

# Direct CPV in D decays at LHCb

Jolanta Brodzicka [INP Krakow]  
on behalf of LHCb

CKM2023 Santiago de Compostela

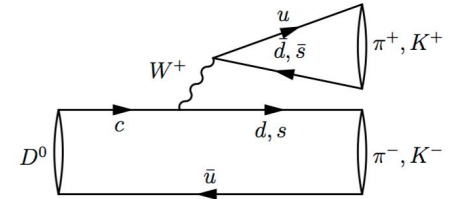
# Outline

- Basics of direct CPV
- CP asymmetries in  $D^0 \rightarrow K^+ K^-$  and  $D^0 \rightarrow \pi^+ \pi^-$
- Search for CPV in  $D_{(s)}^+ \rightarrow \eta^{(\prime)} \pi^+$  decays
- Search for CPV in  $D_{(s)}^+ \rightarrow K^- K^+ K^+$  with Miranda technique
- Examining  $D^0 \rightarrow \pi^+ \pi^- \pi^0$  and  $D^0 \rightarrow K_S K \pi$  with Energy Test
- Summary

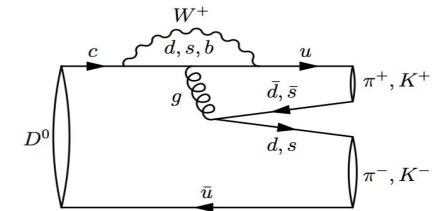
# Basics of direct CPV

- Occurs in decays
- Results in asymmetries of decay widths ( $A_{CP}$ ), amplitudes
- Requires two amplitudes with different weak and strong phases
- In charm decays realized through Tree + Penguin
- $c \rightarrow u$  Penguin is suppressed
  - b-loop is CKM suppressed
  - sd-loops are GIM suppressed, cancel in U-spin limit
- CPV in charm  $O(10^{-4} \div 10^{-3})$  within SM; depends on penguin size

Tree and Penguin contributions  
in  $D^0 \rightarrow K^+ K^-$  and  $D^0 \rightarrow \pi^+ \pi^-$



$$\mathcal{T} \simeq V_{ud} V_{cd}^*, V_{us} V_{cs}^*$$



$$\mathcal{P}_b \simeq \frac{m_b^2}{m_W^2} V_{ub} V_{cb}^*$$

$$\mathcal{P}_{sd} \simeq \frac{m_s^2 - m_d^2}{m_W^2} (V_{us} V_{cs}^* - V_{ud} V_{cd}^*)$$

# Basics of direct CPV (II)

- Impact of phases on sensitivity to CPV

- P-even asymmetry  $A_{CP} \equiv \frac{\Gamma(D \rightarrow f) - \Gamma(\bar{D} \rightarrow \bar{f})}{\Gamma(D \rightarrow f) + \Gamma(\bar{D} \rightarrow \bar{f})} \simeq \left| \frac{\mathcal{P}}{\mathcal{T}} \right| \cos\Delta\phi_{weak} \cos\Delta\phi_{strong}$

- P-odd asymmetry e.g. triple-product or  $\alpha$ -induced asymmetry [in  $D_{(s)} \rightarrow 4h, \Lambda_c^+ \rightarrow \Lambda h^+$ ]

$$A_{CP}^{T-odd}, A_{CP}^{\alpha} \simeq \left| \frac{\mathcal{P}}{\mathcal{T}} \right| \cos\Delta\phi_{weak} \sin\Delta\phi_{strong}$$

- P-even and P-odd asymmetries are complementary
- Direct CPV is decay-dependent; penguin only in SCS decays
- Accessible through time-integrated measurements

# What after the discovery?

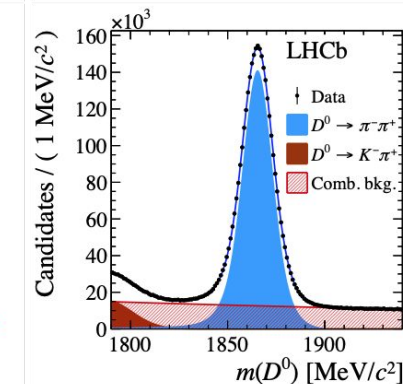
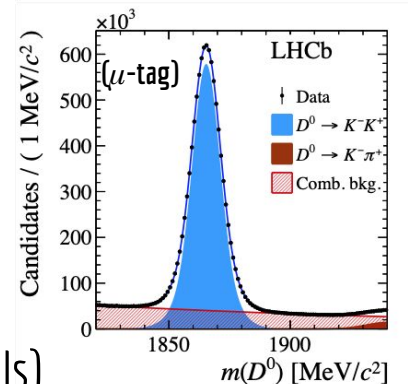
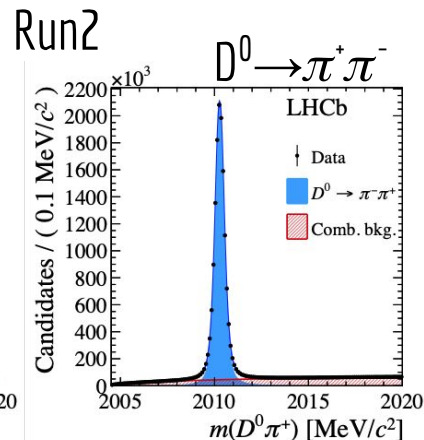
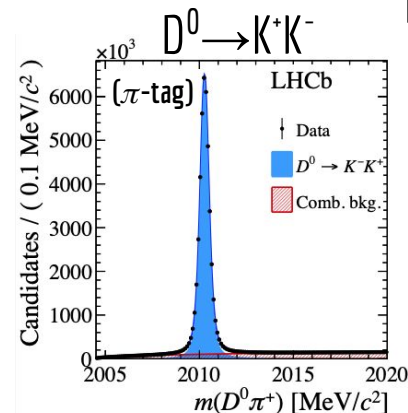
- Discovery of CPV in charm

$$\Delta A_{CP} \equiv A_{CP}(D^0 \rightarrow K^+ K^-) - A_{CP}(D^0 \rightarrow \pi^+ \pi^-)$$

- LHCb Run1+Run2 data
- $D^0$  from  $D^{*+} \rightarrow D^0 \pi^+$  ( $\pi$ -tag) and B decays ( $\mu$ -tag)

$$\Delta A_{CP} = (-15.4 \pm 2.9) \times 10^{-4} \quad (5.3\sigma)$$

- The upper end of SM predictions. Is it SM or beyond?
- How about individual asymmetries within  $\Delta A_{CP}$ ?
- Other decays related to  $D^0 \rightarrow h^+ h^-$  (via  $SU(3)_F$  or models)



# From $\Delta A_{CP}$ to individual $A_{CP}$ 's

- Measure  $A_{CP}(D^0 \rightarrow K^+K^-)$  and disentangle  $A_{CP}(D^0 \rightarrow \pi^+\pi^-)$  from  $\Delta A_{CP}$
- Run2 data,  $\pi$ -tagged sample:  $D^0 \rightarrow K^+K^-$  from  $D^{*+} \rightarrow D^0\pi_{tag}^+$
- Measure raw asymmetry of signal yields

$$A_{raw}(D^0 \rightarrow K^+K^-) = \frac{N(D^0) - N(\bar{D}^0)}{N(D^0) + N(\bar{D}^0)}$$

