

CP violation measurements in three-body charmless B decays

Lucas Falcão

on behalf of the LHCb Collaboration



CKM 2023

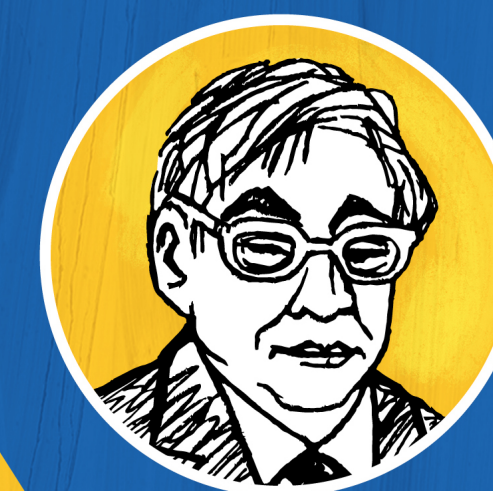
12th INTERNATIONAL WORKSHOP ON THE CKM UNITARITY TRIANGLE



KOBAYASHI



CABIBBO



MASKAWA



SANTIAGO DE COMPOSTELA
18-22 SEPTEMBER 2023

LHCb detector:

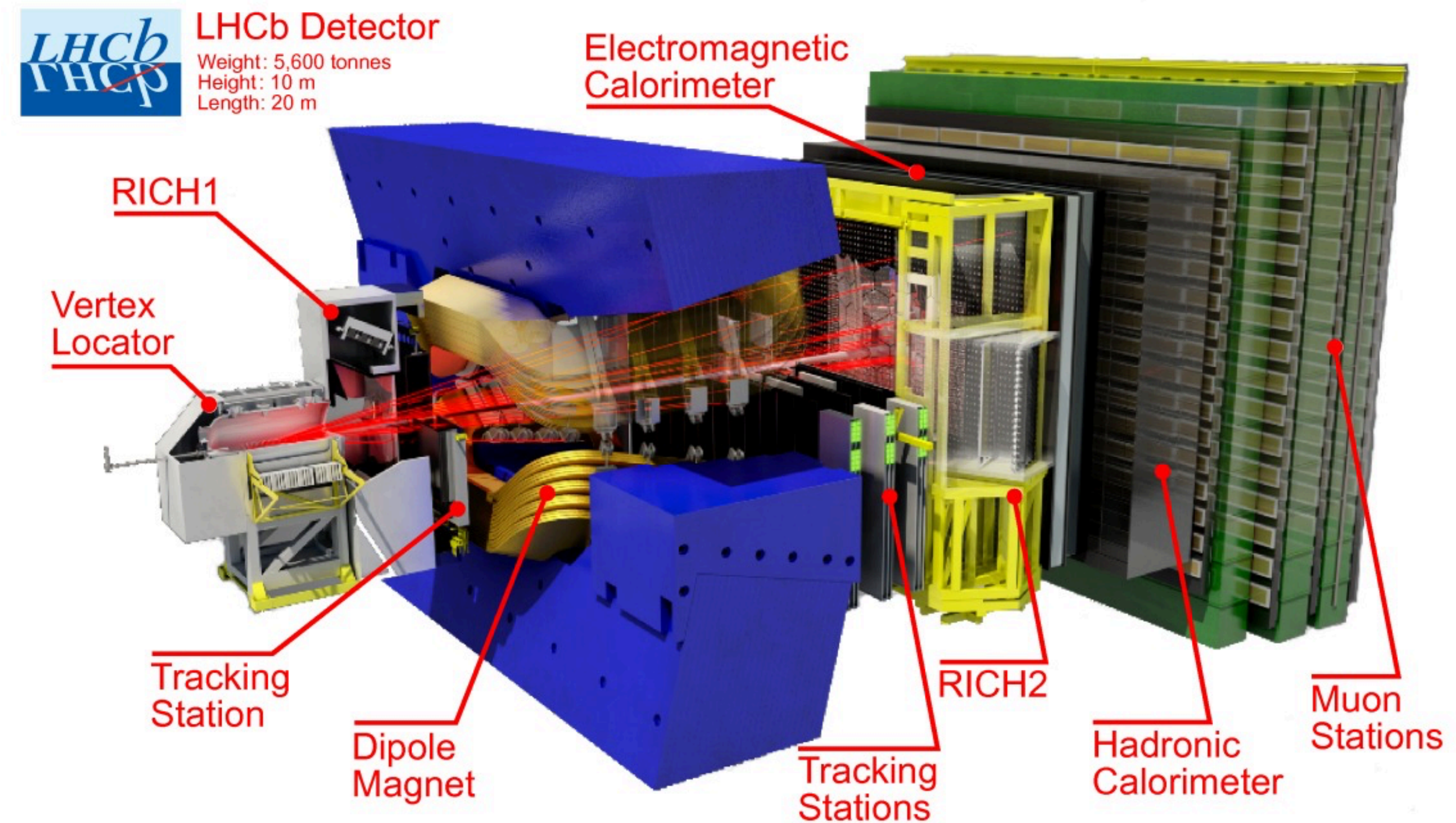
- ✓ Single-arm spectrometer with high-precision of tracking, particle identification and decay vertex system

Presentation based on RUN II data of LHCb:

- ✓ $\mathcal{L} = 5.9 \text{ fb}^{-1}$ using $p - p$ collisions and centre-of-mass energy of 13 TeV (2015 - 2018)

Papers to be presented:

- ✓ Direct CP violation in charmless three-body decays of B^\pm mesons [PRD.108.012008\(2023\)](#)
- ✓ Search for direct CP violation in charged charmless $B \rightarrow PV$ decays [PRD.108.012013\(2023\)](#)



The Analysis is motivated by significant asymmetries observed in $B^\pm \rightarrow h^\pm h^+ h^-$ ($h = K, \pi$) during the RUN I

✓ Measurements of CP violation in three-body phase space [PhysRevD.90.112004](#)
of charmless B^\pm decays

✓ Amplitude analysis of $B^\pm \rightarrow \pi^\pm \pi^+ \pi^-$ and $B^\pm \rightarrow \pi^\pm K^+ K^-$ decays

[PhysRevLett.124.031801\(2020\)](#)

[PhysRevLett.123.231802\(2019\)](#)

[PhysRevD101012006\(2020\)](#)

Decays studied:

✓ $B^\pm \rightarrow \pi^\pm \pi^+ \pi^-$

✓ $B^\pm \rightarrow K^\pm \pi^+ \pi^-$

✓ $B^\pm \rightarrow \pi^\pm K^+ K^-$

✓ $B^\pm \rightarrow K^\pm K^+ K^-$



$B^\pm \rightarrow (V \rightarrow h^+ h^-) h^\pm$ contributions:

✓ $B^\pm \rightarrow (\rho(770)^0 \rightarrow \pi^+ \pi^-) \pi^\pm$

✓ $B^\pm \rightarrow (\rho(770)^0 \rightarrow \pi^+ \pi^-) K^\pm$

✓ $B^\pm \rightarrow (K^*(892)^0 \rightarrow K^+ \pi^-) \pi^\pm$

✓ $B^\pm \rightarrow (K^*(892)^0 \rightarrow K^+ \pi^-) K^\pm$

✓ $B^\pm \rightarrow (\phi(1020) \rightarrow K^+ K^-) K^\pm$

Technical elements

✓ Selection based on Multivariate, PID and charm vetoes

✓ Efficiency obtained from Monte Carlo simulation samples

Direct CPV arises from the interference between amplitudes with **different** weak and strong phases leading to the same final state:

- ✓ **Strong phase:** short-distance penguin contributions, hadronic final-state-interactions(FSI)
- ✓ **Weak phase:** CKM matrix elements

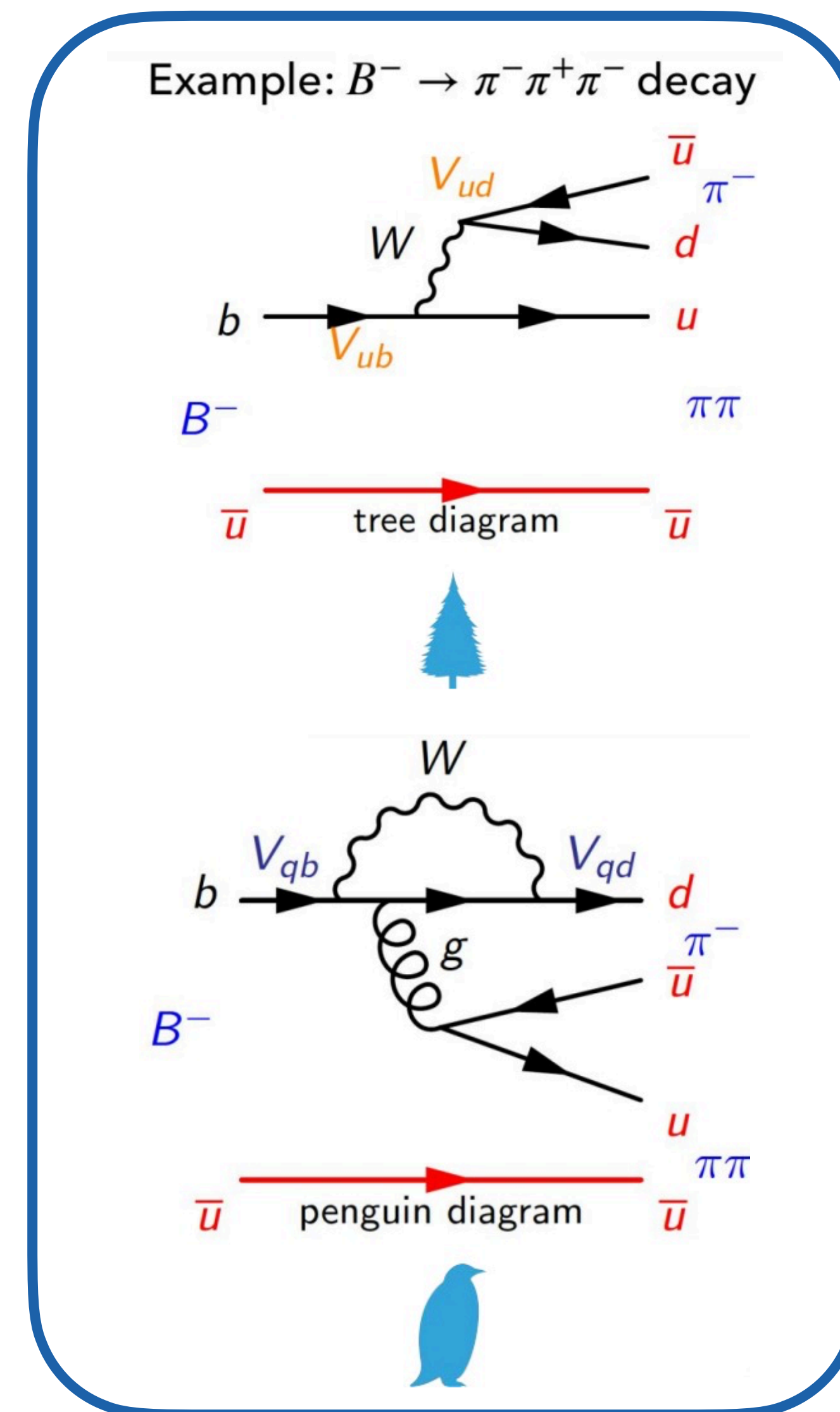
Example of at least 2 competitive amplitudes:

$$A(B \rightarrow f) = |A_1| e^{i(\delta_1 + \gamma_1)} + |A_2| e^{i(\delta_2 + \gamma_2)}$$

