

Global fit to $b \rightarrow c \tau \nu$



Syuhei Iguro

[Inspire](#)
[web page](#)



18/09/2023

Santiago de Compostela

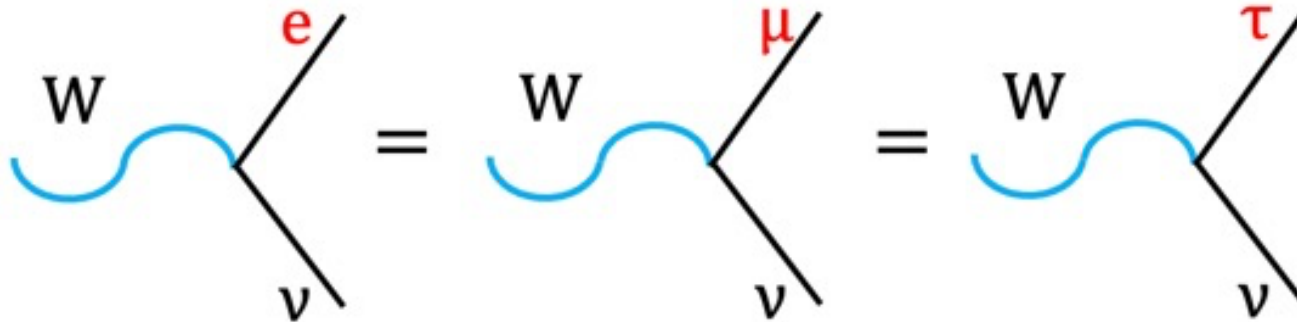
Mainly based on [2210.10751](#) (v3 coming soon)

and many papers with Teppei Kitahara, Yuji Omura, Ryoutaro Watanabe, Hantian Zhang, Monika Blanke, Ulrich Nierste, Fedele Marco, Andreas Crivellin,,,

$R_{D^{(*)}}$ anomaly

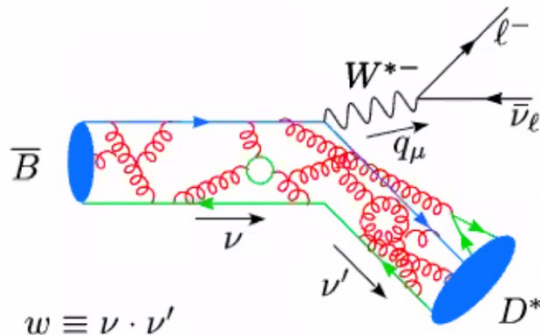
Now persisting more than 10 years

SM: gauge symmetry guarantees



$$R_{D^{(*)}} = \frac{BR(B \rightarrow D^{(*)} \tau \nu)}{BR(B \rightarrow D^{(*)} l \nu)}, \quad l = \mu, e$$

The lepton flavor universality violating (LFUV) effect comes from the lepton mass



Hadronic form factors (FFs) uncertainty is largely cancelled in ratio, V_{cb} also

Good measure to test the LFUV and hence great window to new physics

Experimental update

We had three new data this 1-year

Experiment	R_{D^*}	R_D	Correlation
BaBar	$0.332 \pm 0.024 \pm 0.018$	$0.440 \pm 0.058 \pm 0.042$	-0.27
Belle	$0.293 \pm 0.038 \pm 0.015$	$0.375 \pm 0.064 \pm 0.026$	-0.49
Belle	$0.270 \pm 0.035^{+0.028}_{-0.025}$	-	-
Belle	$0.283 \pm 0.018 \pm 0.014$	$0.307 \pm 0.037 \pm 0.016$	-0.51
LHCb ①	$0.281 \pm 0.018 \pm 0.024$	$0.441 \pm 0.060 \pm 0.066$	-0.43
LHCb ②	$0.257 \pm 0.012 \pm 0.018$	-	-
Belle II ③	$0.267^{+0.041+0.028}_{-0.039-0.033}$	-	-
World average	$0.284 \pm 0.009 \pm 0.008$	$0.356 \pm 0.025 \pm 0.014$	-0.38

- ① [LHCb 2022 Oct. \$\tau \rightarrow \mu \nu \nu\$](#)
 - ② [LHCb 2023 Feb. Hadronic \$\tau\$ \(\$\tau_h\$ \)](#)
 - ③ [Belle II first result 2023 July \$\tau_h\$](#)
- } Run 1
~200fb⁻¹

Now we have data from four experiments!



p-value got improved ($0.92 \times 10^{-3} \rightarrow 0.33$) = more consistent experimental situation

There are new data of relevant processes, $B_c \rightarrow J/\psi \tau \nu$, $B \rightarrow X_c \tau \nu$ EPS2023

Wish list: CMS B-parking, further Belle II data, LHCb Run 2, BaBar

SM prediction

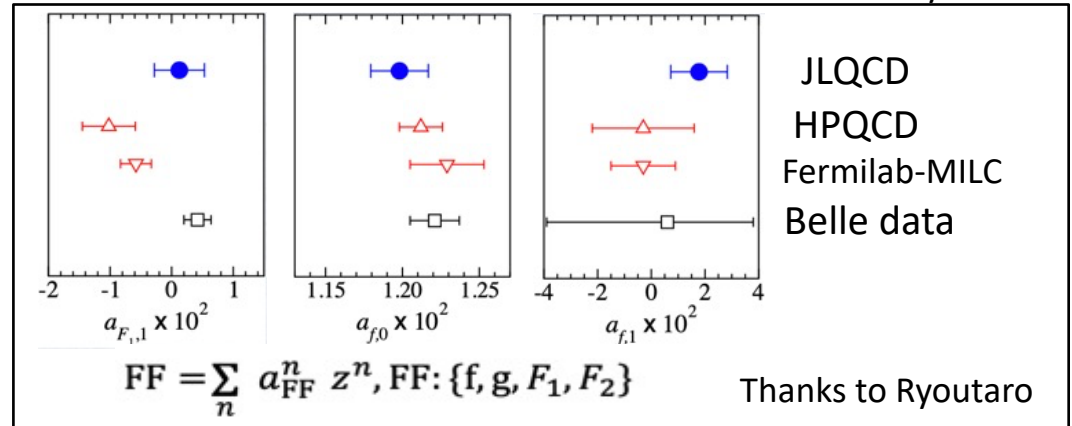
Reference	R_D	R_{D^*}
Bernlochner, <i>et al.</i>	0.288(4)	0.249(3)
Iguro, Watanabe	0.290(3)	0.248(1)
Bordone, <i>et al.</i>	0.298(3)	0.250(3)
HFLAV2023	0.298(4)	0.254(5)

looks relatively stable

See next talk by Prim

New Lattice results for B->D* are not conclusive

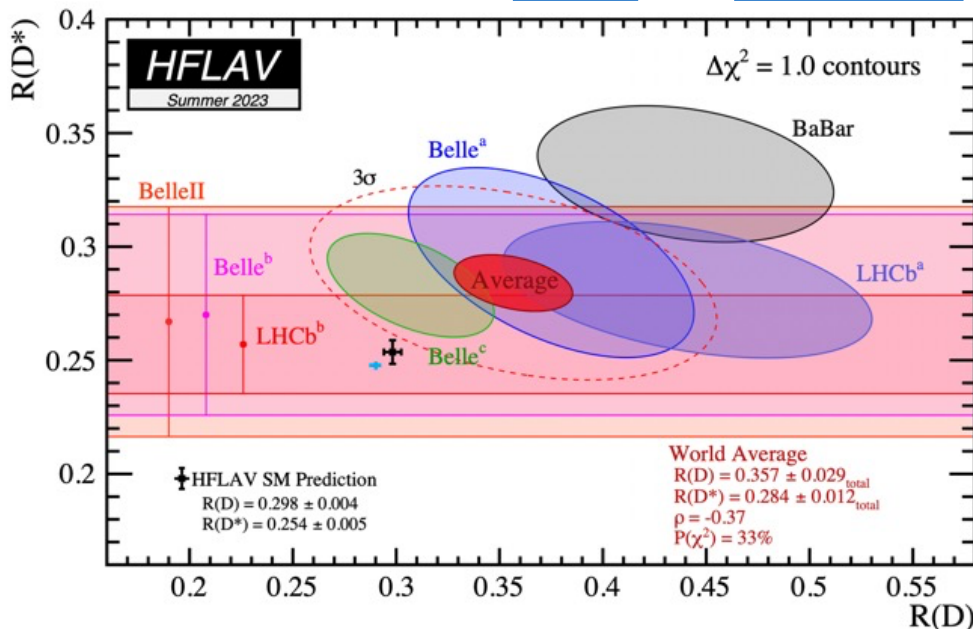
see talk by Kaneko



Regarding the inconsistency of dispersive method based on Fermilab-MILC see talk by Fedele

Current status

[HFLAV](#) and [2004.10208](#)



3.3-4 σ discrepancy

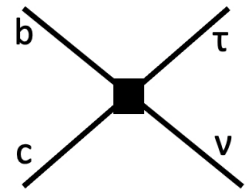
without BaBar $\sim 2.5-3.2\sigma$

Larger (smaller) discrepancy in R_D (R_{D^*}).

We will discuss implication to NP interpretation

Light lepton philic NP can not explain this

Effective Lagrangian for $b \rightarrow c \tau \nu$



$$H_{eff} = \frac{4G_F}{\sqrt{2}} V_{cb} [(1 + C_{VL})O_{VL} + C_{VR}O_{VR} + C_{SR}O_{SR} + C_{SL}O_{SL} + C_T O_T]$$

Dimension 6 due to the size of the discrepancy -> finite particle candidates

Operator basis

$$O_{SR} = (\bar{c} P_R b)(\bar{\tau} P_L \nu_\tau)$$

$$O_{SL} = (\bar{c} P_L b)(\bar{\tau} P_L \nu_\tau)$$

$$O_{VL} = (\bar{c} \gamma^\mu P_L b)(\bar{\tau} \gamma^\mu P_L \nu_\tau)$$

$$O_{VR} = (\bar{c} \gamma^\mu P_R b)(\bar{\tau} \gamma^\mu P_L \nu_\tau)$$

$$O_T = (\bar{c} \sigma^{\mu\nu} P_L b)(\bar{\tau} \sigma_{\mu\nu} P_L \nu_\tau)$$

candidates

Scalar

$$H^- \quad B_c^- \rightarrow \tau \bar{\nu}$$

Vector



Bs mixing
& $bb > \tau\tau$

Tensor

LQ

Relaxed $BR(B_c^- \rightarrow \tau \bar{\nu})$ bound

Previous constraint

~~< 30%~~ R.Alonso et al [1611.06676](#)

< 10% A.G.Akeroyd et al [1708.04702](#)

$\Gamma_{Bc} \propto m_Q^5$ + large error in charm mass
-> large error for Γ_{Bc}

Current constraint

B.Grinstein et al [2105.02988](#)

< 63% M.Blanke et al [1811.09603](#)

Summary of model prediction: correlation

Relaxed $B_c \rightarrow \tau\nu$ bound and shifted $R_{D^{(*)}}$

[2210.10751](#) (v3 soon)

	Spin	Charge	Operators	R_D	R_{D^*}	LHC	Flavor
<u>H^\pm</u>	0	$(\mathbf{1}, \mathbf{2}, 1/2)$	O_{SL}	✓	✓	$b\tau\nu$	$B_c \rightarrow \tau\nu, F_L^{D^*}, P_\tau^D, M_W$
S_1	0	$(\bar{\mathbf{3}}, \mathbf{1}, 1/3)$	O_{VL}, O_{SL}, O_T	✓	✓	$\tau\tau$	$\Delta M_s, P_\tau^D, B \rightarrow K^{(*)}\nu\nu$
$R_2^{(2/3)}$	0	$(\mathbf{3}, \mathbf{2}, 7/6)$	$O_{SL}, O_T, (O_{VR})$	✓	✓	$b\tau\nu, \tau\tau$	$R_{\Upsilon(nS)}, P_\tau^{D^*}, M_W$
<u>U_1</u>	1	$(\mathbf{3}, \mathbf{1}, 2/3)$	O_{VL}, O_{SR}	✓	✓	$b\tau\nu, \tau\tau$	$R_{K^{(*)}}, R_{\Upsilon(nS)}, B_s \rightarrow \tau\tau$
<u>$V_2^{(1/3)}$</u>	1	$(\bar{\mathbf{3}}, \mathbf{2}, 5/6)$	O_{SR}	✓	2σ	$\tau\tau$	$B \rightarrow \tau\nu, B_s \rightarrow \tau\tau, B \rightarrow K\tau\tau$

LQ

See also Angelescu et al, 2103.12504, Athron et al 2104.03691 for the previous version of LQs

$\text{Pull} \equiv \sqrt{\chi_{\text{SM}}^2 - \chi_{\text{NP-best}}^2} \ (\sigma)$
 based on $R_{D^{(*)}}, F_L^{D^*}$
 $\mu_b = \mu$

$C_{SL} = -0.88 \pm 0.88i$	Pull=4.3 σ	H^\pm
$C_{SL} = -8.9C_T = 0.19$	Pull=3.9 σ	S_1
$C_{SL} = 8.4C_T = -0.07 \pm 0.58i$	Pull=4.0 σ	R_2
$C_{VL} = 0.07 = C_{SR}/(-3.7) \times e^{-i\phi_R}, \phi_R = 0.54\pi$	Pull=4.1 σ	U_1
$C_{SR} = -0.2$	Pull=3.8 σ	V_2

Similar goodness of fit

Model discrimination is possible via these correlated predictions

Also, τ polarization in $B \rightarrow D^{(*)}\tau\nu$ is important @ Belle II

NP model dependent recent topics

- Revived Charged Higgs interpretation with sizable C_9



- Testing U_1 LQ with EDM experiments

- LHC proposal: $\tau\nu+b$ final state

- Another revival, V_2 leptoquark

If time allows



necromancer

Since the size of the deviation implies up to $O(1)$ TeV new particle, LHC searches should see something already or soon!

Scalar operator revived

Iguro [2201.06565](#)

$$O_{SL} = (\bar{c}P_L b)(\bar{\tau}P_L \nu_\tau)$$

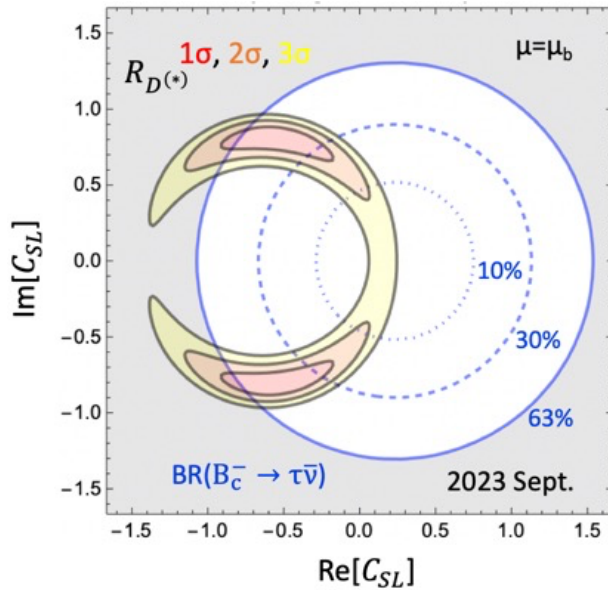
Thanks to the relaxed upper bound from $B_c^- \rightarrow \tau \bar{\nu}$ scalar scenario is still viable!

Only scalar can (slightly) enhance $F_L^{D^*}$

$$F_L^{D^* \text{ exp}} = 0.60 \pm 0.09, \quad F_L^{D^* \text{ SM}} = 0.46 \pm 0.01$$

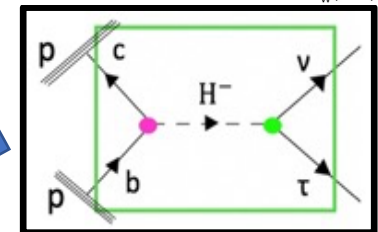
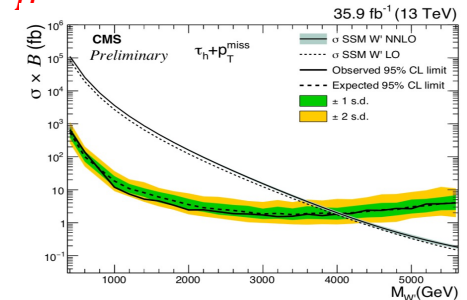
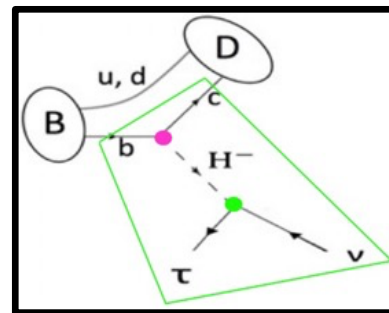
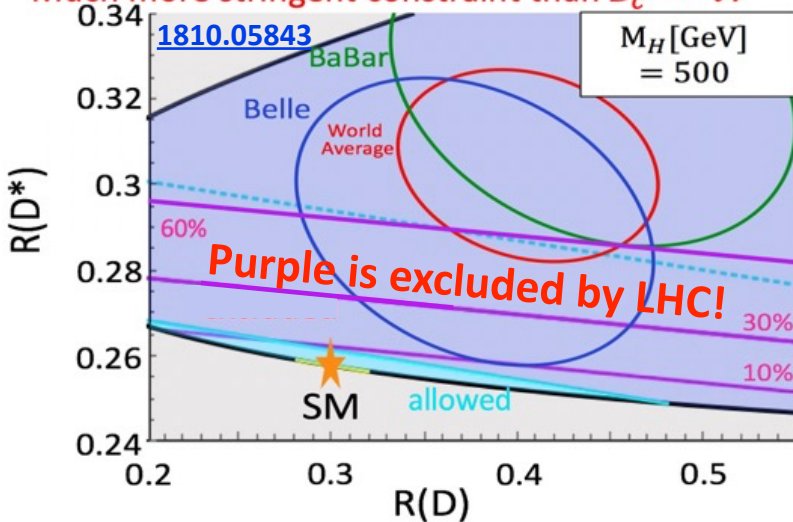
We need complex WC

=> Complex Yukawa in type III (General) 2HDM



Reinterpreting **tau resonance search** from the CMS(36fb⁻¹) excludes the scenario with $m_{H^+} > 400\text{GeV}$

Much more stringent constraint than $B_c^- \rightarrow \tau \bar{\nu}$



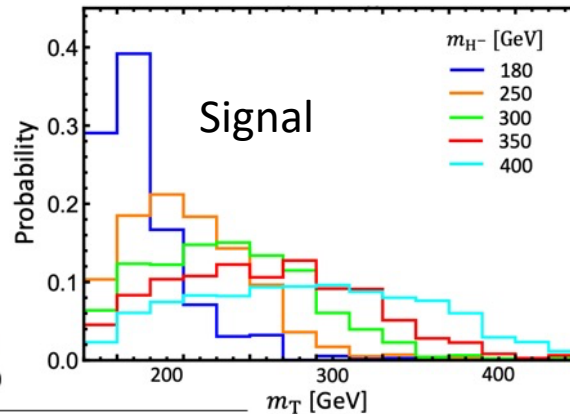
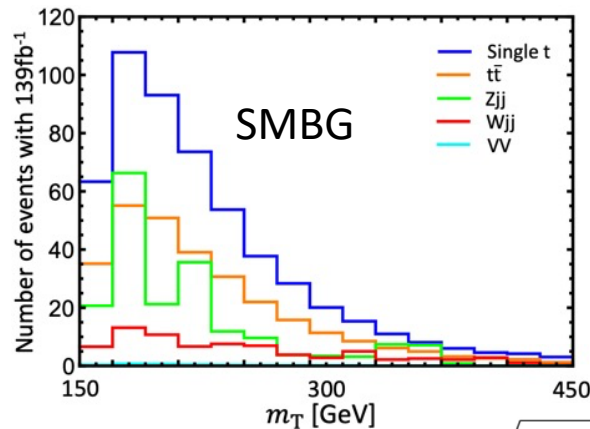
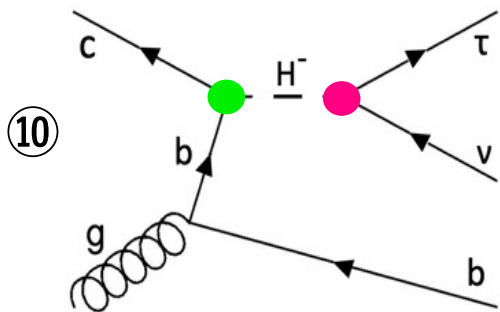
correlation

There is no data available for $m_{H^+} < 400\text{GeV}$ 8
Additional b-jet would suppress the trigger rate

Closing the low mass window with $\tau\nu+b$ search!