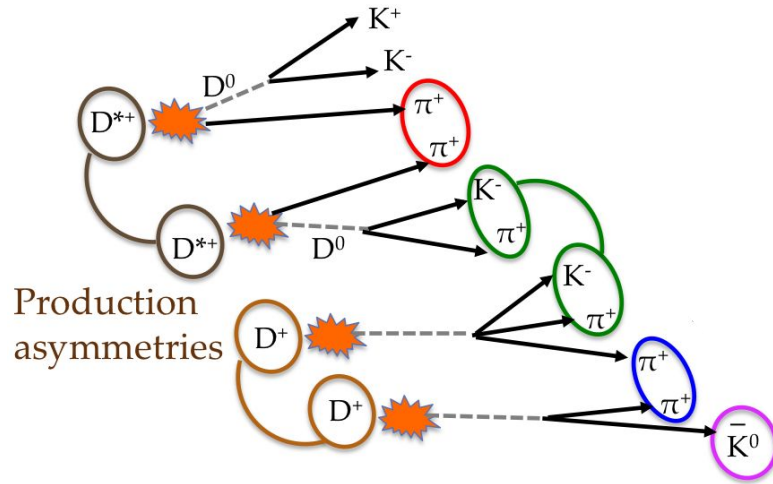
- Nuisance asymmetries of O(%) enter measured asymmetry [they cancel out in  $\Delta A_{CP}$ ]

$$A_{raw} \simeq A_{CP} + \boxed{A_{prod}(D^{*+})} + \boxed{A_{det}(\pi_{tag}^+)}$$

- **Production asymmetry:**  $\sigma(pp \rightarrow DX) < \sigma(pp \rightarrow \bar{D}X)$
- **Detection asymmetry:**  $\epsilon_{rec}(h^+) \neq \epsilon_{rec}(h^-)$  from different interactions with detector and detector asymmetries

# Removing nuisance asymmetries

- Set of calibration CF decays of  $D_{(s)}$  to overconstrain  $A_{\text{raw}}(D^0 \rightarrow K^+ K^-)$  and extract  $A_{\text{CP}}$



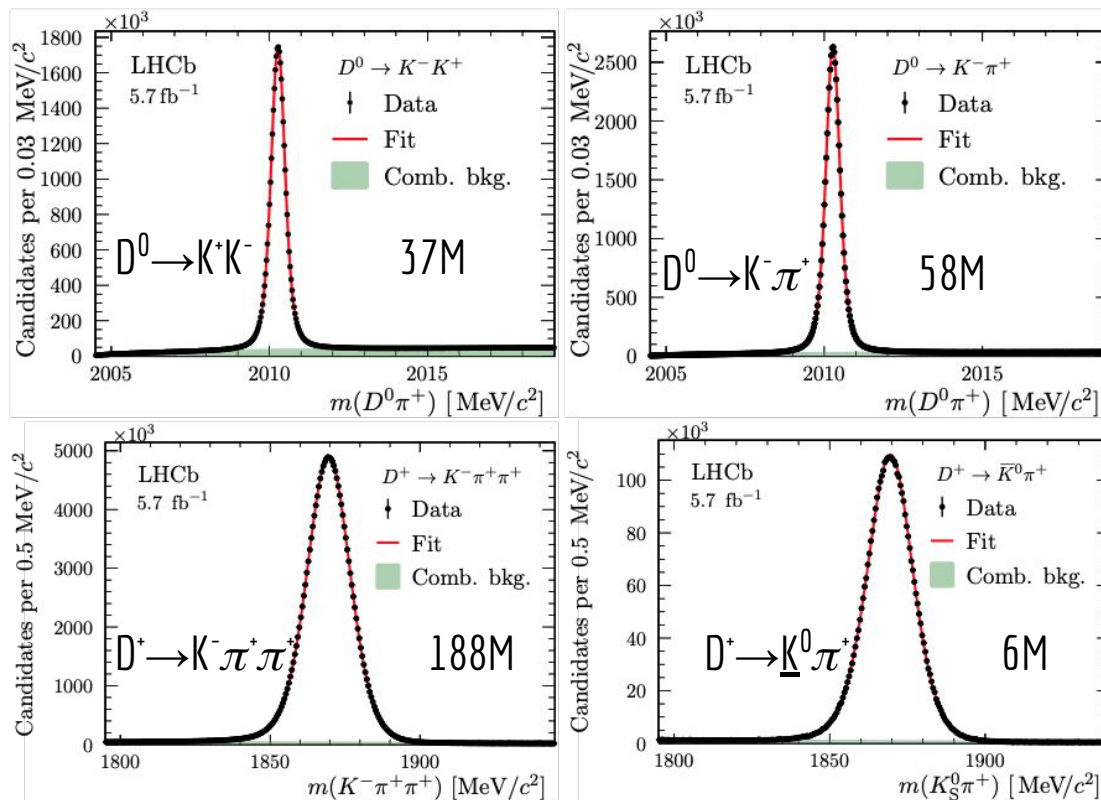
- $A_{\text{prod}}$  and  $A_{\text{det}}$  depend on kinematics of underlying particles. Equalize kinematics of calibration and signal decays
- $A(\bar{K}^0)$  of  $O(10^{-4})$ , calculated from known interactions of  $K^0$  and  $\bar{K}^0$  with detector, and mixing/CPV in kaon system

- Two calibration methods to increase statistical sensitivity

□ with  $D^+$   $A_{\text{CP}}(K^+ K^-) = A_{\text{raw}}(D^0 \rightarrow K^+ K^-) - A_{\text{raw}}(D^0 \rightarrow K^- \pi^+) + A_{\text{raw}}(D^+ \rightarrow K^- \pi^+ \pi^+) - A_{\text{raw}}(D^+ \rightarrow \bar{K}^0 \pi^+) + A(\bar{K}^0)$

□ with  $D_s^+$   $A_{\text{CP}}(K^+ K^-) = A_{\text{raw}}(D^0 \rightarrow K^+ K^-) - A_{\text{raw}}(D^0 \rightarrow K^- \pi^+) + A_{\text{raw}}(D_s^+ \rightarrow \phi \pi^+) - A_{\text{raw}}(D_s^+ \rightarrow \bar{K}^0 K^+) + A(\bar{K}^0)$

# Signal and calibration samples for $D^+$ method





# Individual direct CP asymmetries

- Combining two calibration methods gives

$$A_{CP}(D^0 \rightarrow K^+ K^-) = (6.8 \pm 5.4 \pm 1.6) \times 10^{-4}$$

- $A_{CP}$  is mostly from direct CPV with residual indirect CPV

$$A_{CP} \simeq a_{CP}^{dir} + \frac{\langle t \rangle}{\tau_D} \Delta Y \quad \Delta Y = -A_{\Gamma}(1 + y_{CP})$$

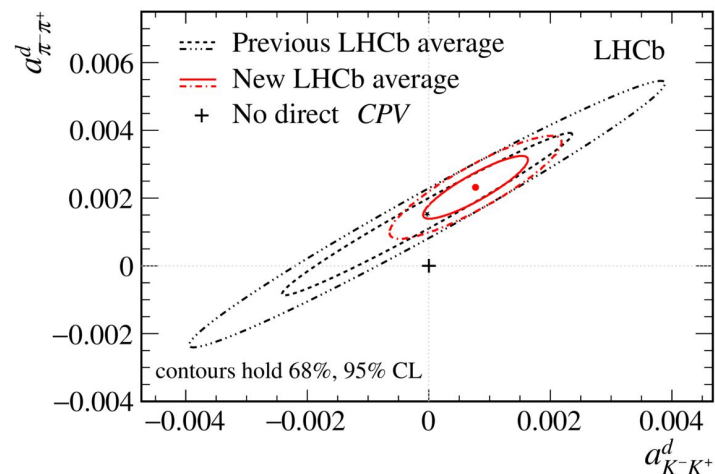
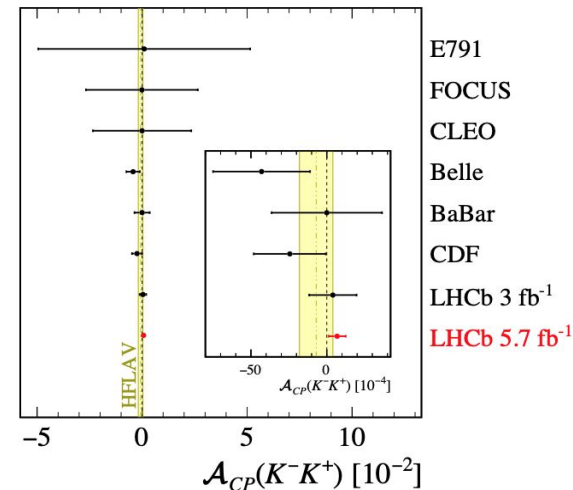
- Direct CP asymmetries extracted from  $A_{CP}(D^0 \rightarrow K^+ K^-)$  and  $\Delta A_{CP}$ , and combined with Run1 results

