

Exploring Composite Higgs Models at FCC

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Motivation

- Composite models 'solve' the Hierarchy problem...
- with new scale in the multi-TeV!



multi-TeV
mountain

- What are we looking for?
 - > Precision EW + Higgs observables
 - > light composite scalars
 - > multi-TeV resonances (top partners, pNGBs, spin-1)

Composite Higgs models 101



- Symmetry broken by a condensate (of TC-fermions)
- Higgs and longitudinal Z/W emerge as mesons (pions)



Scales:

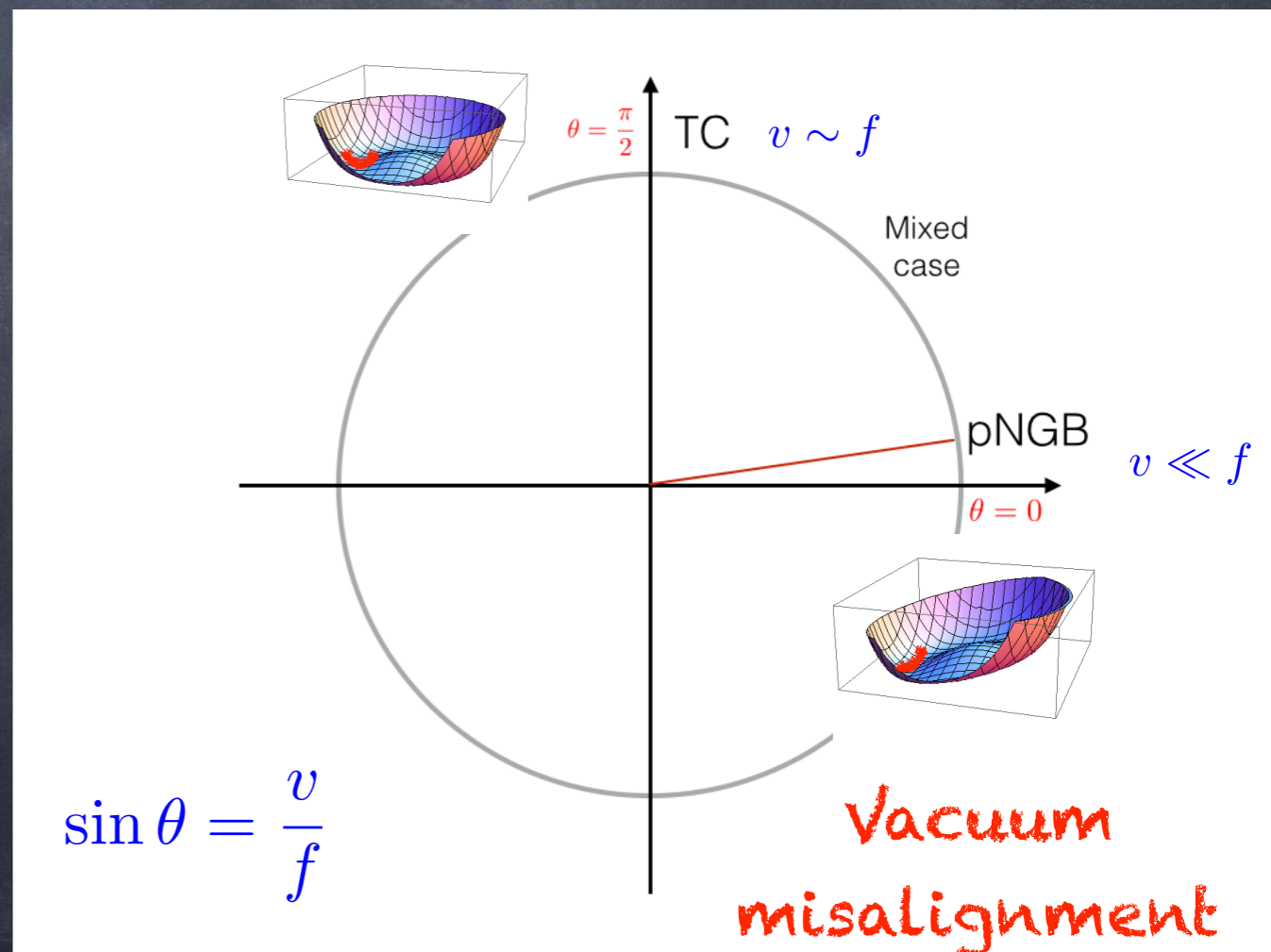
f : Higgs decay constant

v : EW scale

$$m_\rho \sim 4\pi f$$

EWPTs + Higgs coupl. limit:

$$f \gtrsim 4v \sim 1 \text{ TeV}$$



Composite Higgs models 101

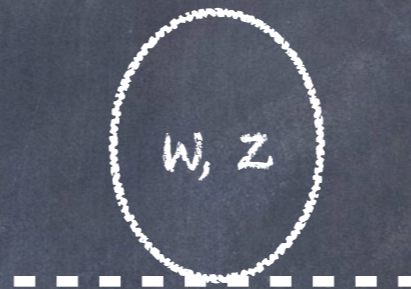


How can light states emerge?

Top Loops

Gauge Loops

TC-fermion masses



ϕ	$\sim y_t^2 f^2$	$\sim g^2 f^2$	$\sim m_\psi f$
h (h massless for vanishing v)	$\sim y_t^2 f^2 s_\theta^2 = y_t^2 v^2$	$\sim g^2 f^2 s_\theta^2 = g^2 v^2$	\times
a	\times	\times	$\sim m_\psi f$ This can be small!

The partial compositeness paradigm

Kaplan Nucl.Phys. B365 (1991) 259

$$\frac{1}{\Lambda_{\text{fl.}}^{d-1}} \mathcal{O}_H q_L^c q_R \quad \Delta m_H^2 \sim \left(\frac{4\pi f}{\Lambda_{\text{fl.}}} \right)^{d-4} f^2 \quad \text{Both irrelevant if}$$

we assume: $d_H > 1$ $d_{H^2} > 4$

Let's postulate the existence of fermionic operators:

$$\frac{1}{\Lambda_{\text{fl.}}^{d_F-5/2}} (\tilde{y}_L q_L \mathcal{F}_L + \tilde{y}_R q_R \mathcal{F}_R)$$

This dimension is not related to the Higgs!

$$f(y_L q_L Q_L + y_R q_R Q_R) \quad \text{with} \quad y_{L/R} f \sim \left(\frac{4\pi f}{\Lambda_{\text{fl.}}} \right)^{d_F-5/2} 4\pi f$$

Composite models at various scales

Planck scale

HC and SM gauge groups partially unified

Symmetry breaking by scalars

4-fermion Ops generated!

Conformal window (large scaling dimensions)

Low energy model + additional fermions

Condensation scale

Usual low energy description of composite Higgs models

Phenomenology accessible to colliders

Standard Model

10 TeV

100 GeV



Composite models at various scales



Planck scale



HC and SM gauge
partially uni



Symmetry br



Conformal
(large scaling)

10 TeV



Condensation scale

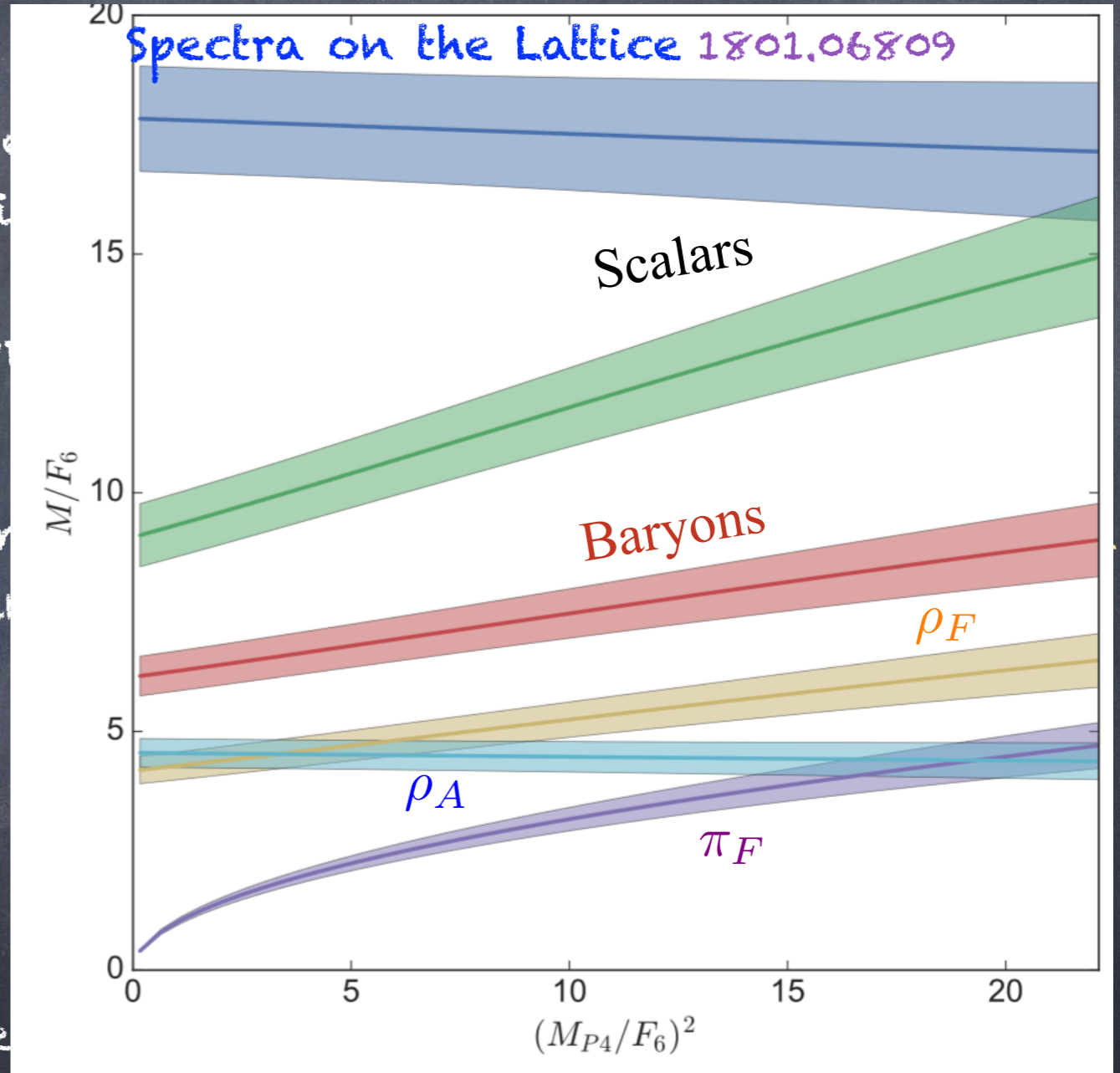


Usual low energy
of composite Higgs models



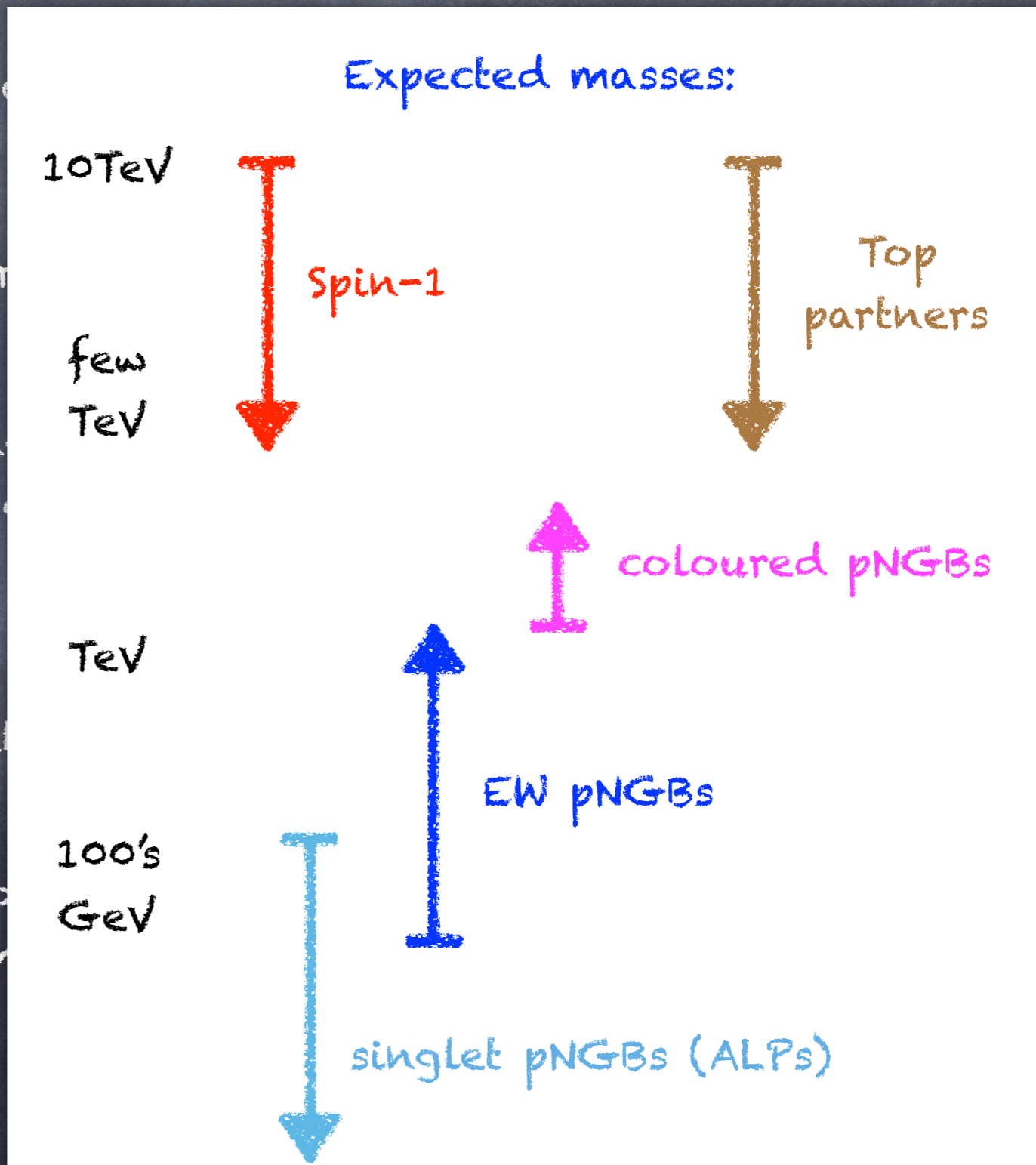
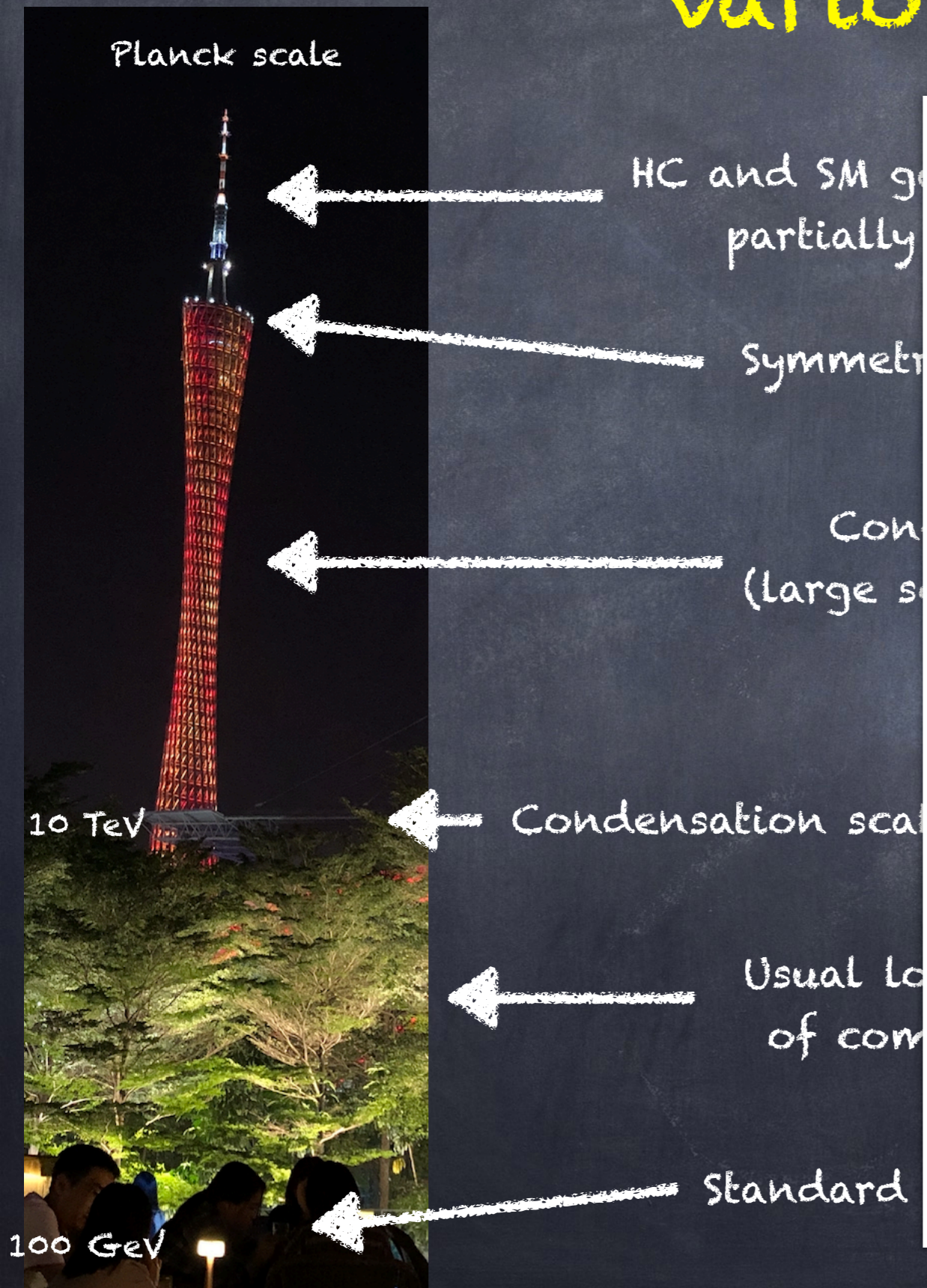
Standard Model