Iguro, Zhang, Blanke [2202.10468](#)

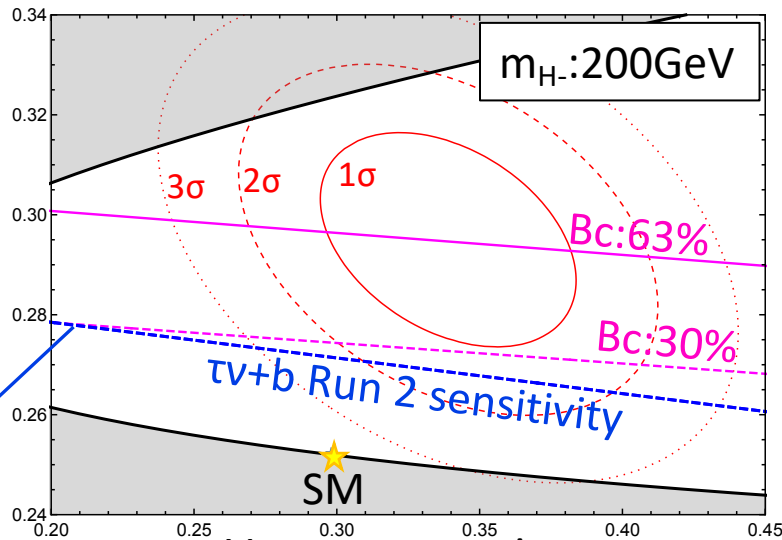
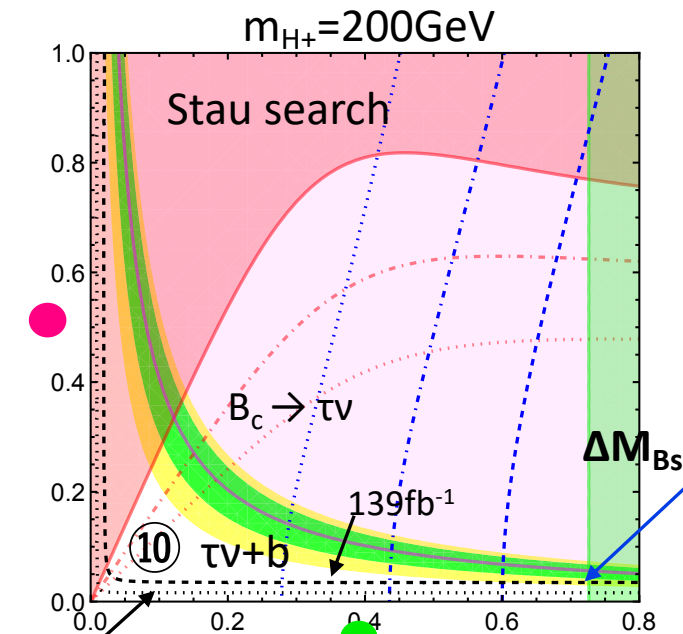
$180\text{GeV} < m_{H^+} < 400\text{GeV}$



b-tagging suppress the SMBG

$$m_T = \sqrt{2p_T^\ell E_T^{\text{miss}}(1 - \cos \theta_{\ell\nu})}$$

NP signal event number (with parameters to explain the anomaly) is comparable with SMBG!



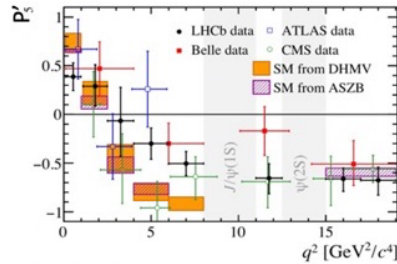
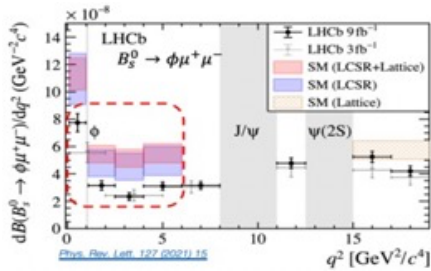
Very conservative syst. error is assigned
Heavier scenario is more easy due to smaller BG!

The current luminosity (139fb^{-1}) is already enough to judge the model!

Flavor universal C_9 ?

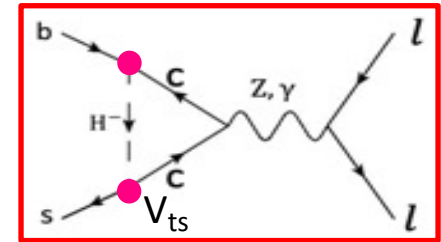
Iguro [2302.08935](#)

Iguro Omura [1802.01732](#)

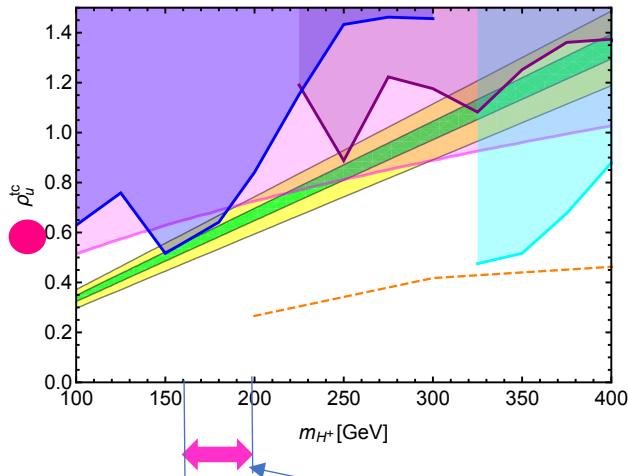


SU(2)_L doublet

$$\begin{pmatrix} H^+ \\ \frac{1}{\sqrt{2}}(H + iA) \end{pmatrix}$$



Parameter space



Green and yellow are interesting $C_9^U \sim -1 \pm 0.2$

Bs mixing and di-jet also put interesting constraints

Stringent upper bound from same sign top (SST) search [2307.14759](#)

Although this can be avoided by taking $m_A = m_H$ at O(1) GeV
 $m_{A,H} < m_t$ is also excluded by multi tau lepton search



O(1) GeV turning or $m_t < m_{A,H} < 200$ GeV

mass window

How to test the remaining mass window?

FCNC top production
($cg \rightarrow t + \tau\tau$)

Naïve Run 2 sensitivity:

100fb for $m_{\tau\tau} = 125$ GeV, [2011.03652](#) (CMS)

but we have heavier resonance -> small BG

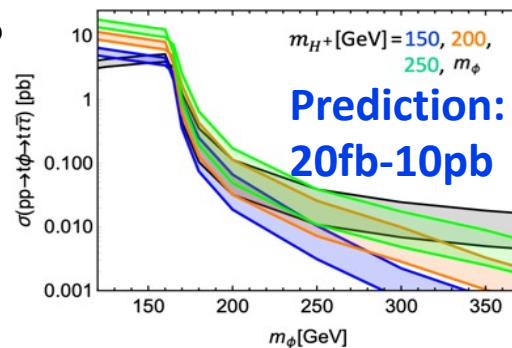
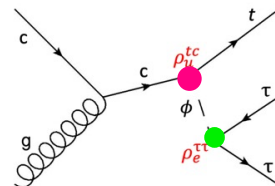
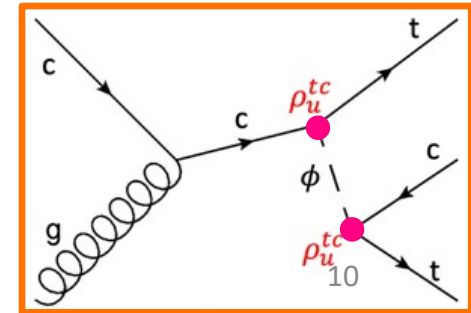


Diagram for SST



Bridging $R_D^{(*)}$ and EDMs

Iguro, Kitahara [2307.11751](#)

U(2) flavored U1 LQ : leading candidate (Zurich model)

Recent finding

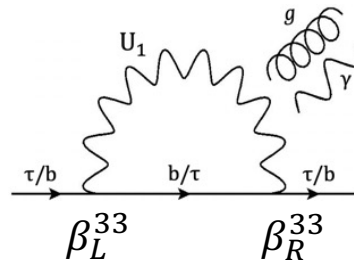
See also [2002.01400](#), [1809.09114](#)

$$\mathcal{L} \supset \left(\beta_L^{ij} \bar{Q}_i \gamma_\mu P_L L_j + \beta_R^{ij} \bar{d}_i \gamma_\mu P_R e_j \right) U_1^\mu + \text{h.c.}$$

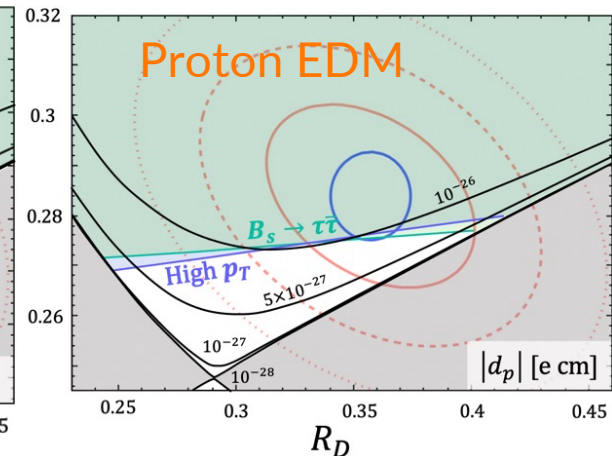
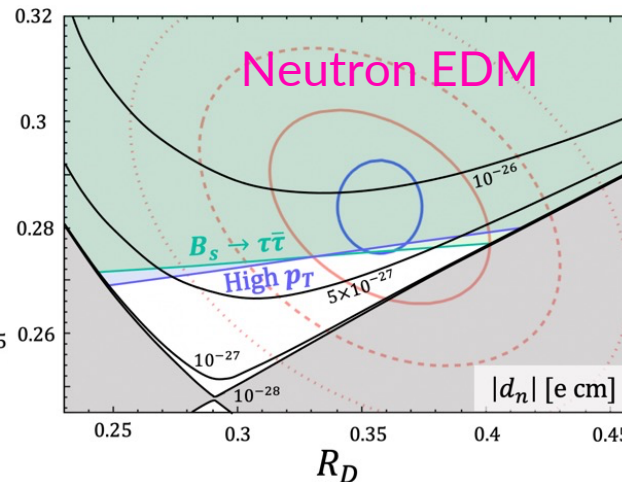
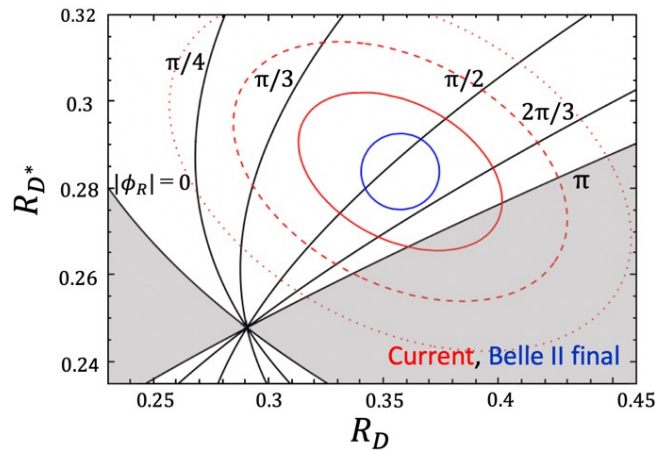
Javier, Claudia, Gino,, [1903.11517](#), [1909.02519](#),,,

$$\beta_L^{ij} \simeq \begin{pmatrix} 0 & 0 & -c_d s_{q_2} s_\chi \left| \frac{V_{td}}{V_{ts}} \right| \\ 0 & 0 & c_d s_{q_2} s_\chi \\ 0 & 0 & c_\chi \end{pmatrix}, \quad \beta_R^{ij} \simeq e^{i\phi_R} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix},$$

$$C_{S_R}(\mu_b) \simeq -3.7 e^{-i\phi_R} C_{V_L}(\mu_b)$$



Bottom induced Weinberg operator contributes to **neutron** and **proton** EDMs
Haisch, Hala [1909.08955](#)



$\phi_R=0$ is not good \Rightarrow CPV

$d_n \sim -d_p = \mathbf{O}(10^{-26 \sim 27})$ e cm, **well within future reach** while $d_e \sim \mathbf{O}(10^{-32})$ e cm

Bridging R_D^* and FDMs

Iguro, Kitahara 2307.11751

U(2) flavored U1 LQ : leading

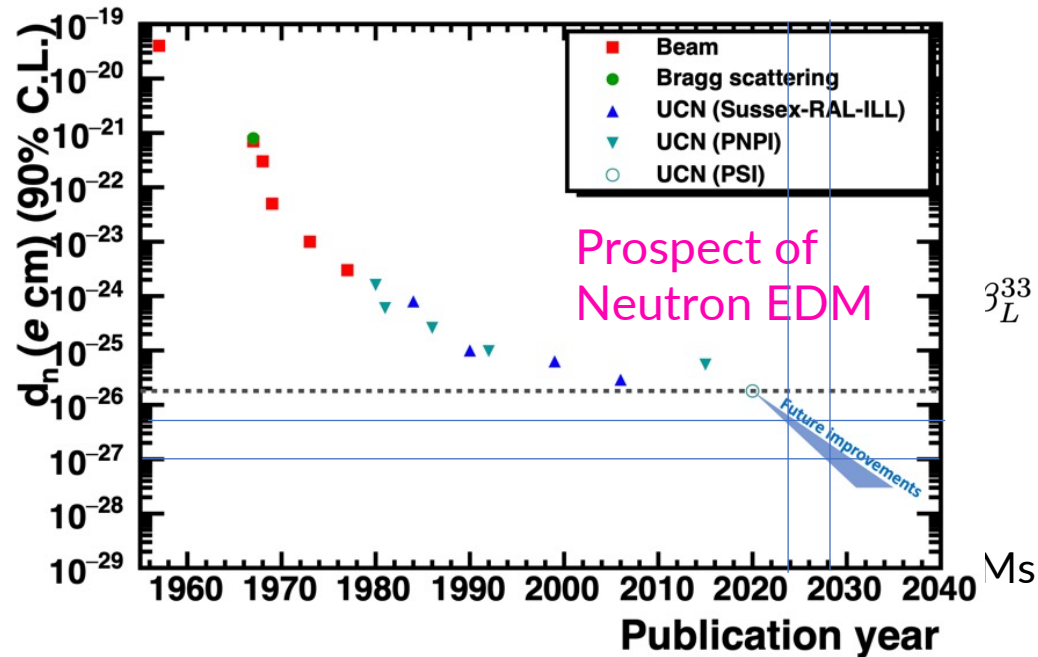
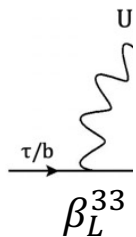
Recent finding

$$\mathcal{L} \supset \left(\beta_L^{ij} \bar{Q}_i \gamma_\mu P_L L_j + \beta_R^{ij} \bar{d}_i \gamma_\mu P_R e_j \right) U_1^\mu + \text{h.c.}$$