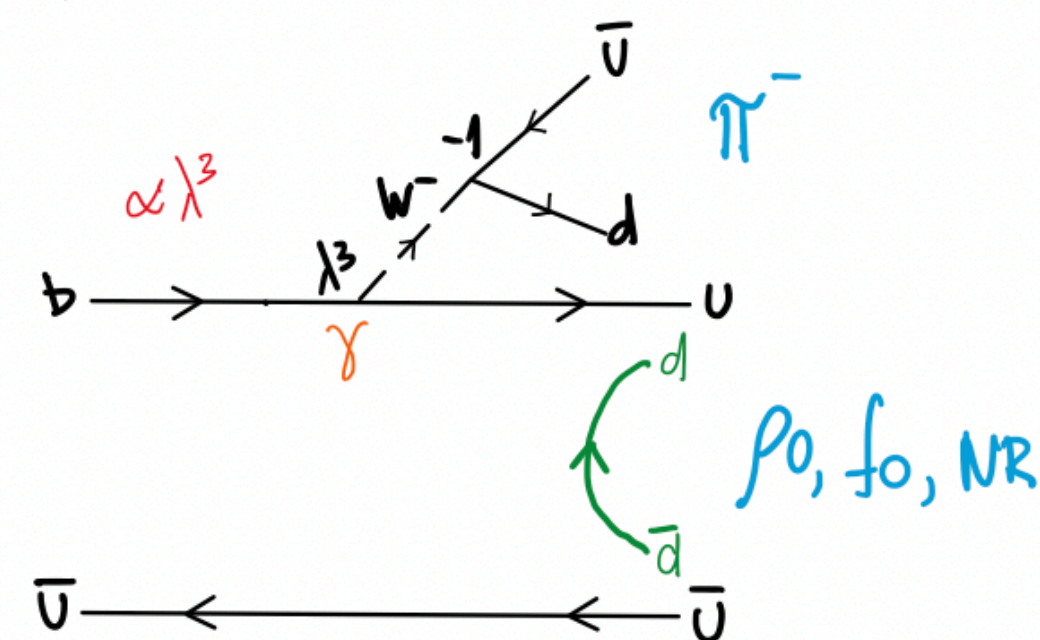
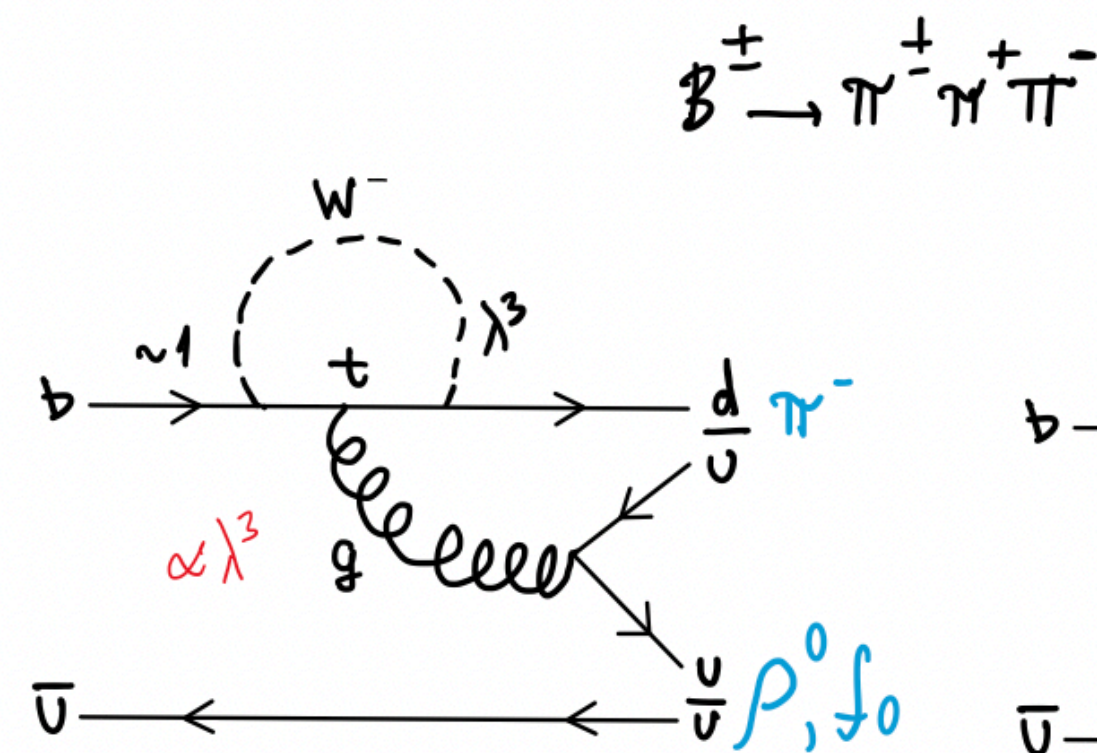
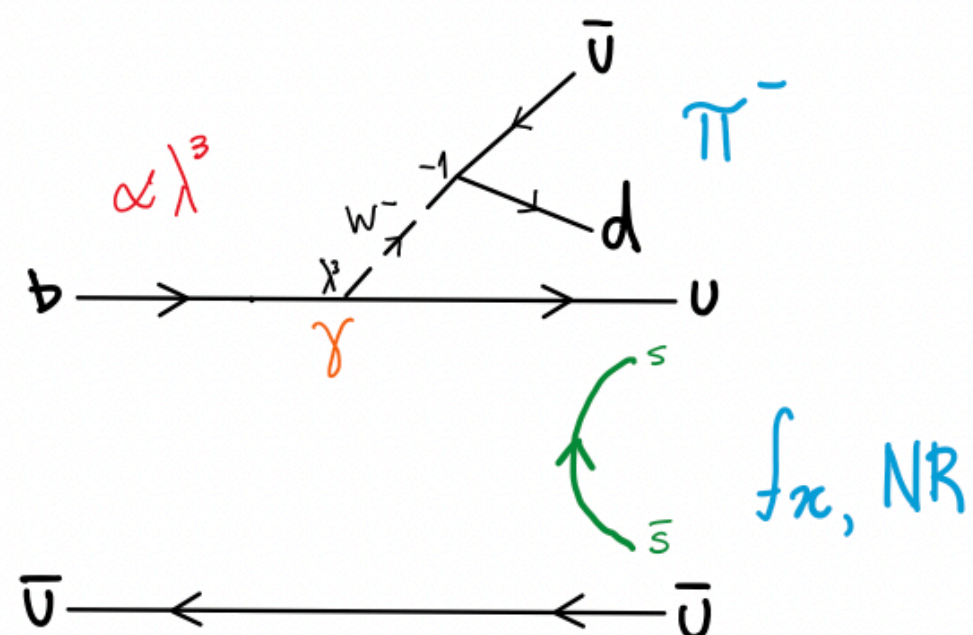
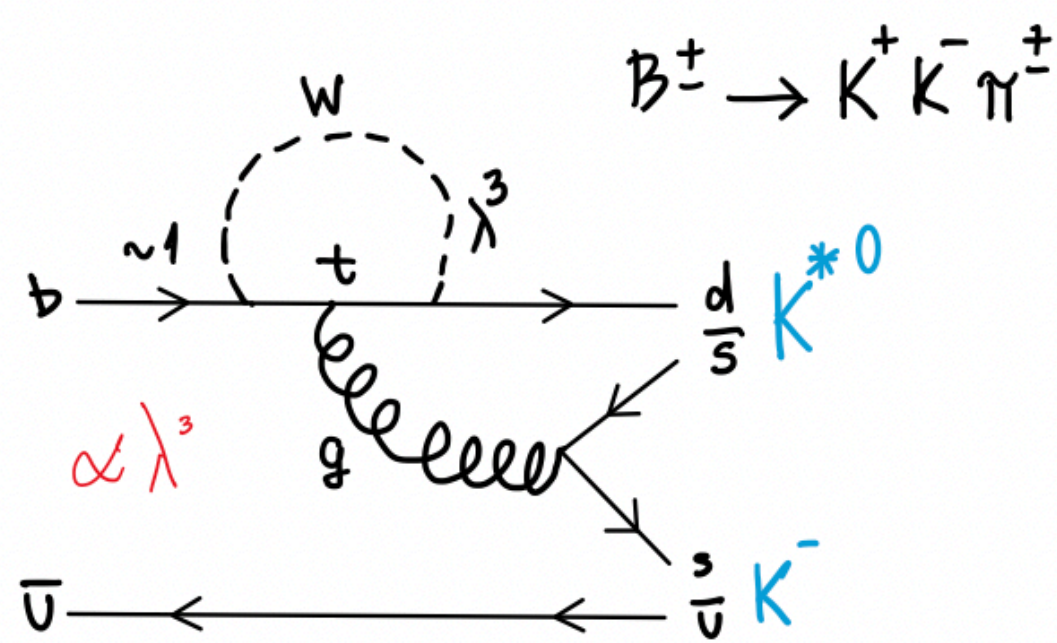
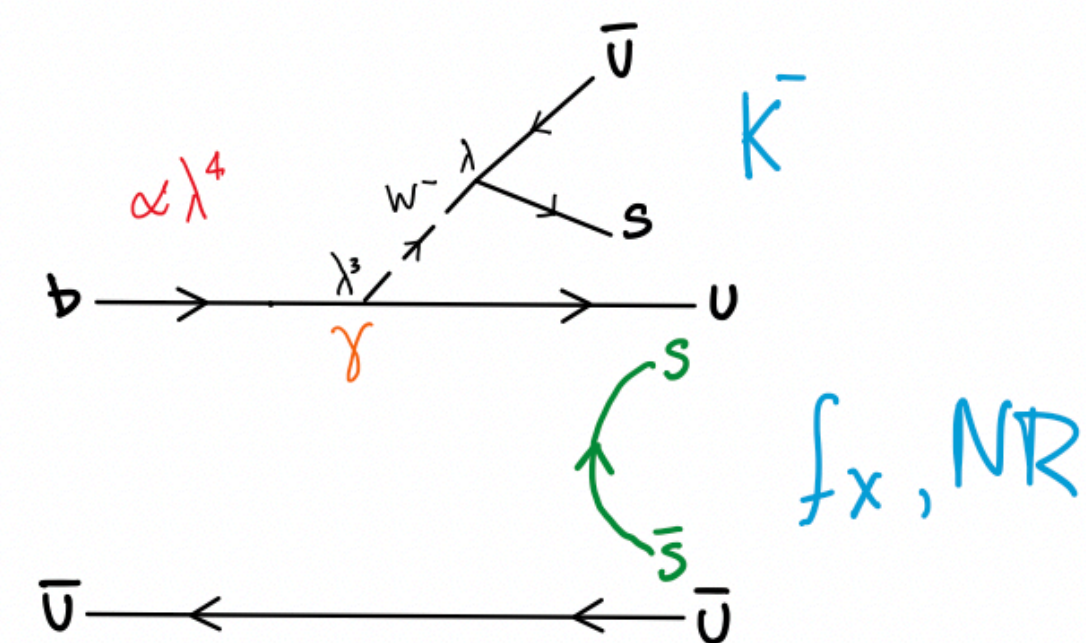
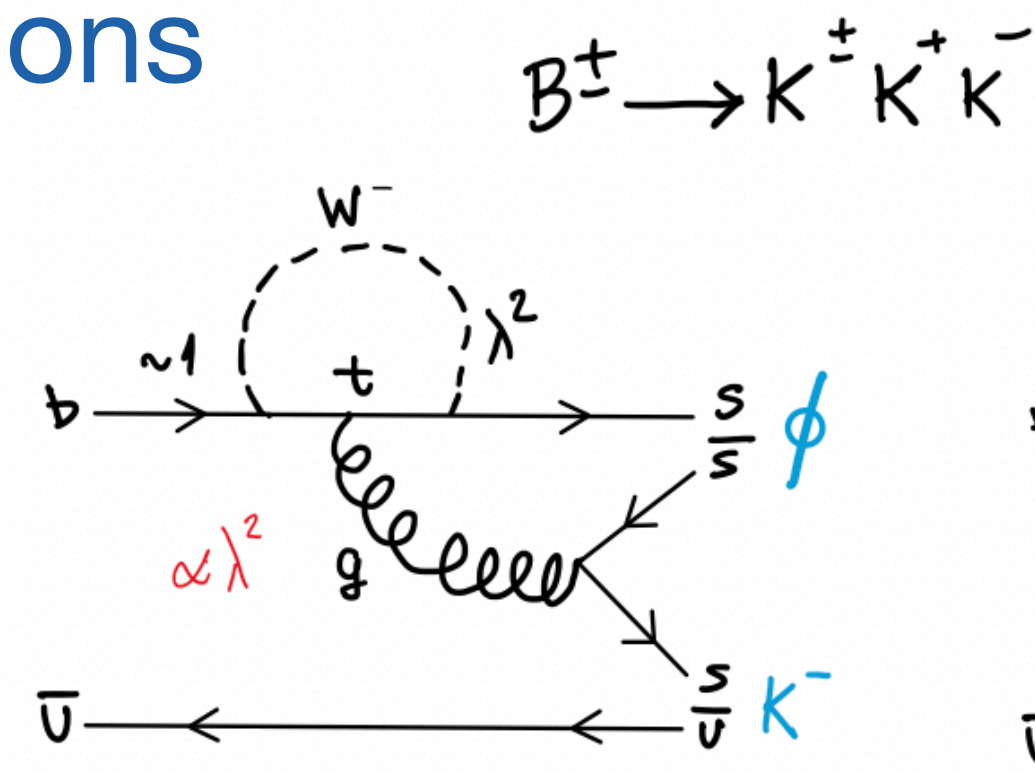
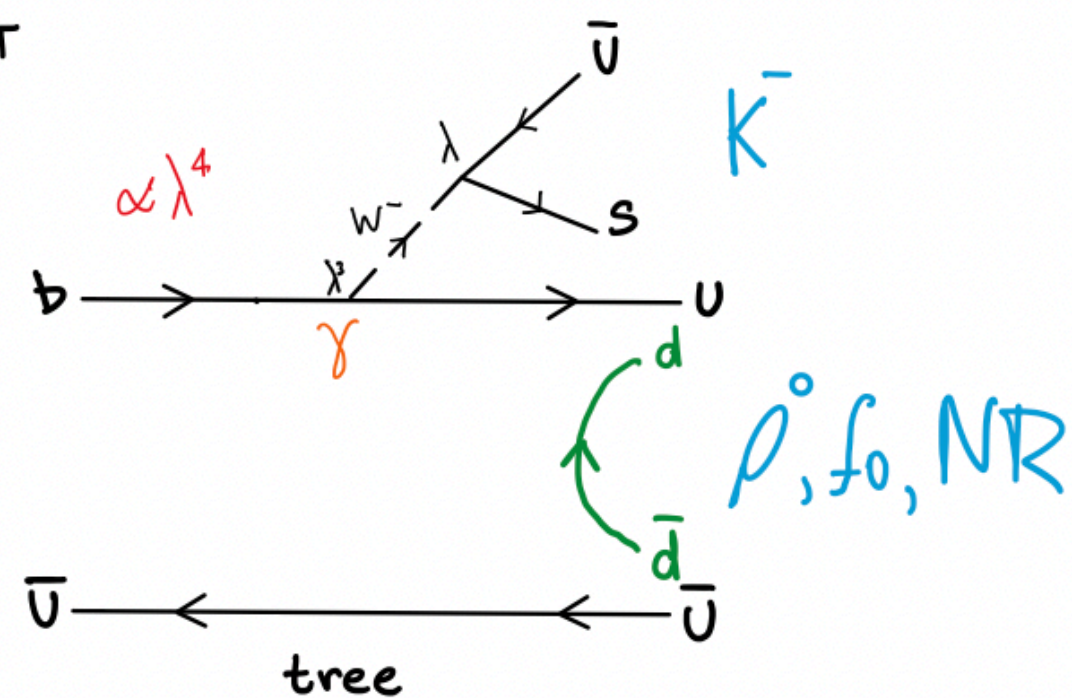
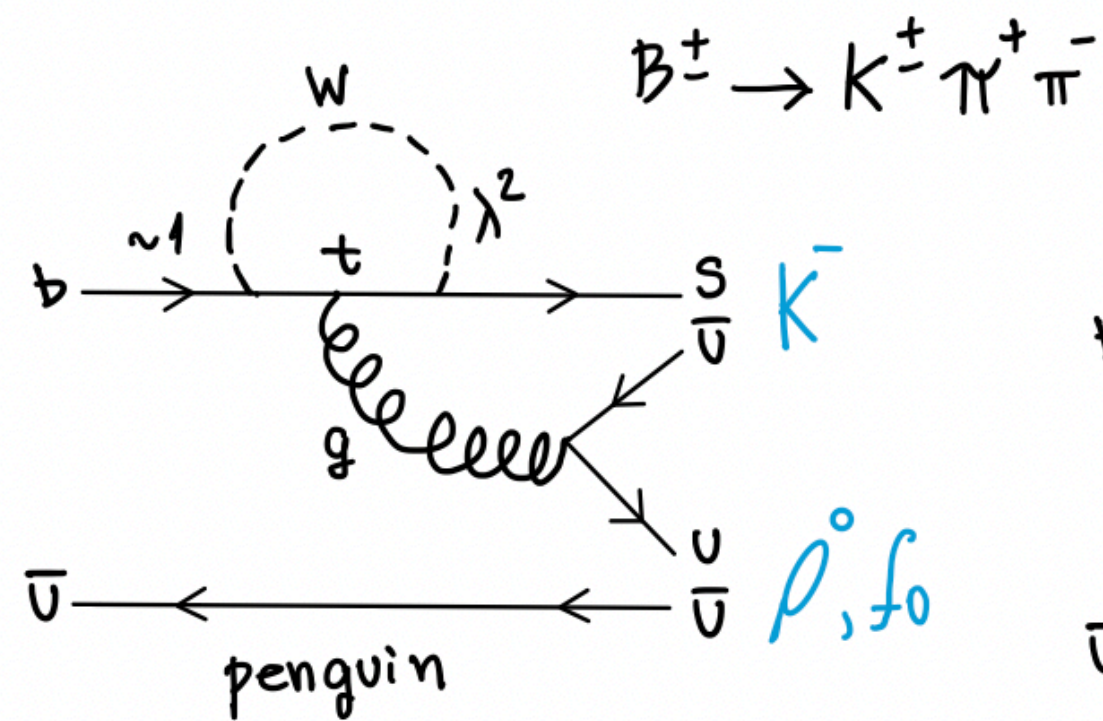
$$A(\bar{B} \rightarrow \bar{f}) = |A_1| e^{i(\delta_1 - \gamma_1)} + |A_2| e^{i(\delta_2 - \gamma_2)}$$

$$A_{CP} = \frac{|A(B \rightarrow f)|^2 - |A(\bar{B} \rightarrow \bar{f})|^2}{|A(B \rightarrow f)|^2 + |A(\bar{B} \rightarrow \bar{f})|^2}$$

$$= \frac{2 |A_2/A_1| \sin(\delta_1 - \delta_2) \sin(\gamma_1 - \gamma_2)}{1 + |A_2/A_1|^2 + |A_2/A_1| \cos(\delta_1 - \delta_2) \cos(\gamma_1 - \gamma_2)}$$



Main Contributions



CPV coming from the interferences between: [PhysRevD.92.054010](https://arxiv.org/abs/hep-ph/0305010)

- Penguin and Tree diagrams
- Resonances in the phase space
- Different final states coupled by the FSI: CPT constraint

Rescattering
 $\pi\pi \leftrightarrow KK$

Hadronic Rescattering

CPT constraints on CP Violation

- CP violation: $\Gamma(P \rightarrow f) - \Gamma(\bar{P} \rightarrow \bar{f}) \neq 0$
- CPT symmetry: total decay widths of P and \bar{P} are the same

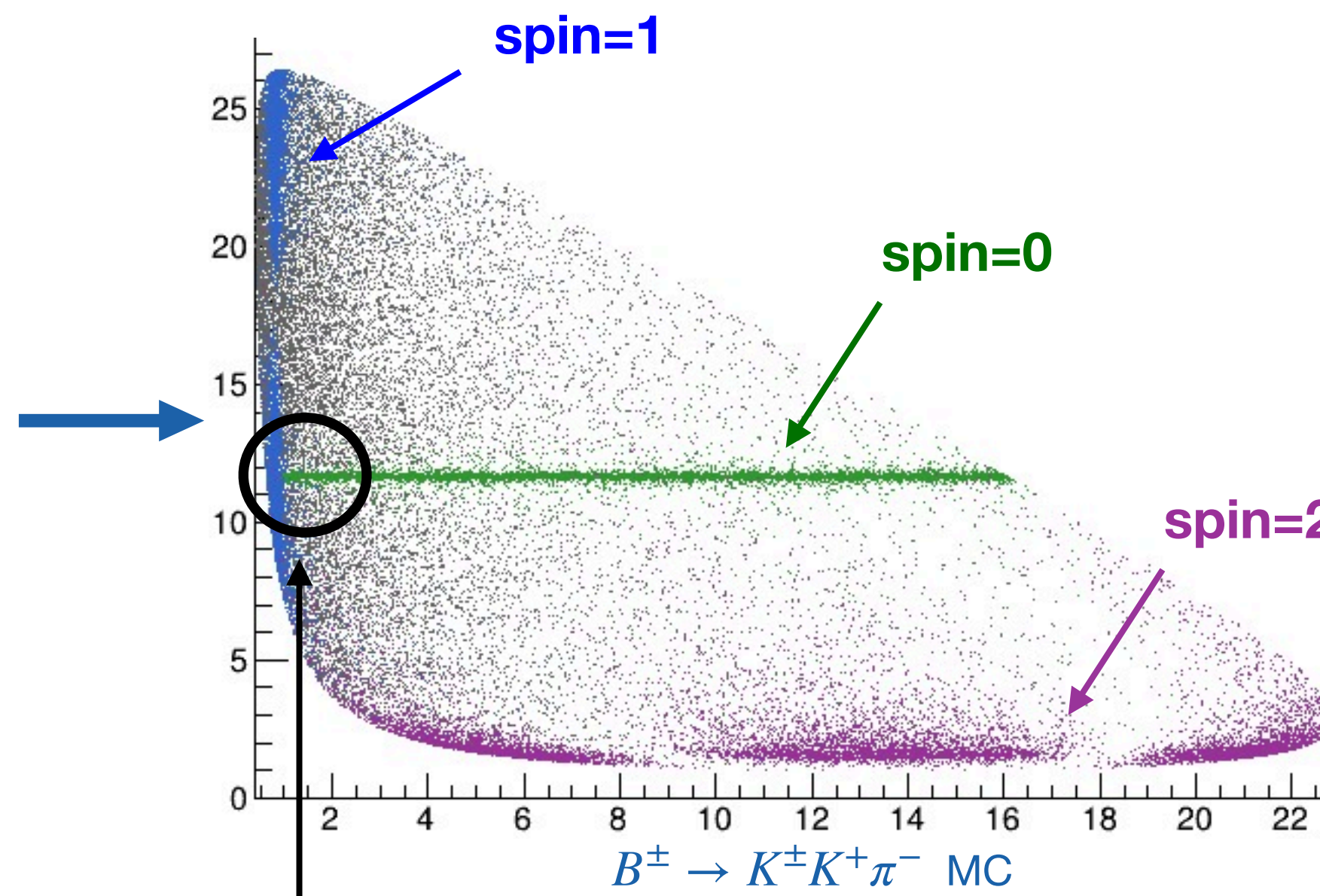
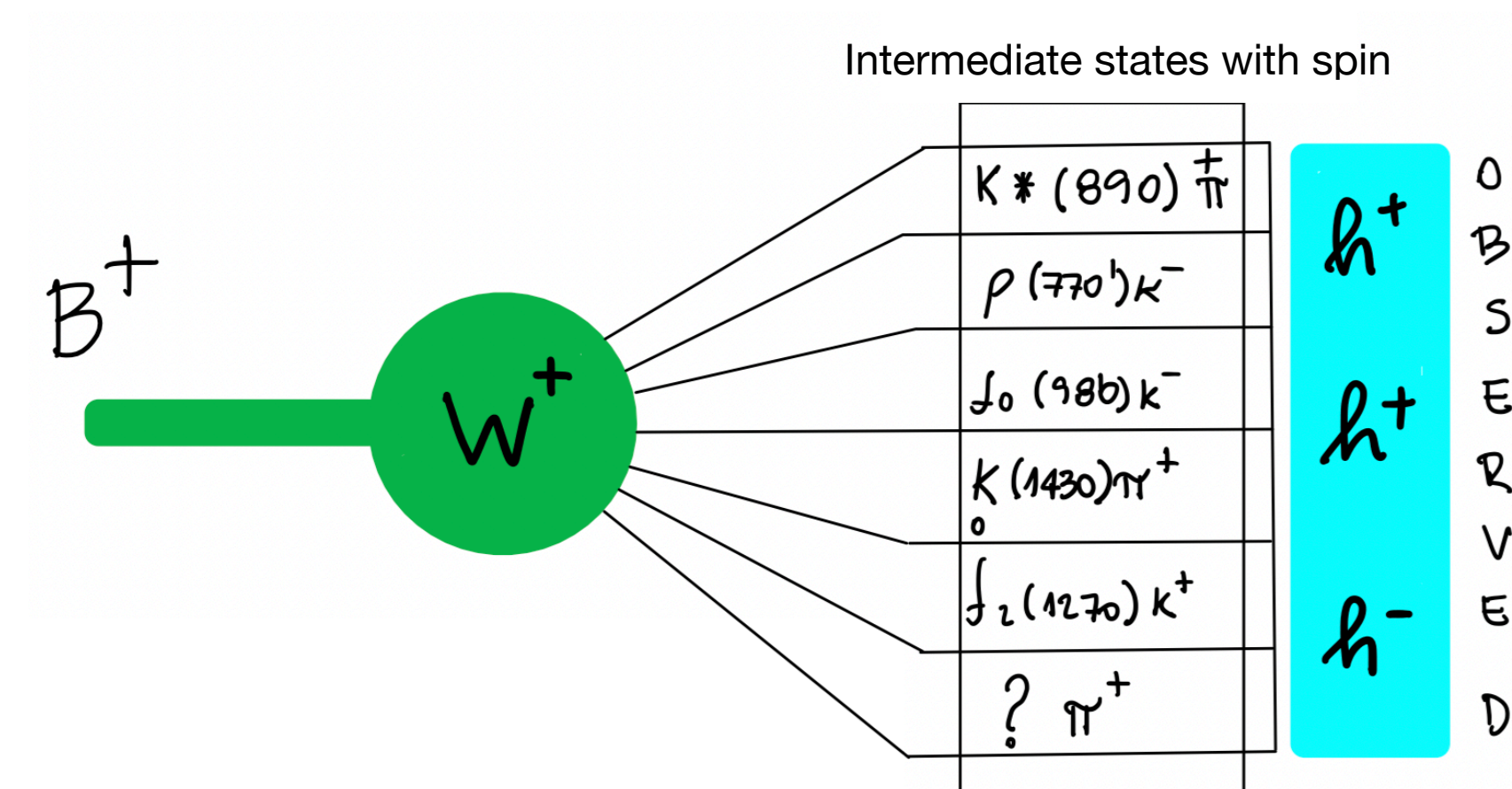
$$\Gamma(P \rightarrow f_1) + \dots + \Gamma(P \rightarrow f_n) = \Gamma(\bar{P} \rightarrow \bar{f}_1) + \dots + \Gamma(\bar{P} \rightarrow \bar{f}_n)$$

“Communication” between the different decay modes with the same flavor quantum numbers

- Ex: $B^\pm \rightarrow \pi^\pm K^+ K^-$ and $B^\pm \rightarrow \pi^\pm \pi^+ \pi^-$
- CPV with opposite signs in partner channels

Final-state-interactions:

- Provides the strong phases for CP violation to be observed
- It is a key ingredient to preserve CPT symmetry



Overlap between vector and scalar resonances

- Two degrees of freedom
- Phase-space graphical representation of the spinless decay

$$d\Gamma = \frac{1}{(2\pi)^3} \frac{1}{32M^3} |\mathcal{M}|^2 dm_{ij}^2 dm_{jk}^2$$

