$|V_{ub}|$ and the potential impact of new physics in exclusive b \rightarrow u l v decays



o D.Leljak, BM (RBI, Zagreb), D. van Dyk (TUM): The B to π form factors from QCD and their impact on Vub, JHEP 07 (2021) 036, arXiv 2102.07233

• D.Leljak, BM (RBI, Zagreb), F. Novak (TUM), M. Reboud, D. van Dyk (Durham): Toward a complete description of $b \rightarrow u \ l v$ decays within the Weak Effective Theory, JHEP 08 (2023) 063, arXiv 2302.05268

CKM 2023: 12th International Workshop on the CKM Unitarity Triangle, Sep 18-22, 2023, Santiago de Compostela

V_{ub} FROM B $\rightarrow \pi$ STATUS 2021

inclusive:

$$10^{3} \times |V_{ub}|_{\text{BLNP}} = 4.44^{+0.13}_{-0.14}|_{\text{exp. -0.22}}|_{\text{theory}} \simeq 4.44^{+0.25}_{-0.26},$$

$$10^{3} \times |V_{ub}|_{\text{GGOU}} = 4.32 \pm 0.12|_{\text{exp. -0.13}}|_{\text{theory}} \simeq 4.32^{+0.17}_{-0.18}$$

BLNP: Bosch,Lange,Neubert,Paz, arXiv [ph]: 0504071 GGOU: Gambino,Giordano,Ossola,Uratsev, arXiv [ph]: 0707.2493

exclusive:

$$10^3 \times |V_{ub}|_{\text{LQCD+LCSR}}^{\bar{B} \to \pi} = 3.67 \pm 0.09|_{\text{exp.}} \pm 0.12|_{\text{theory}} \simeq 3.67 \pm 0.15$$

HFLAV , arXiv:1909.12524

exclusive vs inclusive V_{ub}~\approx 2.7\sigma

! new inclusive Vub measurement:

 $10^3 \times |V_{ub}| = 4.10 \pm 0.09 \pm 0.22 \pm 0.15 = 4.10 \pm 0.28$

Belle , arXiv:2102.00020

V_{ub} FROM b \rightarrow u STATUS 2022/23

Current world HFLAV averages (2206.07501) : $|V_{ub}^{\text{exc}}| = (3.51 \pm 0.12) \cdot 10^{-3}$ $|V_{ub}^{\text{inc}}| = (4.19 \pm 0.16) \cdot 10^{-3}$

$$\frac{|V_{ub}^{\rm exc}|}{|V_{ub}^{\rm inc}|} = 0.84 \pm 0.04 \qquad \textbf{3.7 sigmal}$$



Chunhui Chen (Iowa State University)

On behalf of the Belle and Belle II Collaborations, 31th Lepton Photon, July 21, 2023, Melbourne, Australia

Belle Collaboration, arXiv:2303.17309

"First simultaneous determination of Vub (inc) and Vub (exc)",

 $B
ightarrow \pi \ell
u$ only:



IMPORTANT REMARKS ON V_{ub} **EXTRACTION**:

INCLUSIVE MEASURMENTS include :

- theoretical prediction for non-perturbative shape functions (non-local OPE region) of $B \rightarrow X_u \ell^+ \nu_\ell$
- in the low invariant mass region sum of the exclusive decays (B→π,η,η',ω,ρ) modeled by using LQCD and LCSR form factors
- huge background from $B \to X_c \,\ell^+ \,\nu_\ell$ if meaurement is extended to the B to Xc dominated phase space (like Belle2021)

$$|V_{ub}| = \sqrt{\frac{\Delta \mathcal{B}^{\exp}(B \to X_u \ell^+ \nu_l)}{\tau_B \,\Delta \Gamma^{\text{th}}(B \to X_u \ell^+ \nu_l)}}$$
average of 4 different theoretical predictions (models: BLNP, GGOU, ADGF, DGE)

