

## CP violation in $D \rightarrow \pi\pi$ and $D \rightarrow KK$

Ulrich Nierste

Institute for Theoretical Particle Physics

KIT Center for Elementary Particle and Astroparticle Physics (KCETA)



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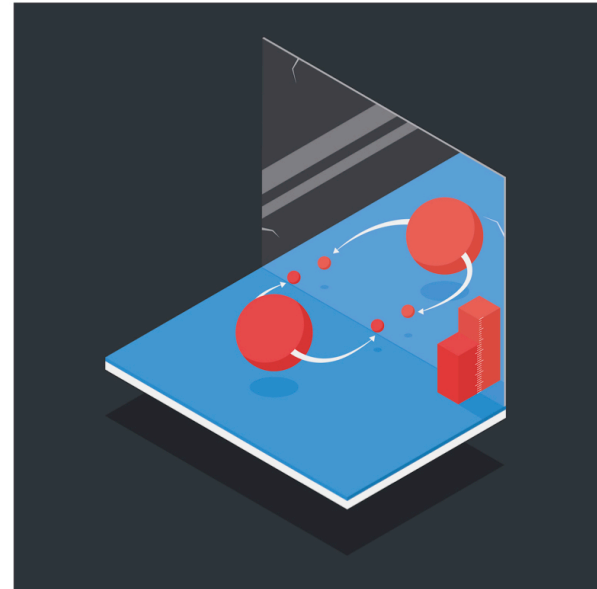
$$\begin{aligned}\Delta a_{CP} &\equiv a_{CP}^{\text{dir}}(D^0 \rightarrow K^+ K^-) \\ &\quad - a_{CP}^{\text{dir}}(D^0 \rightarrow \pi^+ \pi^-) \\ &= (-15.4 \pm 2.9) \cdot 10^{-4}\end{aligned}$$

discovery of CP violation in charm decays

## LHCb sees a new flavour of matter-antimatter asymmetry

The LHCb collaboration has observed a phenomenon known as CP violation in the decays of a particle known as a D0 meson for the first time

21 MARCH, 2019



# Role of charm physics

## Charm decays

- have no stakes in Standard-Model CKM metrology, but
- have a unique role to probe new physics in the flavor sector of **up-type** quarks.

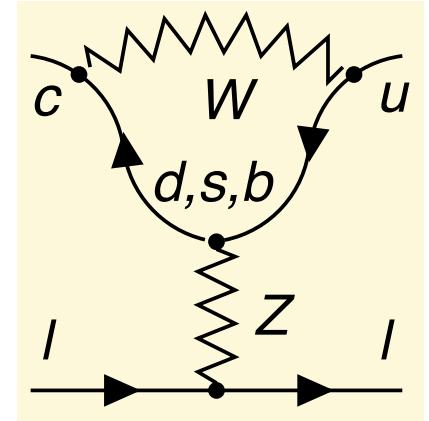
# Problem of charm physics

FCNC example  $D^0 \rightarrow \ell^+ \ell^-$ :

- loop with  $b$  comes with small  $|V_{cb}^* V_{ub}| = 1.6 \cdot 10^{-4}$
- loops with  $d, s$  are proportional to

$$\frac{G_F}{M_Z^2} \cdot \underbrace{(m_s - m_d)}_{\substack{\text{U-spin} \\ \text{breaking} \\ \text{GIM}}} \cdot \underbrace{(m_s + m_d)}_{\substack{\text{artefact of} \\ \text{perturbation theory}}}$$

- No successful calculation of charm FCNC amplitudes.



U-spin symmetry: unitary rotations

of  $\begin{pmatrix} s \\ d \end{pmatrix}$ , exact for  $m_s = m_d$ .

# CKM elements

$D^0 \rightarrow \pi^+\pi^-$  and  $D^0 \rightarrow K^+K^-$  are singly Cabibbo-suppressed (SCS) decays.

In SCS amplitudes three CKM structures appear:

$$\lambda_d = V_{cd}^* V_{ud}, \lambda_s = V_{cs}^* V_{us}, \lambda_b = V_{cb}^* V_{ub} \text{ and}$$

$\lambda_d + \lambda_s + \lambda_b = 0$  is invoked to eliminate one of these.