100 GeV



accessible
to colliders

Composite models at various scales



+ AS

The composite Higgs wilderness

- Light ALPs
- Electroweak pNGBs
- Coloured scalars (not in this talk)
- Common exotic top partner decays
- Exotic top partners
- Spin-1 resonances (not in this talk)
- What are muon anomalies trying to tell us?

The composite Higgs wilderness

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EW and Higgs precision!!!

Typical ALP Lagrangian:

$$\mathcal{L}_{\text{eff}}^{D \leq 5} = \frac{1}{2} (\partial_\mu a)(\partial^\mu a) - \frac{m_{a,0}^2}{2} a^2 + \frac{\partial^\mu a}{\Lambda} \sum_F \bar{\psi}_F \mathbf{C}_F \gamma_\mu \psi_F$$

$$+ g_s^2 C_{GG} \frac{a}{\Lambda} G_{\mu\nu}^A \tilde{G}^{\mu\nu,A} + g^2 C_{WW} \frac{a}{\Lambda} W_{\mu\nu}^A \tilde{W}^{\mu\nu,A} + g'^2 C_{BB} \frac{a}{\Lambda} B_{\mu\nu} \tilde{B}^{\mu\nu},$$

Composite Higgs scenario:

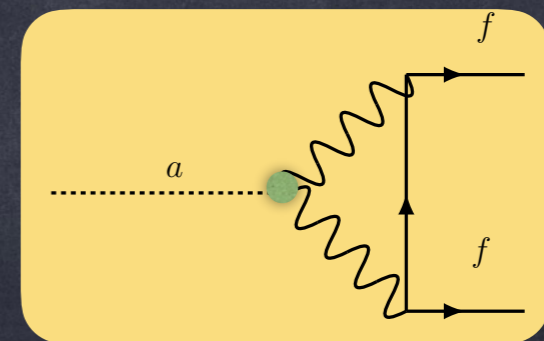
$$\frac{C_{WW}}{\Lambda} \sim \frac{C_{BB}}{\Lambda} \sim \frac{N_{\text{TC}}}{64\sqrt{2} \pi^2 f} \quad \frac{C_{GG}}{\Lambda} = 0$$

(Poor bounds at the LHC)

$$(C_{\gamma\gamma} = C_{WW} + C_{BB})$$

C_F is loop-induced:

M.Bauer et al, 1708.00443



Typical ALP Lagrangian:

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Composite Higgs scenario:

$$\frac{C_{WW}}{\Lambda} \sim \frac{C_{BB}}{\Lambda} \sim \frac{N_{\text{TC}}}{64\sqrt{2} \pi^2 f}$$

Free parameters:

$$(C_{\gamma\gamma} = C_{WW} + C_{BB})$$

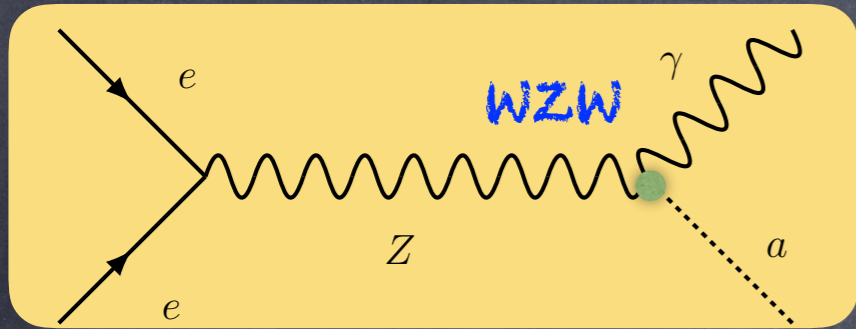
We will consider two scenarios:
Photo-philic and
Photo-phobic



f, m_a

Tera-Z portal to compositeness (via ALPs)

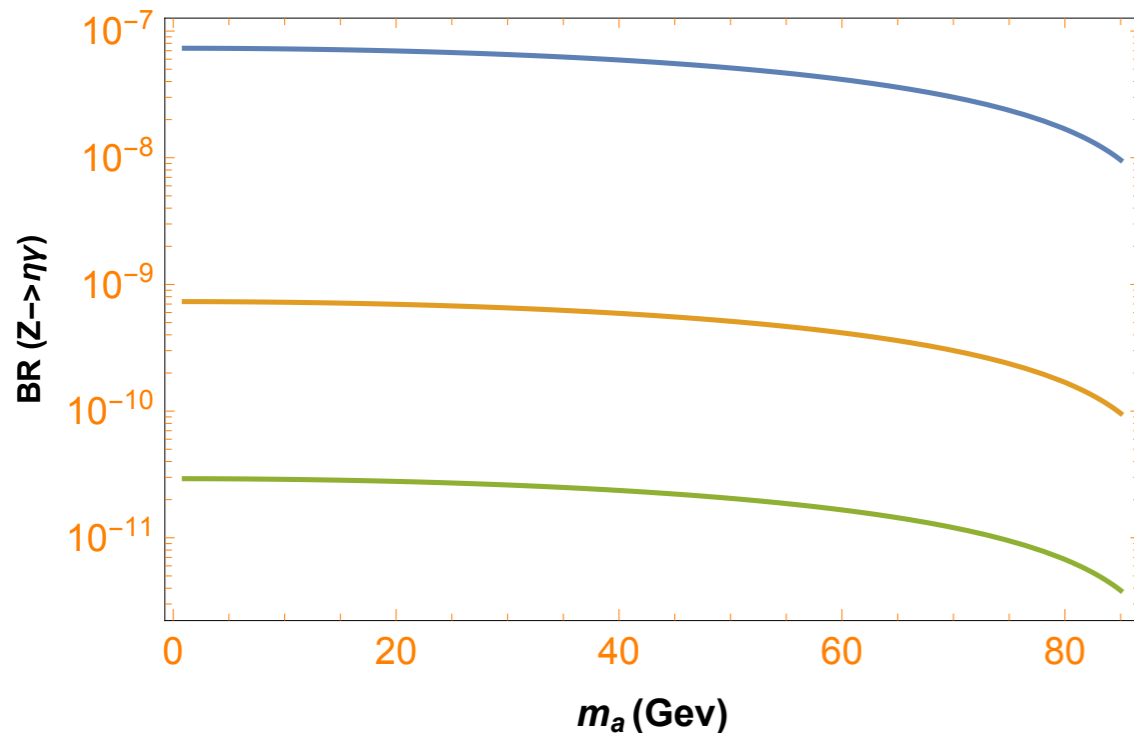
G. Cacciapaglia et al.
2104.11064



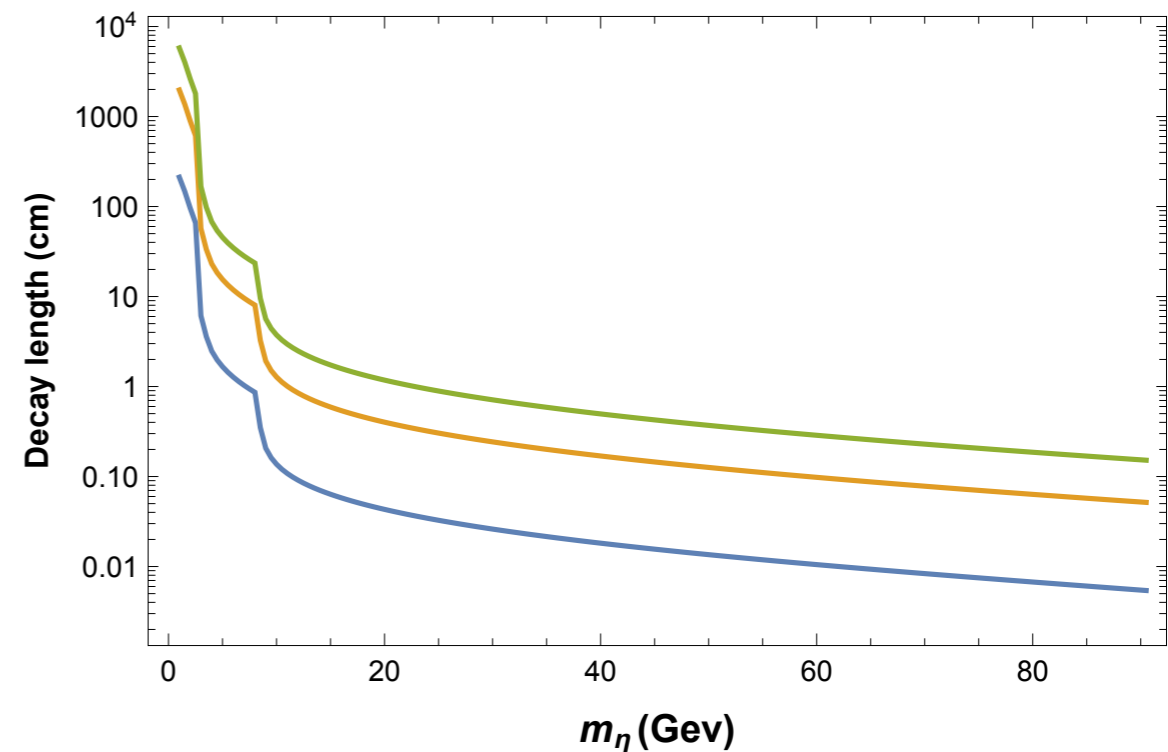
This process is always associated with a monochromatic photon.

Tera Z phase of FCC-ee will lead to 5-6 10^{12} Z bosons at the end of the run.

Ideal test for rare Z decays!!



