

# The new $K_S \rightarrow \pi e \nu$ branching fraction measurement at KLOE

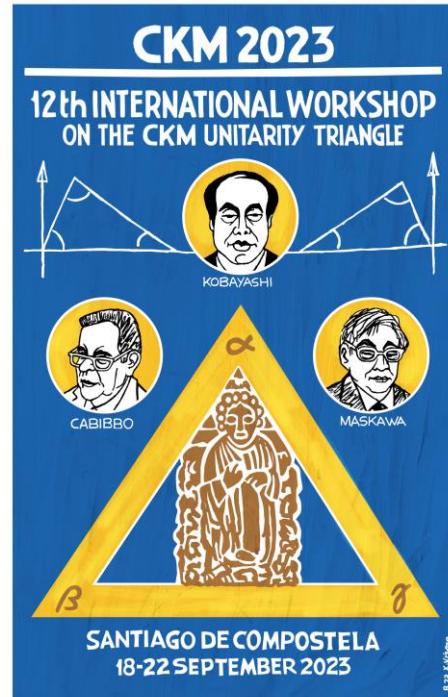
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INFN Roma Tre

on behalf of the KLOE-2 Collaboration



12° International Workshop on the CKM Unitarity Triangle  
Santiago de Compostela, 18-22 september 2023

A.Passeri - KSe3 BR measuremet at KLOE



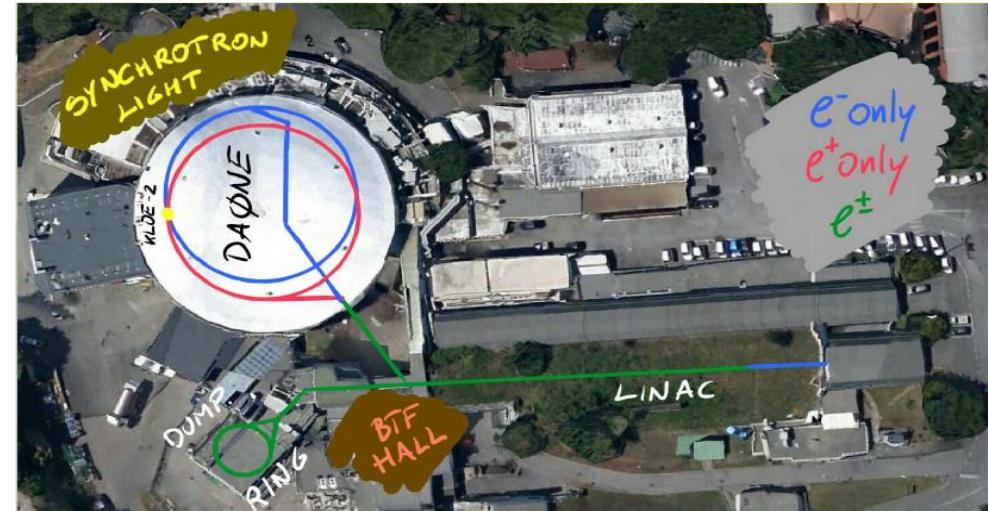
# DAΦNE and KLOE

DAΦNE is a e+e- collider @  $\sqrt{s} = 1020$  MeV,  
located in Frascati National Laboratories.

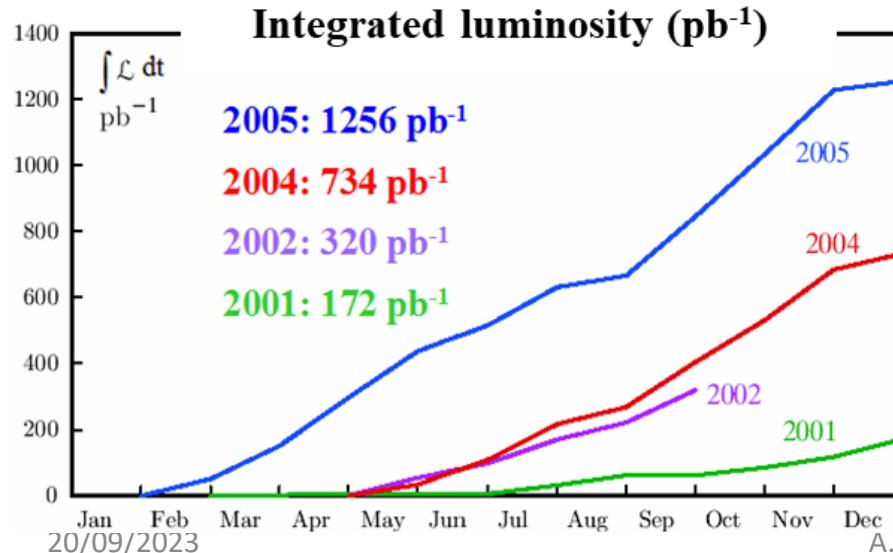
Worked for KLOE (2000-2006): Max peak lumi:  $1.5 \cdot 10^{32} \text{ cm}^{-2} \text{s}^{-1}$   
Best daily int. lumi:  $8.5 \text{ pb}^{-1}$

Upgraded in 2008 with crab-waist scheme

Worked for KLOE-2 (2014-2018): Max peak lumi:  $2.4 \cdot 10^{32} \text{ cm}^{-2} \text{s}^{-1}$   
Best daily int. lumi:  $11 \text{ pb}^{-1}$

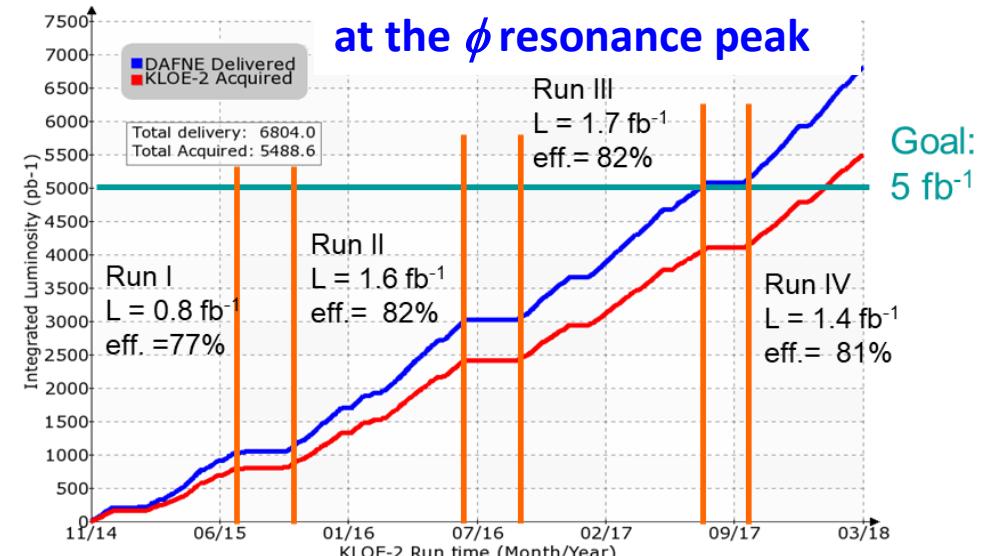


KLOE collected  $2.5 \text{ fb}^{-1}$  at the  $\phi$  resonance peak and  $250 \text{ pb}^{-1}$  at  $\sqrt{s} = 1000$  MeV.