Javier, Claudia, Gino, 1903.11517, 1

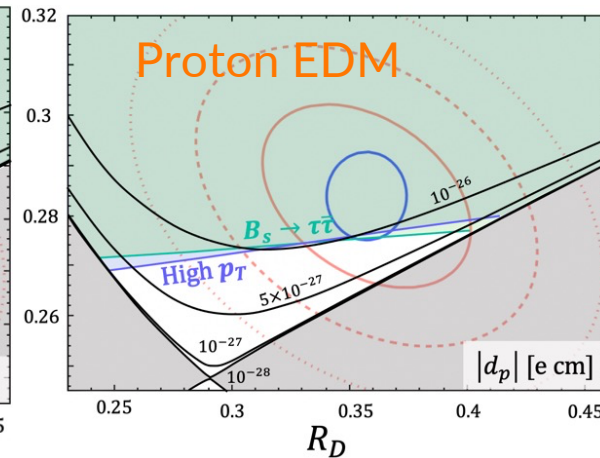
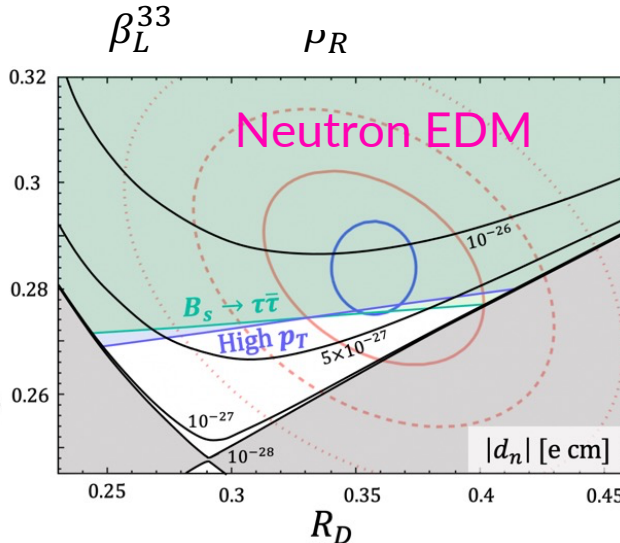
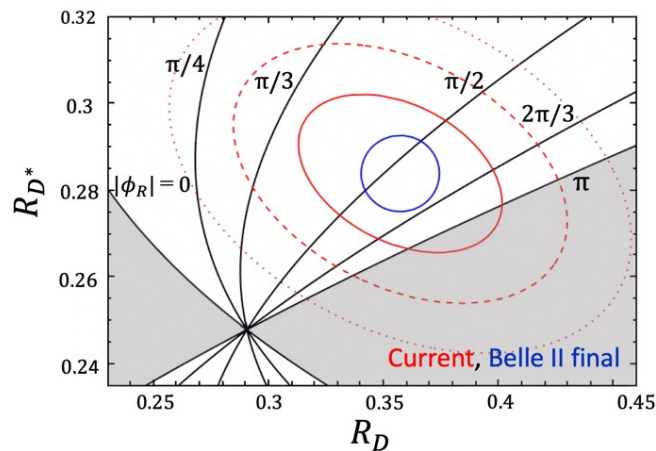


$$C_{SR}(\mu_b) \simeq -3.7 e^{-i\phi_R} C_{VL}(\mu_b)$$



${}^{33}_L$

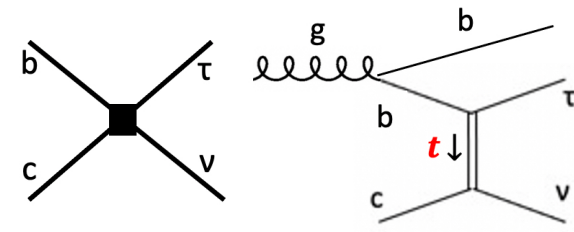
Ms



$\phi_R=0$ is not good => CPV

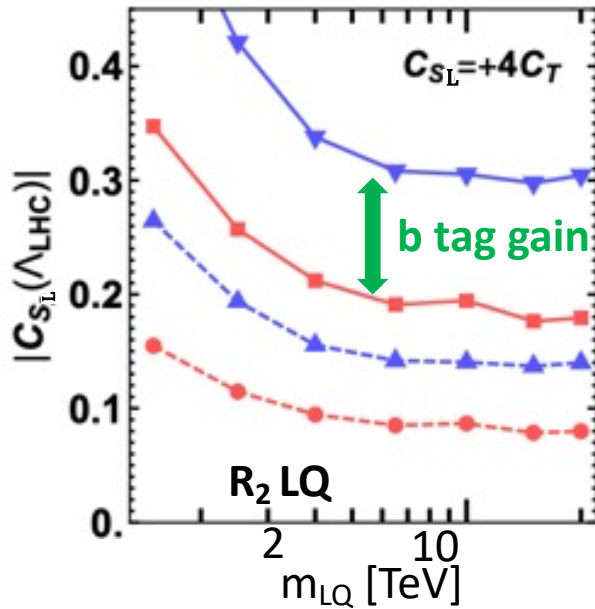
$d_n \sim -d_p = \mathcal{O}(10^{-26 \sim 27})$ e cm, well within future reach while $d_e \sim \mathcal{O}(10^{-32})$ e cm

Improving LHC search in $\tau\nu$ mode with again, additional b-tagging



A. Soni et al [1704.06659](#), Iguro-Tobe [1708.06176](#)

Significant mass dependence

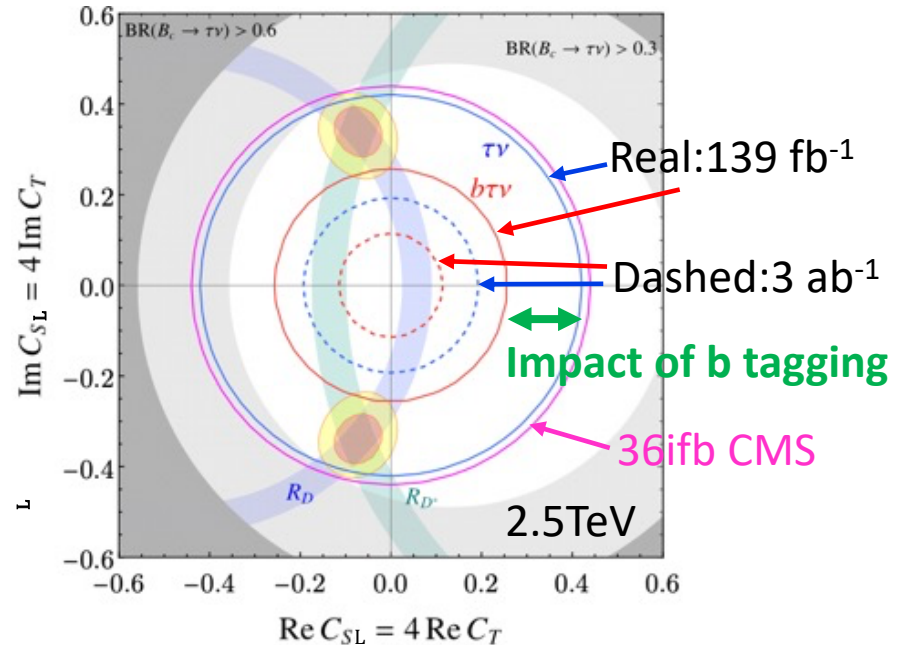


R₂ LQ

- 139 fb⁻¹: $\tau^{\pm}\nu$
- 139 fb⁻¹: $\tau^{\pm}\nu + b$
- 3000 fb⁻¹: $\tau^{\pm}\nu$
- 3000 fb⁻¹: $\tau^{\pm}\nu + b$

[2111.04748](#)

Outside of the circle can be probed!



See also [1811.07920](#), [2008.07541](#), [2206.09717](#)

Run 2 data is enough to judge the R₂ LQ scenario!

Comparable sensitivity with conventional $\tau+b$ searches
but not performed experimentally

excess in τ final state @CMS (not in $\tau + b$), no excess @ ATLAS

V₂ LQ solution for b → cτν

See also Kingman [2204.05942](#)
Iguro, Omura [2306.00052](#) (v2 soon)

V₂ ($\bar{3}, 2, 5/6$) contributes to $(\bar{c}P_R b)(\bar{\tau}P_L \nu)$: **this solution revived recently!**

$$\mathcal{L}_{V_2} = h_1^{ij} (\bar{d}_i^C \gamma_\mu P_L L_j^b) \varepsilon^{ab} V_2^{\mu,a} + h_2^{ij} (\bar{Q}_i^{C,a} \gamma_\mu P_R e_j) \varepsilon^{ab} V_2^{\mu,b} + h_3^{ij} (\bar{Q}_i^C \gamma_\mu P_R u_j) V_2^{\mu*} + \text{h.c.} \quad V_2 = \begin{pmatrix} V_2^{4/3} \\ V_2^{1/3} \end{pmatrix}$$

Assigning approximate τ number to this doublet the fermion interaction is given as

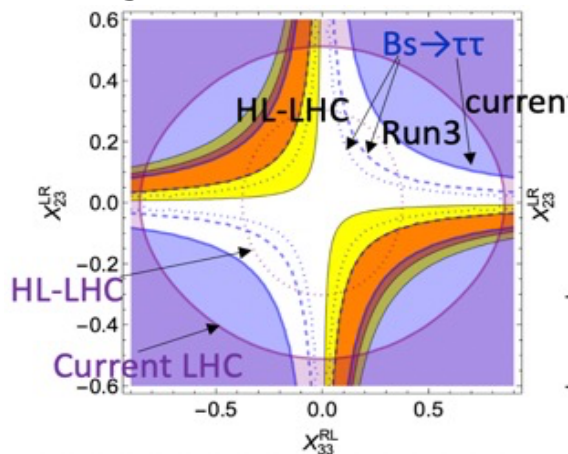
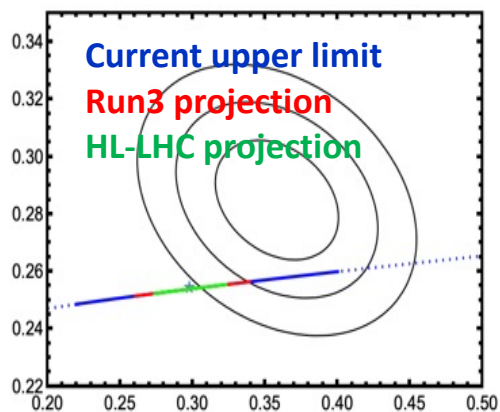
$$h_1^{ij} = \begin{pmatrix} 0 & 0 & h_1^{13} \\ 0 & 0 & h_1^{23} \\ 0 & 0 & \underline{h_1^{33}} \end{pmatrix}, \quad h_2^{ij} = \begin{pmatrix} 0 & 0 & h_2^{13} \\ 0 & 0 & \underline{h_2^{23}} \\ 0 & 0 & h_2^{33} \end{pmatrix}, \quad h_3 = 0.$$

proton decay, $K_L \rightarrow e\mu$ does not occur!
Bottom-up approach

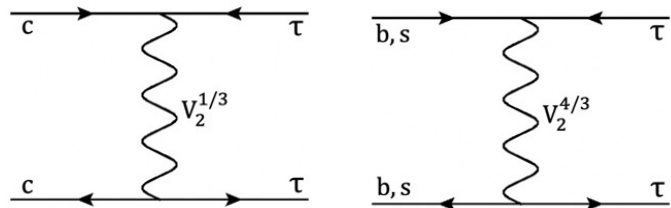
Relevant flavor processes

Coupling product	V ^{4/3}	V ^{1/3}
$h_1^{33} \times h_2^{23}$	$b \rightarrow s\tau\bar{\tau}$ $B_s \rightarrow \tau\bar{\tau}, B \rightarrow K\tau\bar{\tau}$	$b \rightarrow c\tau\bar{\nu}_\tau$ $B \rightarrow D^{(*)}\tau\bar{\nu}_\tau$ $B_c \rightarrow \tau\nu_\tau, B \rightarrow \tau\bar{\nu}$
$h_1^{33} \times h_2^{13}$	$b \rightarrow d\tau\bar{\tau}$ $B \rightarrow \tau\bar{\tau}, B \rightarrow \pi\tau\bar{\tau}$	$b \rightarrow u\tau\bar{\nu}_\tau$ $B \rightarrow D^{(*)}\tau\bar{\nu}_\tau$ $B \rightarrow \tau\nu_\tau, B \rightarrow \pi\tau\bar{\nu}_\tau$
$h_1^{33} \times h_2^{33}$	$b\bar{b} \rightarrow \tau\bar{\tau}$ $\Upsilon(nS) \rightarrow \tau\bar{\tau}$	$t \rightarrow b\tau\bar{\nu}_\tau$
$h_1^{33} \times h_1^{13}$	$b \rightarrow d\tau\bar{\tau}$ $B \rightarrow \tau\bar{\tau}, B \rightarrow \pi\tau\bar{\tau}$	$b \rightarrow d\nu\bar{\nu}$ $B \rightarrow \nu\bar{\nu}, B \rightarrow \pi\nu\bar{\nu}$
$h_1^{33} \times h_1^{23}$	$b \rightarrow s\tau\bar{\tau}$ $B_s \rightarrow \tau\bar{\tau}, B \rightarrow K\tau\bar{\tau}$	$b \rightarrow s\nu\bar{\nu}$ $B_s \rightarrow \nu\bar{\nu}, B \rightarrow K\nu\bar{\nu}$
$h_1^{13} \times h_2^{23}$	$s \rightarrow d\tau\bar{\tau}$	$c \rightarrow d\tau\bar{\nu}$ $D \rightarrow \tau\bar{\nu}$
$h_1^{23} \times h_2^{23}$	$s\bar{s} \rightarrow \tau\bar{\tau}$	$c \rightarrow s\tau\bar{\nu}$ $D_s \rightarrow \tau\bar{\nu}$
$h_2^{13} \times h_2^{23}$	$s \rightarrow d\tau\bar{\tau}$	$c \rightarrow u\tau\bar{\tau}$
$h_2^{33} \times h_2^{23}$	$b \rightarrow s\tau\bar{\tau}$ $B_s \rightarrow \tau\bar{\tau}, B \rightarrow K\tau\bar{\tau}$	$t \rightarrow c\tau\bar{\tau}$

Minimal scenario: $h_1^{33}, h_2^{23} \Rightarrow C_{SR}$



$B_s \rightarrow \tau\tau$ vs. $R_{D^{(*)}}$ $B \rightarrow K\tau\tau$ at Belle II is also important



LHC: di-tau final state

V₂ LQ solution for b → cτν

See also Kingman [2204.05942](#)
Iguro, Omura [2306.00052](#) (v2 soon)

V₂ ($\bar{3}, 2, 5/6$) contributes to $(\bar{c}P_R b)(\bar{\tau}P_L \nu)$: **this solution revived recently!**

$$\mathcal{L}_{V_2} = h_1^{ij} (\bar{d}_i^C \gamma_\mu P_L L_j^b) \varepsilon^{ab} V_2^{\mu,a} + h_2^{ij} (\bar{Q}_i^{C,a} \gamma_\mu P_R e_j) \varepsilon^{ab} V_2^{\mu,b} + h_3^{ij} (\bar{Q}_i^C \gamma_\mu P_R u_j) V_2^{\mu*} + \text{h.c.} \quad V_2 = \begin{pmatrix} V_2^{4/3} \\ V_2^{1/3} \end{pmatrix}$$

Assigning approximate τ number to this doublet the fermion interaction is given as

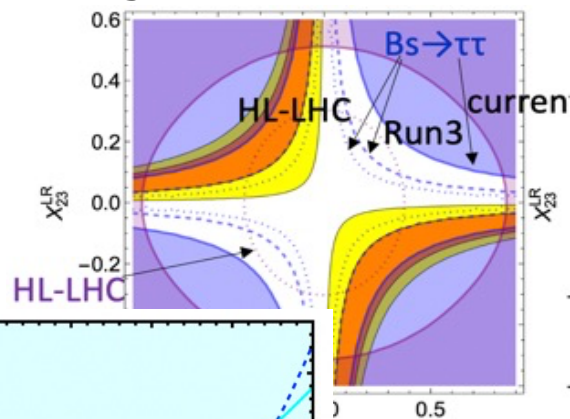
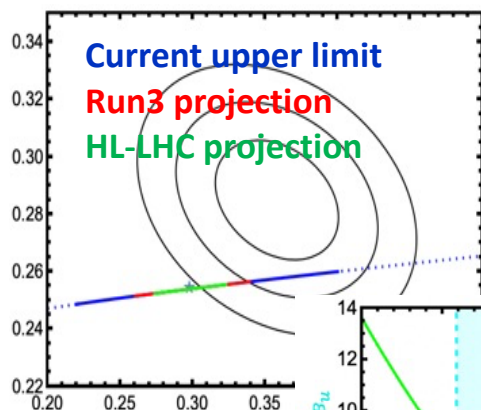
$$h_1^{ij} = \begin{pmatrix} 0 & 0 & h_1^{13} \\ 0 & 0 & h_1^{23} \\ 0 & 0 & \underline{h_1^{33}} \end{pmatrix}, \quad h_2^{ij} = \begin{pmatrix} 0 & 0 & h_2^{13} \\ 0 & 0 & \underline{h_2^{23}} \\ 0 & 0 & h_2^{33} \end{pmatrix}, \quad h_3 = 0.$$

proton decay, $K_L \rightarrow e\mu$ does not occur!
Bottom-up approach

Relevant flavor processes

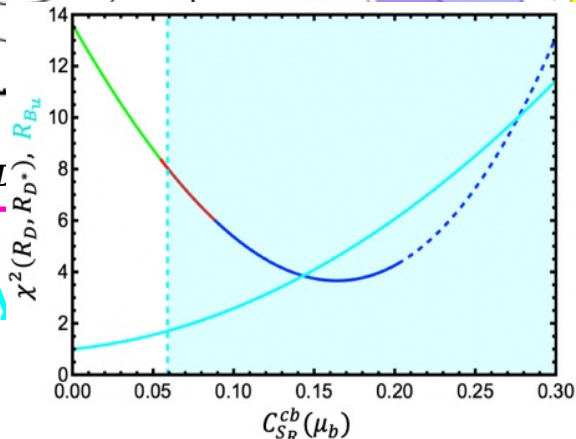
Coupling product	V ^{4/3}	V ^{1/3}
$h_1^{33} \times h_2^{23}$	$b \rightarrow s\tau\bar{\tau}$ $B_s \rightarrow \tau\bar{\tau}, B \rightarrow K\tau\bar{\tau}$	$b \rightarrow c\tau\bar{\nu}_\tau$ $B \rightarrow D^{(*)}\tau\bar{\nu}_\tau$ $B_c \rightarrow \tau\nu_\tau, B \rightarrow \tau\bar{\nu}$
$h_1^{33} \times h_2^{13}$	$b \rightarrow d\tau\bar{\tau}$ $B \rightarrow \tau\bar{\tau}, B \rightarrow \pi\tau\bar{\tau}$	$b \rightarrow u\tau\bar{\nu}_\tau$ $B \rightarrow D^{(*)}\tau\bar{\nu}_\tau$ $B \rightarrow \tau\nu_\tau, B \rightarrow \pi\tau\bar{\nu}_\tau$
$h_1^{33} \times h_2^{33}$	$b\bar{b} \rightarrow \tau\bar{\tau}$ $\Upsilon(nS) \rightarrow \tau\bar{\tau}$	$t \rightarrow b\tau\bar{\nu}_\tau$
$h_1^{33} \times h_1^{13}$	$b \rightarrow d\tau\bar{\tau}$ $B \rightarrow \tau\bar{\tau}, B \rightarrow \pi\tau\bar{\tau}$	$b \rightarrow d\nu\bar{\nu}$ $B \rightarrow \nu\bar{\nu}, B \rightarrow \pi\nu\bar{\nu}$
$h_1^{33} \times h_1^{23}$	$b \rightarrow s\tau\bar{\tau}$ $B_s \rightarrow \tau\bar{\tau}, B \rightarrow K\tau\bar{\tau}$	$b \rightarrow s\nu\bar{\nu}$ $B_s \rightarrow \nu\bar{\nu}, B \rightarrow K\nu\bar{\nu}$
$h_1^{13} \times h_2^{23}$	$s \rightarrow d\tau\bar{\tau}$	$c \rightarrow d\tau\bar{\nu}$ $D \rightarrow \tau\bar{\nu}$
$h_1^{23} \times h_2^{23}$	$s\bar{s} \rightarrow \tau\bar{\tau}$	$c \rightarrow s\tau\bar{\nu}$ $D_s \rightarrow \tau\bar{\nu}$
$h_2^{13} \times h_2^{23}$	$s \rightarrow d\tau\bar{\tau}$	$c \rightarrow u\tau\bar{\tau}$
$h_2^{33} \times h_2^{23}$	$b \rightarrow s\tau\bar{\tau}$ $B_s \rightarrow \tau\bar{\tau}, B \rightarrow K\tau\bar{\tau}$	$t \rightarrow c\tau\bar{\tau}$