— $f = 1$ TeV
— $f = 10$ TeV
— $f = 50$ TeV

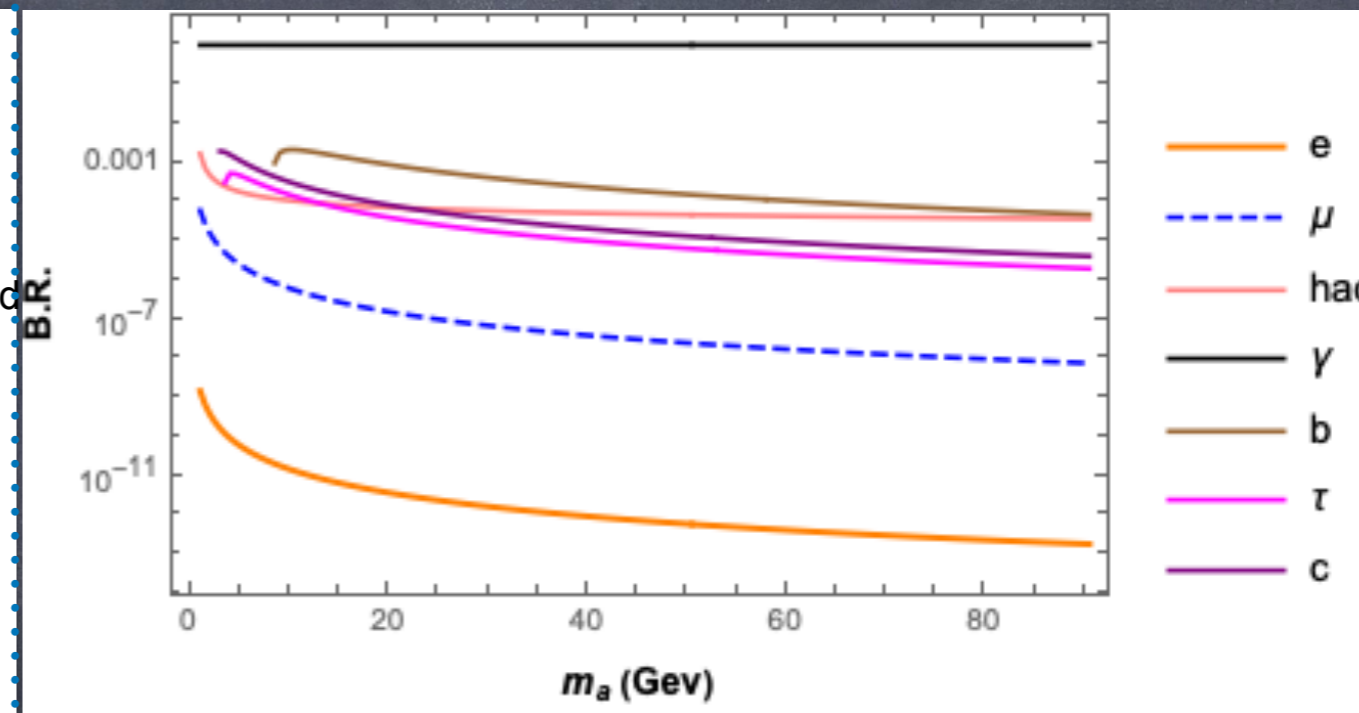
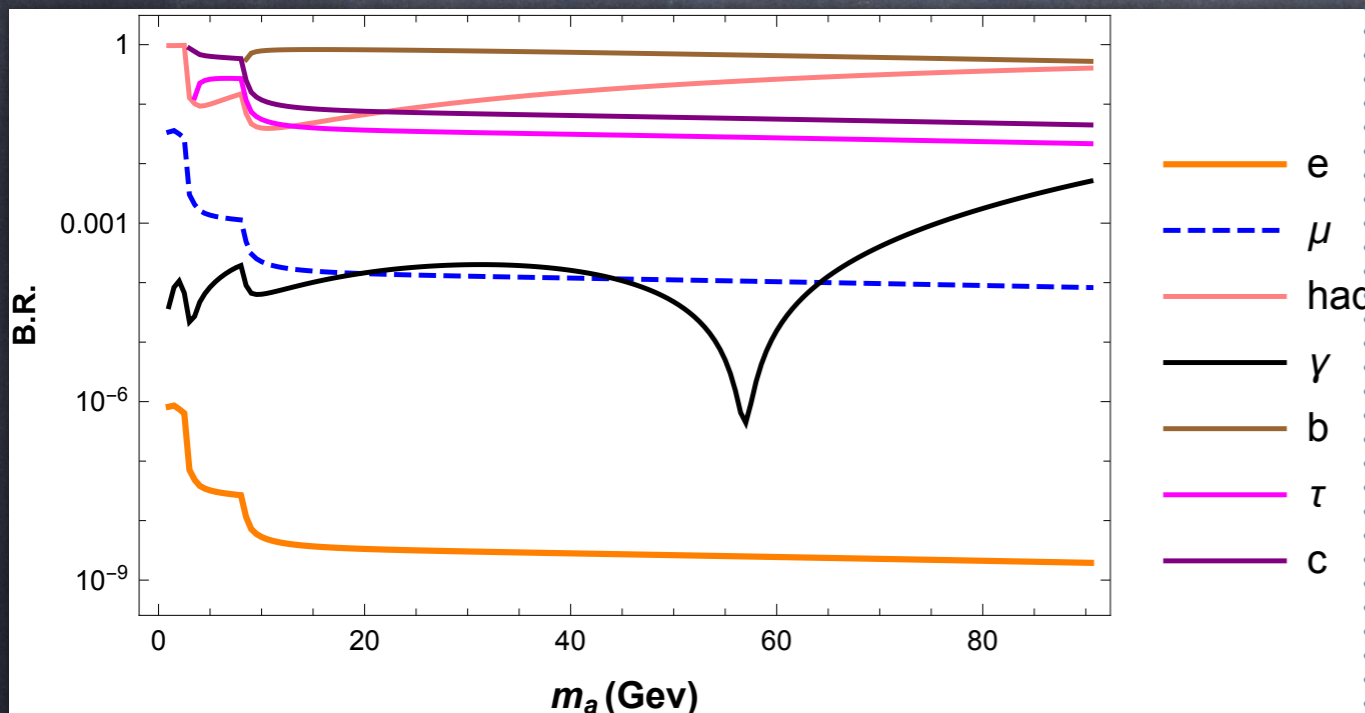


Tera-Z portal to compositeness (via ALPs)

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2104.11064

Photo-phobic

Photo-philic



No leading order coupling to
Photons (WZW interaction is Zero!!)

eg. $SU(4)/SP(4)$,
 $SU(4) \times SU(4)/SU(4)$

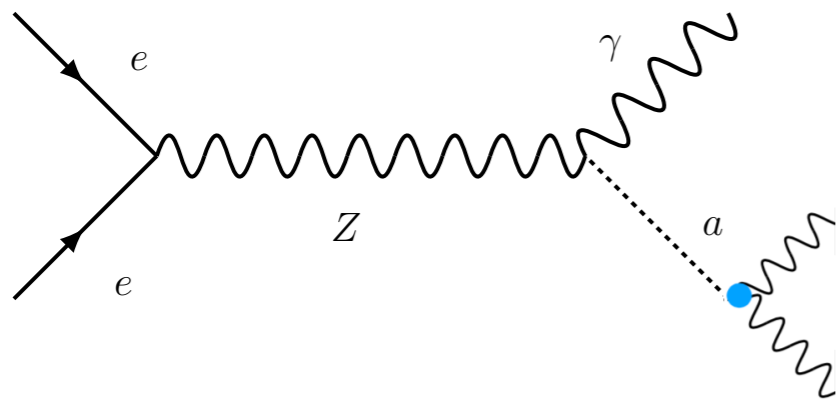
WZW interaction to photons
(Like the pion)

eg. $SU(5)/SO(5)$,
 $SU(6)/SO(6)$

Phenomenology-Prompt Decays

Photo-philic

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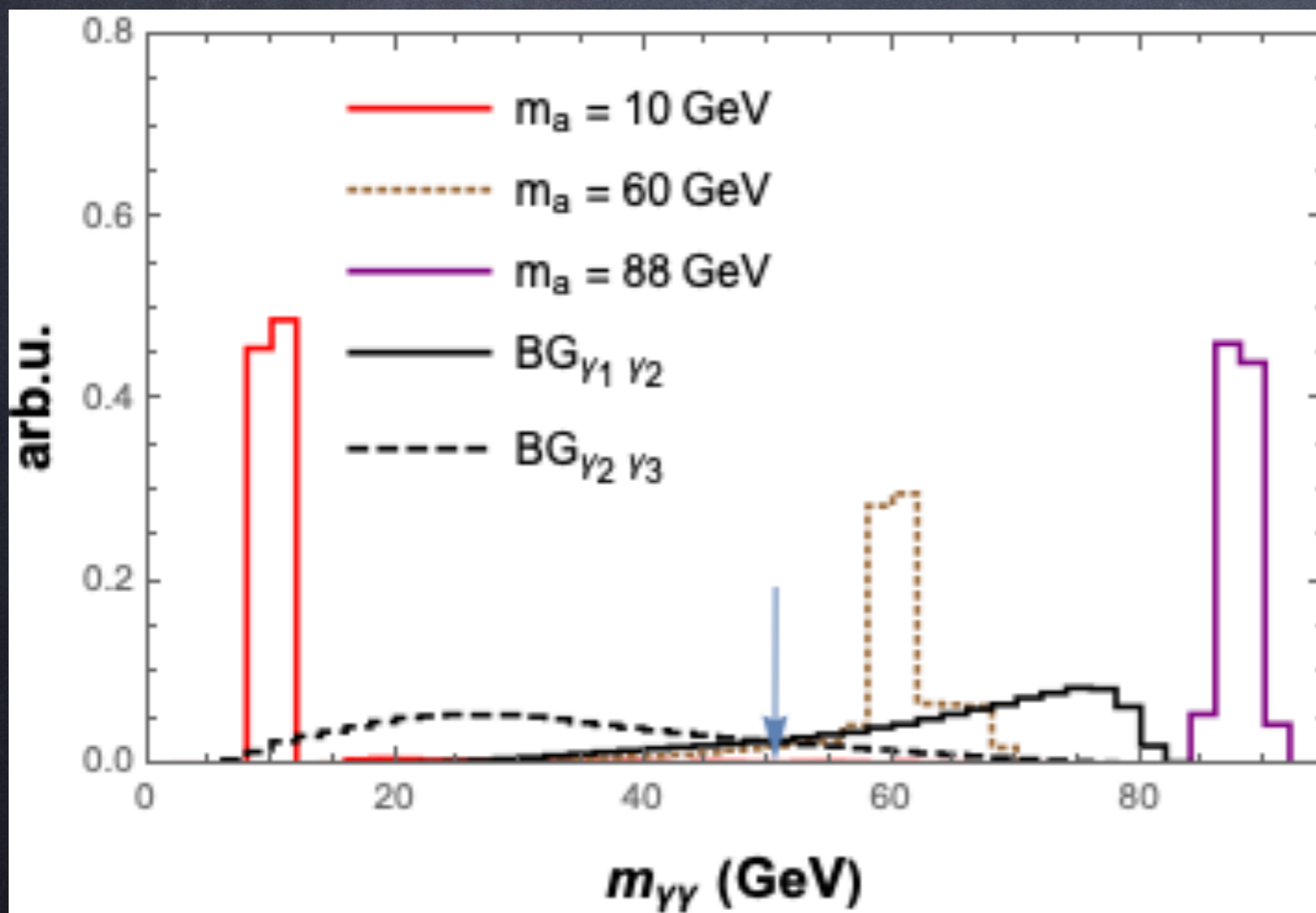
- Three isolated photons

$$BR(Z \rightarrow 3\gamma)_{\text{LEP}} < 2.2 \cdot 10^{-6}$$

Discriminating variable:
invariant mass

Photon ordering changes
at inv. mass 50 GeV

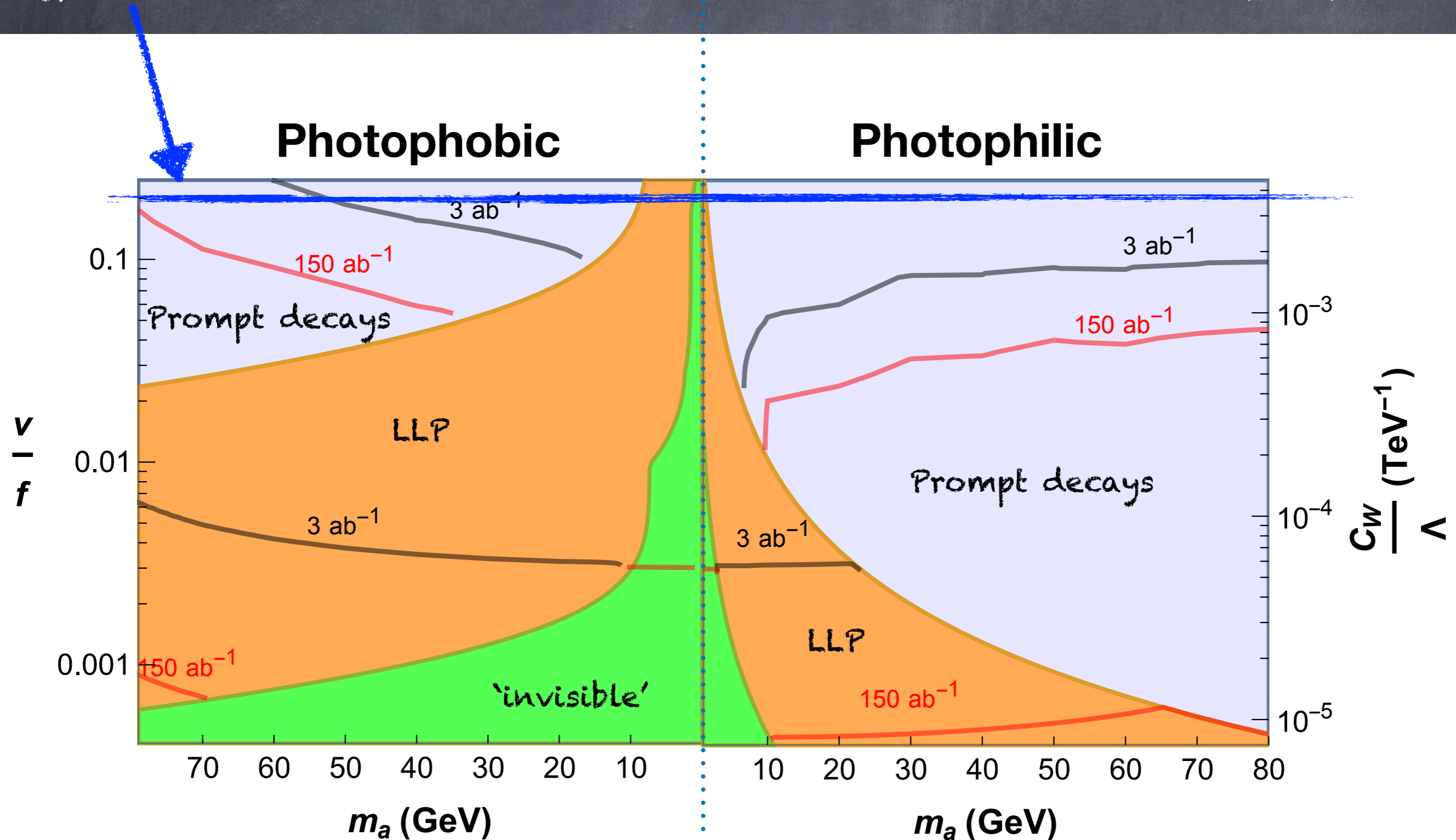
Bins above 80 GeV
populated by fakes:
hard to estimate!