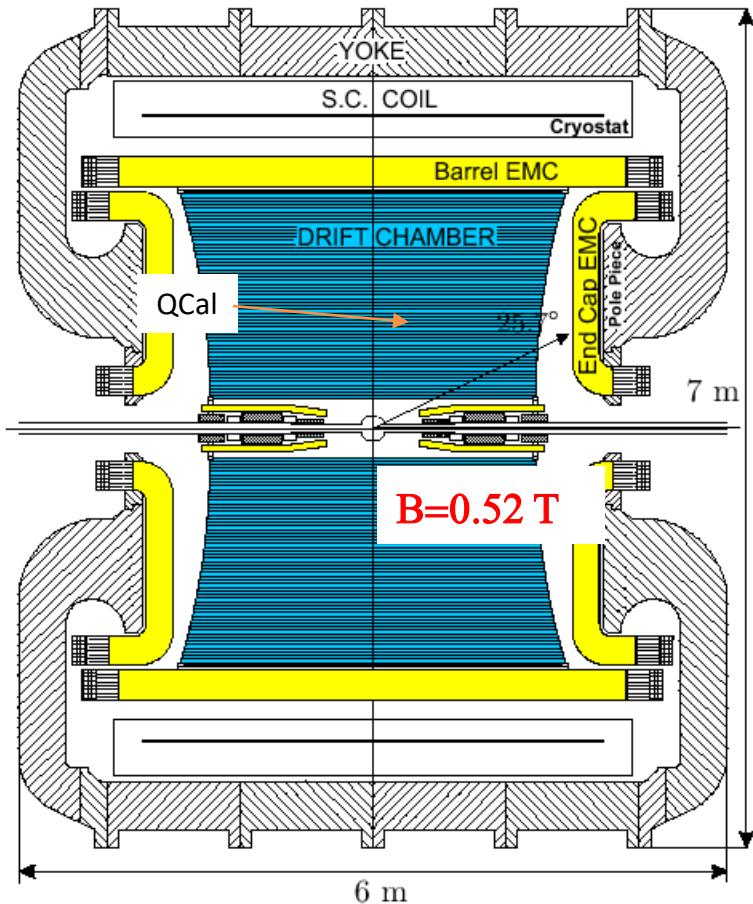


A.Passeri - KSe3 BR measurement at KLOE

KLOE-2 collected  $5.5 \text{ fb}^{-1}$  at the  $\phi$  resonance peak



# The KLOE detector



Interaction region:  
Instrument quadrupoles,  
Al-Be spherical beam pipe

Large volume Drift Chamber  
(13K cells, He gas mixt.) :

4m-Ø, 3.75m-length, all-stereo

$\sigma_p/p = 0.4\%$  (tracks with  $\theta > 45^\circ$ )

$\sigma_x^{\text{hit}} = 150 \mu\text{m}$  (xy), 2 mm (z)

$\sigma_x^{\text{vertex}} \sim 1 \text{ mm}$     $\sigma_{M\pi\pi} \sim 1 \text{ MeV}$

Pb-SciFi Calorimeter  
( barrel + endcap, 15  $X_0$  depth,  
98% solid angle coverage) :

$\sigma_E/E = 5.7\% / \sqrt{E(\text{GeV})}$

$\sigma_T = 54 \text{ ps} / \sqrt{E(\text{GeV})} \oplus 100 \text{ ps}$

• PID capabilities mostly from TOF

# The $\phi$ -factory advantage

$\phi$  decays:

$K^+K^-$  49.1%

$K_L K_S$  34.3%

$\rho\pi$  15.4%

$\eta\gamma$  1.3%

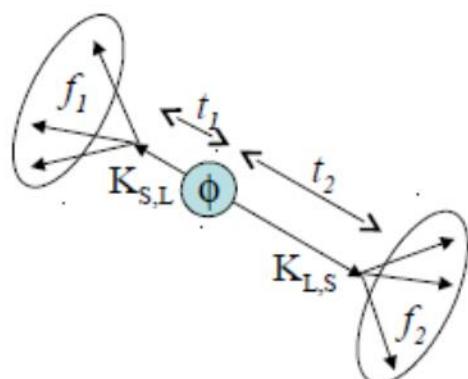
$\sigma_\phi \sim 3 \text{ } \mu\text{b} \rightarrow 10^9 \text{ neutral kaon pairs per fb}^{-1}$

- The final  $K\bar{K}$  state has the same quantum numbers as the  $\phi$  i.e. is a pure  $J^{PC} = 1^{--}$  quantum state

$$|i\rangle \propto \frac{1}{\sqrt{2}} \left( |K_L, \mathbf{p}\rangle |K_S, -\mathbf{p}\rangle - |K_L, -\mathbf{p}\rangle |K_S, \mathbf{p}\rangle \right)$$

- $P_K = -P_{\bar{K}} \sim 110 \text{ MeV/c}$
- $\lambda(K_S) = 6 \text{ mm } (\tau = 90 \text{ ps}), \lambda(K_L) = 3.5 \text{ m } (\tau = 51.7 \text{ ns})$

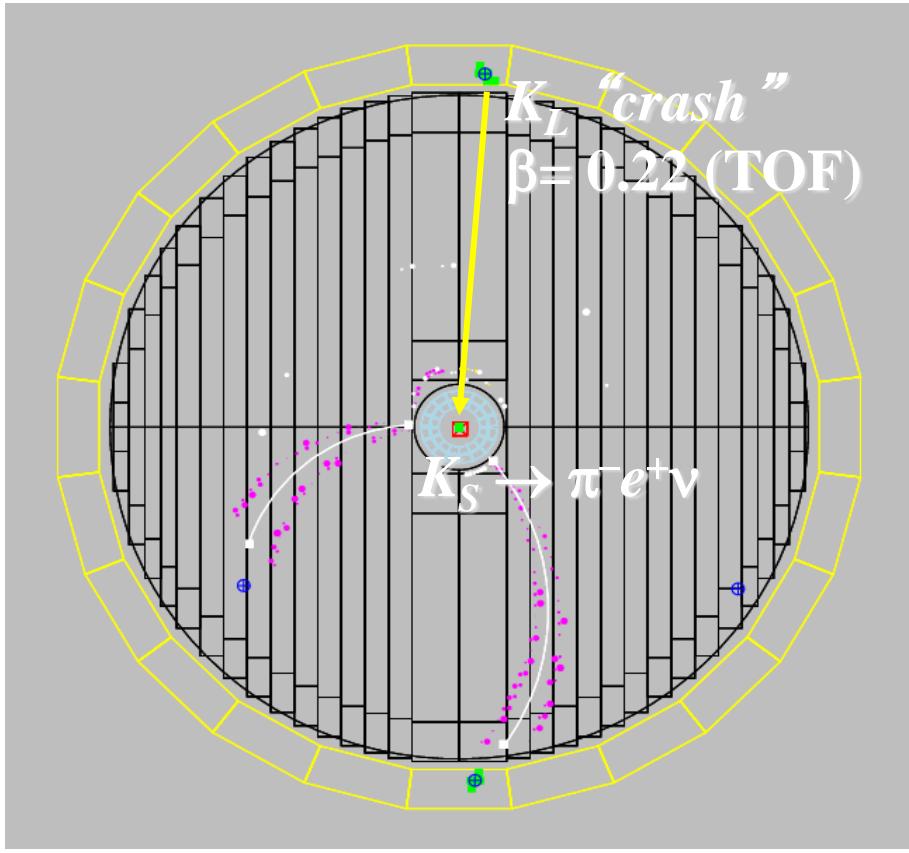
The presence of one kaon tags the other opposite one.  
All  $K_S$  decay near the i.p.



