

# Comments on Elliptic flow (Elliptic flow at RHIC and LHC and percolation of strings)

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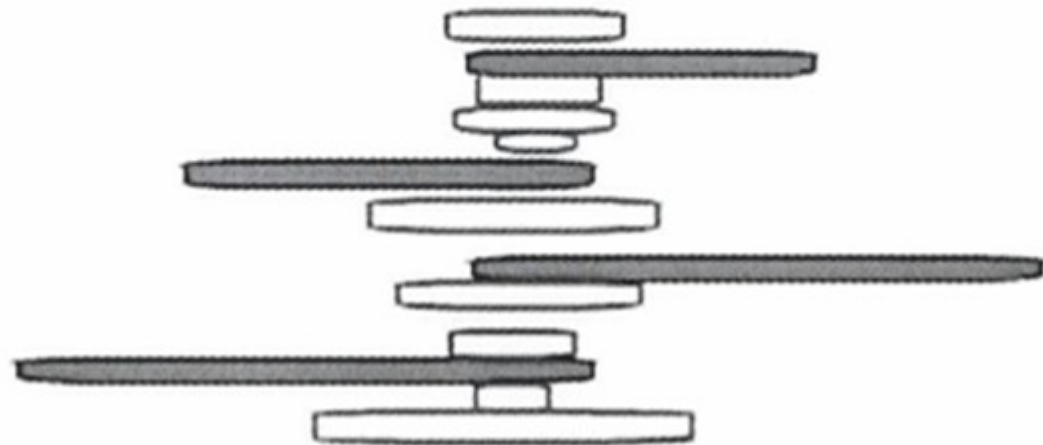
# Outline

- Brief description of string percolation
- Elliptic flow in percolation
- RHIC and LHC results
- Shear viscosity/entropy in percolation



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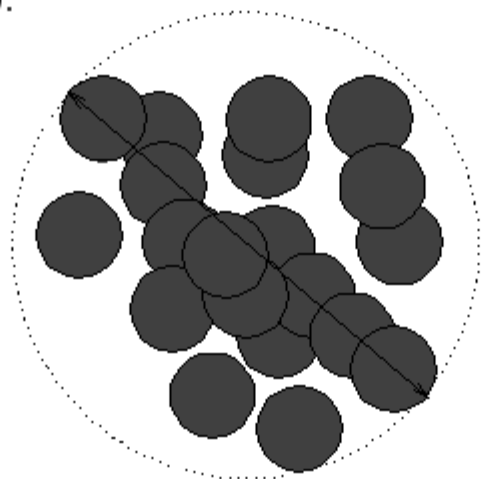
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- **Color strings** are stretched between the projectile and target
  - **Strings = Particle sources**: particles are created via sea  $q\bar{q}$  production in the field of the string
  - **Color strings = Small areas** in the transverse space filled with color field created by the colliding partons
  - With growing energy and/or atomic number of colliding particles, the number of sources grows
  - So the elementary color sources start to **overlap, forming clusters**, very much like disk in the 2-dimensional percolation theory
  - In particular, at a certain critical density, a macroscopic cluster appears, which marks the **percolation phase transition**
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(N. Armesto et al., PRL77 (96); J.Dias de Deus et al., PLB491 (00); M. Nardi and H. Satz(98).

- **How?:** Strings fuse forming clusters. At a certain critical density  $\eta_c$  (central PbPb at SPS, central AgAg at RHIC, central SS at LHC ) a macroscopic cluster appears which marks the percolation phase transition (second order, non thermal).



$$\eta = N_{st} \frac{S_1}{S_A}, \quad S_1 = \pi r_0^2, \quad r_0 = 0.2 \text{ fm}, \quad \eta_c = 1.1 \div 1.2.$$

$$\mu_n = \sqrt{\frac{nS_n}{S_1}} \mu_1 ; \langle p_T^2 \rangle_n = \sqrt{\frac{nS_1}{S_n}} \langle p_T^2 \rangle_1$$

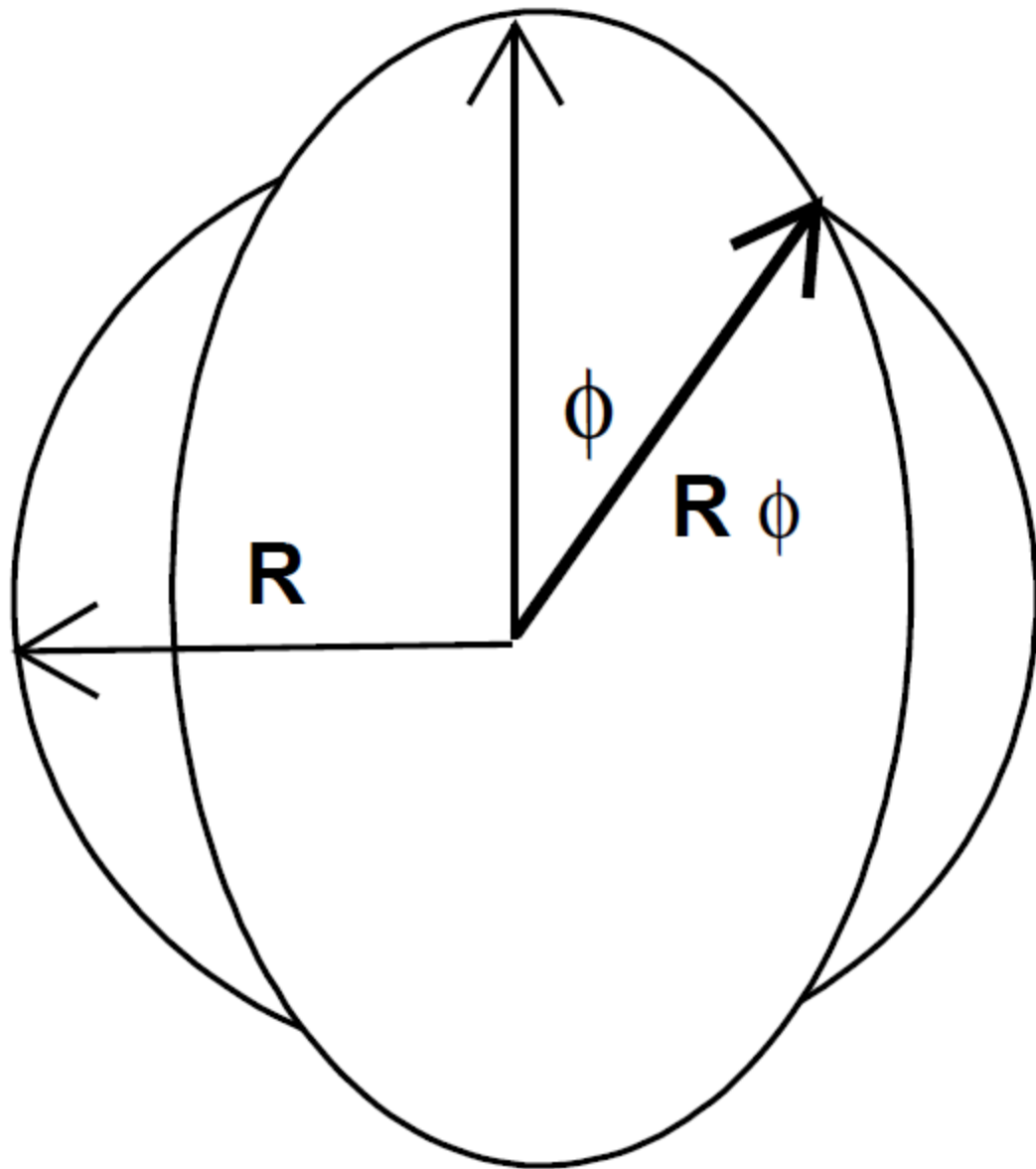
Energy-momentum of the cluster is the sum of the energy-momentum of each string.