Money plot

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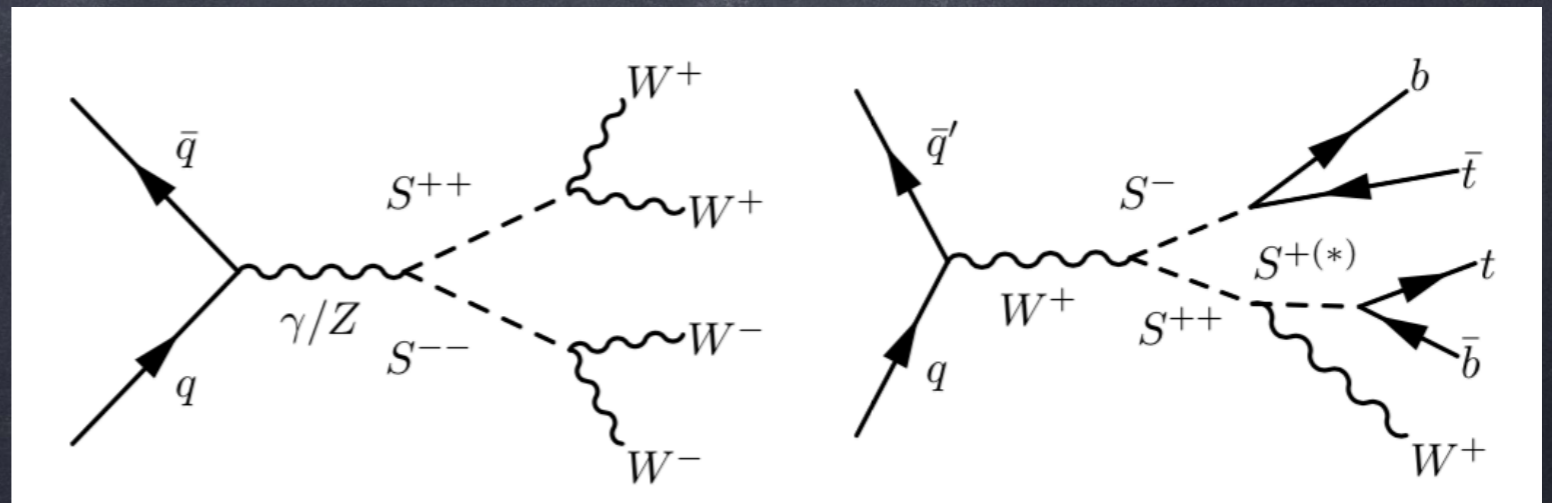
Typical EWPT bound



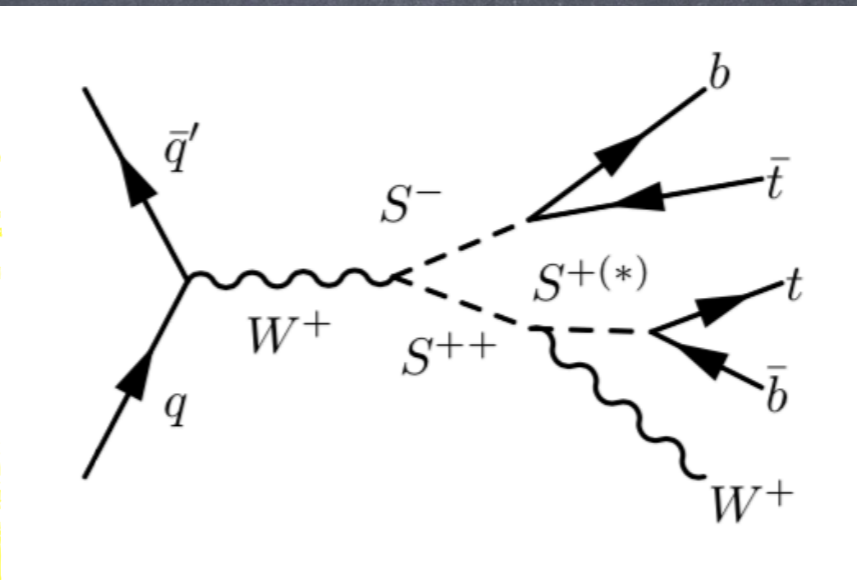
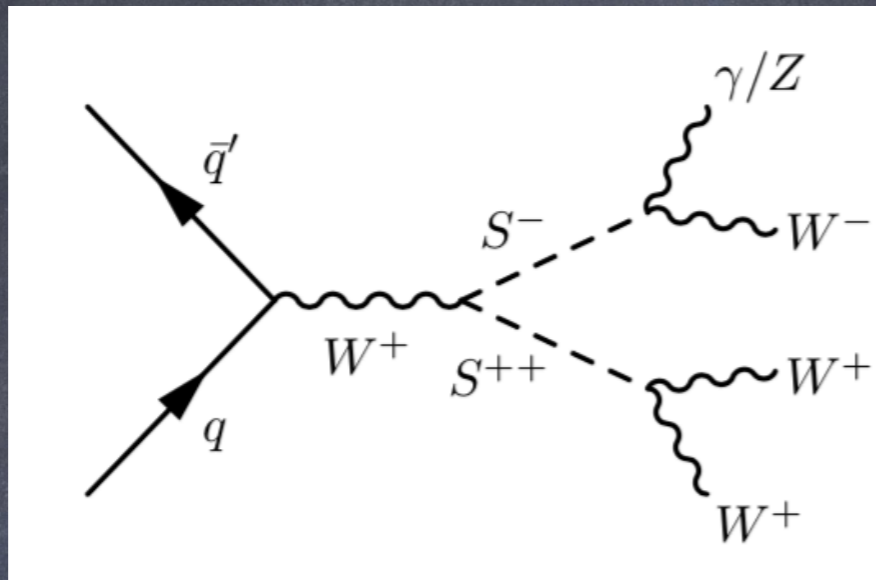
EW pNGB direct production

W.Porod et al.
work in progress

- Dominantly pair-produced (no VEVs except for the doublet)
- Couplings to two EW gauge bosons via WZW
- Couplings to two fermions via partial compositeness
- Few dedicated direct searches (WWWW and WWWZ via doubly-charged scalar)



EW pNGB direct production

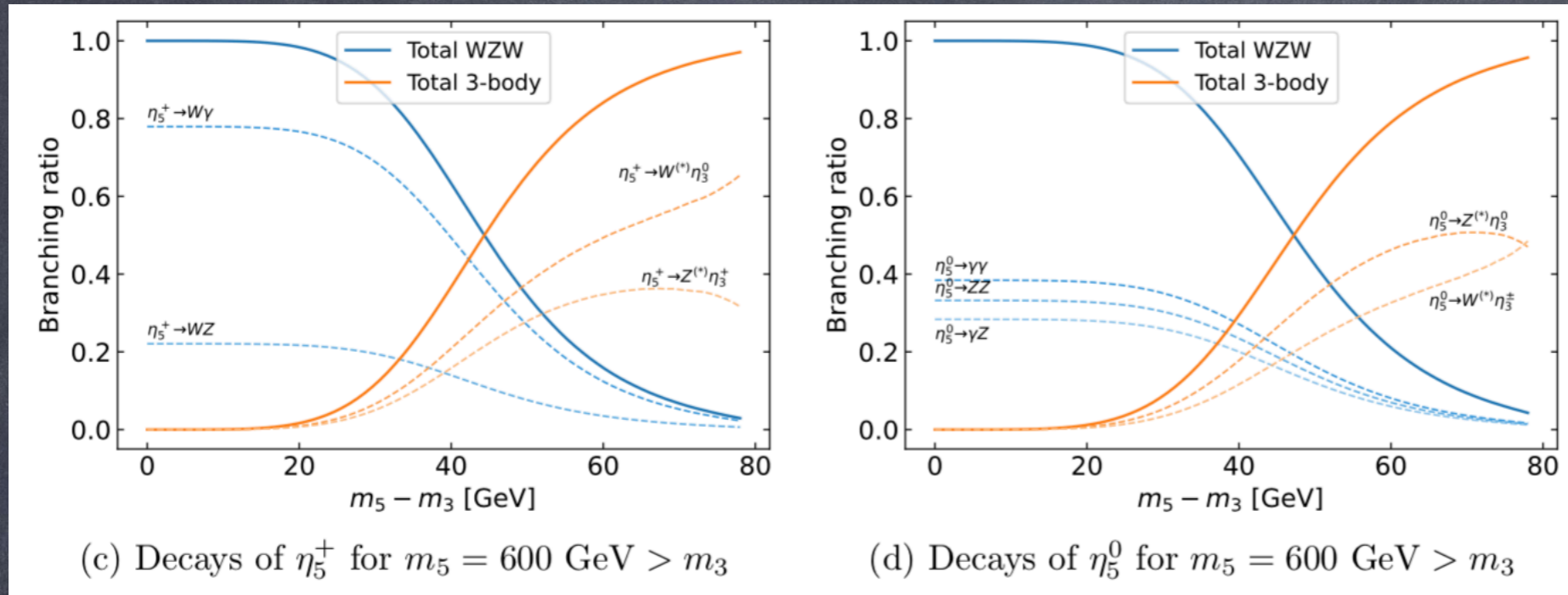


Porod et al.
work in progress

- Decays to two GBs from WZW anomaly
- Small couplings
- Cascade decays can be competitive
- Photon-rich final states!

- Typically sizeable couplings to top and bottom
- Always dominate if present!
- They may be absent - model dependence!

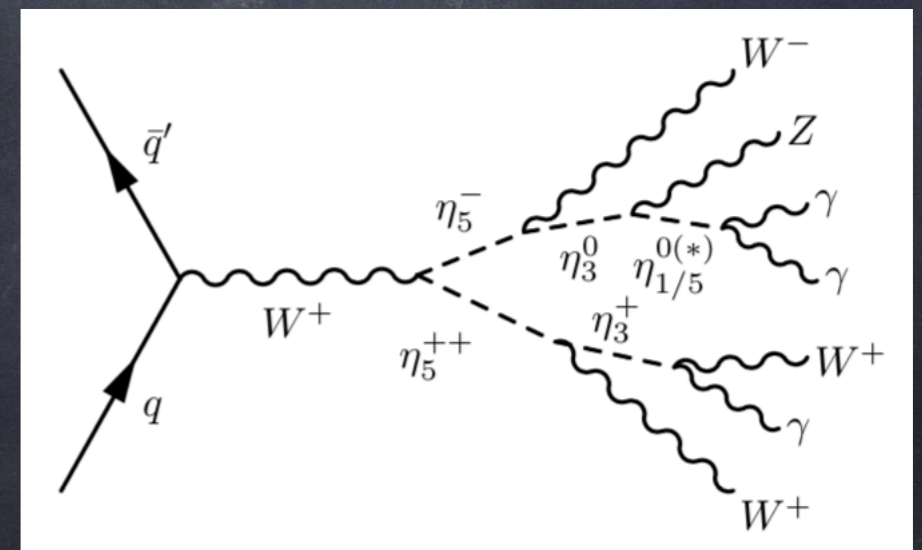
Fermio-phobic SU(5)/SO(5) model



W.Porod et al.
work in progress

- Decays to two GBs from WZW anomaly
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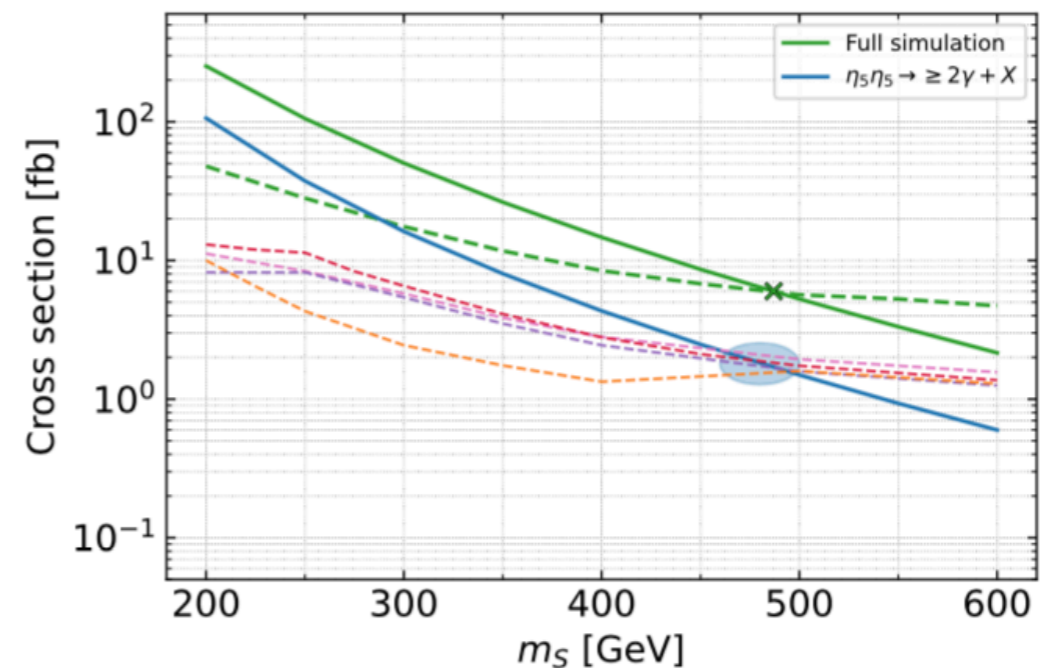
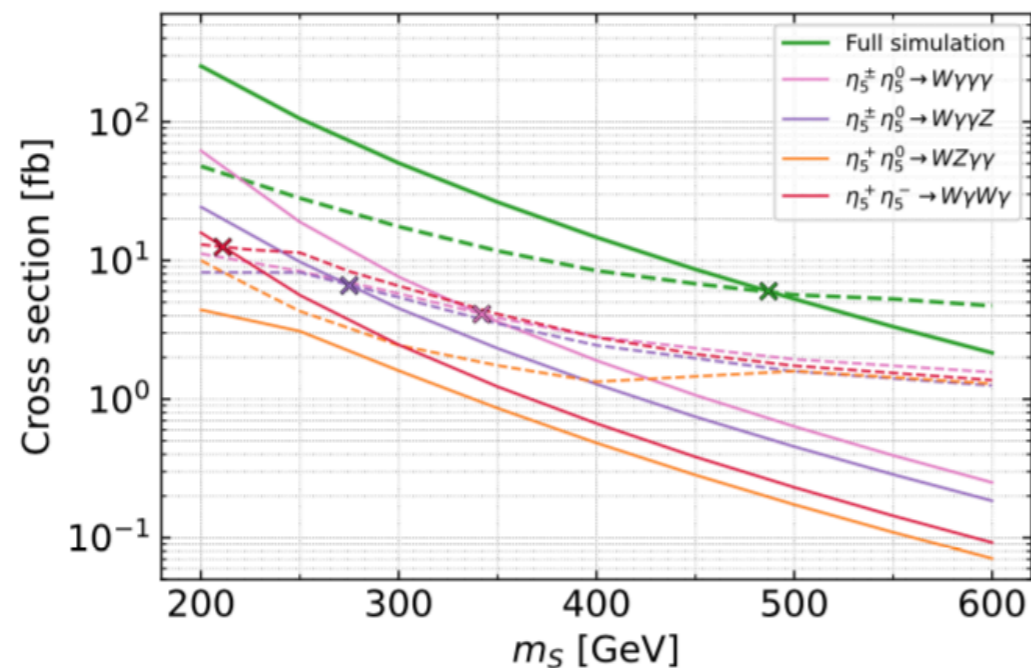
Cascade decays competitive for mass splits around 50 GeV



SU(5)/SO(5) benchmark

W. Porod et al.
work in progress

- Run all searches in MadAnalysis, Checkmate and Contur on all di-scalar pair production channels.
- Best limits from multi-photon searches (ATLAS generic analysis)
- Many channels contribute to the same signal region!