# Decay amplitude

decay amplitude

Recall:  $\lambda_j = V_{cj}^* V_{uj}$

Commonly used:  $\mathcal{A}^{\text{SCS}} \equiv \lambda_{sd} A_{sd} - \frac{\lambda_b}{2} A_b$

with  $\lambda_{sd} = \frac{\lambda_s - \lambda_d}{2} \simeq \lambda_s$  and  $-\frac{\lambda_b}{2} = \frac{\lambda_s + \lambda_d}{2}$ .

U-spin triplet U-spin singlet

Since  $|\lambda_b| / |\lambda_{sd}| \sim 10^{-3}$ , only  $A_{sd}$  is relevant for decay rates.

# CP asymmetries

In the Standard Model all CP asymmetries in hadronic charm decays are proportional to  $\text{Im} \frac{\lambda_b}{\lambda_{sd}} = -6 \cdot 10^{-4}$ .

Recall  $\mathcal{A}^{\text{SCS}} \equiv \lambda_{sd} A_{sd} - \frac{\lambda_b}{2} A_b$

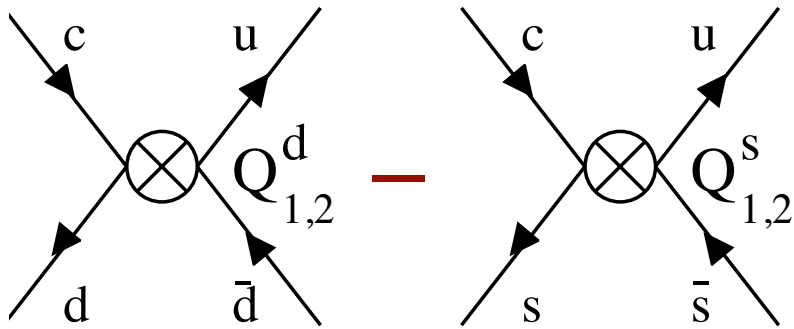
tree penguin

$$a_{CP}^{\text{dir}} = \text{Im} \frac{\lambda_b}{\lambda_{sd}} \text{Im} \frac{A_b}{A_{sd}}$$

U-spin limit:  $A_b(D^0 \rightarrow K^+K^-) = A_b(D^0 \rightarrow \pi^+\pi^-)$  and  
 $A_{sd}(D^0 \rightarrow K^+K^-) = -A_{sd}(D^0 \rightarrow \pi^+\pi^-)$ ,  
so that  $\Delta a_{CP} = 2a_{CP}(D^0 \rightarrow K^+K^-) = -2a_{CP}(D^0 \rightarrow \pi^+\pi^-)$ .

# $D^0 \rightarrow K^+K^-, \pi^+\pi^-$ amplitudes

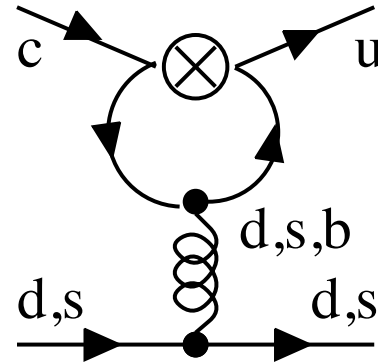
$A_{sd}$  (“tree”) from  $W$  exchange:



$\lambda_s \simeq -\lambda_d \Rightarrow KK$  and  $\pi\pi$  dominantly produced from triplet amplitude  $A_{sd}$

Recall  $\mathcal{A}^{SCS} \equiv \lambda_{sd}A_{sd} - \frac{\lambda_b}{2}A_b$

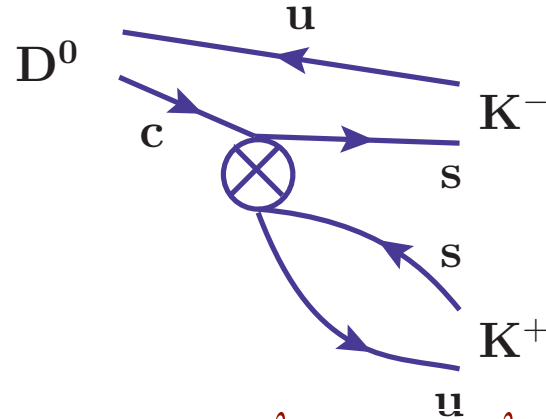
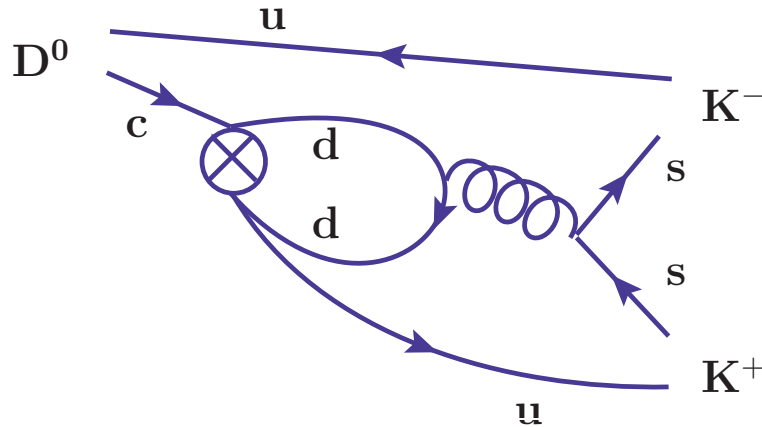
Small  $A_b$  dominantly from penguin topology:





# CP asymmetry in $D^0 \rightarrow K^+K^-$

Interference of  $A_b$  with  $A_{sd}$ :



The penguin diagram involves  $\lambda_d = -\lambda_s - \lambda_b$  and  $a_{CP} \propto \text{Im} \frac{\lambda_d}{\lambda_s} = -\text{Im} \frac{\lambda_b}{\lambda_s}$ .

Its absorptive part leads to  $\text{Im} \frac{A_b}{A_{sd}} \neq 0$ .

# Theory always at your service

The theory community has delivered a **perfect service** to the experimental colleagues:

**Every measurement** hinting at some non-zero CP asymmetry was **successfully postdicted** offering interpretations both

- within the Standard Model  
and
- as evidence for **new physics!**

And we are not stubborn at all: **“New data — new opinions!”**



$\Delta a_{CP}$

LHCb 2019:  $\Delta a_{CP} = (-15.4 \pm 2.9) \cdot 10^{-4}$

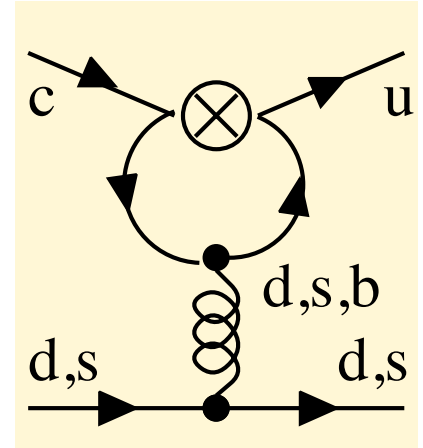
Prediction using QCD sum rules:  $|\Delta a_{CP}| \leq (2.0 \pm 0.3) \cdot 10^{-4}$

A. Khodjamirian, A. Petrov, Phys.Lett. B774 (2017) 235

Difference by a factor of 7.

New physics?

Or poorly understood QCD dynamics enhancing the penguin contribution?



# Long-distance QCD

KCETA



**“I summon the spirits of long-distance enhancement”**

## 2022: $a_{CP}(D^0 \rightarrow K^+K^-)$

LHCb 2022:  $a_{CP}(D^0 \rightarrow K^+K^-) = (7.7 \pm 5.7) \cdot 10^{-4}$ .

Thus  $\Delta a_{CP}$  implies  $a_{CP}(D^0 \rightarrow \pi^+\pi^-) = (23.1 \pm 6.1) \cdot 10^{-4}$ .

- $a_{CP}(D^0 \rightarrow K^+K^-)$  complies with the calculation of Khodjamirian and Petrov.
- For approximate U-spin limit  $a_{CP}(D^0 \rightarrow K^+K^-) \approx -a_{CP}(D^0 \rightarrow \pi^+\pi^-)$  to work, with future data  $a_{CP}(D^0 \rightarrow K^+K^-)$  must flip sign.
- Will future data decrease  $|\Delta a_{CP}|$  and will the  $5\sigma$  discovery eventually go away?
- Or did LHCb discover **new physics** in 2019?

