



Input for γ measurements from BESIII

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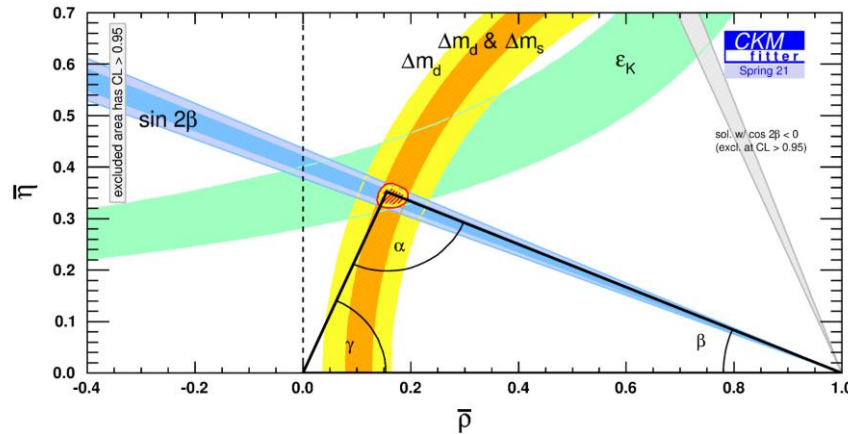
Outline

- ❖ Introduction
- ❖ Method to measure γ
- ❖ Recent strong parameters from BESIII
- ❖ Future prospect of γ
- ❖ Summary

Why measure γ

$$V_{\text{CKM}} = \begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix} \longrightarrow \gamma = \arg \left(-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \right)$$

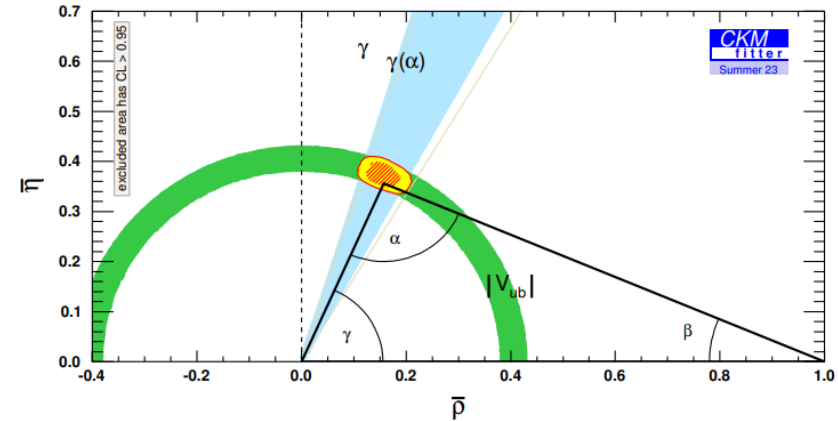
Indirect measurement



- Extrapolate γ from measurement of α and β
- Measured using loop-level decays: sensitivity to NP
- CKMFitter latest: $\gamma = (66.3^{+0.7}_{-1.9})^\circ$

Disagreement = New Physics!

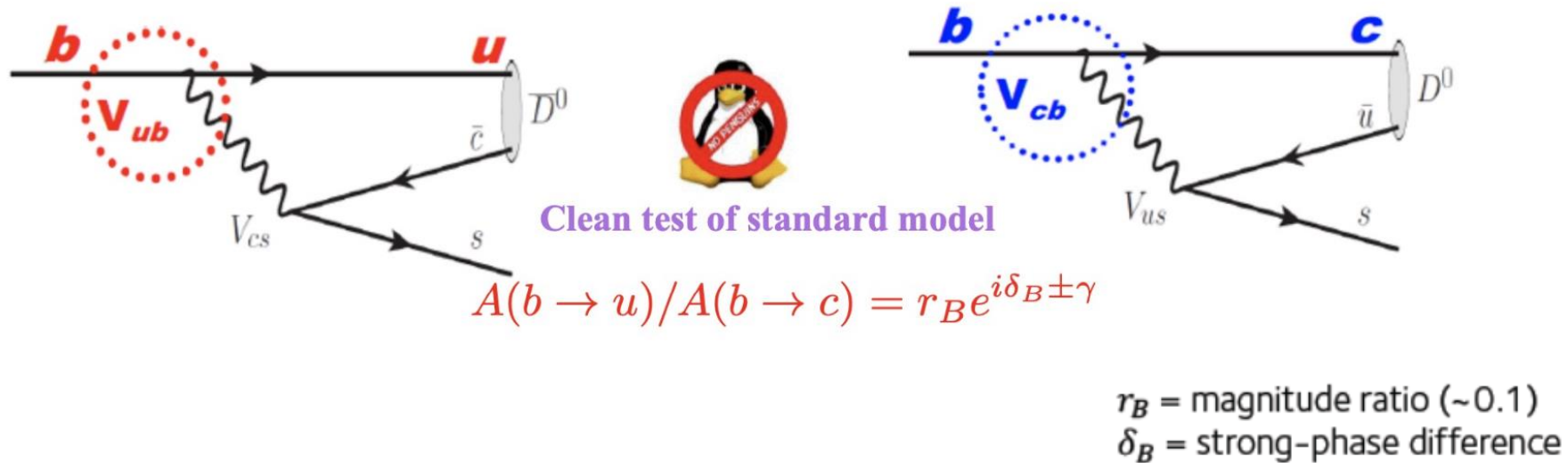
Direct measurement



- Measure γ directly using tree-level decays
- Theoretically clean ($\delta\gamma/\gamma < 10^{-7}$)
[[JHEP 1401\(2014\)051](#)]
- HFLAV latest: $\gamma = (65.9^{+3.3}_{-3.5})^\circ$
- LHCb dominated: $\gamma = (63.8^{+3.5}_{-3.7})^\circ$
[[LHCb-CONF-2022-003](#)]

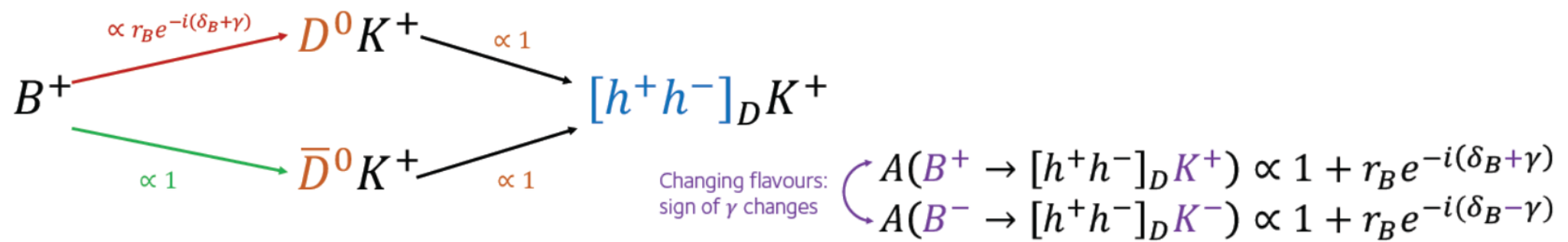
How to measure γ directly

- ❖ **Interference** between favoured $b \rightarrow c$ and suppressed $b \rightarrow u$ decay amplitude
- ❖ Ideal decays: $B \rightarrow DK$ (clean background, large branching fraction)



GLW method [1,2]

- ❖ D CP-even final states such as $D \rightarrow K^+K^-, \pi^+\pi^-, \pi^+\pi^-\pi^0 \dots$



- ❖ Use the yields of B+ and B- to construct observables related to γ

$$A^f = \frac{N(B^- \rightarrow f_D K^-) - N(B^+ \rightarrow f_D K^+)}{N(B^- \rightarrow f_D K^-) + N(B^+ \rightarrow f_D K^+)} = \frac{2\kappa r_B \sin\delta_B \sin\gamma}{R^f}$$

$$R^f = \frac{N(B^- \rightarrow f_D K^-) + N(B^+ \rightarrow f_D K^+)}{N(B^- \rightarrow [K\pi]_D K^-) + N(B^+ \rightarrow [K\pi]_D K^+)} = 1 + r_B^2 + 2\kappa r_B \cos\delta_B \cos\gamma$$