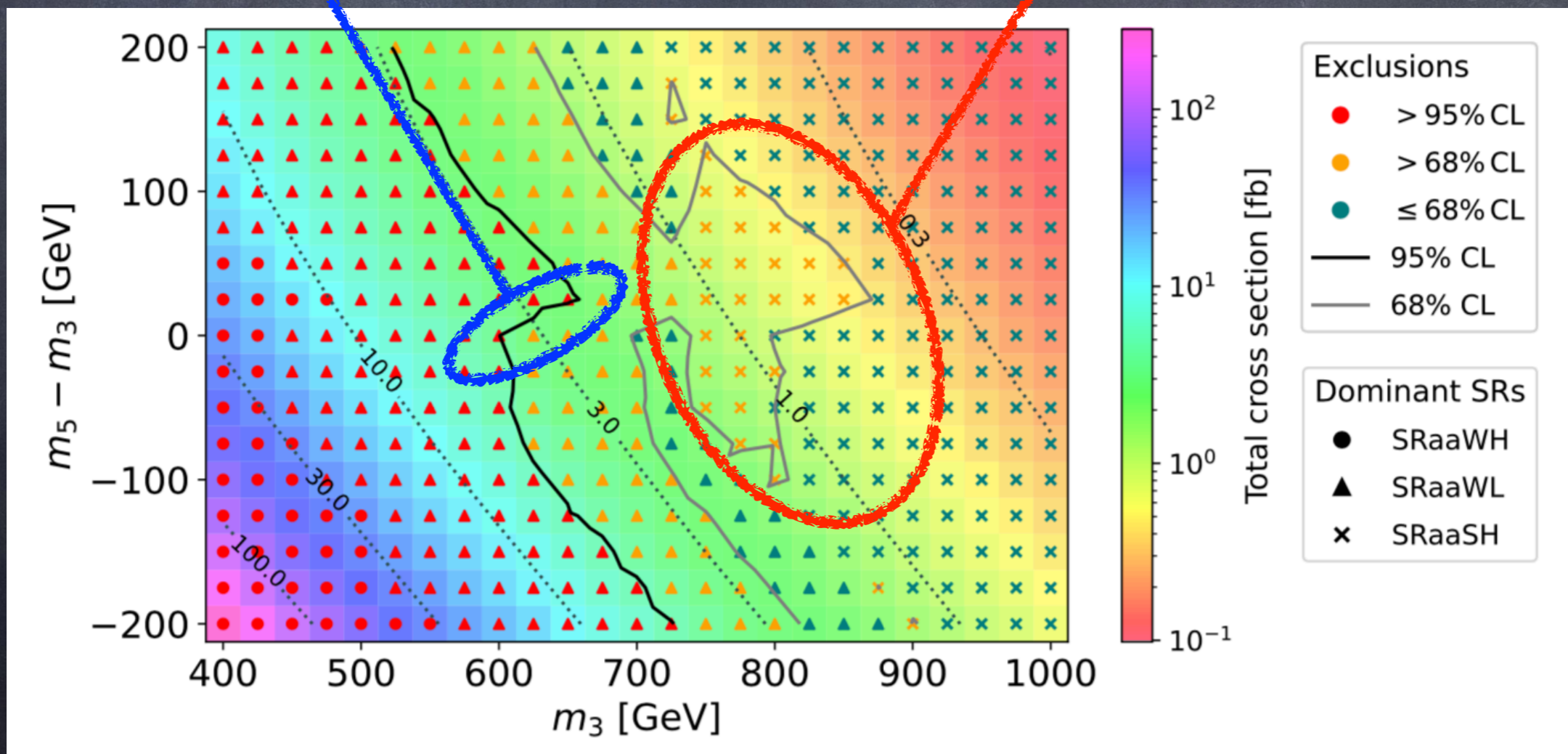
SU(5)/SO(5) benchmark

W. Porod et al.
work in progress

Exclusion from multi-photon search

S_{++} cascade decays

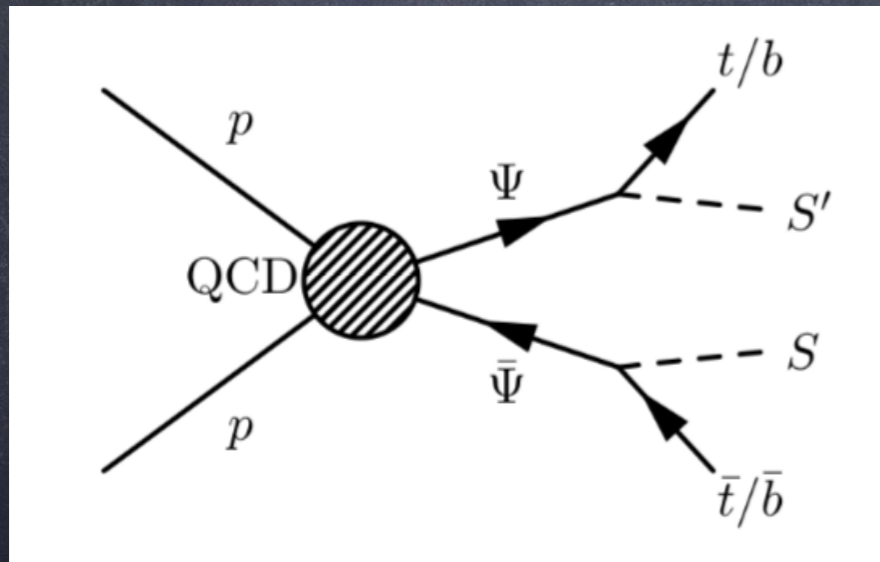
Change in dominant SR



Top partner pheno revisited

A. Banerjee et al
2203.0727 (Snowmass LOI)

- pNGBs lighter than the top partners are to be expected in all composite models



The S decays are model-dependent, but they can be classified:

$$S_i^{++} \rightarrow W^+W^+$$

$$S_i^+ \rightarrow W^+\gamma, W^+Z$$

$$S_i^0 \rightarrow W^+W^-, \gamma\gamma, \gamma Z, ZZ.$$

Calculable ratios (from anomalies) and always present for all models.

$$S^{++} \rightarrow W^+t\bar{b},$$

$$S^+ \rightarrow t\bar{b},$$

$$S^0 \rightarrow t\bar{t}, b\bar{b}.$$

Dominant, if present for the specific S .

Common exotic top partner decays

$$\begin{aligned} \mathcal{L}_{\Psi fV} = & \frac{e}{\sqrt{2}s_W} \kappa_{T,L}^W \bar{T} W^+ P_L b + \frac{e}{2c_W s_W} \kappa_{T,L}^Z \bar{T} Z P_L t + \frac{e}{\sqrt{2}s_W} \kappa_{B,L}^W \bar{B} W^- P_L t \\ & + \frac{e}{2c_W s_W} \kappa_{B,L}^Z \bar{B} Z P_L b + \frac{e}{\sqrt{2}s_W} \kappa_{X,L}^W \bar{X} W^+ P_L t + L \leftrightarrow R + \text{h.c.} \end{aligned} \quad (14)$$

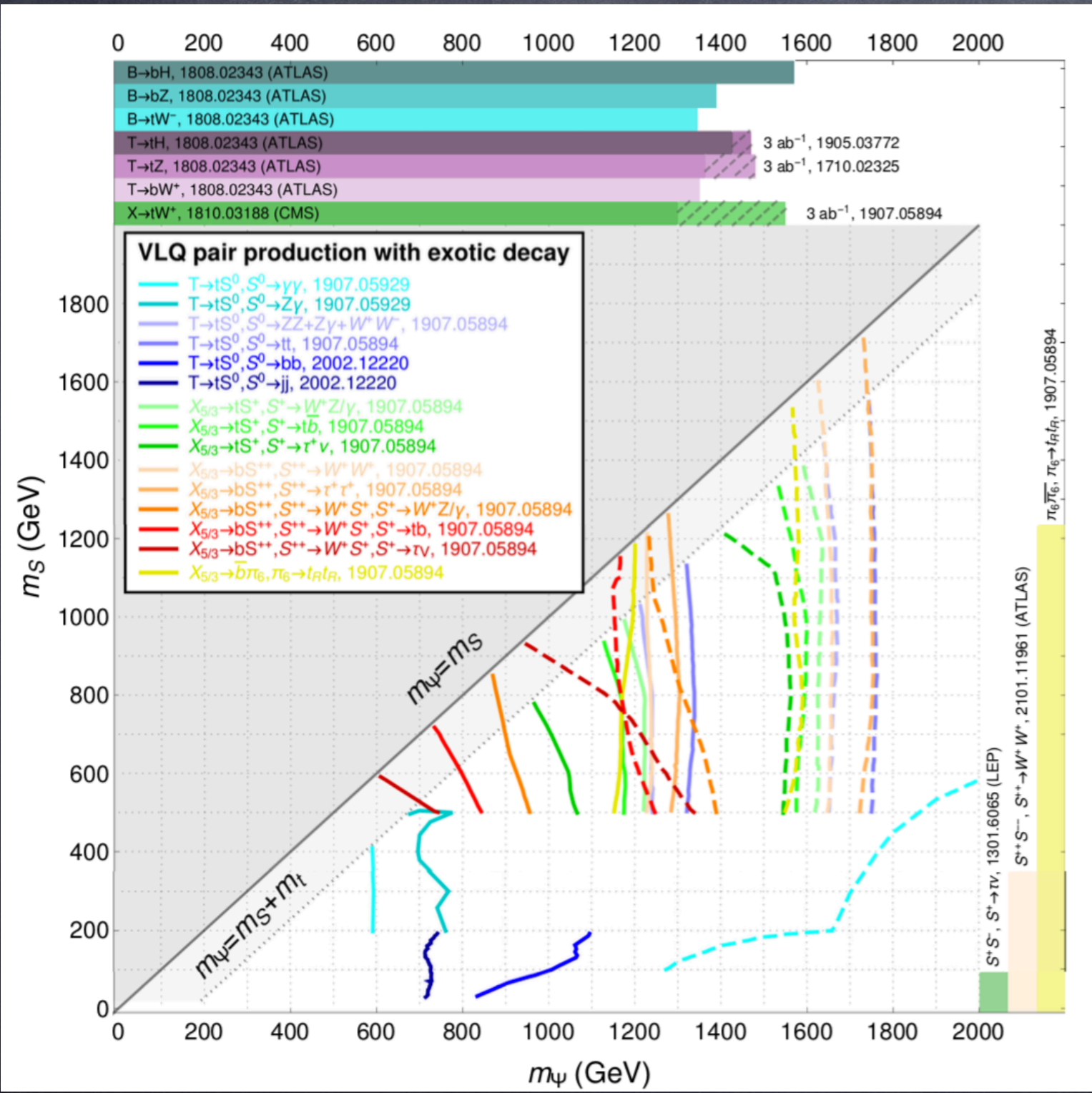
$$\begin{aligned} \mathcal{L}_{\Psi fS} = & \sum_i S_i^+ \left[\kappa_{T,L}^{S_i^+} \bar{T} P_L b + \kappa_{X,L}^{S_i^+} \bar{X} P_L t + L \leftrightarrow R \right] + \text{h.c.} + \sum_i S_i^- \left[\kappa_{B,L}^{S_i^-} \bar{B} P_L t + L \leftrightarrow R \right] + \text{h.c.} \\ & + \sum_i S_i^0 \left[\kappa_{T,L}^{S_i^0} \bar{T} P_L t + \kappa_{B,L}^{S_i^0} \bar{B} P_L b + L \leftrightarrow R \right] + \text{h.c.} \\ & + \sum_i S_i^{++} \left[\kappa_{X,L}^{S_i^{++}} \bar{X} P_L b + L \leftrightarrow R \right] + \text{h.c.} \end{aligned} \quad (15)$$

- Possible to write a Master-Lagrangian containing all possible couplings, implemented at NLO in MG (FSMOG)

Work in progress by A. Deandrea and B. Fuks

Common exotic top partner decays

A. Banerjee et al
2203.0727 (Snowmass LOI)



- Dedicated searches may be useful to push up the limits.
- Projections for FCC-hh are needed..
- in combination with scalar direct production.

Exotic top partners

G.Cacciapaglia et al.
2112.00019

- A specific model: MS of Ferretti's classification

Underlying fermions (like quarks)

	Sp(2N _c)	SU(3) _c	SU(2) _L	U(1) _Y	SU(5)	SU(6)	U(1)
ψ _{1,2}	\square	1	2	1/2	5	1	$-\frac{3q_\chi}{5(N_c-1)}$
ψ _{3,4}	\square	1	2	-1/2			
ψ ₅	\square	1	1	0			
χ ₁	\square	3	1	-x	1	6	q _χ
χ ₂							
χ ₃							
χ ₄	\square	$\bar{3}$	1	x			
χ ₅							
χ ₆							

Baryons (top partners)

	SU(5) × SU(6)	SO(5) × Sp(6)	names
ψχχ	(5, 15)	(5, 14)	B ₁₄ ¹
		+(5, 1)	B ₁ ¹
	(5, 21)	(5, 21)	B ₂₁ ¹
ψχ̄χ̄	(5, $\bar{15}$)	(5, 14)	B ₁₄ ²
		+(5, 1)	B ₁ ²
	(5, $\bar{21}$)	(5, 21)	B ₂₁ ²
ψ̄χ̄χ	($\bar{5}$, 35)	(5, 14)	B ₁₄ ³
		+(5, 21)	B ₂₁ ³
	($\bar{5}$, 1)	(5, 1)	B ₁ ³

$$14 \rightarrow 8_0 + 3_{-2x} + \bar{3}_{2x},$$

$$21 \rightarrow 8_0 + 6_{2x} + \bar{6}_{-2x} + 1_0$$

Exotic top partners

G.Cacciapaglia et al.
2112.00019

- A specific model: MS of Ferretti's classification

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χ_1					1	6	q_χ
χ_2	\square	3	1	$-x$			
χ_3							
χ_4							
χ_5	\square	$\bar{\mathbf{3}}$	1	x			
χ_6							

Baryons (top partners)

