

WG7 summary

Mixing and CP violation in the D system

Patricia Magalhaes, Tara Nanut Petric, Stefan Schacht

Outline

20' + 10' talks

Direct CPV

Direct CPV

Mixing, indirect CPV & strong phases

69 - Direct CPV in D mesons decays at LHCb	Jolanta B	14:45 - 15:15
Sala Palatino		
70 - CPV in D meson decays at Belle and Belle II	Michel Bertemes	15:15 - 15:45
Sala Palatino		
71 - Charm CP Violation	Prof. Ulrich Nierste	15:45 - 16:15
Sala Palatino		
72 - BSM and direct CPV	Hector Gisbert Mullor	16:15 - 16:45
Sala Palatino		
73 - CPV in charmed baryons (theory)	Fu-Sheng Yu	14:45 - 15:15
Aula Magna		
74 - CPV in charmed baryons (experimental)	Dr Artur Ukleja	15:15 - 15:45
Aula Magna		
76 - Earth mover's distance as a measure of CP violation	Ahmed Youssef	15:45 - 16:15
Aula Magna		
77 - HQE, mixing and lifetimes	Alexander Lenz	17:20 - 17:50
Aula Magna		
78 - HFLAV Charm CPV and oscillations	Jolanta Brodzicka	17:50 - 18:20
Aula Magna		
79 - Mixing and indirect CPV in charm decays at LHCb	Federico Betti	18:20 - 18:50
Aula Magna		
80 - Measurements of CPV and phases in charm decays at BESIII	Yang Gao	18:50 - 19:20
Aula Magna		

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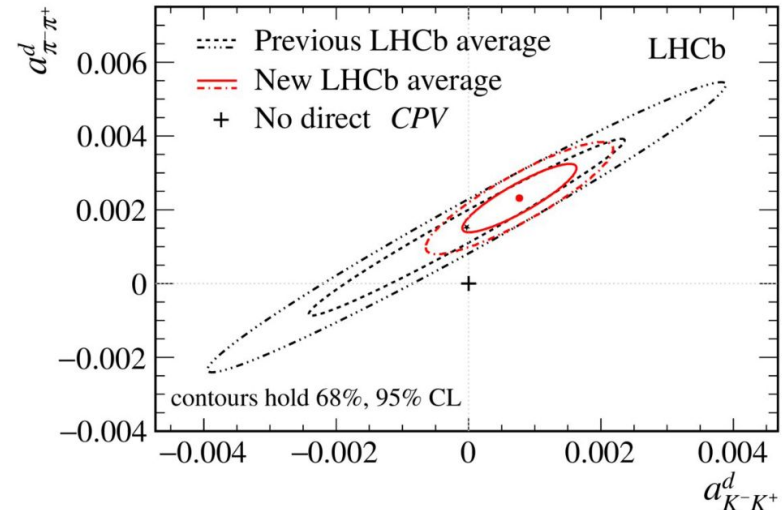
LHCb: CP asymmetry in $D^0 \rightarrow K^+K^-$ and $\pi^+\pi^-$

Measure A_{CP} in K^+K^- : first evidence of CPV in single channel ($\pi^+\pi^-$) when combining with ΔA_{CP}

Breaking U-spin symmetry!

$$a_{K^+K^-}^{dir} = (7.7 \pm 5.7) \times 10^{-4} \quad (1.4\sigma)$$

$$a_{\pi^+\pi^-}^{dir} = (23.2 \pm 6.1) \times 10^{-4} \quad (3.8\sigma)$$



LHCb: other results consistent with CP symmetry

- Search for CPV in $D_{(s)}^+ \rightarrow \eta^{(\prime)} \pi^+$ decays
- Search for CPV in $D_{(s)}^+ \rightarrow K^- K^+ K^+$ with Miranda technique
- Examining $D^0 \rightarrow \pi^+ \pi^- \pi^0$ and $D^0 \rightarrow K_S K \pi$ with Energy Test