B	Value B^+	Value B^0
$B \to X_u \ell^+ \nu_\ell$		
$B o \pi \ell^+ u_\ell$	$(7.8 \pm 0.3) \times 10^{-5}$	$(1.5 \pm 0.06) \times 10^{-4}$
$B o \eta \ell^+ \nu_\ell$	$(3.9 \pm 0.5) \times 10^{-5}$	-
$B o \eta' \ell^+ u_\ell$	$(2.3 \pm 0.8) \times 10^{-5}$	-
$B \to \omega \ell^+ \nu_\ell$	$(1.2 \pm 0.1) \times 10^{-4}$	-
$B o \rho \ell^+ \nu_\ell$	$(1.6 \pm 0.1) \times 10^{-4}$	$(2.9 \pm 0.2) \times 10^{-4}$
$B \to X_u \ell^+ \nu_\ell$	$(2.2 \pm 0.3) \times 10^{-3}$	$(2.0 \pm 0.3) \times 10^{-3}$



EXCLUSIVE MEASUREMENTS include:

 $|V_{ub}|^2 |f_+(q^2)|^2$

- theoretical predictions of B to π from factors modeled by using LQCD and LCSR
- correlations among form factors
- complementary theoretical input: lattice QCD \Rightarrow FFs in the high q² region, LCSR \Rightarrow FFs in the low q² regions



Figure 3: $\Delta \chi^2 = 1$ region for $|V_{ub}|$ for an infinitely precise form factor determination at a single q^2 -value. The plot assumes that the form factor yields the central value $|V_{ub}| = 3.7 \times 10^{-3}$.

To significantly reduce error of Vub one would need to reduce FF errors at $q^2 = 0$ to be less than 10%, while reduction of the error at q^2_{max} has almost no impact \Rightarrow **IMPORTANCE OF THE LCSR CALCULATIONS !**

FORM FACTORS FROM LIGHT-CONE SUM RULES (LCSR)

$$\frac{\mathrm{d}\Gamma}{\mathrm{d}q^2} \left(\bar{B} \to \pi \ell^- \bar{\nu}_\ell \right) = \frac{G_F^2 |V_{ub}|^2}{24\pi^3 m_B^2 q^4} \left(q^2 - m_\ell^2 \right)^2 |\vec{p}_\pi| \times \left[\left(1 + \frac{m_\ell^2}{2q^2} \right) m_B^2 |\vec{p}_\pi|^2 \left[f_+(q^2) \right]^2 + \frac{3m_\ell^2}{8q^2} (m_B^2 - m_\pi^2)^2 \left[f_0(q^2) \right]^2 \right]$$

$$\langle \pi(p_{\pi}) | \bar{u} \gamma^{\mu} b | B(p_B) \rangle = f_{+}(q^{2}) \left[(p_{B} + p_{\pi})^{\mu} - \frac{m_{B}^{2} - m_{\pi}^{2}}{q^{2}} q^{\mu} \right] + f_{0}(q^{2}) \frac{m_{B}^{2} - m_{\pi}^{2}}{q^{2}} q^{\mu} ,$$

$$\langle \pi(p_{\pi}) | \bar{u} \sigma_{\mu\nu} q^{\nu} b | B(p_{B}) \rangle = \frac{i f_{T}(q^{2})}{m_{B} + m_{\pi}} \left[q^{2} (p_{B} + p_{\pi})_{\mu} - \left(m_{B}^{2} - m_{\pi}^{2} \right) q_{\mu} \right]$$

 f_T is important in rare $B \to (P, V) \ell^+ \ell^-$ decays



EXTRAPOLATION TO HIGH Q²

validity of LCSR $q^2 < m_b^2 - 2m_b\bar{\Lambda} \sim 15\,{\rm GeV}^2$

BCL PARAMETRIZATION – SL phase space $0 \le q^2 \le t_- \equiv (m_B - m_\pi)^2$ is mapped onto the real z-axes:

$$z(q^2; t_+, t_0) = \frac{\sqrt{t_+ - q^2} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - q^2} + \sqrt{t_+ - t_0}}$$

$$t_{+} \equiv (m_{B} + m_{\pi})^{2}$$
$$t_{0} = t_{0,\text{opt}} = (m_{B} + m_{\pi})(\sqrt{m_{B}} - \sqrt{m_{\pi}})^{2}$$