The total decay amplitude squared holds information regarding the dynamics

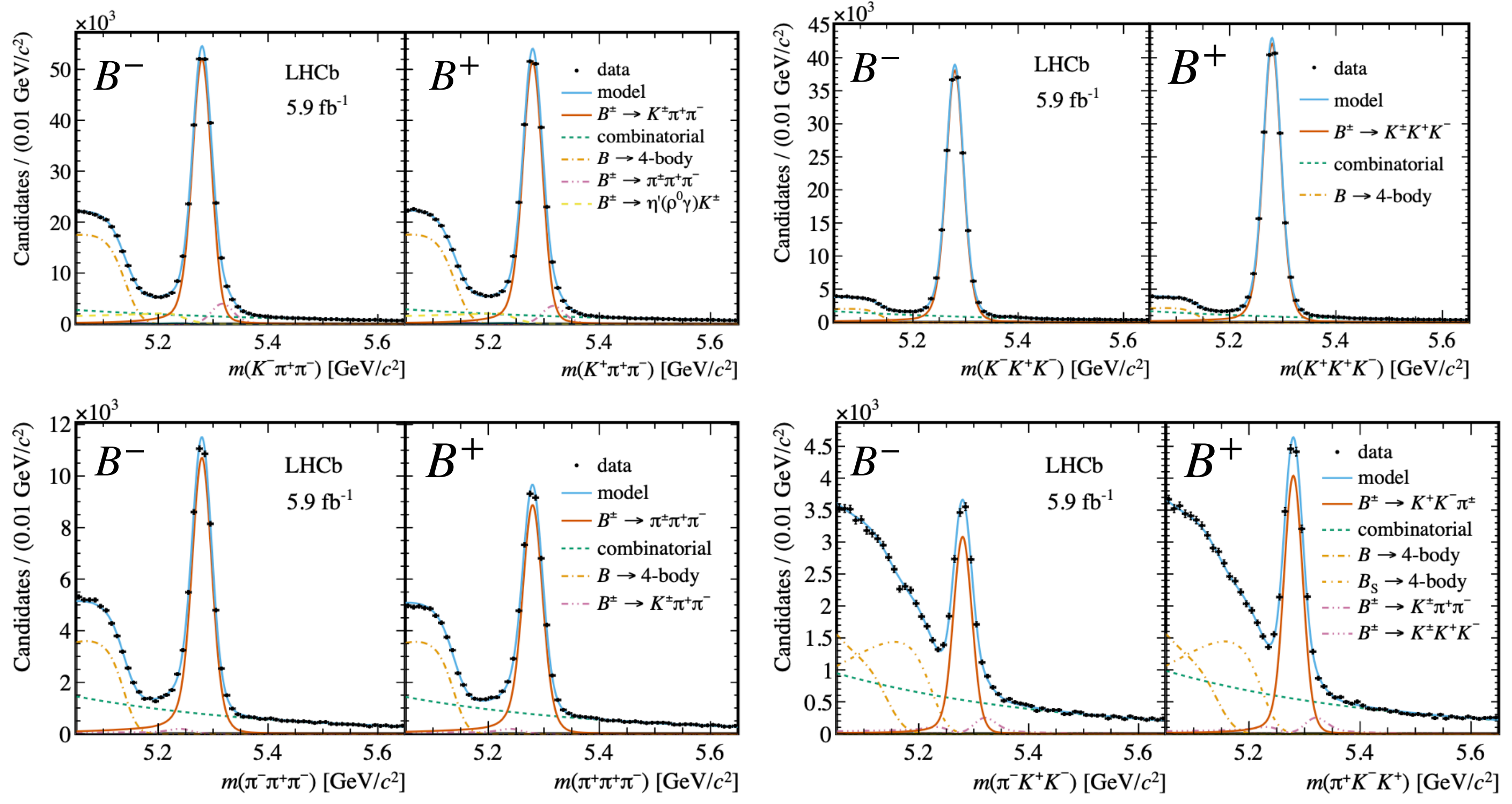
- Why is three-body decays particularly interesting?
 - ✓ All final states have rich resonant structure
 - ✓ Additional source of strong phase difference
 - ✓ Large effects in regions of the Dalitz Plot may arise

Direct CP violation in
charmless three-body decays
of B^\pm mesons

$B^\pm \rightarrow h^\pm h^+ h^-$ — Mass fit results

Invariant mass fit

- Signal PDF:
 - Gaussian + two Crystal Balls functions
- Background:
 - Combinatorial: exponential function
 - Partially reconstructed background: Argus function convolved with a Gaussian
 - Peaking from other $B \rightarrow hhh$ decays: Two Crystal Balls functions



Fit observables

- \otimes Signal yield
- \otimes Raw asymmetry

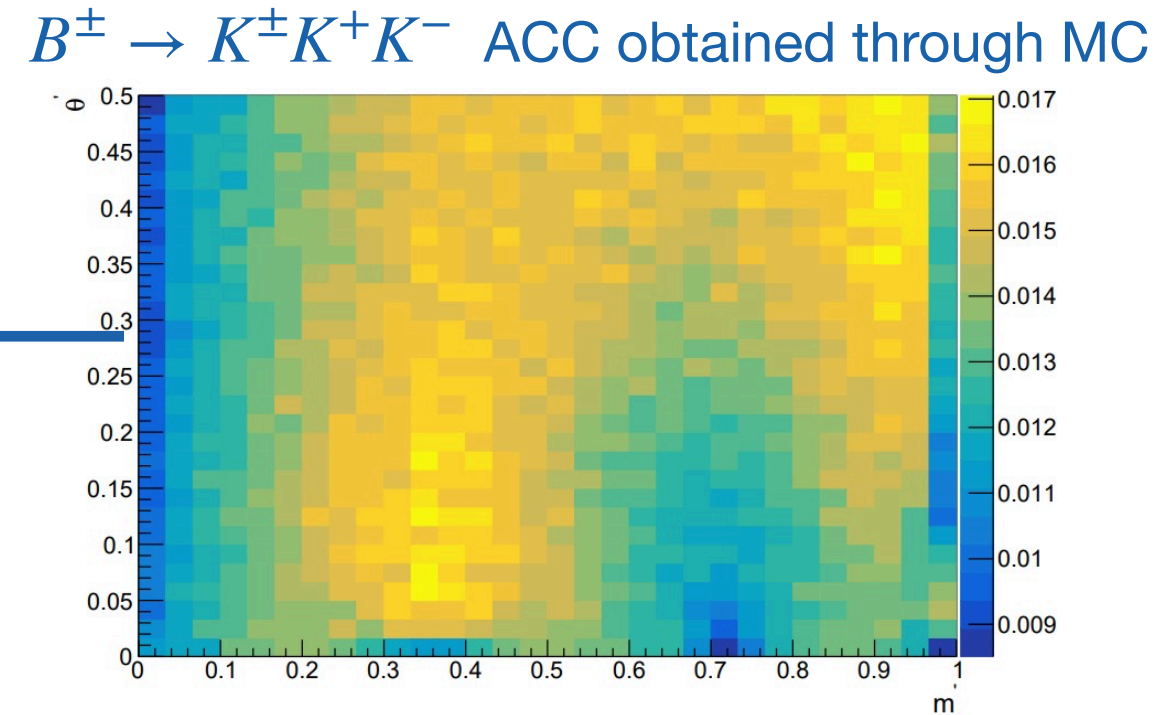
$$A_{raw} = \frac{N^- - N^+}{N^- + N^+}$$

Decay mode	Total yield	A_{raw}
$B^\pm \rightarrow K^\pm \pi^+ \pi^-$	$499\,200 \pm 900$	$+0.006 \pm 0.002$
$B^\pm \rightarrow K^\pm K^+ K^-$	$365\,000 \pm 1000$	-0.052 ± 0.002
$B^\pm \rightarrow \pi^\pm \pi^+ \pi^-$	$101\,000 \pm 500$	$+0.090 \pm 0.004$
$B^\pm \rightarrow \pi^\pm K^+ K^-$	$32\,470 \pm 300$	-0.132 ± 0.007

The efficiency-corrected raw asymmetry:

$$\langle \epsilon^\pm \rangle = \frac{\sum_{i'=1}^{events'} 1}{\sum_{i'=1}^{events'} \frac{1}{acc_i'}}$$

$$R = \frac{\langle \epsilon^- \rangle}{\langle \epsilon^+ \rangle}$$



- ◆ acc_i' : acceptance for the event i
- ◆ ϵ^\pm : efficiency weights
- ◆ R : efficiency correction factor
- ◆ A_{raw}^{corr} : efficiency-corrected raw asymmetries

$$A_{raw}^{corr} = \frac{1 + A_{RAW} - R + A_{RAW} \cdot R}{1 + A_{RAW} + R - A_{RAW} \cdot R}$$

The production asymmetry

$$A_P = A(B^\pm \rightarrow J/\psi K^\pm)_{data} - A(B^\pm \rightarrow J/\psi K^\pm)_{PDG}$$

Used as control channel once CPV is not expected to appear

The physical CP asymmetry:

$$A_{CP} = \frac{A_{raw}^{corr} - A_P}{1 - A_{raw}^{corr} A_P}$$

$$B^\pm \rightarrow K^\pm \pi^+ \pi^-$$

$$A_{CP} = (+1.1 \pm 0.2_{stat} \pm 0.3_{syst} \pm 0.3_{J/\psi K}) \% \quad \leftarrow 2.4\sigma$$

$$B^\pm \rightarrow K^\pm K^+ K^-$$

$$A_{CP} = (-3.7 \pm 0.2_{stat} \pm 0.2_{syst} \pm 0.3_{J/\psi K}) \% \quad \leftarrow 8.5\sigma$$

$$B^\pm \rightarrow \pi^\pm \pi^+ \pi^-$$

$$A_{CP} = (+8.0 \pm 0.4_{stat} \pm 0.3_{syst} \pm 0.3_{J/\psi K}) \% \quad \leftarrow 14.1\sigma$$

$$B^\pm \rightarrow \pi^\pm K^+ K^-$$

$$A_{CP} = (-11.4 \pm 0.7_{stat} \pm 0.3_{syst} \pm 0.3_{J/\psi K}) \% \quad \leftarrow 13.6\sigma$$

First observation of CPV in $B^\pm \rightarrow K^\pm K^+ K^-$,
 $B^\pm \rightarrow \pi^\pm \pi^+ \pi^-$

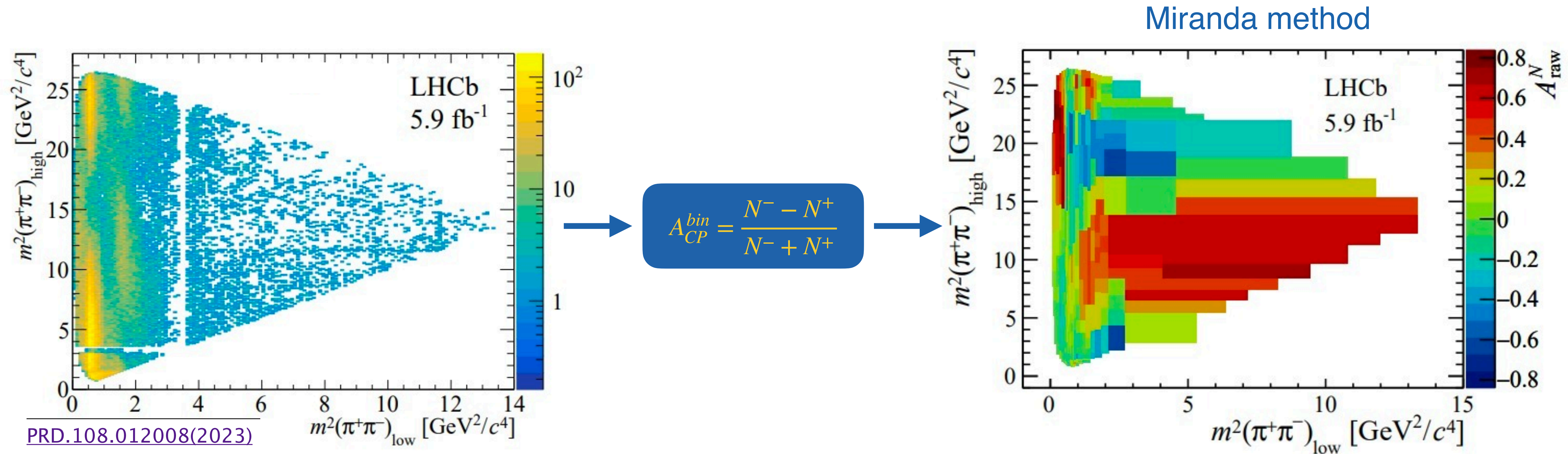
Run I results

$$A_{CP}(B^\pm \rightarrow K^\pm \pi^+ \pi^-) = +0.025 \pm 0.004 \pm 0.004 \pm 0.007 \quad \leftarrow 2.8\sigma$$

$$A_{CP}(B^\pm \rightarrow K^\pm K^+ K^-) = -0.036 \pm 0.004 \pm 0.002 \pm 0.007 \quad \leftarrow 4.3\sigma$$

$$A_{CP}(B^\pm \rightarrow \pi^\pm \pi^+ \pi^-) = +0.058 \pm 0.008 \pm 0.009 \pm 0.007 \quad \leftarrow 4.2\sigma$$

$$A_{CP}(B^\pm \rightarrow \pi^\pm K^+ K^-) = -0.123 \pm 0.017 \pm 0.012 \pm 0.007 \quad \leftarrow 5.6\sigma$$

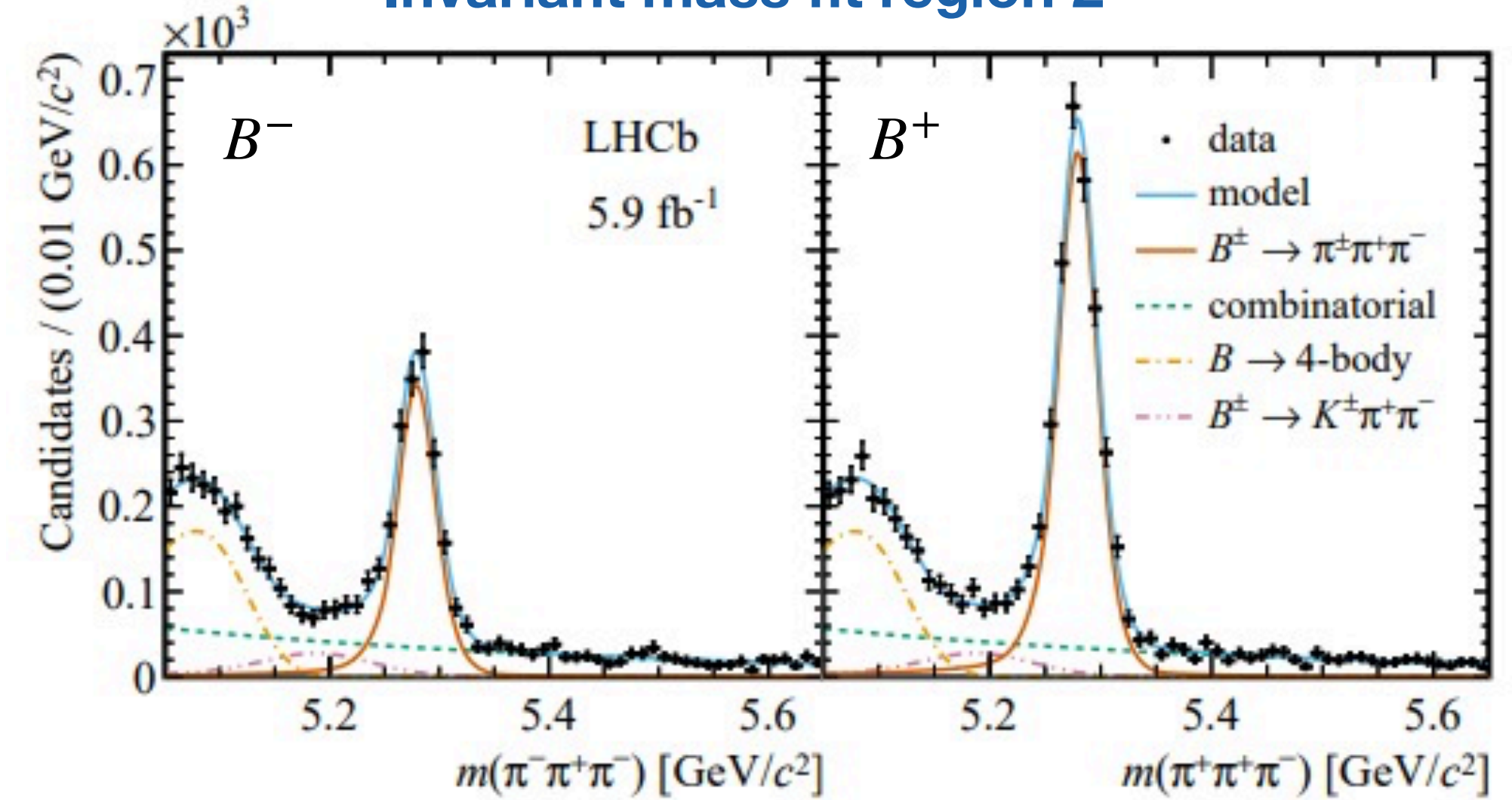
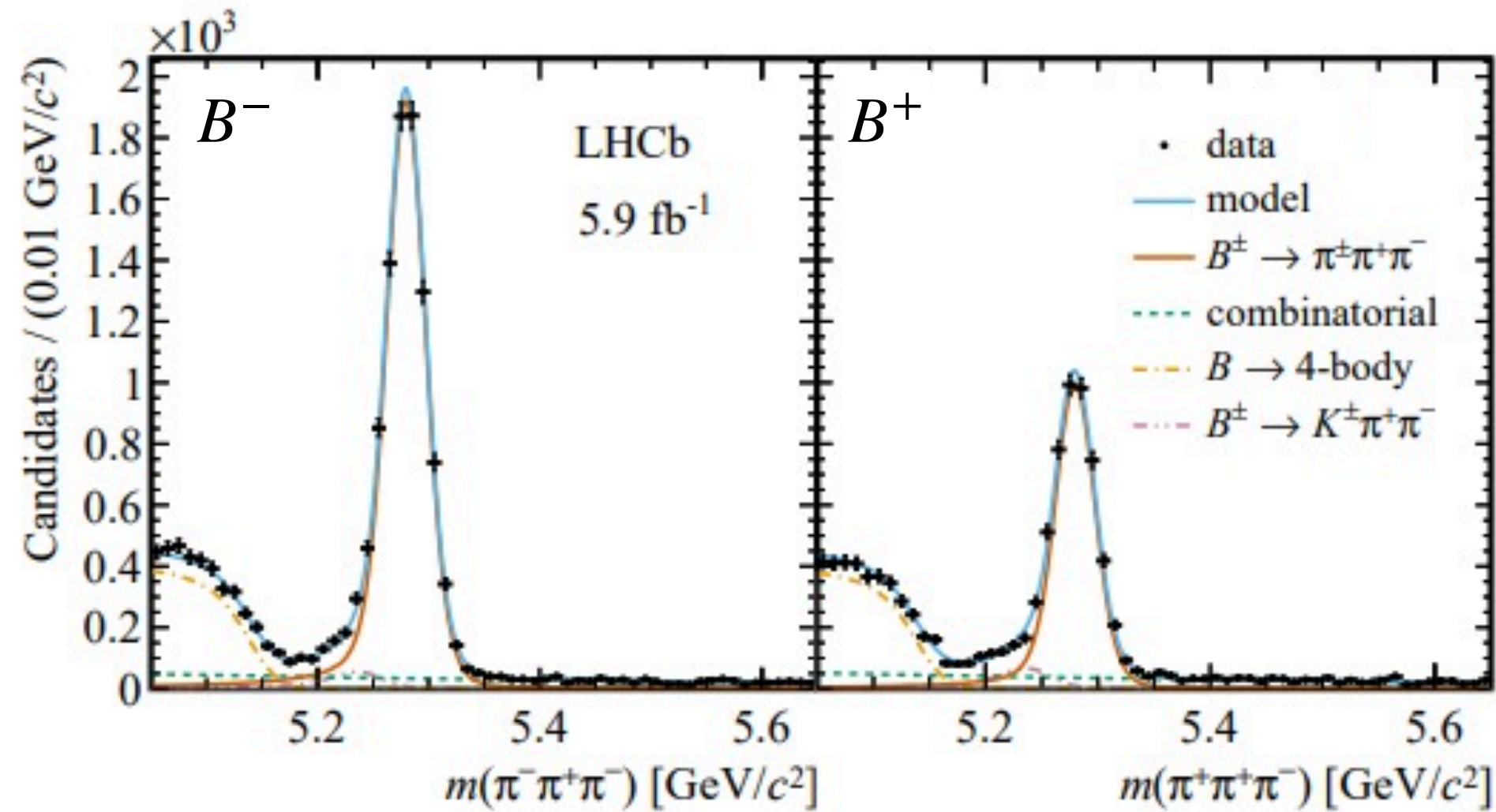