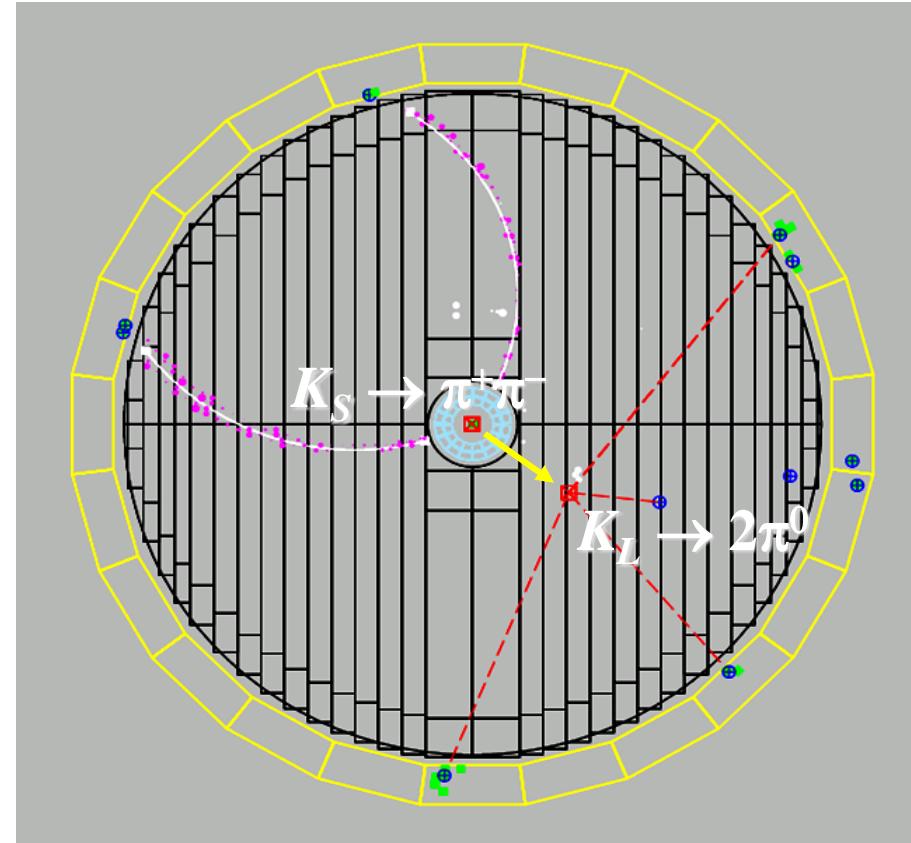
KLOE has the unique capability of selecting pure  $K_S$  and  $K_L$  beams

Moreover: interference pattern and entanglement of  $K_S K_L$  state allows to study fundamental symmetries and quantum mechanics

# Neutral kaon tagging at KLOE



**$K_S$  tagged by  $K_L$  interaction in EmC**  
 $K_L$  velocity in  $\phi$  rest frame  $\beta^* = 0.218$   
Efficiency  $\sim 30\%$  (largely geometrical)  
 $K_S$  angular resolution:  $\sim 1^\circ$  ( $0.3^\circ$  in  $\phi$ )  
 $K_S$  momentum resolution:  $\sim 2$  MeV



**$K_L$  tagged by  $K_S \rightarrow \pi^+ \pi^-$  vertex at IP**  
Efficiency  $\sim 70\%$  (mainly geometrical)  
 $K_L$  angular resolution:  $\sim 1^\circ$   
 $K_L$  momentum resolution:  $\sim 2$  MeV

# The KSe3 decay and the Cabibbo angle

In the SM :

$$\mathcal{B}(K_S \rightarrow \pi \ell \nu) = \frac{G^2 (f_+(0) |V_{us}|)^2}{192\pi^3} \tau_S m_K^5 I_K^\ell S_{\text{EW}} (1 + \delta_{\text{EM}}^{K\ell})$$

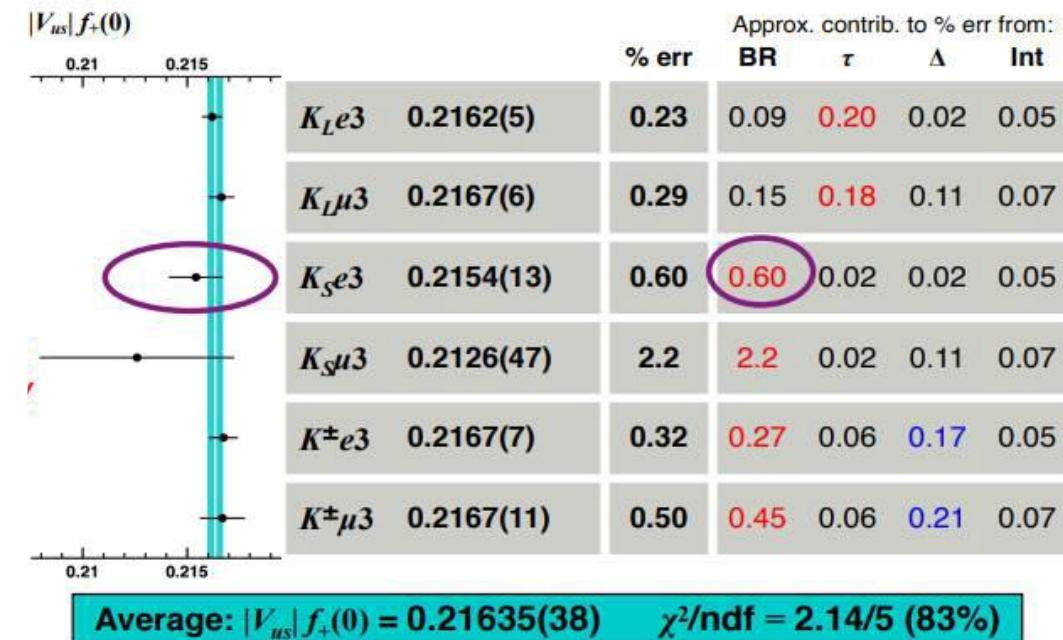
The KSe3 determination of  $|V_{us}| f_+(0)$  is the less accurate (apart from the recently measured and rarer  $K\mu 3$  mode Phys.Lett.B 804 (2020) 135378 ).

