

Decay-time-dependent measurements of the CKM angle γ at LHCb

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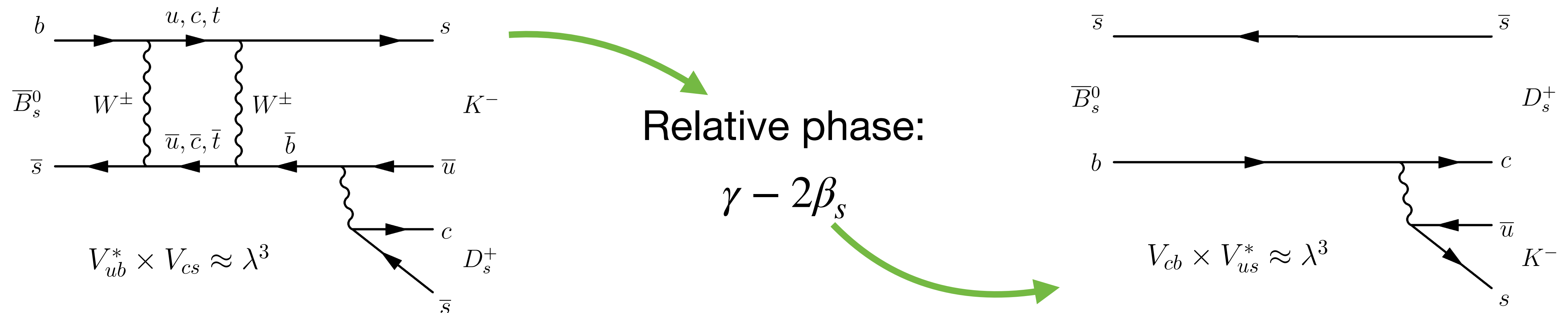
On behalf of the LHCb collaboration

12th International Workshop on the CKM Unitarity

September 19th 2023

Decay-time dependent measurements of γ

- Interference of direct decay and decay after mixing
 - ▶ Accessible in relative phase
- Limited sensitivity in $B^0 \rightarrow D^{\mp} \pi^{\pm}$ -like decays
- Good sensitivity in $B_s^0 \rightarrow D_s^{\mp} K^{\pm}$ -like decays
 - ▶ Large interference effects



Decay-time dependent measurements of γ

- Measurement of four decay rates gives access to:
 - ▶ Relative phase $\gamma - 2\beta_s$
 - ▶ Strong phase difference δ
 - ▶ Amplitude ratio $r_{D_s K}$



$$\Gamma(B_s^0(t) \rightarrow f/\bar{f}) \sim e^{-\Gamma_s t} \left(\cosh\left(\frac{\Delta\Gamma_s}{2} t\right) + C_{f/\bar{f}} \cos(\Delta m_s t) + A_{f/\bar{f}}^{\Delta\Gamma} \sinh\left(\frac{\Delta\Gamma_s}{2} t\right) - S_{f/\bar{f}} \sin(\Delta m_s t) \right)$$

$$C_f = C_{\bar{f}} = \frac{1 - r_{D_s K}^2}{1 + r_{D_s K}^2}$$

$$A_f^{\Delta\Gamma} = \frac{-2 r_{D_s K} \cos(\delta - (\gamma - 2\beta_s))}{1 + r_{D_s K}^2}$$

$$S_f = \frac{2 r_{D_s K} \sin(\delta - (\gamma - 2\beta_s))}{1 + r_{D_s K}^2}$$

$$A_{\bar{f}}^{\Delta\Gamma} = \frac{-2 r_{D_s K} \cos(\delta + (\gamma - 2\beta_s))}{1 + r_{D_s K}^2}$$

$$S_{\bar{f}} = \frac{2 r_{D_s K} \sin(\delta + (\gamma - 2\beta_s))}{1 + r_{D_s K}^2}$$

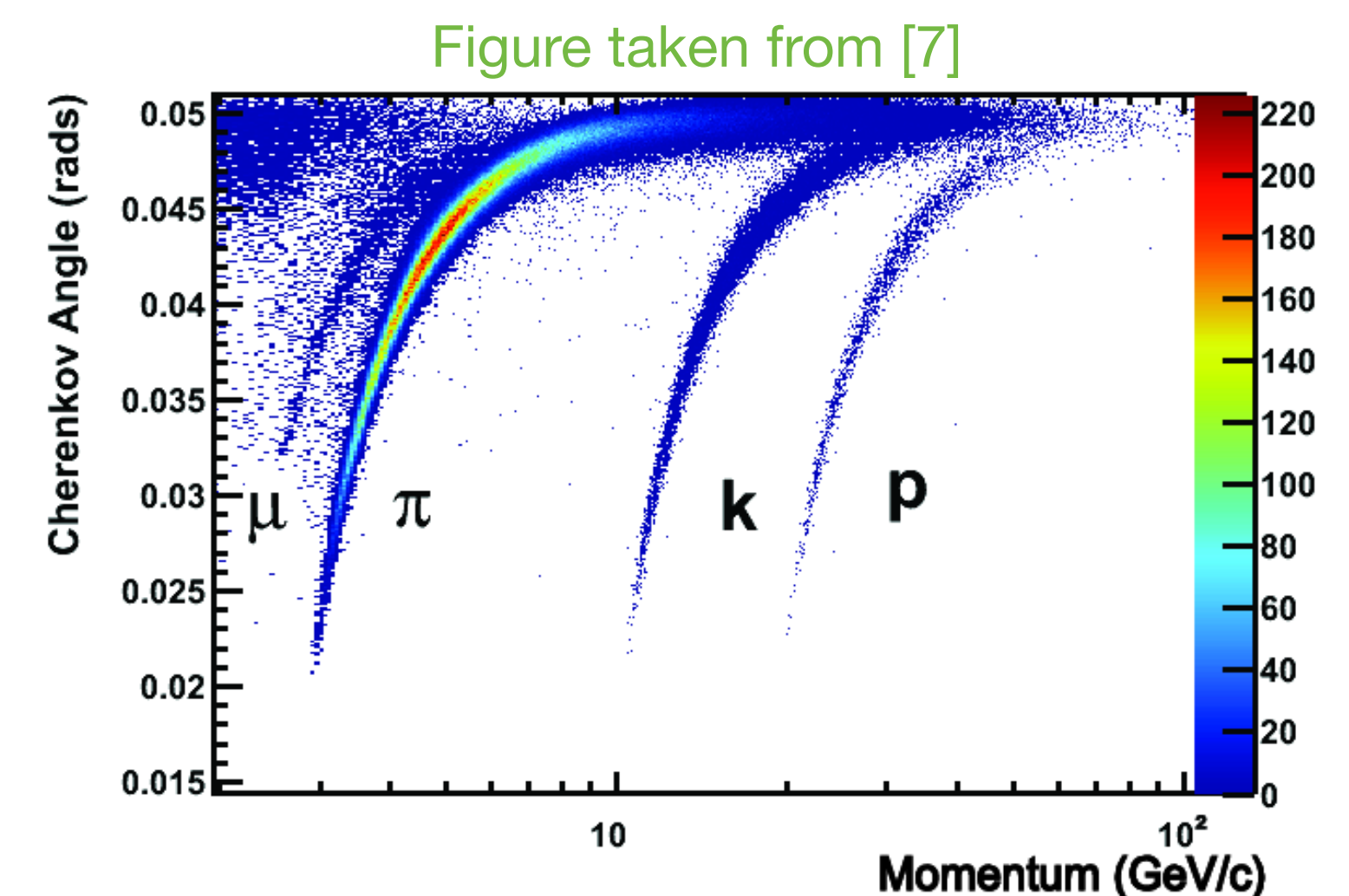
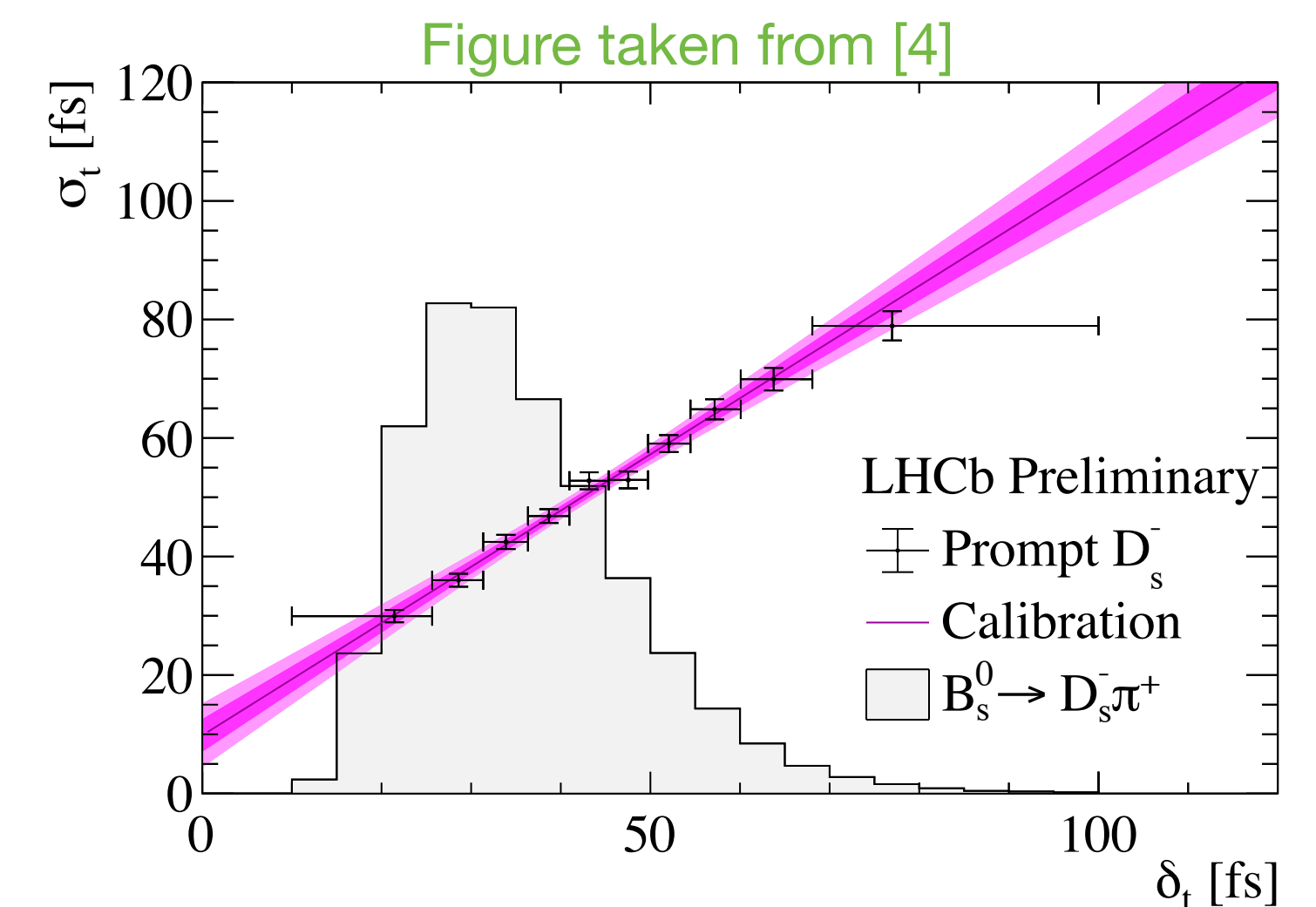


The LHCb experiment

The LHCb experiment

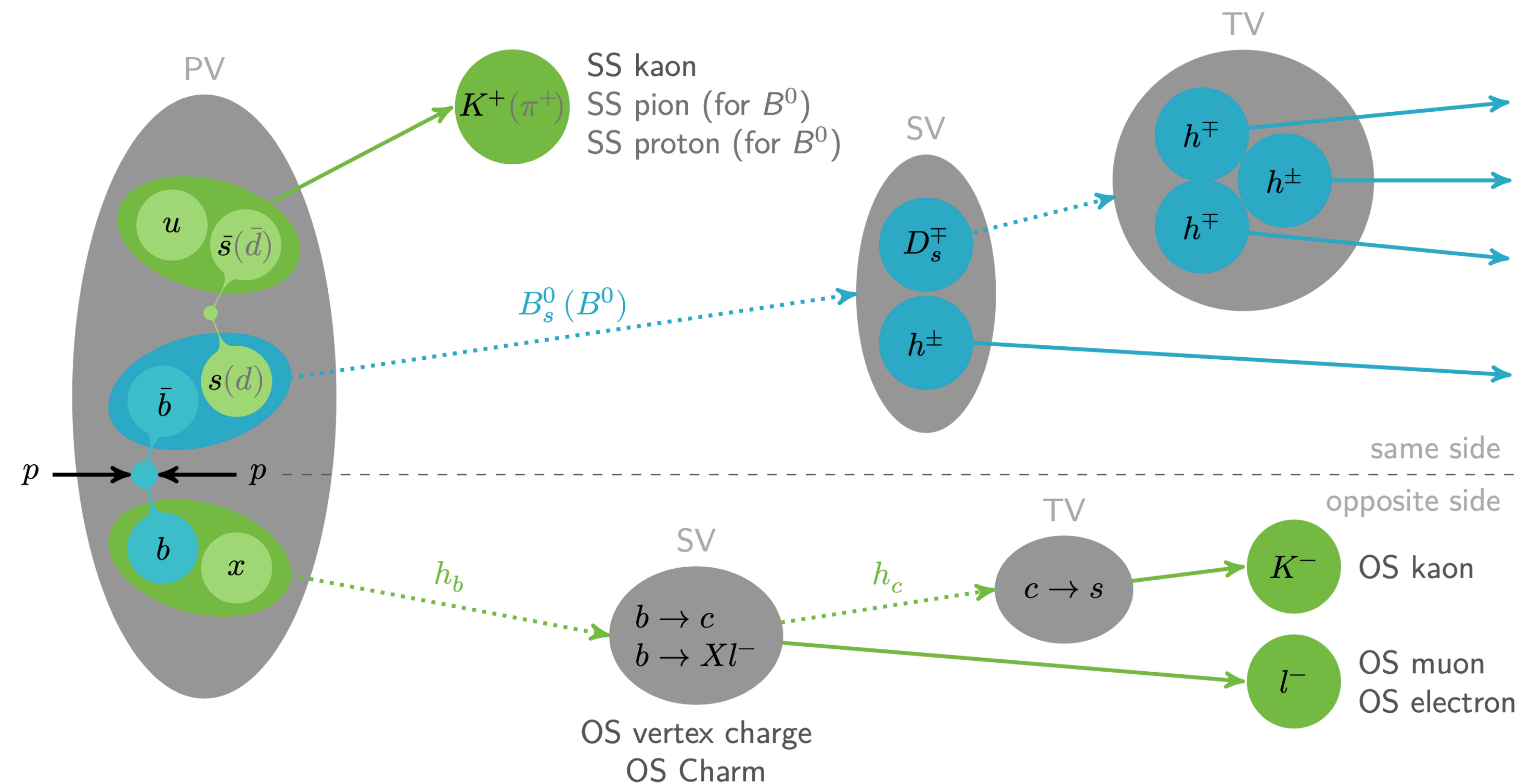
- **Single-arm forward spectrometer**
 - ▶ Precision measurements of b and c decays
- **Good decay-time resolution**
 - ▶ VertexLocator close to interaction region
 - ▶ Average resolution below 50 fs [4]
- **Good hadron identification**
 - ▶ Only 10 % $\pi \rightarrow K$ misID at 95 % K efficiency [6]
 - ▶ Important for the hadronic final-states
 - ▶ Ingredient to flavour tagging