Minimal scenario: $h_1^{33}, h_2^{23} \Rightarrow C_{SR}$



B_s → ττ vs. R_L, R_{Bu}

B_u → τν is key



$$R_{B_u} = BR(B_u \rightarrow \tau\nu) / BR(B_u \rightarrow \tau\nu)_{SM}$$

V₂ LQ solution for b → cτν

See also Kingman [2204.05942](#)
Iguro, Omura [2306.00052](#) (v2 soon)

V₂ (3̄, 2, 5/6) contributes to (c̄P_Rb)(τ̄P_Lν): this solution revived recently!

$$\mathcal{L}_{V_2} = h_1^{ij} (\overline{d_i^C} \gamma_\mu P_L L_j^b) \varepsilon^{ab} V_2^{\mu,a} + h_2^{ij} (\overline{Q_i^C} \gamma_\mu P_R e_j) \varepsilon^{ab} V_2^{\mu,b} + h_3^{ij} (\overline{Q_i^C} \gamma_\mu P_R u_j) V_2^{\mu,*} + \text{h.c.} \quad V_2 = \begin{pmatrix} V_2^{4/3} \\ V_2^{1/3} \end{pmatrix}$$

Assigning approximate τ number to this doublet the fermion interaction is given as

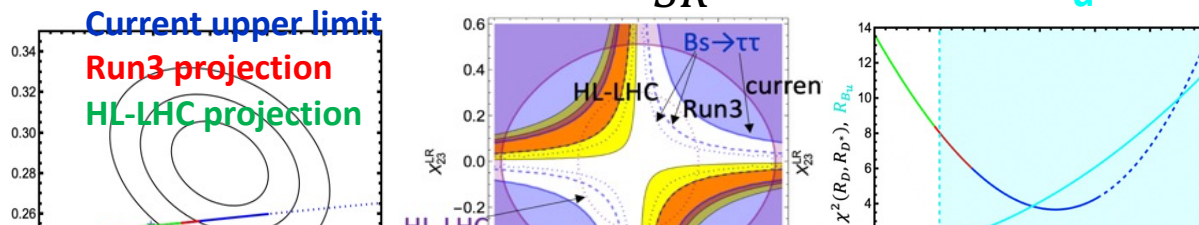
$$h_1^{ij} = \begin{pmatrix} 0 & 0 & h_1^{13} \\ 0 & 0 & h_1^{23} \\ 0 & 0 & h_1^{33} \end{pmatrix}, \quad h_2^{ij} = \begin{pmatrix} 0 & 0 & h_2^{13} \\ 0 & 0 & h_2^{23} \\ 0 & 0 & h_2^{33} \end{pmatrix}, \quad h_3 = 0.$$

proton decay, K_L → eμ does not occur!
Bottom-up approach

Relevant flavor processes

Coupling product	V ^{4/3}	V ^{1/3}
$h_1^{33} \times h_2^{23}$	$b \rightarrow s\tau\bar{\tau}$ $B_s \rightarrow \tau\bar{\tau}, B \rightarrow K\tau\bar{\tau}$	$b \rightarrow c\tau\bar{\nu}_\tau$ $B \rightarrow D^{(*)}\tau\bar{\nu}_\tau$ $B_c \rightarrow \tau\nu_\tau, B \rightarrow \tau\bar{\nu}$
$h_1^{33} \times h_2^{13}$	$b \rightarrow d\tau\bar{\tau}$ $B \rightarrow \tau\bar{\tau}, B \rightarrow \pi\tau\bar{\tau}$	$b \rightarrow u\tau\bar{\nu}_\tau$ $B \rightarrow D^{(*)}\tau\bar{\nu}_\tau$ $B \rightarrow \tau\nu_\tau, B \rightarrow \pi\tau\bar{\nu}_\tau$
$h_1^{33} \times h_2^{33}$	$b\bar{b} \rightarrow \tau\bar{\tau}$ $\Upsilon(nS) \rightarrow \tau\bar{\tau}$	$t \rightarrow b\tau\bar{\nu}_\tau$ —
$h_1^{33} \times h_1^{13}$	$b \rightarrow d\tau\bar{\tau}$ $B \rightarrow \tau\bar{\tau}, B \rightarrow \pi\tau\bar{\tau}$	$b \rightarrow d\nu\bar{\nu}$ $B \rightarrow \nu\bar{\nu}, B \rightarrow \pi\nu\bar{\nu}$
$h_1^{33} \times h_1^{23}$	$b \rightarrow s\tau\bar{\tau}$ $B_s \rightarrow \tau\bar{\tau}, B \rightarrow K\tau\bar{\tau}$	$b \rightarrow s\nu\bar{\nu}$ $B_s \rightarrow \nu\bar{\nu}, B \rightarrow K\nu\bar{\nu}$
$h_1^{13} \times h_2^{23}$	$s \rightarrow d\tau\bar{\tau}$ —	$c \rightarrow d\tau\bar{\nu}$ $D \rightarrow \tau\bar{\nu}$
$h_1^{23} \times h_2^{23}$	$s\bar{s} \rightarrow \tau\bar{\tau}$ —	$c \rightarrow s\tau\bar{\nu}$ $D_s \rightarrow \tau\bar{\nu}$
$h_2^{13} \times h_2^{23}$	$s \rightarrow d\tau\bar{\tau}$ —	$c \rightarrow u\tau\bar{\tau}$ —
$h_2^{33} \times h_2^{23}$	$b \rightarrow s\tau\bar{\tau}$ $B_s \rightarrow \tau\bar{\tau}, B \rightarrow K\tau\bar{\tau}$	$t \rightarrow c\tau\bar{\tau}$ —

Minimal scenario: $h_1^{33}, h_2^{23} \Rightarrow C_{SR}$ is excluded by $B_u \rightarrow \tau\nu$

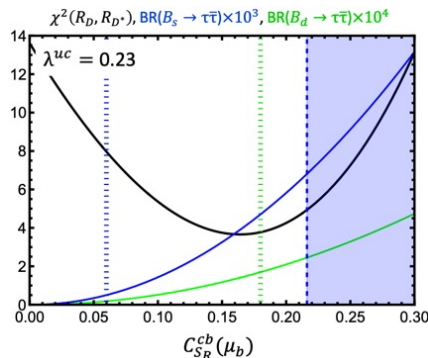
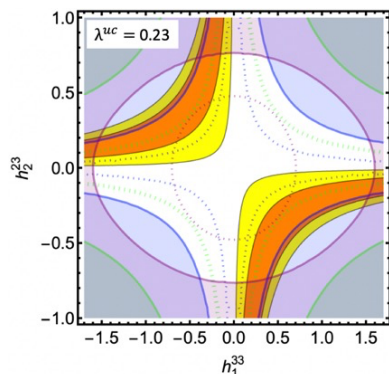


Next to minimal scenario: $h_1^{33}, h_2^{23}, h_2^{13}$ can explain $R_{D^{(*)}}$

$$h_2^{23} = -\lambda_{uc} h_2^{13}$$

$\lambda_{uc} = 0.23$
cancels $B_u \rightarrow \tau\nu$

$0.16 < \lambda_{uc} < 0.37$
is allowed for
2σ explanation



V₂ LQ solution for b → cτν

See also Kingman [2204.05942](#)
Iguro, Omura [2306.00052](#) (v2 soon)

V₂ (3̄, 2, 5/6) contributes to (c̄P_Rb)(τ̄P_Lν): this solution revived recently!

$$\mathcal{L}_{V_2} = h_1^{ij} (\bar{d}_i^C \gamma_\mu P_L L_j^b) \varepsilon^{ab} V_2^{\mu,a} + h_2^{ij} (\bar{Q}_i^{C,a} \gamma_\mu P_R e_j) \varepsilon^{ab} V_2^{\mu,b} + h_3^{ij} (\bar{Q}_i^C \gamma_\mu P_R u_j) V_2^{\mu,*} + \text{h.c.} \quad V_2 = \begin{pmatrix} V_2^{4/3} \\ V_2^{1/3} \end{pmatrix}$$

Assigning approximate τ number to this doublet the fermion interaction is given as

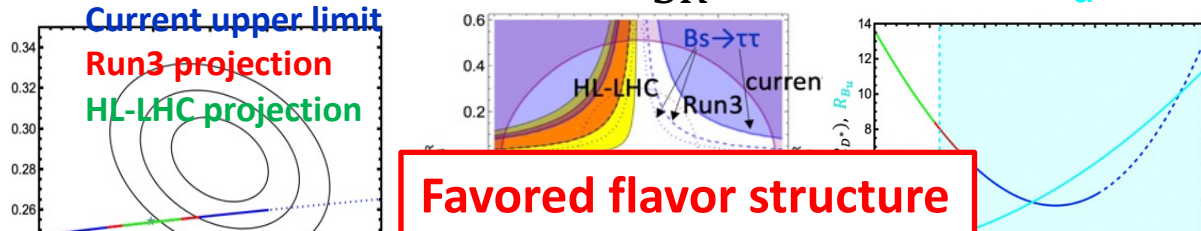
$$h_1^{ij} = \begin{pmatrix} 0 & 0 & h_1^{13} \\ 0 & 0 & h_1^{23} \\ 0 & 0 & h_1^{33} \end{pmatrix}, \quad h_2^{ij} = \begin{pmatrix} 0 & 0 & h_2^{13} \\ 0 & 0 & h_2^{23} \\ 0 & 0 & h_2^{33} \end{pmatrix}, \quad h_3 = 0.$$

proton decay, K_L → eμ does not occur!
Bottom-up approach

Relevant flavor processes

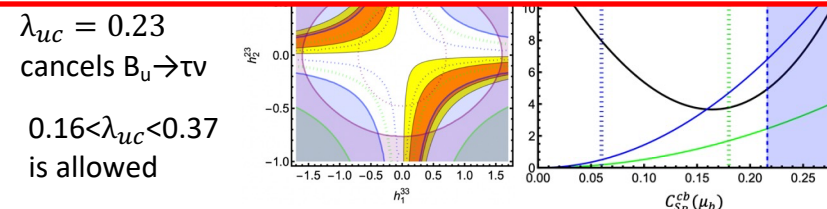
Coupling product	V ^{4/3}	V ^{1/3}
$h_1^{33} \times h_2^{23}$	$b \rightarrow s\tau\bar{\tau}$ $B_s \rightarrow \tau\bar{\tau}, B \rightarrow K\tau\bar{\tau}$	$b \rightarrow c\tau\bar{\nu}_\tau$ $B \rightarrow D^{(*)}\tau\bar{\nu}_\tau$ $B_c \rightarrow \tau\nu_\tau, B \rightarrow \tau\bar{\nu}$
$h_1^{33} \times h_2^{13}$	$b \rightarrow d\tau\bar{\tau}$ $B \rightarrow \tau\bar{\tau}, B \rightarrow \pi\tau\bar{\tau}$	$b \rightarrow u\tau\bar{\nu}_\tau$ $B \rightarrow D^{(*)}\tau\bar{\nu}_\tau$ $B \rightarrow \tau\nu_\tau, B \rightarrow \pi\tau\bar{\nu}_\tau$
$h_1^{33} \times h_2^{33}$	$b\bar{b} \rightarrow \tau\bar{\tau}$ $\Upsilon(nS) \rightarrow \tau\bar{\tau}$	$t \rightarrow b\tau\bar{\nu}_\tau$ —
$h_1^{33} \times h_1^{13}$	$b \rightarrow d\tau\bar{\tau}$ $B \rightarrow \tau\bar{\tau}, B \rightarrow \pi\tau\bar{\tau}$	$b \rightarrow d\nu\bar{\nu}$ $B \rightarrow \nu\bar{\nu}, B \rightarrow \pi\nu\bar{\nu}$
$h_1^{33} \times h_1^{23}$	$b \rightarrow s\tau\bar{\tau}$ $B_s \rightarrow \tau\bar{\tau}, B \rightarrow K\tau\bar{\tau}$	$b \rightarrow s\nu\bar{\nu}$ $B_s \rightarrow \nu\bar{\nu}, B \rightarrow K\nu\bar{\nu}$
$h_1^{13} \times h_2^{23}$	$s \rightarrow d\tau\bar{\tau}$ —	$c \rightarrow d\tau\bar{\nu}$ $D \rightarrow \tau\bar{\nu}$
$h_1^{23} \times h_2^{23}$	$s\bar{s} \rightarrow \tau\bar{\tau}$ —	$c \rightarrow s\tau\bar{\nu}$ $D_s \rightarrow \tau\bar{\nu}$
$h_2^{13} \times h_2^{23}$	$s \rightarrow d\tau\bar{\tau}$ —	$c \rightarrow u\tau\bar{\tau}$ —
$h_1^{33} \times h_2^{23}$	$b \rightarrow s\tau\bar{\tau}$	$t \rightarrow c\tau\bar{\tau}$

Minimal scenario: $h_1^{33}, h_2^{23} \Rightarrow C_{SR}$ is excluded by $B_u \rightarrow \tau\nu$



Favored flavor structure

$$h_1^{ij} \simeq \begin{pmatrix} 0 & 0 & \mathcal{O}(10^{-3}) \\ 0 & 0 & \mathcal{O}(10^{-2}) \\ 0 & 0 & \mathcal{O}(1) \end{pmatrix}, \quad h_2^{ij} \simeq \begin{pmatrix} 0 & 0 & -0.23h_2^{23} \\ 0 & 0 & \mathcal{O}(1) \\ 0 & 0 & \mathcal{O}(0.1) \end{pmatrix}$$



Construction of an UV model is necessary
Then loop induced obs. should be calculated

Summary

To be honest I thought that there is nothing to do more (Feb. 2022)

- Situation has been changed gradually with new experimental data, Lattice input,,,
- Discrepancy in R_D, R_{D^*} remains but scalar contribution would be more interesting
- Key predictions of H^+ solution to R_D, R_{D^*} and C_9 is found
- Connection to nucleon EDM is clarified within $U(2)$ flavored U_1 LQ model
- $\tau\nu+b$ provide a powerful collider probe
- V_2 LQ model now is possible to explain the anomaly and $b \rightarrow s\tau\tau$ is key process

Implication of $\Lambda_b \rightarrow \Lambda_c \tau\nu$ data and $b \rightarrow c\tau\nu$ sum rule, see Marco's talk

Stay tuned for new inputs from LHC, B-factories

Backyard start from the next

Apology: sorry for forgetting your papers

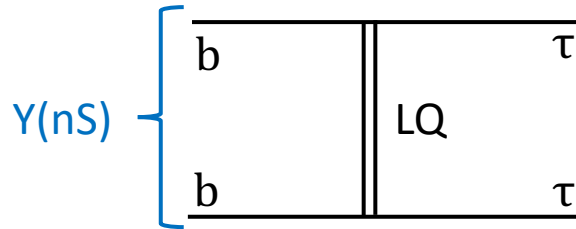
New process: LFUV in Upsilon decay

Upsilon $\Upsilon(nS)$ [$n=1,2,3,\dots$] is $b\bar{b}$ resonance

See also D. Aloni. et al 1702.07356

Leptonic decays of $\Upsilon(nS)$ provides new LFU test of $b\bar{b} \rightarrow \tau\bar{\tau}$

$$R_{\Upsilon(nS)} = \frac{\mathcal{B}(\Upsilon(nS) \rightarrow \tau^+\tau^-)}{\mathcal{B}(\Upsilon(nS) \rightarrow \ell^+\ell^-)},$$



$$R_{\Upsilon(3S)}^{\text{exp}} = 0.968 \pm 0.016 \quad R_{\Upsilon(3S)}^{\text{SM}} = 0.9948 \pm \mathcal{O}(10^{-5})$$

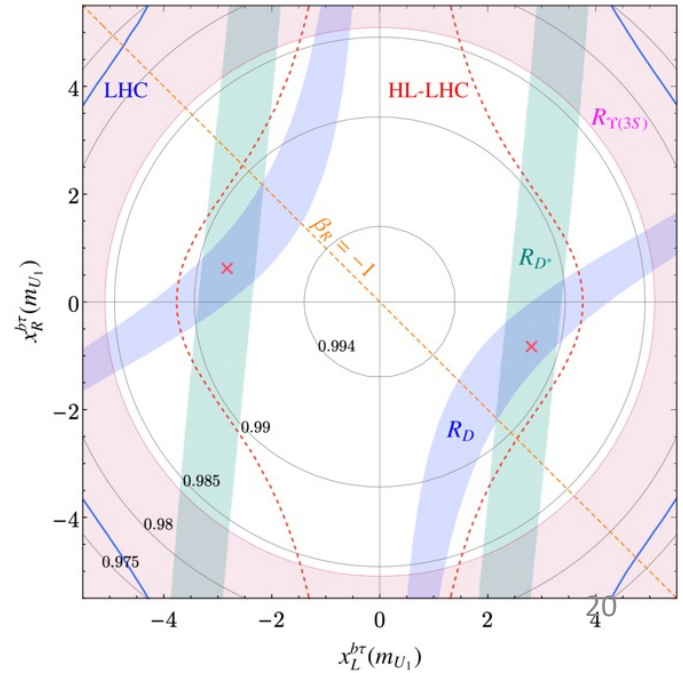
BaBar+CLEO

Systematic dominant

Nevertheless Belle II can improve

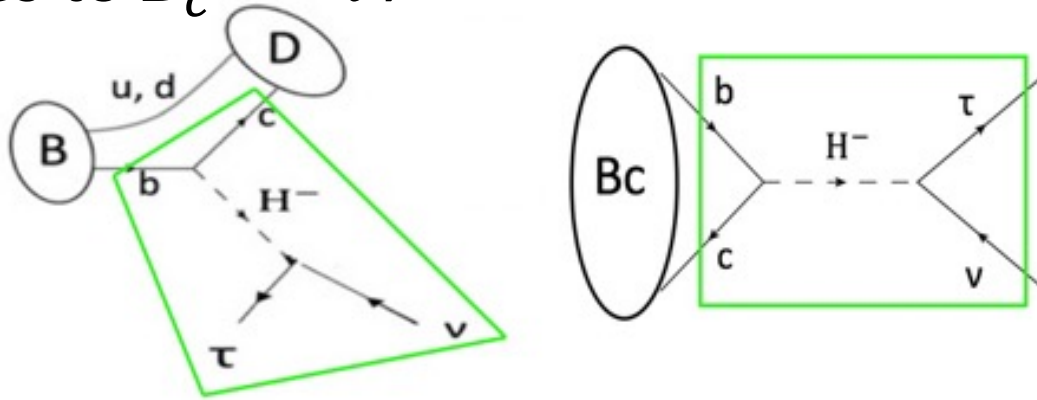
Less than 1% accuracy is necessary

For instance U_1 LQ scenario predicts $\sim 1\%$ deviation



Importance of $B_c^- \rightarrow \tau \bar{\nu}$ bound

Vector and scalar operators for $R(D^{(*)})$ automatically contributes to $B_c^- \rightarrow \tau \bar{\nu}$