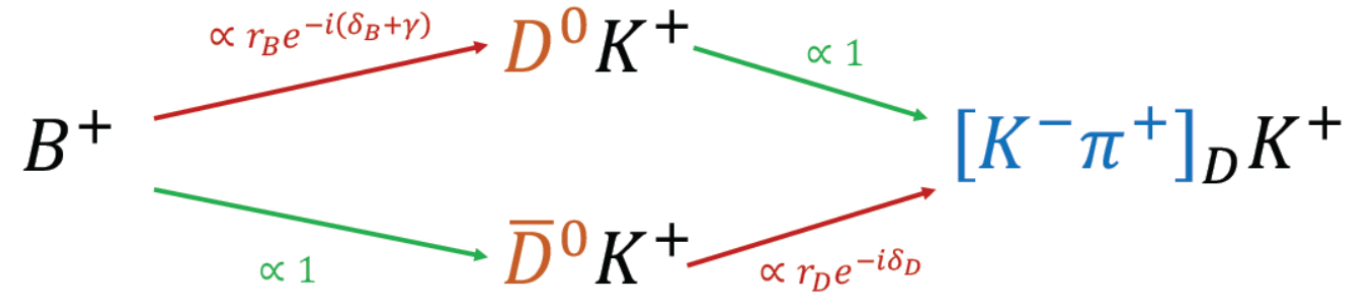
insert a factor of $(\kappa=2F_+-1)$ before interference terms ($F_+=$ CP even content), need charm input

Notice r_B/δ_B need input

[1] M. Gronau and D. Wyler, Phys. Lett. B265 (1991) 172
 [2] M. Gronau and D. London, Phys. Lett. B253 (1991) 483

ADS method^[1,2]

- ❖ Consider the Cabibbo-favored decay $D^0 \rightarrow K^- \pi^+$ and doubly-Cabibbo-suppressed decay $D^0 \rightarrow K^+ \pi^-$



- ❖ r_B/δ_B can be obtained directly, but external input r_D/δ_D

$$\Gamma(B^\pm \rightarrow f_D K^\pm) \propto r_B^2 + r_D^2 + 2R_f r_B r_D \cos(\delta_B + \delta_D \pm \gamma)$$

$$\Gamma(B^\pm \rightarrow \bar{f}_D K^\pm) \propto 1 + r_B^2 r_D^2 + 2R_f r_B r_D \cos(\delta_B - \delta_D \pm \gamma)$$

Need inputs from charm factory

$$R_{K3\pi} e^{-i\delta_{K3\pi}} = \frac{\int A_{K^-3\pi}(x) A_{K^+3\pi}(x) dx}{A_{K^-3\pi}(x) A_{K^+3\pi}(x)}$$

- For $K3\pi$ mode, coherence factor $R_{K3\pi}$ and $\delta_{K3\pi}$ averaged over phase space not good for whole space

[1] D. Atwood, I. Dunietz, and A. Soni, Phys. Rev. Lett. 78 (1997) 3257

[2] D. Atwood, I. Dunietz, and A. Soni, Phys. Rev. D63 (2001) 036005

Dalitz method^[1]

- ❖ Golden mode: $D \rightarrow K_S \pi \pi / K_S K K$ (large statistic, large r_D)
 - Model-dependent method (not used now)
 - Model-independent binned method (BPGGSZ method^[1])
- ❖ Binned Dalitz plane according to δ_D , measure B^\pm yields in each bins
 - Sensitivity from **phase-space distribution**, not overall asymmetries \rightarrow not impacted by production/detection asymmetries
 - LHCb latest $K_S h h$ result: $\gamma = (68.7_{-5.1}^{+5.2})^\circ$ (uncertainty $\sim 1^\circ$ from BESIII input)

$$r_B \exp[i(\delta_B \pm \gamma)] = x_\pm + iy_\pm$$

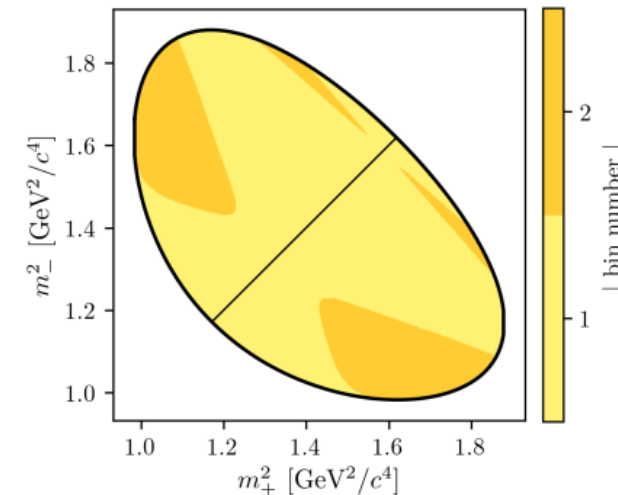
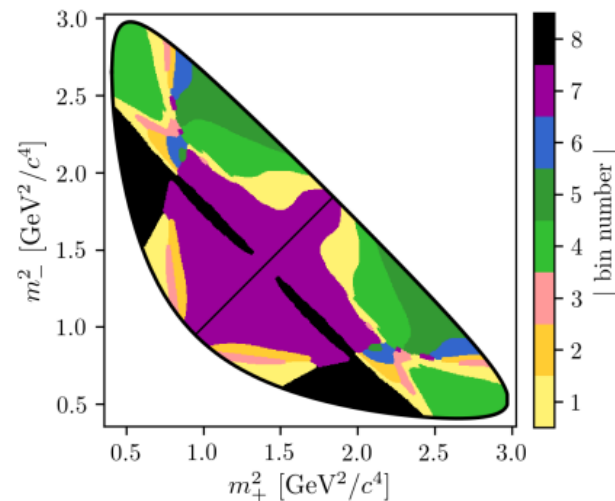
$$N_{\pm i}^- \propto F_{\pm i} + (x_\pm^2 + y_\pm^2) F_{\mp i} + 2\sqrt{F_i F_{-i}} (x_\pm c_{\pm i} \mp y_\pm s_{\pm i})$$

F_i : Fractional yield of flavour tagged D^0 into bin i

Measured in control channel:
 $\bar{B}^0 \rightarrow D^{*+} \mu^- \nu_\mu X$

c_i/s_i : Strong phase difference of $D^0 - \bar{D}^0$ decays

External input from BESIII and CLEO-c



Quantum correlated $D\bar{D}$ measurement

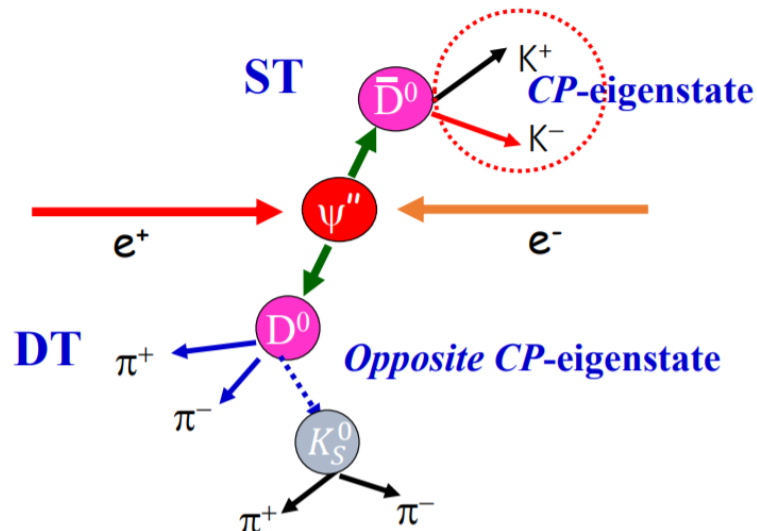
- ❖ $\psi(3770)$ is a spin -1 states, therefore the amplitude of $\psi(3770) \rightarrow D\bar{D}$:

$$(|D^0\rangle|\bar{D}^0\rangle - |\bar{D}^0\rangle|D^0\rangle)/\sqrt{2} \quad [\text{anti-symmetric wave function}]$$

The amplitude for two D mesons to decay to states F and G is [D. Atwood and A. Soni, PRD68, 033003 (2003)]:

$$\Gamma(F|G) = \Gamma_0 [A_F^2 \bar{A}_G^2 + \bar{A}_F^2 A_G^2 - 2R_F R_G A_F \bar{A}_F A_G \bar{A}_G \cos[\delta_D^F - \delta_D^G]]$$

The coherence factor κ_F and the strong phase difference δ_D can be extracted



The DT mode K^+K^- vs. $K_S^0\pi^+\pi^-$ is selected as an example.