[4] LHCb-CONF-2023-004
[6] Int. J. Mod. Phys. A 30, 1530022 (2015)
[7] Eur. Phys. J. C 73, 2431 (2013)



Flavour tagging at LHCb

- Flavour tagging estimates initial flavour
 - ▶ Exploits various fragmentation processes
 - ▶ MVA-based mistag probability
- Reduction of effective sample size
 - ▶ Tagging efficiency
 - ▶ Dilution from mistagged candidates



$$\epsilon_{\text{eff}} = \epsilon_{\text{tag}} \cdot (1 - 2\omega(\eta))^2$$

$$\sigma(A_{CP}) \sim \frac{1}{\sqrt{\epsilon_{\text{eff}} \cdot N}}$$

TD B_s^0 measurements at LHCb

[8] Nat. Phys. 18, 1–5 (2022)

- Signal extraction
- Careful handling of:
 - ▶ Flavour tagging calibration
 - ▶ Decay-time resolution
 - ▶ Decay-time acceptance

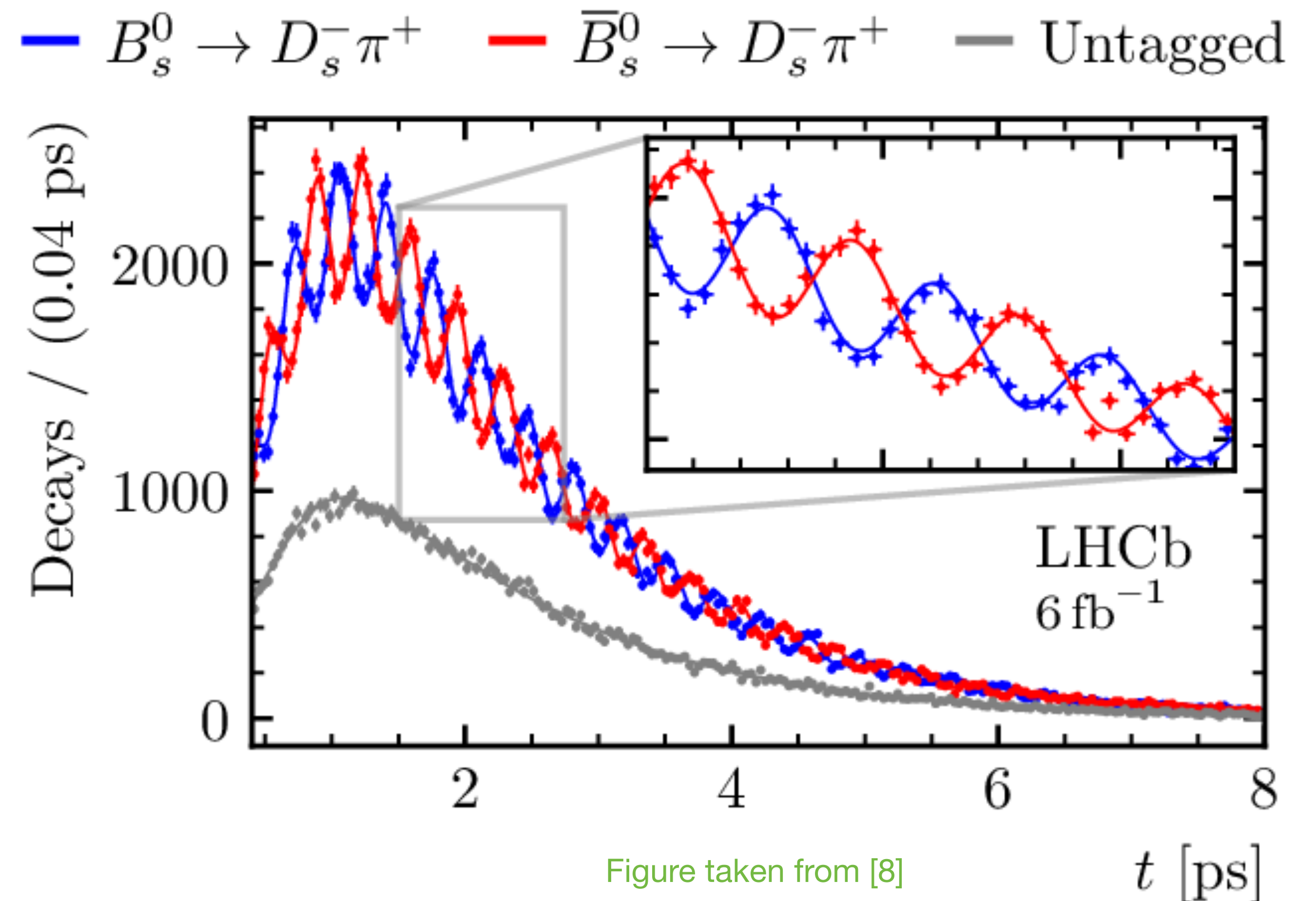


Figure taken from [8]

[1] JHEP 06 (2018) 084
[2] JHEP 03 (2018) 059
[3] JHEP 03 (2021) 137
[4] LHCb-CONF-2023-004
[5] LHCb-CONF-2022-003

TD measurements of γ at LHCb

- Time-dependent measurements of γ

- $B^0 \rightarrow D^{\mp} \pi^{\pm}$ (Run1, 3 fb⁻¹) [1]
- $B_s^0 \rightarrow D_s^{\mp} K^{\pm}$ (Run1, 3 fb⁻¹) [2]
- $B_s^0 \rightarrow D_s^{\mp} K^{\pm} \pi^{\mp} \pi^{\pm}$ (Run1+2, 9 fb⁻¹) [3]
- $B_s^0 \rightarrow D_s^{\mp} K^{\pm}$ **NEW!** (Run2, 6 fb⁻¹) [4]

- Small tensions

- Charged vs neutral
- Within B_s^0 measurements
- Time-dependent vs integrated

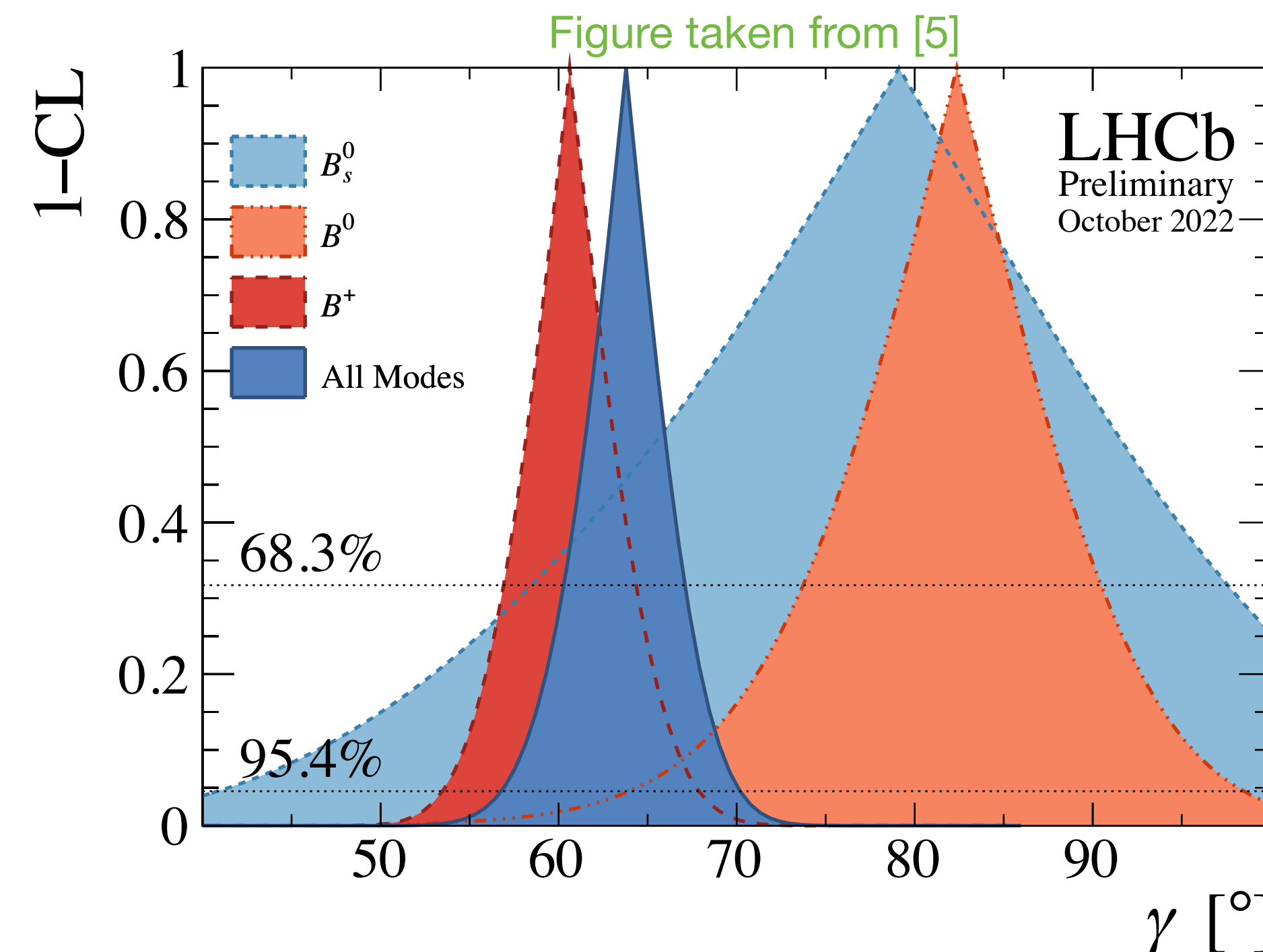


Table taken from [5]

Method	Value [°]	68.3% CL		95.4% CL	
		Uncertainty	Interval	Uncertainty	Interval
Time-dependent	79	+21 -23	[56, 100]	+51 -48	[31, 130]
Time-integrated	63.3	+3.7 -3.9	[59.4, 67.0]	+7.1 -7.8	[55.5, 70.4]

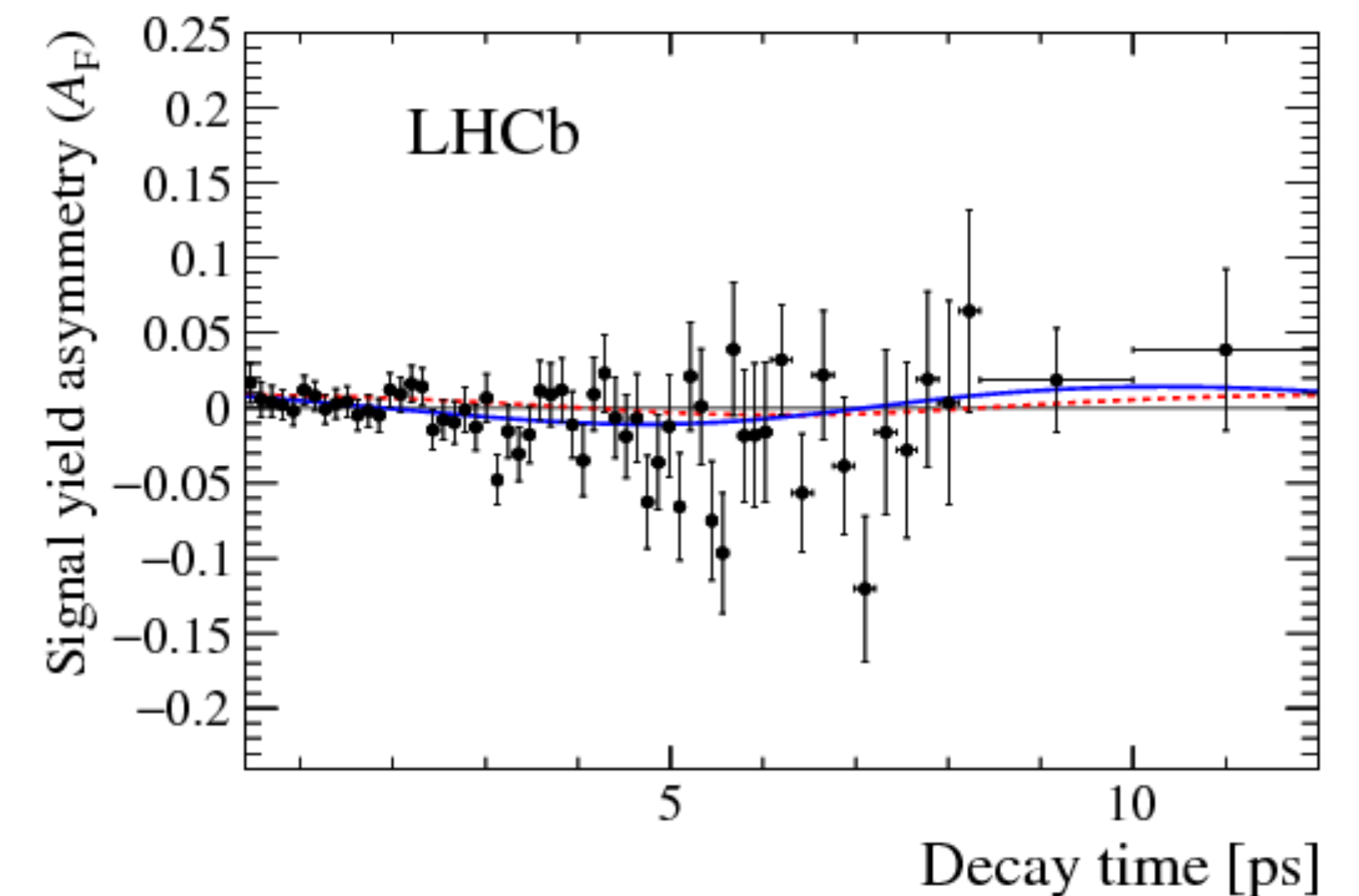
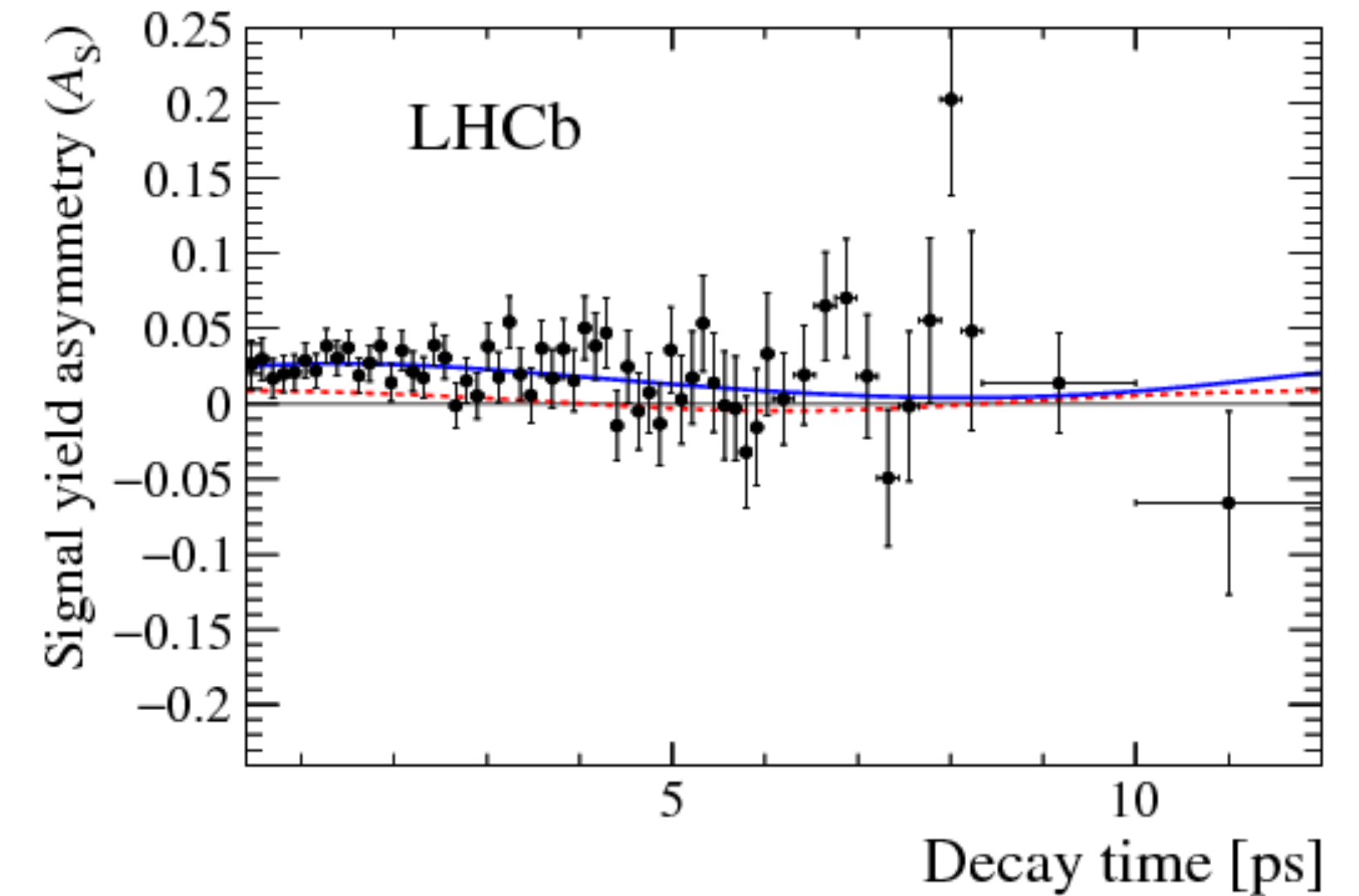
Overview on previous measurements