- Histogram created by an adaptive binning algorithm
- The asymmetry is calculated from the number of events in the bin
- Localized asymmetry within the range -80% — +80%

Invariant mass fit region 1



Invariant mass fit region 2



Region 1

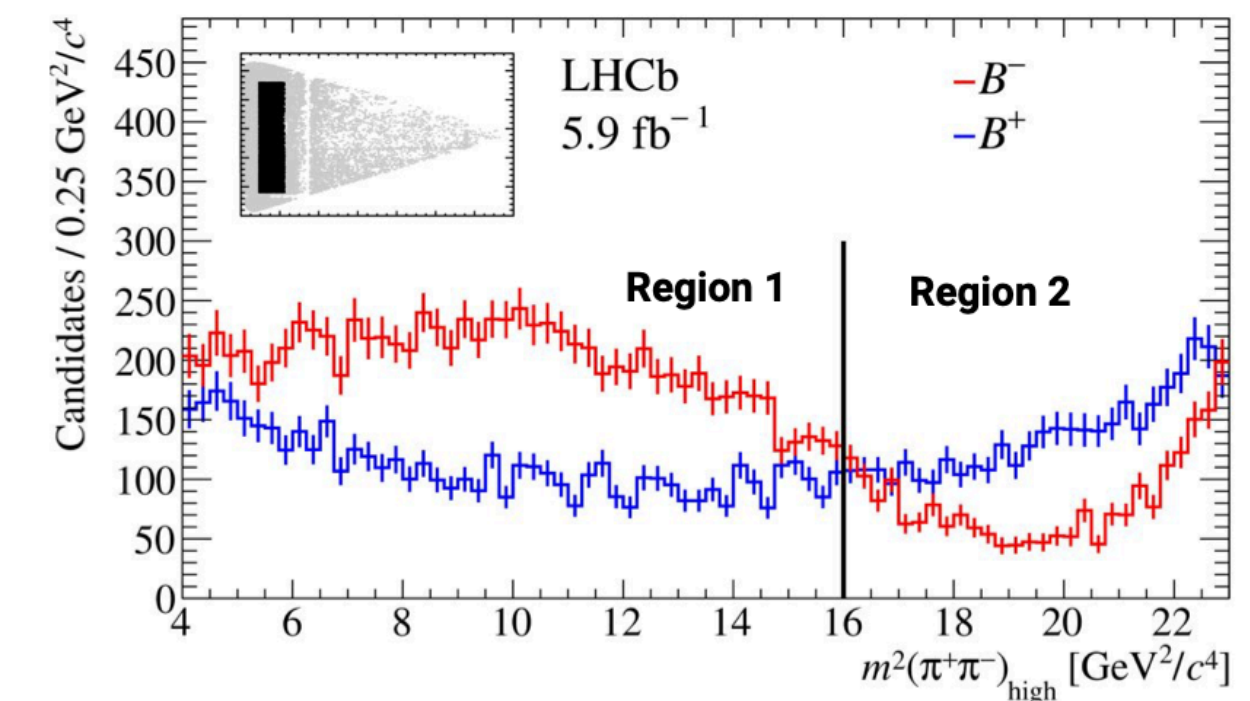
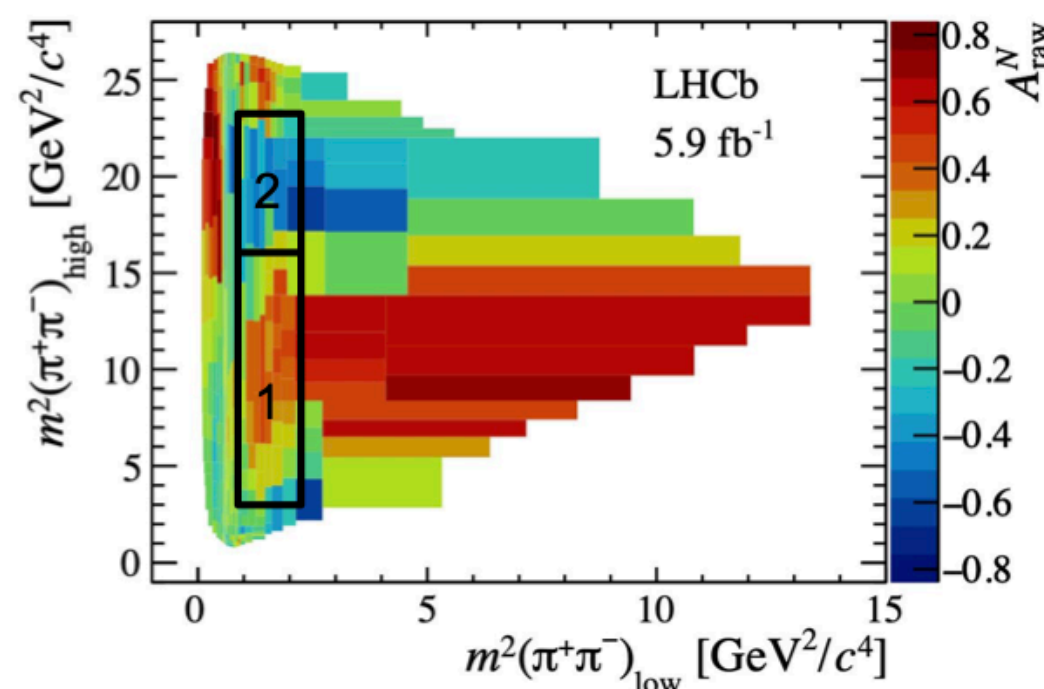
Region 2

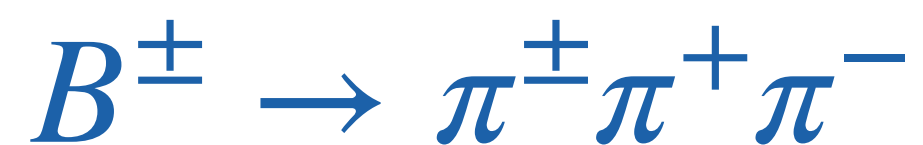
[PRD.108.012008\(2023\)](#)

$$A_{CP} = (+30.3 \pm 0.9_{stat} \pm 0.4_{syst} \pm 0.3_{J/\psi K}) \%$$

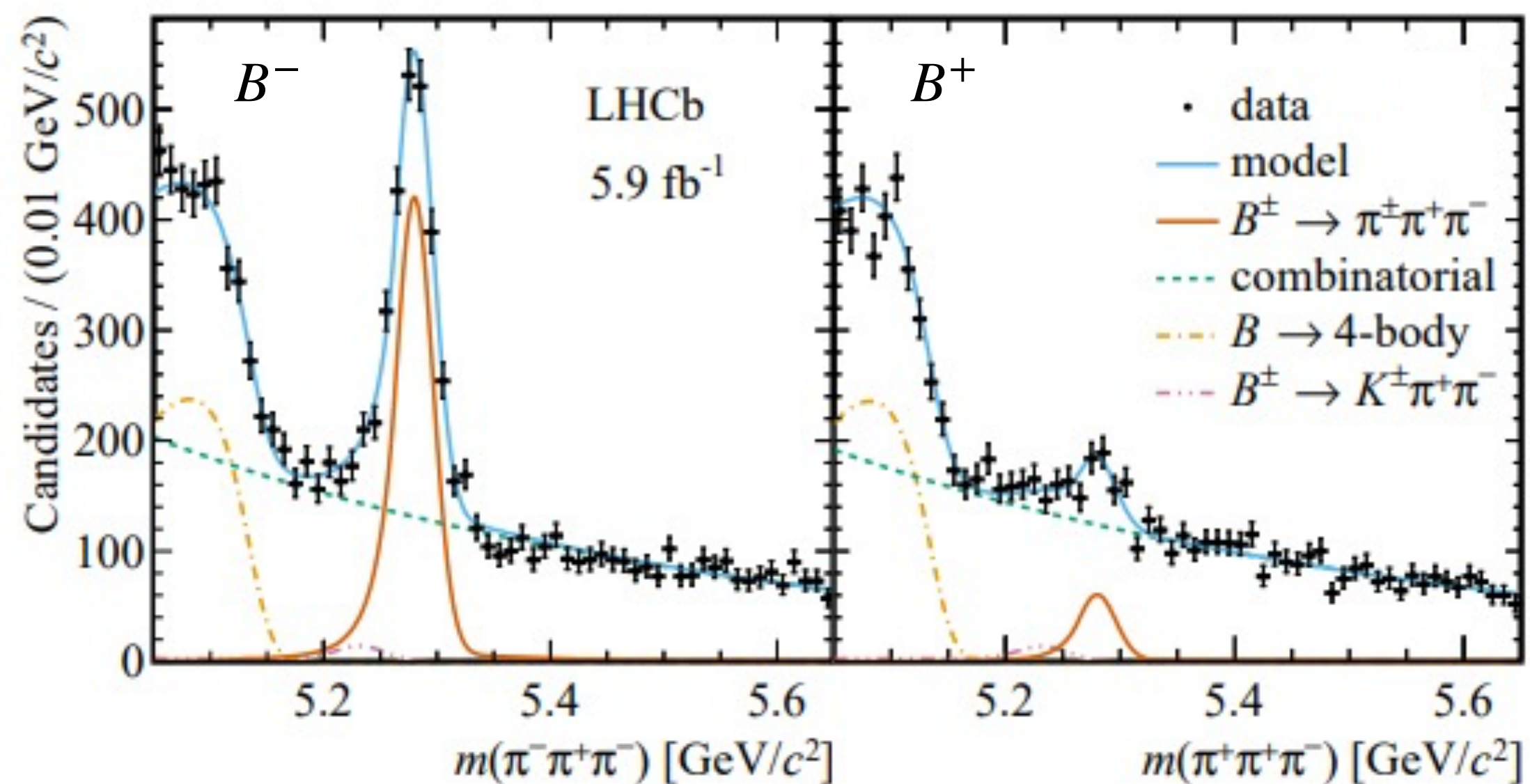
$$A_{CP} = (-28.4 \pm 1.7_{stat} \pm 0.7_{syst} \pm 0.3_{J/\psi K}) \%$$

Asymmetry in bins of phase space



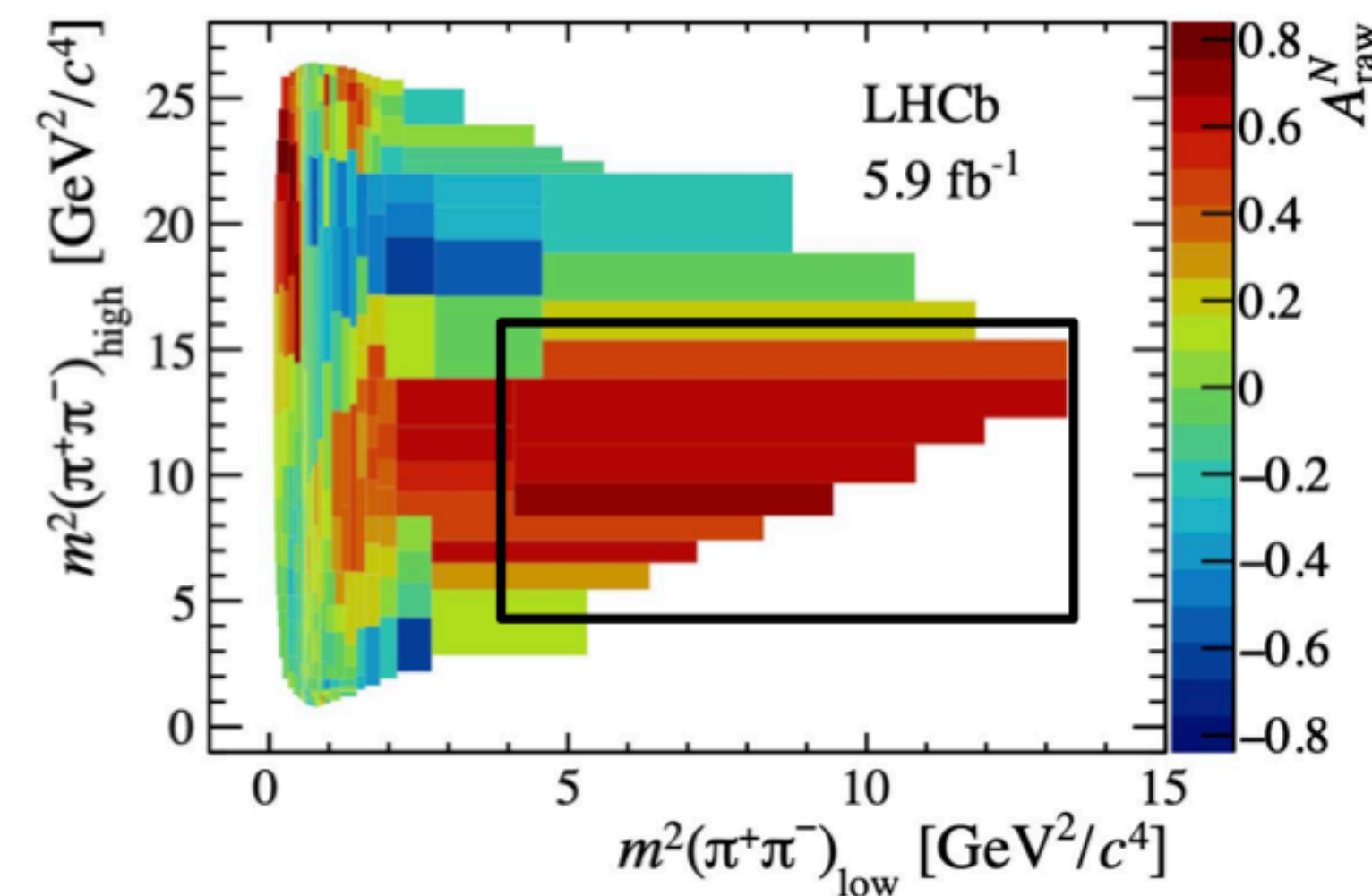


Invariant mass fit region 3



**Large
CPV
observed**

Asymmetry in bins of phase space

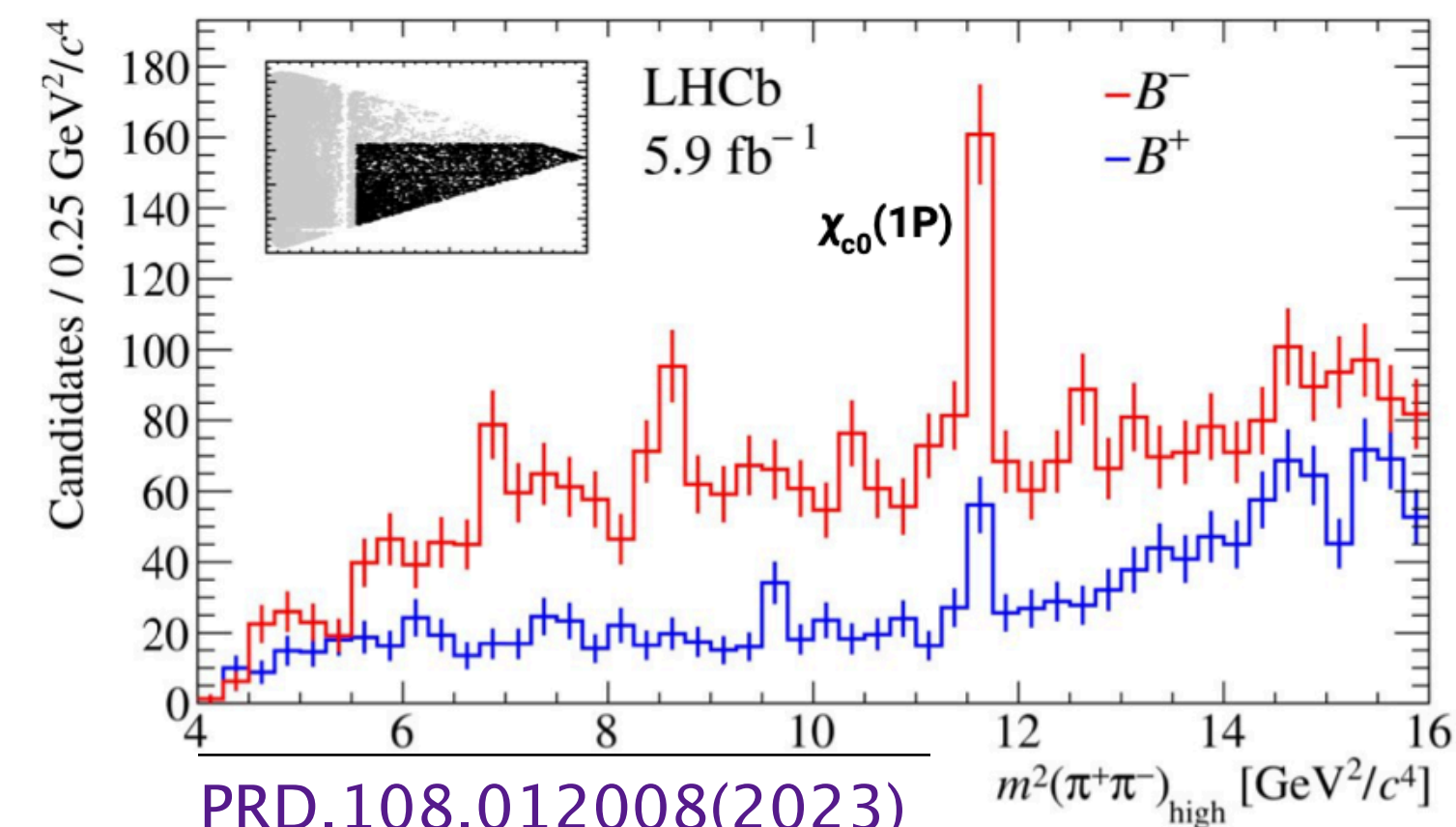


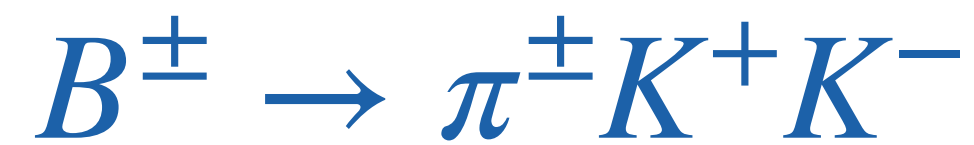
Region 3

$$A_{CP} = (+74.5 \pm 2.7_{stat} \pm 1.8_{syst} \pm 0.3_{J/\psi K}) \%$$

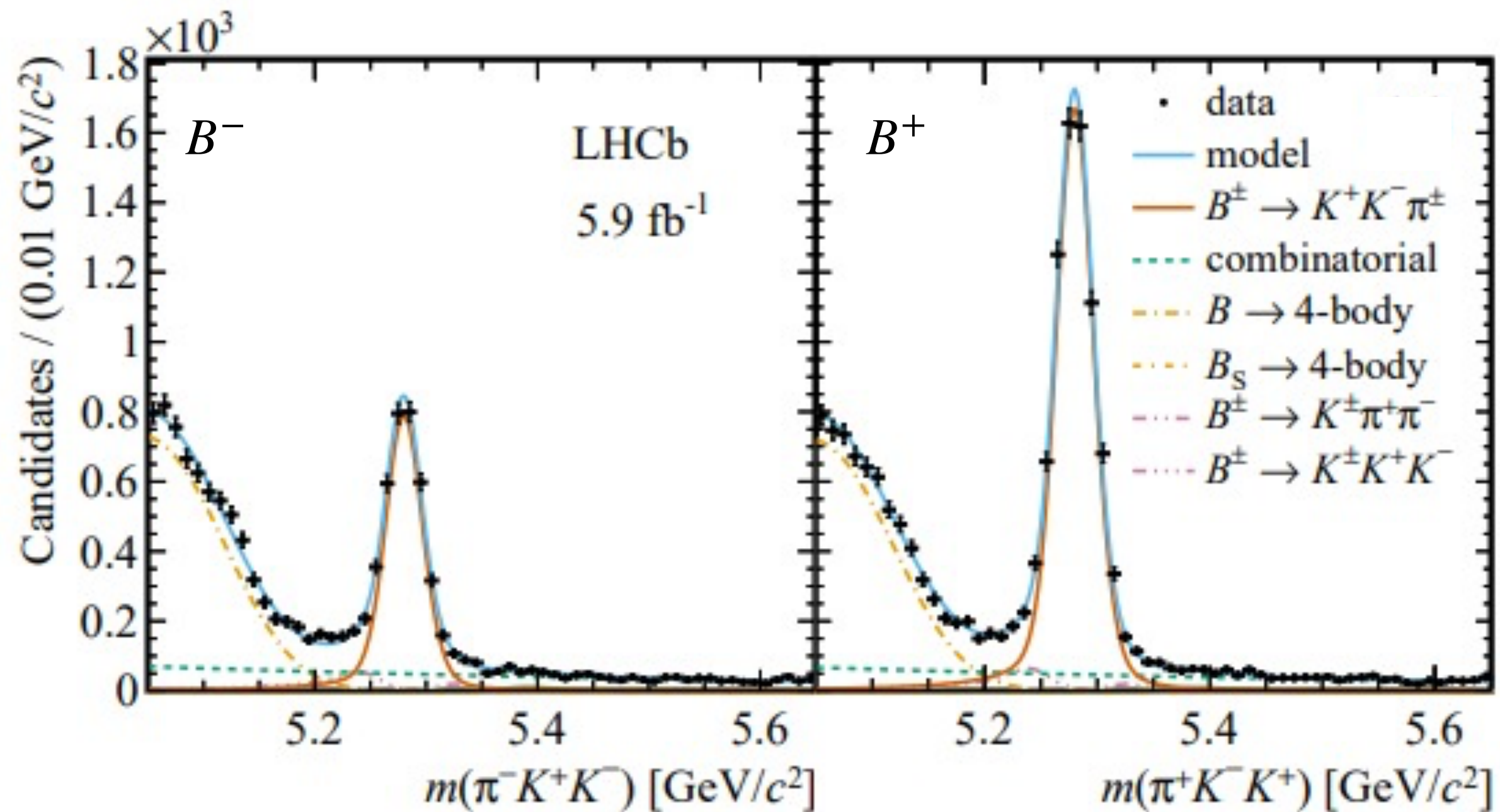
• No direct CPV expected in $\chi_{c0}(1P)$ in SM [Phys. Rev. Lett. 74 4984\(1995\)](#)