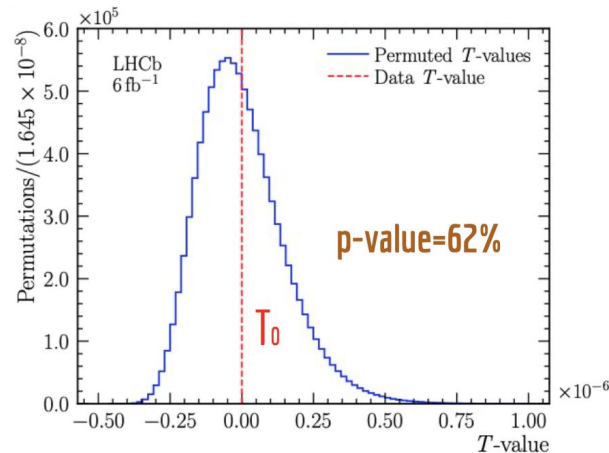


Binned

Discovery methods

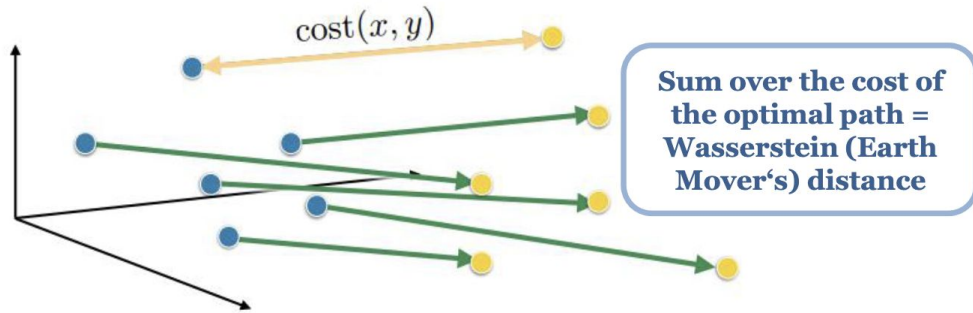
Unbinned

Similar mechanism as $\pi^+ \pi^-$



New method for CPV searches: Earth mover's distance

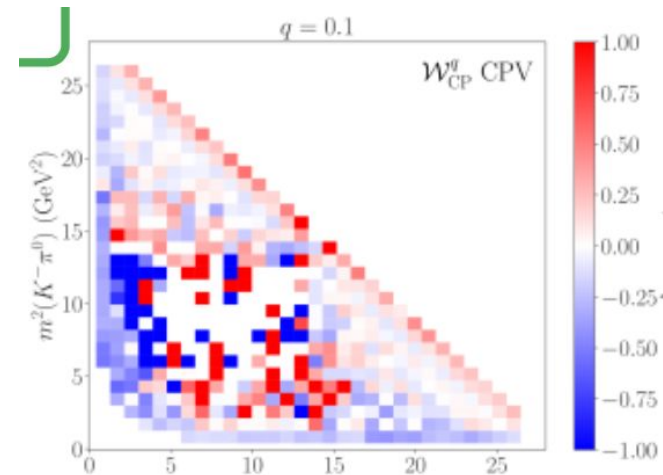
Another test statistics: aiming to match the energy test performance with added benefits in interpretability - pinpointing which part of the Dalitz plot the CPV originates from



For high statistics a modification can be applied to reduce computation cost: “sliced” EMD

EMD asymmetry:

$$W_{\text{CP}}^q(s_{12}, s_{13}) = \frac{\sum_{\bar{i}} \delta \bar{W}_q(\bar{i}) - \sum_i \delta W_q(i)}{\sum_{\bar{i}} \delta \bar{W}_q(\bar{i}) + \sum_i \delta W_q(i)}$$





Belle: all results consistent with CP symmetry

$$A_{CP} \propto \sin(\phi)\sin(\delta)$$

Measurement of BR and search for CPV in

$$D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^- \text{ decays}$$

PRD 107, 052001 (2023)

Search for CPV in $D_{(s)}^+ \rightarrow K^+ K_S^0 h^+ h^-$ decays

$$\text{and observation of } D_s^+ \rightarrow K^+ K^- K_S^0 \pi^+$$

arXiv:2305.11405

First observation of decay $D_{(s)}^+ \rightarrow K^+ K^- K_S^0 \pi^+$

$$a_{CP}^{T\text{-odd}} \propto \sin(\phi)\cos(\delta)$$

Search for CPV using T-odd correlations in

$$D_{(s)}^+ \rightarrow K^+ K^- \pi^+ \pi^0, K^+ \pi^- \pi^+ \pi^0 \text{ and}$$

$$D^+ \rightarrow K^- \pi^+ \pi^+ \pi^0 \text{ decays}$$

arXiv:2305.12806

$$a_{CP}^{T\text{-odd}} = (0.34 \pm 0.87(\text{stat.}) \pm 0.32(\text{syst.})) \%$$

Measure also in subregions of phasespace:

- largest asymmetry found in $D_s^+ \rightarrow K^{*0} \rho^+$
- $a_{CP}^{T\text{-odd}} = (6.2 \pm 3.0(\text{stat}) \pm 0.4(\text{syst})) \%$



