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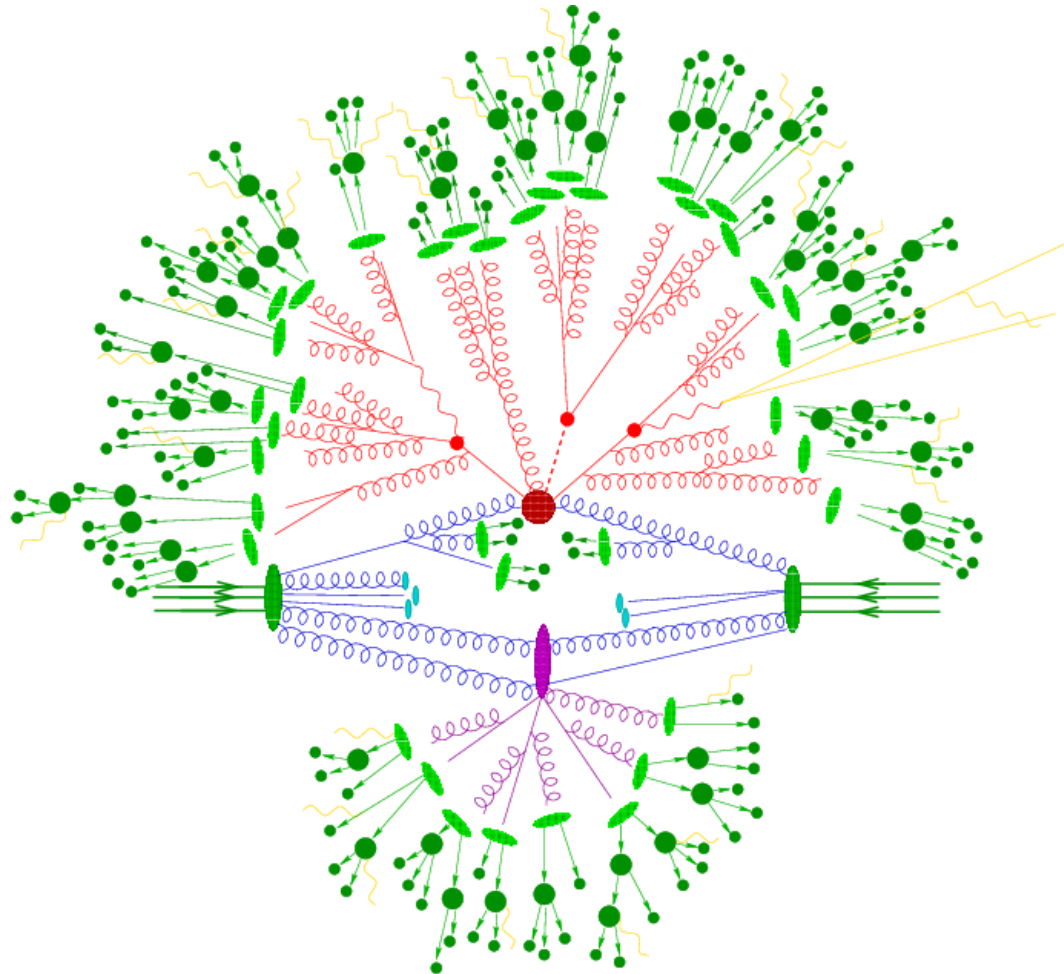
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# PARTON SHOWER EVOLUTION AT THE AMPLITUDE LEVEL

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Supervised by Jeff Forshaw and Simon Plätzer

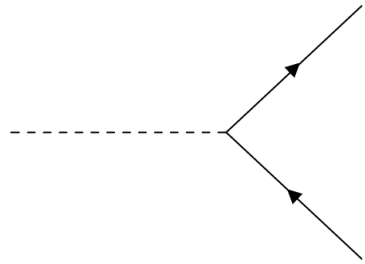
# Parton showers: the current state of the art