# New physics

New physics amplitude interfering with Standard-Model (SM) tree amplitude:

$$\mathcal{A}^{\text{SCS}} \equiv \lambda_{sd} A_{sd} + a A_{\text{NP}}$$

with complex coupling  $a$ ,

neglecting SM penguin.

$$a_{\text{CP}}^{\text{dir}} = -2 \text{Im} \frac{a}{\lambda_{sd}} \text{Im} \frac{A_{\text{NP}}}{A_{sd}}$$

Two generic scenarios:

$A_{\text{NP}}$  is  $\Delta U = 0$  amplitude 

indistinguishable from SM penguin enhancement

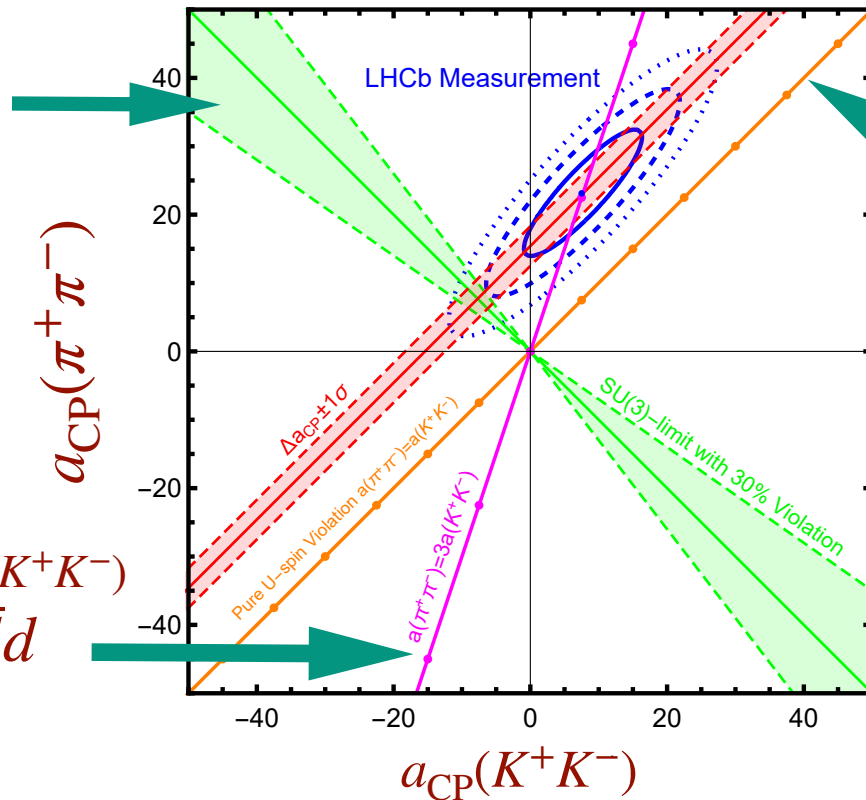
$A_{\text{NP}}$  is  $\Delta U = 1$  amplitude 

same sign of  $a_{\text{CP}}(D^0 \rightarrow K^+ K^-)$   
and  $a_{\text{CP}}(D^0 \rightarrow \pi^+ \pi^-)$

$a_{\text{CP}}(D^0 \rightarrow \pi^+ \pi^-)$  vs.  $a_{\text{CP}}(D^0 \rightarrow K^+ K^-)$

green wedge:  
 $\Delta U = 0$  with  
 30% U-spin  
 breaking

$a_{\text{CP}}(D^0 \rightarrow \pi^+ \pi^-) = 3a_{\text{CP}}(D^0 \rightarrow K^+ K^-)$   
 inspired by NP in  $c \rightarrow u\bar{d}d$



$\Delta U = 1$   
 NP only

from Bachelor  
 thesis of  
 Maurice Schüssler,  
 KIT, 2022

# $a_{CP}$ sum rules

“Extraordinary claims require extraordinary evidence.”

*(Sherlock Holmes in The Sign of Four)*

Derive sum rules between further CP asymmetries; distinguish between the  $\Delta U = 0$  and  $\Delta U = 1$  cases.

Emil Overduin

Maurice Schüßler

Syuhei Iguro

Ulrich Nierste



Bachelor theses



## $a_{\text{CP}}$ sum rules

Recall:  $\mathcal{A}^{\text{SCS}} \equiv \lambda_{sd} A_{sd} + a A_{\text{NP}}$

Tool: Use **Wigner Eckart theorem** to express  $A_{sd}$  and  $A_{\text{NP}}$  in terms of Clebsch-Gordan coefficients (related to **U-spin SU(2)**) and reduced matrix elements.  
Known from SM analysis.