Belle II: toward future measurements

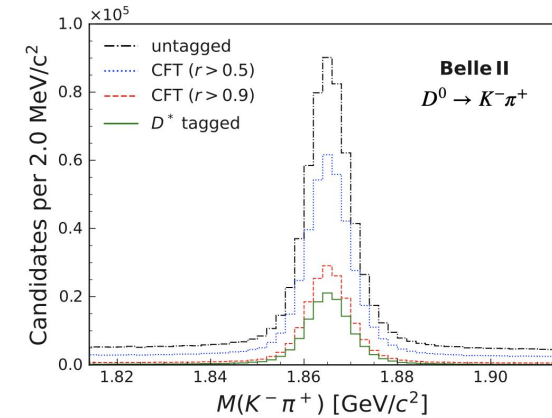
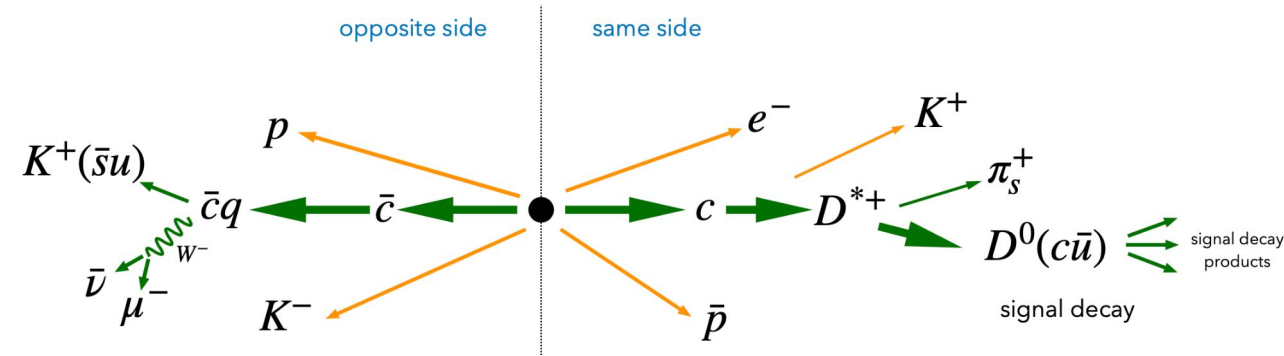
- excellent reconstruction of **final states with neutrals** e.g. $D^+ \rightarrow \pi^+ \pi^0$,
 $D^0 \rightarrow \rho^0 \gamma, \pi^0 \pi^0, K_S^0 K_S^0, K \pi \pi^0, \pi \pi \pi^0 \dots$
- unique access to final states with invisible particles: e.g. decay into neutrinos

Some of these measurements are well under way already

Combine Belle + Belle II datasets



Belle II: new charm flavour tagger for D^0



- D^* tag: loss in statistics (only $\sim 25\%$ of all charm quarks hadronize into D^* at Belle (II))
- CFT: reconstruct particles most collinear with signal meson
- Doubles the signal wrt D^* tag, but introduces more background (depending on channel)
- BDT-based decision based on kinematics and PID: predicts decision and dilution (qr)
- Future expansions possible

Direct CPV - theory

2022: $a_{CP}(D^0 \rightarrow K^+K^-)$



LHCb 2022: $a_{CP}(D^0 \rightarrow K^+K^-) = (7.7 \pm 5.7) \cdot 10^{-4}$.

Thus Δa_{CP} implies $a_{CP}(D^0 \rightarrow \pi^+\pi^-) = (23.1 \pm 6.1) \cdot 10^{-4}$.

- $a_{CP}(D^0 \rightarrow K^+K^-)$ complies with the calculation of Khodjamirian and Petrov.
- For approximate U-spin limit $a_{CP}(D^0 \rightarrow K^+K^-) \approx -a_{CP}(D^0 \rightarrow \pi^+\pi^-)$ to work, with future data $a_{CP}(D^0 \rightarrow K^+K^-)$ must flip sign.
- Will future data decrease $|\Delta a_{CP}|$ and will the 5σ discovery eventually go away?
- Or did LHCb discover **new physics** in 2019?

The challenge: low-energy QCD or genuine BSM physics?

$D^0, D_{(s)}^+ \rightarrow$ **two pseudoscalars**

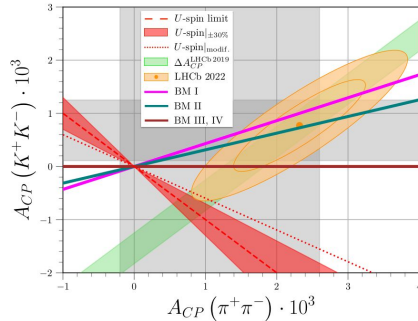


Strategy: Use sum rules as a tool to probe for U-spin breaking beyond the SM.