As the individual color field of the individual string may be oriented in an arbitrary manner respective to one another,  $Q_n^2 = nQ_1^2$

■ At high densities

- $\langle \mu \rangle_n = nF(\eta) \langle \mu \rangle_1 \quad \langle p_T^2 \rangle_n = \frac{\langle p_T^2 \rangle_1}{F(\eta)}$
- $F(\eta) = \sqrt{\frac{1-e^{-\eta}}{\eta}}, \quad \eta = N_S \frac{\pi r_0^2}{S_A}$
- $r_0$  is the transverse size of a single string  $\simeq 0.2$  fm.

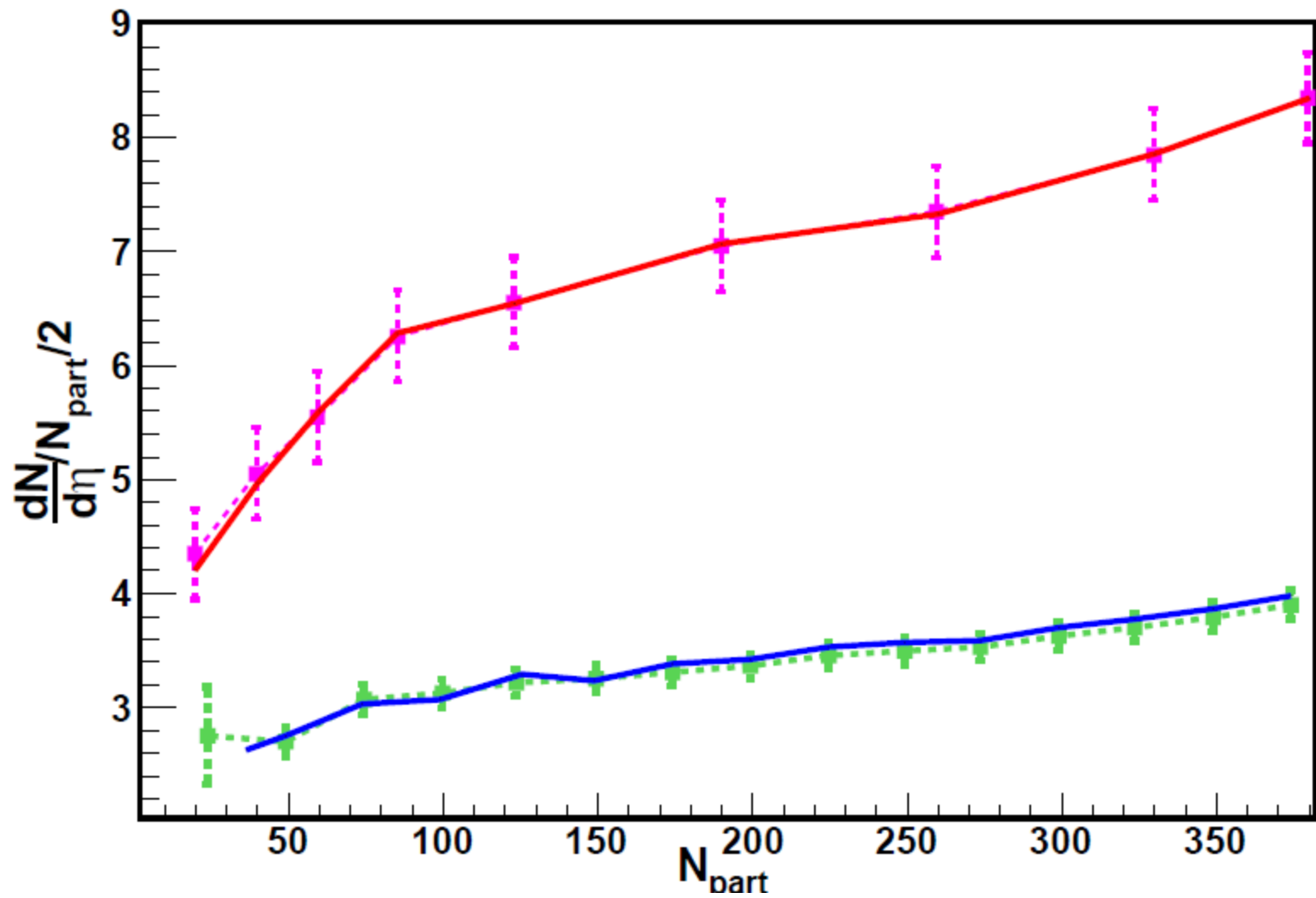


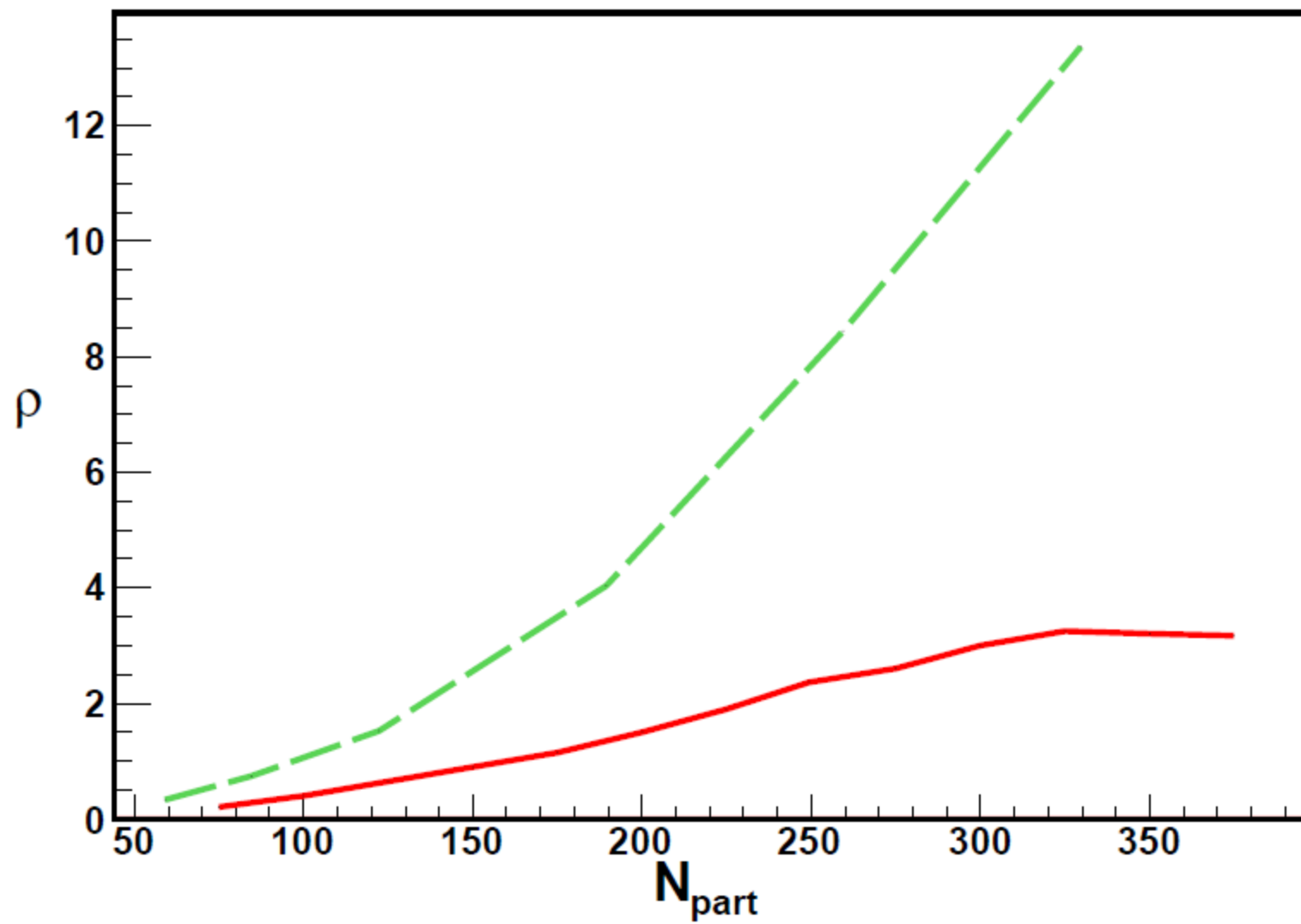


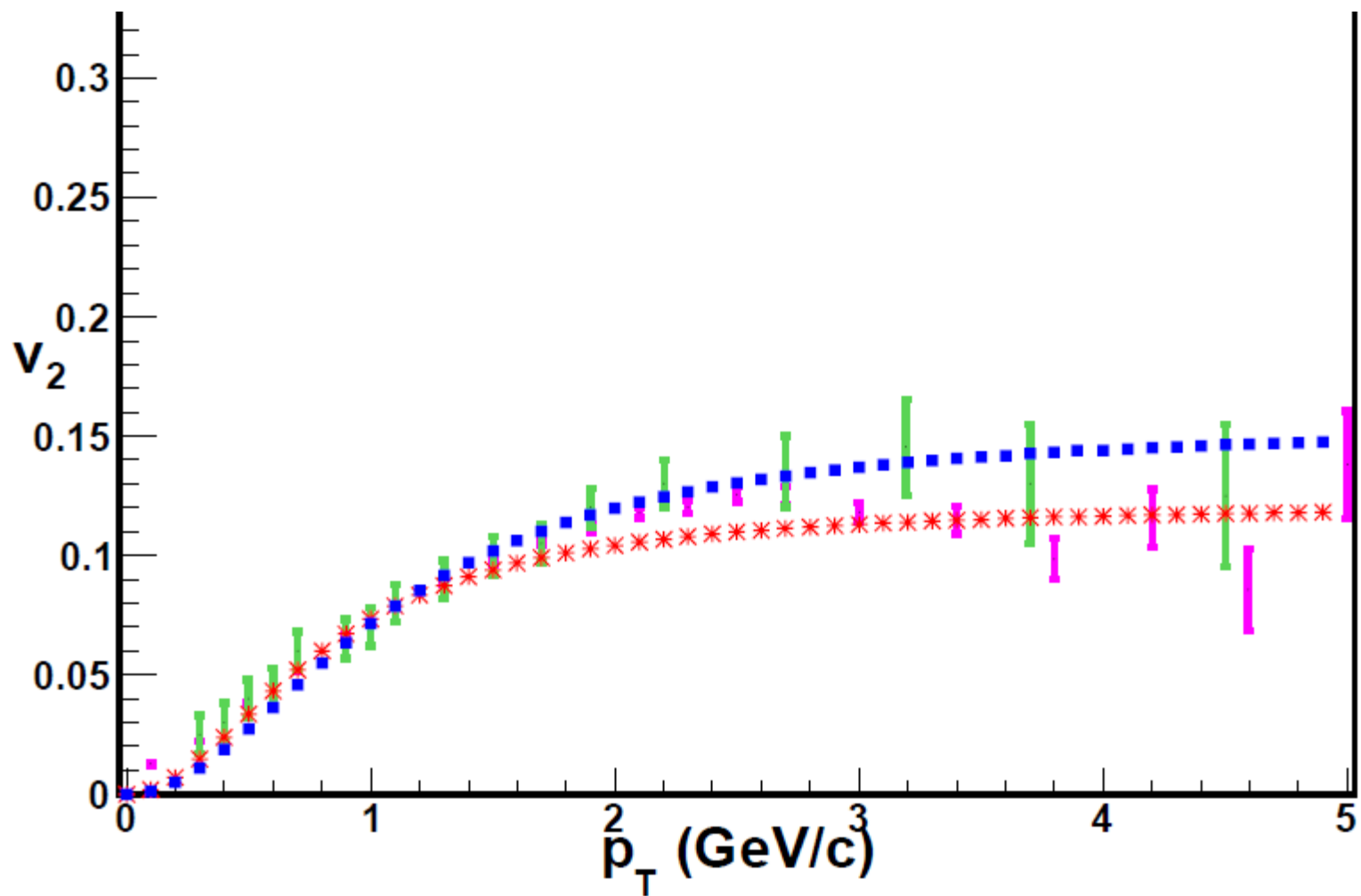
$$\eta_\varphi = \eta \left( \frac{R}{R_\varphi} \right)^2$$