$$a_{K^+ K^-}^{dir} = (7.7 \pm 5.7) \times 10^{-4} \quad (1.4\sigma)$$

$$a_{\pi^+ \pi^-}^{dir} = (23.2 \pm 6.1) \times 10^{-4} \quad (3.8\sigma) \quad \text{First evidence!}$$

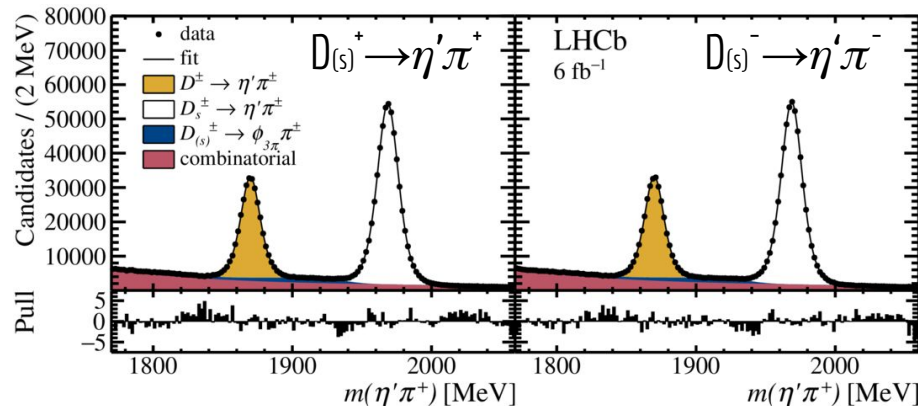
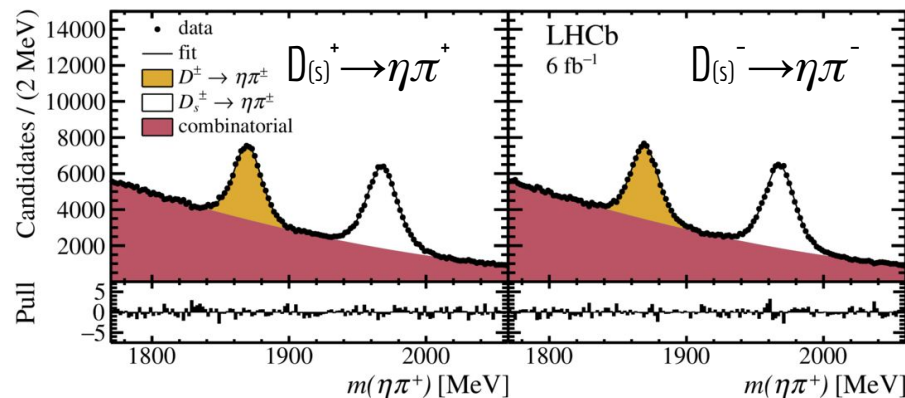
- The sum breaks U-spin limit at  $2.7\sigma$

$$a_{K^+ K^-}^{dir} + a_{\pi^+ \pi^-}^{dir} = (30.8 \pm 11.4) \times 10^{-4}$$



# Search for CPV in $D^+ \rightarrow \eta^{(\prime)} \pi^+$ and $D_s^+ \rightarrow \eta^{(\prime)} \pi^+$

- $D^+ \rightarrow \eta^{(\prime)} \pi^+$  are SCS decays ( $c \rightarrow \underline{d} \underline{d} u, s \underline{s} u$ ),  
 $D_s^+ \rightarrow \eta^{(\prime)} \pi^+$  are CF ( $c \rightarrow s \underline{d} u$ )
- Run2 data, with  $\eta^{(\prime)} \rightarrow \pi^+ \pi^- \gamma$
- $m(\eta^{(\prime)})$  constrained in  $m(\eta^{(\prime)} \pi^+)$
- $D_{(s)}^+$  signals from fits to  $m(\eta^{(\prime)} \pi^+)$
- x-check:  $m(\eta^{(\prime)} \pi^+)$  fits in  $m(\eta^{(\prime)})$  bins
- Total yields:  
0.1M of  $D \rightarrow \eta \pi$ , 0.6M of  $D \rightarrow \eta' \pi$   
0.1M of  $D_s \rightarrow \eta \pi$ , 1.1M of  $D_s \rightarrow \eta' \pi$



# Search for CPV in $D^+ \rightarrow \eta^{(\prime)} \pi^+$ and $D_s^+ \rightarrow \eta^{(\prime)} \pi^+$

- Nuisance asymmetries to account for

$$A_{raw}(D_{(s)}^+ \rightarrow \eta^{(\prime)} \pi^+) \simeq A_{CP}(D_{(s)}^+ \rightarrow \eta^{(\prime)} \pi^+) + A_{prod}(D_{(s)}^+) + A_{det}(\pi^+)$$

- Use  $D_{(s)}^+ \rightarrow \phi \pi^+$  calibration channels, with  $A_{CP}(D^+ \rightarrow \phi \pi^+) = (0.5 \pm 5.1) \times 10^{-4}$  and  $A_{CP}(D_s^+ \rightarrow \phi \pi^+) = 0$

$$A_{CP}(D^+ \rightarrow \eta^{(\prime)} \pi^+) = A_{raw}(D^+ \rightarrow \eta^{(\prime)} \pi^+) - A_{raw}(D^+ \rightarrow \phi \pi^+) + A_{CP}(D^+ \rightarrow \phi \pi^+)$$

$$A_{CP}(D_s^+ \rightarrow \eta^{(\prime)} \pi^+) = A_{raw}(D_s^+ \rightarrow \eta^{(\prime)} \pi^+) - A_{raw}(D_s^+ \rightarrow \phi \pi^+) + \cancel{A_{CP}(D_s^+ \rightarrow \phi \pi^+)}$$

- Results consistent with CP symmetry

$$A_{CP}(D^+ \rightarrow \eta \pi^+) = (3.4 \pm 6.6 \pm 1.6 \pm 0.5) \times 10^{-3}$$

$$A_{CP}(D^+ \rightarrow \eta' \pi^+) = (4.9 \pm 1.8 \pm 0.6 \pm 0.5) \times 10^{-3}$$

$$A_{CP}(D_s^+ \rightarrow \eta \pi^+) = (3.2 \pm 5.1 \pm 1.2) \times 10^{-3}$$

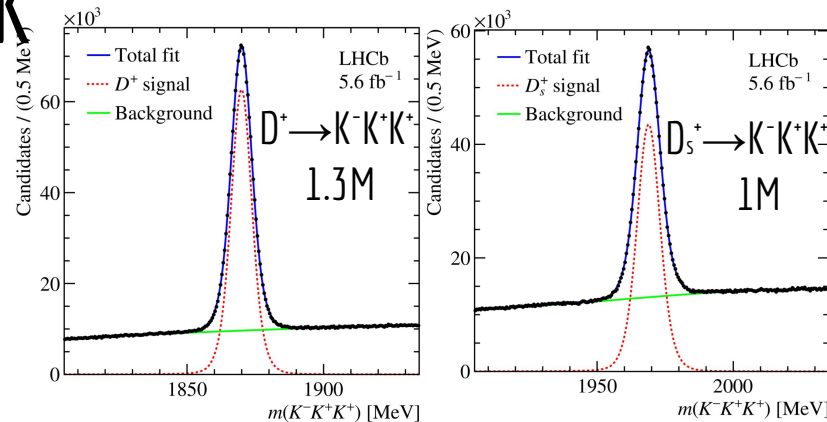
$$A_{CP}(D_s^+ \rightarrow \eta' \pi^+) = (0.1 \pm 1.2 \pm 0.8) \times 10^{-3}$$