$BR(B_c^- \rightarrow \tau \bar{\nu}) =$

$$BR(B_c^- \rightarrow \tau \bar{\nu})_{SM} \times \left| 1 + C_{V1} - C_{V2} + \frac{m_{B_c}^2}{m_\tau(m_b + m_c)} (C_{S1} - C_{S2}) \right|^2$$

$BR(B_c^- \rightarrow \tau \bar{\nu})_{SM} = 2\%$

~ 4.35

Scalar operator drastically enhances $BR(B_c^- \rightarrow \tau \bar{\nu})$

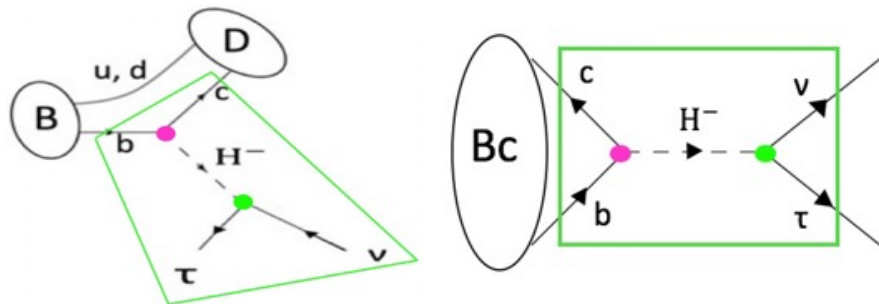
Limitation of the bound:

charm mass uncertainty, LEP data of $N(B, B_c \rightarrow \tau \bar{\nu})$

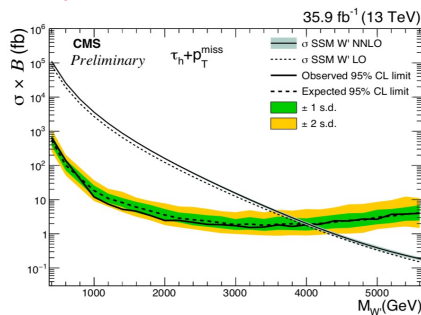
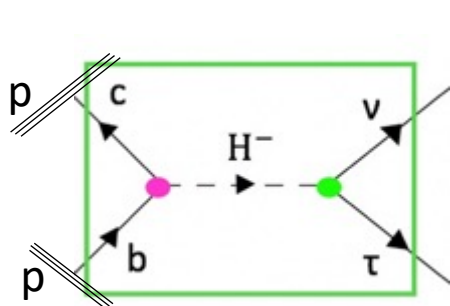
H⁻ interpretation of R_D, R_D* anomalies silently revived

Summary of the status and prospect are discussed

Syuhei Iguro, 2201.06565



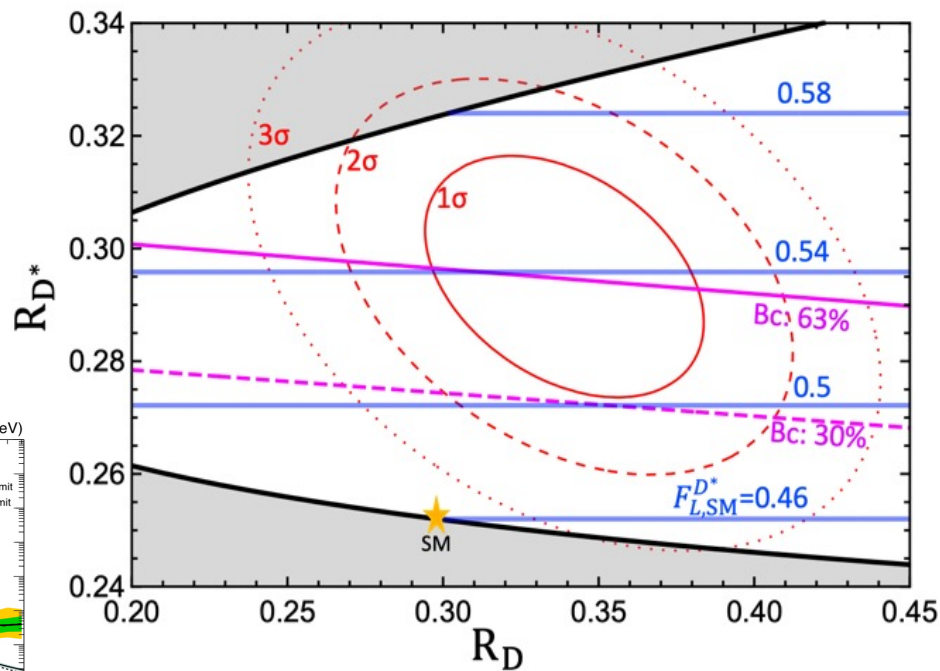
Due to the charm mass scheme dependence,
The bound is relaxed $BR(Bc \rightarrow \tau\nu) < 63\%$ Grinstein 2021



$\tau\nu$ resonance search at LHC gives more stringent constraint for $m_{H^-} > 400\text{GeV}$ Iguro 2018

$\tau\nu$ resonance search result for $m_{H^-} < 400\text{GeV}$ is not available at $\sqrt{s}=13\text{TeV}$ probably because

- they originally search for W' in SSM and wanted to push up the lower bound on $m_{W'}$
- SMBG ($W \rightarrow \tau\nu$ tail) is huge at low m_T

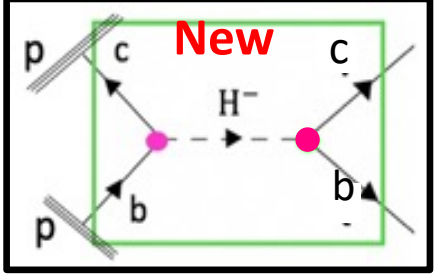
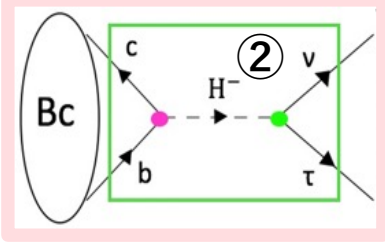
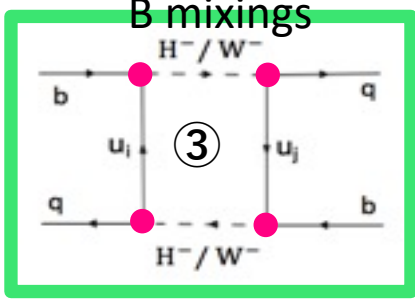
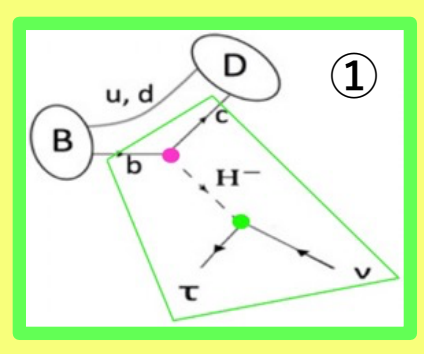


$$F_{L,SM}^{D^*} = 0.46, F_{L,Belle}^{D^*} = 0.60 \pm 0.09$$

Only scalar can enhance $F_L^{D^*}$

How is the situation and prospect for $m_{H^-} < 400\text{GeV}$?

Various bounds are very complementary
HL-LHC can probe large parameter space!



3 categories of bounds

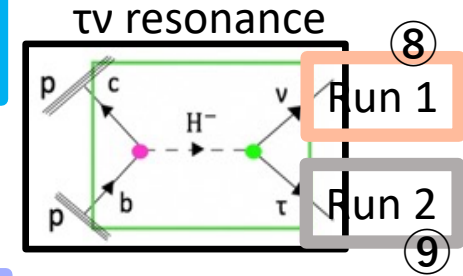
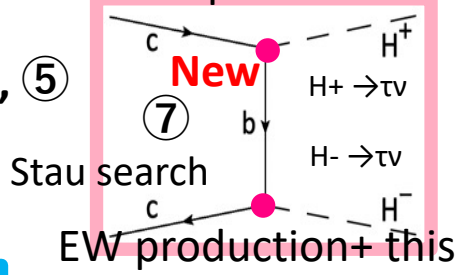
- 1. right to left e.g. ③, ④, ⑤
- 2. above to below ⑦
- 3. constrain \angle e.g. ②

bb resonance search
 $\sqrt{s}=8\text{TeV}$ ④

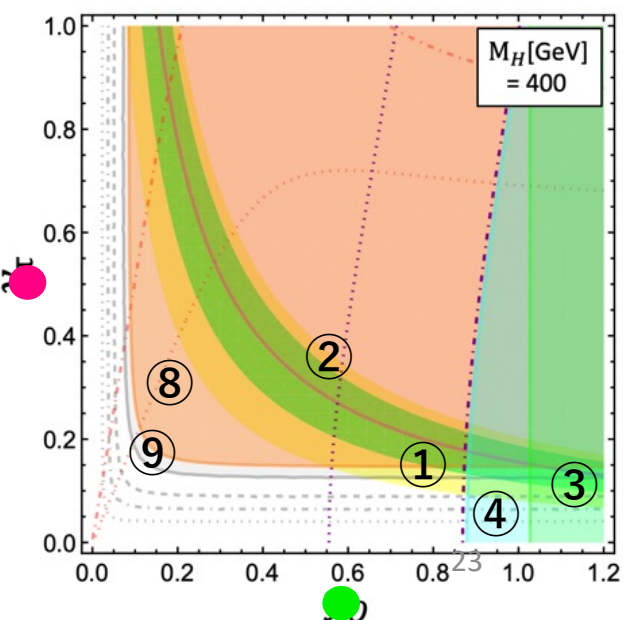
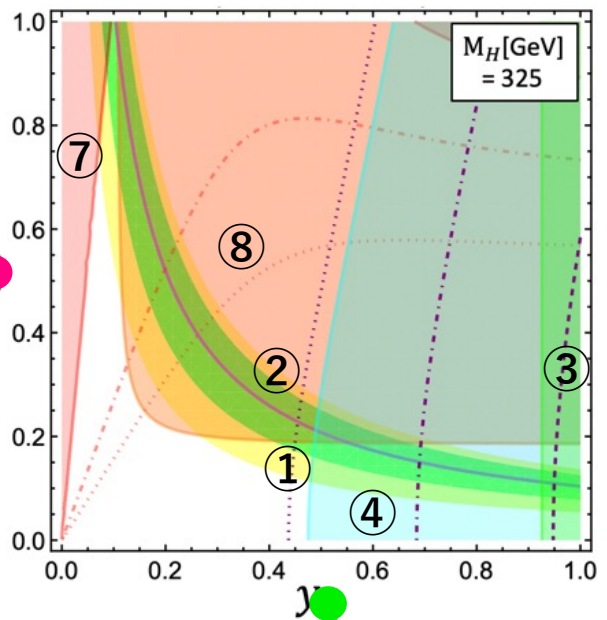
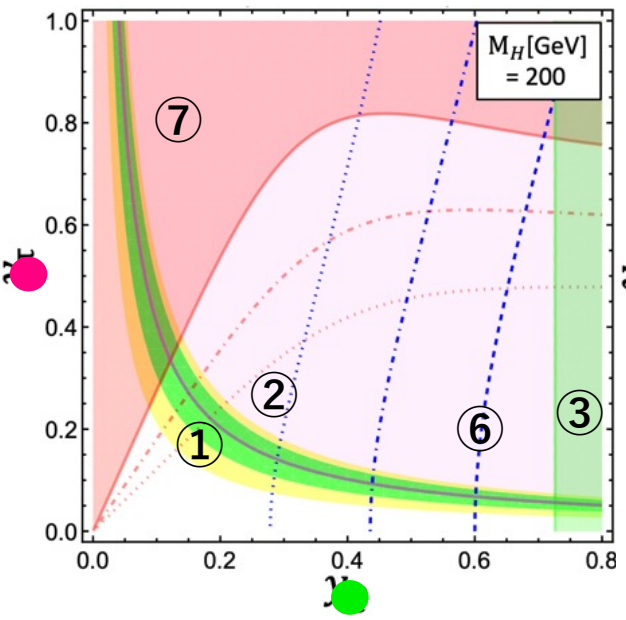
bb + photon search
 $\sqrt{s}=13\text{TeV}$ ⑤

Flavor inclusive di-jet
 $\sqrt{s}=13\text{TeV}$ ⑥

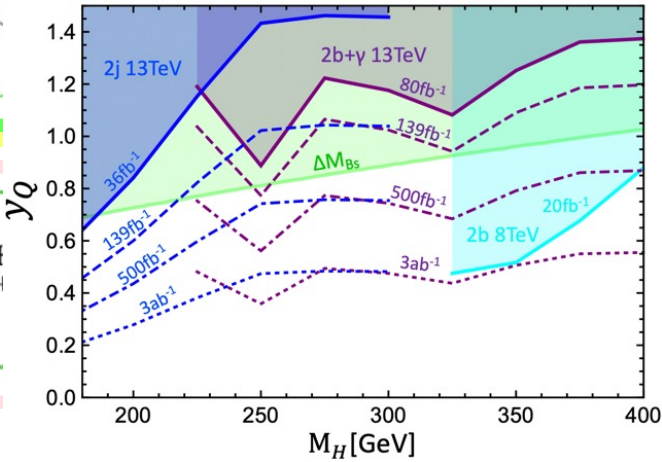
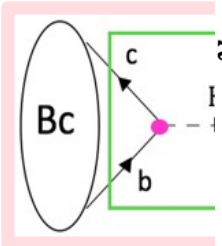
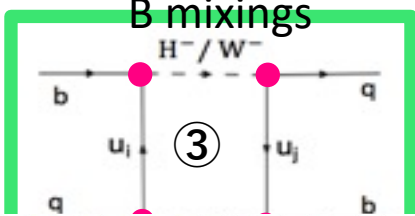
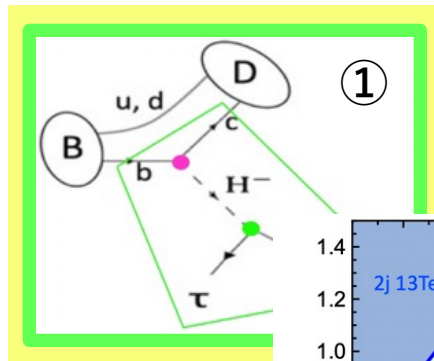
Pair production



Luminosity
 — Current — · · · 500fb⁻¹
 - - - 139fb⁻¹ ····· 3ab⁻¹



Various bounds are very complementary
HL-LHC can probe large parameter space!