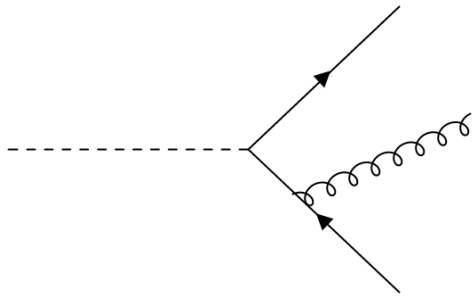
Parton showers model the cascade of QCD radiation that occurs from coloured high-energy particles

- Angular ordered shower: up to NLL accuracy of global, two-jet observables but it fails beyond the two-jet limit or for non-global observables.
- Dipole shower: accurate for global and non-global observables, only up to LL and LC

Real emissions and virtual exchanges factorise in the soft kinematic limit

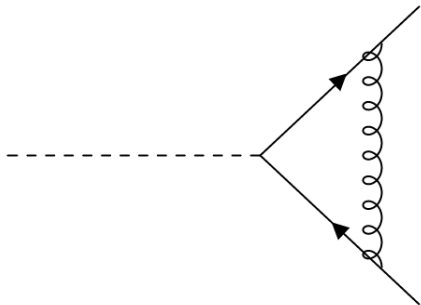


$$|H\rangle$$



$$\mathbf{D}^\mu |H\rangle$$

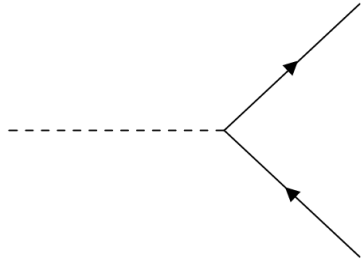
$$\mathbf{D}_i^\mu = \sum_j \mathbf{T}_j E_i \frac{p_j^\mu}{p_j \cdot q_i}$$



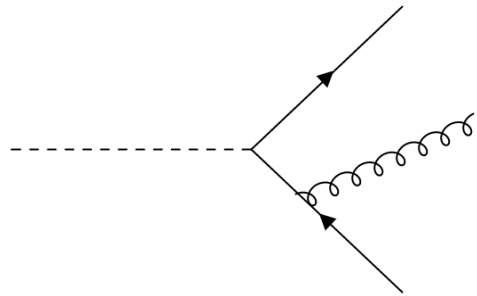
$$\mathbf{\Gamma} |H\rangle$$

$$\mathbf{\Gamma} = \frac{\alpha_s}{\pi} \sum_{i < j} (-\mathbf{T}_i \cdot \mathbf{T}_j) \left\{ \int \frac{d\Omega_k}{4\pi} \omega_{ij}(\hat{k}) - i\pi \tilde{\delta}_{ij} \right\}$$