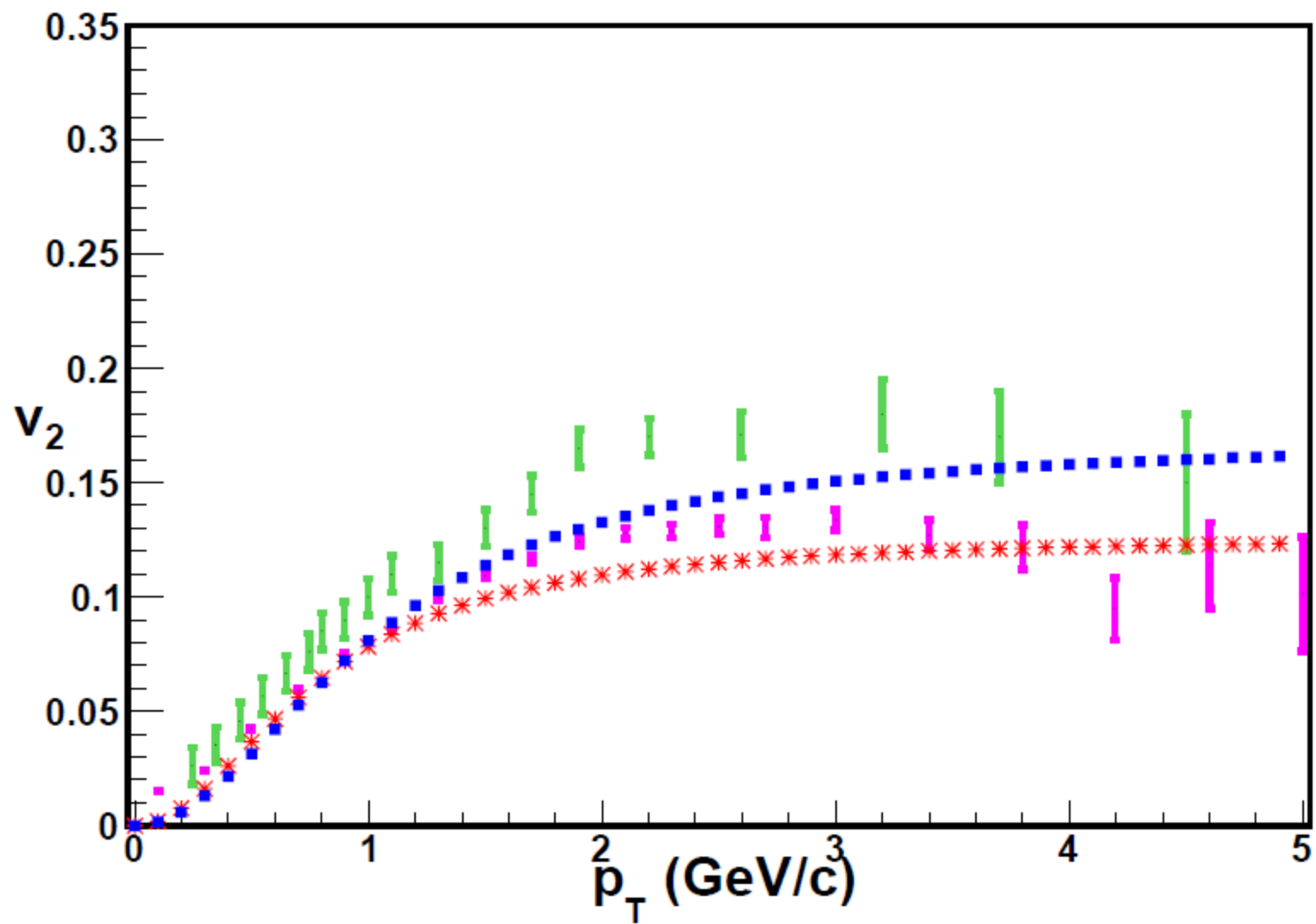
$$\begin{aligned} v_2(p_T^2, y) &= \frac{2}{\pi} \int_0^{\pi/2} d\varphi \cos(2\varphi) \left[ 1 + \frac{\partial \ln f(p_T^2, \eta, y)}{\partial R^2} (R_\varphi^2 - R^2) \right] \\ &= \frac{2}{\pi} \int_0^{\pi/2} d\varphi \cos 2\varphi \left( \frac{R_\varphi}{R} \right)^2 \left( \frac{e^{-\eta} - F(\eta)^2}{2F(\eta)^2} \right) \frac{F(\eta) p_T^2 / \langle p_T^2 \rangle_1}{(1 + F(\eta) p_T^2 / \langle p_T^2 \rangle_1)} \end{aligned}$$

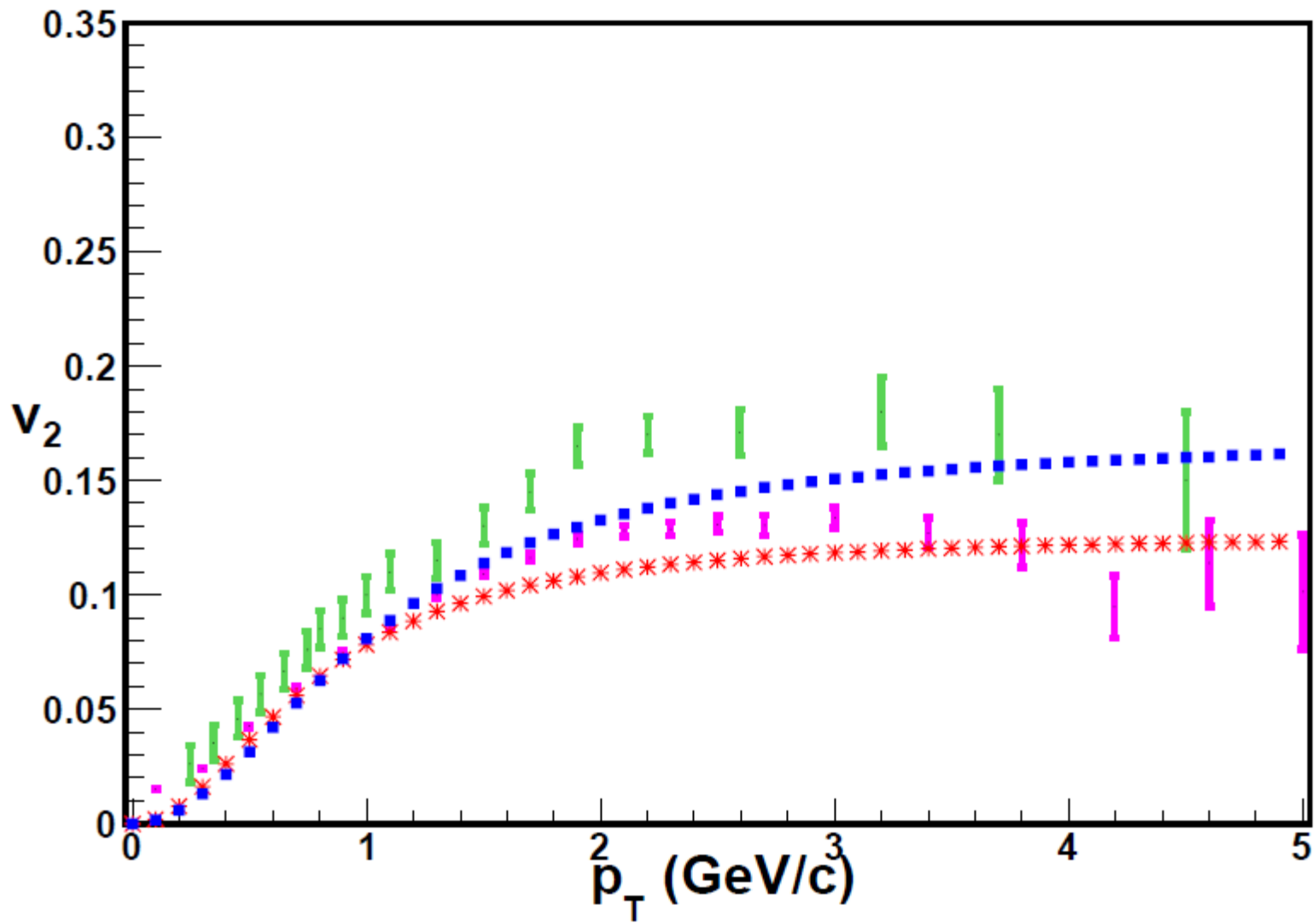
$$v_2 = \frac{2}{\pi} \int_0^{\pi/2} d\varphi \cos(2\varphi) \left( \frac{R_\varphi}{R} \right) \left( \frac{e^{-\eta} - F(\eta)^2}{2F(\eta)^3} \right) \frac{R}{R-1}$$

