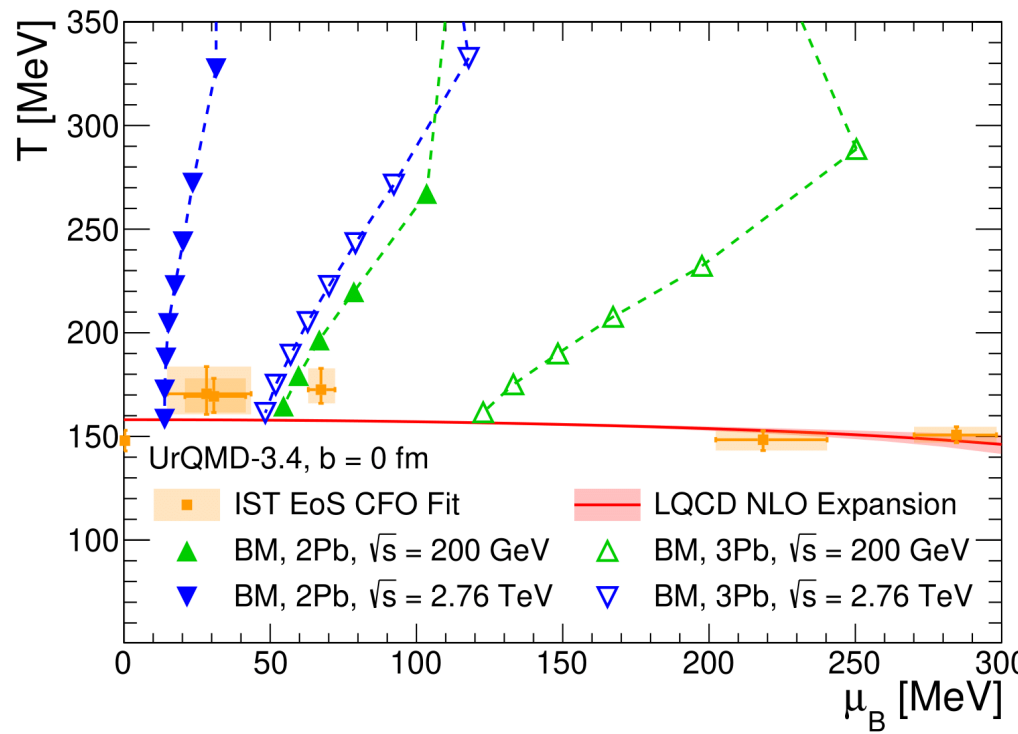


Bag Model EoS

$$p = \frac{19}{36} \pi^2 T^4 + \frac{1}{6} \mu_B^2 T^2 + \frac{\mu_B^4}{108 \pi^2} - B_{vac}$$

$$\varepsilon = \frac{19}{12} \pi^2 T^4 + \frac{1}{2} \mu_B^2 T^2 + \frac{\mu_B^4}{36 \pi^2} + B_{vac}$$

$$n_B = \frac{\mu_B}{3} \left(T^2 + \frac{\mu_B^2}{9 \pi^2} \right), B_{vac}^{1/4} = 206 \text{ MeV}$$

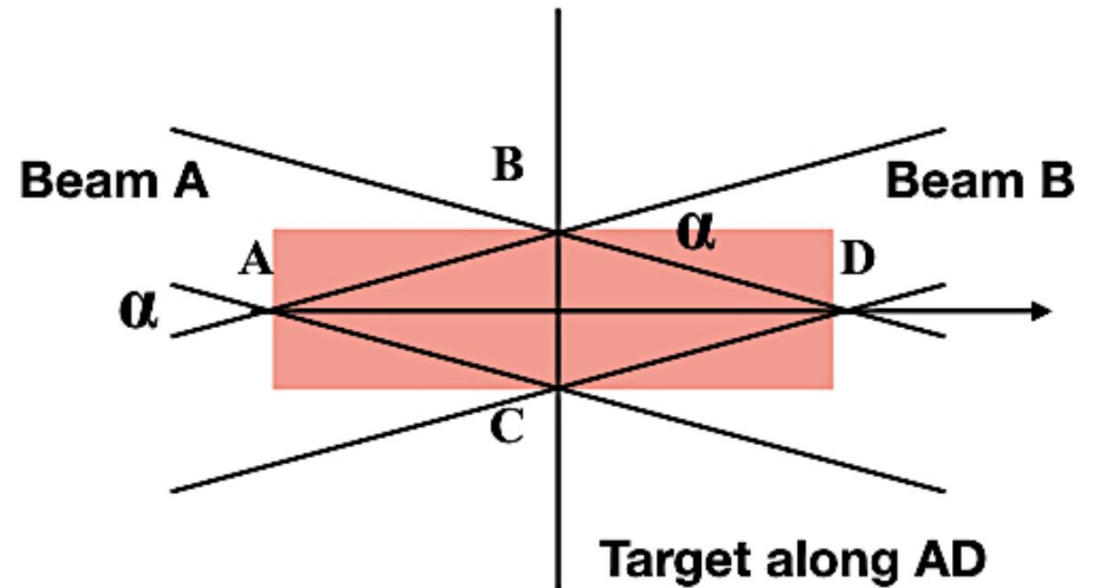
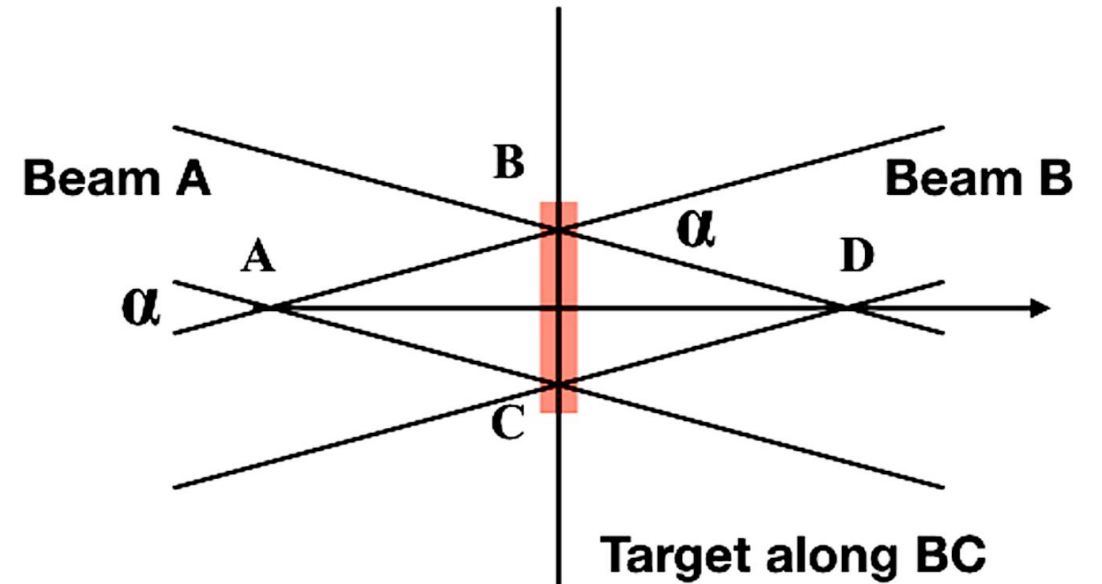