Real emissions and virtual exchanges factorise in the soft kinematic limit

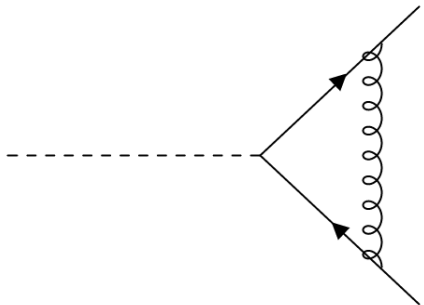


$$|H\rangle$$



$$\mathbf{D}^\mu |H\rangle$$

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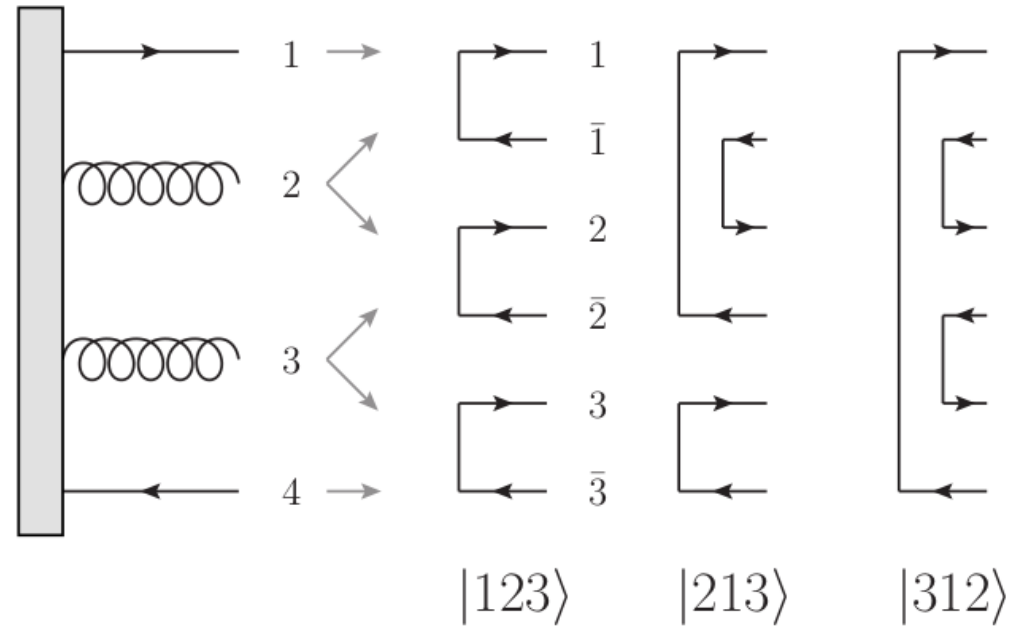
Gell-Mann basis

$$\lambda_1 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \lambda_2 = \begin{pmatrix} 0 & -i & 0 \\ i & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \lambda_3 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$\lambda_4 = \begin{pmatrix} 0 & 0 & 1 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix}, \lambda_5 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \lambda_6 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}$$