$\Delta U = 0$	$\Delta U = 1$
$a_{CP}(K^+K^-) + a_{CP}(\pi^+\pi^-) = 0$	$a_{CP}(K^+K^-) - a_{CP}(\pi^+\pi^-) = 0$
$a_{CP}(K^0\pi^+) + a_{CP}(\bar{K}^0K^+) = 0$	$a_{CP}(K^0\pi^+) - a_{CP}(\bar{K}^0K^+) = 0$
$a_{CP}(\eta\eta) + a_{CP}(\pi^0\pi^0) + 2a_{CP}(\eta\pi^0) = 0$	$a_{CP}(\eta\eta) - a_{CP}(\pi^0\pi^0) = 0$
$a_{CP}(\eta K^+) + a_{CP}(\eta\pi^+) + a_{CP}(\pi^0K^+) = 0$	$a_{CP}(\eta\eta) - a_{CP}(\eta\pi^0) = 0$
$3a_{CP}(\eta K^+) - 3a_{CP}(\pi^0K^+) + a_{CP}(K^0\pi^+) = 0$	two sum rules connecting four modes each

Direct CPV - BSM

What tells the new LHCb result? [2207.00539](#), [2210.16330](#)



1 $a_{\pi^-\pi^+}^d$ is larger than $|\Delta A_{CP}|$. SM needs even more enhancement!

$$a_{\pi^-\pi^+}^d|_{SM} \sim 2 \text{Im}(\lambda_b/\lambda_s) \left(\frac{h}{t}\right) \sim 1.2 \cdot 10^{-3} \left(\frac{h}{t}\right) \rightarrow \boxed{\frac{h}{t} \sim 2}$$

2 Violation of U-spin, $a_{K^-\bar{K}^+}^d + a_{\pi^-\pi^+}^d \neq 0$, at the level of 2.7σ !

BSM CP & U-spin violation?



Prediction of a leptophobic, light Z' below $O(20 \text{ GeV})$.

Large U-spin breaking can be explained in Z' models. Smoking gun predictions for BSM physics.

Anomaly-free $U(1)'$ models [2210.16330](#)

$$\begin{aligned} 2\langle \mathcal{F}_Q \rangle - \langle \mathcal{F}_u \rangle - \langle \mathcal{F}_d \rangle &= 0, \\ 3\langle \mathcal{F}_Q \rangle + \langle \mathcal{F}_L \rangle &= 0, \\ \langle \mathcal{F}_Q \rangle + 3\langle \mathcal{F}_L \rangle - 8\langle \mathcal{F}_u \rangle - 2\langle \mathcal{F}_d \rangle - 6\langle \mathcal{F}_e \rangle &= 0, \\ 6\langle \mathcal{F}_Q \rangle + 2\langle \mathcal{F}_L \rangle - 3\langle \mathcal{F}_u \rangle - 3\langle \mathcal{F}_d \rangle - \langle \mathcal{F}_e \rangle - \langle \mathcal{F}_\nu \rangle &= 0, \\ \langle \mathcal{F}_Q^2 \rangle - \langle \mathcal{F}_L^2 \rangle - 2\langle \mathcal{F}_u^2 \rangle + \langle \mathcal{F}_d^2 \rangle + \langle \mathcal{F}_e^2 \rangle &= 0, \\ 6\langle \mathcal{F}_Q^3 \rangle + 2\langle \mathcal{F}_L^3 \rangle - 3\langle \mathcal{F}_u^3 \rangle - 3\langle \mathcal{F}_d^3 \rangle - \langle \mathcal{F}_e^3 \rangle - \langle \mathcal{F}_\nu^3 \rangle &= 0. \end{aligned}$$

$$\begin{aligned} \mathcal{F}_X &= \text{diag}(F_{X_1}, F_{X_2}, F_{X_3}) \\ \langle \mathcal{F}_X \rangle &= \text{Tr}(\mathcal{F}_X) \end{aligned}$$

Model	F_{Q_i}			F_{U_i}			F_{D_i}			F_{L_i}			F_{E_i}			F_{ν_i}		
BM I	0	0	0	9	-16	7	20	-11	-9	15	-6	-9	-16	0	16	6	12	-18
BM II	0	0	0	-19	9	10	20	-8	-12	4	1	-5	15	2	-17	8	2	-10
BM III	0	0	0	0	-1	0	1	0	0	0	0	0	0	0	1	0	0	-1
BM IV	0	0	0	$-\frac{985}{1393}$	$\frac{985}{1393}$	0	1	0	-1	0	0	0	$\frac{1}{1393}$	0	$-\frac{1}{1393}$	F_ν	$-F_\nu$	0