# CPV in multibody $D_{(s)}$ decays

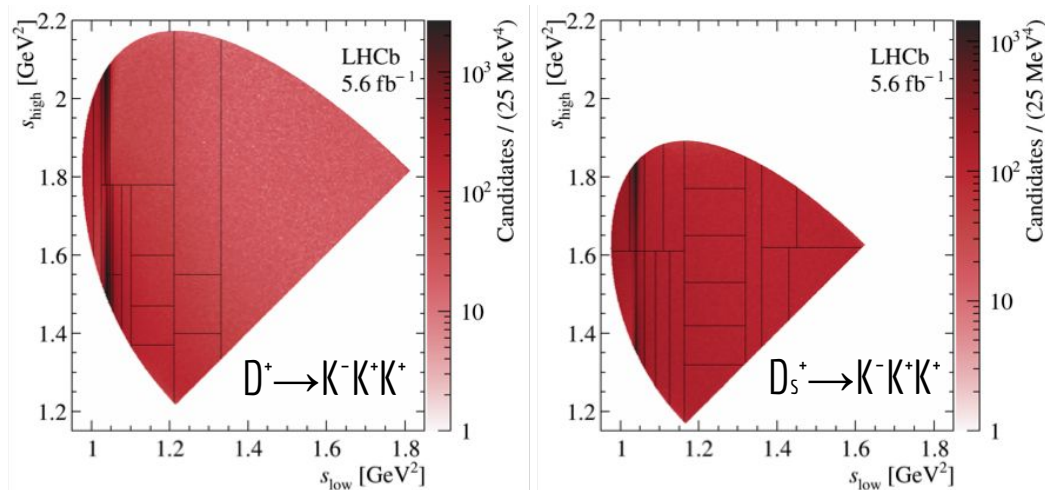
- Weak amplitudes as in two-body decays
- Similarities between  $D^0 \rightarrow \pi^+ \pi^- \pi^0$  and  $D \rightarrow \pi \pi$ ,  $D^0 \rightarrow K_s K^- \pi^+$  and  $D \rightarrow K K$
- *Complications* arise from strong amplitudes
- But rich dynamics (resonances, rescattering, partial-waves) assure large strong-phase variation across decay phase-space  $\Rightarrow$  increase sensitivity to CPV
  
- Probe  $D_{(s)}$  decay phase-space to search for local CPV
  - **Model-dependent** amplitude analysis: CP asymmetry per amplitude
  - **Model-independent** techniques: discovery tools checking consistency with CP symmetry

# Search for CPV in $D_{(s)}^+ \rightarrow K^- K^+ K^+$

- $D^+ \rightarrow K^- K^+ K^+$  is DCS, while  $D_s^+ \rightarrow K^- K^+ K^+$  is SCS
- S-wave dominated decays LHCb JHEP 04, 063 (2019)
- Run2 data, signal significance optimised with BDT
- Dalitz plots folded into higher vs. lower  $m^2(K^+ K^-)$

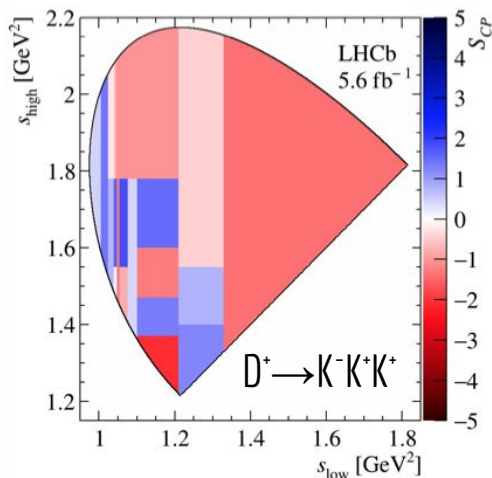


- $\phi$  state + broad S-wave
- 21 bins of similar statistics
- For CPV test, bckgd. subtracted with  $m(K^- K^+ K^+)$  fits in Dalitz bins

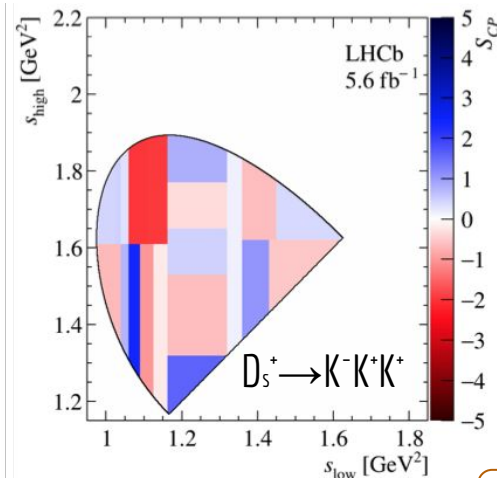


# Miranda Test for $D_{(s)}^+ \rightarrow K^- K^+ K^+$ decays

- Local-CPV observable in i-th Dalitz bin  $S_{CP}^i = \frac{N^i(D_{(s)}^+) - \alpha N^i(D_{(s)}^-)}{\sqrt{\alpha(\delta_{N^i(D_{(s)}^+) }^2) + \delta_{N^i(D_{(s)}^-)}^2}}$ , with  $\alpha = \frac{\sum_i N^i(D_{(s)}^+)}{\sum_i N^i(D_{(s)}^-)}$
- $S_{CP}$  is significance of difference between  $D_{(s)}^+$  and  $D_{(s)}^-$  signals



**p-value=32%**



**p-value=13%**

- With no-CPV,  $S_{CP}$  follows standard normal distribution
- $\chi^2$  test,  $\chi^2 = \sum (S_{CP}^i)^2$   
ndf = nbins - 1
- Give p-value for consistency with no-CPV hypothesis

Both consistent with CP symmetry

# Energy Test

- Unbinned method for statistical comparison of two distributions, e.g.  $D$  and  $\bar{D}$  phase space
- Test Statistics based on distance of event pairs (ij)

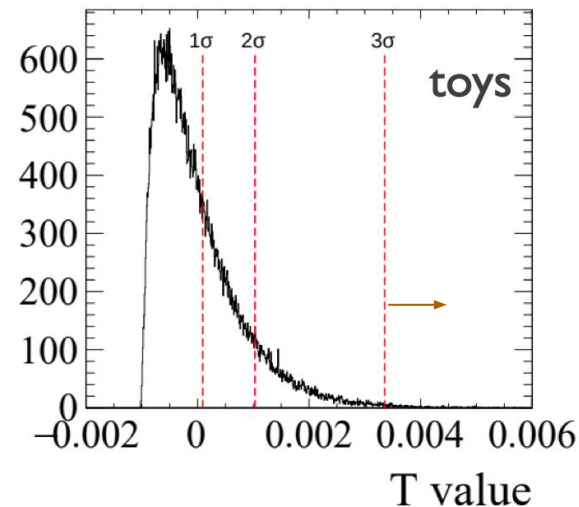
$$T \equiv \frac{1}{2n(n-1)} \sum_{i,j \neq i}^n \psi_{ij} + \frac{1}{2\bar{n}(\bar{n}-1)} \sum_{i,j \neq i}^{\bar{n}} \psi_{ij} - \frac{1}{n\bar{n}} \sum_{i,j}^{n,\bar{n}} \psi_{ij}$$