BCL, Bourrely, Caprini, Lellouch, arXiv:0807.2722

 $\bar{z}_n \equiv z^n - z_0^n, \ z_0 = z(0; t_+, t_0)$

$$f_{+}(q^{2}) = \frac{f_{+}(q^{2}=0)}{1-q^{2}/m_{B^{*}}^{2}} \left[1 + \sum_{n=1}^{K-1} b_{n}^{+} \left(\bar{z}_{n} - (-1)^{n-K} \frac{n}{K} \bar{z}_{K} \right) \right],$$

$$f_{0}(q^{2}) = f_{+}(q^{2}=0) \left[1 + \sum_{n=1}^{K-1} b_{n}^{0} \bar{z}_{n} \right],$$

$$f_{T}(q^{2}) = \frac{f_{T}(q^{2}=0)}{1-q^{2}/m_{B^{*}}^{2}} \left[1 + \sum_{n=1}^{K-1} b_{n}^{T} \left(\bar{z}_{n} - (-1)^{n-K} \frac{n}{K} \bar{z}_{K} \right) \right],$$

subthreshold pole

LCSR FIT AND RESULTS

 $a,b{=}\{+{,}0{,}T\}{,}i{,}j$

 $\chi^2_{\rm LCSR} = \sum \delta f_a^{\rm LCSR}(q_i^2, \vec{b}_a) \left(C^{\rm LCSR} \right)_{abij}^{-1} \delta f_b^{\rm LCSR}(q_j^2, \vec{b}_b)$

Leljak, BM, van Dyk, 2102.07233

all form factors are fitted simultaneously, with correlations among them included !



INTERPOLATION BETWEEN LCSR AND LATTICE QCD RESULTS

LCSR:
$$q^2 < m_b^2 - 2m_b\bar{\Lambda} \sim 15 \,{\rm GeV}^2$$

LATTICE QCD: $19 \,\mathrm{GeV}^2 \lesssim q^2 \lesssim 25 \,\mathrm{GeV}^2$

FNAL/MILC coll: Nf = 2 + 1 gauge ensambles and staggered-quark action (staggering gets rid of some of degenerate fermions (doublers) in the fermion action by redistributing the fermionic degrees of freedom across different lattice sites) **RBC/UKQCD coll**: Nf = 2 + 1 gauge ensambles and domain-wall fermions (by introducing an extra dimension the chirality of quarks is separted and controlled) HPOCD pot considered (share the same ensambles with ENAL/MILC; no correlations between form factors)

HPQCD – not considered (share the same ensambles with FNAL/MILC; no correlations between form factors)

$$\chi^2_{\rm theory} = \chi^2_{\rm LCSR} + \chi^2_{\rm LQCD}$$

$$\chi_{\mathrm{LX}}^{2} = \sum_{a,b=\{+,0,T\},i,j} \delta f_{a}^{\mathrm{LX}}(q_{i}^{2},\vec{b}_{a}) \begin{pmatrix} C^{\mathrm{LX}} \end{pmatrix}_{abij}^{-1} \\ \delta f_{b}^{\mathrm{LX}}(q_{j}^{2},\vec{b}_{b}) \end{pmatrix}$$
covariance matrix accounts for correlations between different FFs and different q² points $\delta f_{a}^{\mathrm{LX}}(q_{i}^{2},\vec{b}_{a}) = f_{a}^{\mathrm{LX}}(q_{i}^{2}) - f_{a}(q_{i}^{2},\vec{b}_{a})$



scalar pole - modifies the shape parameters and allows for more flexibility of the fit:

 $\frac{1}{1 - q(z)^2 / m_{B_0}^2} \approx \frac{1}{1 - \frac{t_0}{m_{B_0}^2}} + 4 \frac{m_{B_0}^2(t_0 - t_+)}{(m_{B_0}^2 - t_0)^2} z + \mathcal{O}\left(z^2\right)$