- ✓ Single tag (ST) samples: decay products of only one D meson are reconstructed
- ✓ Double tag (DT) samples: decay products of both D mesons are reconstructed
- ✓ Some typical reconstructed D decay modes

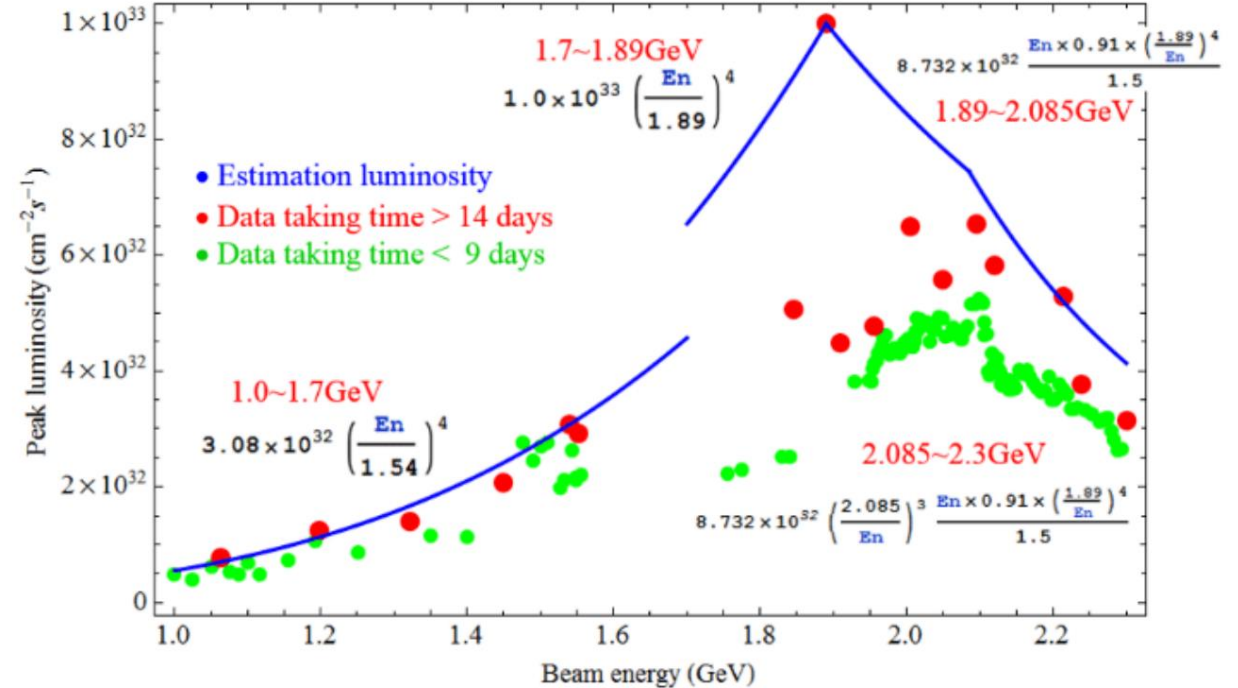
Tag group	
Flavor	$K^+\pi^-, K^+\pi^-\pi^0, K^+\pi^-\pi^-\pi^+, K^+e^-\bar{\nu}_e$
CP-even	$K^+K^-, \pi^+\pi^-, K_S^0\pi^0\pi^0, K_L^0\pi^0, \pi^+\pi^-\pi^0$
CP-odd	$K_S^0\pi^0, K_S^0\eta, K_S^0\omega, K_S^0\eta', K_L^0\pi^0\pi^0$
Mixed-CP	$K_S^0\pi^+\pi^-$

The BESIII experiment

Key datasets for charm physics:

- 2010-2011: 2.9 fb^{-1} at $\psi(3770)$
- 2013-2019: 7.3 fb^{-1} of $D_s \bar{D}_s^*$
- 2020: 4.5 fb^{-1} of $\Lambda_c^+ \bar{\Lambda}_c^-$
- 2021-2022: 5.0 fb^{-1} at $\psi(3770)$
- 2022-: $\sim 8 \text{ fb}^{-1}$ at $\psi(3770)$

7.9 fb^{-1} $\psi(3770)$ data is ready for physics
 20 fb^{-1} $\psi(3770)$ data will be obtained in 2024



BEPCII peak luminosity.

Threshold produced $\psi(3770) \rightarrow D \bar{D}$ provide a unique access to strong parameters information for γ measurement at LHCb/BelleII

Results in this talk

- ❖ Update measurement of $\delta_{K\pi}$ [EPJC 82 1009 \(2022\)](#)
- ❖ $D \rightarrow K^- \pi^+ \pi^- \pi^+ / K^- \pi^+ \pi^0$ strong parameters measurement [JHEP 5\(2021\)164](#)
- ❖ $D \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ F+ measurement [PRD 106 \(2022\) 092004](#)
- ❖ $D \rightarrow K^+ K^- \pi^+ \pi^-$ F+ measurement [PRD 107 \(2023\) 032009](#)
- ❖ $D \rightarrow K_S \pi^+ \pi^- \pi^0$ F+ measurement [PRD 108 \(2023\) 032003](#)

Update measurement of $\delta_{K\pi}$

EPJC 82 (2022)1009

- ❖ Based on 2.9 fb⁻¹ data
- ❖ More modes are used comparing to previous work ([PLB 734 \(2014\) 227](#))
 - D→K_LX included (statistics improved a lot) →Independent determinations their BRS
 - D→K_S/K_Lππ included
- ❖ Asymmetry between CP-odd and CP-even eigenstate decays to Kπ: $\mathcal{A}_{K\pi} = \frac{-2r_D^{K\pi} \cos(\delta_{K\pi}) + y}{1 + (r_D^{K\pi})^2}$
- ❖ D→K_S/K_Lππ in bins: $Y_i \propto \left(K_i + (r_D^{K\pi})^2 K_{-i} - 2r_D^{K\pi} \sqrt{K_i K_{-i}} \left[c_i \cos(\delta_D^{K\pi}) - s_i \sin(\delta_D^{K\pi}) \right] \right)$

- ❖ Combine these modes:

$$\delta_D^{K\pi} = (187.6^{+8.9+5.4}_{-9.7-6.4})^\circ$$

Used in latest LHCb γ fit (LHCb-CONF-2022-003)