✓ Run2 amplitude analysis will provide further details





Invariant mass fit Rescattering region



Rescattering Region

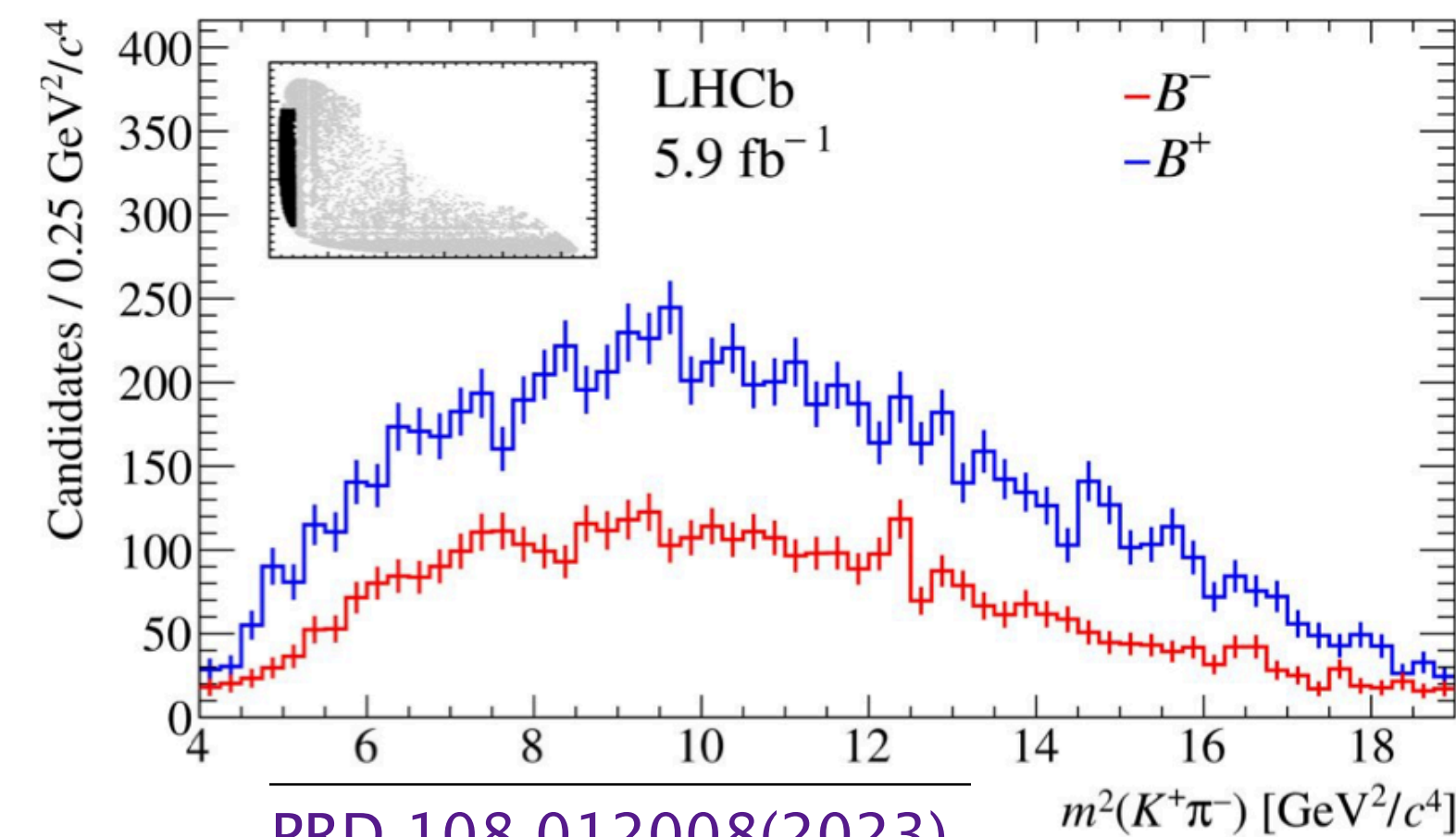
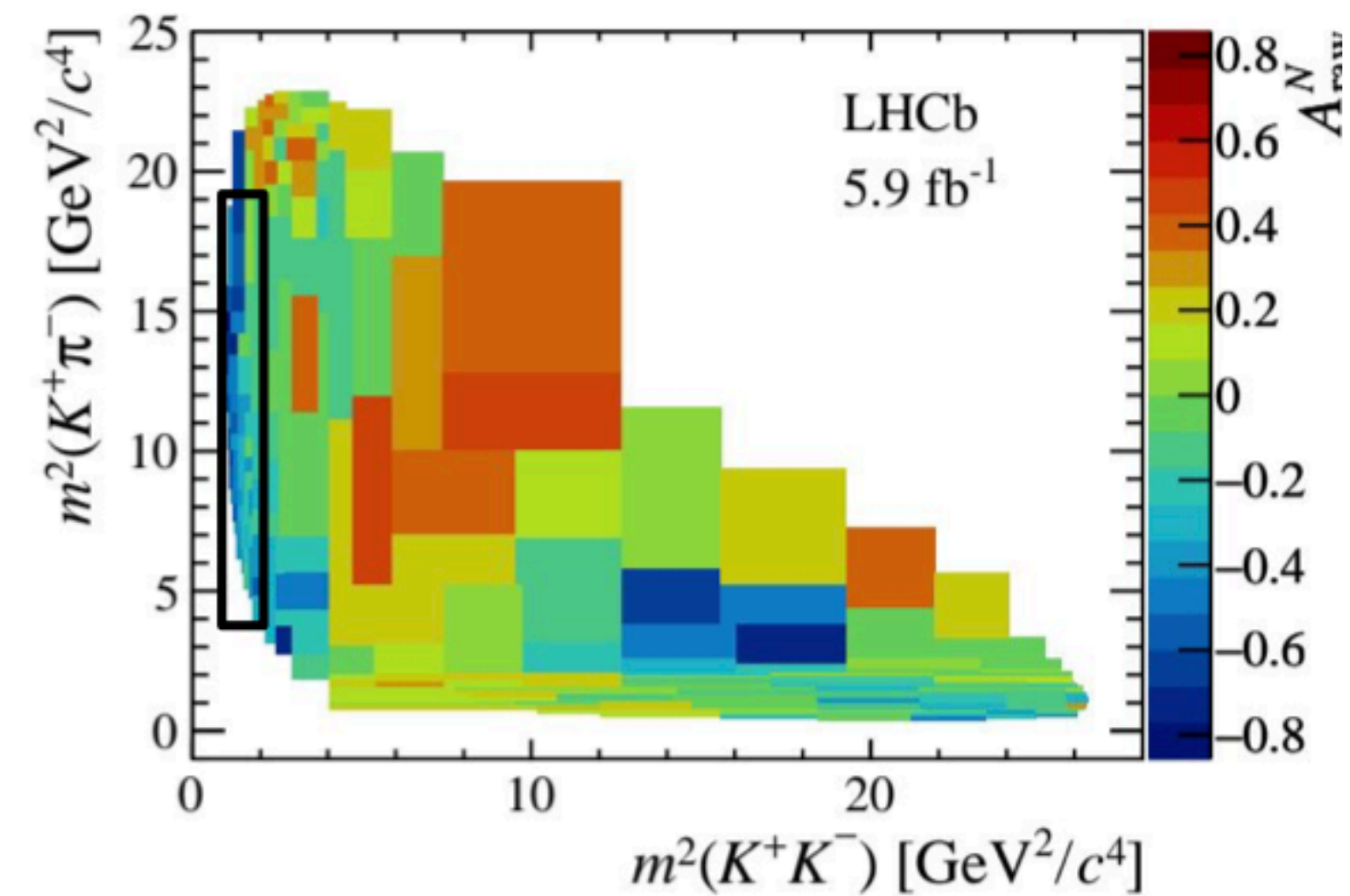
$$A_{CP} = (-35.8 \pm 1.0_{stat} \pm 1.4_{syst} \pm 0.3_{J/\psi K}) \%$$

- Nearly constant CPV for the Rescattering region
- Features of Rescattering during run I:

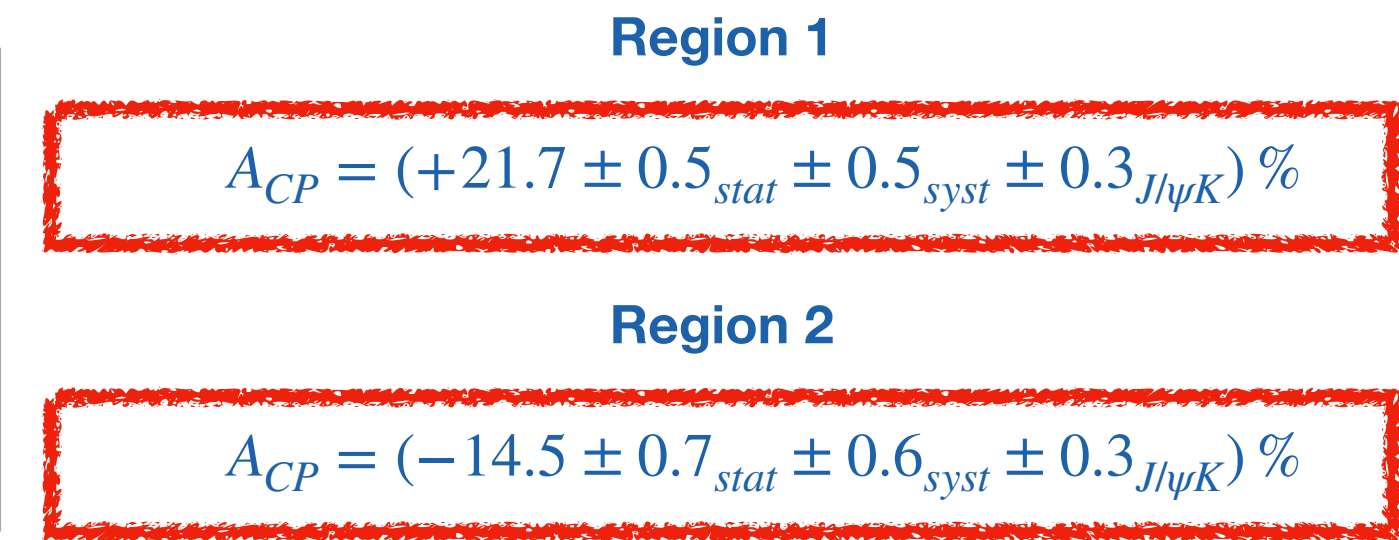
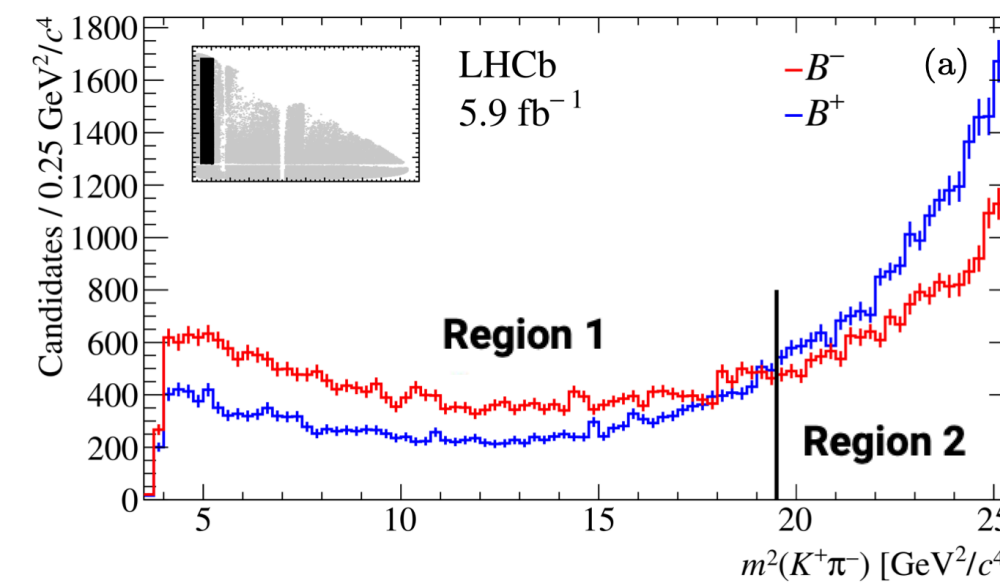
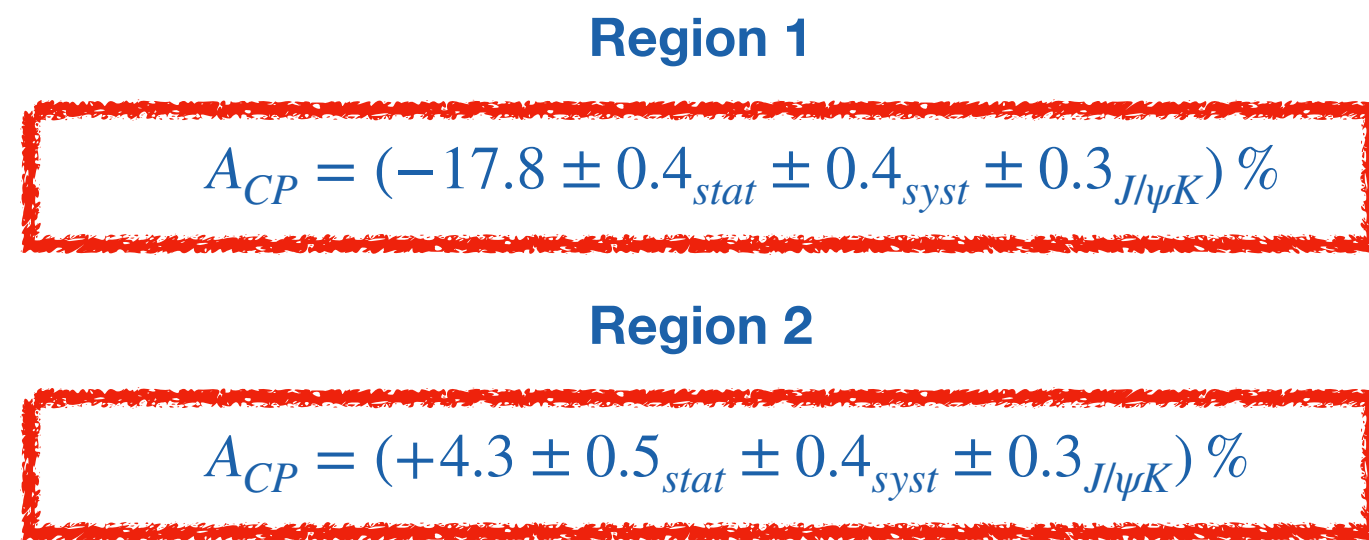
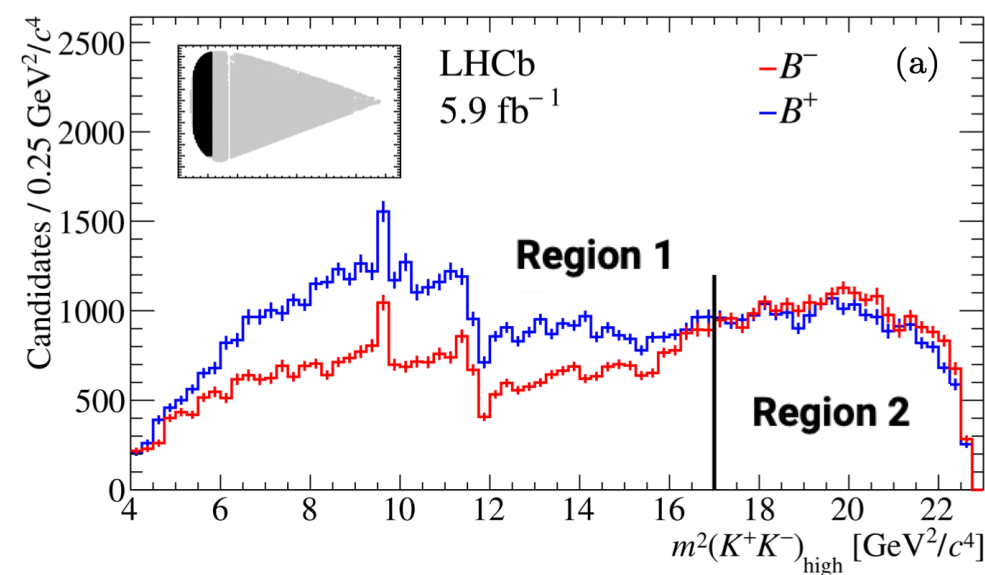
- ✓ Asymmetry of -66%
- ✓ Fit Fraction of 16%

[Phys. Rev. Lett. 123 \(2019\) 231802](https://arxiv.org/abs/1905.02701)