3 categories of bounds

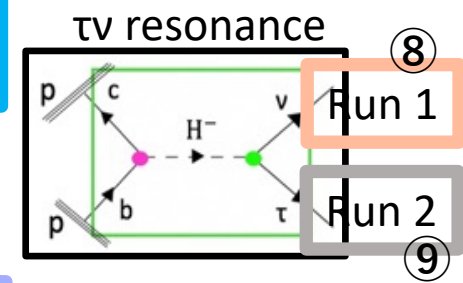
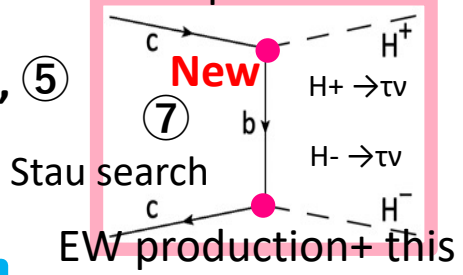
1. right to left e.g. ③, ④, ⑤
2. above to below ⑦
3. constrain \sphericalangle e.g. ②

bb resonance search
 $\sqrt{s}=8\text{TeV}$ ④

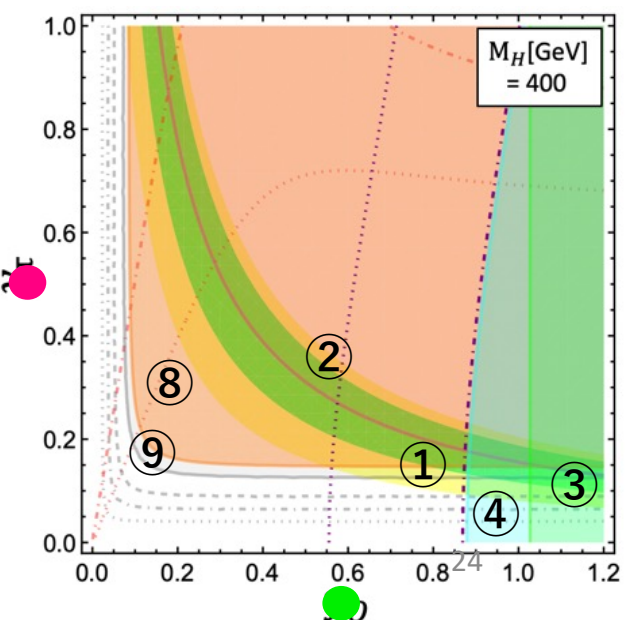
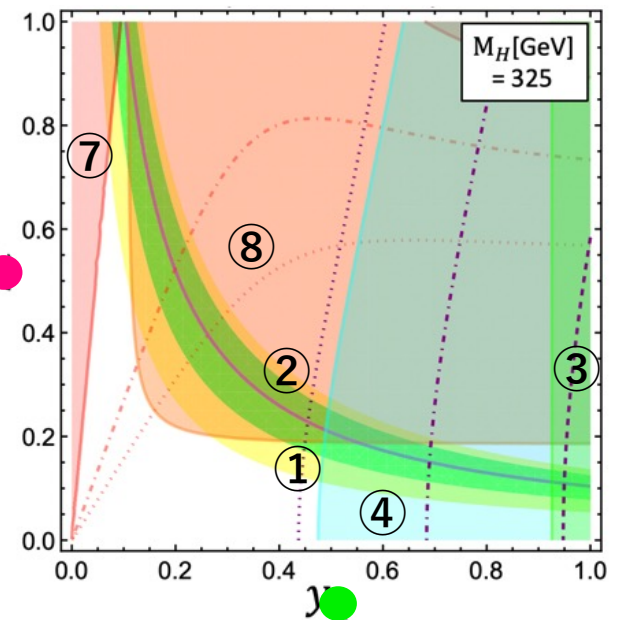
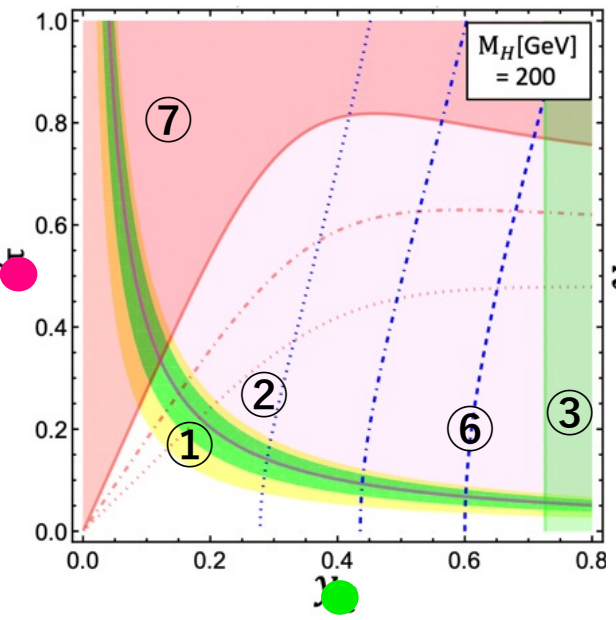
bb + photon search
 $\sqrt{s}=13\text{TeV}$ ⑤

Flavor inclusive di-jet
 $\sqrt{s}=13\text{TeV}$ ⑥

Pair production



Luminosity
— Current — · · · 500fb⁻¹
- - - 139fb⁻¹ ····· 3ab⁻¹

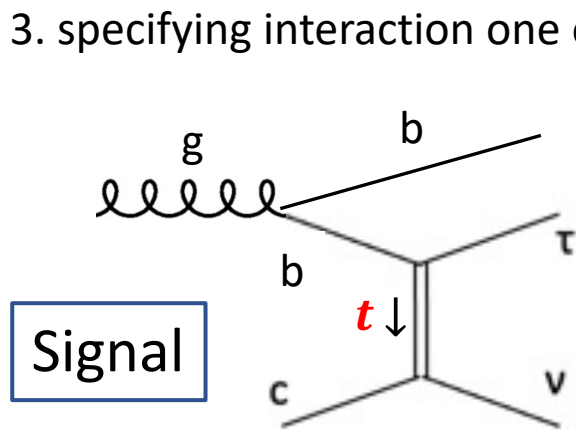


Improving LHC search in $\tau\nu$ mode

again, additional b-tagging A. Soni et al [1704.06659](#), Iguro-Tobe [1708.06176](#)

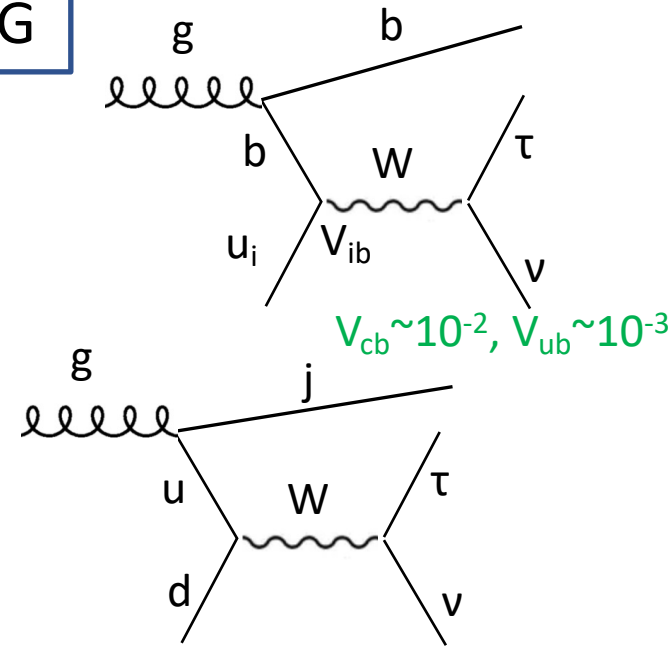
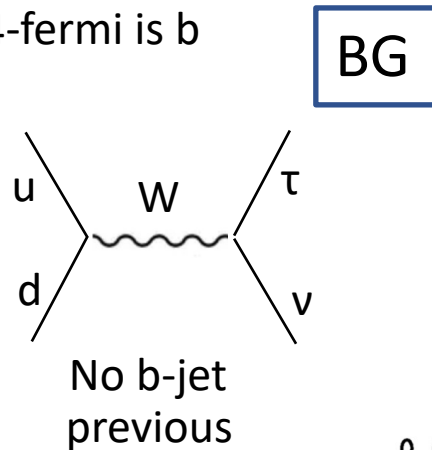
Importance of b-tagging

1. smaller BG, 2. different BG \rightarrow semi-independent cross check
3. specifying interaction one of quarks in 4-fermi is b



Greljo et al. 1811.07920

Within the EFT framework,
an additional b-jet tagging improve WC sensitivity
by 30-40% [Minho et al 2008.07541](#)



j \rightarrow b mis tag **less than 1%**

**We keep mediator mass dependence
even with b-jet tagging** [Iguro et al 2111.04748](#)

WZ, single t, ... are also important

Implication of $\Lambda_b \rightarrow \Lambda_c \tau \nu$ data and $b \rightarrow c \tau \nu$ sum rule

Syuhei Iguro, M. Fedele, U. Nierste, T. Kitahara, R. Watanabe, M. Blanke, A. Crivellin
2211.14172

Currently we have discrepancy
in $b \rightarrow c \tau \nu$

Experimental mistake? Statistical Fluctuation?
Underestimation of uncertainties?
Wrong SM prediction? New physics?

$$R_{D^{(*)}} = \frac{BR(B \rightarrow D^{(*)} \tau \nu)}{BR(B \rightarrow D^{(*)} l \nu)}, R_{J/\psi} = \frac{BR(B_c \rightarrow J/\psi \tau \nu)}{BR(B_c \rightarrow J/\psi \mu \nu)}, R_{\Lambda_c} = \frac{BR(\Lambda_b \rightarrow \Lambda_c \tau \nu)}{BR(\Lambda_b \rightarrow \Lambda_c \mu \nu)}$$

They all are described by $b \rightarrow c \tau \nu$ transition.

Compared to the SM predictions, current experimental results are

Larger $+4\sigma$

Larger $+2\sigma$

Smaller -2σ



Based on the updated sum rule which connects different ratios, we investigated whether the current data can be explained within a generic Model.

Sum rule

$$\frac{\mathcal{R}(\Lambda_c)}{\mathcal{R}_{SM}(\Lambda_c)} = 0.280 \frac{\mathcal{R}(D)}{\mathcal{R}_{SM}(D)} + 0.720 \frac{\mathcal{R}(D^*)}{\mathcal{R}_{SM}(D^*)} + \delta_{\Lambda_c}$$

correction \nearrow

$$\delta_{\Lambda_c} = \text{Re} \left[(1 + C_{V_L}^\tau) (0.314 C_T^{\tau*} - 0.003 C_{S_R}^{\tau*}) \right] + 0.014 (|C_{S_L}^\tau|^2 + |C_{S_R}^\tau|^2) + 0.004 \text{Re} (C_{S_L}^\tau C_{S_R}^{\tau*}) - 1.30 |C_T^\tau|^2.$$

How to derive this?

Detail: sum rule

Based on the our FF we updated the sum rule proposed in 1905.08253 (KIT group).

$$\frac{\mathcal{R}(\Lambda_c)}{\mathcal{R}_{\text{SM}}(\Lambda_c)} = |1 + C_{V_L}^\tau|^2 + 0.50 \text{Re} [(1 + C_{V_L}^\tau) C_{S_R}^{\tau*}] + 0.33 \text{Re} [(1 + C_{V_L}^\tau) C_{S_L}^{\tau*}] + 0.52 \text{Re} (C_{S_L}^\tau C_{S_R}^{\tau*}) \\ + 0.32 (|C_{S_L}^\tau|^2 + |C_{S_R}^\tau|^2) - 3.11 \text{Re} [(1 + C_{V_L}^\tau) C_T^{\tau*}] + 10.4 |C_T^\tau|^2,$$

$$\frac{R_D}{R_D^{\text{SM}}} = |1 + C_{V_L} + C_{V_R}|^2 + 1.01 |C_{S_L} + C_{S_R}|^2 + 0.84 |C_T|^2 \\ + 1.49 \text{Re} [(1 + C_{V_L} + C_{V_R})(C_{S_L}^* + C_{S_R}^*)] + 1.08 \text{Re} [(1 + C_{V_L} + C_{V_R})C_T^*],$$

$$\frac{R_{D^*}}{R_{D^*}^{\text{SM}}} = |1 + C_{V_L}|^2 + |C_{V_R}|^2 + 0.04 |C_{S_L} - C_{S_R}|^2 + 16.0 |C_T|^2 \\ - 1.83 \text{Re} [(1 + C_{V_L})C_{V_R}^*] - 0.11 \text{Re} [(1 + C_{V_L} - C_{V_R})(C_{S_L}^* - C_{S_R}^*)] \\ - 5.17 \text{Re} [(1 + C_{V_L})C_T^*] + 6.60 \text{Re} [C_{V_R}C_T^*],$$

Eliminating interference terms

2211.14172

Small correction

$$\frac{\mathcal{R}(\Lambda_c)}{\mathcal{R}_{\text{SM}}(\Lambda_c)} = 0.280 \frac{\mathcal{R}(D)}{\mathcal{R}_{\text{SM}}(D)} + 0.720 \frac{\mathcal{R}(D^*)}{\mathcal{R}_{\text{SM}}(D^*)} + \delta_{\Lambda_c},$$

$$\delta_{\Lambda_c} = \text{Re} [(1 + C_{V_L}^\tau) (0.314 C_T^{\tau*} - 0.003 C_{S_R}^{\tau*})] \\ + 0.014 (|C_{S_L}^\tau|^2 + |C_{S_R}^\tau|^2) \\ + 0.004 \text{Re} (C_{S_L}^\tau C_{S_R}^{\tau*}) - 1.30 |C_T^\tau|^2.$$

$$\mathcal{R}(\Lambda_c) = 0.367 \pm 0.013$$

Prediction form R_D, R_{D^*}

$$R_{\Lambda_c}^{\text{LHCb}} = 0.24 \pm 0.08,$$

$$R_{\Lambda_c}^{\text{Ligeti}} = 0.285 \pm 0.073$$

Solid correlation

Small R_{D^*} is more consistent but we need more data to conclude

Even if we include the NP in light lepton mode, we can not explain all.

Implication of $\Lambda_b \rightarrow \Lambda_c \tau \nu$ data and $b \rightarrow c \tau \nu$ sum rule

Syuhei Iguro, M. Fedele, U. Nierste, T. Kitahara, R. Watanabe, M. Blanke, A. Crivellin
2211.14172

Currently we have discrepancy
in $b \rightarrow c \tau \nu$

Experimental mistake? Statistical Fluctuation?
Underestimation of uncertainties?
Wrong SM prediction? New physics?

$$R_{D^{(*)}} = \frac{BR(B \rightarrow D^{(*)} \tau \nu)}{BR(B \rightarrow D^{(*)} l \nu)}, R_{J/\psi} = \frac{BR(B_c \rightarrow J/\psi \tau \nu)}{BR(B_c \rightarrow J/\psi \mu \nu)}, R_{\Lambda_c} = \frac{BR(\Lambda_b \rightarrow \Lambda_c \tau \nu)}{BR(\Lambda_b \rightarrow \Lambda_c \mu \nu)}$$

They all are described by $b \rightarrow c \tau \nu$ transition.

Compared to the SM predictions, current experimental results are

Larger $+4\sigma$

Larger $+2\sigma$

Smaller -2σ



Based on the updated sum rule which connects different ratios, we investigated whether the current data can be explained within a generic Model.

Sum rule

$$\frac{\mathcal{R}(\Lambda_c)}{\mathcal{R}_{SM}(\Lambda_c)} = 0.280 \frac{\mathcal{R}(D)}{\mathcal{R}_{SM}(D)} + 0.720 \frac{\mathcal{R}(D^*)}{\mathcal{R}_{SM}(D^*)} + \delta_{\Lambda_c}$$

correction \rightarrow

$$\delta_{\Lambda_c} = \text{Re} [(1 + C_{V_L}^\tau) (0.314 C_T^{\tau*} - 0.003 C_{S_R}^{\tau*})] + 0.014 (|C_{S_L}^\tau|^2 + |C_{S_R}^\tau|^2) + 0.004 \text{Re} (C_{S_L}^\tau C_{S_R}^{\tau*}) - 1.30 |C_T^\tau|^2.$$

New LHCb data prefers smaller (larger) deviation in $R_D(R_{D^*})$.
Nevertheless, R_{Λ_c} is still 2σ off from the sum rule.

Conclusion

Even if we allow the New physics in both τ and light lepton modes,

satisfactory simultaneous explanation of all $R_{D^{(*)}}$, $R_{J/\psi}$, R_{Λ_c} is not possible within QFT.

This result implies that the current data is something wrong and needs reanalysis or more data.

Generic formulae updated!

2210.10751

Syuhei Iguro, T.Kitahara, R. Watanabe

We updated generic NP formulae based on the updated $\bar{B} \rightarrow D^{(*)}$ form factors
Iguro-Watanabe 2020 and performed global fit

$$P_{\tau}(D^{(*)}) = \frac{\Gamma(B \rightarrow D^{(*)}\tau^{\lambda=+1/2}\nu) - \Gamma(B \rightarrow D^{(*)}\tau^{\lambda=-1/2}\nu)}{\Gamma(B \rightarrow D^{(*)}\tau\nu)}$$

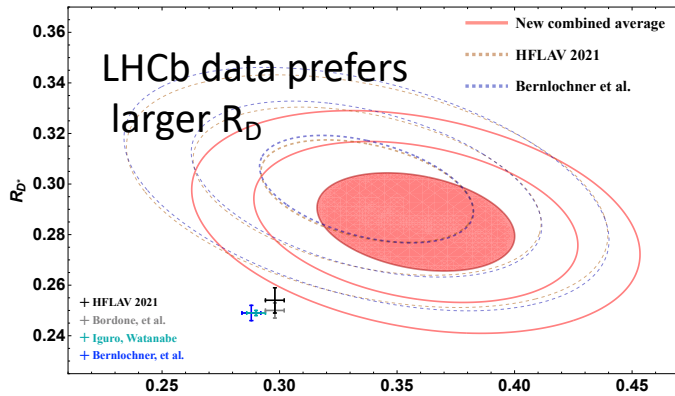
$$\frac{R_D}{R_D^{\text{SM}}} = |1 + C_{V_L} + C_{V_R}|^2 + 1.01|C_{S_L} + C_{S_R}|^2 + 0.84|C_T|^2 + 1.49\text{Re}[(1 + C_{V_L} + C_{V_R})(C_{S_L}^* + C_{S_R}^*)] + 1.08\text{Re}[(1 + C_{V_L} + C_{V_R})C_T^*],$$

$$\frac{P_{\tau}^D}{P_{\tau,\text{SM}}^D} = \left(\frac{R_D}{R_D^{\text{SM}}}\right)^{-1} \times (|1 + C_{V_L} + C_{V_R}|^2 + 3.04|C_{S_L} + C_{S_R}|^2 + 0.17|C_T|^2 + 4.50\text{Re}[(1 + C_{V_L} + C_{V_R})(C_{S_L}^* + C_{S_R}^*)] - 1.09\text{Re}[(1 + C_{V_L} + C_{V_R})C_T^*])$$

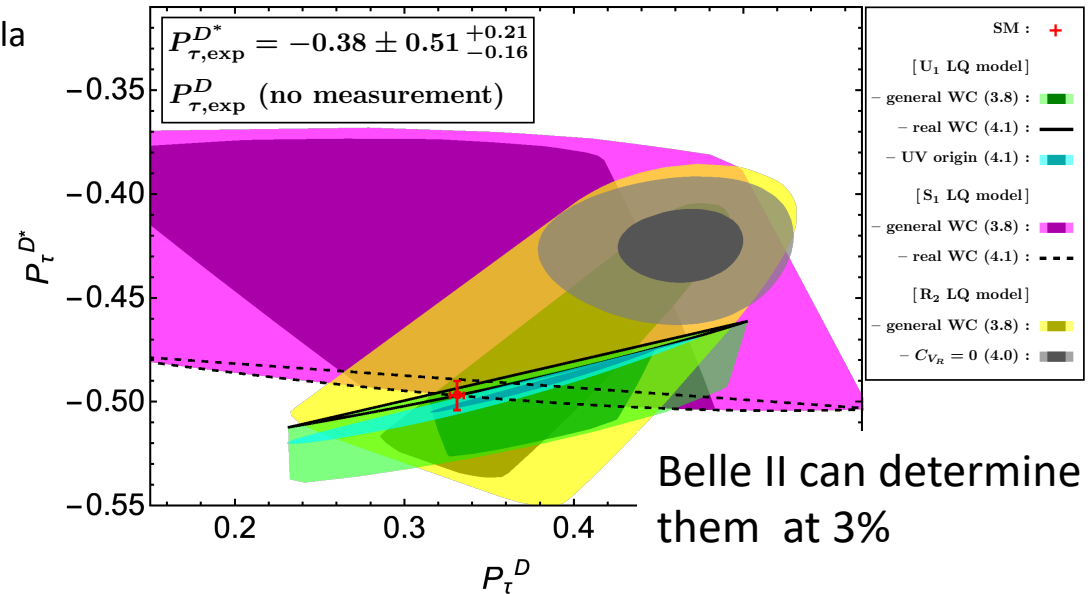
$$\frac{R_{D^*}}{R_{D^*}^{\text{SM}}} = |1 + C_{V_L}|^2 + |C_{V_R}|^2 + 0.04|C_{S_L} - C_{S_R}|^2 + 16.0|C_T|^2 - 1.83\text{Re}[(1 + C_{V_L})C_{V_R}^*] - 0.11\text{Re}[(1 + C_{V_L} - C_{V_R})(C_{S_L}^* - C_{S_R}^*)] - 5.17\text{Re}[(1 + C_{V_L})C_T^*] + 6.60\text{Re}[C_{V_R}C_T^*],$$

$$\frac{P_{\tau}^{D^*}}{P_{\tau,\text{SM}}^{D^*}} = \left(\frac{R_{D^*}}{R_{D^*}^{\text{SM}}}\right)^{-1} \times (|1 + C_{V_L}|^2 + |C_{V_R}|^2 - 0.07|C_{S_L} - C_{S_R}|^2 - 1.85|C_T|^2 - 1.79\text{Re}[(1 + C_{V_L})C_{V_R}^*] + 0.23\text{Re}[(1 + C_{V_L} - C_{V_R})(C_{S_L}^* - C_{S_R}^*)] - 3.47\text{Re}[(1 + C_{V_L})C_T^*] + 4.41\text{Re}[C_{V_R}C_T^*]),$$

We also discussed the uncertainty of the formula



Scalar operator came back

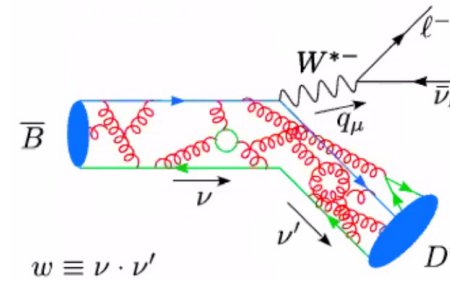


Belle II can determine them at 3%

τ polarization in $\bar{B} \rightarrow D^{(*)}\tau\nu$ is crucial to test the NP possibilities!