The presently available BR(KSe3) value is dominated by the KLOE measurement based on  $0.4 \text{ fb}^{-1}$  data sample:

$$\text{BR}(K_S \rightarrow \pi e \nu) = (7.046 \pm 0.078 \pm 0.049) \times 10^{-4}$$

PLB 636 (2006) 173

1.4% total uncertainty (1.1% stat  $\pm$  0.7% syst)



We present here a new measurement based on  $1.63 \text{ fb}^{-1}$  independent KLOE data sample.

M.Moulson and E.Passemar, CKM 2021

## What we measure

$$\mathcal{R} = \frac{\Gamma(K_S \rightarrow \pi e \nu)}{\Gamma(K_S \rightarrow \pi^+ \pi^-)} = \frac{N_{\pi e \nu}}{\epsilon_{\pi e \nu}} \times \frac{\epsilon_{\pi \pi}}{N_{\pi \pi}} \times R_\epsilon$$

$N_{\pi e \nu}, N_{\pi \pi}$ : number of selected events for  $K_S \rightarrow \pi e \nu$  and  $K_S \rightarrow \pi^+ \pi^-$

$\epsilon_{\pi e \nu}, \epsilon_{\pi \pi}$ : selection efficiencies

$R_\epsilon$ : ratio of common efficiencies for trigger, online filter, event classification and preselection

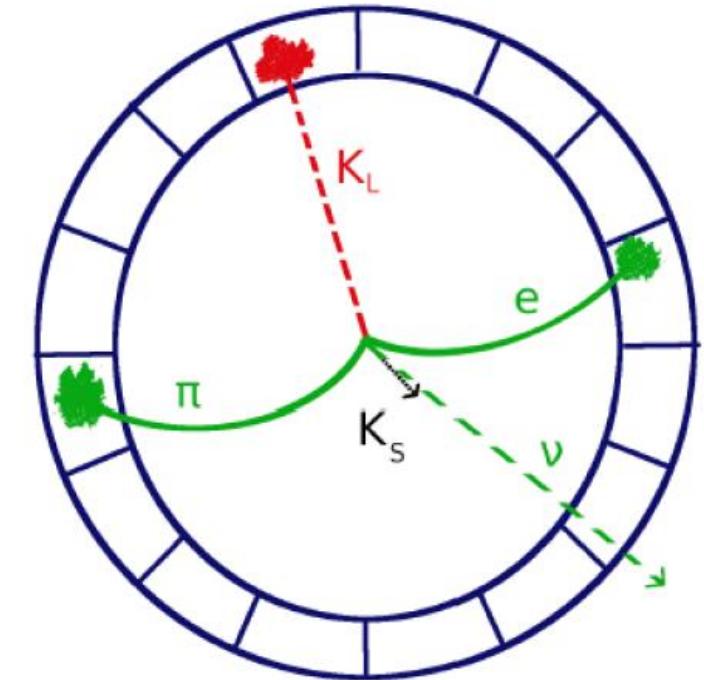
# Preselection and normalization sample

## $K_L$ -crash:

- one neutral cluster with  $E > 100$  MeV and polar angle  $15^\circ < \theta < 165^\circ$
- velocity  $0.17 < \beta^* < 0.28$  in the  $\phi$  c.m.s. (in the lab:  $\beta = r_{\text{clu}}/\text{ct}_{\text{clu}}$ )

## $K_S$ side selection:

two charged tracks of opposite curvature forming a vertex inside the cylinder ( $\rho < 5$  cm ;  $z < 10$  cm)



The normalization sample of  $K_S \rightarrow \pi^+ \pi^-$  decays is selected at this stage by requiring each of the two charged tracks momentum to be  $140 \text{ MeV} < p < 280 \text{ MeV}$ . We obtain:

$$N_{\pi\pi} = (282.314 \pm 0.017) \times 10^6 \text{ events}$$

Efficiency 97.4 and purity 99.9% determined by simulation.

# Sample composition after preselection

	n. events	Fraction (%)
Data	301 645 500	
MC	312 018 500	
$K_S \rightarrow \pi \nu \bar{\nu}$	259 264	0.08
$K_S \rightarrow \pi^+ \pi^-$	301 976 400	96.78
$\phi \rightarrow K^+ K^-$	9 565 465	3.07
$K_S \rightarrow \pi^0 \pi^0$	30 353	0.01
$K_S \rightarrow \pi \mu \nu$	139 585	0.04
$K_S \rightarrow \pi^+ \pi^- e^+ e^-$	18 397	$6 \cdot 10^{-3}$
$\phi \rightarrow \pi^+ \pi^- \pi^0$	24 153	$8 \cdot 10^{-3}$
others	4 852	$2 \cdot 10^{-3}$

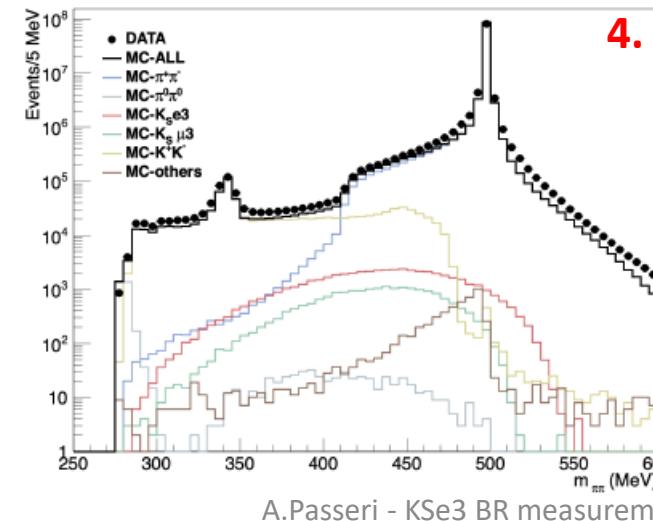
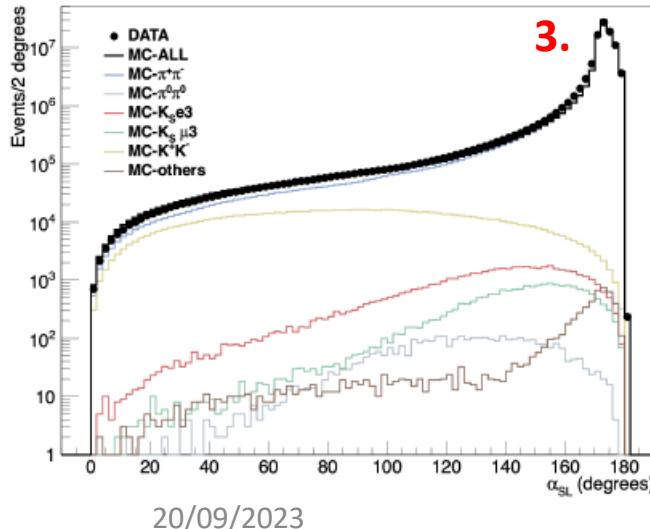
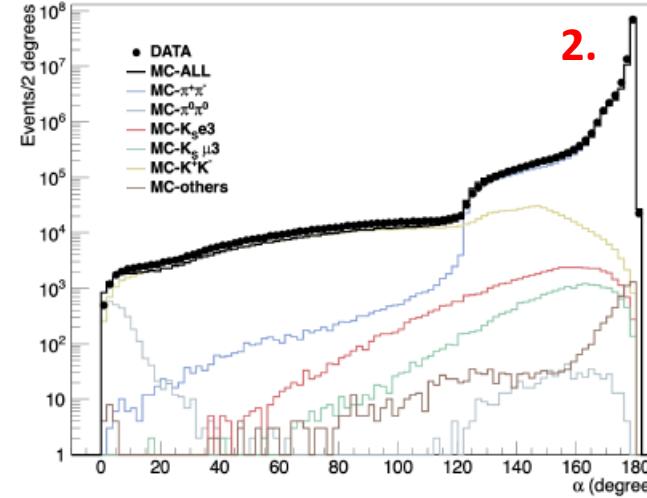
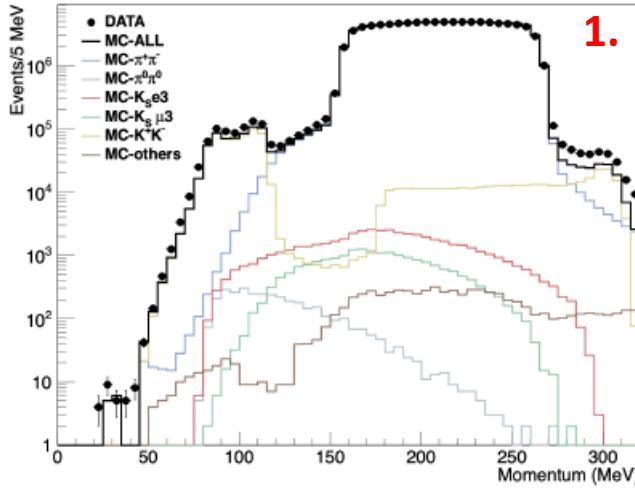
Signal selection is then performed in two steps based on uncorrelated information:

1) the event kinematics using only DC tracking variables

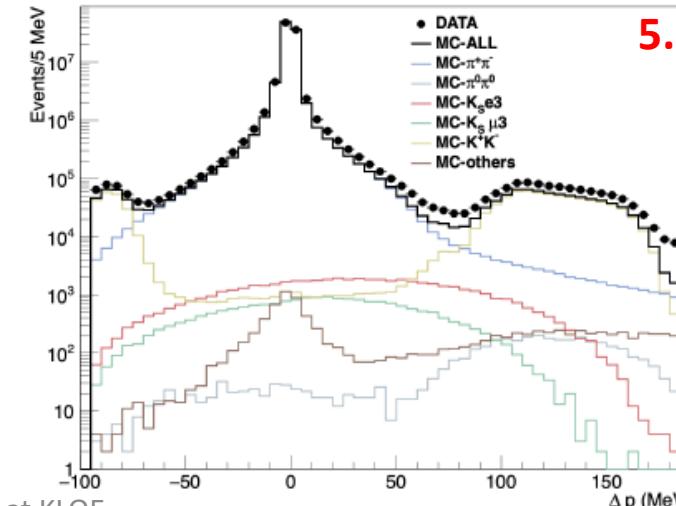
2) the time-of-flight measured with the calorimeter

# Multivariate selection based on tracking variables/1

5 discriminating variables are selected. In the signal region they show satisfactory data-MC agreement



1. the tracks momenta:  $\vec{p}_1, \vec{p}_2$
2.  $\alpha_{1,2}$  angle formed by tracks momenta in the  $K_S$  reference system
3.  $\alpha_{LS}$  angle between the total momentum and the  $K_L$  crash direction
4.  $m_{\pi\pi}$  the 2 tracks invariant mass in 2 pion hypothesis
5.  $\Delta p$  difference between total momentum and  $|p_{K_S}|$  (determined from  $p_{KL}$  and  $p_\phi$ )

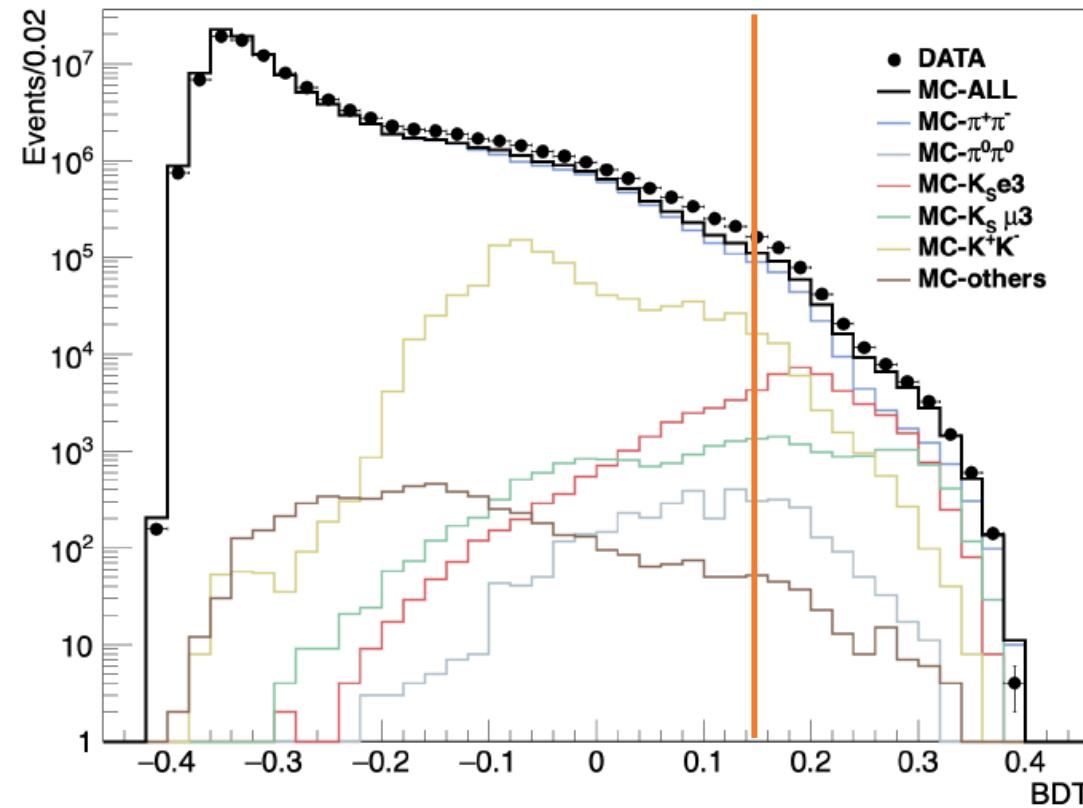


## Multivariate selection based on tracking variables/2

BDT classifier trained on 5000 signal events and 50000 background simulated events

Tested on same size samples and run over the both full data and MC samples.

Events with BDT output > 0.15 are retained  
to reduces main backgrounds from charged  
kaons and  $K_S \rightarrow \pi\pi$



# Time of flight selection/1

Track-to-cluster association (TCA) is required for both tracks:

clusters must have  $E_{\text{clu}} > 20 \text{ MeV}$ ,  $\theta_{\text{clu}} > 15^\circ$ , centroid within 30 cm of the track extrapolation.