Average distance in  $D$  sample

in  $\bar{D}$  sample

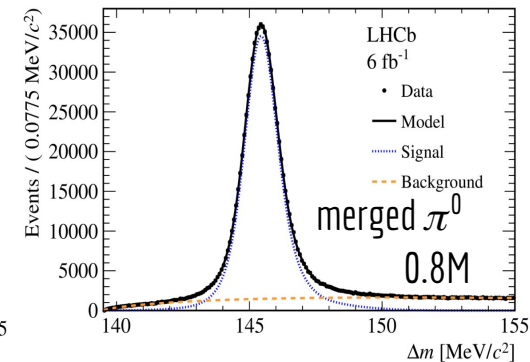
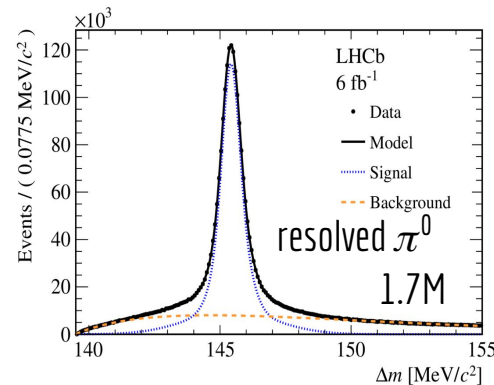
between  $D$  and  $\bar{D}$

- Distance function  $\psi(d_{ij}) = \exp(-d_{ij}^2/2\delta)$
- Distance in Dalitz space  $d_{ij}^2 = (\Delta s_{12})_{ij}^2 + (\Delta s_{13})_{ij}^2 + (\Delta s_{23})_{ij}^2$
- Compare **measured  $T_0$  value** with T-distribution for CP-symmetrized sample (permutations)
- p-value =  $n(T > T_0)/n$  for no-CPV hypothesis

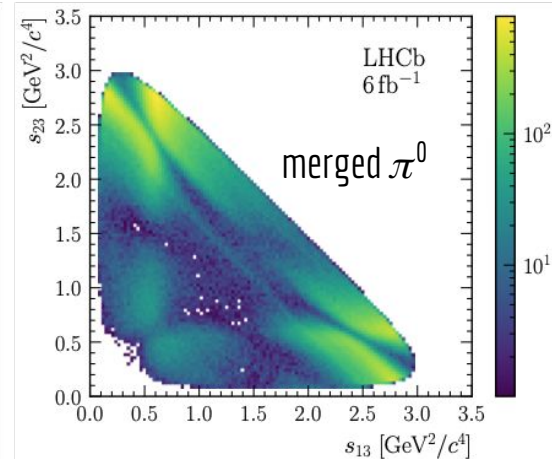
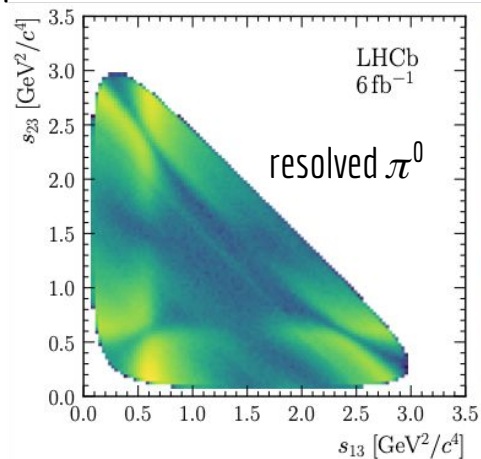


# Search for CPV in $D^0 \rightarrow \pi^+ \pi^- \pi^0$

- SCS decays
- p-value  $\approx 2\%$  in Run1 PLB 740, 158 (2015)
- Run2 data,  $D^0$  from  $D^{*+} \rightarrow D^0 \pi_{\text{tag}}^+$
- Resolved and merged  $\pi^0 \rightarrow \gamma\gamma$
- BDT selection for resolved sample



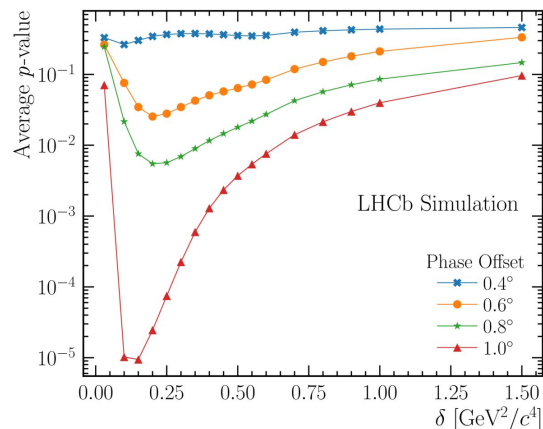
- $\rho^\pm, \rho^0$  dominate Dalitz space
- Efficiency drop for low- $p_T \pi^0$  in merged sample





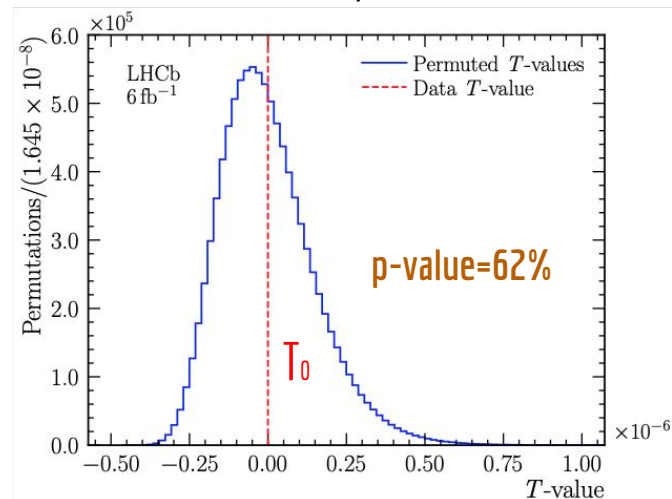
# Energy Test for $D^0 \rightarrow \pi^+ \pi^- \pi^0$

- For combined merged and resolved samples
- Optimisation of  $\delta$  metric parameter with *realistic* toys CPV induced via phase offset between  $D^0 \rightarrow \rho^- \pi^+$  and  $\bar{D}^0 \rightarrow \rho^+ \pi^-$



- Method validated with  $D^0 \rightarrow K^- \pi^+ \pi^0$ , toys with detection asymmetries,  $\Delta m$  sidebands