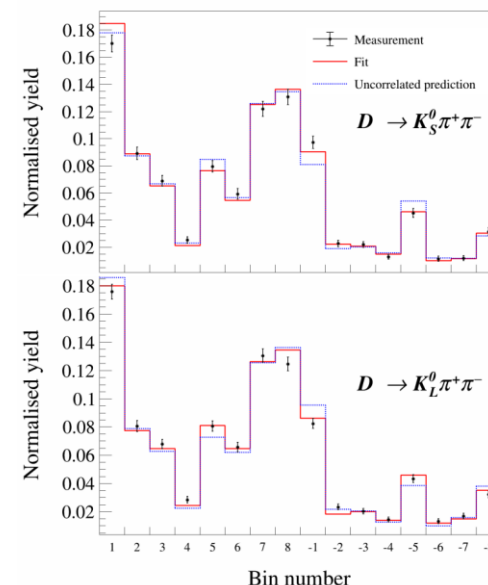
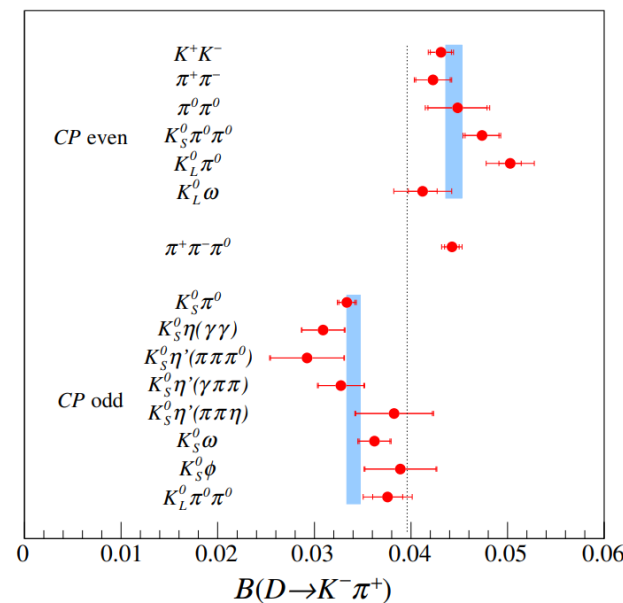
- ❖ Also BRs:

$$\mathcal{B}(D^0 \rightarrow K_L^0 \pi^0) = (0.97 \pm 0.03 \pm 0.02) \times 10^{-2}$$

$$\mathcal{B}(D^0 \rightarrow K_L^0 \omega) = (1.09 \pm 0.06 \pm 0.03) \times 10^{-2}$$

$$\mathcal{B}(D^0 \rightarrow K_L^0 \pi^0 \pi^0) = (1.26 \pm 0.05 \pm 0.03) \times 10^{-2}$$

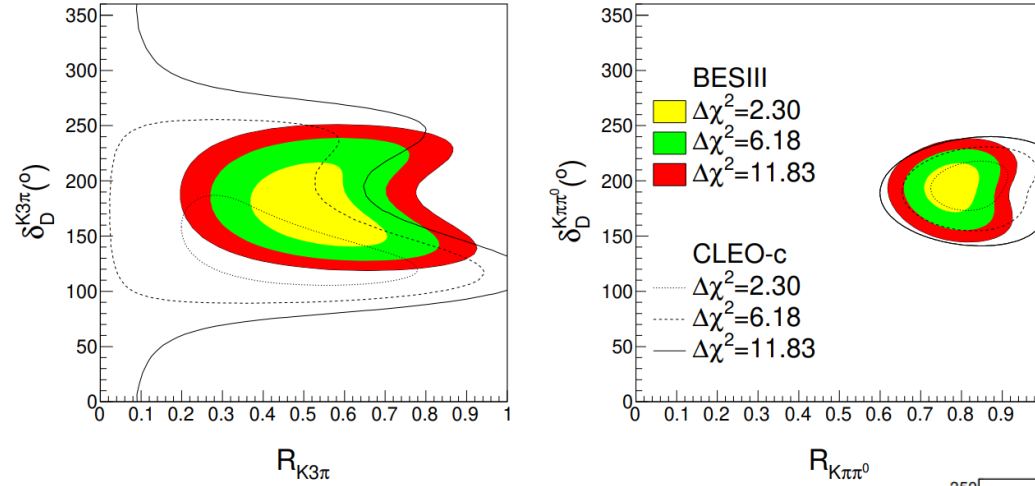
- ❖ Analysis with 8fb⁻¹ data is ongoing



$D \rightarrow K \pi^+ \pi^- \pi^+ / K \pi^+ \pi^0$ strong parameters measurement

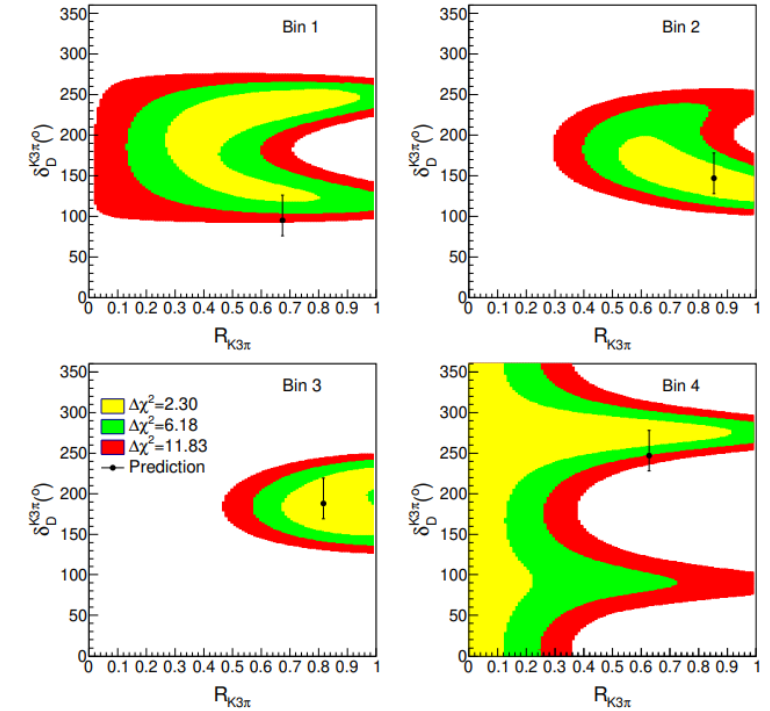
JHEP 5(2021)164

- ❖ Based on 2.9 fb⁻¹ data
- ❖ Similar analysis strategy
 - CP tags
 - $D \rightarrow K_S / K_L \pi \pi$ included

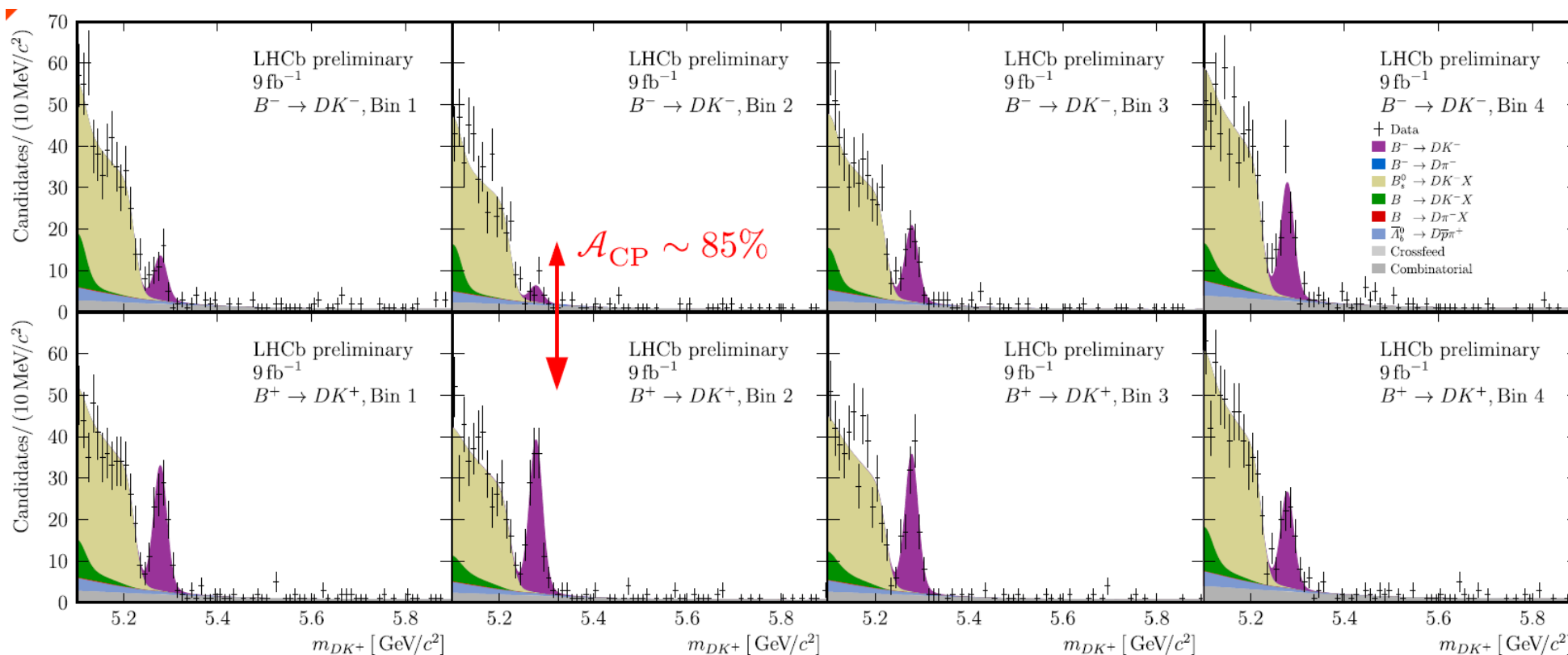


- ❖ A binning scheme for $\delta_{K3\pi}$ ([PLB 802\(2020\)135188](#))
- ❖ Obtain corresponding $\delta_{K3\pi}$ and $R_{K3\pi}$