- Comparing to chemical freeze-out \Rightarrow accuracy of $\mu_B \sim 15$ MeV
- Central cell parameters at LHC are similar to A+A at RHIC, but initial n_B is 2 times higher
- Much higher μ_B can be reached in TNC!

TNC Rates

But what are the TNC rates?

Are the TNC the **dreams of theoreticians?**

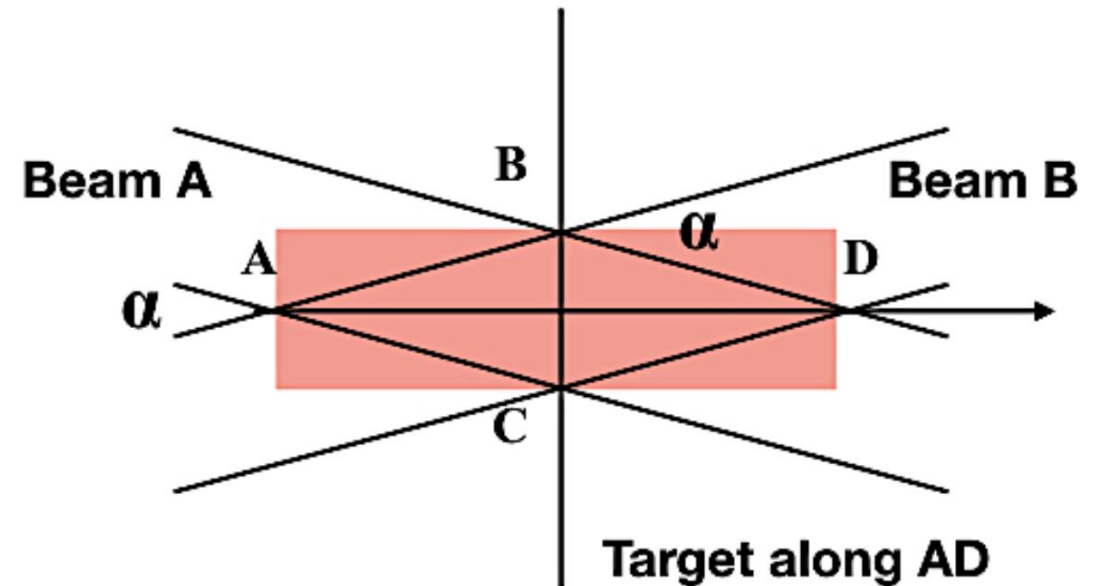
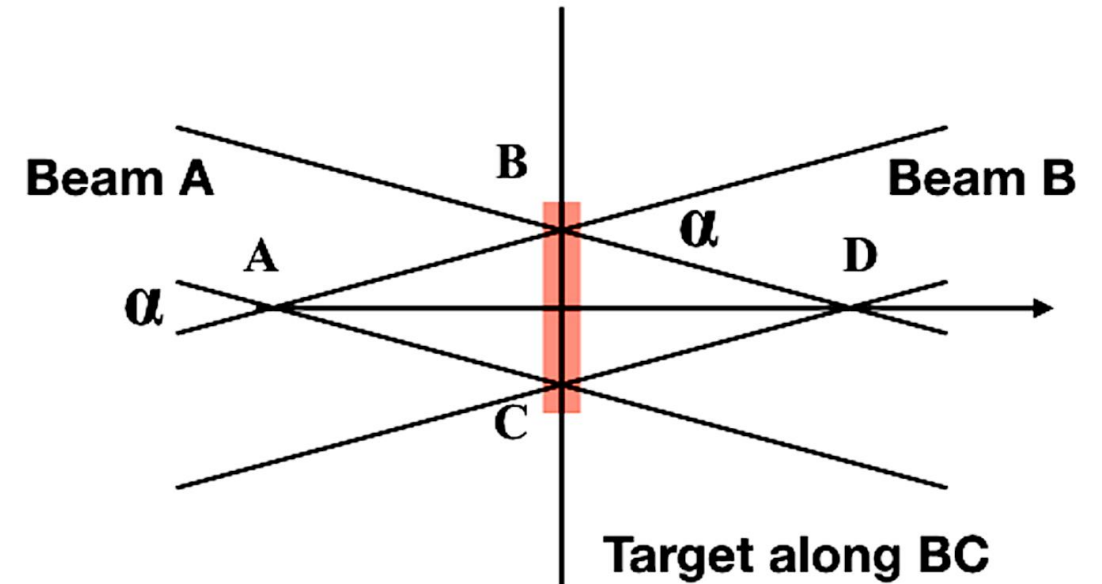