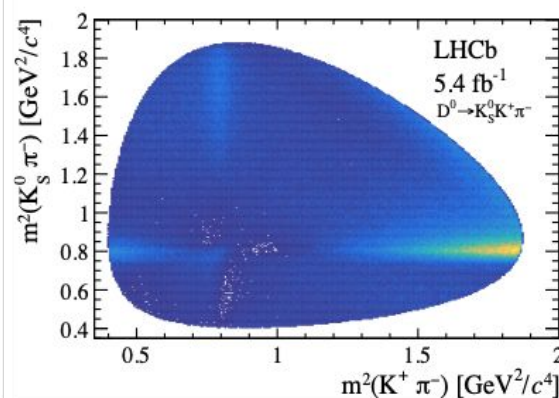
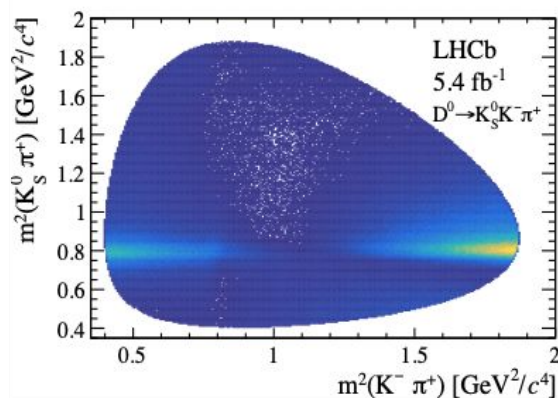
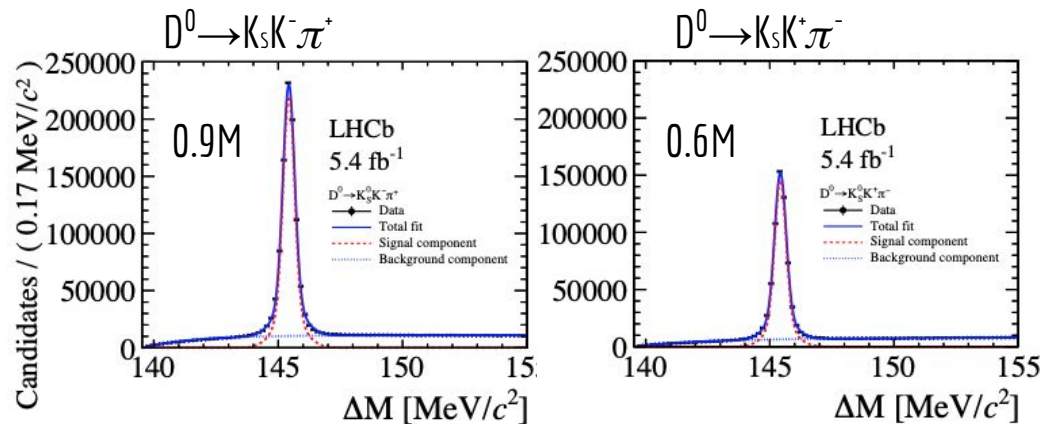
- Measurement for data



- Data consistent with CP symmetry

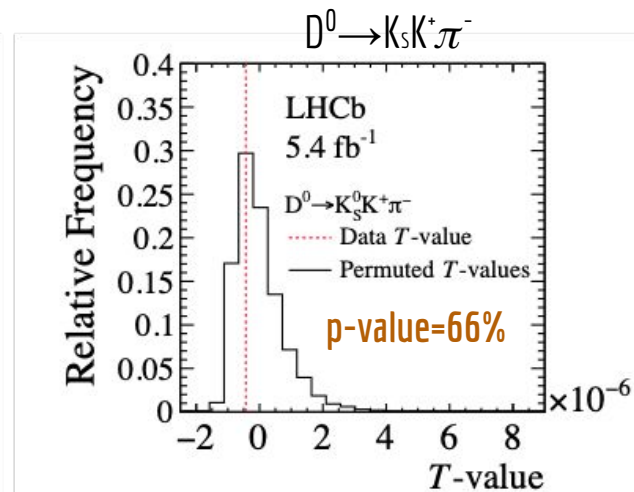
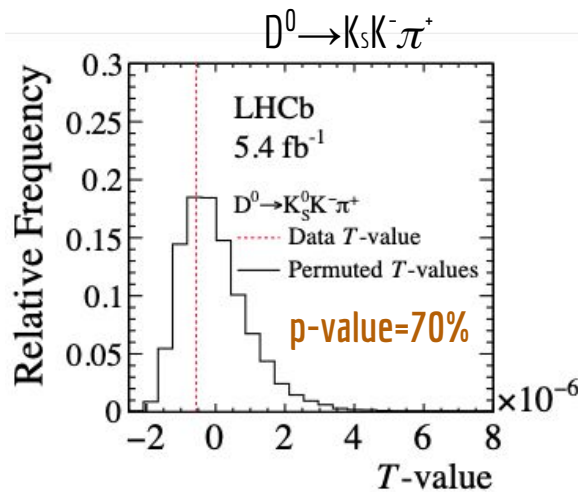
# Search for CPV in $D^0 \rightarrow K_S K^- \pi^+$ and $D^0 \rightarrow K_S K^+ \pi^-$ PRELIMINARY

- SCS decays
- Model-dependent search in Run1  
PRD 93, 052018 (2016)
- Run2 data,  $D^0$  from  $D^{*+} \rightarrow D^0 \pi_{\text{tag}}^+$
- $K_S \rightarrow \pi^+ \pi^-$  inside or outside VELO



# Energy Test for $D^0 \rightarrow K_s K^- \pi^+$ and $D^0 \rightarrow K_s K^+ \pi^-$

- Optimal metric parameter  $\delta \approx 0.2 \text{ GeV}^2$
- Sensitivity to CPV scenarios with phase offset  $\approx 2^\circ$  or amplitude difference  $\approx 2\%$  between  $D^0$  and  $\bar{D}^0$  in  $\bar{D}^0 \rightarrow K^{*\pm} K^\mp$
- Data consistent with no-CPV



- Method validated with  $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$  and  $D^0 \rightarrow K_s \pi^+ \pi^-$  decays, and  $\Delta m$  sidebands

# Summary

- Large charm samples at LHCb give a unique opportunity for CP violation searches
- Milestone: CPV discovery through  $\Delta A_{CP}$  in 2019
- First evidence in individual channel,  $D^0 \rightarrow \pi^+ \pi^-$

$$a_{\pi^+ \pi^-}^{dir} = (23.2 \pm 6.1) \times 10^{-4} \quad (3.8\sigma)$$

- Recent searches in other two-body channels,  $D^0 \rightarrow K^+ K^-$  and  $D_s^+ \rightarrow \eta^{(\prime)} \pi^+$
- Testing multibody decays for local CPV  
 $D_{(s)}^+ \rightarrow K^- K^+ K^+$ ,  $D^0 \rightarrow \pi^+ \pi^- \pi^0$  and  $D^0 \rightarrow K_S K^+ \pi^\mp$  All consistent with CP symmetry
- More to come with Run2 data

# Backup slides

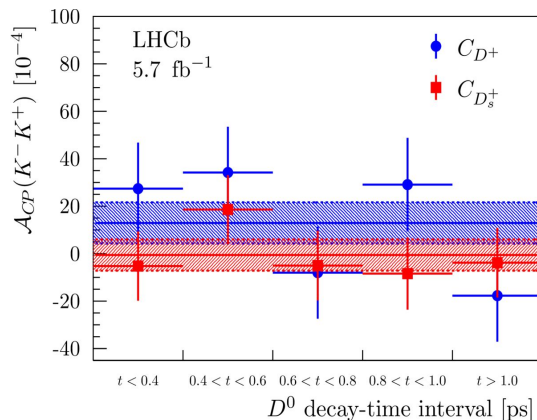
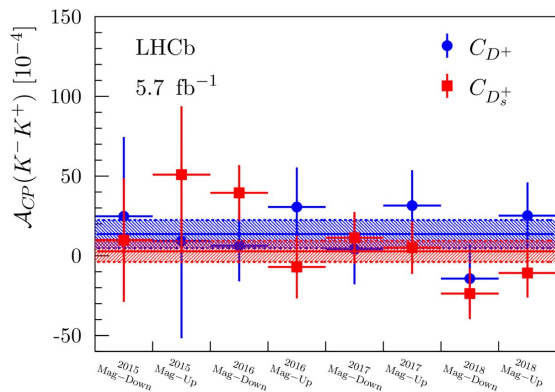
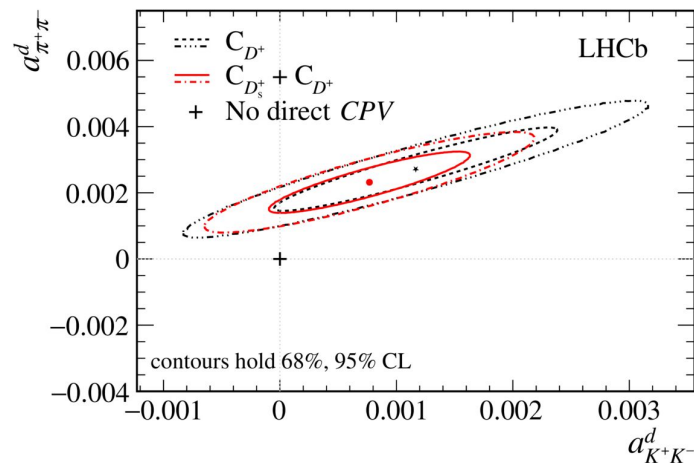
# Cross-checks in $A_{CP}(D^0 \rightarrow K^+K^-)$