	$SU(5) \times SU(6)$	$SO(5) \times Sp(6)$	names
$\psi\chi\chi$	(5, 15)	(5, 14)	\mathcal{B}_{14}^1
		+(5, 1)	\mathcal{B}_1^1
	(5, 21)	(5, 21)	\mathcal{B}_{21}^1
$\psi\bar{\chi}\bar{\chi}$	(5, $\bar{15}$)	(5, 14)	\mathcal{B}_{14}^2
		+(5, 1)	\mathcal{B}_1^2
	(5, $\bar{21}$)	(5, 21)	\mathcal{B}_{21}^2
$\bar{\psi}\bar{\chi}\chi$	($\bar{5}$, 35)	(5, 14)	\mathcal{B}_{14}^3
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Exotic top partners

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ψ_5	\square	1	1	0			
χ_1	\square	3	1	$-x$	1	6	q_χ
χ_2							
χ_3							
χ_4	$\bar{3}$	1	x				
χ_5							
χ_6							

Baryons (top partners)

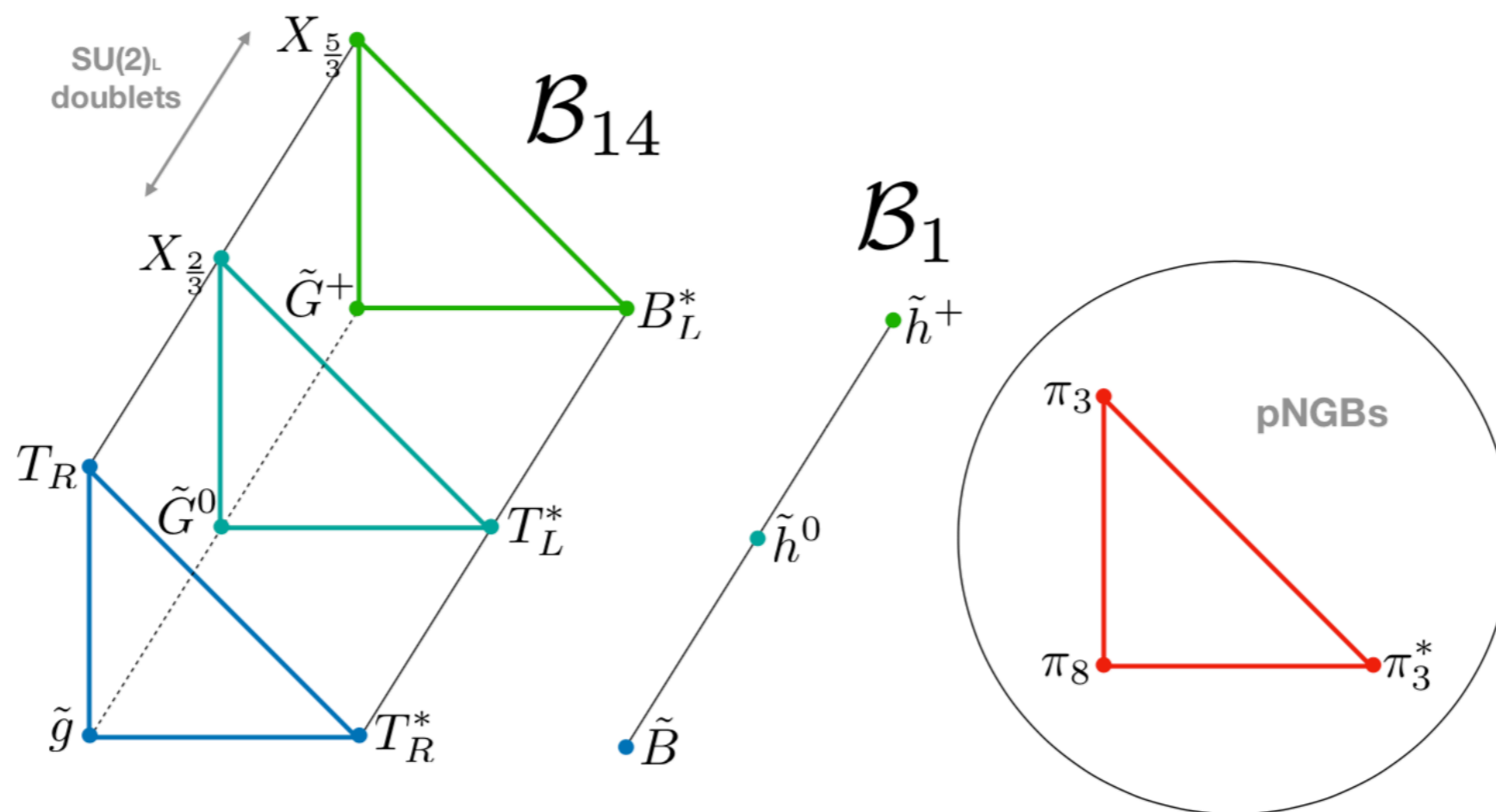
	$SU(5) \times SU(6)$	$SO(5) \times Sp(6)$	names
$\psi\chi\chi$	(5, 15)	(5, 14)	\mathcal{B}_{14}^1
		+(5, 1)	\mathcal{B}_1^1
	(5, 21)	(5, 21)	\mathcal{B}_{21}^1
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$\bar{\psi}\bar{\chi}\bar{\chi}$	($\bar{5}$, 35)	(5, 14)	\mathcal{B}_{14}^3
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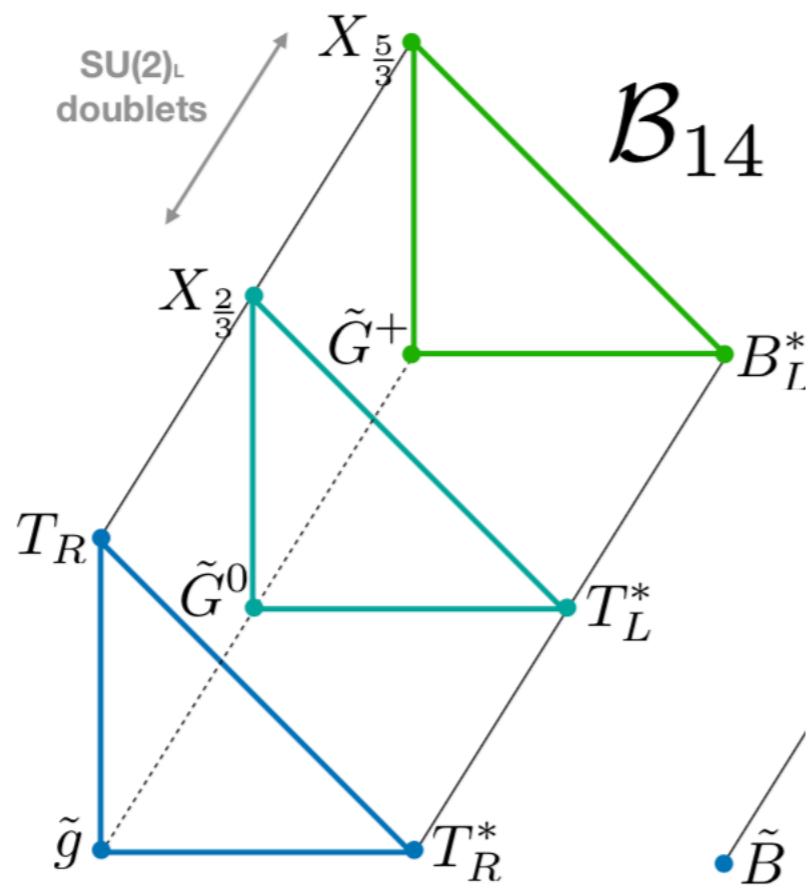
Exotic top partners

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2112.00019



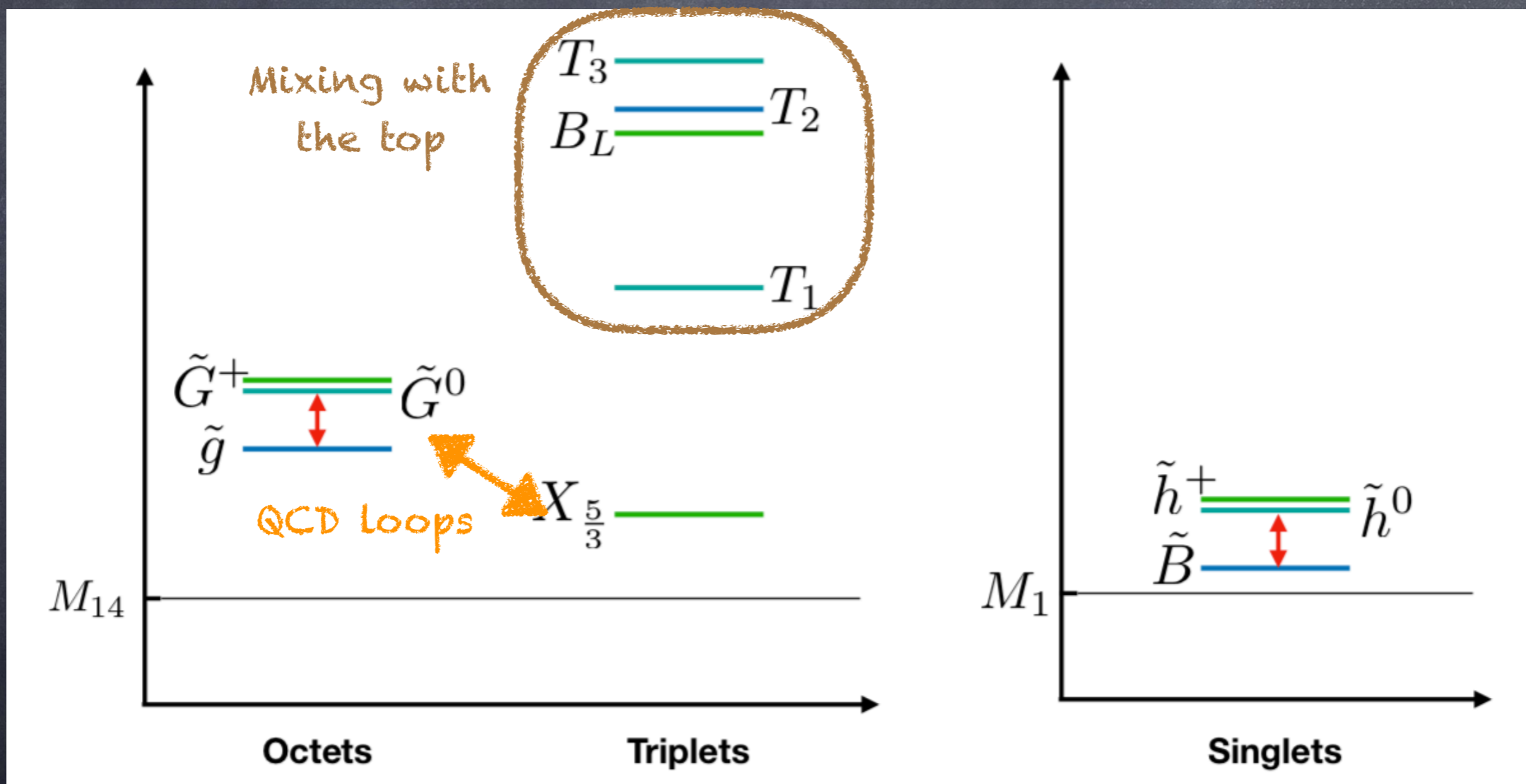
Exotic top partners

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2112.00019



Exotic top partners

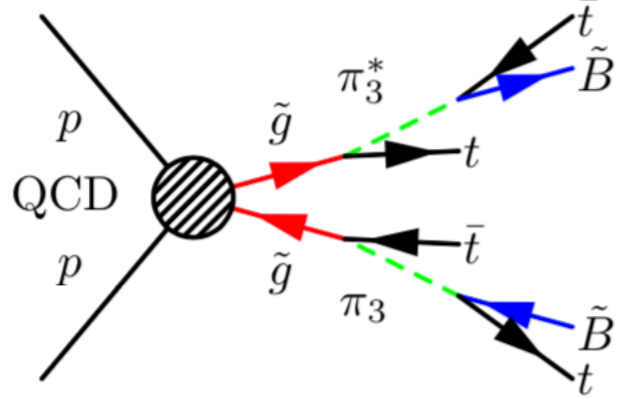
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2112.00019



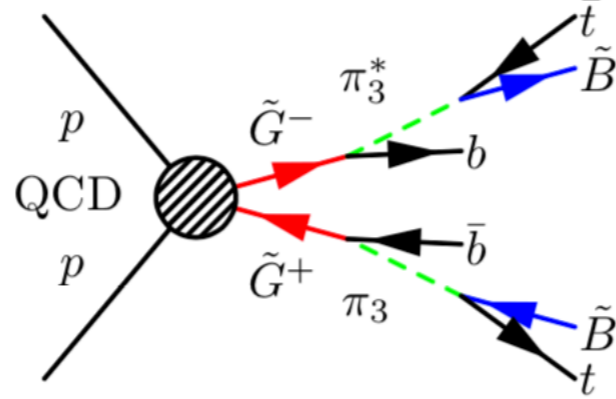
Octoni bounds

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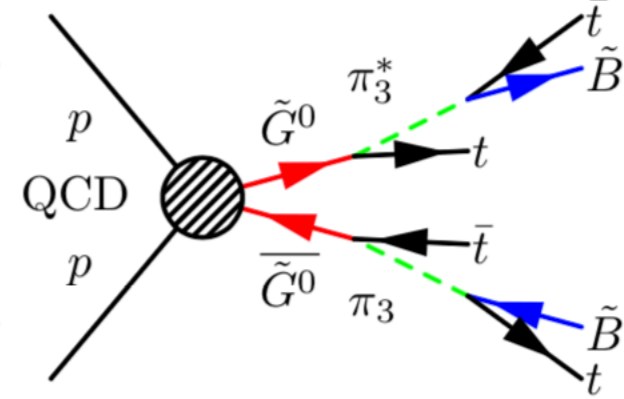
- Model implemented in MG.
- Check limits from searches in MadAnalysis and CheckMate.
- Strongest bound from gluino and stop searches!