input

RESULTS

scena	rio LCSR-	LCSR+LQCD	
param.	<u> </u>	K = 4	K = 3
$f_{+}(0)$	$0.237\substack{+0.017\\-0.017}$	$0.235\substack{+0.019\\-0.019}$	$0.283\substack{+0.027\\-0.027}$
b_1^+	$-2.38\substack{+0.33\\-0.38}$	$-2.45^{+0.49}_{-0.54}$	$-1.0^{+3.5}_{-3.6}$
b_2^+	$-0.82\substack{+0.76\\-0.81}$	$-0.2^{+1.1}_{-1.2}$	$-2.8^{+4.9}_{-4.7}$
b_3^+		$-0.9^{+4.2}_{-4.0}$	
b_1^0	$0.48\substack{+0.07\\-0.07}$	$0.40^{+0.18}_{-0.20}$	-5^{+52}_{-51}
b_2^0	$0.14\substack{+0.39 \\ -0.44}$	$0.1^{+1.1}_{-1.2}$	22^{+200}_{-200}
b_3^0	$2.79_{-0.77}^{+0.71}$	$3.7^{+1.6}_{-1.6}$	-32^{+240}_{-240}
b_4^0		1^{+14}_{-13}	
$f_T(0)$	$0.240\substack{+0.016\\-0.016}$	$0.235\substack{+0.017\\-0.017}$	$0.281\substack{+0.025\\-0.025}$
b_1^T	$-2.05\substack{+0.32\\-0.36}$	$-2.45^{+0.45}_{-0.50}$	$-0.6^{+4.2}_{-4.4}$
b_2^T	$-1.45\substack{+0.63\\-0.66}$	$-1.08^{+0.68}_{-0.71}$	$-3.2^{+5.9}_{-5.8}$
b_3^T		$2.6^{+2.1}_{-2.0}$	
p value	$\sim 52\%$	$\sim 54\%$	$\sim 100\%$
$\chi^2/{ m d.o.f}$	$\sim 21.01/22$	$\sim 17.75/19$	$\sim 0.0278/3$

form factor	# of points	q^2 values (in GeV^2)	type	source
	5	-10.0, -5.0, 0.0, 5.0, 10.0	LCSR	this work
f_+	3	21.0, 23.0, 25.0	LQCD	FNAL/MILC $[33]$
	3	$19.0,\ 22.6,\ 25.1$	LQCD	RBC/UKQCD [35]
	4	-10.0, -5.0, 5.0, 10.0	LCSR	this work
f_0	4	19.0,21.0,23.0,25.0	LQCD	FNAL/MILC $[33]$
	3	$19.0,\ 22.6,\ 25.1$	LQCD	RBC/UKQCD [35]
f	5	-10.0, -5.0, 0.0, 5.0, 10.0	LCSR	this work
JT	4	19.0,21.0,23.0,25.0	LQCD	FNAL/MILC $[34]$





LCSR + LQCD FORM FACTORS RESULTS vs OTHERS

Leljak, BM, van Dyk, 2102.07233

Source	$f_{+}(0) = f_{0}(0)$	$f_T(0)$	
Latti			
Fermilab/MILC [33, 34]	0.2 ± 0.2	0.2 ± 0.2	
RBC/UKQCD [35]	0.24 ± 0.08		
combination w/ Pade approx. $[51]$	$0.265 \pm 0.010 \pm 0.002$		
Light-cone sum rules			
Duplancic et al. [16]	$0.26\substack{+0.04\\-0.03}$	0.255 ± 0.035	
Imsong et al. $[21]$	0.31 ± 0.02		
Bharucha [17]	$0.261\substack{+0.020\\-0.023}$		
Khodjamirian/Rusov $[30]$	0.301 ± 0.023	0.273 ± 0.021	
Gubernari et al. $(B \text{ LCDA})$ [22]	0.21 ± 0.07	0.19 ± 0.06	
this work	0.283 ± 0.027	0.282 ± 0.026	
Light-cone sum rules + Lattice QCD combination			
this work	0.235 ± 0.019	0.235 ± 0.017	

V_{ub} DETERMINATION FROM EXTRACTED FORM FACTORS

$$\chi^{2} = \chi^{2}_{\bar{B} \to \pi \ell^{-} \bar{\nu}_{\ell}} + \chi^{2}_{\text{LCSR}} + \chi^{2}_{\text{LQCD}}$$
$$\chi^{2}_{\bar{B} \to \pi \ell^{-} \bar{\nu}_{\ell}} = \sum_{i,j} \delta \mathcal{B}_{i} (C^{\text{EXP}})^{-1}_{ij} \delta \mathcal{B}_{j} \qquad \delta \mathcal{B}_{i} = \mathcal{B}^{\text{exp}}_{i} - \frac{\tau_{B}}{C_{v}} \int_{\Delta q^{2}_{i}} \frac{G^{2}_{F}}{24\pi^{3}} |V_{ub}|^{2} \left| f_{+}(q^{2}, \vec{b}) \right|^{2} |\vec{p}_{\pi}|^{3} dq^{2}$$