- $A_{CP}$  from two methods, correlations: 0.05 (stat), 0.28 (syst)

$$C_{D^+} : \mathcal{A}_{CP}(K^-K^+) = [13.6 \pm 8.8 \text{ (stat)} \pm 1.6 \text{ (syst)}] \times 10^{-4},$$

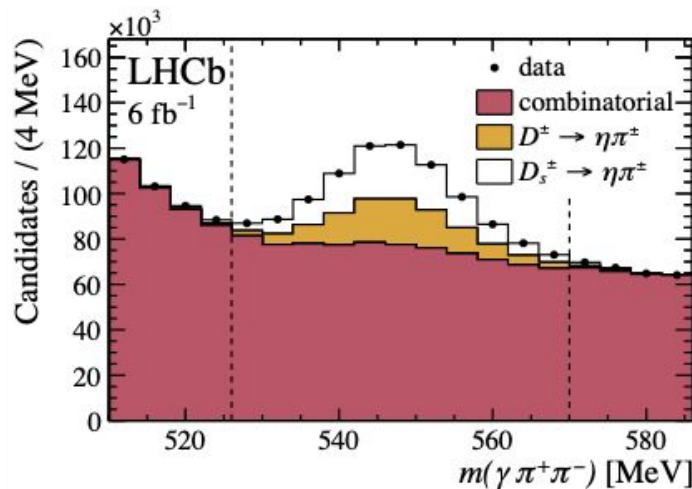
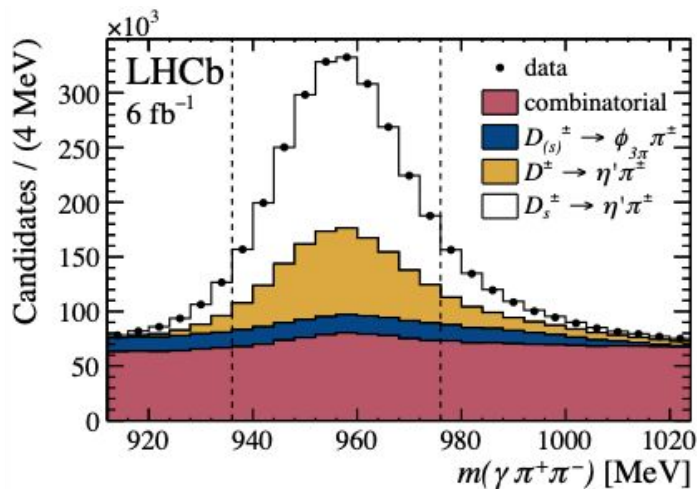
$$C_{D_s^+} : \mathcal{A}_{CP}(K^-K^+) = [2.8 \pm 6.7 \text{ (stat)} \pm 2.0 \text{ (syst)}] \times 10^{-4},$$

- Stability against various conditions



# Search for CPV in $D_{(s)}^+ \rightarrow \eta \pi^+$ and $D_{(s)}^+ \rightarrow \eta' \pi^+$

- Fits to  $m(\eta^{(\prime)} \pi^+)$  in  $m(\eta^{(\prime)})$  bins to check for non- $\eta^{(\prime)}$  background



- $D_{(s)}^+$  signal contains correctly reconstructed  $\eta^{(\prime)}$  signal
- Small background from random combinations of correct  $\eta^{(\prime)}$

# Search for CPV in $D_{(s)}^+ \rightarrow \eta \pi^+$ and $D_{(s)}^+ \rightarrow \eta' \pi^+$

Table 1: Systematic uncertainties associated to values of  $\mathcal{A}^{\text{raw}}$  (%).

Source	$D_s^+ \rightarrow \eta' \pi^+$	$D^+ \rightarrow \eta' \pi^+$	$D_s^+ \rightarrow \eta \pi^+$	$D^+ \rightarrow \eta \pi^+$
Fit model, signal	0.04	0.04	0.10	0.16
Fit bias	0.01	0.01	0.01	0.02
Secondary decays	0.06	0.03	0.06	0.03
$\mathcal{A}^{\text{KK}}$	0.01	0.02	0.01	0.02
Fit model, control	0.03	0.00	0.03	0.00
Weighting	0.01	0.01	0.02	0.00
Total	0.08	0.06	0.12	0.16

- 1% correlation btw  $\mathcal{A}_{\text{CP}}$  of  $D_{(s)}^+$  channels due to using shared control mode  $D_{(s)}^+ \rightarrow \phi \pi^+$
- Combination with Run1 PLB 771, 21 (2017) and Run2 results for  $D_{(s)}^+ \rightarrow \eta \pi^+$  with  $\eta \rightarrow e^+ e^- \gamma$  JHEP 06, 019 (2021)

$$\mathcal{A}^{\text{CP}}(D^+ \rightarrow \eta \pi^+) = (0.34 \pm 0.66 \pm 0.16 \pm 0.05)\%,$$

$$\mathcal{A}^{\text{CP}}(D_s^+ \rightarrow \eta \pi^+) = (0.32 \pm 0.51 \pm 0.12)\%,$$

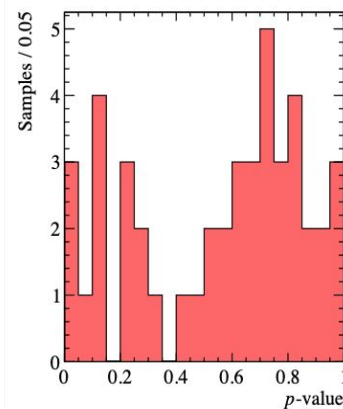
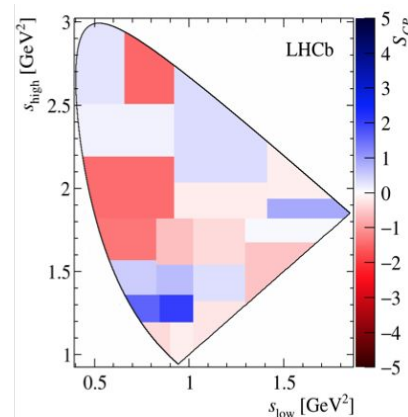
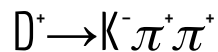
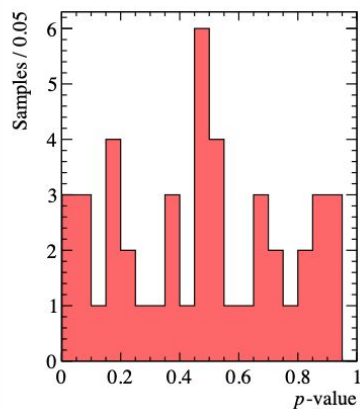
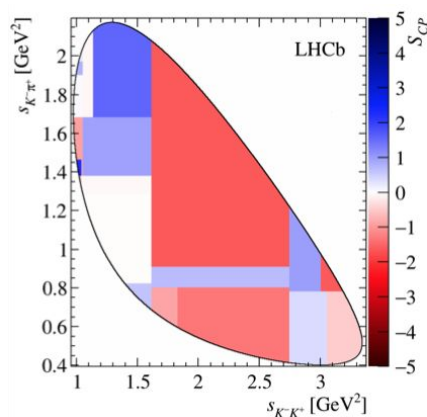
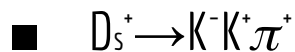
$$\mathcal{A}^{\text{CP}}(D^+ \rightarrow \eta' \pi^+) = (0.49 \pm 0.18 \pm 0.06 \pm 0.05)\%,$$

$$\mathcal{A}^{\text{CP}}(D_s^+ \rightarrow \eta' \pi^+) = (0.01 \pm 0.12 \pm 0.08)\%,$$