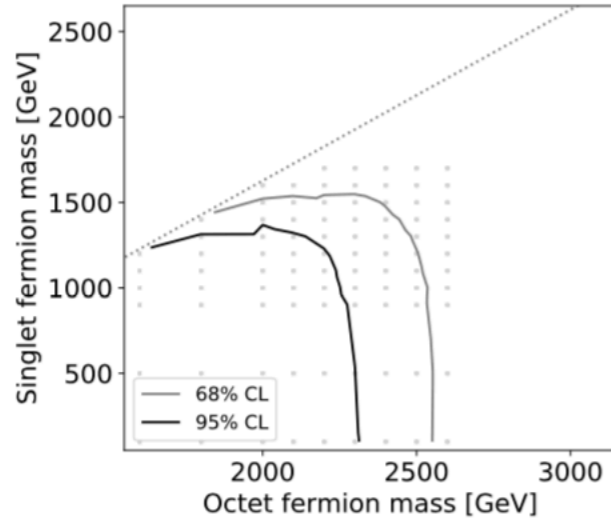
(a) $\tilde{g} \rightarrow \bar{t}\pi_3, t\pi_3^* \rightarrow \bar{t}t\tilde{B}$



(b) $\tilde{G}^+ \rightarrow \bar{b}\pi_3 \rightarrow \bar{b}t\tilde{B}$

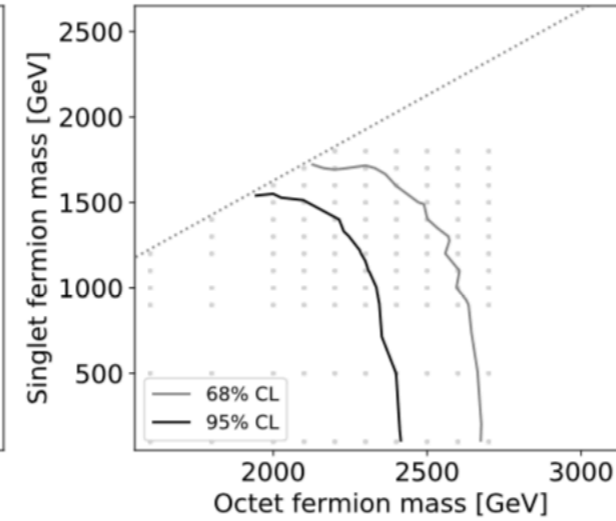


(c) $\tilde{G}^0 \rightarrow \bar{t}\pi_3 \rightarrow \bar{t}t\tilde{B}$



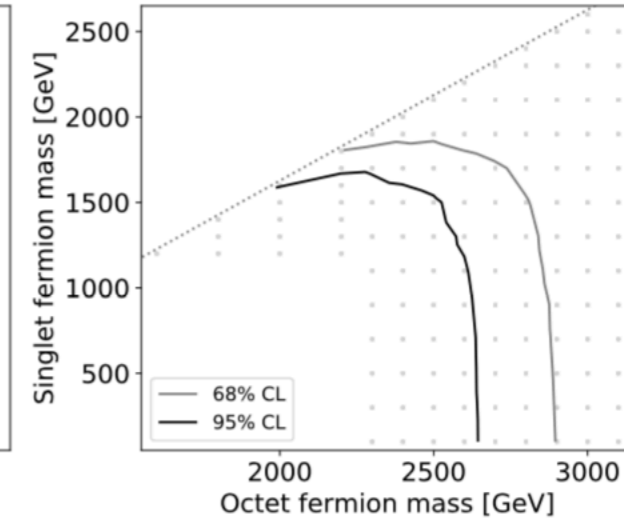
(a) $\tilde{g} \rightarrow \bar{t}\pi_3, t\pi_3^* \rightarrow \bar{t}t\tilde{B}$,

$$m_{\tilde{g}} - m_{\pi_3} = 200 \text{ GeV}$$



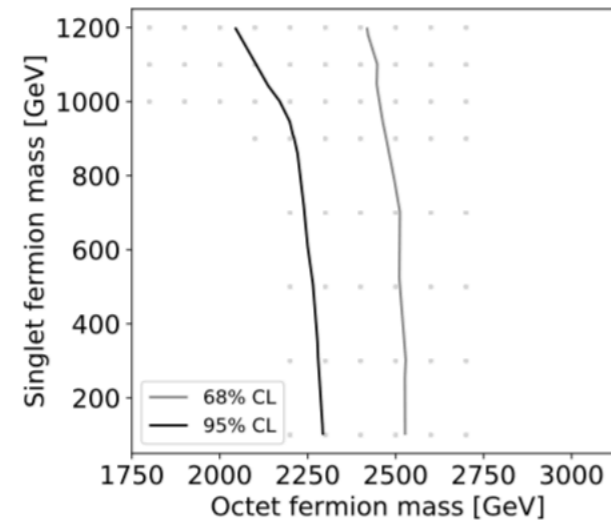
(b) $\tilde{G}^+ \rightarrow \bar{b}\pi_3 \rightarrow \bar{b}t\tilde{B}$,

$$m_{\tilde{G}^+} - m_{\pi_3} = 200 \text{ GeV}$$



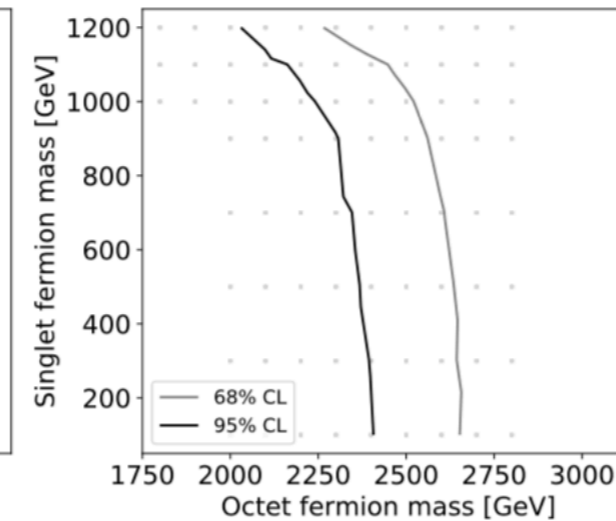
(c) $Q_8 \rightarrow \bar{q}\pi_3 \rightarrow \bar{q}t\tilde{B}$,

$$m_{Q_8} - m_{\pi_3} = 200 \text{ GeV}$$



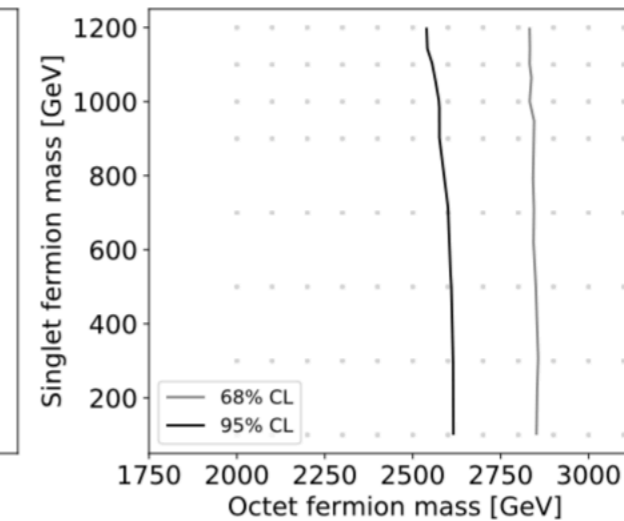
(d) $\tilde{g} \rightarrow \bar{t}\pi_3, t\pi_3^* \rightarrow \bar{t}t\tilde{B}$,

$$m_{\pi_3} = 1.4 \text{ TeV}$$



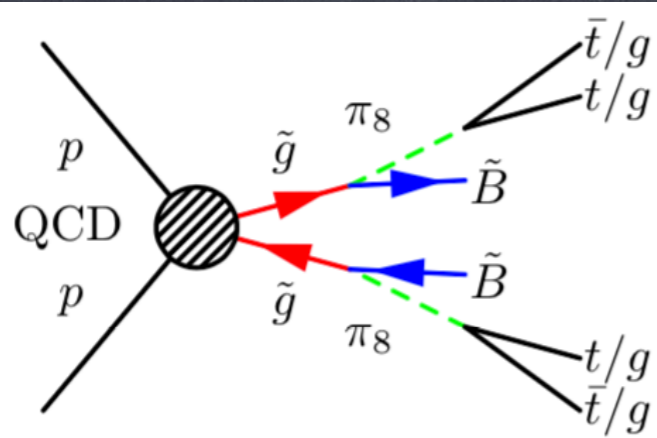
(e) $\tilde{G}^+ \rightarrow \bar{b}\pi_3 \rightarrow \bar{b}t\tilde{B}$,

$$m_{\pi_3} = 1.4 \text{ TeV}$$

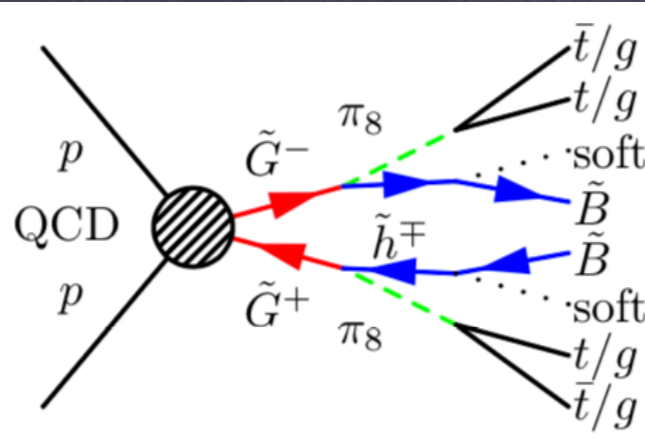


(f) $Q_8 \rightarrow \bar{q}\pi_3 \rightarrow \bar{q}t\tilde{B}$,

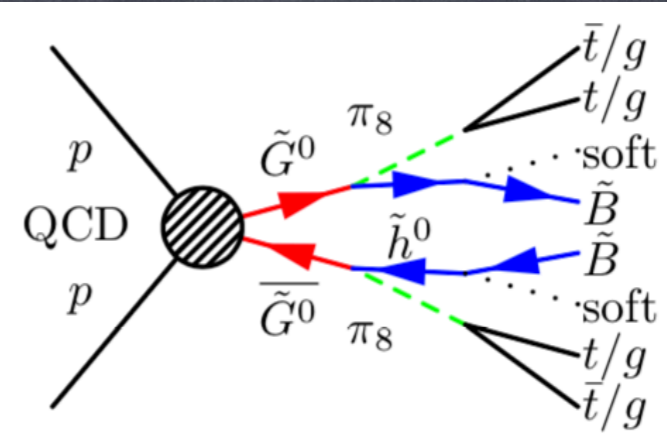
$$m_{\pi_3} = 1.4 \text{ TeV}$$



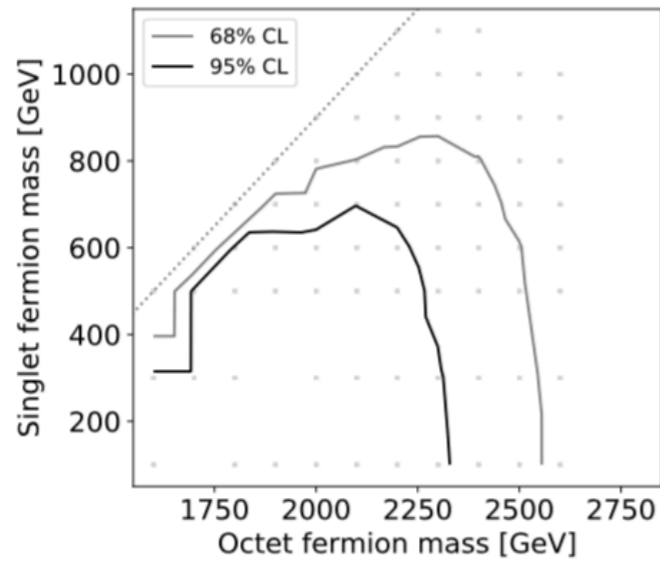
(a) $\tilde{g} \rightarrow \tilde{B}\pi_8, \pi_8 \rightarrow \bar{t}t/gg.$



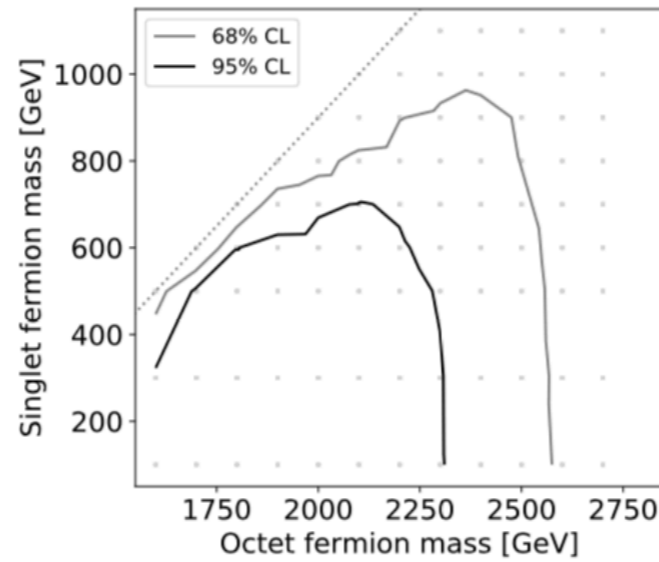
(b) $\tilde{G}^+ \rightarrow \tilde{h}^+\pi_8, \pi_8 \rightarrow \bar{t}t/gg.$



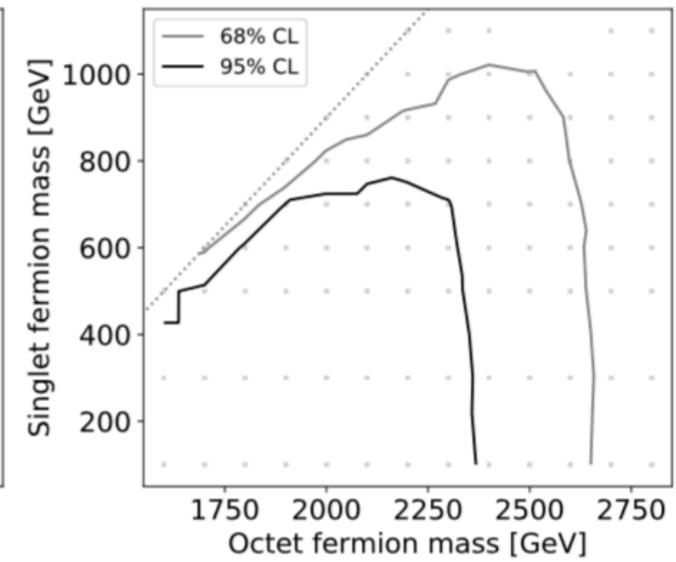
(c) $\tilde{G}^0 \rightarrow \tilde{h}^0\pi_8, \pi_8 \rightarrow \bar{t}t/gg.$



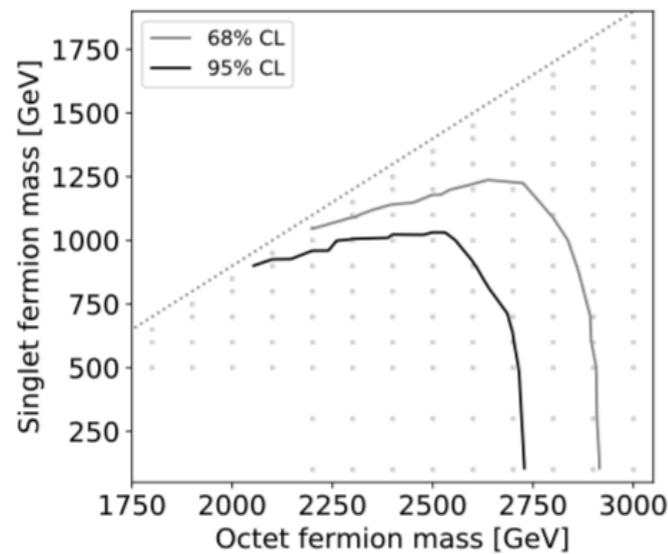
(a) $\tilde{g} \rightarrow \pi_8\tilde{B}, \pi_8 \rightarrow gg$