For each track:

$$\delta t_i = t_{\text{clu},i} - L_i/c\beta_i(m_i)$$

$$L_i \text{ track length, } \beta_i = p_i/\sqrt{p_i^2 + m_i^2}$$

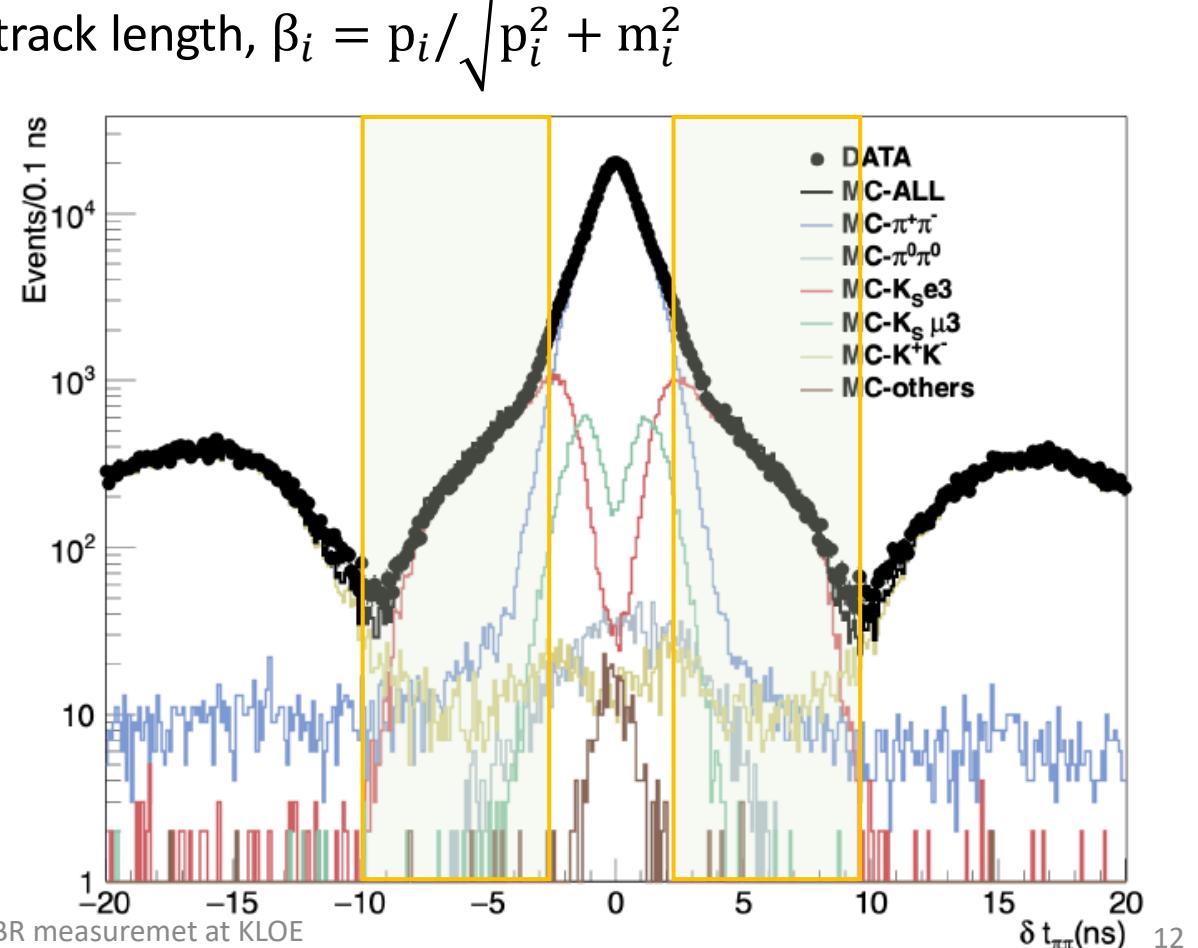
Correct mass hypothesis yields null  $\delta t_i$

$\delta t = \delta t_1 - \delta t_2$  minimize event  $T_0$  uncertainty

Test of the  $\pi\pi$  hypothesis:

$$\delta t_{\pi\pi} = \delta t_{1,\pi} - \delta t_{2,\pi}$$

Selection applied:  $2.5 \text{ ns} < |\delta t_{\pi\pi}| < 10 \text{ ns}$



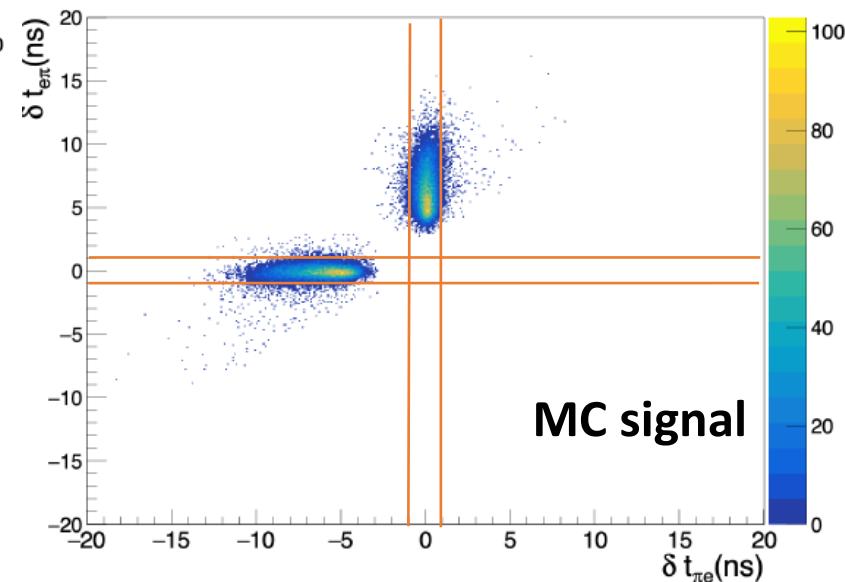
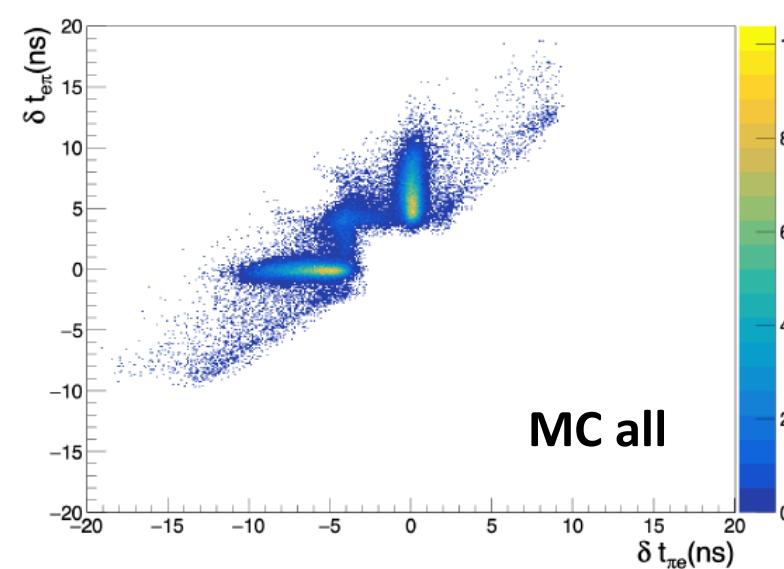
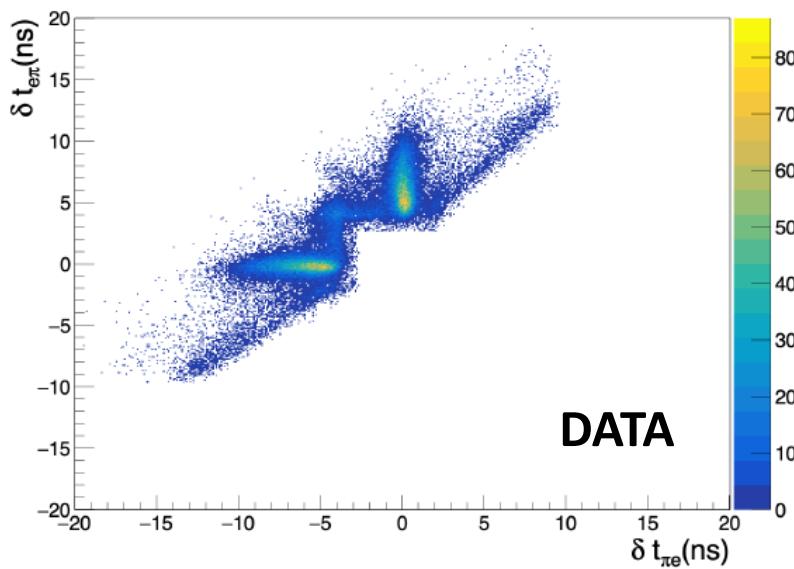
# Time of flight selection/2