$B^0 \rightarrow D^{\mp} \pi^{\pm}$ - Run1 [1]

[1] JHEP 06 (2018) 084

- 2011 & 12 data (3 fb^{-1})
- Large statistics
 - ▶ 479000 ± 700 candidates
 - ▶ $\epsilon_{\text{eff}} = (5.59 \pm 0.01) \%$
- Minor sensitivity to γ
 - ▶ Amplitude ratio $r_{D\pi} \approx 0.02$
 - ▶ Negligible $\Delta\Gamma \approx 0$

$$\gamma \in [5^\circ, 86^\circ] \cup [185^\circ, 266^\circ] \text{ at } 68 \% \text{ CL}$$



[2] JHEP 03 (2018) 059

$B_s^0 \rightarrow D_s^\mp K^\pm$ - Run1 [2]

- 2011 & 12 data (3 fb^{-1})
 - ▶ 5955 ± 90 candidates
 - ▶ $\epsilon_{\text{eff}} = (5.80 \pm 0.25) \%$
- High sensitivity to γ
 - ▶ Amplitude ratio $r_{D_s K} \approx 0.4$

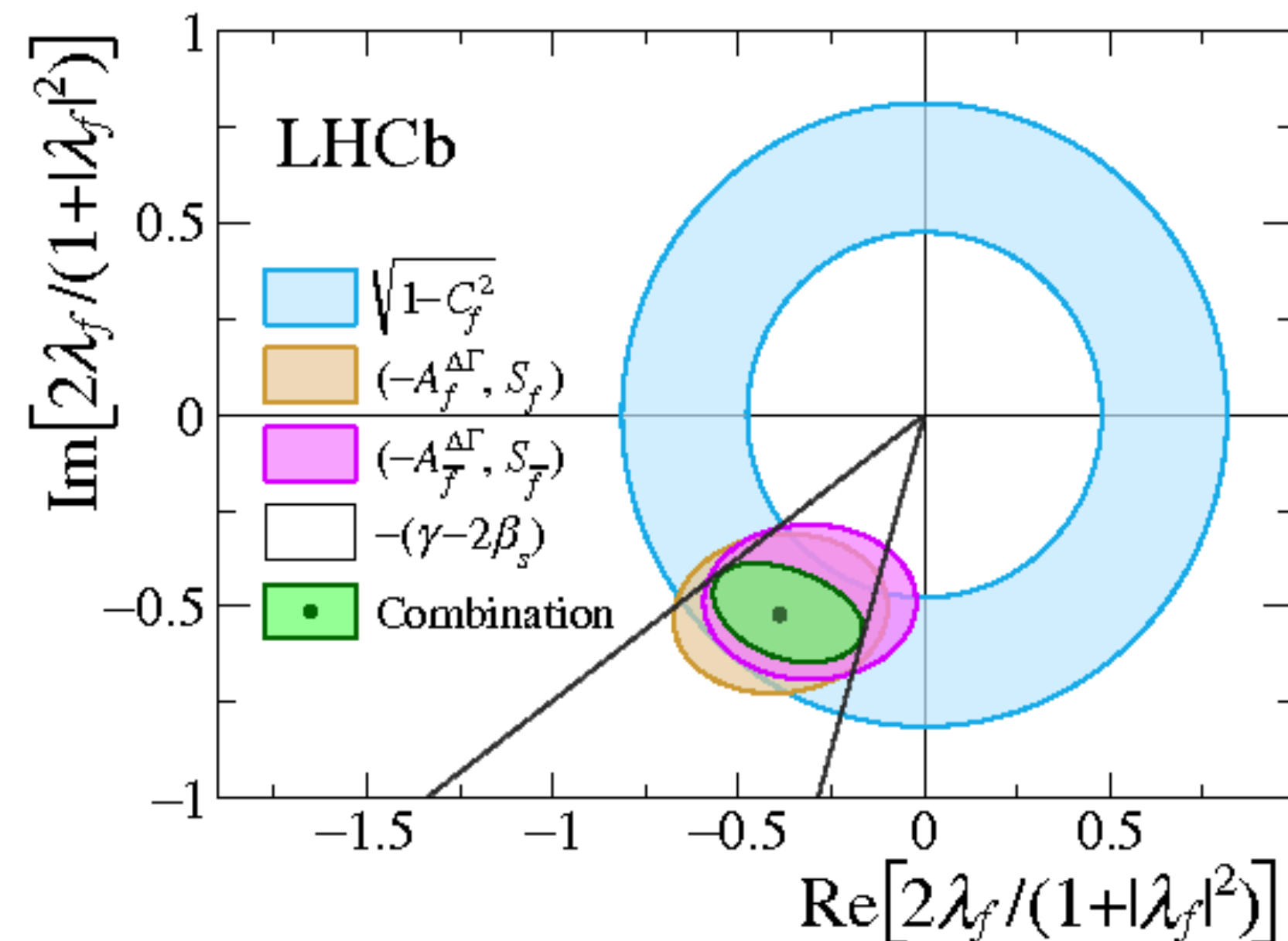
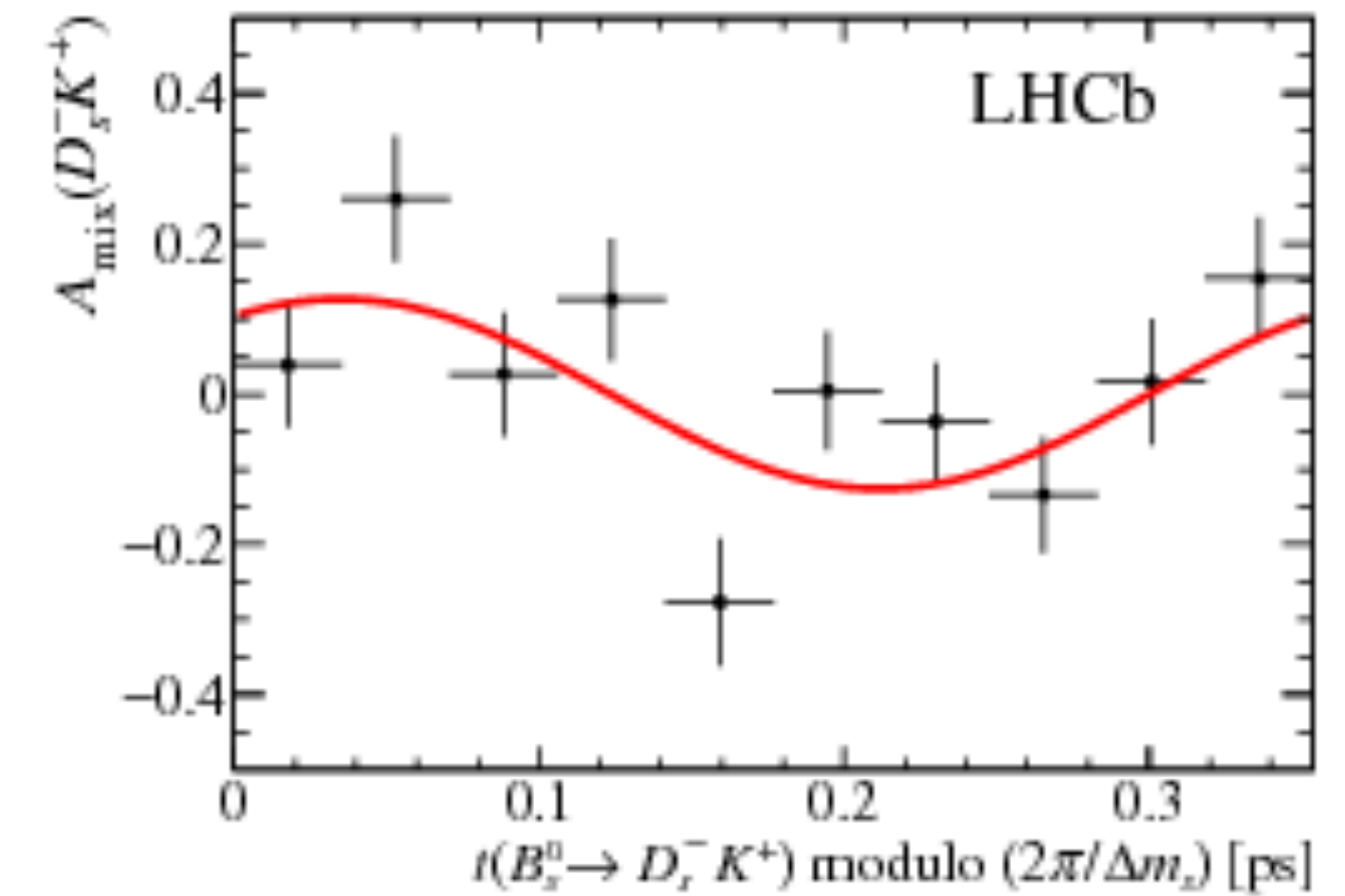
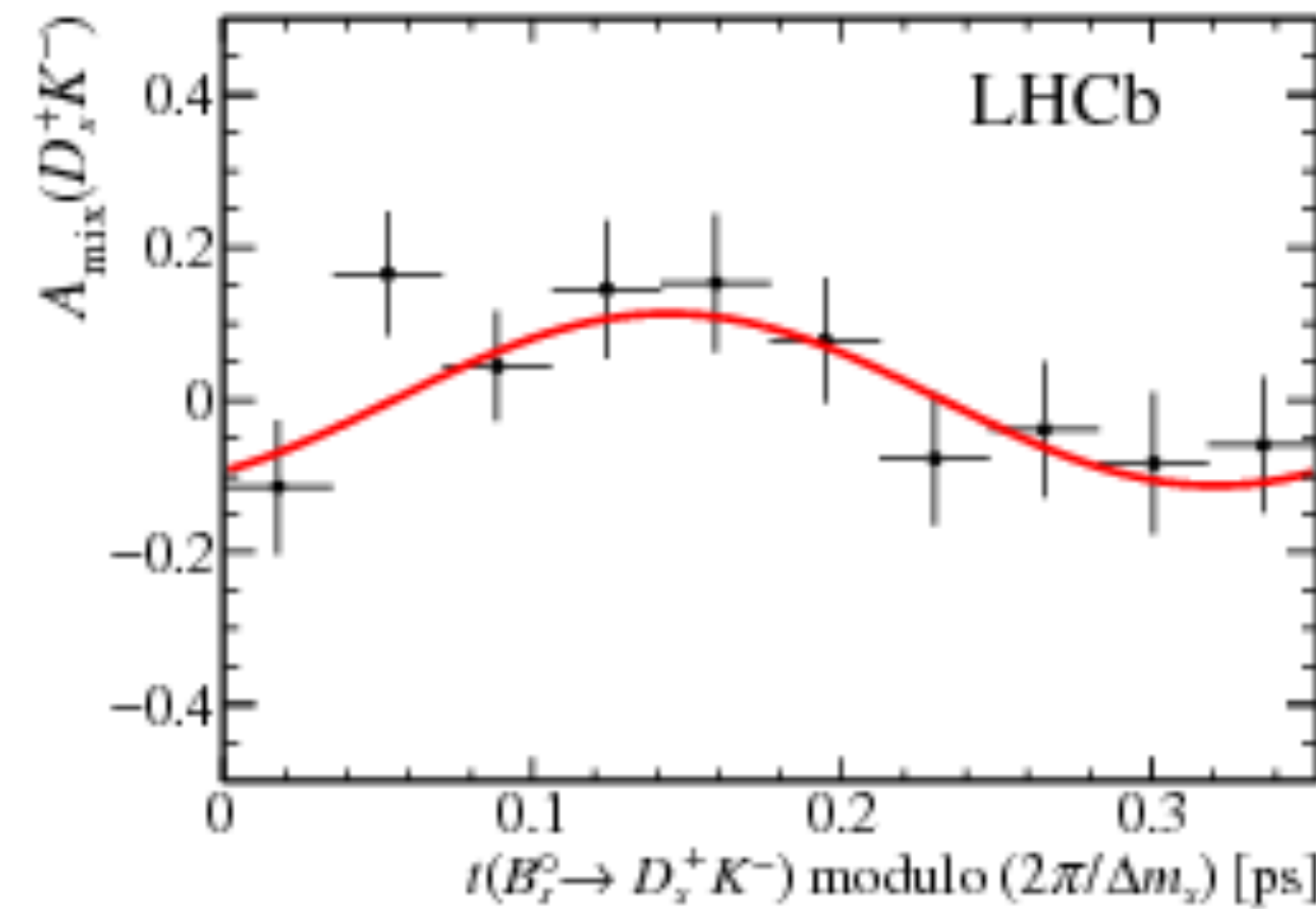
$$C_f = 0.73 \pm 0.14 \pm 0.05$$

$$A_f^{\Delta\Gamma} = 0.39 \pm 0.28 \pm 0.15$$

$$A_{\bar{f}}^{\Delta\Gamma} = 0.31 \pm 0.28 \pm 0.15$$

$$S_f = -0.52 \pm 0.20 \pm 0.07$$

$$S_{\bar{f}} = -0.49 \pm 0.20 \pm 0.07$$



$$\gamma = (128^{+17}_{-22})^\circ$$

$B_s^0 \rightarrow D_s^\mp K^\pm \pi^\mp \pi^\pm$ - Run1 & 2 [3]