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$$\frac{dN_{A+T+B}}{dt} = L\sigma_{A+B}\rho_T V_{A+T+B}^{int} \frac{V_{irrad}^T}{V_{beams}}$$



TNC Rates

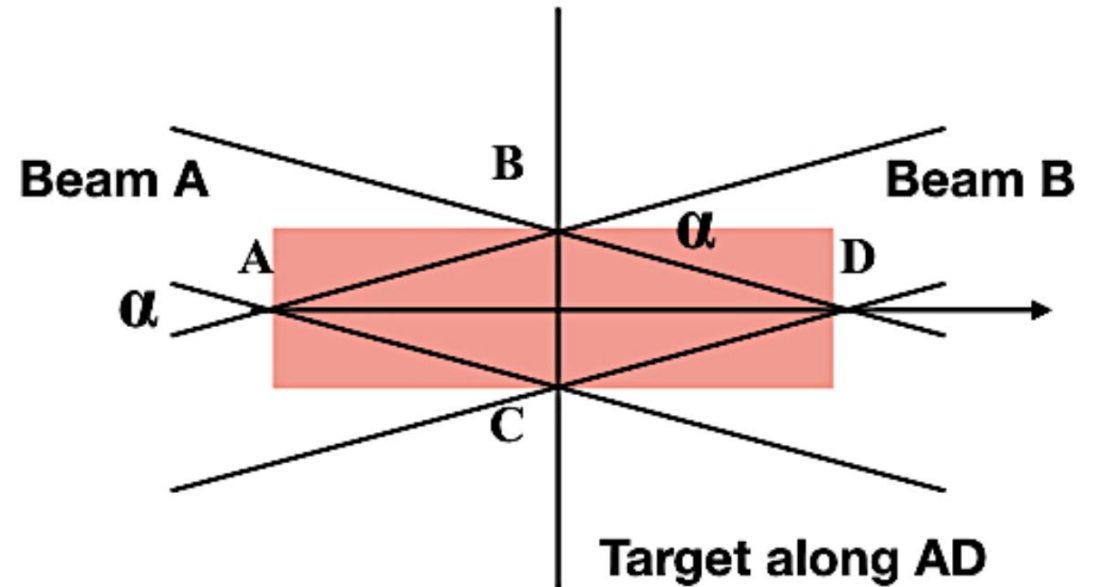
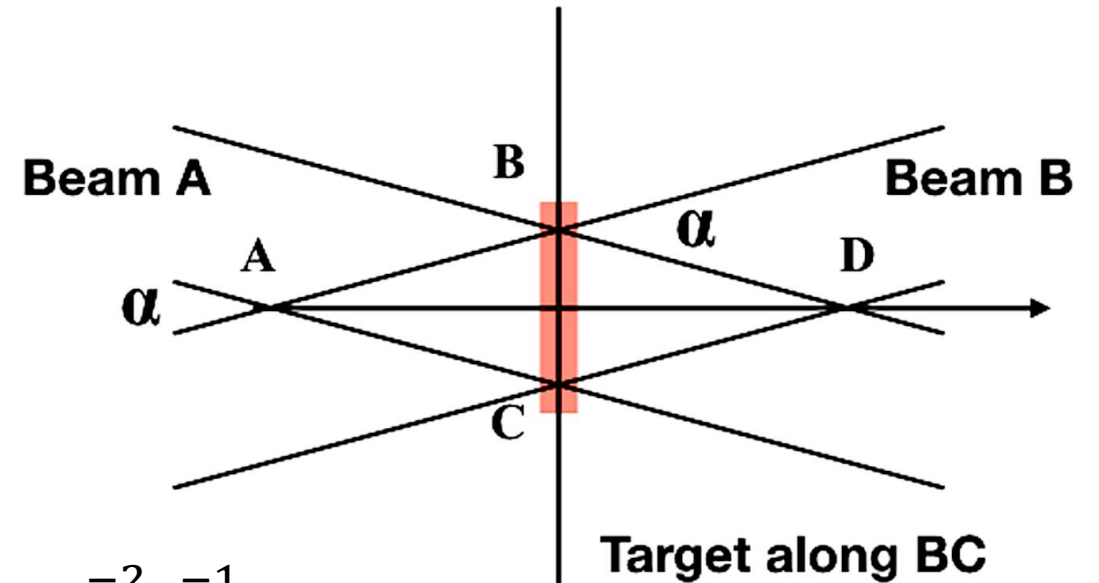
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Assuming the Pb beams luminosity value $L = 10^{28} \text{cm}^{-2} \text{s}^{-1}$

$$\frac{dN_{3Pb}}{dt} = \begin{cases} 2.4 \times 10^{-11} \text{s}^{-1}, & \text{for } 3.3 \mu\text{m target} \\ 3.4 \times 10^{-7} \text{s}^{-1}, & \text{for large target} \end{cases}$$