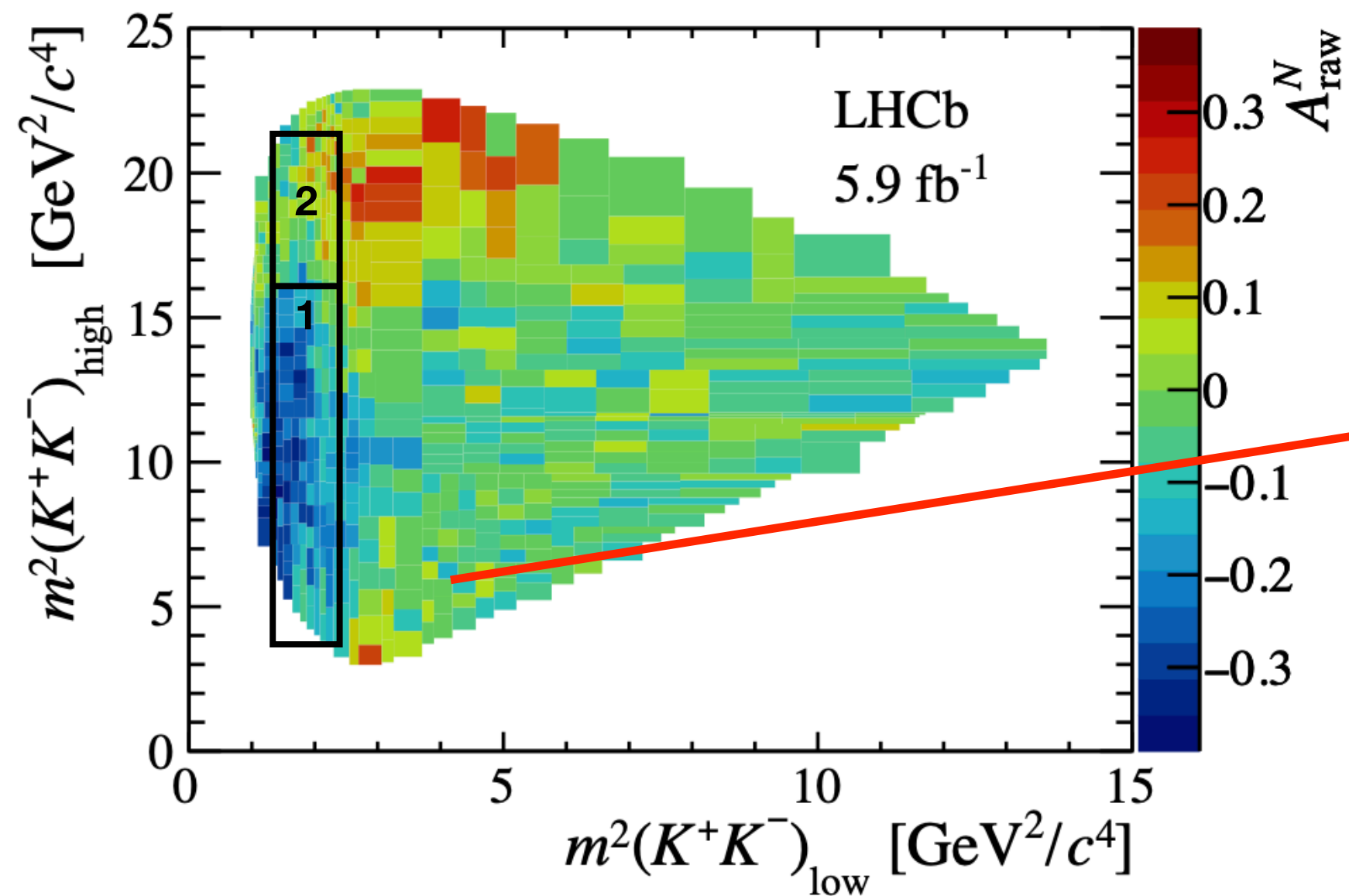
Asymmetry in bins of phase space



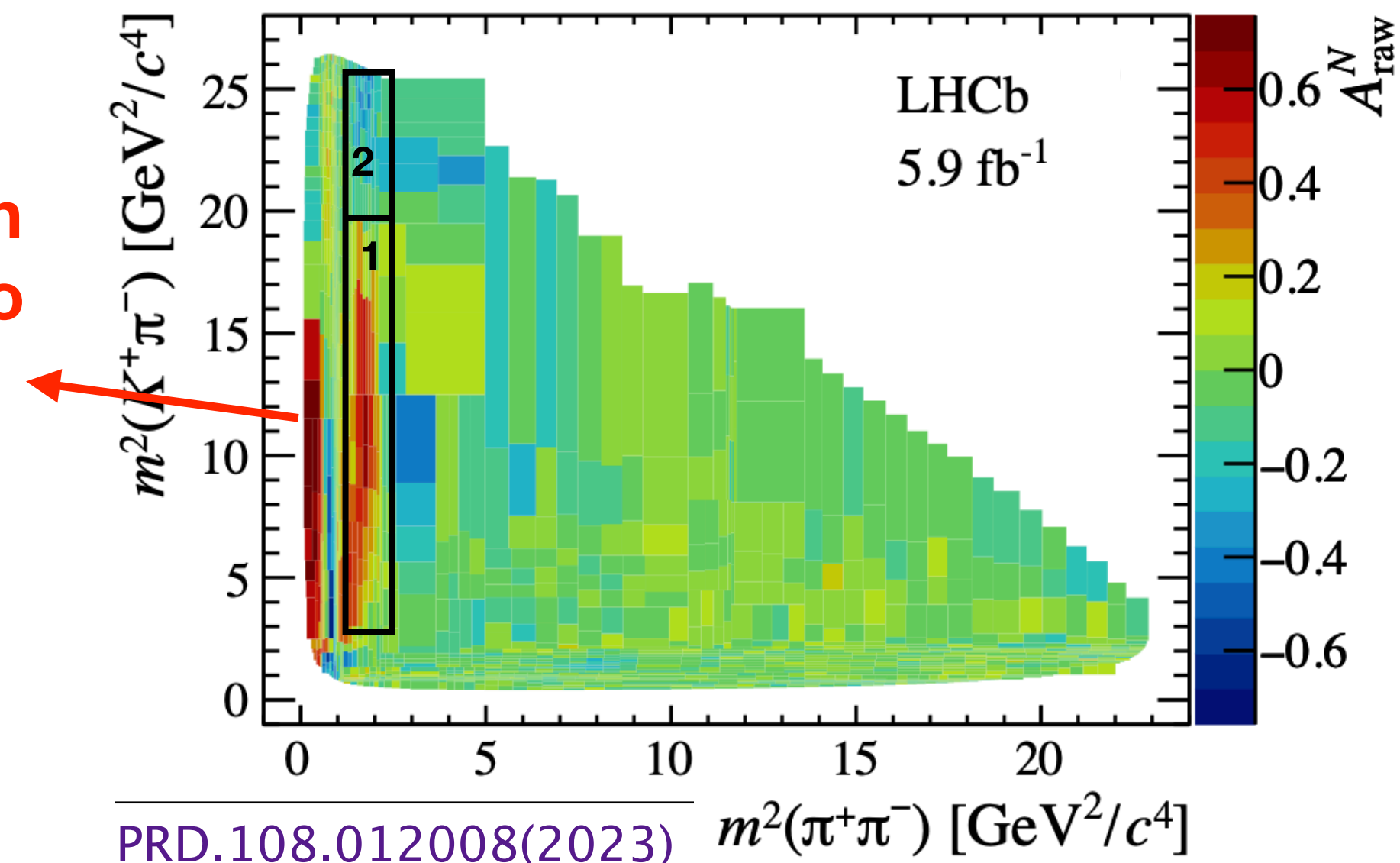
[PRD.108.012008\(2023\)](https://arxiv.org/abs/2208.01208)



Asymmetry in bins of phase space



Asymmetry sign is changing in an opposite direction with respect to each other



PRD.108.012008(2023)

Search for direct CPV in $B \rightarrow PV$

📌 Motivated by:

- ✓ Great interest involving the CPV in quasi-two-body decays [Nucl.Phys.B675\(2003\)](#)
- ✓ Contribution of short- and long-distance to strong phase
- ✓ This method does not require a full amplitude analyses

📌 Features of three-body B decays:

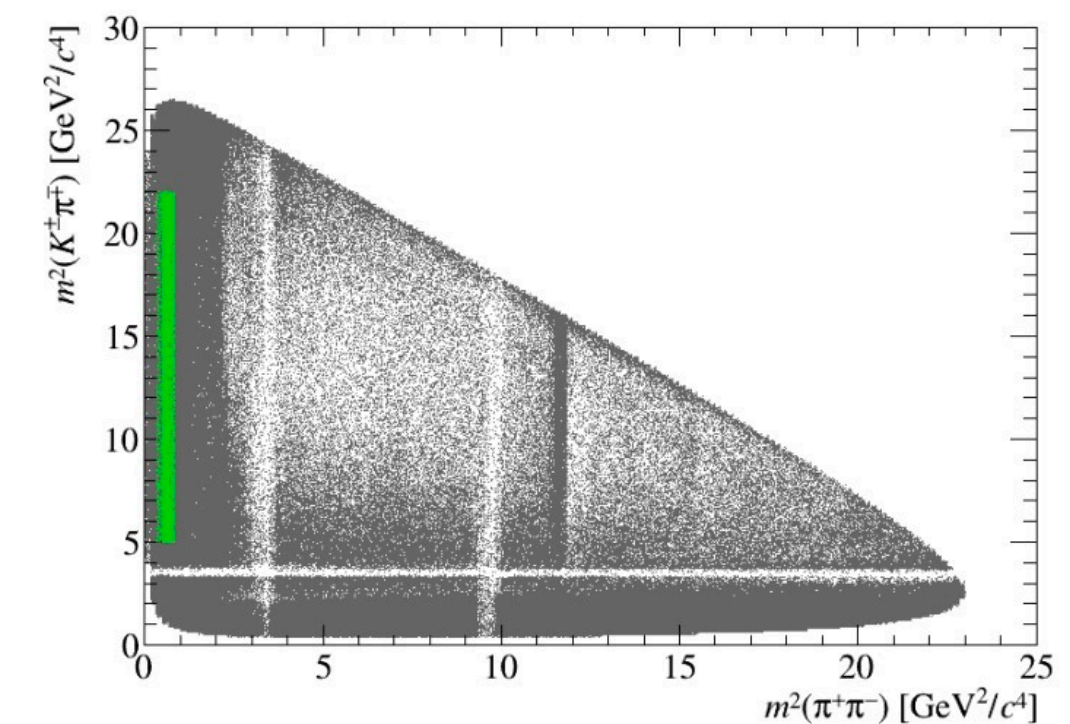
- ✓ Large phase-space
- ✓ Dominance of scalars and vectors resonances with low mass
- ✓ Signature of the resonances in the phase-space

📌 First time this method is used with data [PhysRevD.94.054028](#)

- ✓ Method validated with Monte Carlo Simulation

Model independent method

- 📌 Select a central mass slice of a vector involving interference with a single scalar



- The decay amplitudes can be represented by: [PhysRevD.94.054028](#)

$$\mathcal{M}_\pm = a_\pm^V e^{i\delta_\pm^V} F_V^{BW} \cos\theta(s_\perp, s_\parallel) + a_\pm^{NR} e^{i\delta_\pm^{NR}} F_{NR}^{BW}$$

- The matrix element squared is:

$$|\mathcal{M}_\pm|^2 = \underbrace{(a_\pm^V)^2 (\cos\theta)^2 |F_V^{BW}|^2}_{\text{Direct vector } A_{CP}} + \underbrace{(a_\pm^S)^2 |F_S^{BW}|^2}_{\text{Direct scalar } A_{CP}}$$

$$+ 2a_\pm^V a_\pm^S \cos\theta |F_V^{BW}|^2 |F_S^{BW}|^2 \times \{ \cos(\delta_\pm^V - \delta_\pm^S) [(m_V^2 - s_\parallel)(m_S^2 - s_\parallel) + (m_V \Gamma_V)(m_S \Gamma_S)] + \sin(\delta_\pm^V - \delta_\pm^S) [(m_S \Gamma_S)(m_V^2 - s_\parallel) - (m_V \Gamma_V)(m_S^2 - s_\parallel)] \},$$

Scalar and vector interference

Assumptions

- a_\pm^V and a_\pm^S independent of s_\perp
- $s_\parallel = (p_{h^+} + p_{h^-})^2$
- $s_\perp = (p_{h_b} + p_{h^\pm})^2$

B^\pm decays into a vector + scalar resonance

Asymmetry \propto amplitude square:

$$|\mathcal{M}_\pm|^2 = \underbrace{p_0^\pm}_{\text{Direct scalar } A_{CP}} + \underbrace{p_1^\pm \cos\theta(m_V^2, s_\perp)}_{\text{Scalar and vector interference}} + \underbrace{p_2^\pm \cos^2\theta(m_V^2, s_\perp)}_{\text{Direct vector } A_{CP}}$$

Quadratic function to get amplitude parameters:

$$\checkmark f(x) = p_0 + p_1 x + p_2 x^2$$

$$A_{CP}^V = \frac{|\mathcal{M}_-|^2 - |\mathcal{M}_+|^2}{|\mathcal{M}_-|^2 + |\mathcal{M}_+|^2} = \frac{p_2^- - p_2^+}{p_2^- + p_2^+}$$

$B^\pm \rightarrow (V \rightarrow h^+ h^-) h^\pm$ contributions:

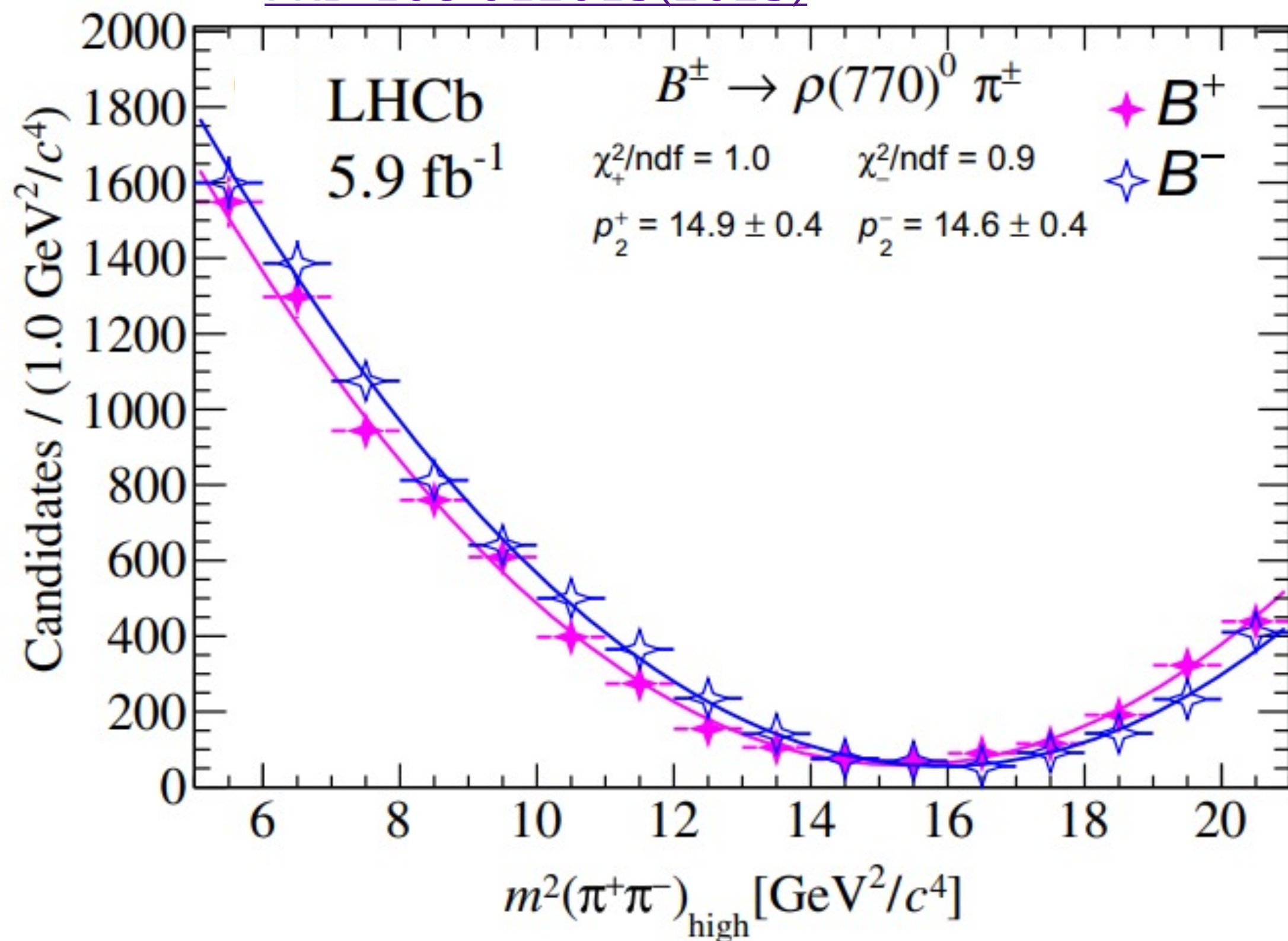
- $B^\pm \rightarrow (\rho(770)^0 \rightarrow \pi^+ \pi^-) \pi^\pm$
- $B^\pm \rightarrow (\rho(770)^0 \rightarrow \pi^+ \pi^-) K^\pm$
- $B^\pm \rightarrow (K^*(892)^0 \rightarrow K^+ \pi^-) \pi^\pm$
- $B^\pm \rightarrow (K^*(892)^0 \rightarrow K^+ \pi^-) K^\pm$
- $B^\pm \rightarrow (\phi(1020) \rightarrow K^+ K^-) K^\pm$

Given this approximation the A_{CP} can be obtained from the s_\perp

$$\cos\theta(s_\parallel, s_\perp) \approx \cos\theta(m_V^2, s_\perp)$$

$\cos\theta$ becomes a linear function of s_\perp

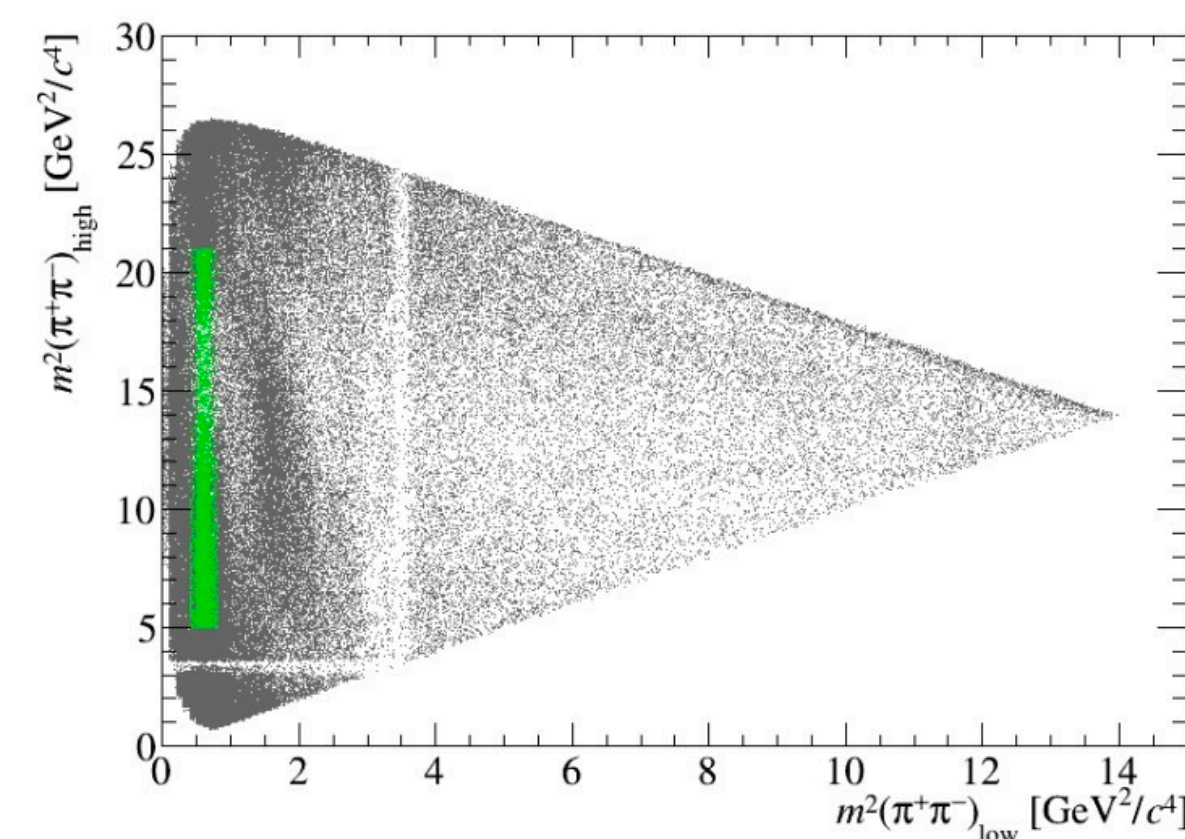
PRD.108.012013(2023)