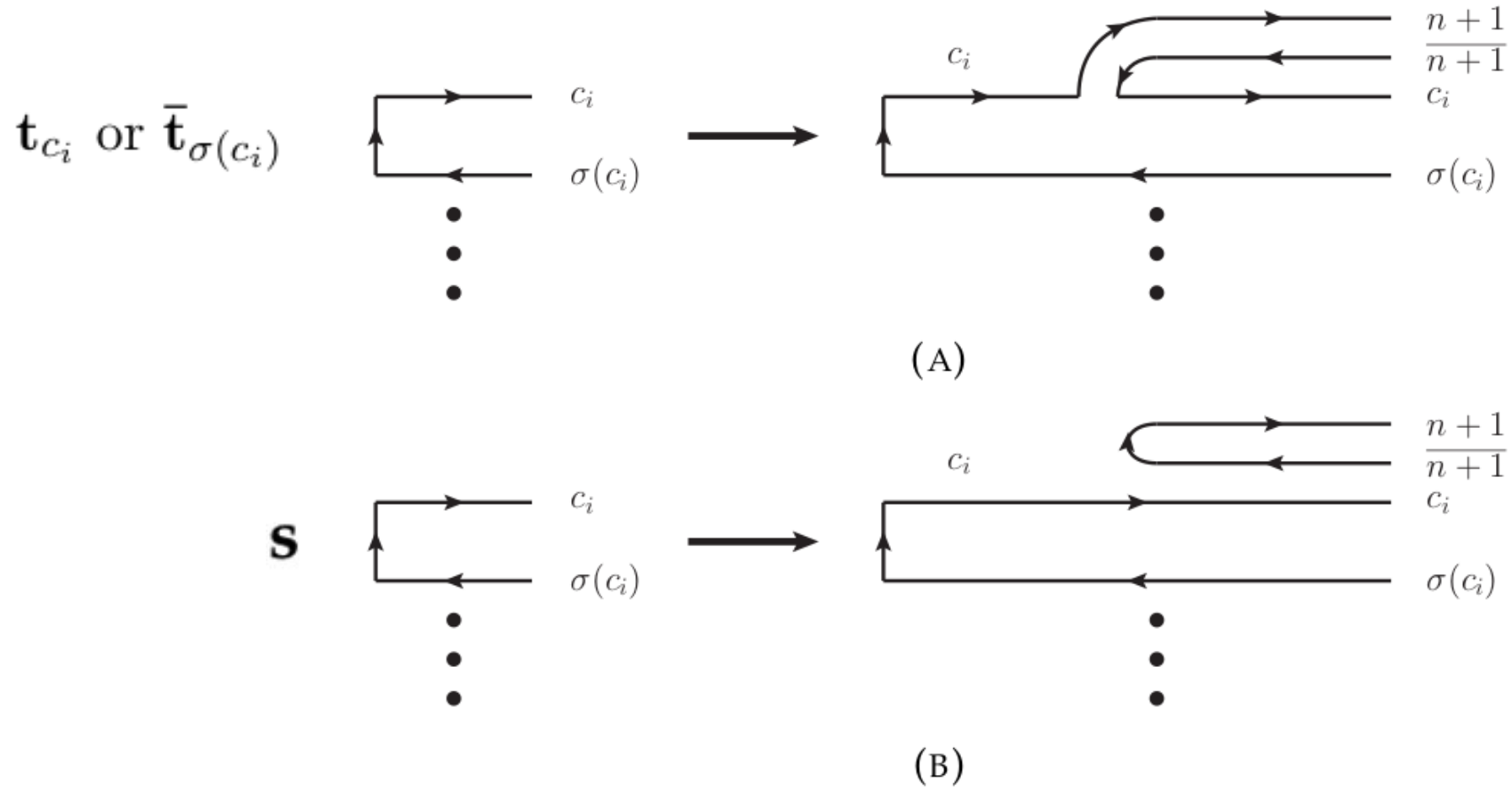
$$\lambda_7 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & -i \\ 0 & i & 0 \end{pmatrix}, \lambda_8 = \frac{1}{\sqrt{3}} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -2 \end{pmatrix}$$