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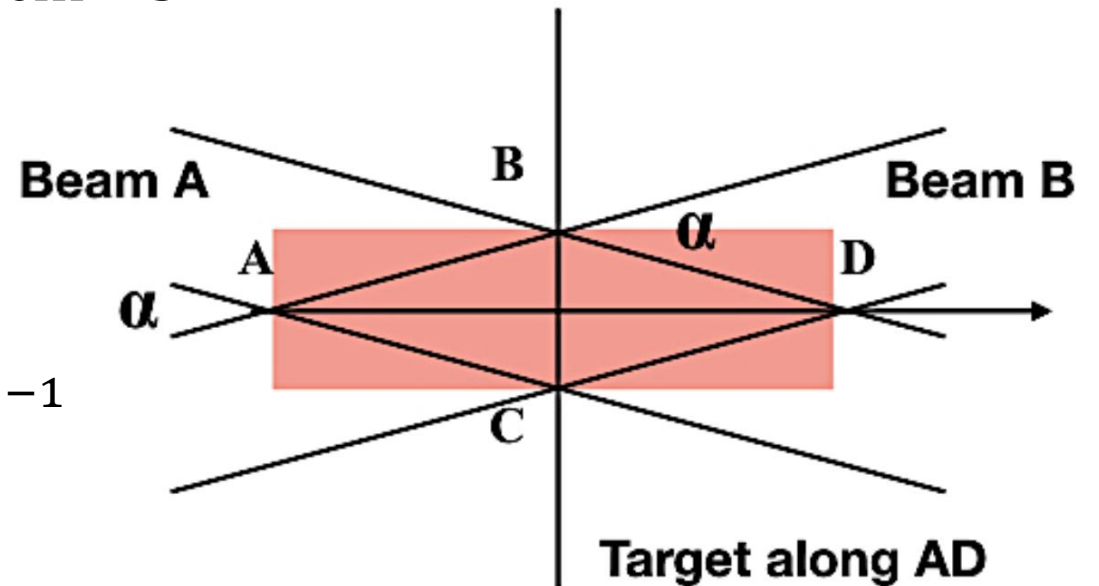
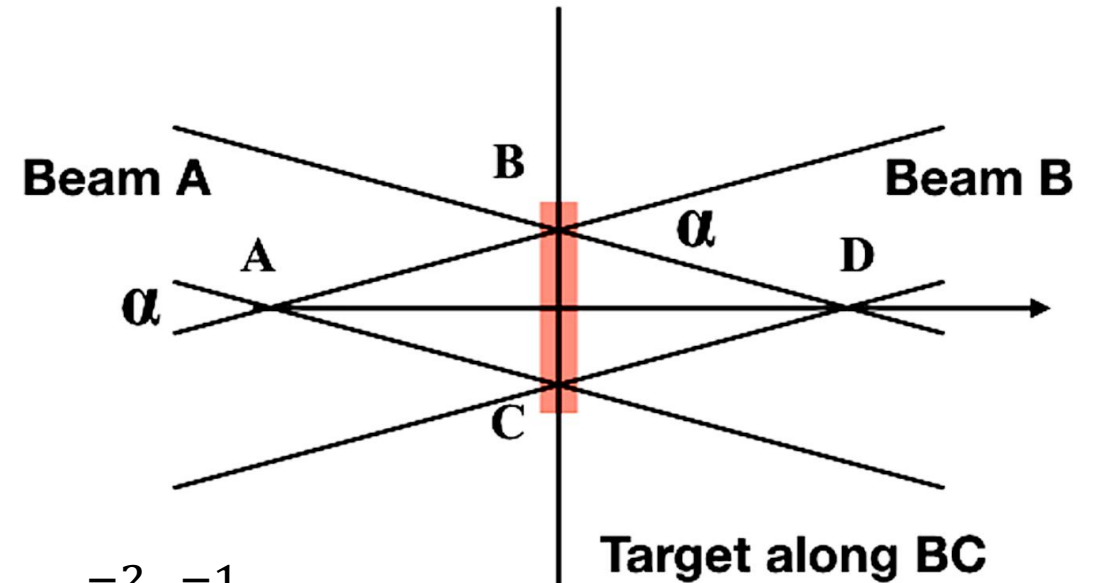
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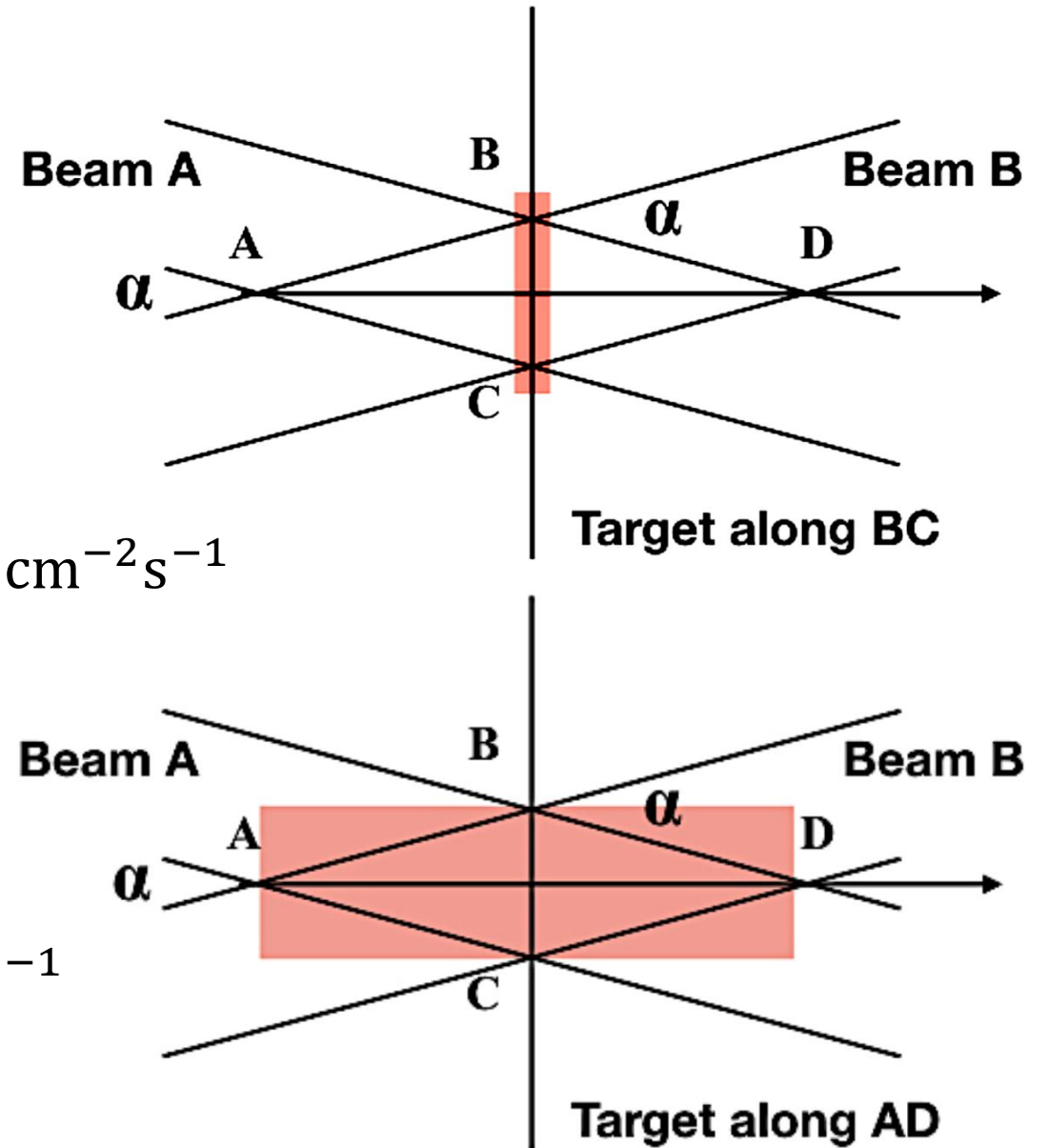