Test of  $\pi e$  vs  $e\pi$  hypotheses:

$$\delta t_{\pi e} = \delta t_{1,\pi} - \delta t_{2,e} \quad \text{vs} \quad \delta t_{e\pi} = \delta t_{1,e} - \delta t_{2,\pi} \quad (\text{random track ordering})$$

Lowest  $|\delta t|$  is chosen as the correct hypothesis  $\delta t_e$

$|\delta t_e| < 1 \text{ ns}$  is required



# Signal extraction

Selected sample is now signal dominated.  
 $m_e^2$  distribution is used to fit number of events:

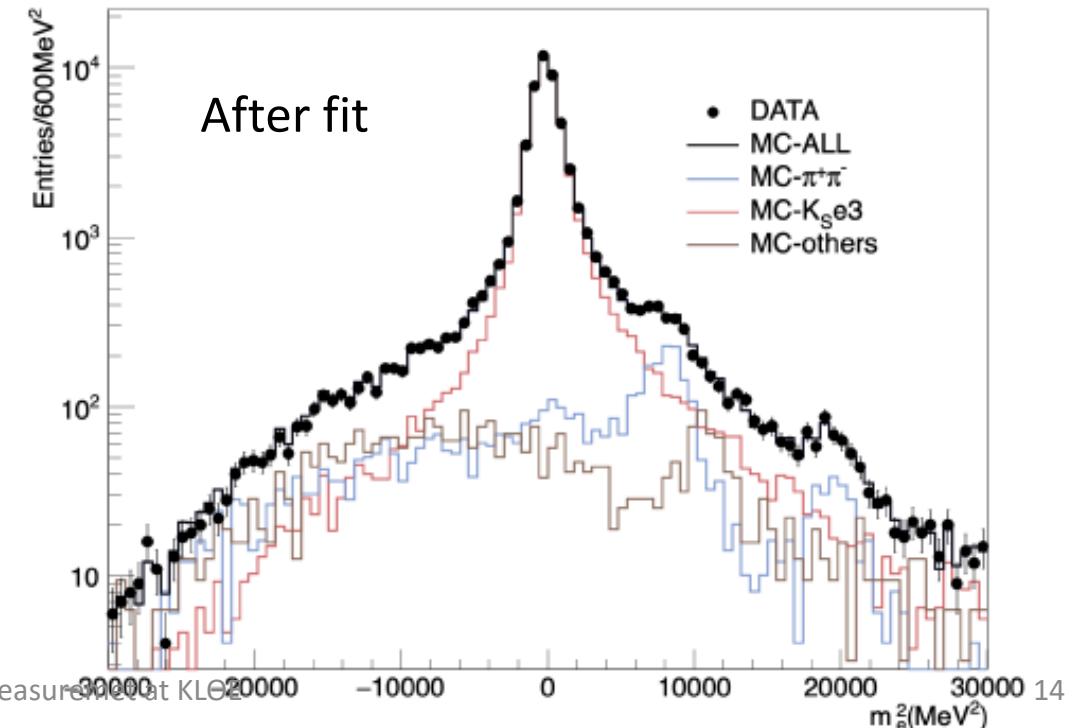
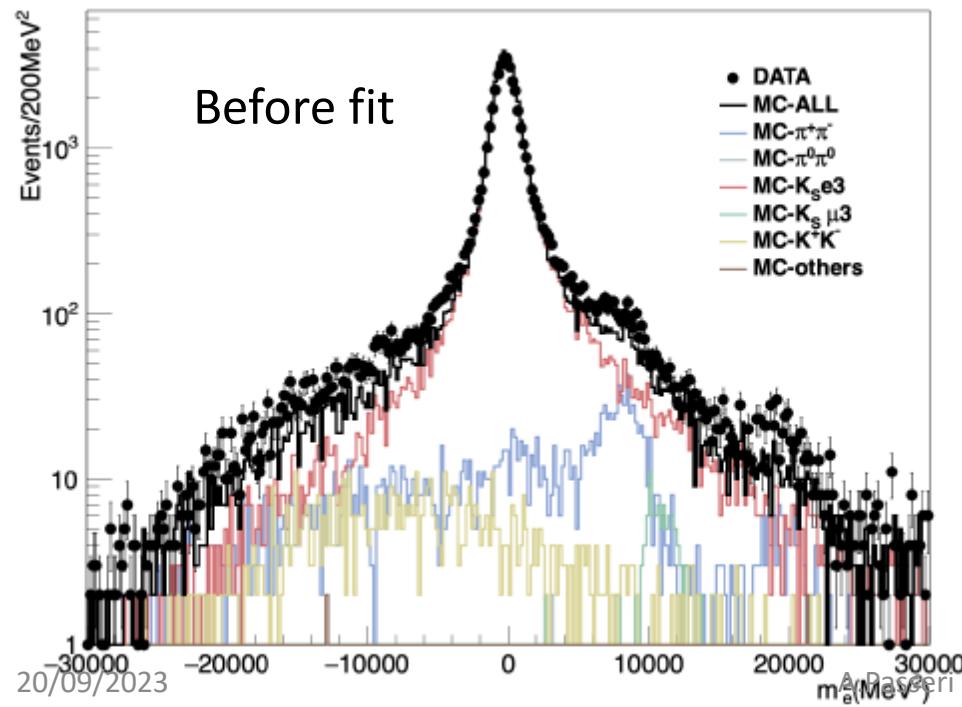
$$m_e^2 = (E_{KS} - E_\pi - p_{miss})^2 - p_e^2 \quad (E_{KS} \text{ and } p_{KS} \text{ from KL-crash})$$