exp from HFLAV , arXiv:1909.12524 - q² binned average of BaBar (2010,2012) and Belle (2010,2013) data

$$|V_{ub}|_{\rm LCSR+LQCD}^{\bar{B}\to\pi} = (3.77\pm0.15)\cdot10^{-3}$$

Leljak, BM, van Dyk, 2102.07233

	method	LCSR+LQCD		LCSR only	
	param.	K = 3	K = 4	K = 3	
$\left(\right)$	$10^{-3} \times V_{ub} $	$3.80\substack{+0.14\\-0.14}$	$3.77^{+0.15}_{-0.15}$	$3.28^{+0.33}_{-0.28}$	
	$f_+(0)$	$0.248^{+0.009}_{-0.009}$	$0.246^{+0.009}_{-0.009}$	$0.284^{+0.025}_{-0.025}$	
	b_1^+	$-2.13\substack{+0.19\\-0.19}$	$-2.10\substack{+0.22\\-0.21}$	$-1.91\substack{+0.31\\-0.30}$	
	b_2^+	$-0.82^{+0.54}_{-0.55}$	$0.23\substack{+0.87\\-0.87}$	$-1.42^{+0.85}_{-0.89}$	
	b_3^+		$-3.0^{+2.8}_{-2.8}$		
	$\chi^2/{ m d.o.f}$	$\sim 32.33/34$	$\sim 29.30/31$	$\sim 10.72/17$	
	p value	$\sim 55\%$	$\sim 55\%$	$\sim 87\%$	

INCLUSION OF $\,B ightarrow ho,\omega\,$ decays and test of the SM

Leljak, BM , Novak, Reboud, van Dyk , 2302.05268

 $|V_{ub}|$ from $B
ightarrow
ho, \omega$ is constantly below other exclusive (and inclusive) extractions !

We perform the statistical fit of b to u decays in EOS program [EOS Authors collaboration 2111.15428] :



exp: HFLAV average (Babar & Belle) th: FF from LCSR + lattice, BCL q² param of FF [Leljak, BM, van Dyk, 2102.07233]

$$B^- \to \rho \, \ell^- \bar{\nu}$$
$$B^- \to \omega \ell^- \bar{\nu}$$

exp: average from Bernlochner, Prim, Robinson, 2104.05739 (Babar & Belle) th: FF from LCSR [Bharucha, Strub, Zwicky (BSZ) 2015], BSZ q² param. of FF

(similar analysis in EOS for $B_s \rightarrow K \ell \nu$ only, Bolognoni, van Dyk, Vos, 2308.04347)

WET setup

$$\begin{aligned} \mathcal{H}^{ub\ell\nu} &= -\frac{4G_F}{\sqrt{2}} \tilde{V}_{ub} \sum_i C_i^{\ell} \mathcal{O}_i^{\ell} + \dots + \text{h.c.} \\ \mathcal{O}_{V,L} &= \left[\bar{u} \gamma^{\mu} P_L b \right] \left[\bar{\ell} \gamma_{\mu} P_L \nu \right], \quad \mathcal{O}_{V,R} = \left[\bar{u} \gamma^{\mu} P_R b \right] \left[\bar{\ell} \gamma_{\mu} P_L \nu \right], \\ \mathcal{O}_{S,L} &= \left[\bar{u} P_L b \right] \left[\bar{\ell} P_L \nu \right], \quad \mathcal{O}_{S,R} = \left[\bar{u} P_R b \right] \left[\bar{\ell} P_L \nu \right], \\ \mathcal{O}_T &= \left[\bar{u} \sigma^{\mu\nu} b \right] \left[\bar{\ell} \sigma_{\mu\nu} P_L \nu \right]. \end{aligned}$$

SM - null hypothesis $\tilde{V}_{ub} \, \mathcal{C}_{V,L}^{\ell} = 3.67 \times 10^{-3} \qquad C_{V,L}^{\ell} = 1 + O(\alpha_e) \qquad \mathcal{C}_i^{\ell}(i \neq (V,L)) = 0$

CKM $ilde{V}_{ub} \, \mathcal{C}^{\ell}_{V,L} \in [3.0, 4.5] \times 10^{-3}$ $\mathcal{C}^{\ell}_{i} (i \neq (V,L)) = 0$