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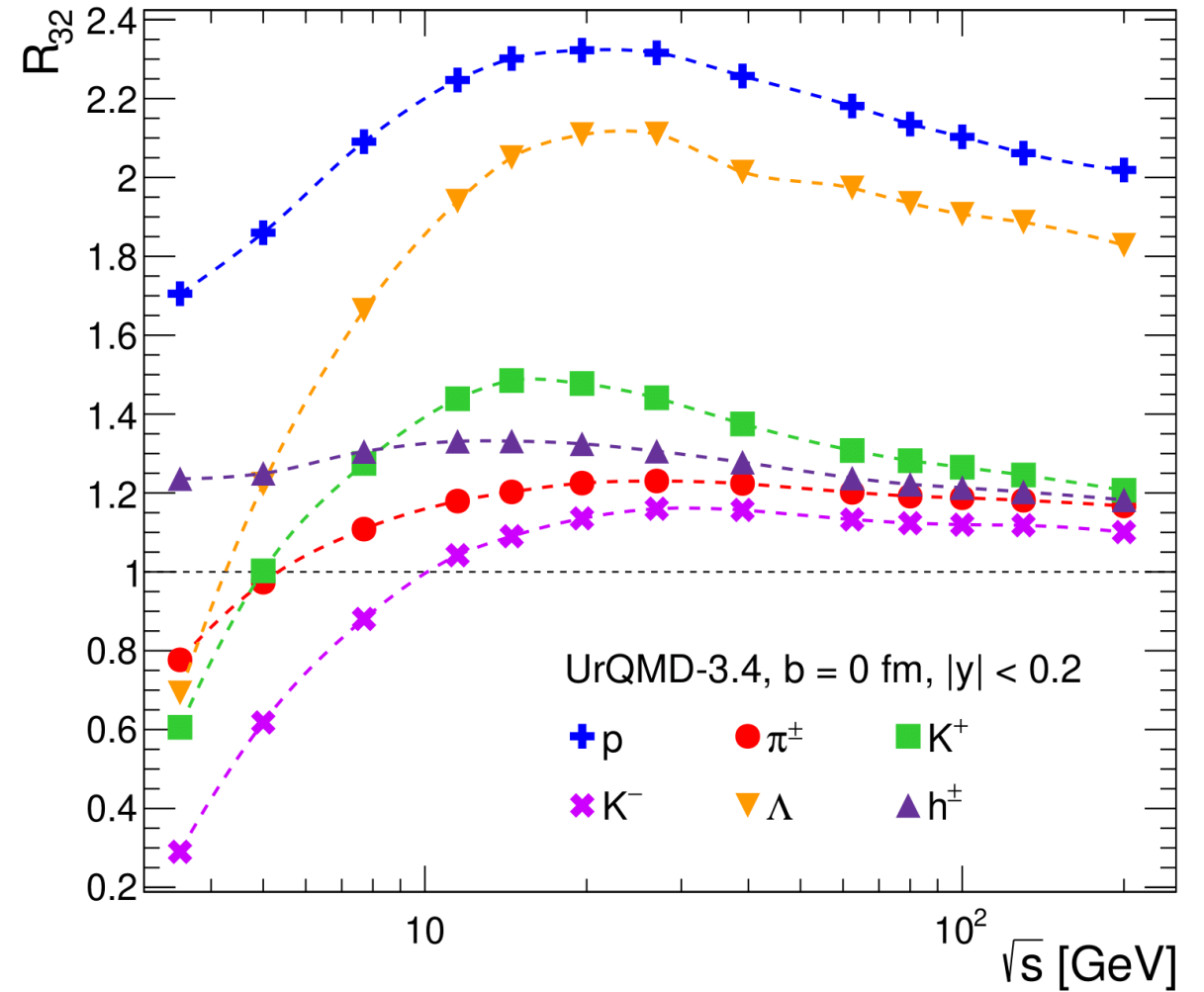
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New ideas are needed!