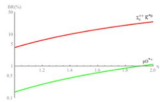
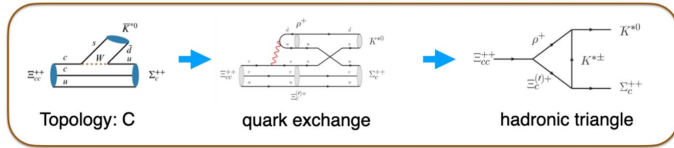
- All these BMs survive the previous constraints!
- BMs feature U-spin and IB with signals in $\pi^+\pi^0$, $\pi^0\pi^0$:

$$A_{CP}(\pi^0\pi^0) \simeq A_{CP}(\pi^+\pi^0) \simeq \left(1 - \frac{F_{U_1}}{F_{D_1}}\right) |\Delta A_{CP}| \simeq (1 - 2) 10^{-3}$$

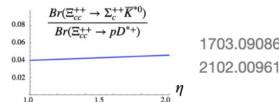
Direct CPV baryons - theory

Rescattering mechanism

- Rescattering mechanism have been successfully used to predict the discovery channel of $\Xi_{cc}^{++} \rightarrow \Lambda_c^+ K^- \pi^+ \pi^+$ [FSY, Jiang, Li, Lu, Wang, Zhao, '17]



Theoretical uncertainty is under control in the **ratio** of branching fractions of different processes



- It deserves to develop the rescattering mechanism to study CPV of charmed baryons

Complementary observables with different dependence on the strong phase.

Many additional opportunities with baryons.

Models of underlying rescattering mechanism can be tested with future data.

Important guidance for experiment.

CPV induced by T-odd and T-even

$$a_{CP}^{T\text{-odd}} \propto \sum_{m,n} \text{Im}(A_m^* A_n - \bar{A}_m^* \bar{A}_n) \propto \cos \delta_s \sin \phi_w$$

$$a_{CP}^{T\text{-even}} \propto \sum_{m,n} \text{Re}(A_m^* A_n - \bar{A}_m^* \bar{A}_n) \propto \sin \delta_s \sin \phi_w$$

- Example: $\Lambda_c^+ \rightarrow \Lambda^0 K^+$, Lee-Yang decay-asymmetry parameter

T-even: $\vec{s}_i \cdot \vec{p}$	$\alpha \propto \text{Re}[S^* P]$	$a_{CP}^\alpha = \frac{\alpha + \bar{\alpha}}{\alpha - \bar{\alpha}} \propto \sin \delta$	complementary
T-odd: $(\vec{s}_i \times \vec{s}_f) \cdot \vec{p}$	$\beta \propto \text{Im}[S^* P]$	$a_{CP}^\beta = \frac{\beta + \bar{\beta}}{\beta - \bar{\beta}} \propto \cos \delta$	

Direct CPV baryons - theory

Charmed baryon decays

- Charmed baryon decays are **the next opportunity and challenge of charm physics**
- CP asymmetry sum rules based on SU(3) flavor symmetry are firstly obtained [Grossman and Schacht, PRD (2019)][Di Wang, EPJC (2019)]

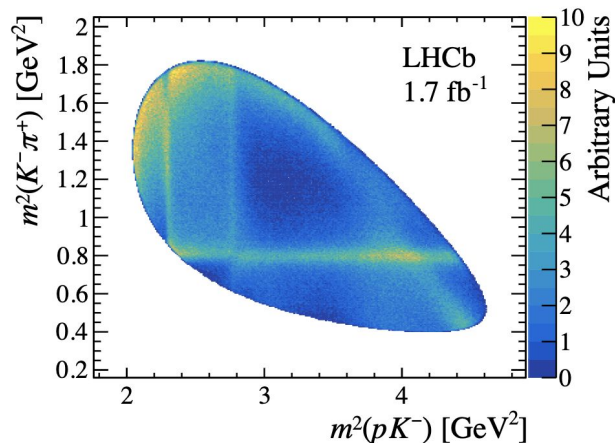
$$A_{CP}(\Lambda_c^+ \rightarrow pK^-K^+) + A_{CP}(\Xi_c^+ \rightarrow \Sigma^+\pi^-\pi^+) = 0,$$

$$A_{CP}(\Lambda_c^+ \rightarrow \Sigma^+\pi^-K^+) + A_{CP}(\Xi_c^+ \rightarrow pK^-\pi^+) = 0,$$

$$A_{CP}(\Lambda_c^+ \rightarrow p\pi^-\pi^+) + A_{CP}(\Xi_c^+ \rightarrow \Sigma^+K^-K^+) = 0.$$