# Search for CPV in $D_{(s)}^+ \rightarrow K^- K^+ K^+$ decays

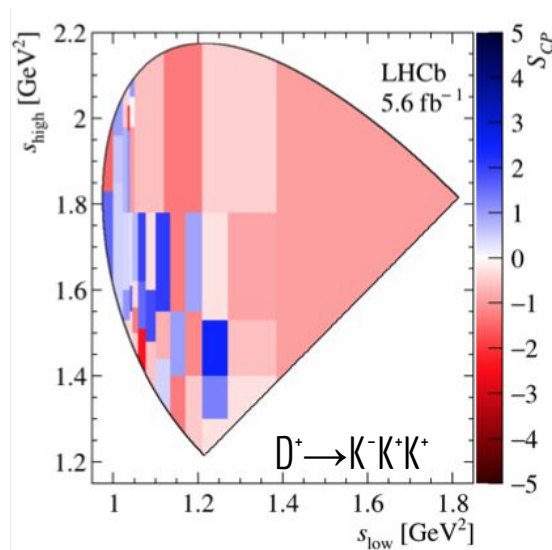
- Sensitivity to (local) nuisance asymmetries tested with CF decays, with various binning schemes



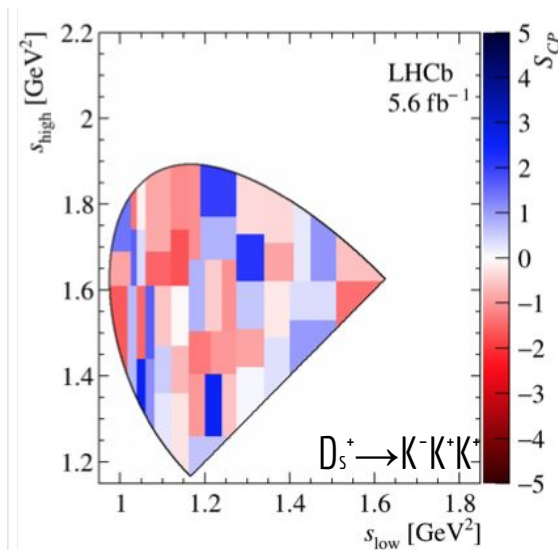
- p-value distributions for CF samples split into subsamples of signal-like statistics

# Miranda Test for $D_{(s)}^+ \rightarrow K^- K^+ K^+$ decays

- Alternative binning schemes [50 bins]



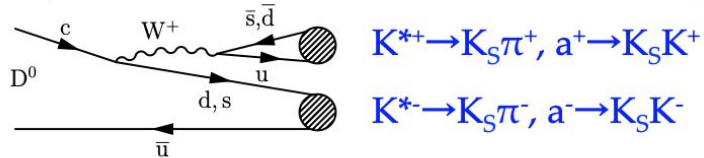
p-value=8%



p-value=10%

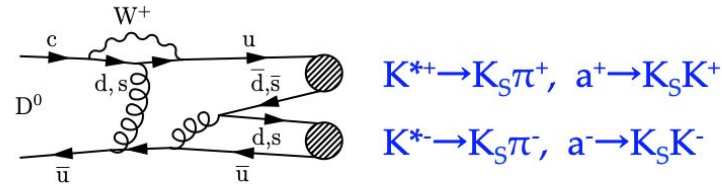
# Quark diagrams for $D^0 \rightarrow K_S K^- \pi^+$ and $D^0 \rightarrow K_S K^+ \pi^-$

- $D^0 \rightarrow K_S K^- \pi^+$  favoured over  $D^0 \rightarrow K_S K^+ \pi^-$  (BF ratio  $\sim 0.65$ ) [\*]
- External W-emission, SCS



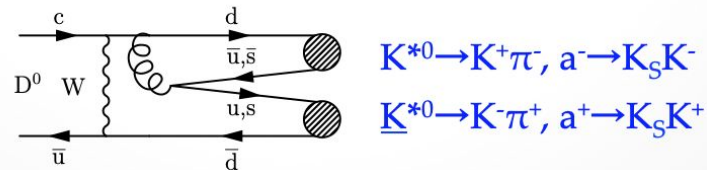
[\*]  $BR(D^0 \rightarrow K^*(892)^+ K^-) > BR(D^0 \rightarrow K^*(892)^- K^+)$ , as respectively  $K^{*+}$  and  $K^+$  couple to  $W^+$

- Penguin diagram



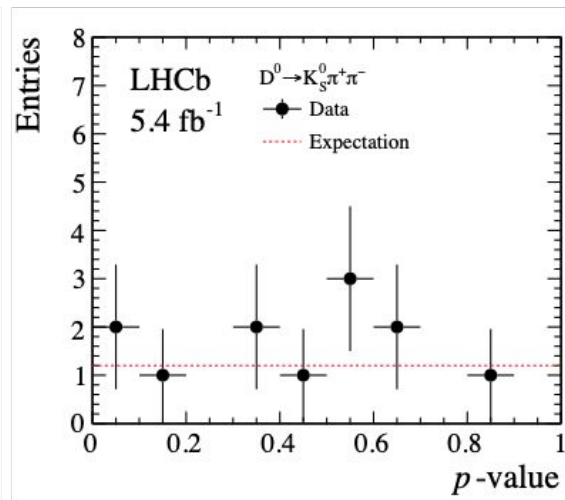
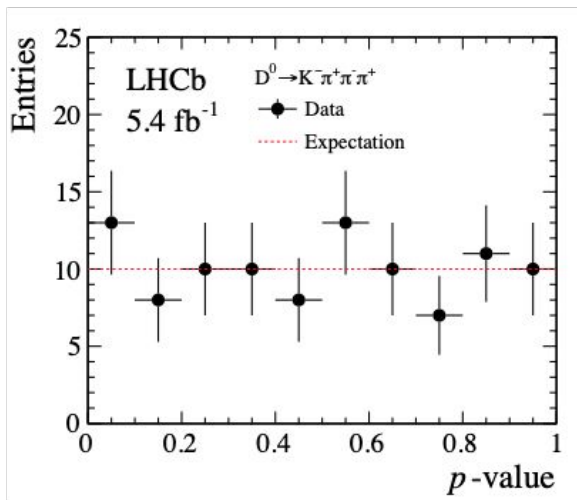
- W-exchange, SCS & colour suppressed

the only way to get  $K^{*0} \bar{K}^0$  and  $K^0 \bar{K}^{*0}$ ; they contribute with opposite signs



# Energy Test for $D^0 \rightarrow K_s K^- \pi^+$ and $D^0 \rightarrow K_s K^+ \pi^-$

- Method validation with CF-dominated decays,  $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$  and  $D^0 \rightarrow K_s \pi^+ \pi^-$



- No sensitivity to detection asymmetries of  $K\pi$  system or  $K_s$  related asymmetries