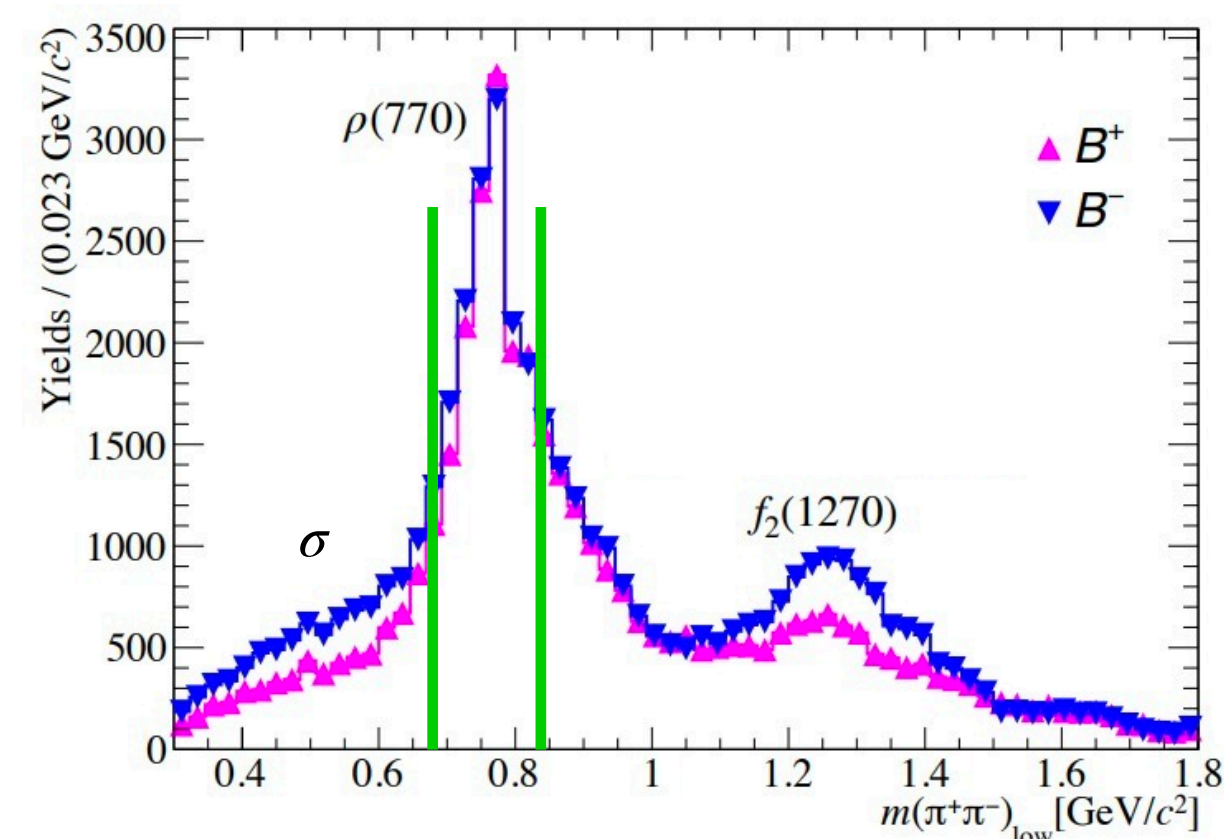
$$A_{CP} = (-0.4 \pm 1.7_{stat} \pm 0.9_{syst}) \%$$

LHCb previous results: [Phys. Rev. Lett. 124\(2020\) 031801](#)

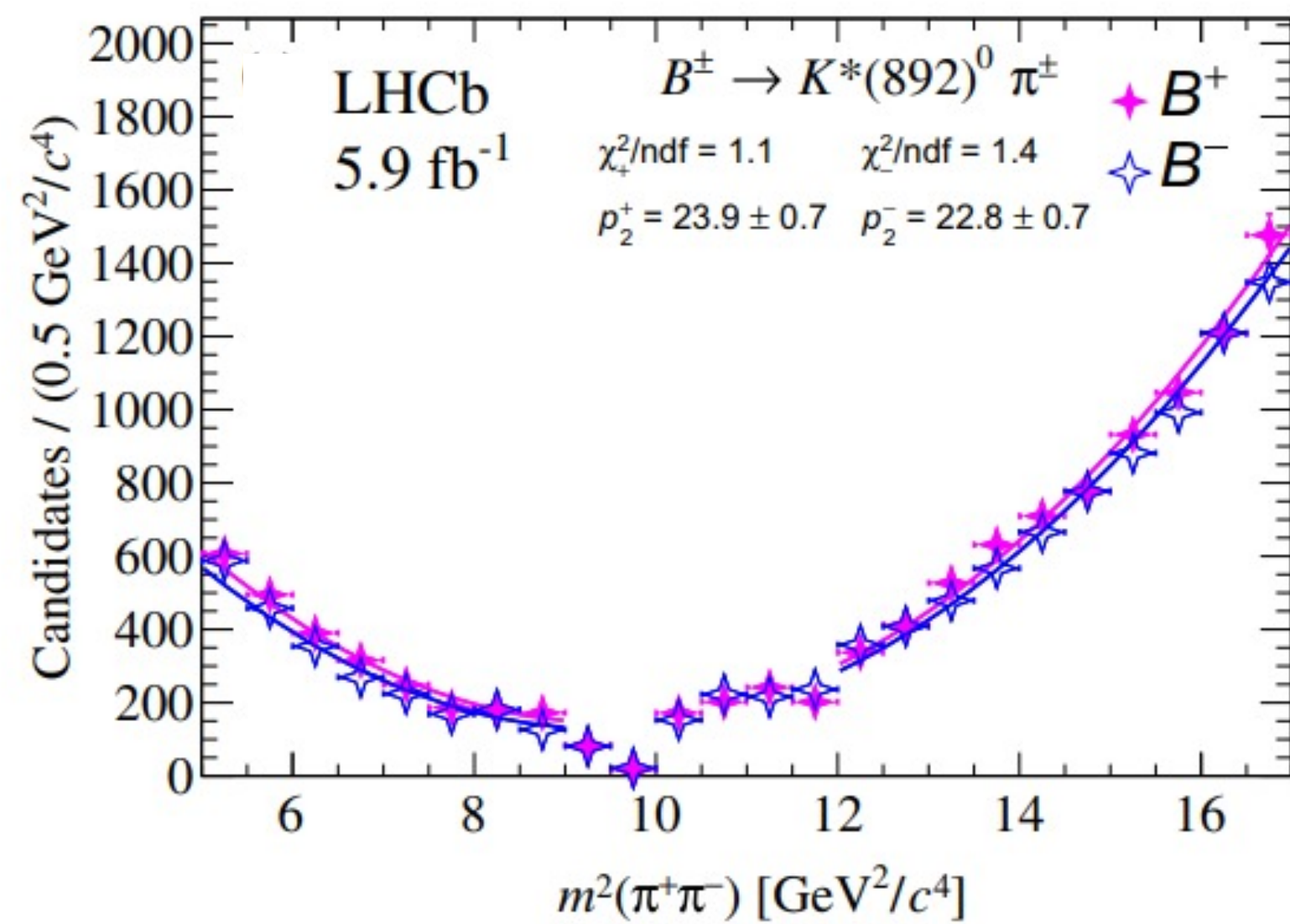
☑ $A_{CP} = (+0.7 \pm 1.1 \pm 1.6) \%$



Selected region
 $0.49 < m_{\pi^+\pi^-(low)}^2 < 0.72$
 $5 < m_{\pi^+\pi^-(high)}^2 < 21$

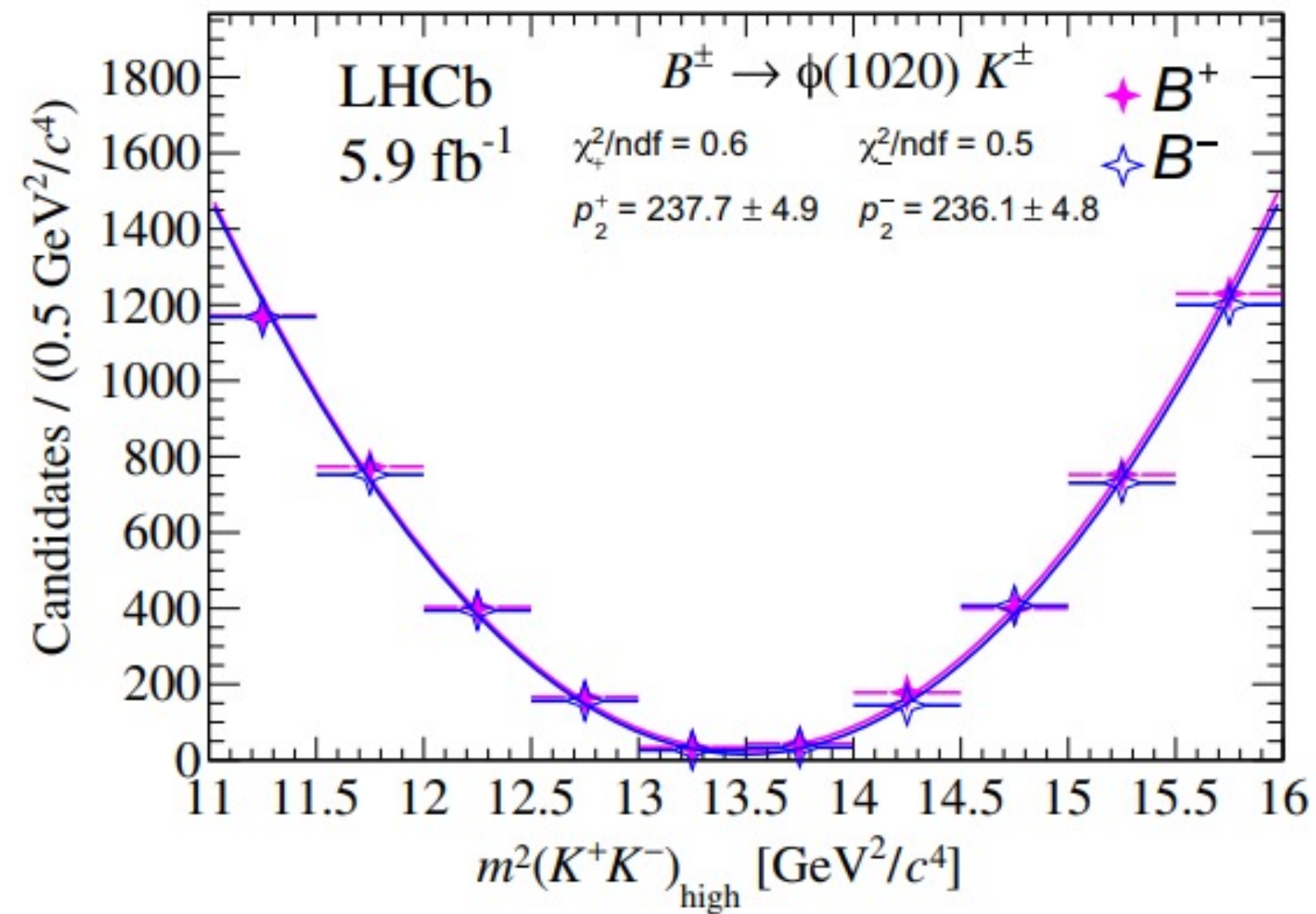


$$B^\pm \rightarrow K^*(892)^0 \pi^\pm$$



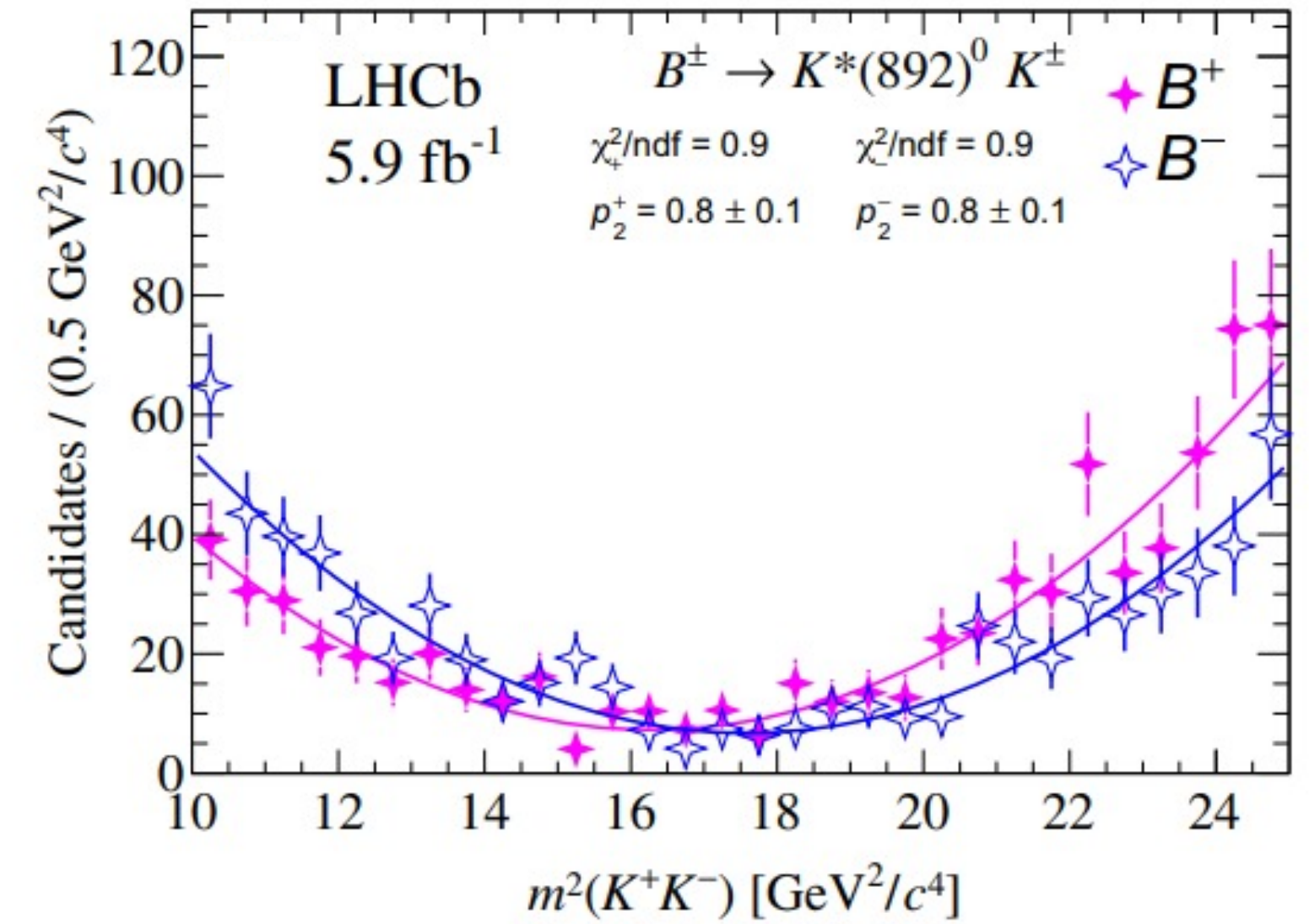
$$A_{CP} = (-1.5 \pm 2.1_{stat} \pm 1.2_{syst}) \%$$

$$B^\pm \rightarrow \phi(1020) K^\pm$$



$$A_{CP} = (+0.4 \pm 1.4_{stat} \pm 0.7_{syst}) \%$$

$$B^\pm \rightarrow K^*(892)^0 K^\pm$$



$$A_{CP} = (+0.7 \pm 5.4_{stat} \pm 3.2_{syst}) \%$$

[PRD.108.012013\(2023\)](#)

$B^\pm \rightarrow K^\pm \pi^+ \pi^-$

- Asymmetry in the region dominated by $B^\pm \rightarrow \rho(770)K^\pm$ decays for the **first time**

observed

- Large scalar contribution from $f_0(980)$

- Large A_{CP} probably from FSI

Babar results: [Phys. Rev. D78 \(2008\) 012004](#)

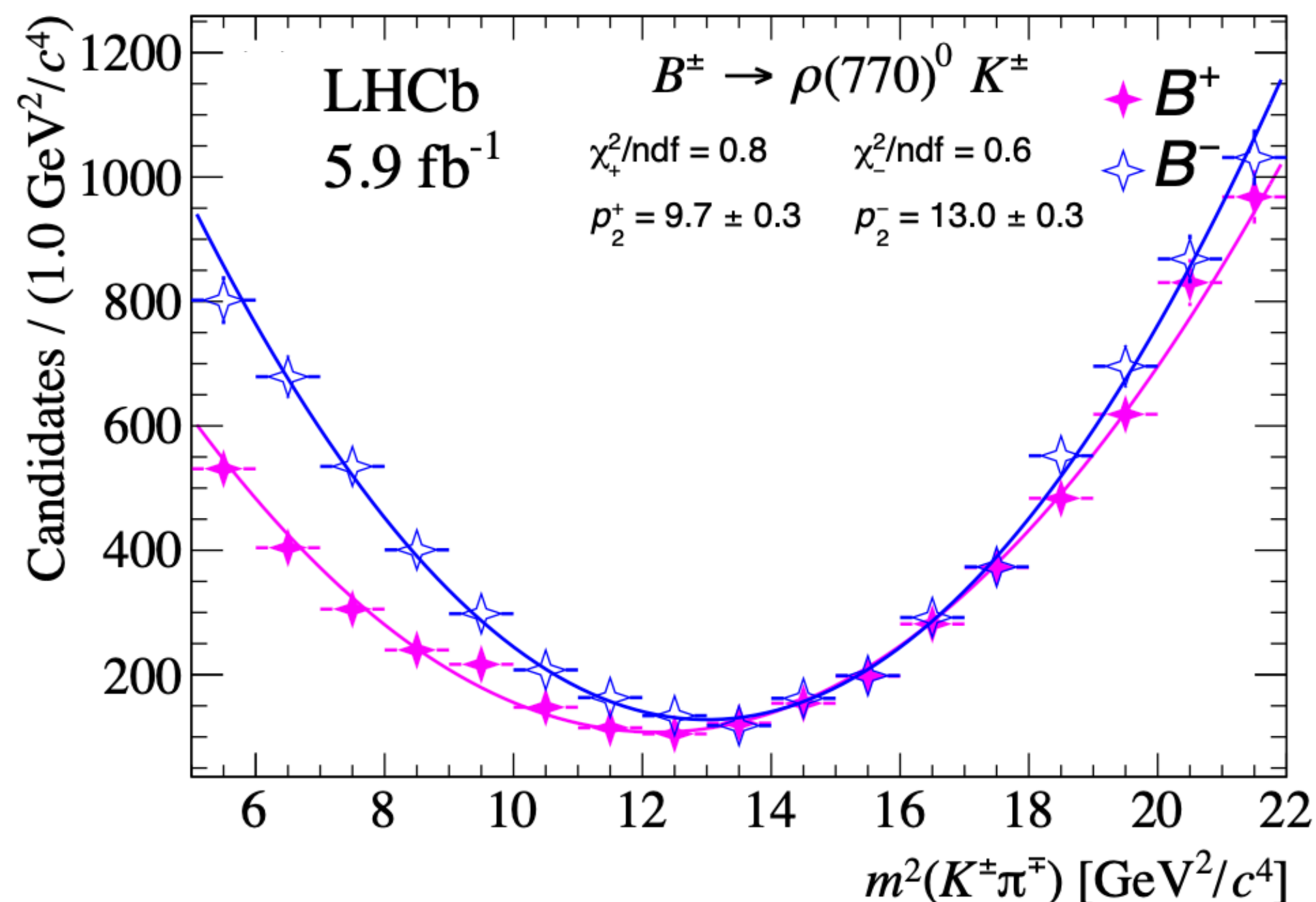
$A_{CP} = (44 \pm 10 \pm 4^{+5}_{-13})\%$ $\leftarrow 3.7\sigma$

Belle results: [Phys. Rev. Lett. 96 \(2006\) 251803](#)