- **No any numerical prediction on CPV of charm-baryon decays**

Direct CPV baryons - experimental

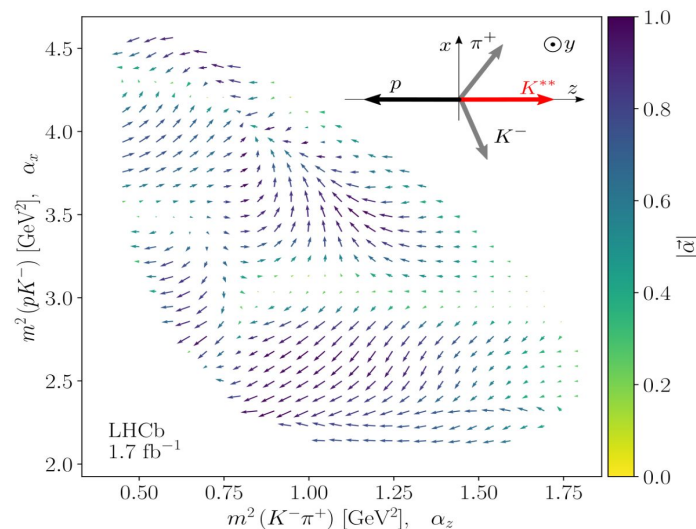


- Λ_c polarization of O(65%) found.
- Can be used to probe $b \rightarrow c$ transitions in semileptonic Λ_b decays.

LHCb: amplitude analysis performed for $\Lambda_c^+ \rightarrow pK^-\pi^+$.

Input can be used for model-independent CPV searches.

LHCb-PAPER-2022-044, JHEP 2023(2023) 228



Charm Mixing and Lifetimes - Theory



Cancellations



Is the charm quark heavy enough for the heavy quark expansion?

The charm system is theoretically more difficult than the b system since

$$\alpha_s(m_c) \approx 0.33 \quad \text{and} \quad \frac{\Lambda_{QCD}}{m_c} \approx 3 \frac{\Lambda_{QCD}}{m_b}$$

Nevertheless the **Heavy Quark Expansion** might still converge

But things will become very ugly, if in addition cancellations arising

- A. No cancellations, e.g. $\Gamma(D^0)$
- B. Strong cancellations, e.g. $\Gamma(D^+)$
- C. Crazy cancellations, e.g. D -mixing

More progress on the way.



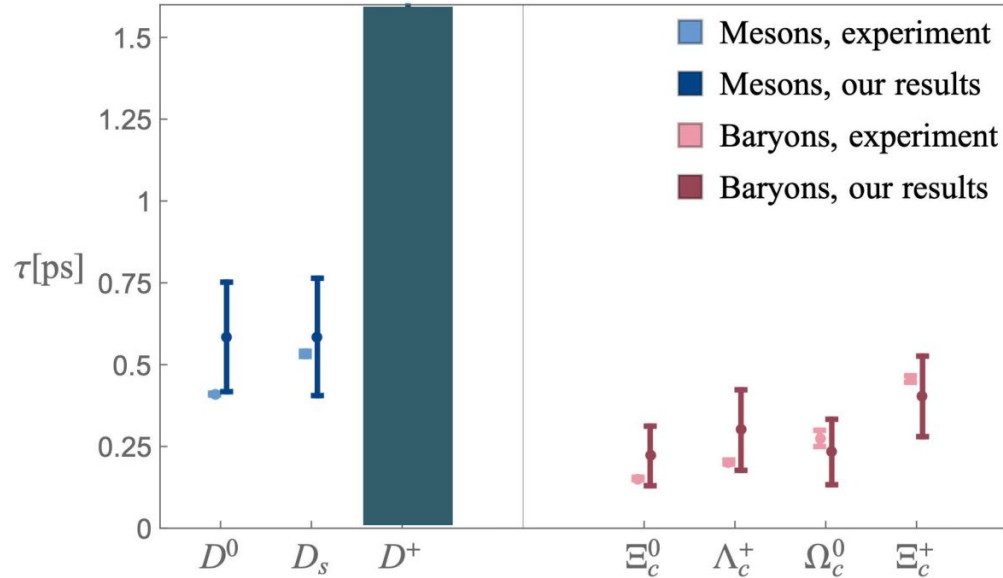
Theory for Charm



Theory for Charm Observable \neq Theory for Charm Observable

- No cancellations, e.g. Lifetime of D^0 can be predicted, $1/m_c$ works
- Cancellations, e.g. Lifetime of D^+ lies in the right ball park, $1/m_c$ might work
- Crazy cancellations, e.g. Mixing of D^0 HQE might overlap with exp., $1/m_c$ not excluded
- Hadronic decays: **we have to first understand the B-system!**

Lifetime hierarchy



(Far) future: can theory/lattice predict the hierarchy?