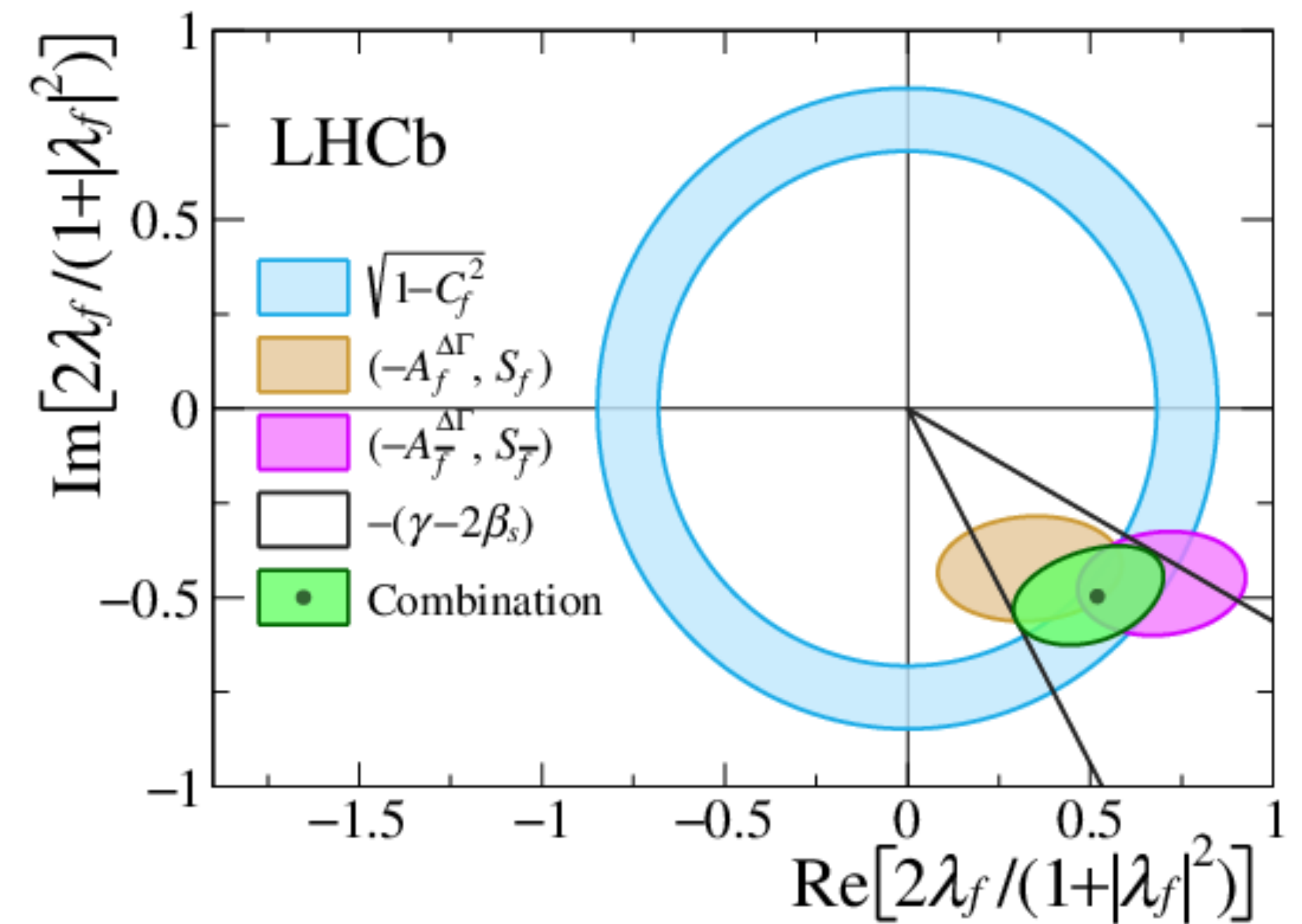
[3] JHEP 03 (2021) 137

- Full LHCb dataset (Run1 & 2, 9 fb^{-1})

- ▶ 7500 ± 100 candidates
- ▶ $\epsilon_{\text{eff}} = (5.71 \pm 0.40) \%$ (Run1)
- ▶ $\epsilon_{\text{eff}} = (6.52 \pm 0.17) \%$ (Run2)

- Two strategies

1. Phase-space integrated analysis



$$C_f = 0.631 \pm 0.096 \pm 0.032$$

$$A_f^{\Delta\Gamma} = -0.334 \pm 0.232 \pm 0.097$$

$$S_f = -0.424 \pm 0.135 \pm 0.033$$

$$A_{\bar{f}}^{\Delta\Gamma} = -0.695 \pm 0.215 \pm 0.081$$

$$S_{\bar{f}} = -0.463 \pm 0.134 \pm 0.031$$

$$\gamma = \left(44_{-13}^{+20} \right)^\circ$$

$B_s^0 \rightarrow D_s^\mp K^\pm \pi^\mp \pi^\pm$ - Run1 & 2 [3]

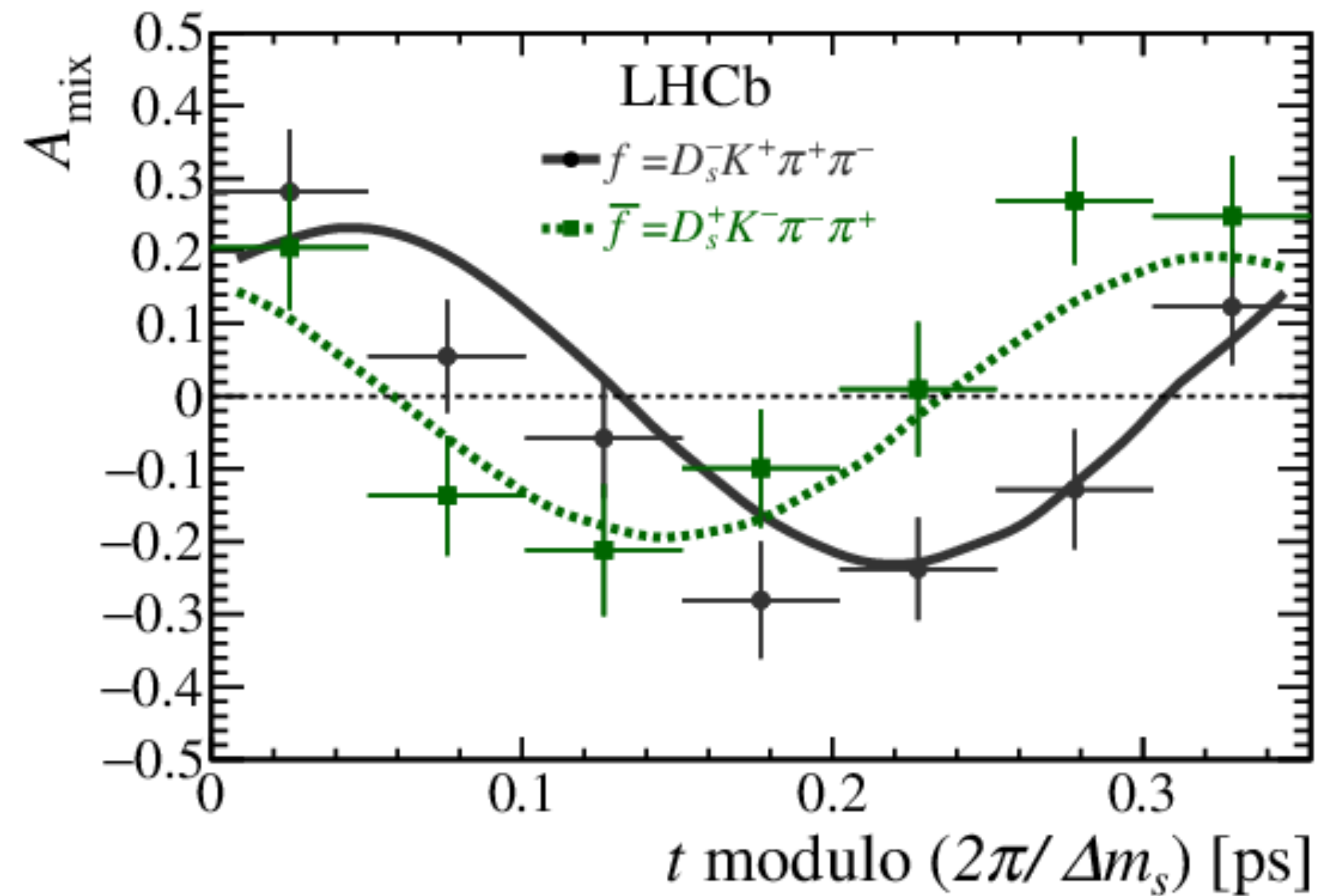
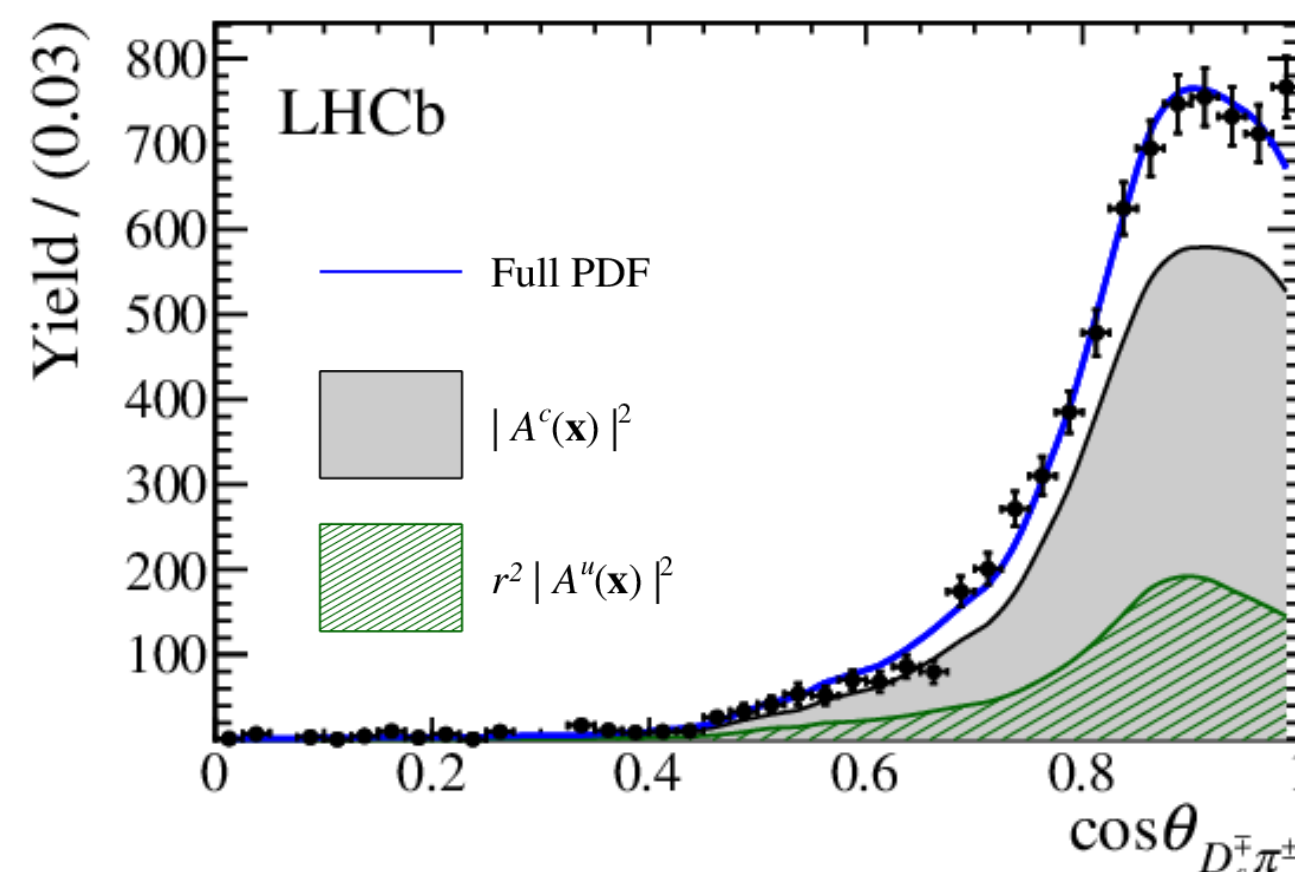
[3] JHEP 03 (2021) 137

- Full LHCb dataset (Run1 & 2, 9 fb^{-1})

- ▶ 7500 ± 100 candidates
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- ▶ $\epsilon_{\text{eff}} = (6.52 \pm 0.17) \%$ (Run2)

- Two strategies

2. Model-dependent amplitude analysis



$$\gamma = (44 \pm 12)^\circ$$

**Analysis of $B_s^0 \rightarrow D_s^{\mp} K^{\pm}$ decays
in the LHCb Run2 dataset**

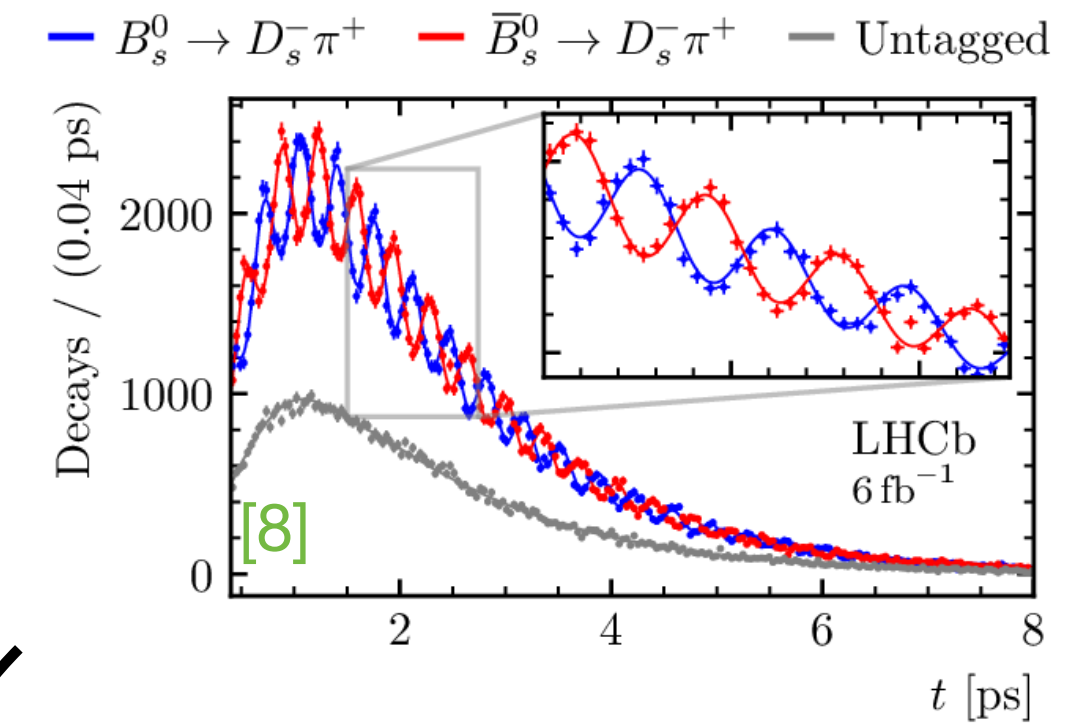
$B_s^0 \rightarrow D_s^\mp K^\pm$ - Run2