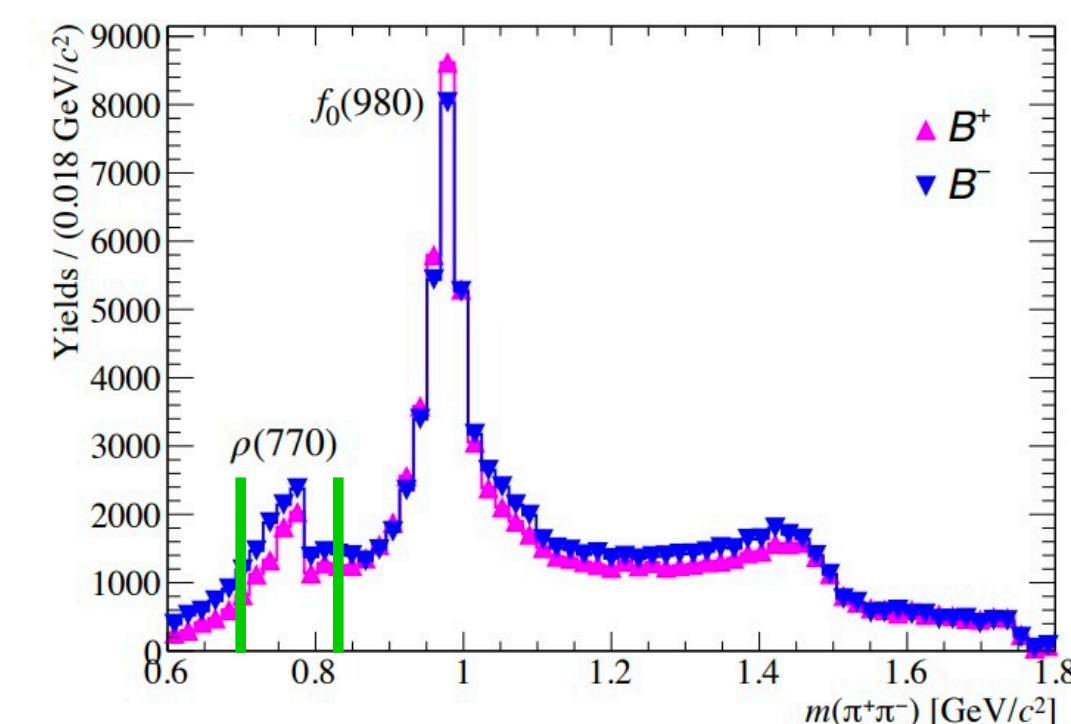
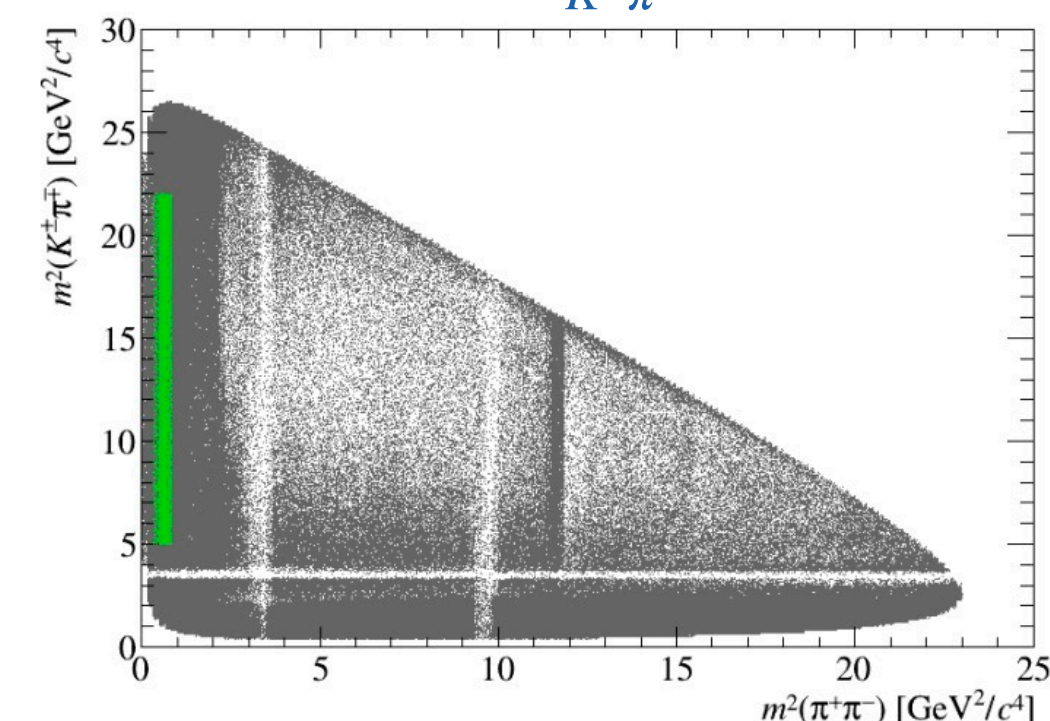
$A_{CP} = (30 \pm 11 \pm 2^{+11}_{-4})\%$ $\leftarrow 3.9\sigma$

$A_{CP} = (+15.0 \pm 1.9_{stat} \pm 1.1_{syst})\%$ $\leftarrow 7.9\sigma$

[PRD.108.012013\(2023\)](#)



Selected region
 $0.49 < m_{\pi^+\pi^-}^2 < 0.72$
 $5 < m_{K^+\pi^-}^2 < 22$



Final results for all channels:

Decay channel	This work	Previous measurements
$B^\pm \rightarrow (\rho(770)^0 \rightarrow \pi^+ \pi^-) \pi^\pm$	$-0.004 \pm 0.017 \pm 0.009$	$+0.007 \pm 0.011 \pm 0.016$ (LHCb)
$B^\pm \rightarrow (\rho(770)^0 \rightarrow \pi^+ \pi^-) K^\pm$	$+0.150 \pm 0.019 \pm 0.011$	$+0.44 \pm 0.10 \pm 0.04$ (BABAR) $+0.30 \pm 0.11 \pm 0.02$ (Belle)
$B^\pm \rightarrow (K^*(892)^0 \rightarrow K^\pm \pi^\mp) \pi^\pm$	$-0.015 \pm 0.021 \pm 0.012$	$+0.032 \pm 0.052 \pm 0.011$ (BABAR) $-0.149 \pm 0.064 \pm 0.020$ (Belle)
$B^\pm \rightarrow (K^*(892)^0 \rightarrow K^\pm \pi^\mp) K^\pm$	$+0.007 \pm 0.054 \pm 0.032$	$+0.123 \pm 0.087 \pm 0.045$ (LHCb)
$B^\pm \rightarrow (\phi(1020) \rightarrow K^+ K^-) K^\pm$	$+0.004 \pm 0.014 \pm 0.007$	$+0.128 \pm 0.044 \pm 0.013$ (BABAR)

$$B^{\pm} \rightarrow h^{\pm} h^{+} h^{-}$$

- 📌 Measurements of CP asymmetries in charmless three-body:
 - ☑ $B^{\pm} \rightarrow \pi^{\pm} \pi^{+} \pi^{-}$ (First Observation)
 - ☑ $B^{\pm} \rightarrow K^{\pm} K^{+} K^{-}$ (First Observation)
 - ☑ $B^{\pm} \rightarrow \pi^{\pm} K^{+} K^{-}$ (Confirmation)
 - ☑ $B^{\pm} \rightarrow K^{\pm} \pi^{+} \pi^{-}$ (No asymmetry)
- 📌 The phase space reveals non-uniform asymmetries
- 📌 Indication of CP violation involving the $\pi\pi \leftrightarrow KK$ rescattering
- 📌 Indication of CP violation involving the $\chi_{c0}(1P)$ resonance

$$B \rightarrow PV$$

- 📌 Measurements of CP asymmetries in $B \rightarrow PV$:
 - ☑ New method to measure CPV
 - ☑ $B^{\pm} \rightarrow \rho(770) K^{\pm}$ (First Observation)
 - ☑ All other channels (No asymmetry)

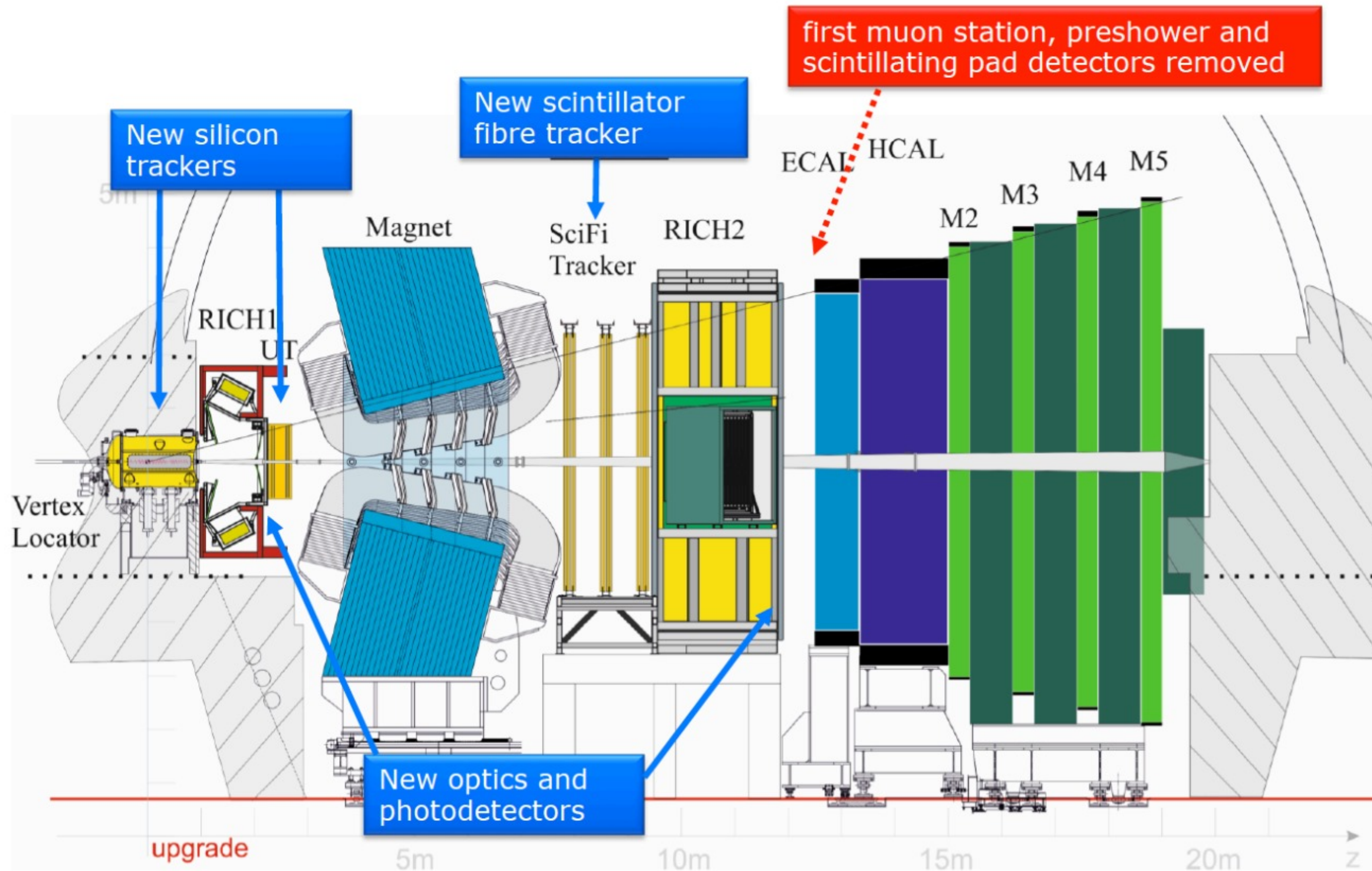


Gracias!!!

Thank you!!!

Obrigado!!!

Backup



Trigger requirements

Hardware trigger

- ✓ The event is selected if the transverse energy is larger than 3.5 GeV for at least one hadron from the $B^\pm \rightarrow h^\pm h^+ h^-$

Software trigger

- ✓ Requires a two-, three- or four-track vertex with a significant displacement from any PV

Stripping requirements

Variables	Selection cuts
Tracks P_T	$> 0.1 \text{ GeV}/c$
Tracks P	$> 1.5 \text{ GeV}/c$
Tracks $IP\chi^2$	> 1
Tracks $\chi^2/\text{n.d.f.}$	< 3
Tracks GhostProb	< 0.5
Sum of P_T of tracks	$> 4.5 \text{ GeV}/c$
Sum of P of tracks	$> 20. \text{ GeV}/c$
Sum of $IP\chi^2$ of tracks	> 500
P_T of the highest- P_T track	$> 1.5 \text{ GeV}/c$
Maximum DOCA	$< 0.2 \text{ mm}$
B^\pm candidate M_{KKKK}	$5.05 - 6.30 \text{ GeV}/c^2$
B^\pm candidate M_{KKKK}^{COR}	$4 - 7 \text{ GeV}/c^2$
B^\pm candidate $IP \chi^2$	< 10
B^\pm candidate P_T	$> 1. \text{ GeV}/c$
Distance from SV to any PV	$> 3 \text{ mm}$
Secondary Vertex χ^2	< 12
B^\pm candidate $\cos(\theta)$	> 0.99998
B^\pm Flight Distance χ^2	> 500

$$B^{\pm} \rightarrow h^{\pm} h^{+} h^{-}$$

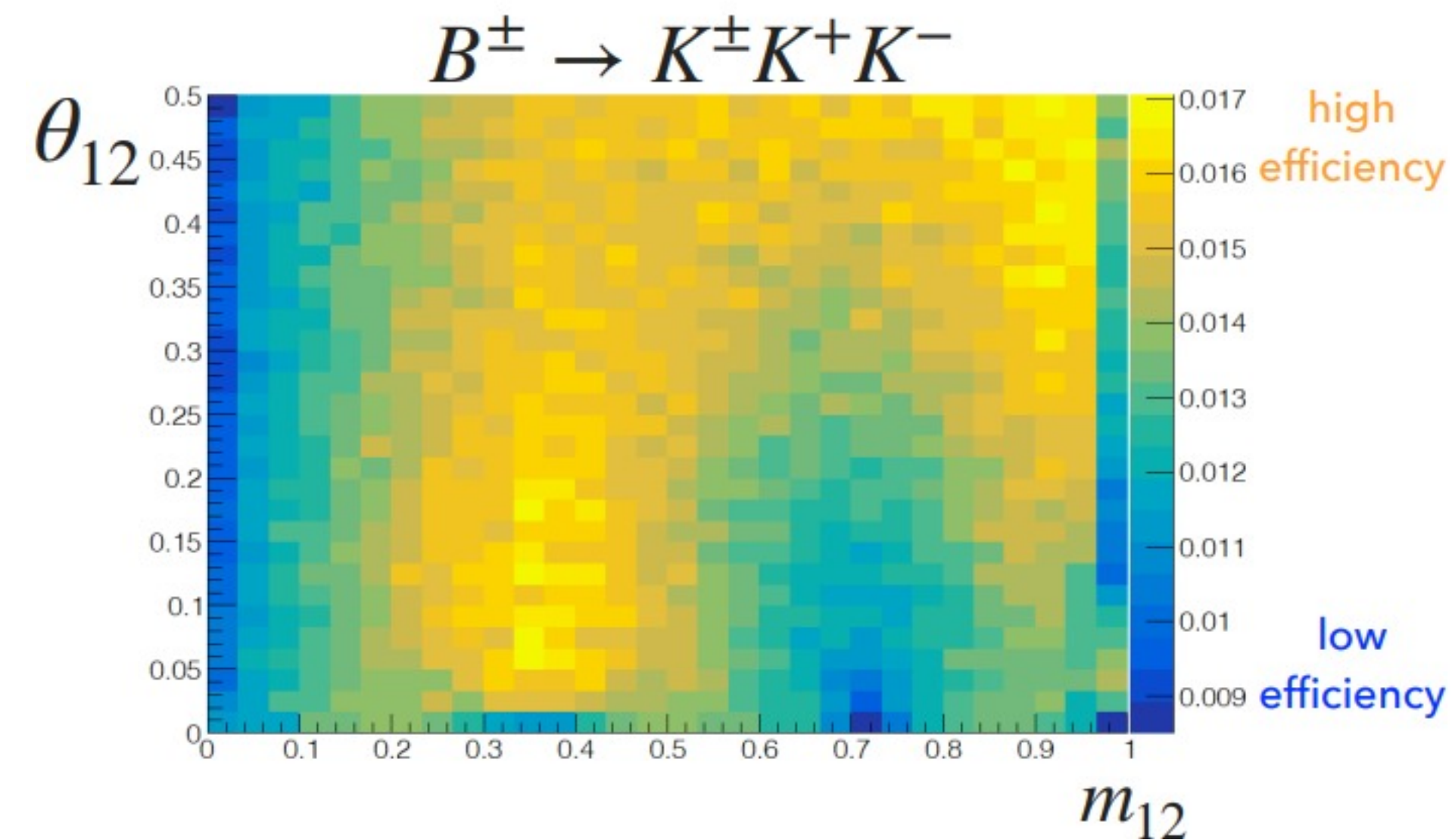
- 📌 Divided into three groups
 - ☑️ Potential mismodelling of the invariant mass distribution
 - ☑️ Phase-space efficiency corrections
 - ☑️ Production asymmetry

Source of uncertainty	$K^{\pm}\pi^{+}\pi^{-}$	$K^{\pm}K^{+}K^{-}$	$\pi^{\pm}\pi^{+}\pi^{-}$	$\pi^{\pm}K^{+}K^{-}$
Signal model	0.0004	0.0007	0.0000	0.0001
Peaking background fraction	0.0005	0.0010	0.0002	0.0004
Peaking background asymmetry	0.0022	0.0001	0.0005	0.0007
Combinatorial model	0.0002	0.0005	0.0015	0.0025
Efficiency correction	0.0014	0.0016	0.0018	0.0019
Production asymmetry	0.0011	0.0011	0.0011	0.0011
Total	0.0029	0.0024	0.0027	0.0035

$$B \rightarrow PV$$

- 📌 Divided into three groups
 - ☑️ Variation of fit regions
 - ☑️ Variations of resonance mass window
 - ☑️ Change of the projected variable

- 📌 The acceptance maps are generated by data weighted Monte Carlo subsamples of:
 - ☑️ Year: The acceptance maps are separated by year to account for differences between the periods of data taking.
 - ☑️ Polarity: Separated by each magnet polarity to take into account the left-right asymmetry of the detector.
 - ☑️ Trigger configuration: Subsamples of TOS and TISnotTOS to account for possible differences between data and MC with respect to the L0Hadron_TOS efficiency.
 - ☑️ Charge: Separated by B^+ and B^- candidates



- 📌 PID corrections performed using the PIDCalib package using bands of kinematic variables

Relation between CPV of the different decay modes

Based on U-spin symmetry

$$\Delta\Gamma(B^\pm \rightarrow \pi^\pm \pi^+ \pi^-) = -\Delta\Gamma(B^\pm \rightarrow K^\pm K^+ K^-)$$

$$\Delta\Gamma(B^\pm \rightarrow \pi^\pm K^+ K^-) = -\Delta\Gamma(B^\pm \rightarrow K^\pm \pi^+ \pi^-)$$

The above relations can be rewritten like:

$$\Delta\Gamma(B^\pm \rightarrow \pi^\pm K^+ K^-) = \frac{A_{CP}(B^\pm \rightarrow \pi^\pm K^+ K^-)\mathcal{B}(B^\pm \rightarrow \pi^\pm K^+ K^-)}{\tau(B^\pm)}$$

Using the measures values of the integrated asymmetry

$$\frac{A_{CP}(B^\pm \rightarrow \pi^\pm K^+ K^-)\mathcal{B}(B^\pm \rightarrow \pi^\pm K^+ K^-)}{A_{CP}(B^\pm \rightarrow K^\pm \pi^+ \pi^-)\mathcal{B}(B^\pm \rightarrow K^\pm \pi^+ \pi^-)} = -0.92 \pm 0.18$$

$$\frac{A_{CP}(B^\pm \rightarrow \pi^\pm \pi^+ \pi^-)\mathcal{B}(B^\pm \rightarrow \pi^\pm \pi^+ \pi^-)}{A_{CP}(B^\pm \rightarrow K^\pm K^+ K^-)\mathcal{B}(B^\pm \rightarrow K^\pm K^+ K^-)} = -1.06 \pm 0.08$$



Both results are consistent with -1 as predicted by the U-spin symmetry