Lifetimes of singly charmed hadrons

#17

James Gratx (Boskovic Inst., Zagreb), Blaženka Melić (Boskovic Inst., Zagreb), Ivan Nišandžić (Boskovic Inst., Zagreb)
(Apr 25, 2022)

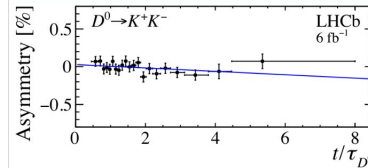
Published in: *JHEP* 07 (2022) 058, *JHEP* 07 (2022) 058 • e-Print: 2204.11935 [hep-ph]

Charm Mixing and time-dep. CPV - experimental

- ΔY_f in $D^0 \rightarrow h^+ h^-$
- $y_{CP}^f - y_{CP}^{K\pi}$
- $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

$$A_{CP}(D^0 \rightarrow f, t) = a_f^d(D^0 \rightarrow f) + \Delta Y_f \frac{t}{\tau_{D^0}}$$

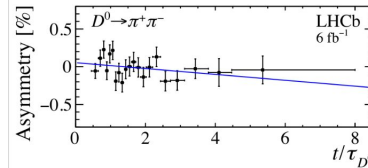
ΔY_f in $D^0 \rightarrow K^+ K^-$ and $D^0 \rightarrow \pi^+ \pi^-$



$$\Delta Y_{K^+K^-} = (-0.4 \pm 0.5 \pm 0.2) \times 10^{-4}$$

PRD_104 (2021) 072010

Result on control sample

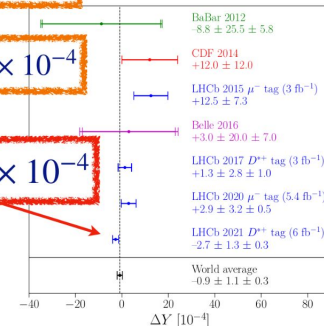


$$\Delta Y_{K^+K^-} = (-2.3 \pm 1.5 \pm 0.3) \times 10^{-4}$$

$$\Delta Y_{\pi^+\pi^-} = (-4.0 \pm 2.8 \pm 0.4) \times 10^{-4}$$

$$\Delta Y = (-2.7 \pm 1.3 \pm 0.3) \times 10^{-4}$$

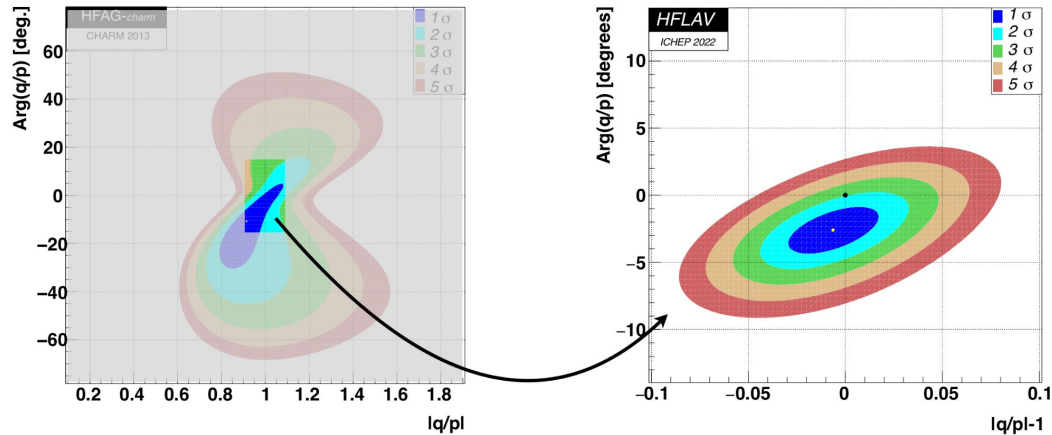
- Compatible with 0 within 2σ
- This result improves by nearly a **factor 2** the precision of the previous world average



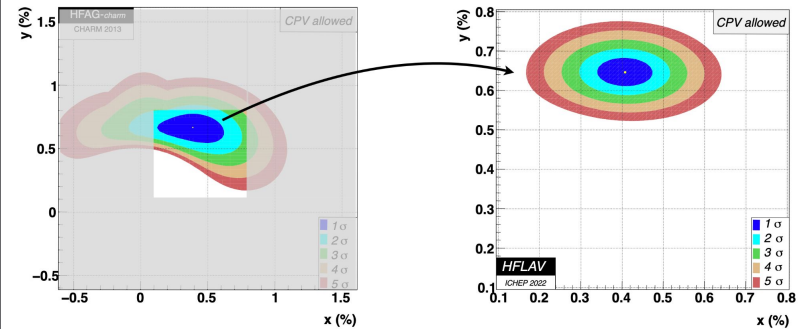
Charm Mixing and time-dep. CPV - experimental