 $\Box \text{ WET } \quad \tilde{V}_{ub} = 3.67 \times 10^{-3} \qquad 0 \le \mathcal{C}_{V,L}^{\ell} \le 1, \qquad 0 \le \mathcal{C}_{V,R}^{\ell} \le 1.1, \\ 0 \le \mathcal{C}_{S,L}^{\ell} \le 0.7, \quad -0.7 \le \mathcal{C}_{S,R}^{\ell} \le 0.3, \quad -0.25 \le \mathcal{C}_{T}^{\ell} \le 0.25$

values are fixed by the upper bound on BR(B $\rightarrow \pi$ l v) < 5 σ of HFLAV avarage

CKM FIT RESULTS:



Goodness of fit				
Data set	χ^2	d.o.f.	p value $[%]$	$ V_{ub} \times 10^3$
$\bar{B} \to \pi \ell \nu$	27.83	31	62.98	$3.79_{-0.15}^{+0.15}$
$\bar{B} \to \rho \ell \nu$	4.05	10	94.49	$2.92^{+0.28}_{-0.25}$
$\bar{B} \to \omega \ell \nu$	4.20	4	37.90	$3.00\substack{+0.38\\-0.32}$
all data	43.75	47	60.78	$3.59^{+0.13}_{-0.12}$

WET FIT RESULTS:

1

1.2 1.0 0.8 3^{3} 3^{3} 0.6 0.2 0.2 0.2 0.0 0.2 0.6 0.2 0.60.2

 $0.0 \xrightarrow{\mathcal{C}_{s}^{npc}}_{S^{s}} 0.0$ -0.2 -0.4 -0.6 0.6 0.4

$$\begin{aligned} \mathcal{C}_{V,L}^{\ell} &= 0.14, \quad \mathcal{C}_{V,R}^{\ell} = 0.89, \\ \mathcal{C}_{S,L}^{\ell} &= 0.00, \quad \mathcal{C}_{S,R}^{\ell} = 0.00, \quad \mathcal{C}_{T}^{\ell} = 0.00, \\ \mathcal{C}_{V,L}^{\ell} &= 0.89, \quad \mathcal{C}_{V,R}^{\ell} = 0.14, \\ \mathcal{C}_{S,L}^{\ell} &= 0.00, \quad \mathcal{C}_{S,R}^{\ell} = 0.00, \quad \mathcal{C}_{T}^{\ell} = 0.00, \end{aligned}$$

WET (only v_L) describes preferably the data:

$$\frac{P(\text{all data} | \text{WET})}{P(\text{all data} | \text{SM})} = 55, \quad \frac{P(\text{all data} | \text{WET})}{P(\text{all data} | \text{CKM})} = 60$$
$$Z \equiv P(D | M) = \int d\vec{x} P(D | \vec{x}, M) P_0(\vec{x} | M)$$

WET - BSM is favoured model!



CONCLUSIONS

- \Box we revisit LCSR prediction for the full set of $B \rightarrow \pi$ form factors by simultaneously fitting them, including correlations and focus on systematic uncertainties by using Bayesian fit and extrapolation in the full q² region
- □ we carry out combined fit with precise QCD lattice results and provide the most up-to-date theoretical (LCSR + LQCD) form factors in $B \rightarrow \pi$ decays

□ we add B → ρ, ω decays and usings average of experimental measurements of B → (π, ρ, ω) I v with correlations we perform fits and extract IVubI_{excl}

$$|V_{ub}|^{B \to \pi, \rho, \omega} = (3.59^{+0.13}_{-0.12}) \times 10^{-3}$$

compatible with the global CKMfitter fit:

$$|V_{ub}|^{\text{CKMfitter}} = (3.67^{+0.09}_{-0.07}) \times 10^{-3}$$

□ with perform WET (with only left-handed neutrinos) fit of all B → (π, ρ, ω) I v data, and conclude that the BSM is preferred over SM interpretation /more input is needed, in particular from theory side on B → (ρ, ω) I v decays/

□ we provide Gaussian Mixture Model of marginalized WET Wilson coefficients

- to provide computationally efficient way of using the WET parameter space without having to re-run a complicated, computationally expensive statistical analysis /in ancillary material of 2302. 05268 paper/