Parameter	Global fit	Binned fit			
		Bin 1	Bin 2	Bin 3	Bin 4
$R_{K3\pi}$	$0.52^{+0.12}_{-0.10}$	$0.58^{+0.25}_{-0.33}$	$0.78^{+0.50}_{-0.21}$	$0.85^{+0.15}_{-0.12}$	$0.45^{+0.33}_{-0.37}$
$\delta_D^{K3\pi}$	$(167^{+31}_{-19})^\circ$	$(131^{+124}_{-16})^\circ$	$(150^{+37}_{-39})^\circ$	$(176^{+57}_{-21})^\circ$	$(274^{+19}_{-30})^\circ$
$r_D^{K3\pi} (\times 10^{-2})$	5.46 ± 0.09	$5.44^{+0.45}_{-0.14}$	$5.80^{+0.14}_{-0.13}$	$5.75^{+0.41}_{-0.14}$	$5.09^{+0.14}_{-0.14}$
$R_{K\pi\pi^0}$	0.78 ± 0.04		0.80 ± 0.04		
$\delta_D^{K\pi\pi^0}$	$(196^{+14}_{-15})^\circ$		$(200 \pm 11)^\circ$		
$r_D^{K\pi\pi^0} (\times 10^{-2})$	4.40 ± 0.11		4.41 ± 0.11		



❖ Large CPV observed in local bins!



$$\gamma = \left(54.8 \pm \begin{matrix} 6.0 \\ -5.8 \end{matrix} + 0.6 + 6.7 \right)^\circ$$

Comparable to golden mode!

Large expected improvement from incoming 20fb⁻¹ of BESIII $\psi(3770)$ data

$D \rightarrow \pi^+ \pi^- \pi^+ \pi^- F^+$ measurement

PRD 106 (2022) 092004

- ❖ Based on 2.9 fb^{-1} data
- ❖ $\text{Br}(\pi\pi\pi\pi) = (7.56 \pm 0.20) \times 10^{-3}$
- ❖ Similar analysis strategy as previous

- CP tags $\frac{N^{\text{DT}}}{N^{\text{ST}}} \propto 1 \mp (2F_+ - 1)$

- $K_S/K_L \pi\pi$ included

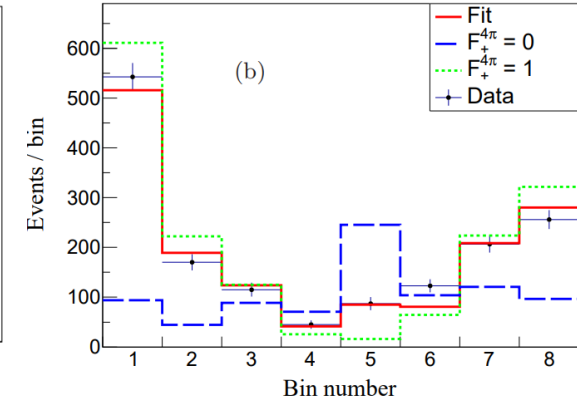
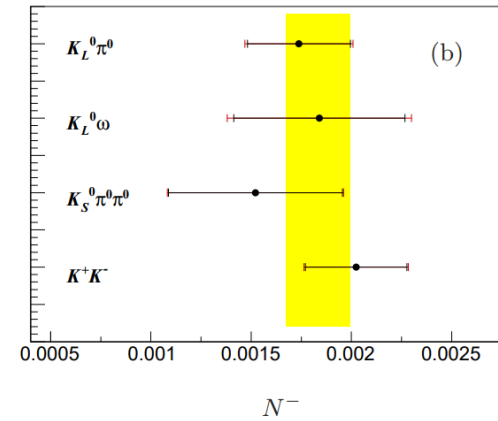
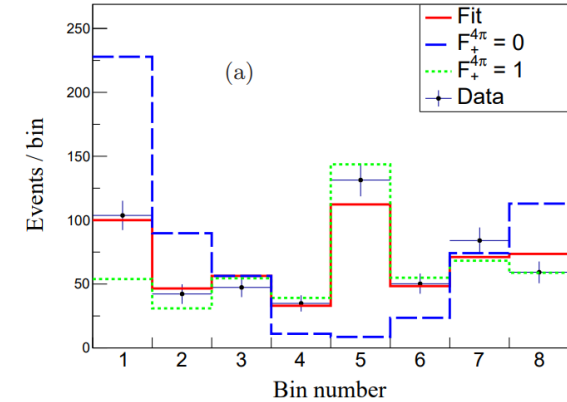
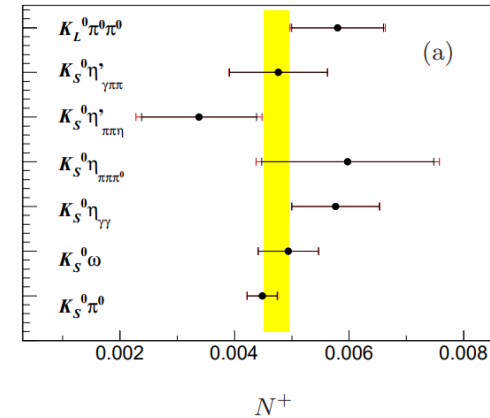
$$M_i = h \left[K_i + K_{-i} - 2c_i \sqrt{K_i K_{-i}} (2F_+ - 1) \right]$$

$$M'_i = h' \left[K'_i + K'_{-i} + 2c'_i \sqrt{K'_i K'_{-i}} (2F_+ - 1) \right]$$

- ❖ Combined: $F_+^{4\pi} = 0.735 \pm 0.015 \pm 0.005$,

- ❖ Consistent with previous results, but more precise

- ❖ This result is used for γ measurement in LHCb



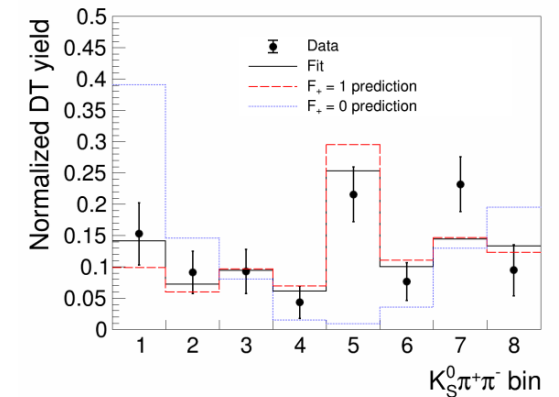
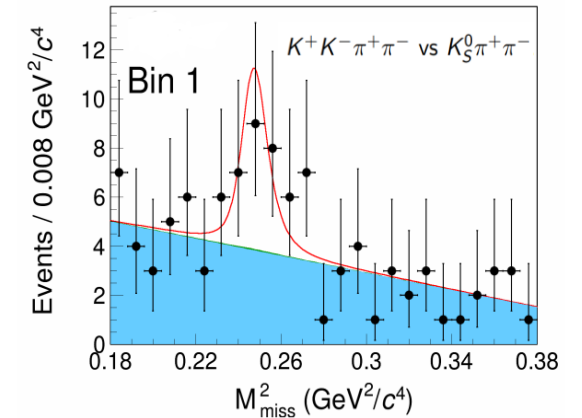
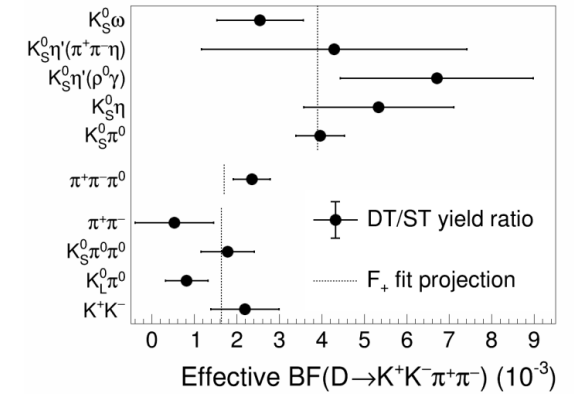
Tag modes	$F_+^{4\pi}$
CP eigenstates	$0.721 \pm 0.019 \pm 0.007$
$D \rightarrow \pi^+ \pi^- \pi^0$	$0.753 \pm 0.028 \pm 0.010$
$D \rightarrow K_{S,L}^0 \pi^+ \pi^-$	$0.754 \pm 0.031 \pm 0.009$
Combination	$0.735 \pm 0.015 \pm 0.005$