We came a long way :

Landscape after 10 years



Landscape after 10 years



HFLAV Charm CPV and mixing

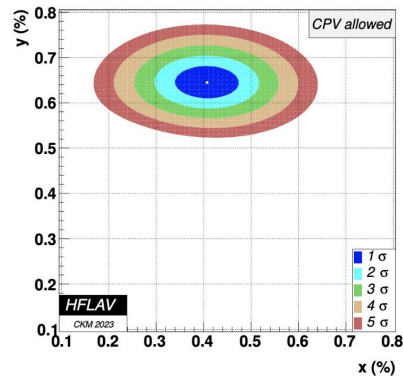
Recent experimental additions

- A_r with $D^0 \rightarrow K^+ K^-$ and $D^0 \rightarrow \pi^+ \pi^-$, LHCb Run2, (π -tag)
PRD 104, 072010 (2021)
- $x_{CP}, y_{CP}, \Delta x, \Delta y$ in $D^0 \rightarrow K_S \pi^+ \pi^-$, LHCb Run2, (π -tag) + (μ -tag)
PRL 127, 111801 (2021) PRD108, 052005 (2023)
- $y_{CP} - y_{CP}(K\pi)$ with $D^0 \rightarrow K^+ K^-$, $D^0 \rightarrow \pi^+ \pi^-$, Run2, (π -tag)
PRD 105, 092013 (2022)
- $A_{CP}(D^0 \rightarrow K^+ K^-)$, $A_{CP}(D^0 \rightarrow \pi^+ \pi^-)$, LHCb Run2, (π -tag)
PRL 131, 091802 (2023)
- $A_{CP}[K\pi] [\rightarrow \delta_{K\pi}]$, BESIII
Eur. Phys. J. C 82, 1009 (2022)

Included in global fit for CKM2023

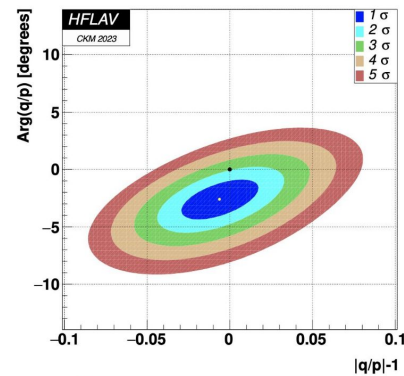
[Thanks to Alan Schwartz]

Mixing fit with all CPV allowed



$$x = (0.407 \pm 0.044)\%$$

$$y = (0.645_{-0.023}^{+0.024})\%$$



$$\phi = (-2.6_{-1.2}^{+1.1})^\circ$$

$$|q/p| = 0.994_{-0.015}^{+0.016}$$

- Mixing well established, no indirect CPV, but ϕ non-zero at 2.2σ

- Hence ΔA_{CP} equivalent for baryons would be:

$$\Delta \Delta A_{CP} \equiv (A_{CP}(\Lambda_c^+ \rightarrow p K^+ K^-) - A_{CP}(\Lambda_c^+ \rightarrow p \pi^+ \pi^-)) - (A_{CP}(\Xi_c^+ \rightarrow \Sigma^+ K^+ K^-) - A_{CP}(\Xi_c^+ \rightarrow \Sigma^+ \pi^+ \pi^-))$$

- $\Delta \Delta A_{CP} = 0$ in U-spin limit

CPV and strong phases at BESIII

Looking Forward

- For CPV, the decay of $D^0\bar{D}^0$ to the same CP final states has been studied based on blind analysis and will open data after finishing data taking plan.
- The CPV from polarization from Λ_c decay is in preparation.
- For some flavor decays, the strong phases would be updated using 20 fb^{-1} .
- For $\pi^+\pi^-\pi^0$ and $K^+K^-\pi^0$, the precision of F_+ would be improve with a factor more than 2 compared with CLEO-c's measurement. ($\sim 8 \text{ fb}^{-1}$ in preparation)
- An optimized binning scheme and a precise c_i and s_i would be determined. ($\sim 8 \text{ fb}^{-1}$, $\sim 20 \text{ fb}^{-1}$)
- More precise c_i and s_i for $K_S^0\pi^+\pi^-$ and $K_L^0\pi^+\pi^-$, it is worthwhile to explore other binning. ($\sim 20 \text{ fb}^{-1}$)
- A strong phase analysis of $K^+K^-\pi^+\pi^-$ is performed to measure the strong phase differences in bins of phase space. ($\sim 8 \text{ fb}^{-1}$ in preparation) This would be the first binned analysis of this decay.
- The statistical uncertainty would be reduce significantly with 20 fb^{-1} .

A BIG THANKS TO THE ORGANIZERS!!!!