- Three time-dependent legacy measurements coming together

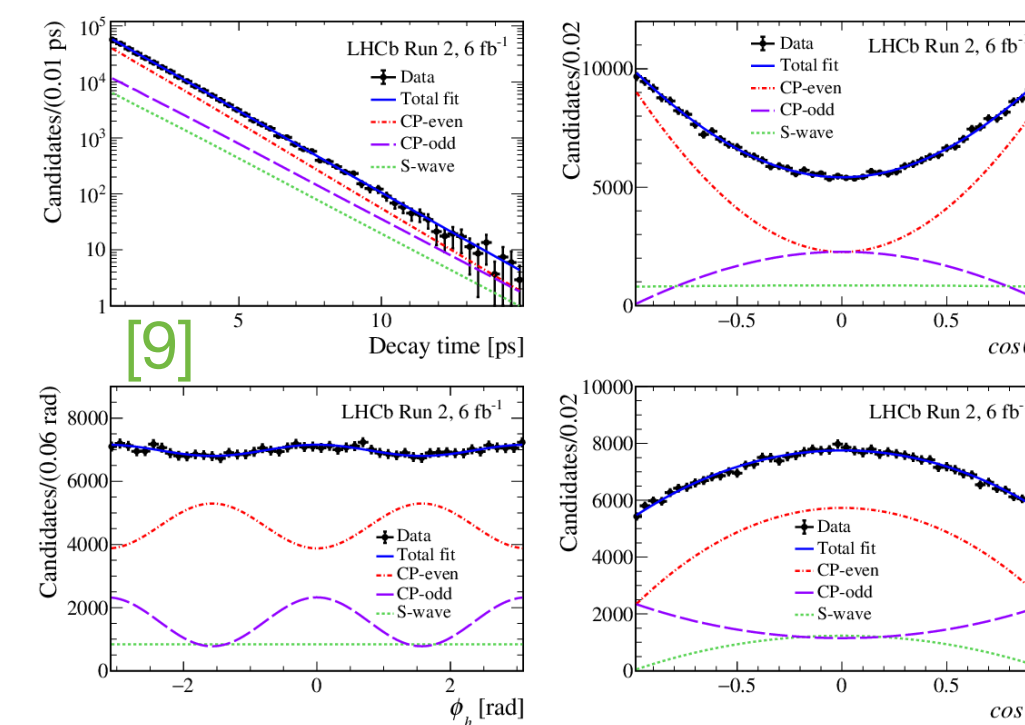
- ▶ $B_s^0 \rightarrow D_s^- \pi^+$ Run2 [8]
- ▶ $B_s^0 \rightarrow D_s^\mp K^\pm$ Run2 [4]
- ▶ $B_s^0 \rightarrow J/\psi K^+ K^-$ Run2 [9]

- Most precise TD measurement of γ

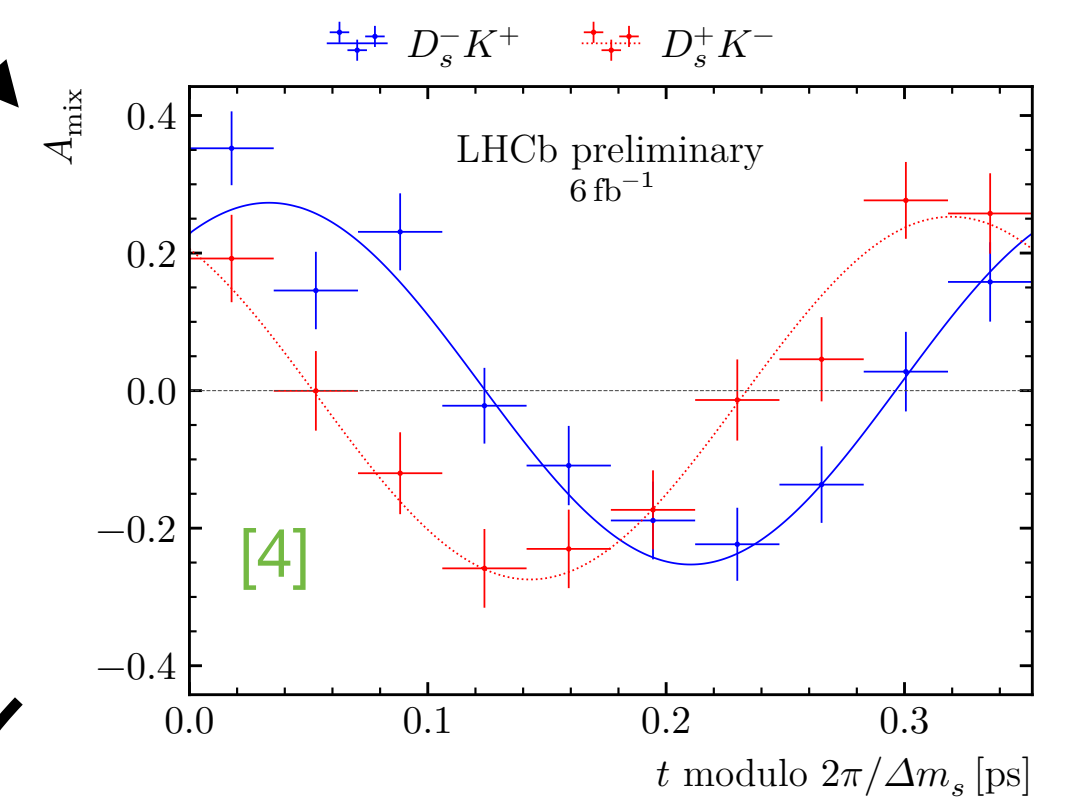
[4] LHCb-CONF-2023-004
[8] Nat. Phys. 18, 1–5 (2022)
[9] LHCb-PAPER-2023-016, submitted to Phys. Rev. Lett.



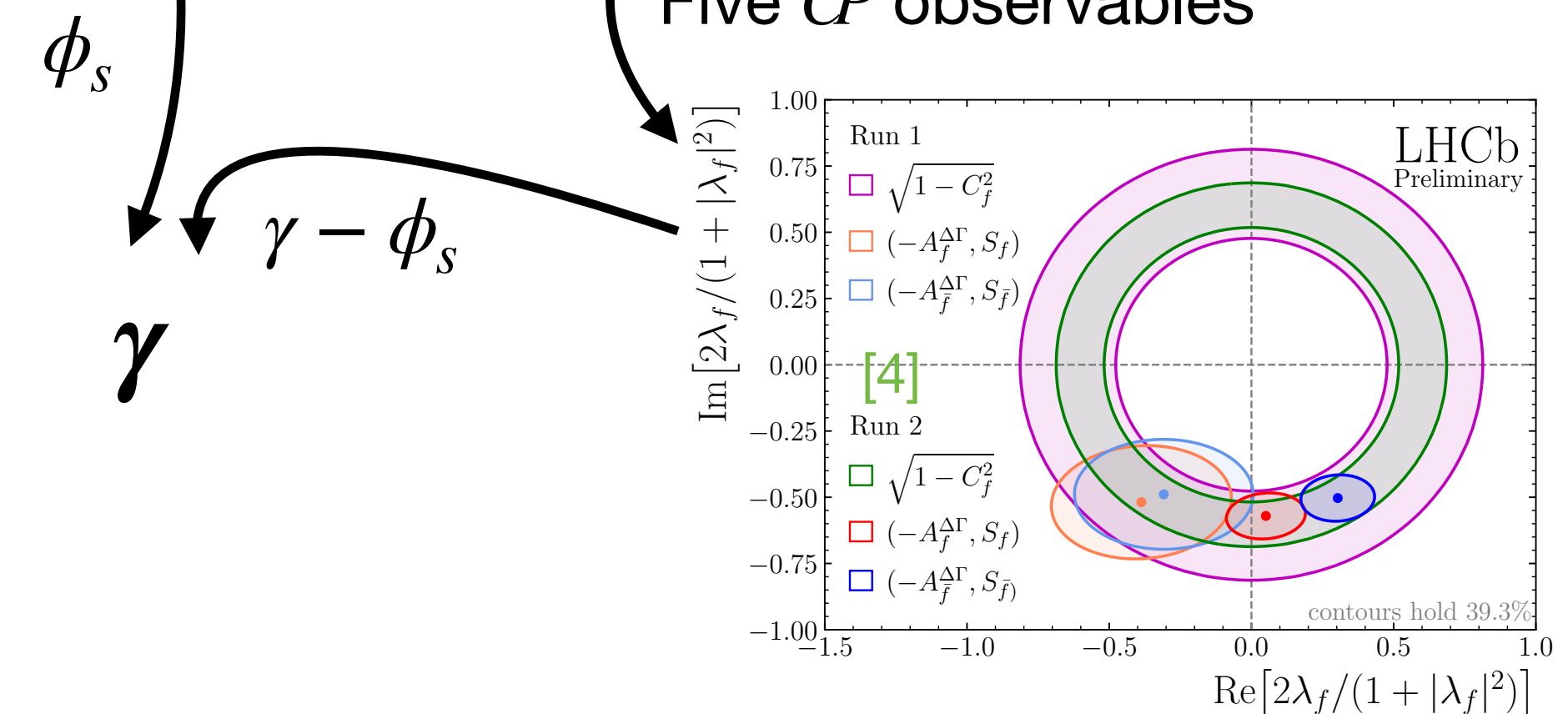
WG4, Mon 14:45



Inputs (Δm_s , calibrations)



Five CP observables

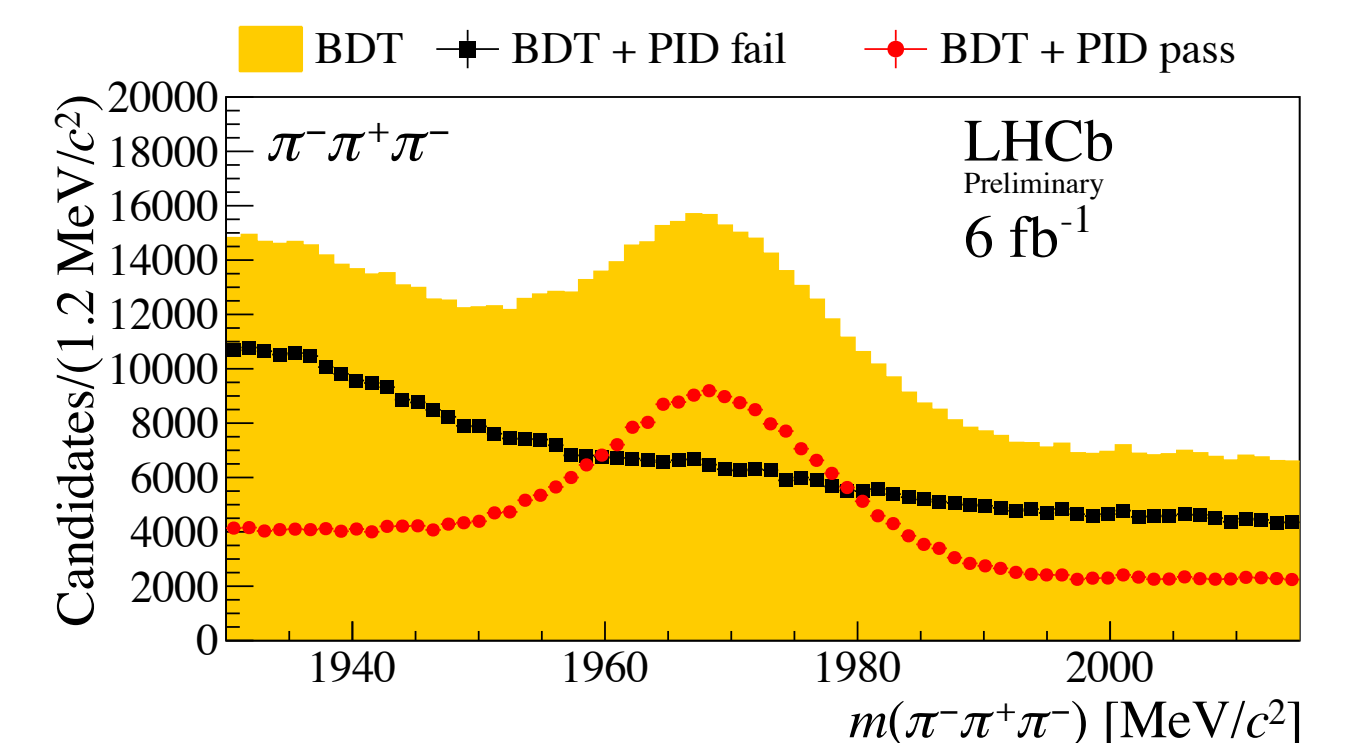
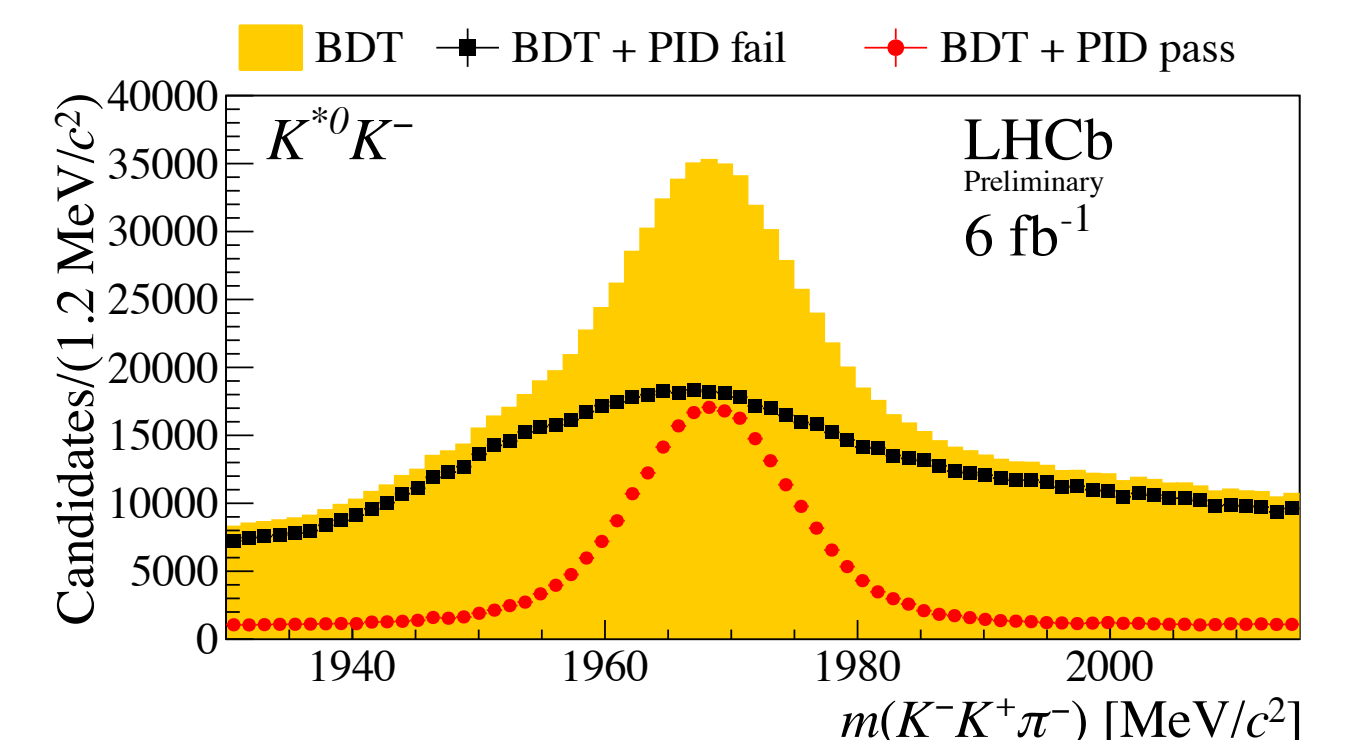
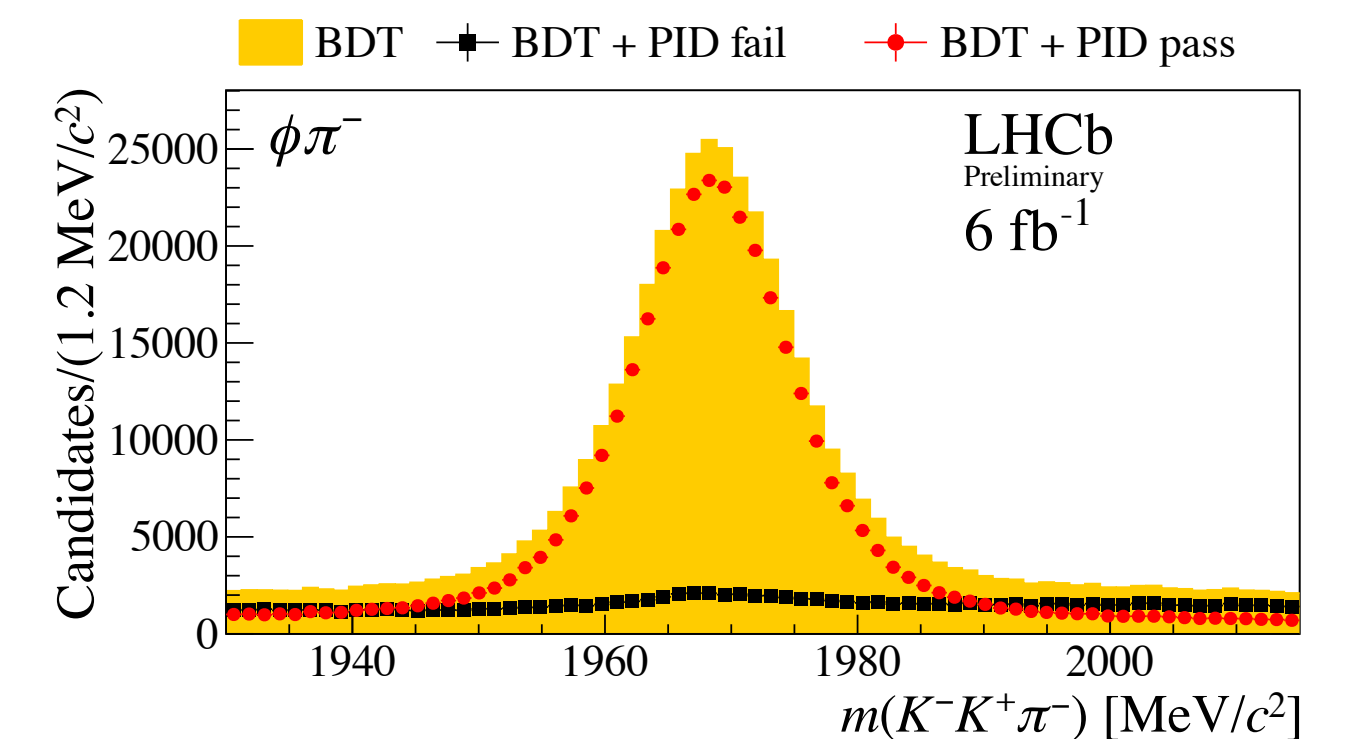