D → K⁺K⁻π⁺π⁻ F⁺ measurement

PRD 107 (2023) 032009

- ❖ Based on 2.9 fb⁻¹ data
- ❖ Br(KKππ) = (2.47 ± 0.11) × 10⁻³
- ❖ Similar analysis strategy as previous
- ❖ Partial reconstruction method to improve statistics
- ❖ Finally: $F_+ = 0.730 \pm 0.037 \pm 0.021$
- ❖ This result is used for γ measurement in LHCb

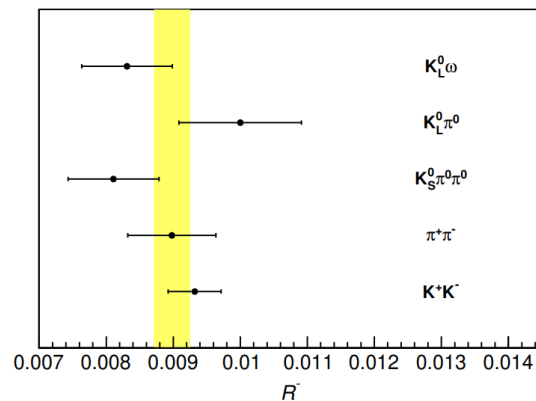
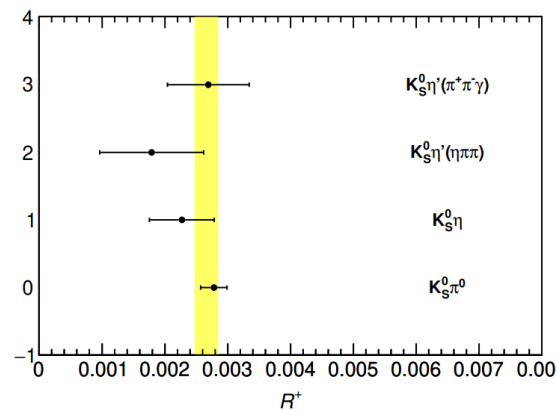
EPJC 83 (2023) 547



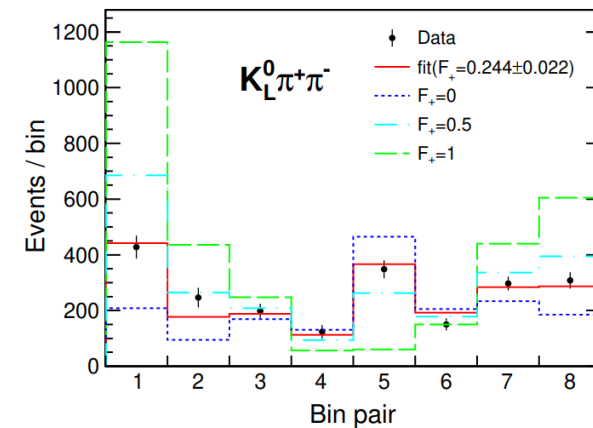
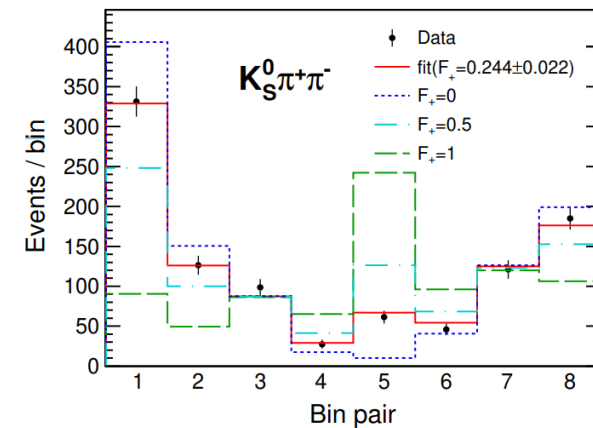
$D \rightarrow K_S \pi^+ \pi^- \pi^0$ F_+ measurement

- ❖ Based on 2.9 fb^{-1} data
- ❖ $\text{Br}(K_S \pi^+ \pi^- \pi^0) = (5.2 \pm 0.6)\%$
- ❖ Similar analysis strategy
- ❖ Consistent with CLEO-c's result, a factor 1.7 times more precise

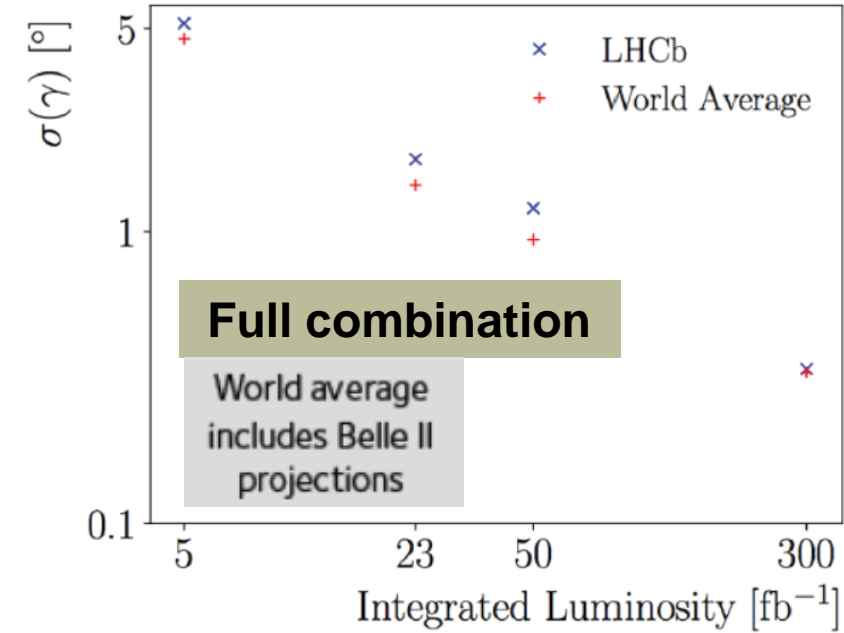
Method	F_+
CP -tag modes	$0.229 \pm 0.013 \pm 0.002$
$\pi^+ \pi^- \pi^0$ tag mode	$0.227 \pm 0.014 \pm 0.003$
$\pi^+ \pi^- \pi^+ \pi^-$ tag mode	$0.227 \pm 0.016 \pm 0.003$
Self-tag modes	$0.244 \pm 0.019 \pm 0.002$
$K_{S,L}^0 \pi^+ \pi^-$	$0.244 \pm 0.021 \pm 0.006$
Combined	$0.235 \pm 0.010 \pm 0.002$