Although large part of the uncertainty cancels
 precise non-perturbative input ($B \rightarrow D^{(*)}$ transition form factor) is necessary

$$R_{D^{(*)}} = \frac{BR(B \rightarrow D^{(*)} \tau \nu)}{BR(B \rightarrow D^{(*)} l \nu)}, \quad l = \mu, e$$

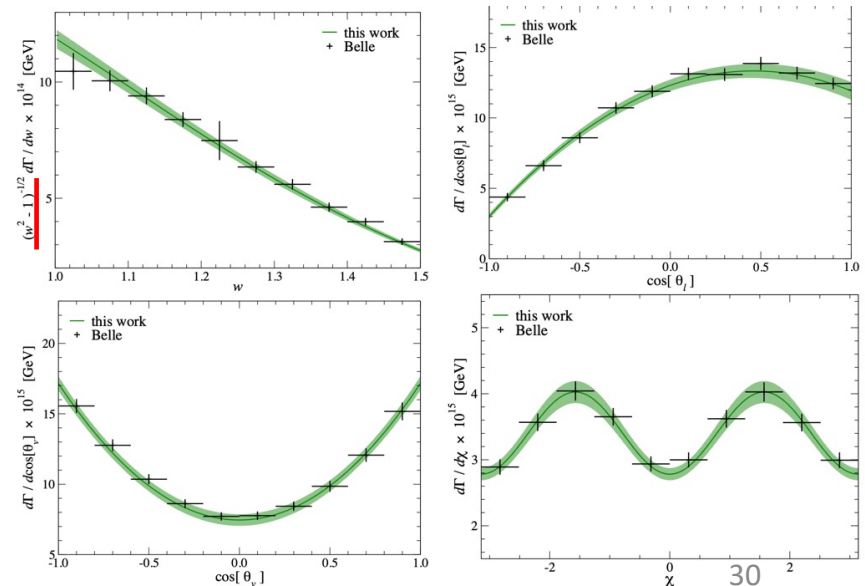
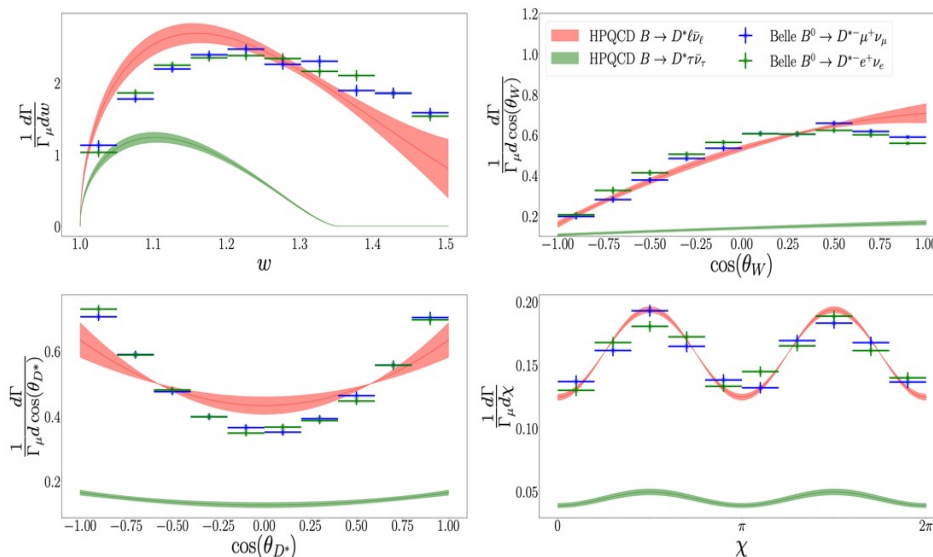


Non-perturbative information extracted from Lattice, experiments, QCDSR,,,,

- New Lattice results for $B \rightarrow D^*$ at non-zero recoil

HPQCD 2304.03137

JLQCD 2306.05657



Lattice results are not stable

Dispersive method (DM) can solve all?

Di Carlo, et al, 2105.02497; Martinelli, et al, 2105.07851

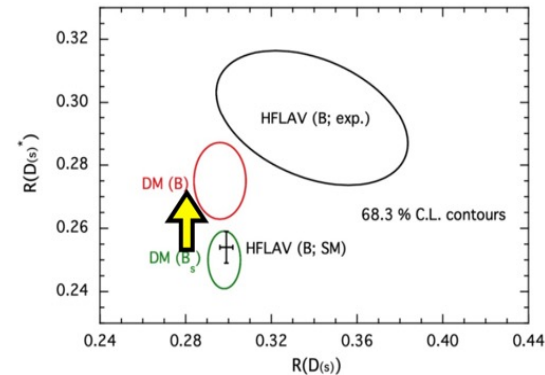
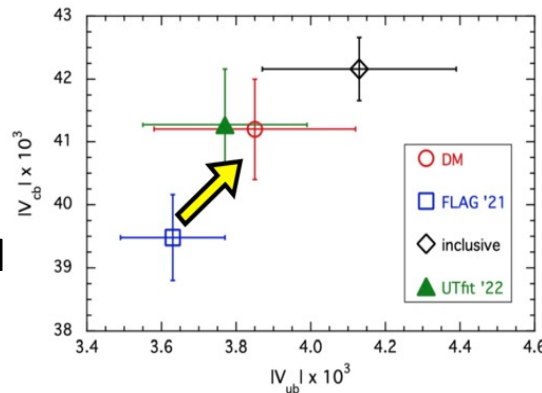
Usually form factor parameterization relies on heavy quark expansion and describe the different currents with common functions (Isger-Wise function)

or assume the simple polynomial in terms of conformal variable $z = \ll 1$ e.g. Boyd-Grinstein-Lebed (BGL) method

While DM method, with only lattice data (Fermi-MILC) and unitarity condition gives a **parameterization independent form factor**

Interestingly this DM method would simultaneously relax the tension

Since DM method yields considerably different result from others, it is natural to ask if this is really compatible with other observables?



31

We found that the DM method at least in $B \rightarrow D^*$ transition conflicts with angular distribution data by more than $3\sigma \Rightarrow$ we have discrepancies!

Playing with $FLD^*(e, \mu)$

$$F_L^{D^*}(e) = \frac{BR(B \rightarrow D_L^* e \nu)}{BR(B \rightarrow D^* e \nu)}$$

[1903.03102](#) $1ab^{-1}$
Belle K. Adamczyk

$FLD^*(e) = 0.56 \pm 0.02$ unpublished

[2301.07529](#)
Belle M. Prim
 $1ab^{-1}$

	stat	syst
$B^{(0,-)} \rightarrow D^{*(+,0)} e \bar{\nu}_e$	0.485 ± 0.017	± 0.005
$B^{(0,-)} \rightarrow D^{*(+,0)} \mu \bar{\nu}_\mu$	0.518 ± 0.017	± 0.005
$B \rightarrow D^* \ell \bar{\nu}_\ell$	0.501 ± 0.012	± 0.003

Preliminary

Belle II $189fb^{-1}$

$$F_L^e = 0.521 \pm 0.005 \pm 0.007,$$

$$F_L^\mu = 0.534 \pm 0.005 \pm 0.006,$$

$$\Delta F_L = 0.013 \pm 0.007 \pm 0.007,$$

ALPS2023 Chaoyi Lyu

Why statistic uncertainty is smaller than Belle?

this Belle II data is based on untagged events and hence statistics is better

Theoretical prediction

Iguro-Watanabe

$$0.534 \pm 0.002$$

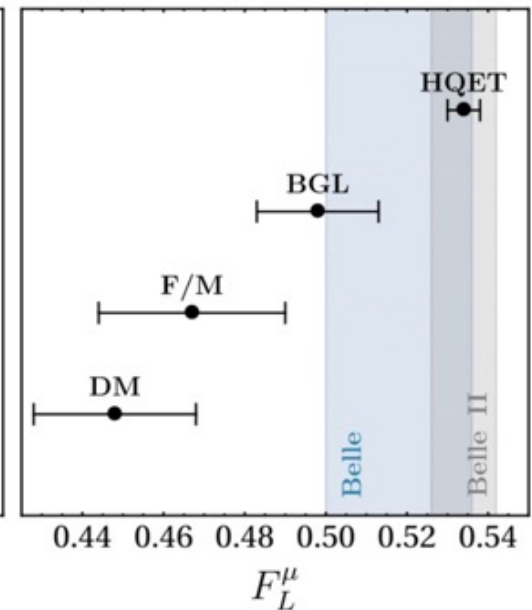
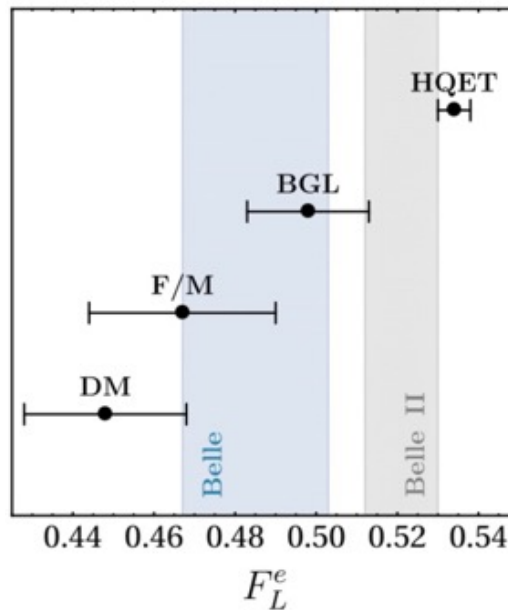
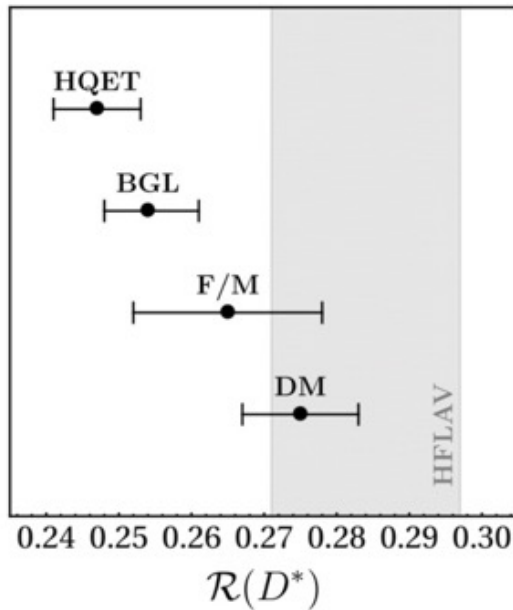
$$RD^*(SM) = 0.249 \pm 0.001$$

DM method

$$0.45 \pm 0.02$$

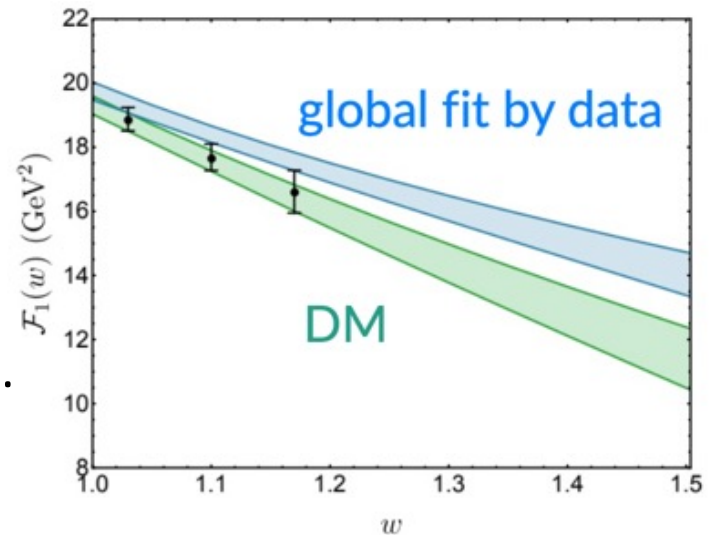
$$RD^*(SM) = 0.272 \pm 0.014$$

F/M:Fermi-MILC



If we perform the global fit including angular observables, the fitted form factor is considerably different from the original one.

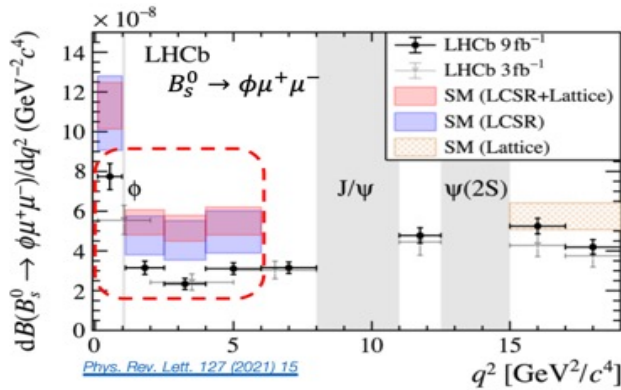
This global fitted DM yields discrepancies again.
Conclusion: DM method with F/M data also has difficulty



Flavor universal C_9 ?

$$\mathcal{L} = \frac{\alpha G_F V_{td_i} V_{td_k}^*}{\sqrt{2}\pi} \left[m_b C_7 (\bar{s} \sigma_{\mu\nu} P_R b) F^{\mu\nu} + m_b C_8 (\bar{s} \sigma_{\mu\nu} T^a P_R b) G^{a,\mu\nu} + C_9^{\ell} (\bar{s} \gamma_{\mu} P_L b) (\bar{\ell} \gamma_{\mu} \ell) + C_{10}^{\ell} (\bar{s} \gamma_{\mu} P_L b) (\bar{\ell} \gamma_{\mu} \gamma_5 \ell) \right] \quad (3)$$

The tensions in $BR(B_s \rightarrow \phi \mu^+ \mu^-)$, $BR(\Lambda_b \rightarrow \Lambda \mu^+ \mu^-)$, $BR(B \rightarrow K(*) \mu^+ \mu^-)$ and angular observable P_5' in $B \rightarrow K(*) \mu^+ \mu^-$

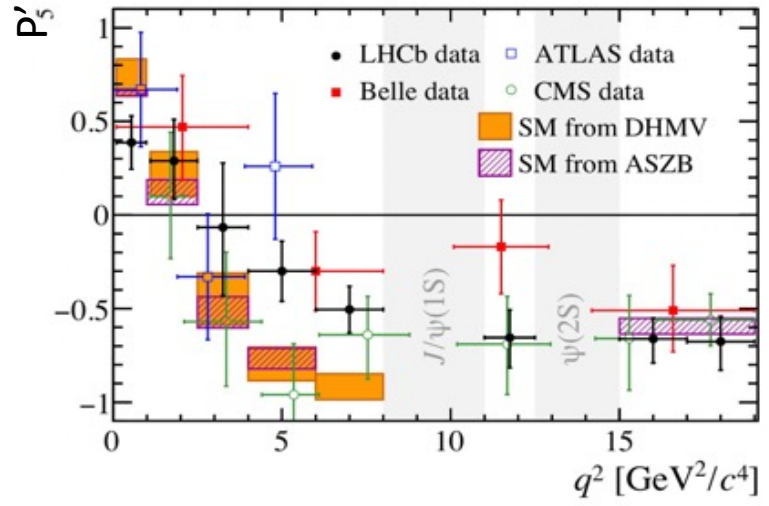


$$\frac{1}{d\Gamma/dq^2 d\cos\theta_{\ell} d\cos\theta_K d\phi} \frac{d^4\Gamma}{dq^2 d\cos\theta_{\ell} d\cos\theta_K d\phi} = \frac{9}{32\pi} \left[\frac{3}{4}(1-F_L)\sin^2\theta_K + F_L \cos^2\theta_K \right. \quad \text{Matias 11}$$

$$\left. + \frac{1}{4}(1-F_L)\sin^2\theta_K \cos 2\theta_{\ell} - F_L \cos^2\theta_K \cos 2\theta_{\ell} + S_3 \sin^2\theta_K \sin^2\theta_{\ell} \cos 2\phi + S_4 \sin 2\theta_K \sin 2\theta_{\ell} \cos \phi + S_5 \sin 2\theta_K \sin \theta_{\ell} \cos \phi + S_6 \sin^2\theta_K \cos \theta_{\ell} + S_7 \sin 2\theta_K \sin \theta_{\ell} \sin \phi + S_8 \sin 2\theta_K \sin 2\theta_{\ell} \sin \phi + S_9 \sin^2\theta_K \sin^2\theta_{\ell} \sin 2\phi \right]$$