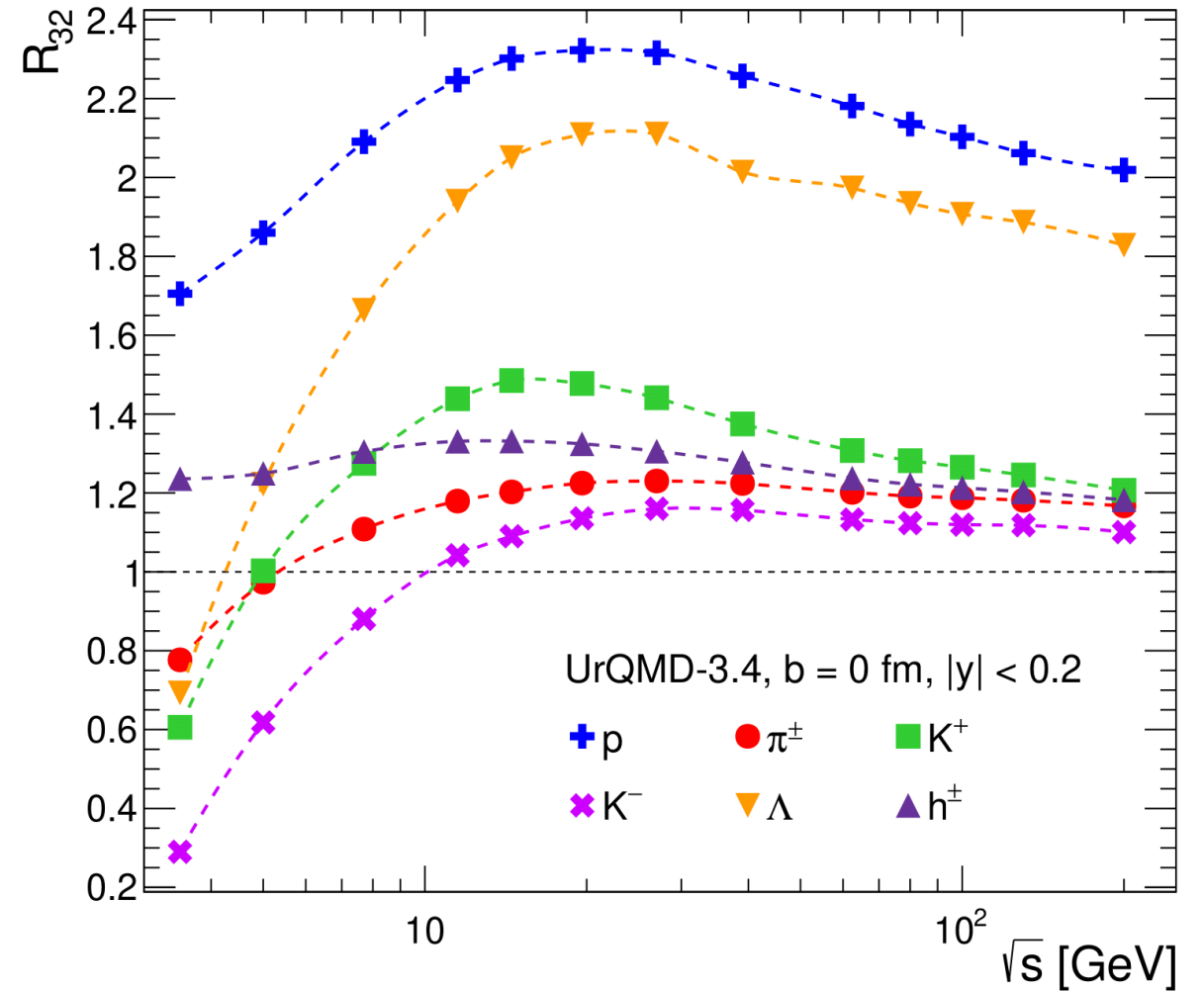
Summary & Conclusions



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With TNC we can probe very high densities of baryonic and electric charges