ϕ_s
 $\gamma - \phi_s$
 γ

[4] LHCb-CONF-2023-004

$B_s^0 \rightarrow D_s^\mp K^\pm$ - Run2 [4] - Signal

- D_s^- reconstructed in five modes
 - ▶ Different levels of contamination
 - ▶ $\phi(1020)\pi^-$ ▶ $K^- \pi^+ \pi^-$
 - ▶ $K^{*0}(892)K^-$ ▶ $\pi^- \pi^+ \pi^-$
 - ▶ $K^- K^+ \pi^-$ (nonresonant)
- Selection
 - ▶ BDT to reduce combinatorial
 - ▶ Various specific vetoes
 - ▶ FD requirements to suppress non- D_s^- backgrounds
 - ▶ Sample split by hadron PID $h \in \{K, \pi\}$

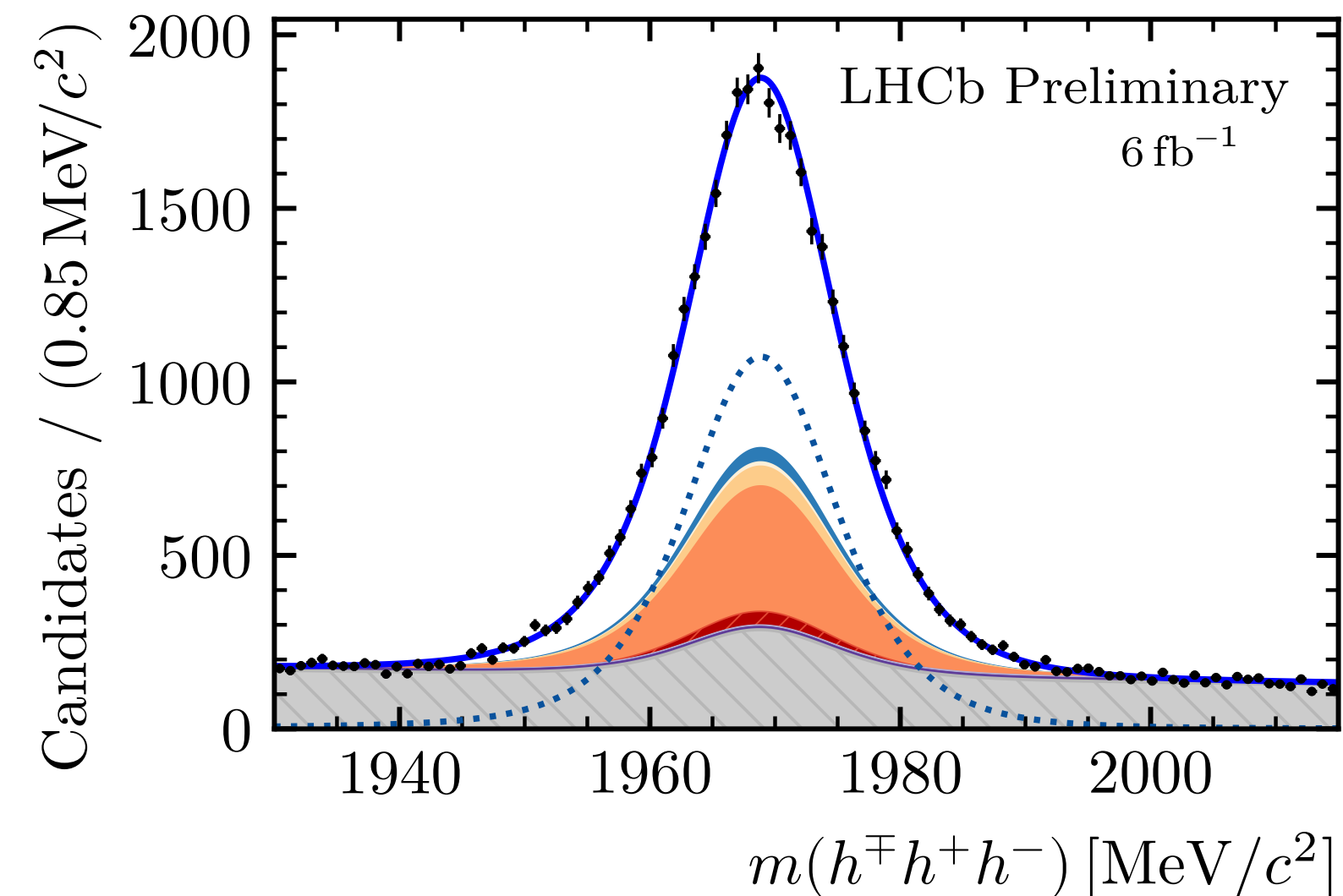
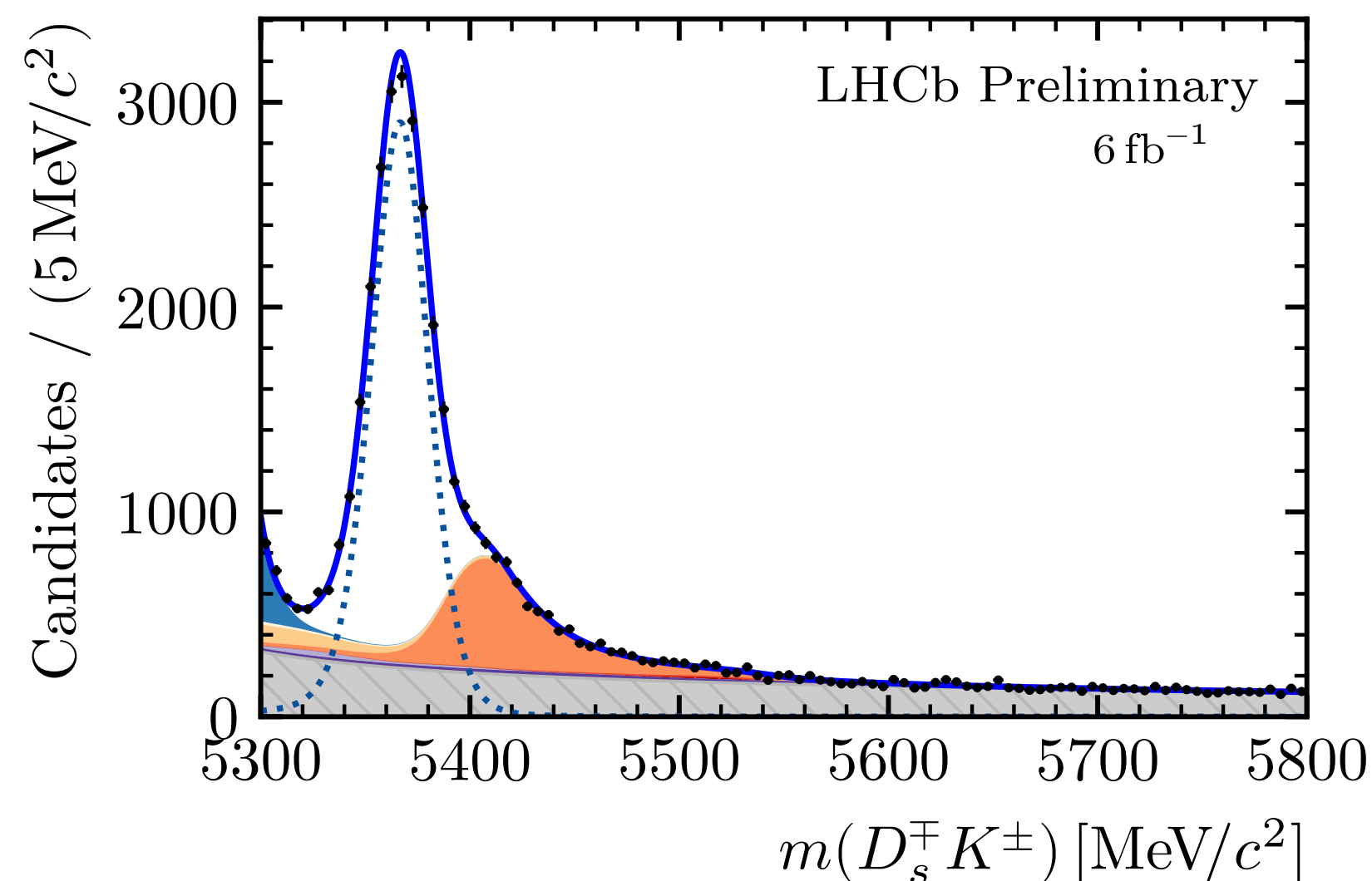


$B_s^0 \rightarrow D_s^\mp K^\pm$ - Run2 [4] - Signal

[4] LHCb-CONF-2023-004
[10] Eur. Phys. J. C 82, 393 (2022)

- Invariant mass fit to extract sWeights [10]
 - ▶ 2-dimensional
 - ▶ Simultaneous for all D_s^- modes and years (2015+16, 2017, 2018)
 - ▶ 20950 ± 180 candidates

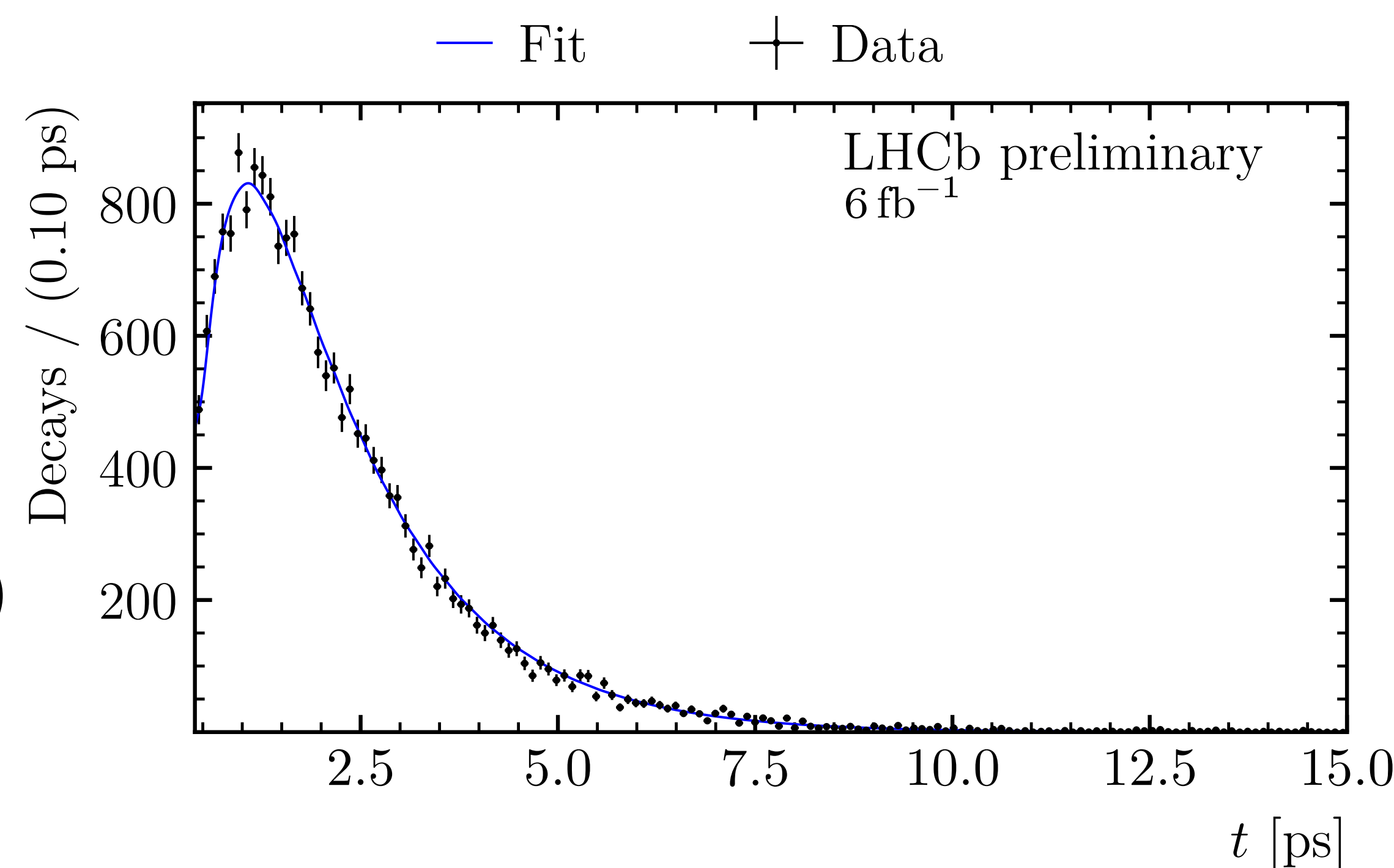
+ Data ▨ Combinatorial ▨ $B_s^0 \rightarrow D_s^- \rho^+$ ▨ $B_s^0 \rightarrow D_s^- \pi^+$ ▨ $B^0 \rightarrow D^- \{K^+, \pi^+\}$
 ⋯ $B_s^0 \rightarrow D_s^\mp K^\pm$ ▨ $B^0 \rightarrow D_s^- K^+$ ▨ $B_s^0 \rightarrow D_s^{*-} \pi^+$ ▨ $\Lambda_b^0 \rightarrow D_s^{(*)-} p$ ▨ $\bar{\Lambda}_b^0 \rightarrow \bar{\Lambda}_c^- \{K^+, \pi^+\}$