Grossman, Ligeti, Robinson, *JHEP* 01 (2014) 066

$D^0, D_{(s)}^+ \rightarrow$  two pseudoscalars

$$\Delta U = 0$$

$$a_{\text{CP}}(K^+K^-) + a_{\text{CP}}(\pi^+\pi^-) = 0$$

$$a_{\text{CP}}(K^0\pi^+) + a_{\text{CP}}(\bar{K}^0K^+) = 0$$

$$a_{\text{CP}}(\eta\eta) + a_{\text{CP}}(\pi^0\pi^0) + 2a_{\text{CP}}(\eta\pi^0) = 0$$

$$a_{\text{CP}}(\eta K^+) + a_{\text{CP}}(\eta\pi^+) + a_{\text{CP}}(\pi^0K^+) = 0$$

$$3a_{\text{CP}}(\eta K^+) - 3a_{\text{CP}}(\pi^0K^+) + a_{\text{CP}}(K^0\pi^+) = 0$$

$$\Delta U = 1$$

$$a_{\text{CP}}(K^+K^-) - a_{\text{CP}}(\pi^+\pi^-) = 0$$

$$a_{\text{CP}}(K^0\pi^+) - a_{\text{CP}}(\bar{K}^0K^+) = 0$$

$$a_{\text{CP}}(\eta\eta) - a_{\text{CP}}(\pi^0\pi^0) = 0$$

$$a_{\text{CP}}(\eta\eta) - a_{\text{CP}}(\eta\pi^0) = 0$$

two sum rules connecting four modes each

$D^0, D_{(s)}^+ \rightarrow$  two pseudoscalars

Remarkable: One sum rule holds for both  $\Delta U = 0$  and  $\Delta U = 1$ :

$$6a_{\text{CP}}(\pi^0\pi^+) - 3a_{\text{CP}}(\eta K^+) + 3a_{\text{CP}}(\pi^0 K^+) - a_{\text{CP}}(K^0\pi^+) = 0$$

→ consistency check of experiment and test of quality of U-spin symmetry

$D^0, D_{(s)}^+ \rightarrow$  pseudoscalar + vector

$$\Delta U = 0$$

$$a_{\text{CP}}(K^0 \bar{K}^{*0}) + a_{\text{CP}}(\bar{K}^0 K^{*0}) = 0$$

$$a_{\text{CP}}(K^{\mp} K^{*\pm}) + a_{\text{CP}}(\pi^{\mp} \rho^{\pm}) = 0$$

$$a_{\text{CP}}(K^{*0} \pi^+) + a_{\text{CP}}(\bar{K}^{*0} K^+) = 0$$

$$a_{\text{CP}}(\pi^0 K^{*+}) + a_{\text{CP}}(\eta K^{*+})$$

$$+ a_{\text{CP}}(\pi^0 \rho^+) + a_{\text{CP}}(\eta \rho^+) = 0$$

$$\Delta U = 1$$

$$a_{\text{CP}}(K^0 \bar{K}^{*0}) - a_{\text{CP}}(\bar{K}^0 K^{*0}) = 0$$

$$a_{\text{CP}}(K^{\mp} K^{*\pm}) - a_{\text{CP}}(\pi^{\mp} \rho^{\pm}) = 0$$

$$a_{\text{CP}}(K^{*0} \pi^+) - a_{\text{CP}}(\bar{K}^{*0} K^+) = 0$$

$$a_{\text{CP}}(\pi^0 K^{*+}) + a_{\text{CP}}(\eta K^{*+})$$

$$- a_{\text{CP}}(\pi^0 \rho^+) - a_{\text{CP}}(\eta \rho^+) = 0$$

and more.

# Summary

- LHCb measurements  $\Delta a_{CP} = (-15.4 \pm 2.9) \cdot 10^{-4}$  and  $a_{CP}(D^0 \rightarrow K^+ K^-) = (7.7 \pm 5.7) \cdot 10^{-4}$  are not consistent with SM and U-spin symmetry.
- New physics explanations involve a  $\Delta U = 1$  amplitude (with a different phase than  $V_{cs}^* V_{us}$ ) and a  $\Delta U = 0$  amplitude (SM or NP) as well.
- One can check this in the future in other decay modes in which CP asymmetries are not yet measured to be non-zero.
  - sum rules between CP asymmetries
- $D$  decays into two pseudoscalars obey a sum rule which holds in the SM and for both  $\Delta U = 0$  and  $\Delta U = 1$  new physics.
  - consistency check, probing quality of U-spin symmetry