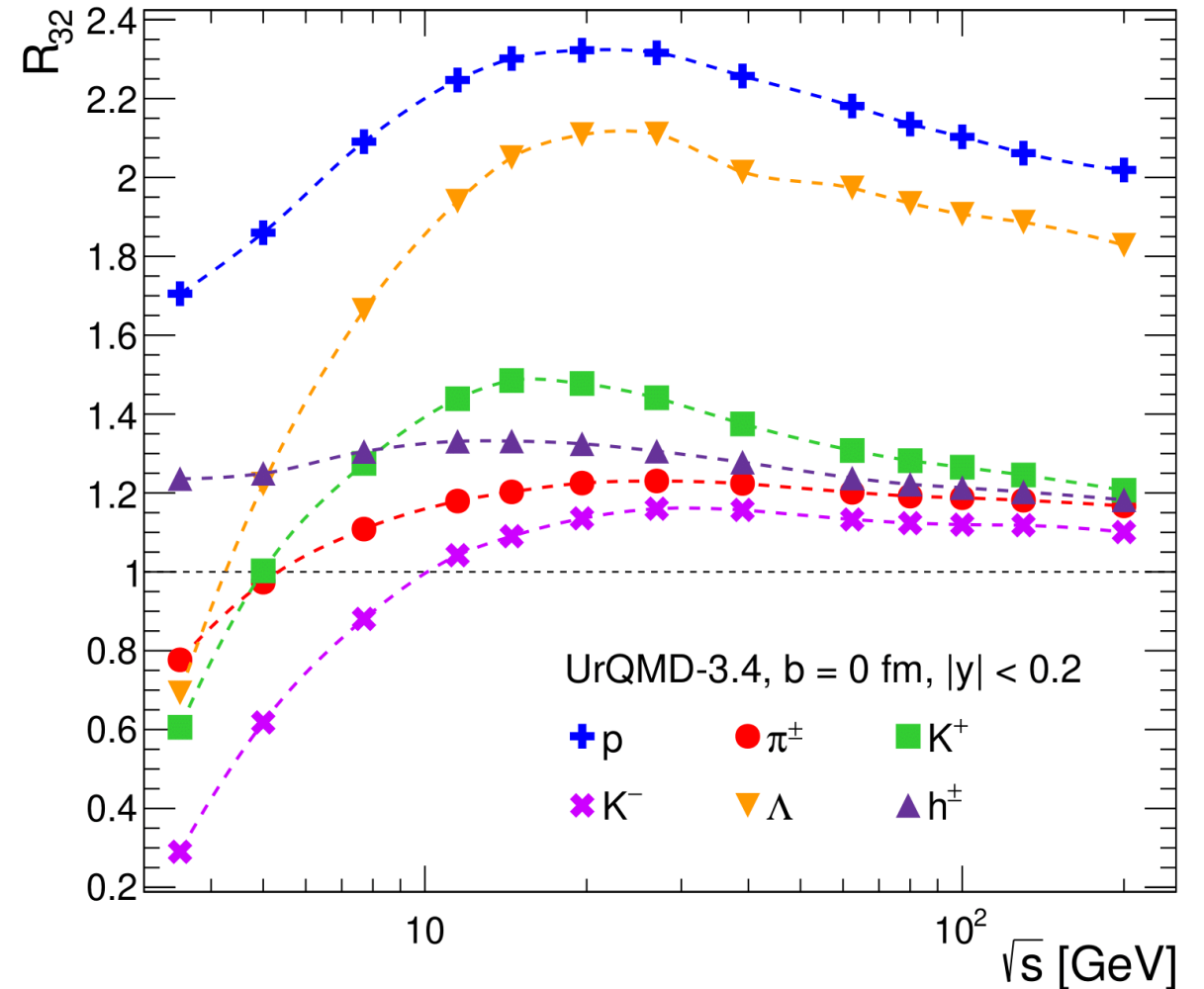
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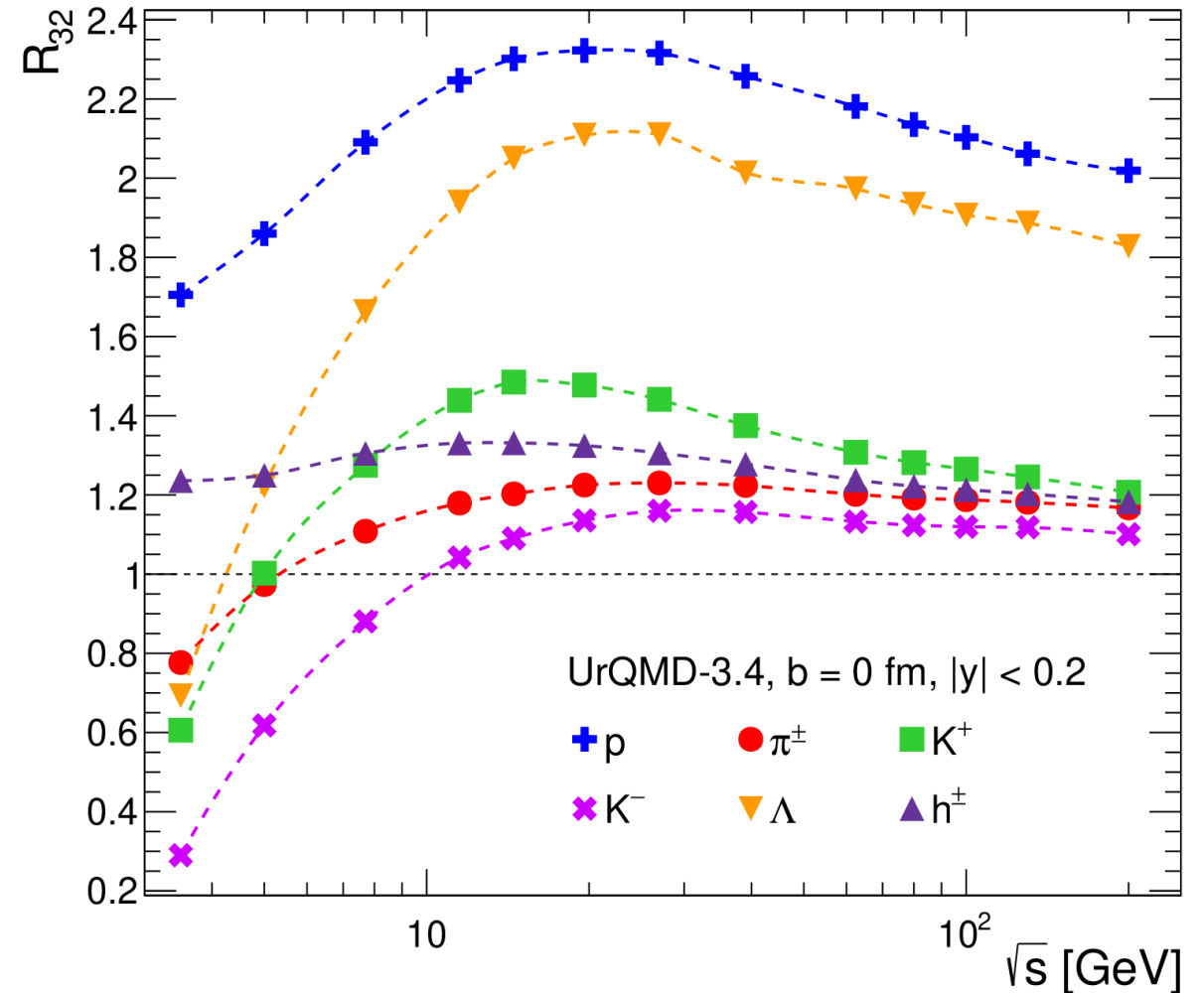