Optimized observable

$$P'_{i=4,5,6,8} = \frac{S_{j=4,5,7,8}}{\sqrt{F_L(1-F_L)}}$$

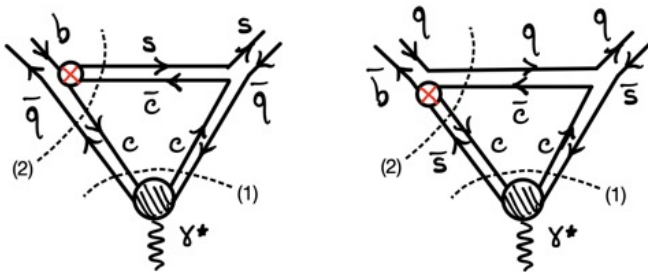


Global fit

Hurth, et al 2210.07221

$$C_9^{\ell}(\mu_b) = -0.95 \pm 0.13$$

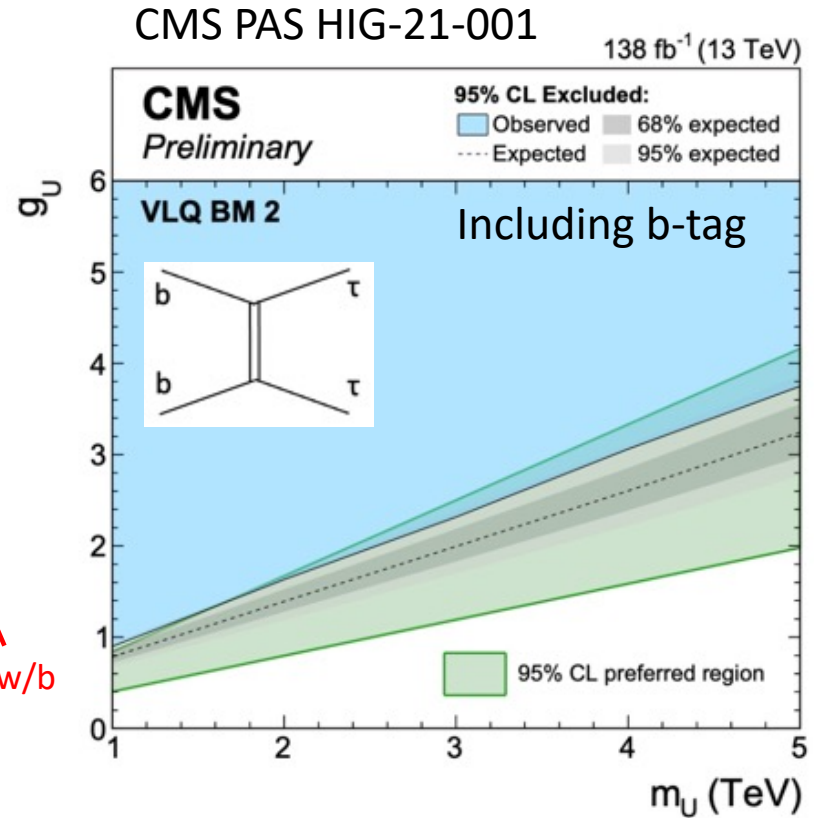
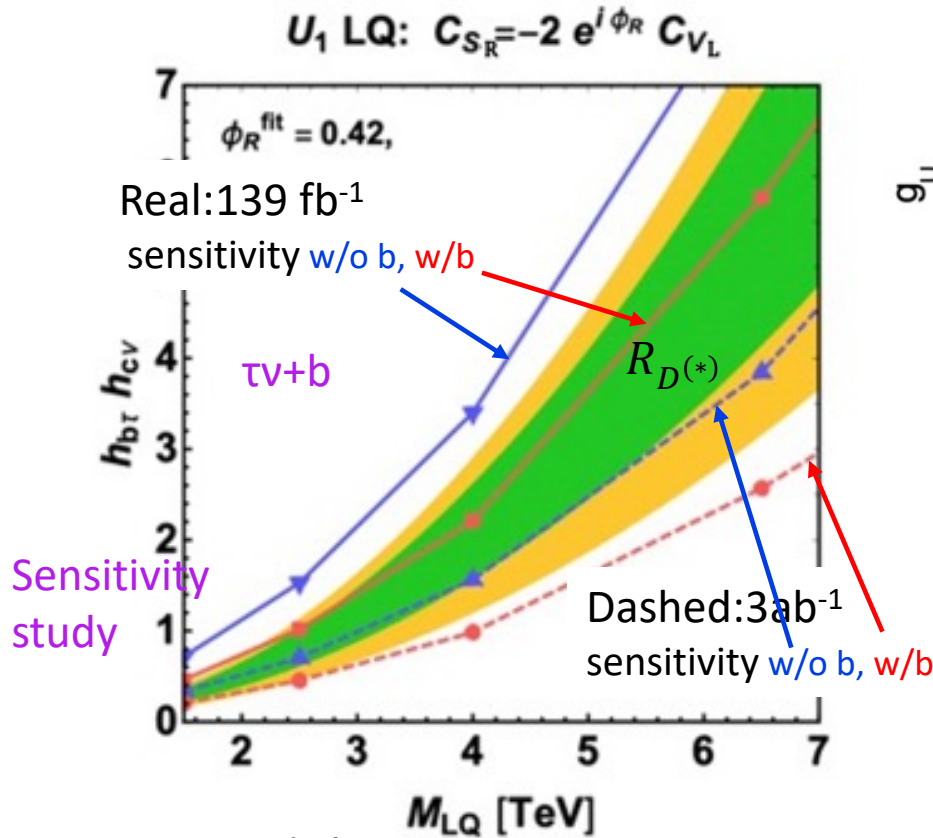
Similar result is obtained (2212.10516) if charm rescattering contribution is small.



New physics would account for Lepton flavor universal C_9

Other scenarios: U_1 LQ with $U(2)$ flavor symmetry

[2111.04748](#)



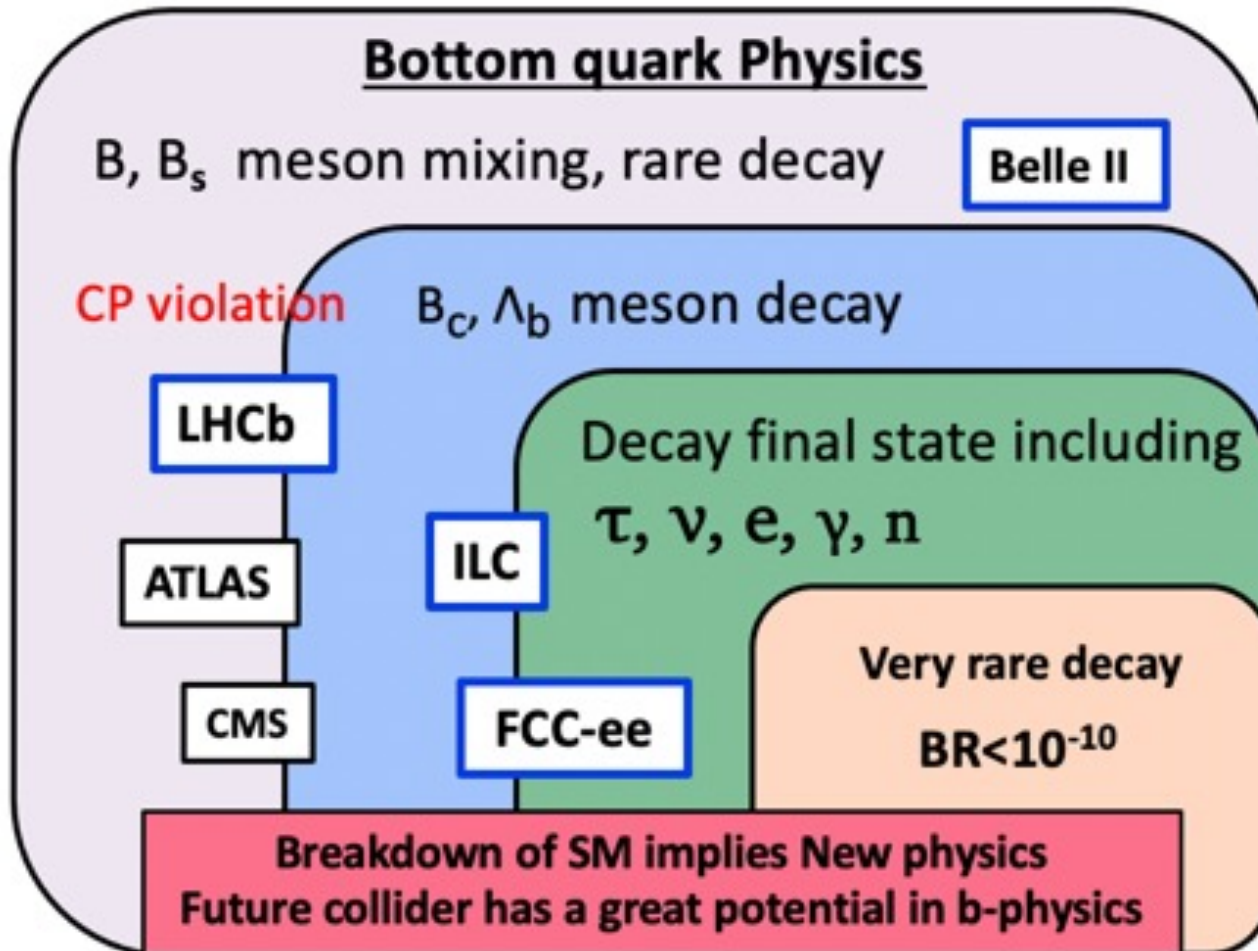
We assigned the conservative uncertainty corresponding to the one with 36 fb^{-1} to estimate the sensitivity with 139 fb^{-1} \rightarrow our sensitivity is conservative.

We can touch the interesting region with the LHC.

An additional b-tagging is important but not performed yet

Global view: B physics at future lepton colliders

In which field future machine plays a role?



We are waiting for your suggestion (process) to evaluate the potential! ³⁶

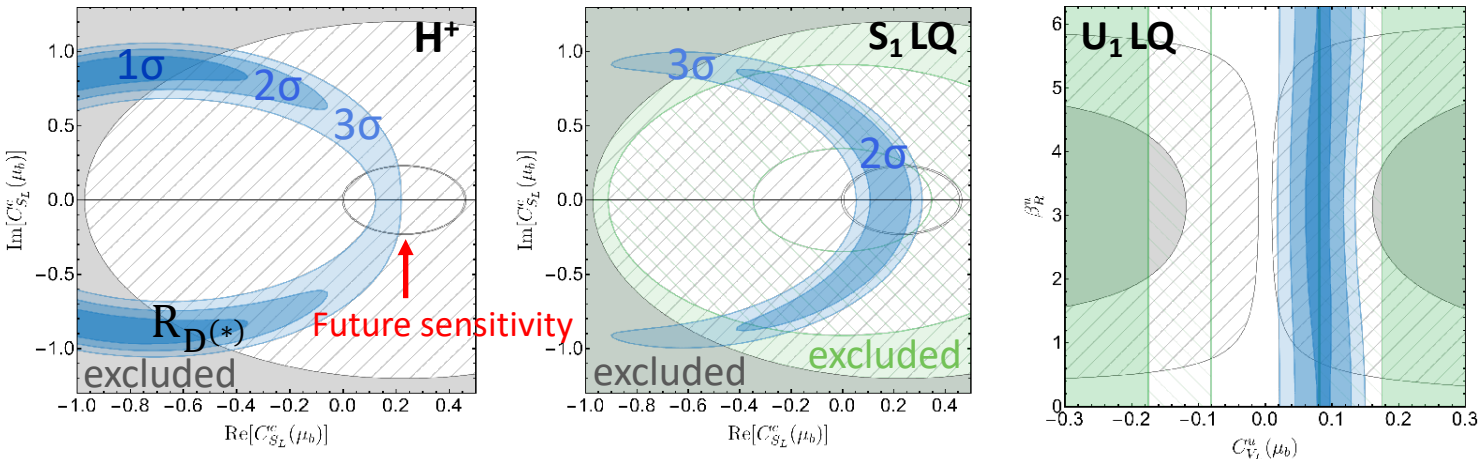
$B_{u,c} \rightarrow \tau \nu$ at FCC-ee

2305.02998

Syuhei Iguro, Marco Fedele, Xunwu Zuo, , , ,

Improving $B_{u,c} \rightarrow \tau \nu$ accuracy is super important for V_{ub} , V_{cb} , $R_{D^{(*)}}$ and testing the SM and HQET. At the previous Z pole e^+e^- collider, the number of the produced b quark is smaller than BaBar, Belle. LHCb has tremendous number of b, however, not suitable for precision physics. FCC-ee is an unique opportunity for τ , ν , involving precision B physics with $O(10^{11})$ b-hadron!

They can determine $BR(B_c \rightarrow \tau \nu)$ at O(1)% of the SM prediction



FCC-ee and HL-LHC can search

  meshed region

Except for the thin ring, we can probe whole region for H^+ and S_1 .
FCC-ee can probe the broader parameter space than HL-LHC.

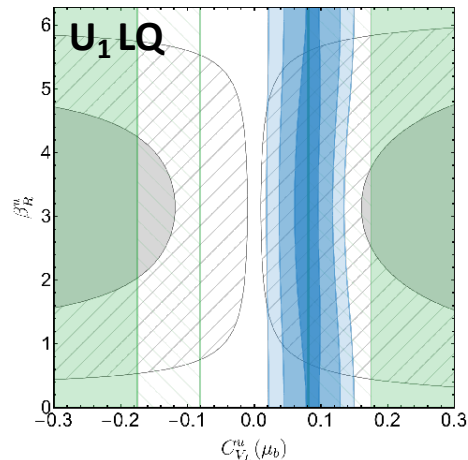
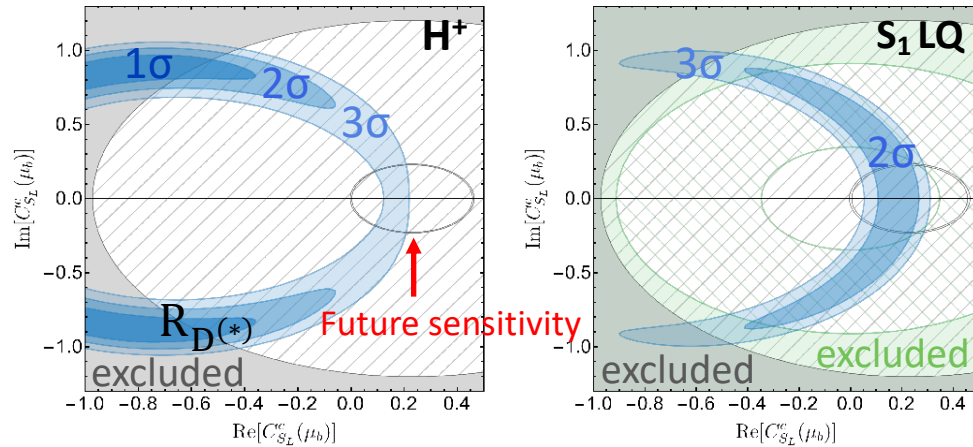
FCC-ee is super powerful tool not only EW precision physics but also heavy flavor physics!

$B_{u,c} \rightarrow \tau \nu$ at FCC-ee

2305.02998

Syuhei Iguro, Marco Fedele, Xunwu Zuo, , , ,

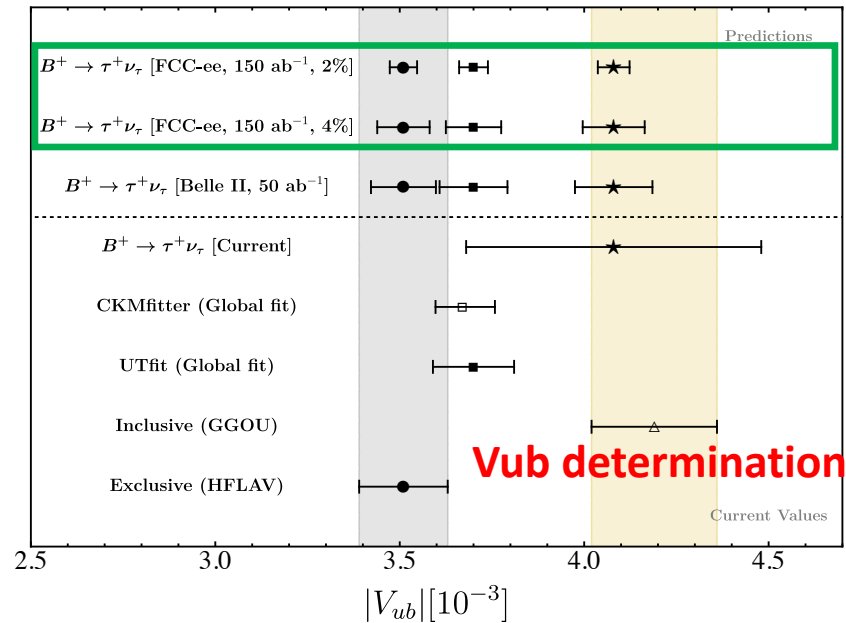
Improving $B_{u,c} \rightarrow \tau \nu$ accuracy is super important for V_{ub} , V_{cb} , $R_{D^{(*)}}$ and testing the SM and HQET. At the previous Z pole e^+e^- collider, the number of the produced b quark is smaller than BaBar, Belle. LHCb has tremendous number of b, however, not suitable for precision physics. FCC-ee is an unique opportunity for τ , ν , involving precision B physics with $O(10^{11})$ b-hadron!



FCC-ee and HL-LHC can search
  meshed region

Except for the thin ring, we can probe whole region for H^+ and S_1 . FCC-ee can probe the broader parameter space than HL-LHC.

FCC-ee is super powerful tool not only EW precision physics but also heavy flavor physics!



Future $B \rightarrow \tau \nu$ is the independent third cross check of V_{ub} . This determination is free from form factors and inclusive hadronic parameters

Other interesting modes e.g. Λ_b decays at FCC-ee are waiting for the detailed analysis!

Global fit to $b \rightarrow c \tau \nu$



Syuhei Iguro

Inspire
web page



Mainly based on [2210.10751 v3](https://arxiv.org/abs/2210.10751) (coming soon)

and many papers with Teppei Kitahara, Yuji Omura, Ryoutaro Watanabe, Hantian Zhang, Monika Blanke, Ulrich Nierste, Fedele Marco, Andreas Crivellin,,,