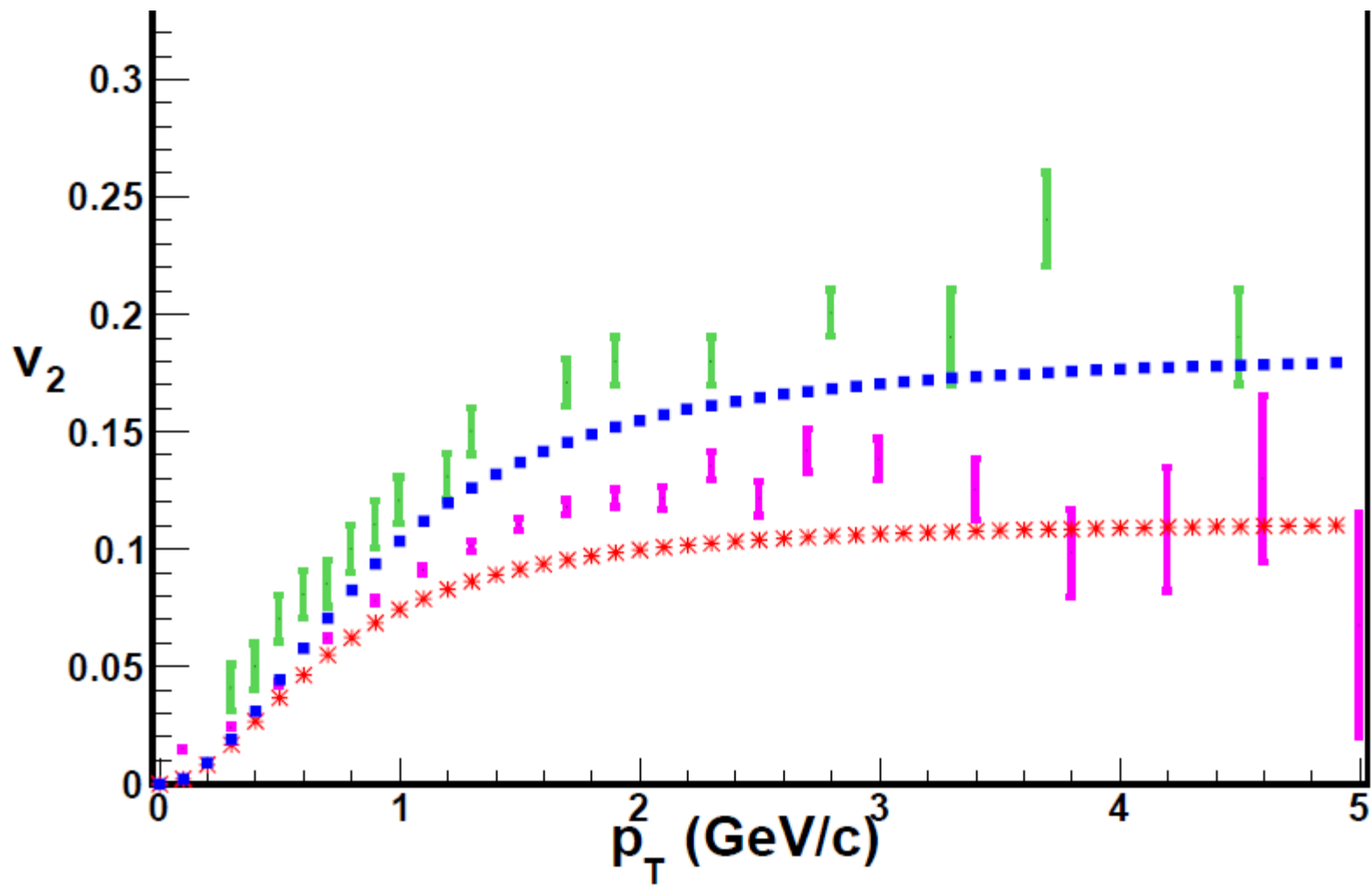




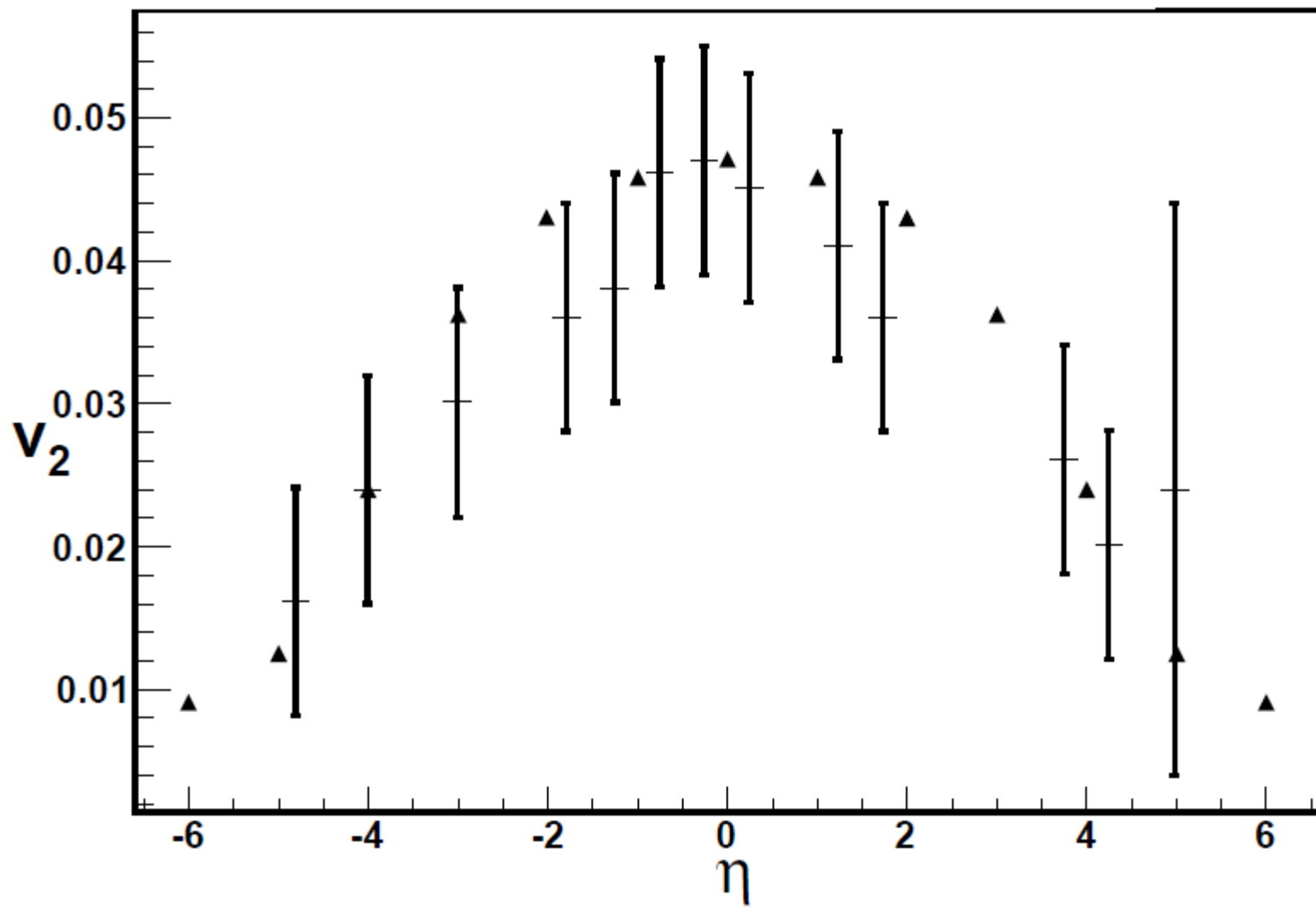


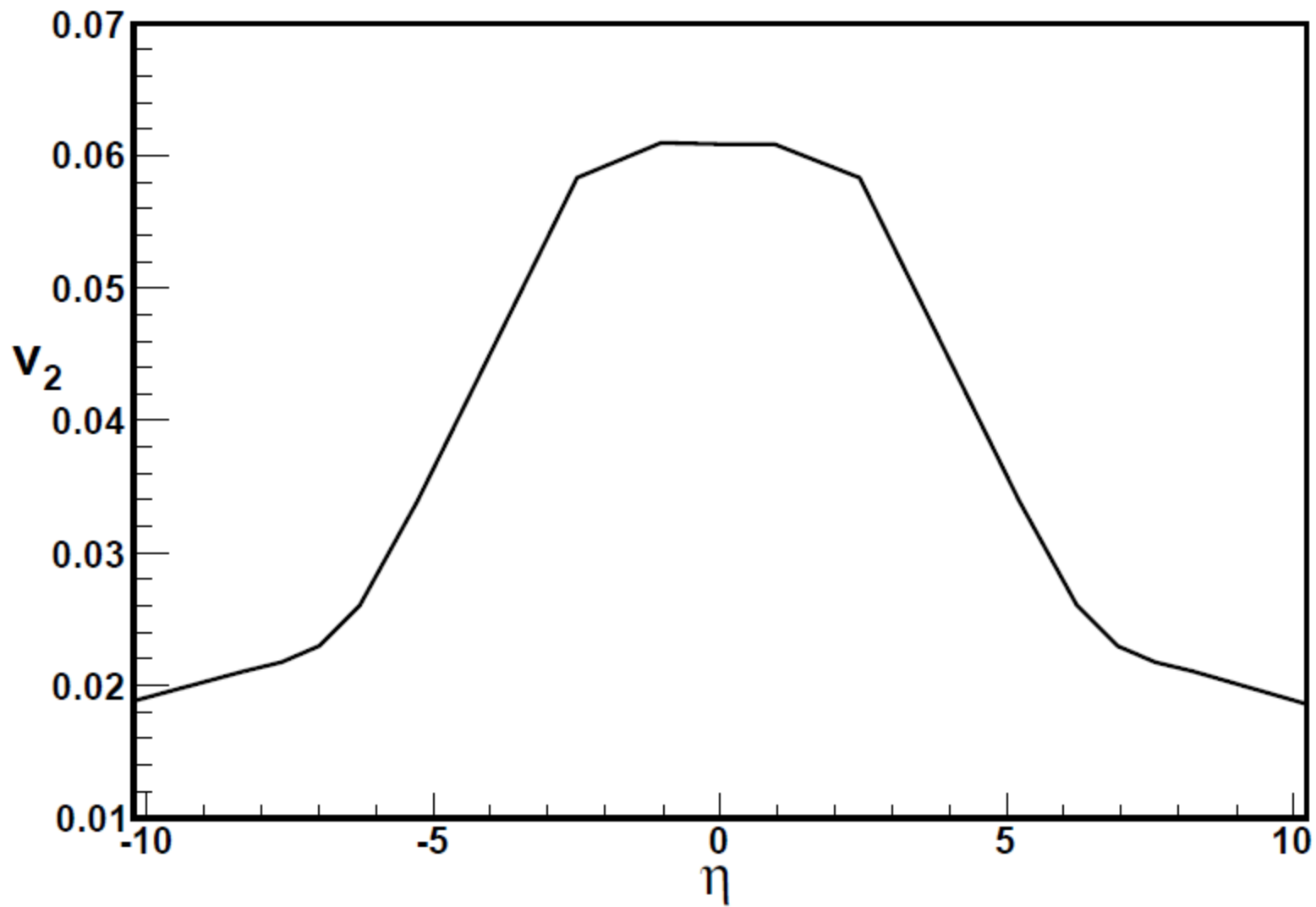


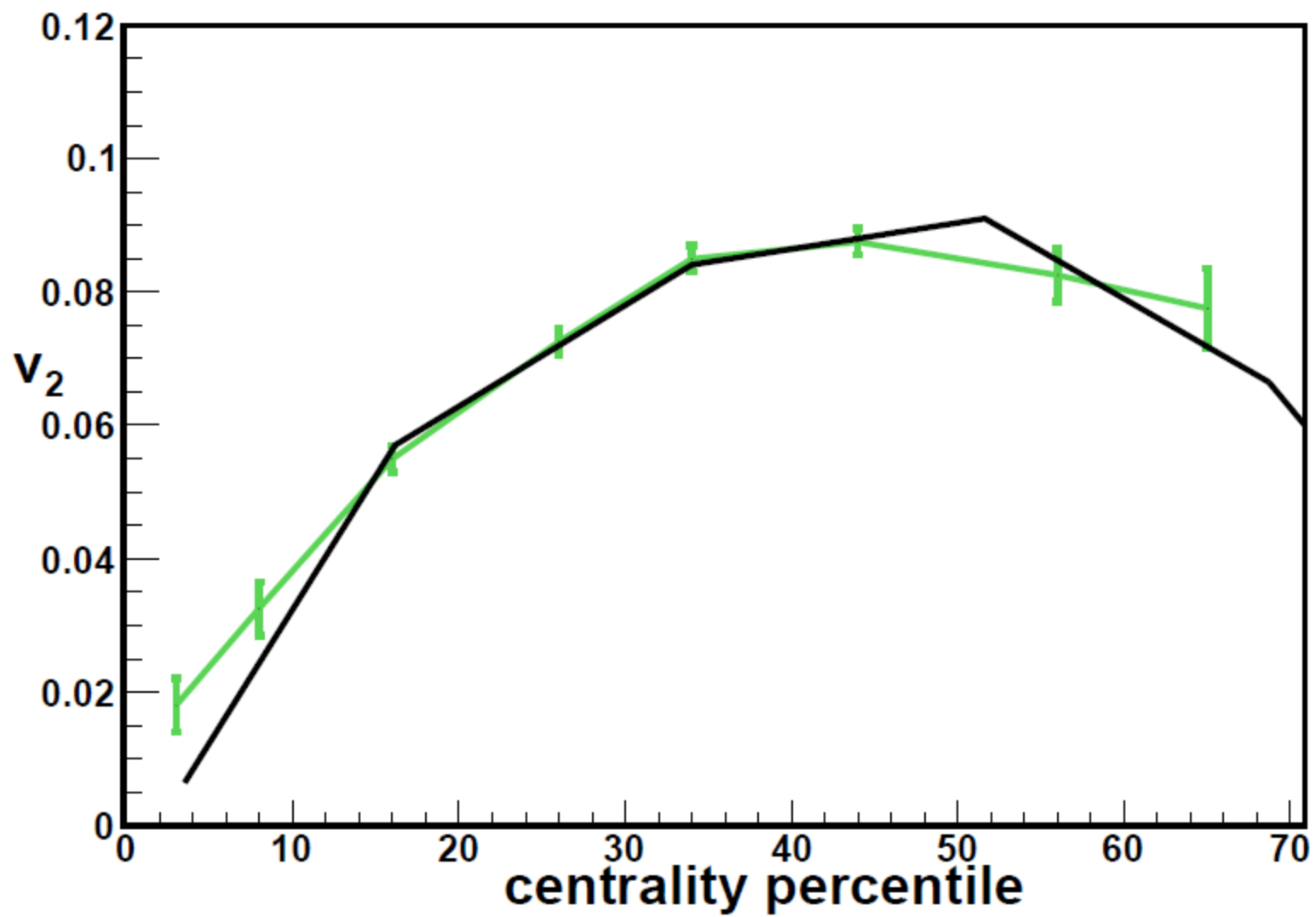