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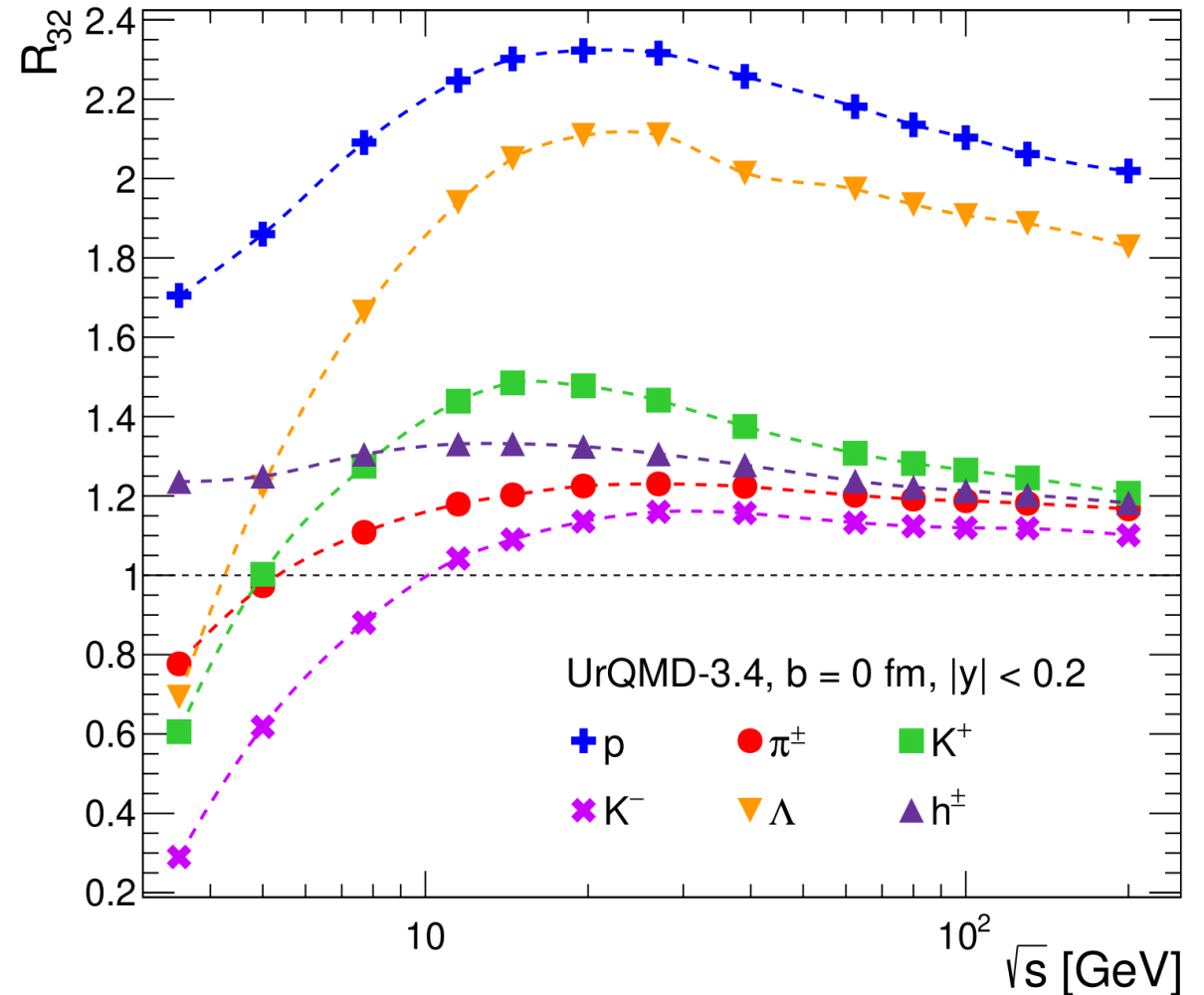


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