$B_s^0 \rightarrow D_s^\mp K^\pm$ - Run2 [4] - Fit

[4] LHCb-CONF-2023-004
[9] LHCb-PAPER-2023-016 (submitted to Phys. Rev. Lett.)
[11] LHCb-PUB-2018-004

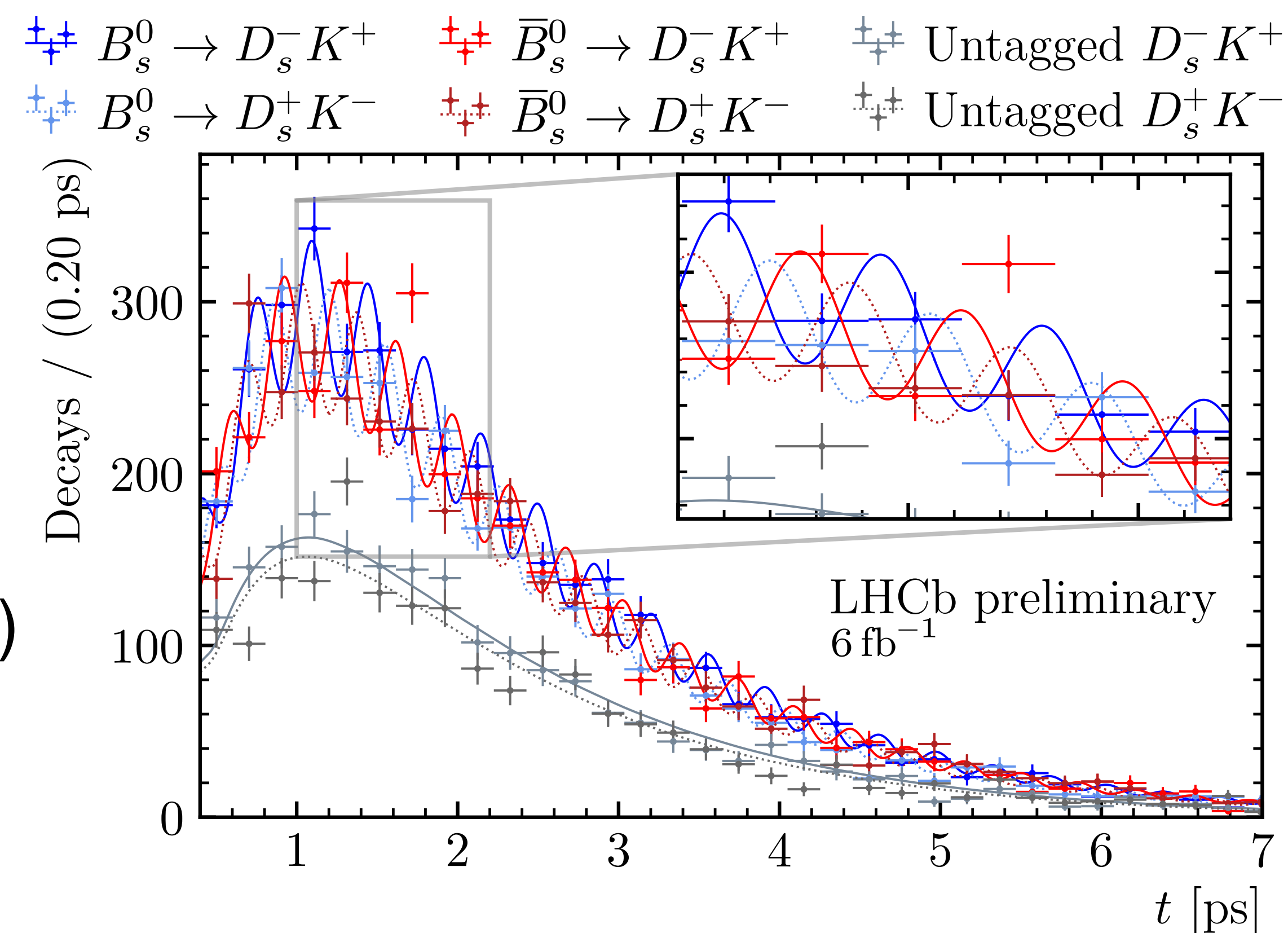
- Simultaneous fit of all modes and years
- Inputs from $B_s^0 \rightarrow D_s^- \pi^+$
 - ▶ Resolution calibration
 - ▶ VELO alignment correction
 - ▶ Decay-time acceptance with small simulation-based corrections
 - ▶ Tagging calibration ($\epsilon_{\text{eff}} = (6.10 \pm 0.15) \%$)
 - ▶ Production asymmetry and Δm_s
- External inputs
 - ▶ Γ_s and $\Delta\Gamma_s$ [9]
 - ▶ Detection asymmetry [11]



$B_s^0 \rightarrow D_s^\mp K^\pm$ - Run2 [4] - Fit

[4] LHCb-CONF-2023-004
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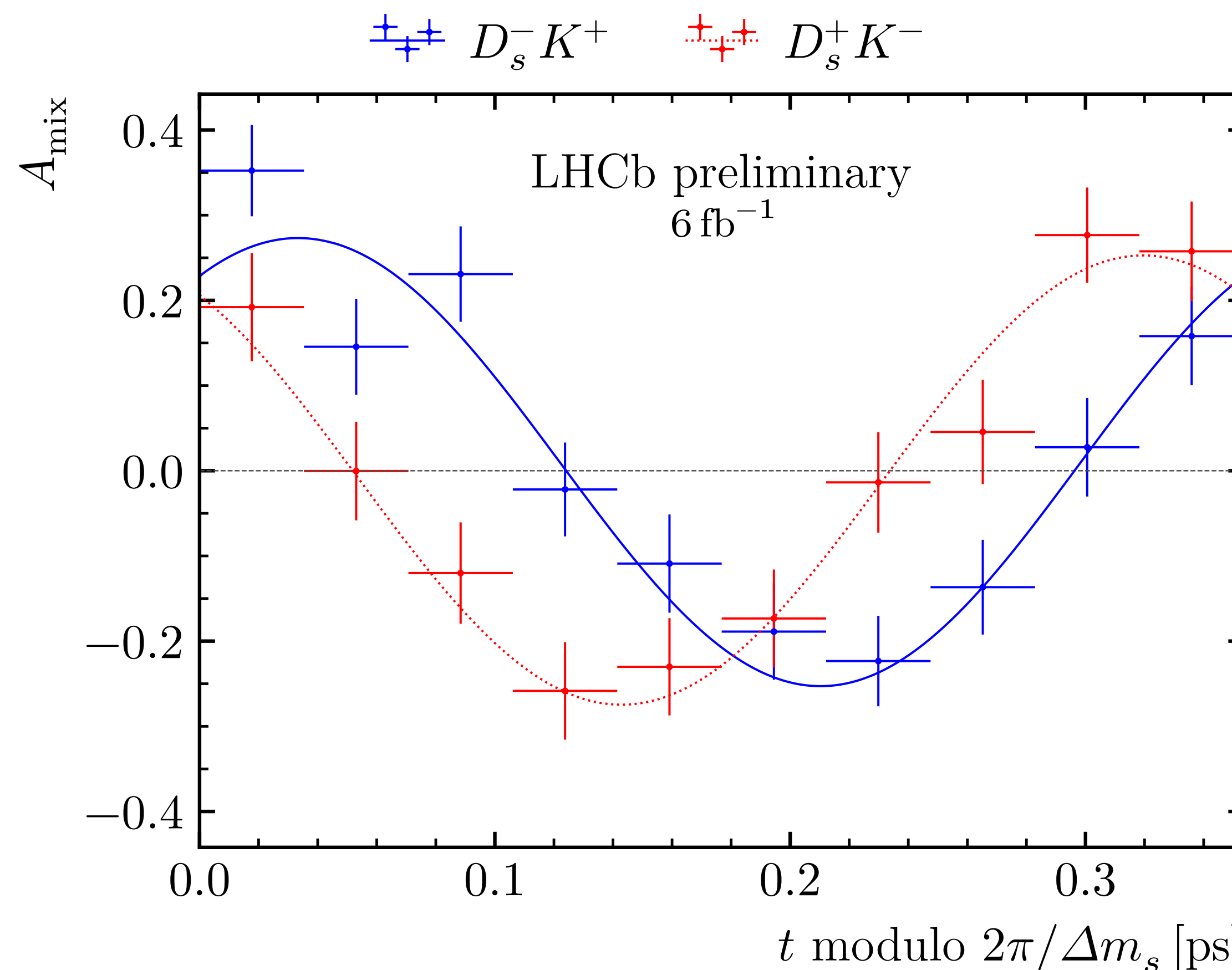
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$B_s^0 \rightarrow D_s^\mp K^\pm$ - Run2 [4] - Fit

[4] LHCb-CONF-2023-004

- **Uncertainties improved beyond statistics**
 - ▶ e.g. improvement in FT
- **Systematics also reduced**
- **Significant CP violation in the interference**
 $S_f \neq -S_{\bar{f}}$ at 8.8σ



$$C_f = 0.791 \pm 0.061 \pm 0.022$$

$$A_f^{\Delta\Gamma} = 0.051 \pm 0.134 \pm 0.037$$

$$S_f = -0.571 \pm 0.084 \pm 0.023$$

$$A_{\bar{f}}^{\Delta\Gamma} = 0.303 \pm 0.125 \pm 0.036$$

$$S_{\bar{f}} = -0.503 \pm 0.084 \pm 0.025$$

[4] LHCb-CONF-2023-004

$B_s^0 \rightarrow D_s^{\mp} K^{\pm}$ - Run2 [4] - Systematics

- **Systematics evaluated**
 - ▶ Peseudoexperiment studies
 - ▶ Data-driven approaches
 - ▶ Bootstrapping simulation

Source	C_f	$A_f^{\Delta\Gamma}$	$A_{\bar{f}}^{\Delta\Gamma}$	S_f	$S_{\bar{f}}$
Δm_s	0.007	0.004	0.004	0.108	0.103
Detection asymmetry	—	0.079	0.083	0.006	0.007
Multivariate fit	0.045	0.095	0.121	0.088	0.112
Flavour tagging	0.256	0.026	0.028	0.012	0.070
Decay-time resolution model	0.195	0.002	0.003	0.058	0.167
Decay-time bias	0.062	0.027	0.046	0.188	0.167
Decay-time acceptance, $\Gamma_s, \Delta\Gamma_s$	0.006	0.225	0.231	0.003	0.003
Decay-time acceptance ratios	0.001	0.018	0.018	—	—
Neglecting correlations	0.137	0.081	0.054	0.135	0.043
Total	0.358	0.273	0.285	0.278	0.294

- **Further checks**
 - ▶ Simulation-based closure tests
 - ▶ Analysis performed in subsamples
- **No systematic limitation expected in Run3**

$B_s^0 \rightarrow D_s^\mp K^\pm$ - Run2 [4] - Results

[4] LHCb-CONF-2023-004
[9] LHCb-PAPER-2023-016, submitted to Phys. Rev. Lett.

- Extraction of physics parameters

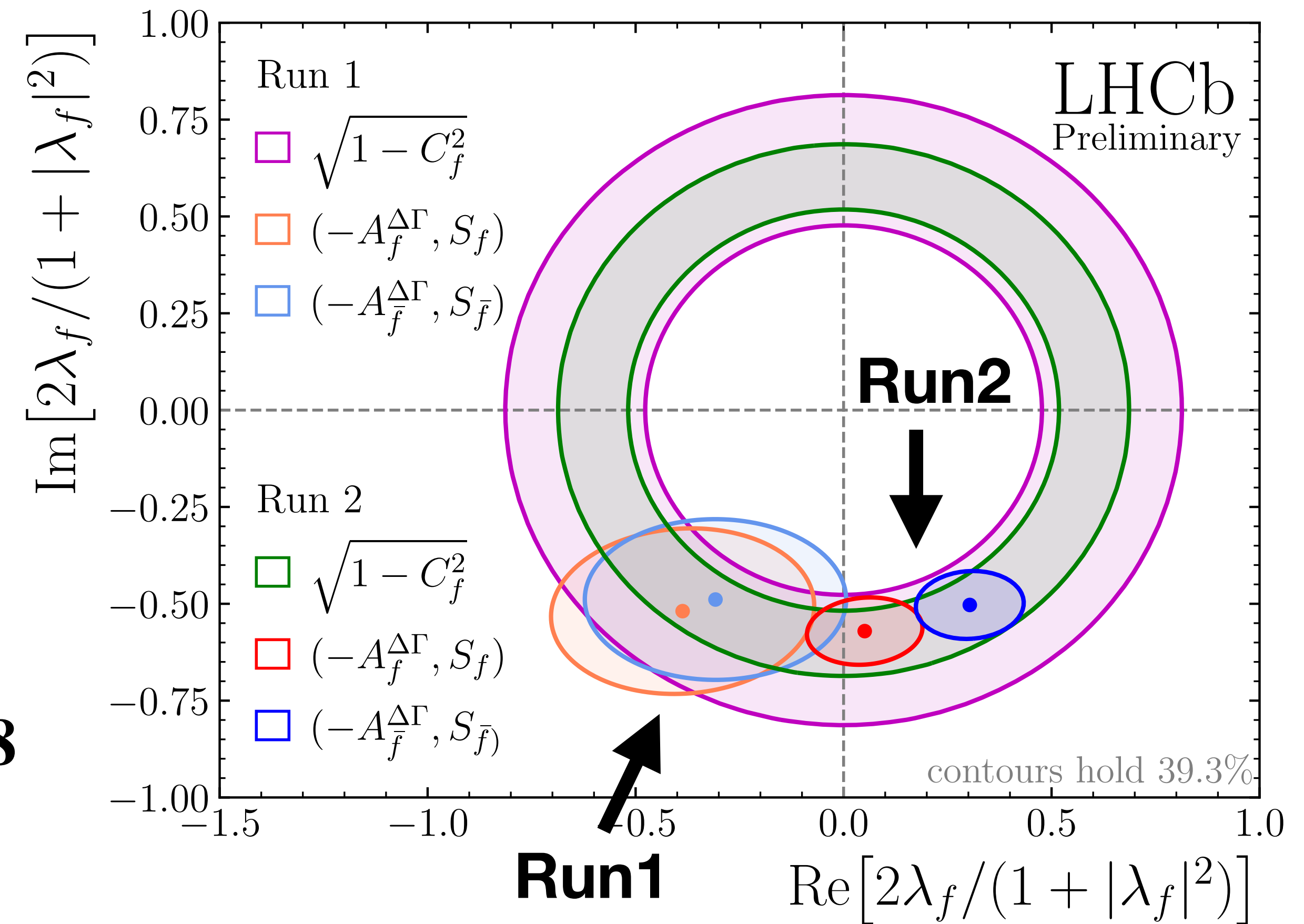
- External input [9]

$$-2\beta_s = \phi_s = (-0.031 \pm 0.018) \text{ rad}$$

- Run2 standalone result:

$$\gamma = (74 \pm 11)^\circ$$

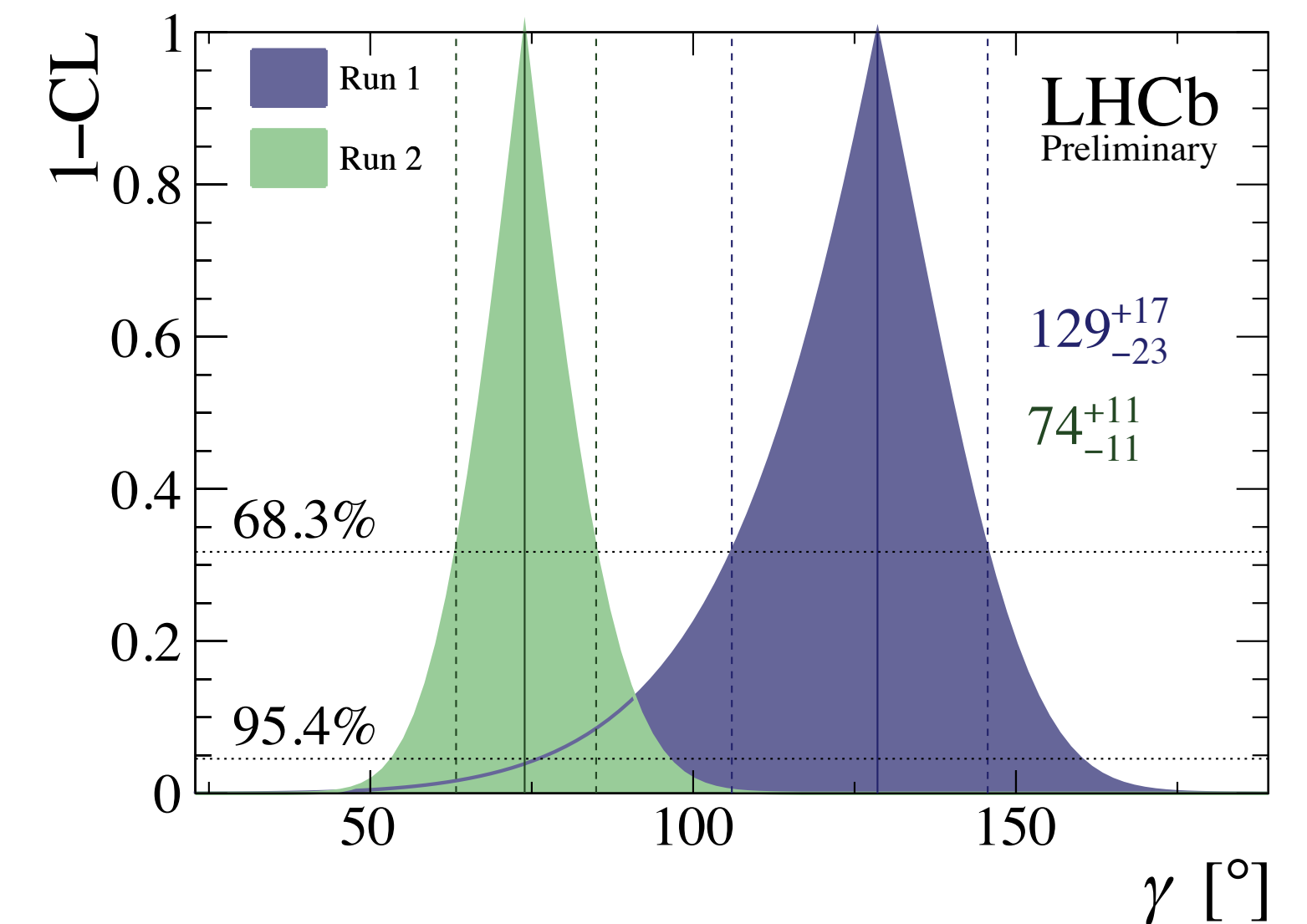
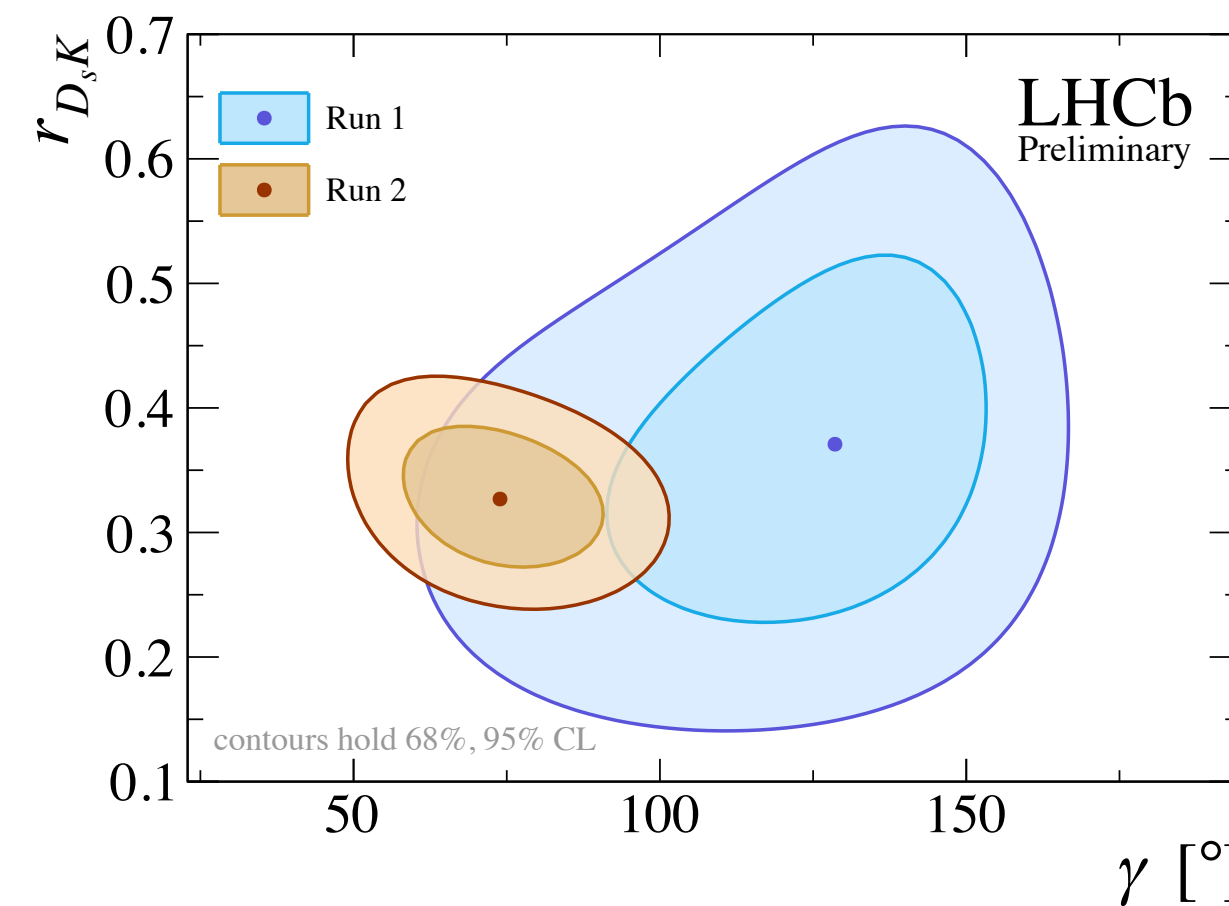
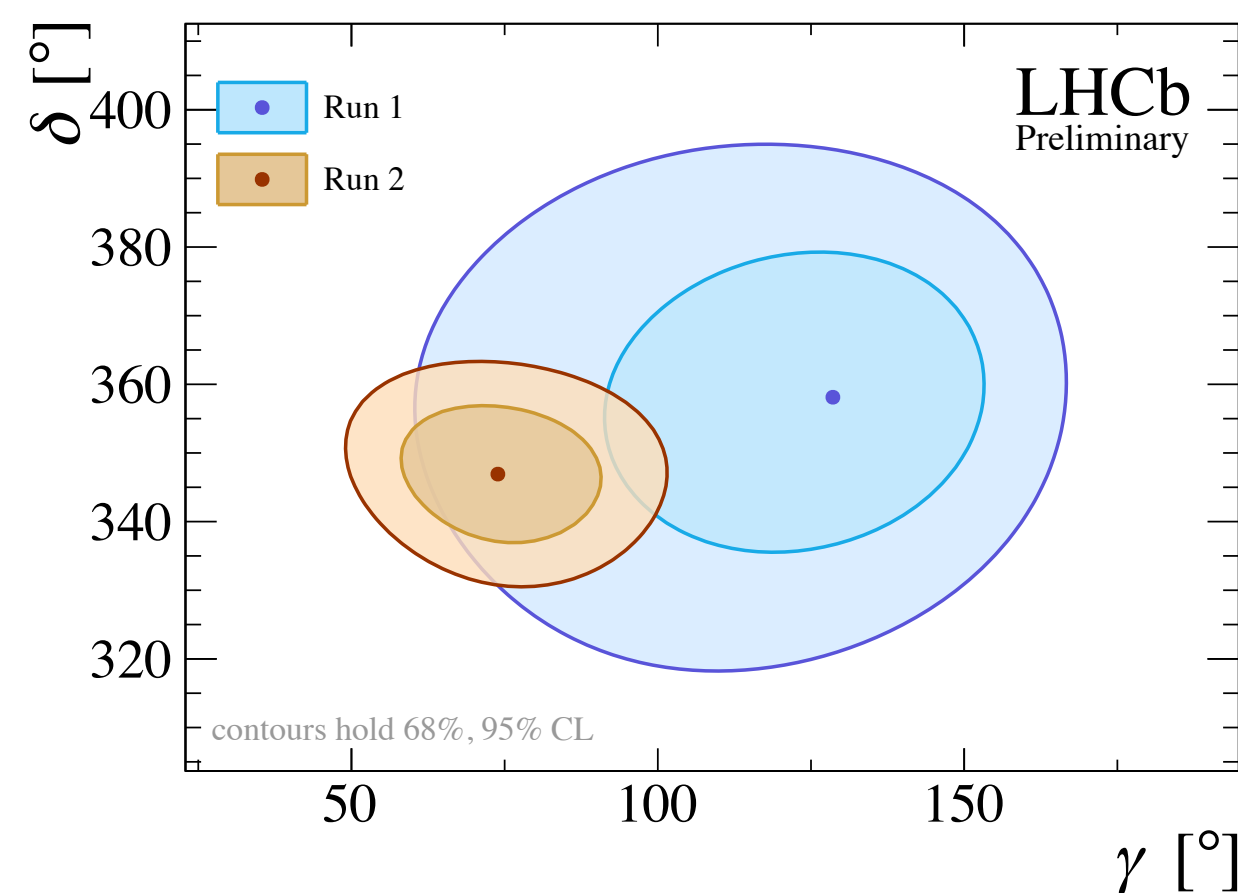
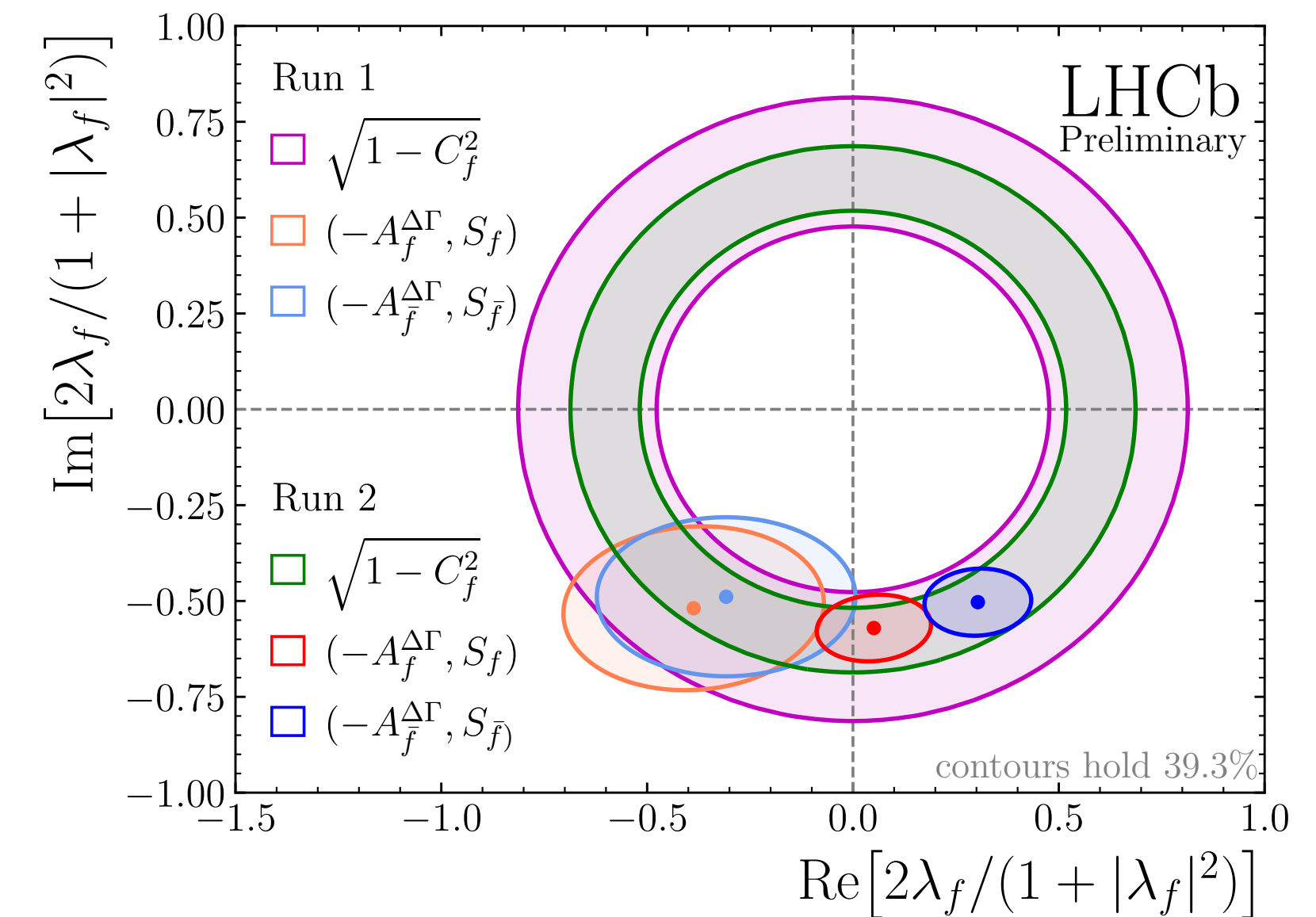
$$\delta = (346.9 \pm 6.6)^\circ \quad r_{D_s K} = 0.327 \pm 0.038$$



$B_s^0 \rightarrow D_s^\mp K^\pm$ - Run2 [4] - Results

[2] JHEP 03 (2018) 059
[4] LHCb-CONF-2023-004

- **Compatibility to Run1 [2] at 1.3σ**
 - ▶ Driven by γ at 2σ and $\text{Re}[\lambda_f]$
 - ▶ $r_{D_s K}$ and δ at 0.6σ each
- **Updated machinery reproduces Run1 result [2]**
- **Combination in preparation**



Summary

Summary

- New TD analysis of $B_s^0 \rightarrow D_s^{\mp} K^{\pm}$ decays in LHCb Run2 data set: [4]

$$\gamma_{D_s^{\mp} K^{\pm}}^{6\text{fb}^{-1}} = (74 \pm 11)^{\circ}$$

- Combinations with new result in preparation

[1] JHEP 06 (2018) 084	[2] JHEP 03 (2018) 059
[3] JHEP 03 (2021) 137	[4] LHCb-CONF-2023-004
[5] LHCb-CONF-2022-003	[6] Int. J. Mod. Phys. A 30, 1530022 (2015)
[7] Eur. Phys. J. C 73, 2431 (2013)	[8] Nat. Phys. 18, 1–5 (2022)
[9] LHCb-PAPER-2023-016, submitted to Phys. Rev. Lett. (Presentation: WG4, Mon 14:45)	
[10] Eur. Phys. J. C 82, 393 (2022)	[11] LHCb-PUB-2018-004