PRD 108 (2023) 032003



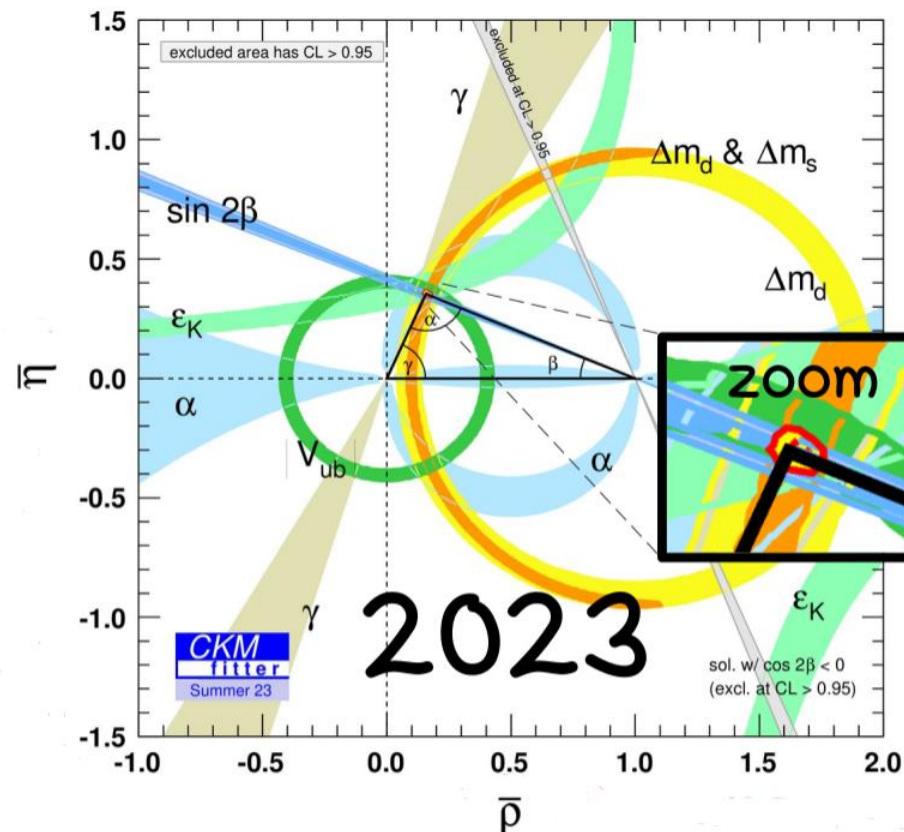
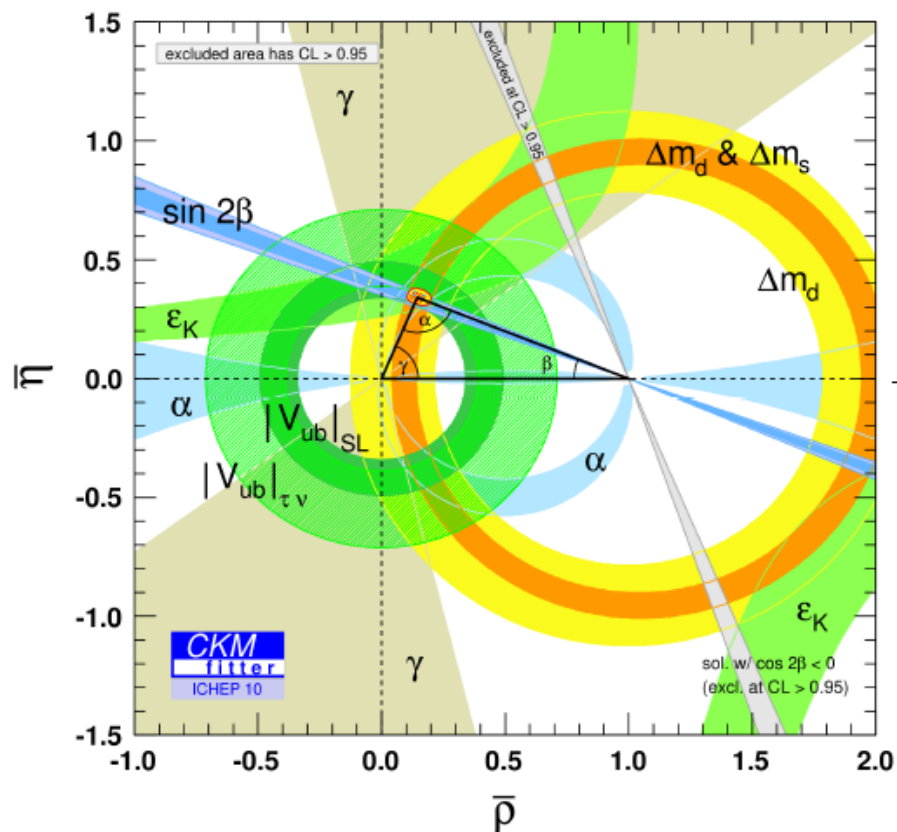
Future prospects for γ



- ❖ Status now:
 - Error for γ is about 4°
 - BESIII contribute about 1°
- ❖ Around 2030
 - Less than 1° will be achieved
 - BESIII 20fb^{-1} data \rightarrow improve the error to $<0.5^\circ$
- ❖ (>)2035
 - LHCb upgradell \rightarrow sensitivity $<0.4^\circ$
 - Need more charm factory data (STCF)

dataset	Int. Lum.	year	sensitivity
LHCb Run1 (7,8TeV)	3 fb^{-1}	2012	8°
LHCb Run2 (13TeV)	6 fb^{-1}	2018	4°
BelleII Run	50 ab^{-1}	2025	$1\text{-}2^\circ$
LHCb upgrade (14TeV)	50 fb^{-1}	2030	$<1^\circ$
LHCb upgradeII (14TeV)	200 fb^{-1}	(>)2035	$<0.4^\circ$

Summary

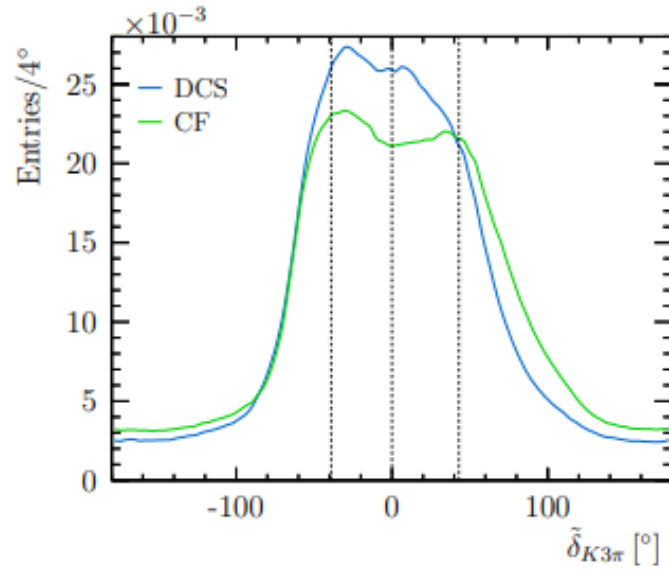


- ❖ 10 years of measurements have been game changing for flavor physics
- ❖ γ no longer the least precisely known of the weak phases!
- ❖ Now precision of $< 4^\circ$, many more modes still need to add!
- ❖ BESIII (STCF) will play important roles for the charm inputs

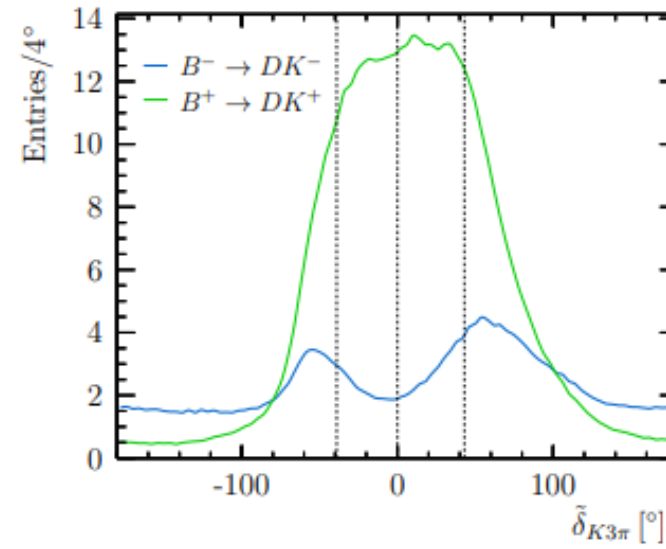
Thank you!