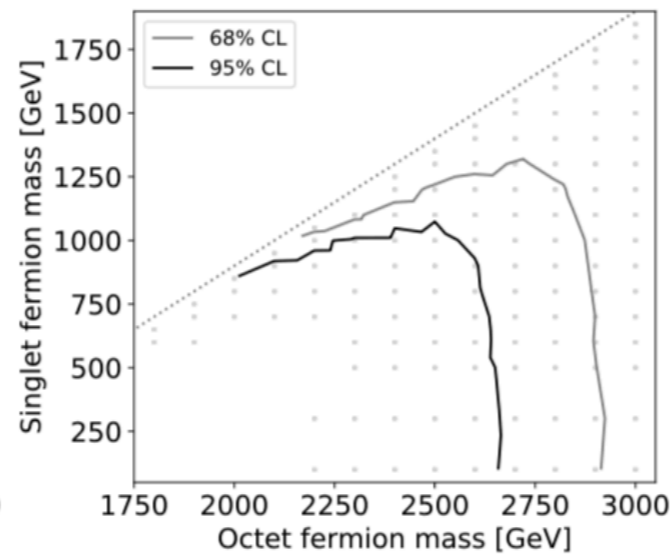
(b) $\tilde{g} \rightarrow \pi_8\tilde{B}, \pi_8 \rightarrow gg, t\bar{t}$



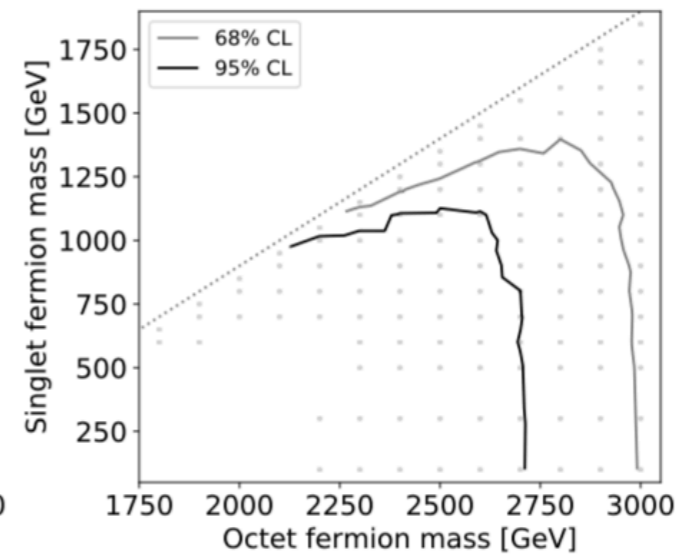
(c) $\tilde{g} \rightarrow \pi_8\tilde{B}, \pi_8 \rightarrow t\bar{t}$



(d) $Q_8 \rightarrow \pi_8 Q_1, \pi_8 \rightarrow gg$



(e) $Q_8 \rightarrow \pi_8 Q_1, \pi_8 \rightarrow gg, t\bar{t}$

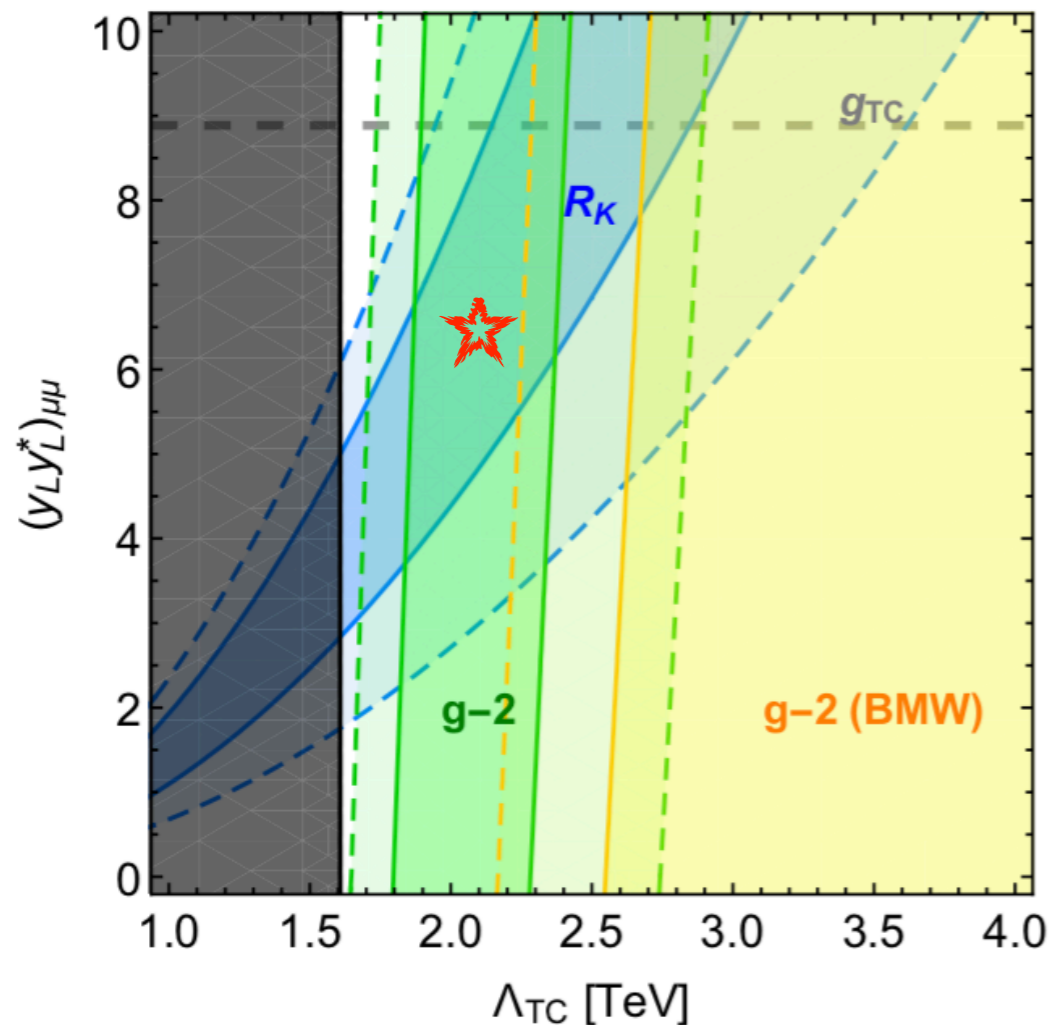


(f) $Q_8 \rightarrow \pi_8 Q_1, \pi_8 \rightarrow t\bar{t}$

There's something about Muons



$N_{TC}=2, (y_Q y_Q^*)_{bs}=0.035$



$$R_K = \frac{\text{BR}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\text{BR}(B^+ \rightarrow K^+ e^+ e^-)} = 0.846_{-0.041}^{+0.044}$$

- $g-2$ fixes the scale of new physics
- natural values for TC-like theories!
- RK requires large muon couplings (attainable in strong dynamics)

These anomalies will be further probed in the near future!

Bonus tracks

What if FCC-ee discovers $Z \rightarrow \gamma a$?

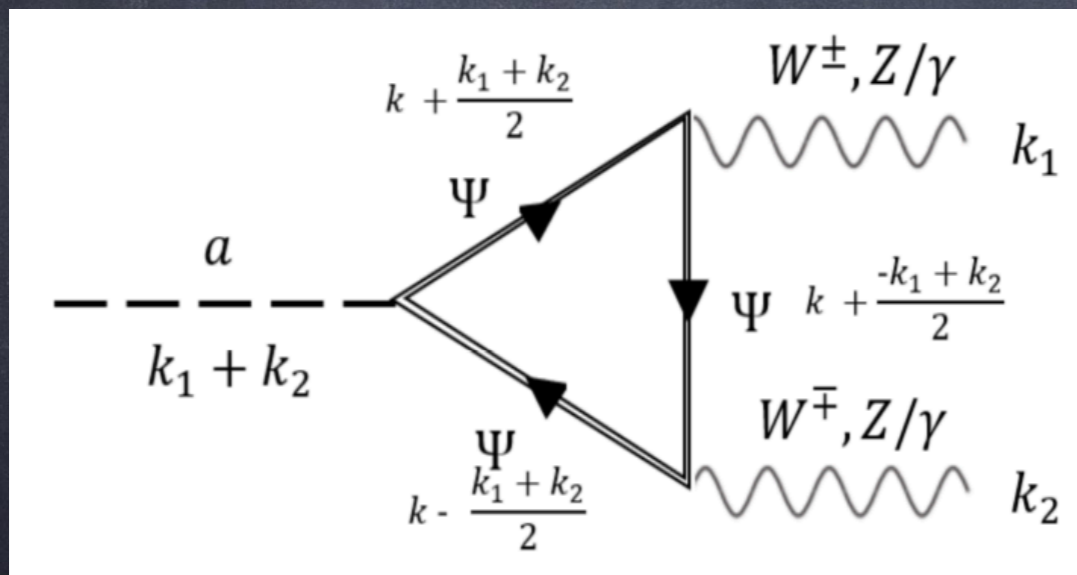
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work in progress

- Is it possible to distinguish the composite scenario, from an elementary mock-up model?

$$\Phi = H + i a$$

Singlet scalar

$$\Psi = \text{doublet} + \text{singlet}$$



Triangle loops can mimic the WZW interactions of the composite ALP:

doublet + singlet =
photo-phobic case

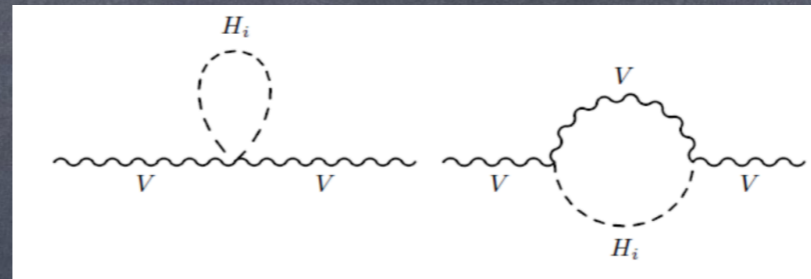
- Note: fermion masses of the order of TeV, potentially discoverable at HL-LHC or FCC-hh (QCD-neutral)

What if FCC-ee discovers $Z \rightarrow \gamma a$?

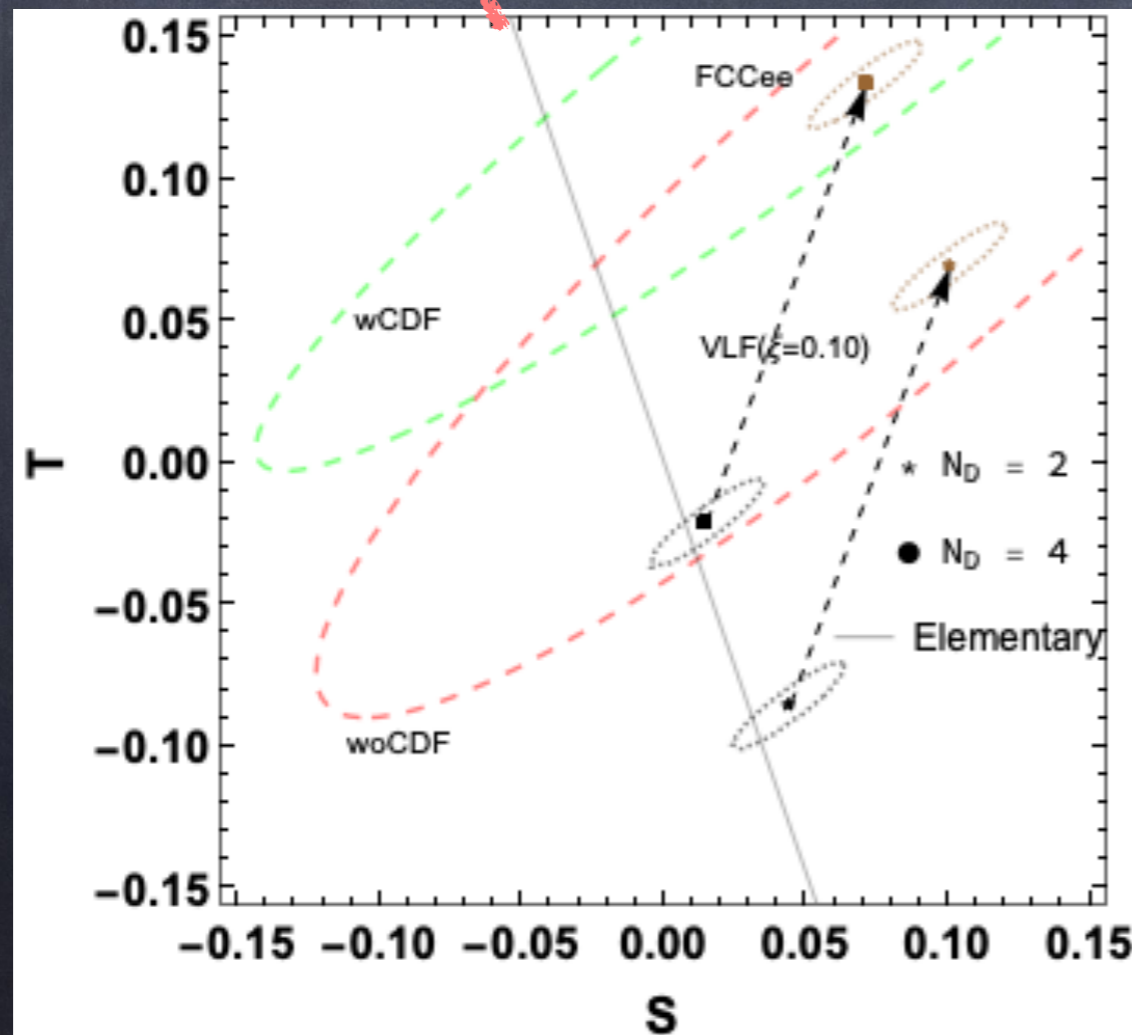
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work in progress

- Is it possible to distinguish the composite scenario, from an elementary mock-up model?

EWPT only depend on H loops



composite case:
see 1502.04718



For fixed $BR = 10^{-8}$,
i.e. discovery.

Arrows: naive contribution
of top partner loops.