Colour Flow Basis

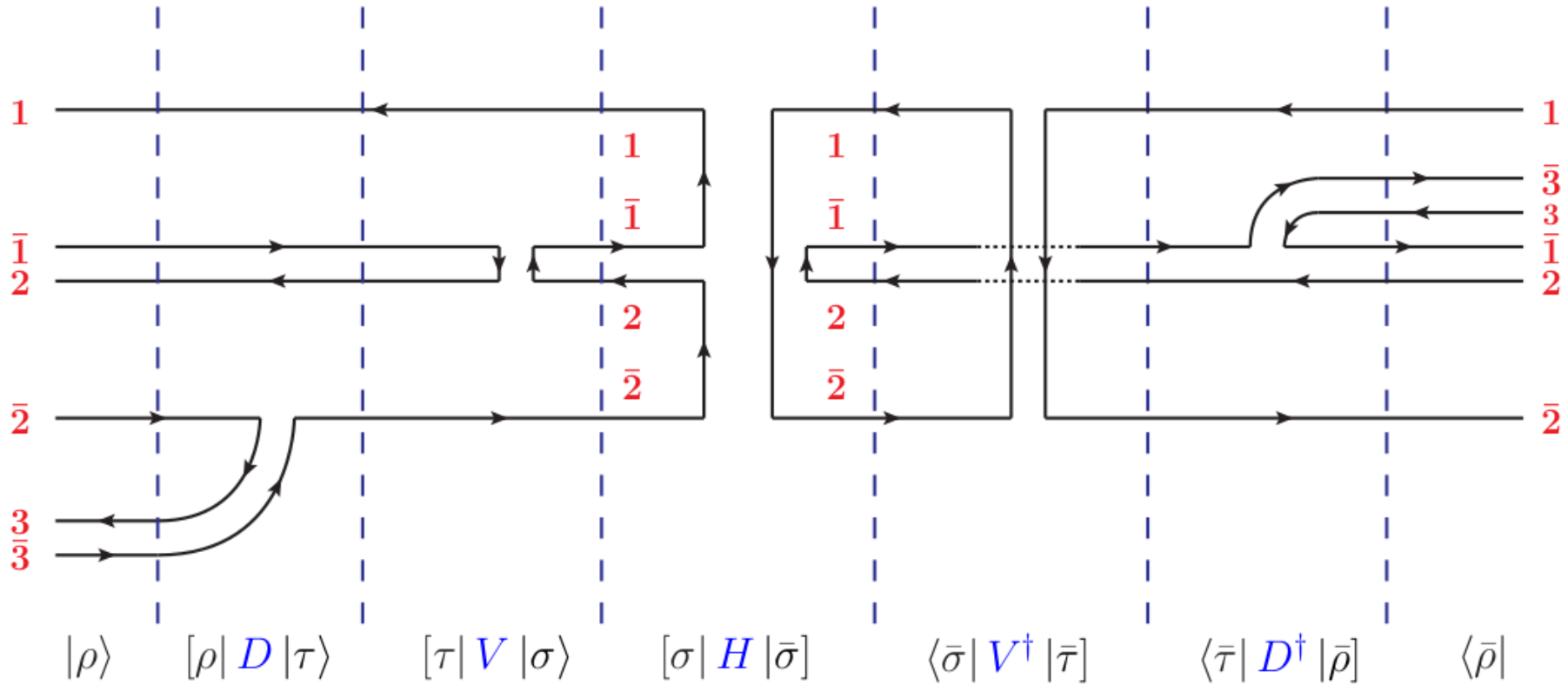


# Colour evolution: real emissions

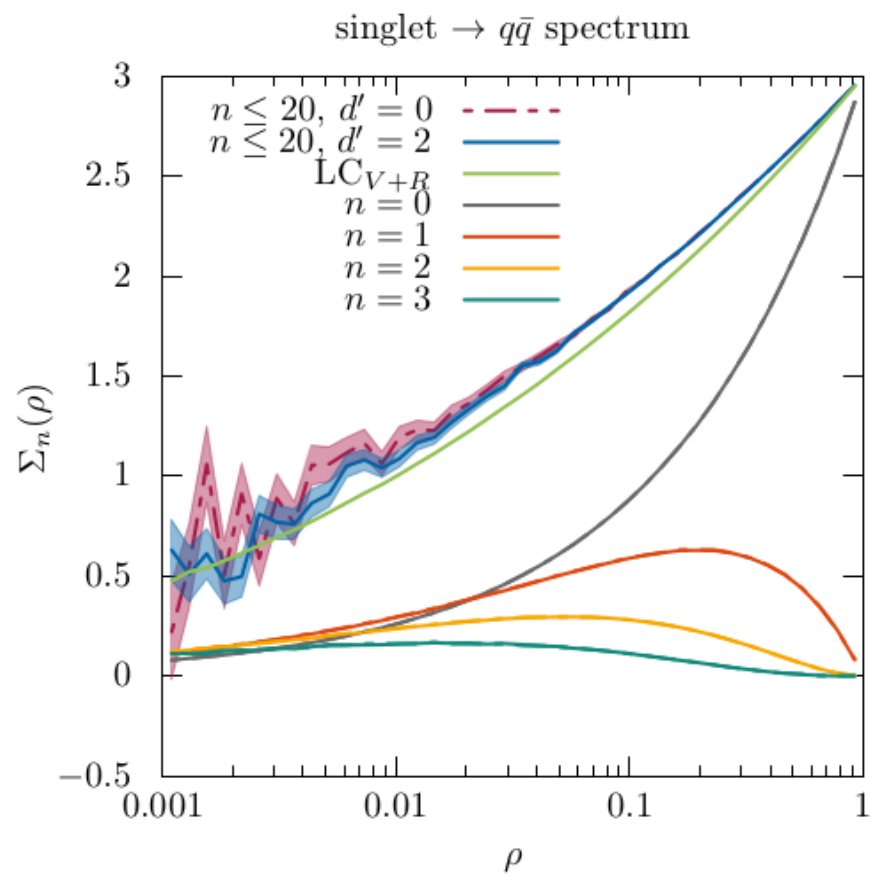
$$\mathbf{T}_i = \lambda_i \mathbf{t}_{c_i} + \bar{\lambda}_i \bar{\mathbf{t}}_{\bar{c}_i} - \frac{1}{N_c} (\lambda_i - \bar{\lambda}_i) \mathbf{s}$$