backup

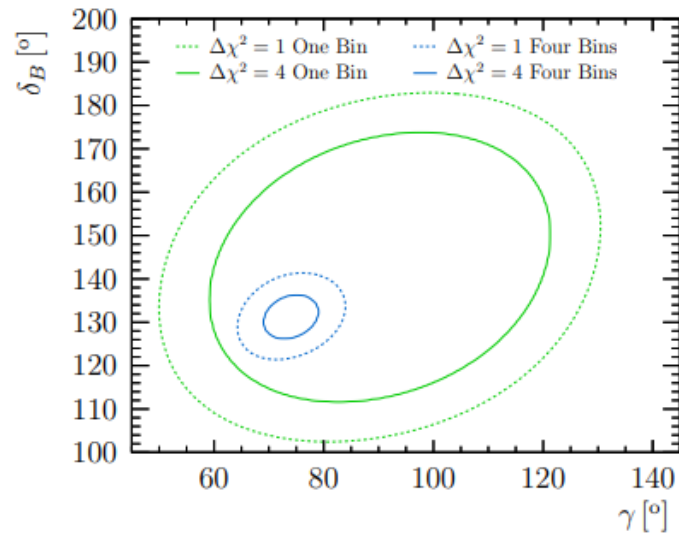
$K3\pi$ binning scheme



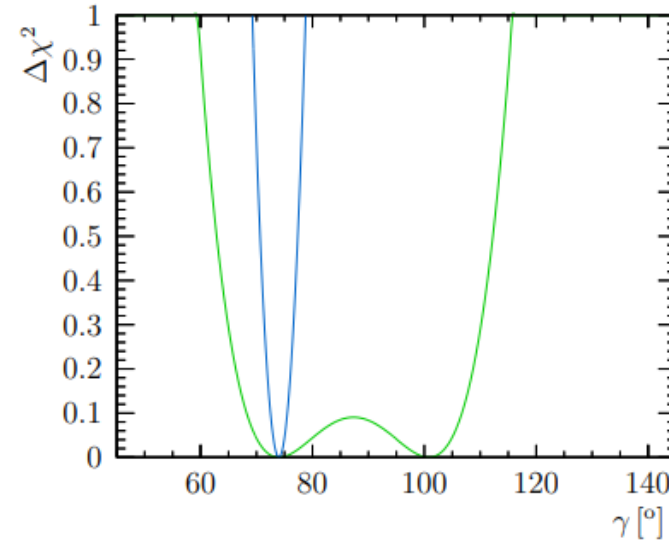
(a)



(b)



(a)

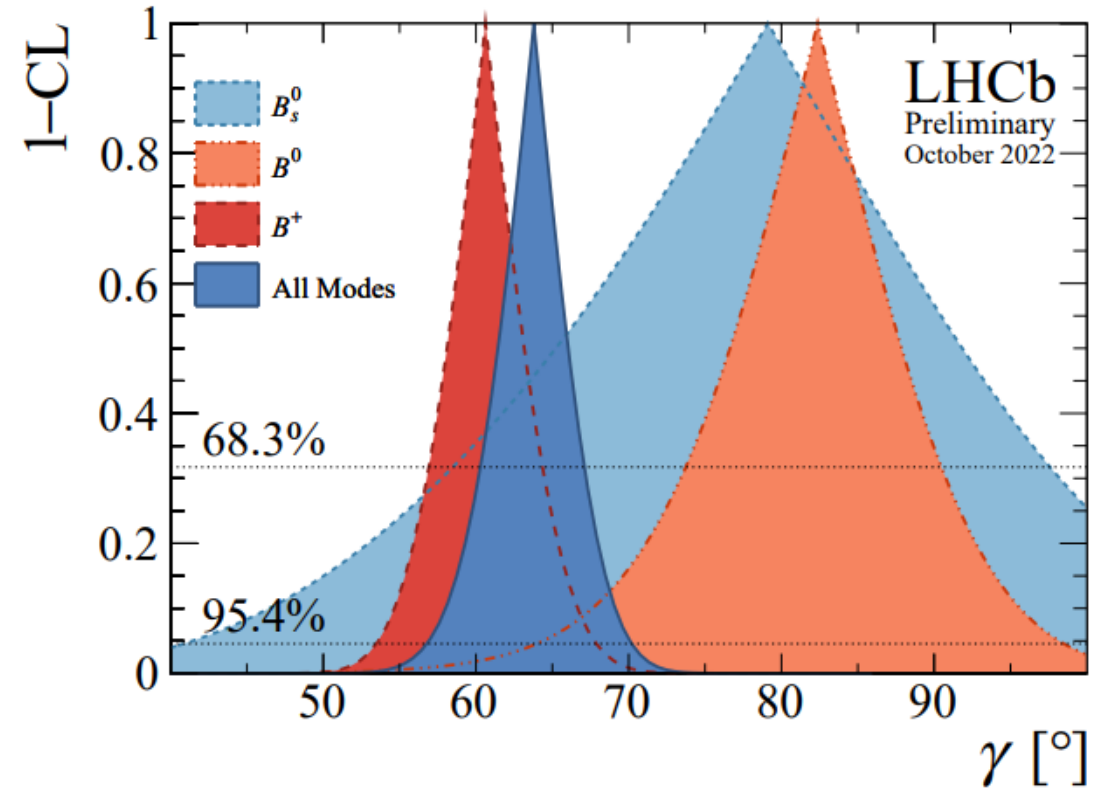


(b)

LHCb γ combination

- ❖ Best knowledge of γ comes from combination of many measurements
- ❖ Maximum likelihood fit
 - 173 observables
 - 52 free parameters
- ❖ Most precise determination of γ by a single experiment:

$$\gamma = (63.8^{+3.5}_{-3.7})^\circ$$



Input parameters

Decay	Parameters	Source	Ref.	Status since Ref. [14]
$B^\pm \rightarrow DK^{*\pm}$	$\kappa_{B^\pm}^{DK^{*\pm}}$	LHCb	[33]	As before
$B^0 \rightarrow DK^{*0}$	$\kappa_{B^0}^{DK^{*0}}$	LHCb	[53]	As before
$B^0 \rightarrow D^\mp \pi^\pm$	β	HFLAV	[13]	As before
$B_s^0 \rightarrow D_s^\mp K^\pm(\pi\pi)$	ϕ_s	HFLAV	[13]	As before
$D \rightarrow K^+ \pi^-$	$\cos \delta_D^{K\pi}, \sin \delta_D^{K\pi}, (r_D^{K\pi})^2, x^2, y$	CLEO-c	[27]	New
$D \rightarrow K^+ \pi^-$	$A_{K\pi}, A_{K\pi\pi^0}^{\pi\pi\pi^0}, r_D^{K\pi} \cos \delta_D^{K\pi}, r_D^{K\pi} \sin \delta_D^{K\pi}$	BESIII	[28]	New
$D \rightarrow h^+ h^- \pi^0$	$F_{\pi\pi\pi^0}^+, F_{KK\pi^0}^+$	CLEO-c	[54]	As before
$D \rightarrow \pi^+ \pi^- \pi^+ \pi^-$	$F_{4\pi}^+$	CLEO-c+BESIII	[26, 54]	Updated
$D \rightarrow K^+ \pi^- \pi^0$	$r_D^{K\pi\pi^0}, \delta_D^{K\pi\pi^0}, \kappa_D^{K\pi\pi^0}$	CLEO-c+LHCb+BESIII	[55–57]	As before
$D \rightarrow K^\pm \pi^\mp \pi^+ \pi^-$	$r_D^{K3\pi}, \delta_D^{K3\pi}, \kappa_D^{K3\pi}$	CLEO-c+LHCb+BESIII	[49, 55–57]	As before
$D \rightarrow K_S^0 K^\pm \pi^\mp$	$r_D^{K_S^0 K\pi}, \delta_D^{K_S^0 K\pi}, \kappa_D^{K_S^0 K\pi}$	CLEO	[58]	As before
$D \rightarrow K_S^0 K^\pm \pi^\mp$	$r_D^{K_S^0 K\pi}$	LHCb	[59]	As before