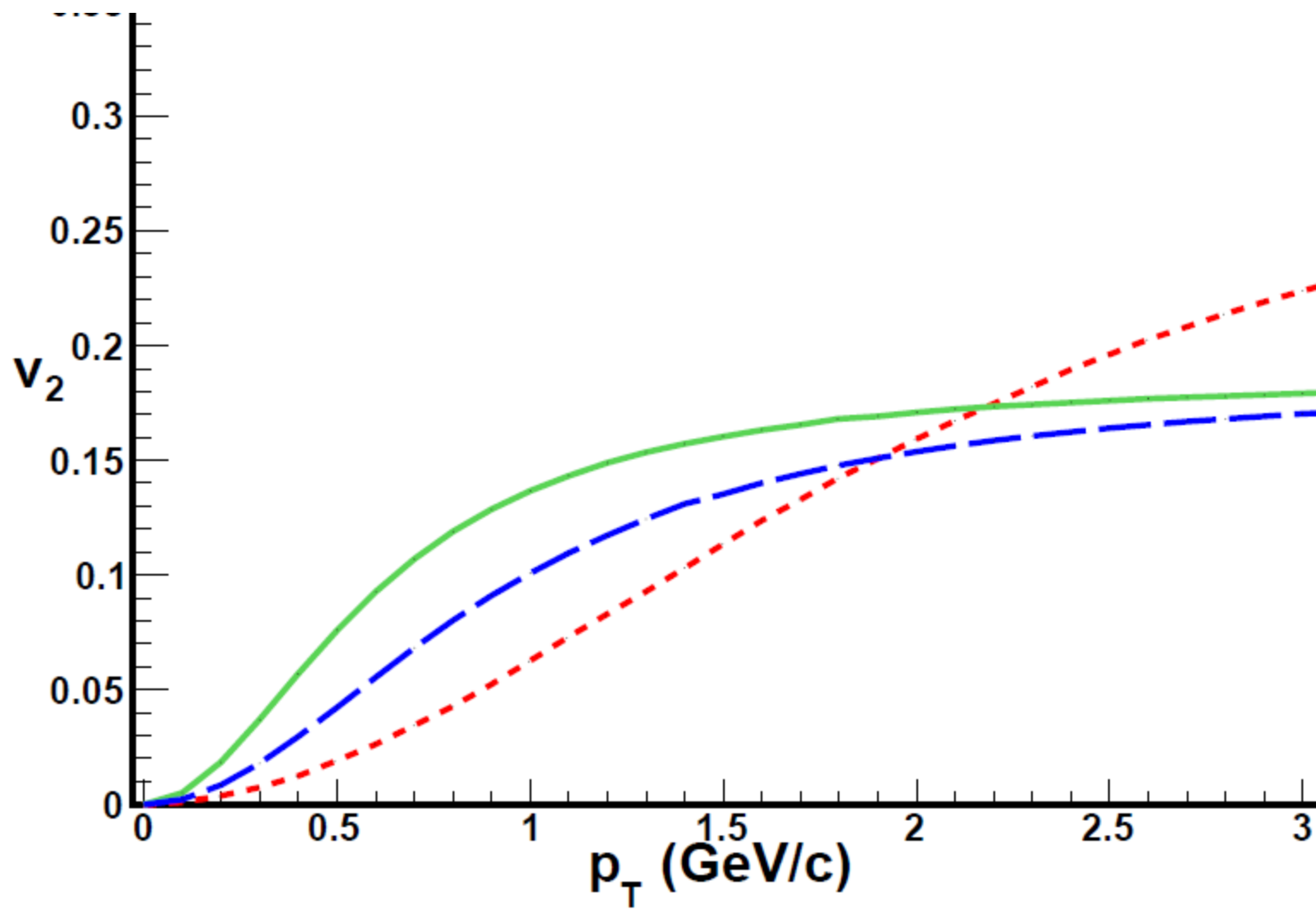


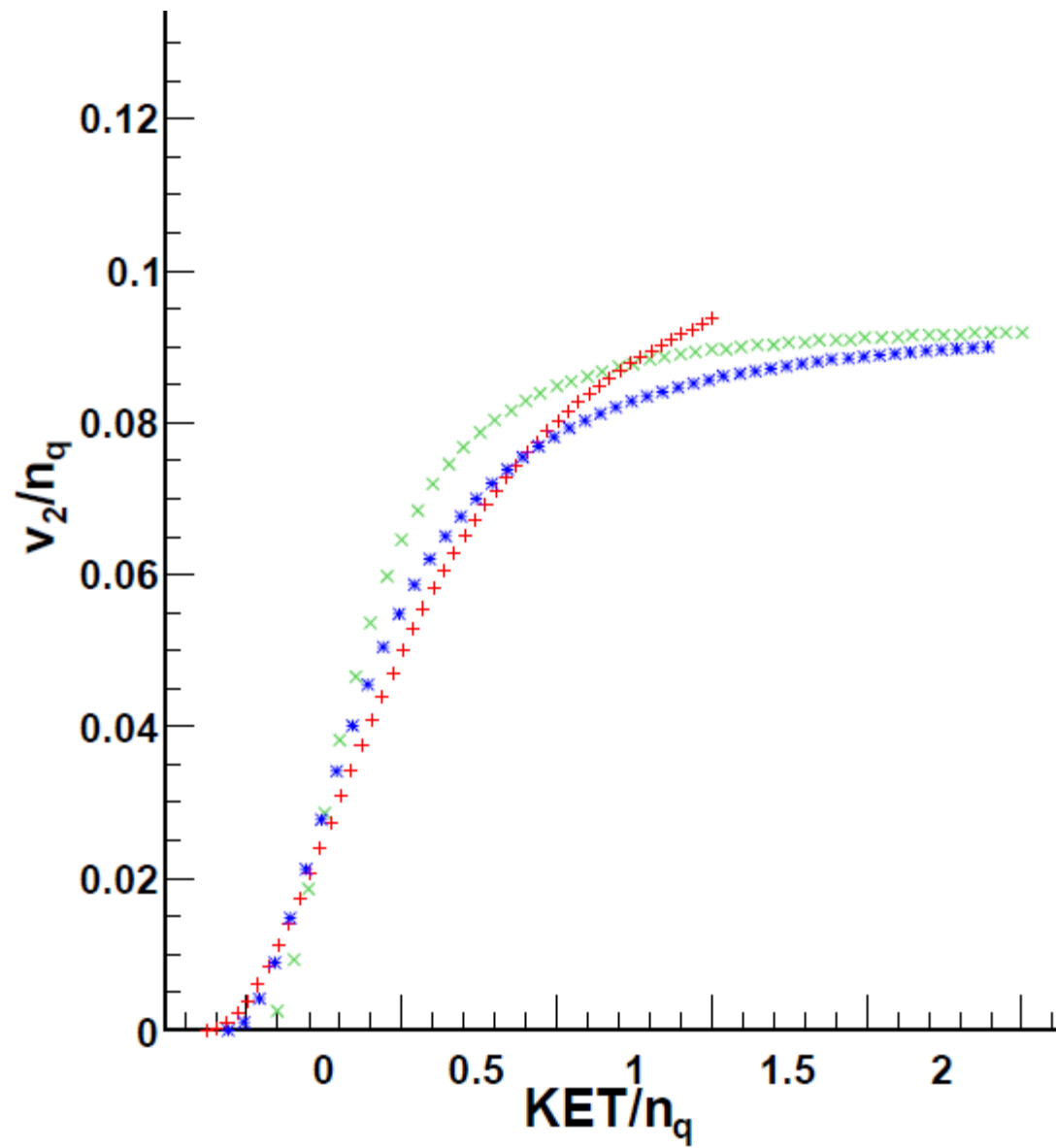




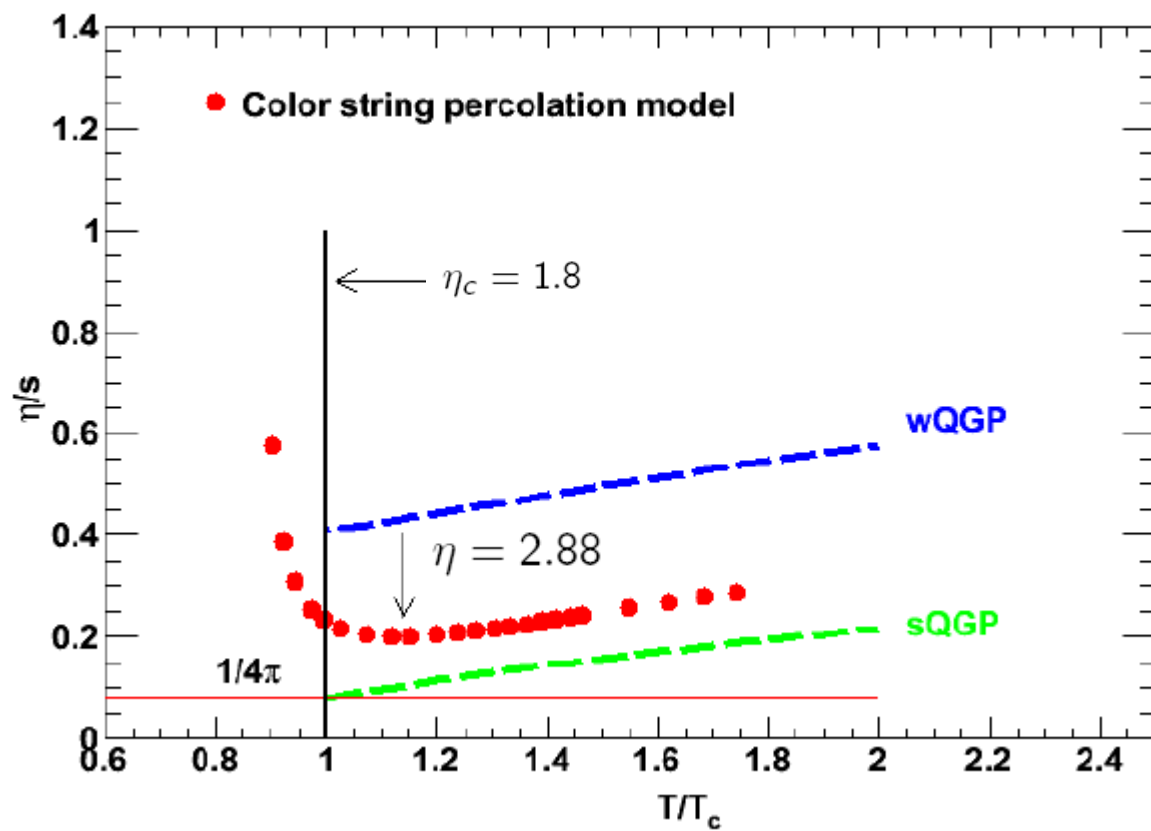








$$\frac{\eta}{s} = \frac{1}{5\sqrt{2}} \frac{\langle p_T \rangle_1 \eta^{1/4}}{(1 - e^{-\eta})^{5/4}} L$$



# Conclusions

- A good agreement with RHIC and LHC data(Close analytical formula)
- Low ratio shear viscosity/entropy density in the whole energy range RHIC-LHC (increasing very slowly as a power $1/4$  of the string density)
- Percolation provides an microscopic framework of the elliptic flow