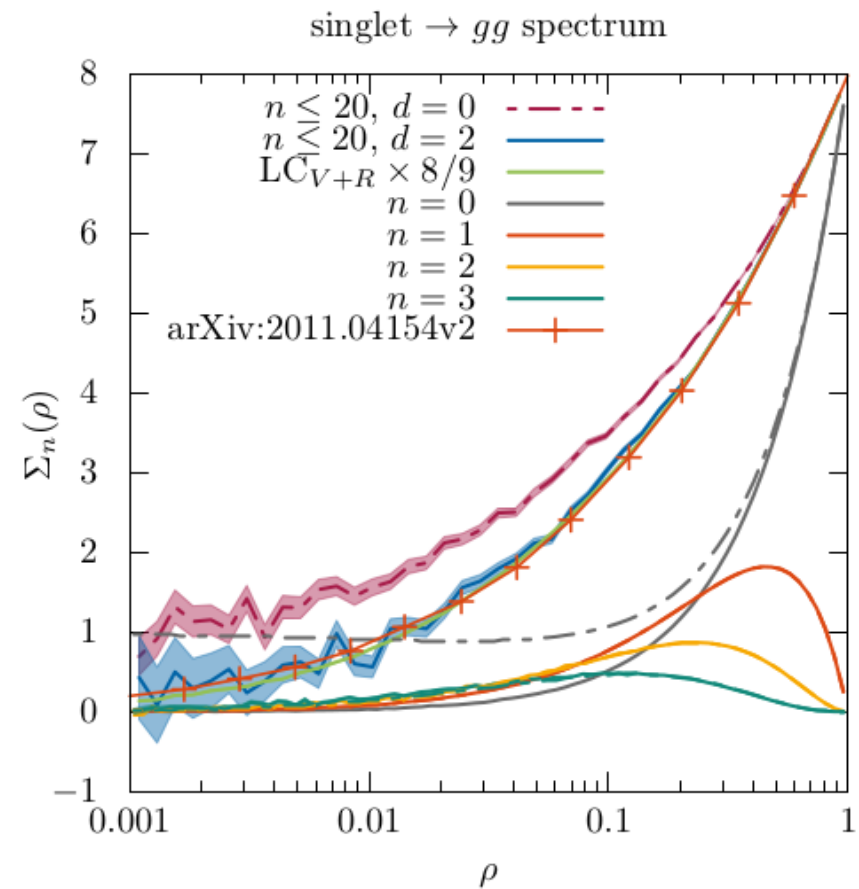
# An example of colour evolution



M. De Angelis, J. R. Forshaw, and S. Plätzer, “Resummation and simulation of soft gluon effects beyond leading color,” *Physical Review Letters*, vol. 126, March 2021.



(A) Breakdown of the jet veto cross section by multiplicity and colour order, for the process singlet  $\rightarrow q\bar{q}$ .



(B) Breakdown of the jet veto cross section by multiplicity and colour order, for the process singlet  $\rightarrow gg$ .