Fit with 3 components ( $\pi ev$ ,  $\pi\pi$ , others) yields:

$$N_{\pi ev} = 49647 \pm 316$$

$$\chi^2 / \text{ndf} = 76/96$$

	n. events	Fraction (%)
Data	57577	
MC	56843	
$K_S \rightarrow \pi ev$	<b>53559</b>	<b>94.22</b>
$K_S \rightarrow \pi^+\pi^-$	2175	3.83
$\phi \rightarrow K^+K^-$	903	1.59
$K_S \rightarrow \pi\mu\nu$	136	0.24
others	70	0.12



# Evaluation of efficiencies

The  $K_L \rightarrow \pi^+ \pi^- \nu \bar{\nu}$  control sample (CS) allows to determine efficiencies from data:

$$\epsilon_{\pi e \nu} = \epsilon_{\text{CS}} \times \frac{\epsilon_{\pi e \nu}^{\text{MC}}}{\epsilon_{\text{CS}}^{\text{MC}}}$$

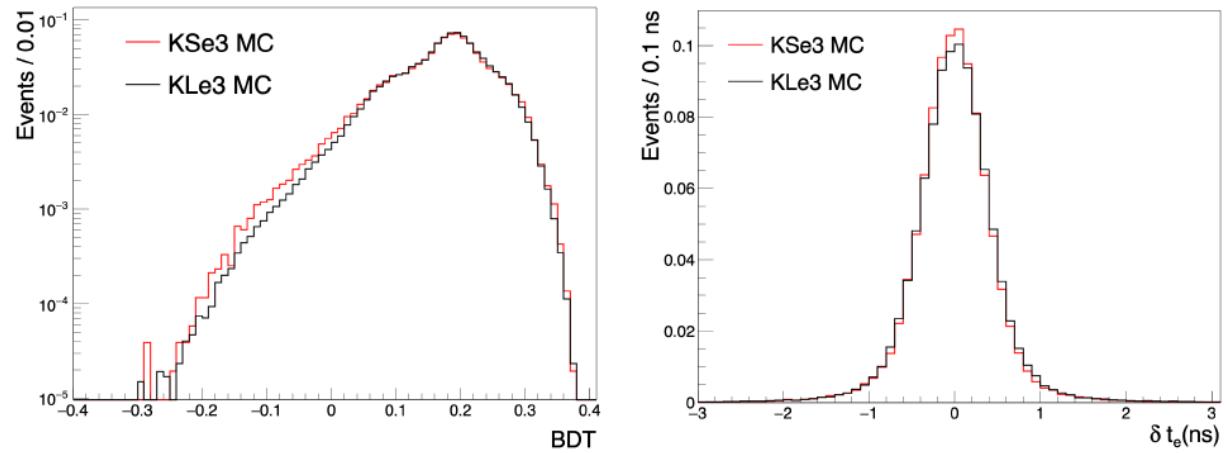
CS Selected by  $K_S$  tag, requiring  $K_L$  decay radius in the range (1 cm, 5 cm). Missing mass cut discards  $\pi^+ \pi^- \pi^0$  component.

Two high purity (>95%) CS are built by cutting on TOF variables (for  $\epsilon_{\text{kine}}$  evaluation) or kine variables (for  $\epsilon_{\text{t0f}}$  evaluation).

Good comparison of CS and signal samples observed in MC

We obtain:

Selection	Efficiency
Preselection (from MC)	$0.9961 \pm 0.0002$
Kin. variables selection	$0.9720 \pm 0.0007$
BDT selection	$0.6534 \pm 0.0013$
TCA selection	$0.4639 \pm 0.0009$
TOF selection	$0.6605 \pm 0.0012$
Total	$0.1938 \pm 0.0006$



The  $K_S \rightarrow \pi^+ \pi^-$  selection efficiency is evaluated from the preselected sample with 2 methods and their difference is used as systematics. We get:

$$\epsilon_{\pi\pi} = (96.657 \pm 0.002) \%$$

From simulation:  $R_\epsilon = 1.1882 \pm 0.0012$

## Systematic uncertainty

BDT cut is varied in the range (0.135,0.17) and good  $N_{\pi e \nu}$  stability is observed. Spread is used as uncertainty.

TCA checked in CS.  $\delta t$  resolution checked to be identical in signal and control samples.

Lower  $\delta t_{\pi\pi}$  cut varied in (2-3 ns) range,  $|\delta t_e|$  cut varied in (0.8-1.2 ns) range.

$m_e^2$  fit repeated varying range and bin width. Separate components for  $K_S \mu 3$  and  $\phi \rightarrow K^+ K^-$  backgrounds are tested.

Selection	$\delta \epsilon_{\pi e \nu}^{\text{syst}} [10^{-4}]$	$\delta \epsilon_{\pi^+ \pi^-}^{\text{syst}} [10^{-4}]$
BDT selection	5.3	
TCA & TOF selection	6.0	
Fit parameters	3.0	
$K_S \rightarrow \pi^+ \pi^-$ efficiency		8.8
Total	8.5	8.8

$R_\varepsilon$  systematics evaluated to be 0.48% by comparing data and MC for each of the included common selections

# Result

$$N_{\pi e\nu} = 49647 \pm 316$$

$$N_{\pi\pi} = (282.314 \pm 0.017) \times 10^6$$

$$\epsilon_{\pi^+\pi^-} = (96.657 \pm 0.088)\%$$

$$\epsilon_{\pi e\nu} = (19.38 \pm 0.10)\%$$

$$R_\epsilon = 1.1882 \pm 0.0059$$

Including  
systematics

$$\mathcal{R} = \frac{\Gamma(K_S \rightarrow \pi e\nu)}{\Gamma(K_S \rightarrow \pi^+ \pi^-)} = \frac{N_{\pi e\nu}}{\epsilon_{\pi e\nu}} \times \frac{\epsilon_{\pi\pi}}{N_{\pi\pi}} \times R_\epsilon$$

**New KLOE result:**

$$\mathcal{R} = (1.0421 \pm 0.0066_{\text{stat}} \pm 0.0075_{\text{syst}}) \times 10^{-3}$$

**Previous KLOE result:** 0.41 fb<sup>-1</sup> independent data sample. Phys.Lett. B **636** (2006) 173

$$\mathcal{R} = (1.019 \pm 0.011_{\text{stat}} \pm 0.007_{\text{syst}}) \times 10^{-3}$$

**Systematics correlation factor between the two measurements is 12%, due to the determination of the preselection and time of flight efficiencies. Combination yields:**

$$\mathcal{R} = (1.0338 \pm 0.0054_{\text{stat}} \pm 0.0064_{\text{syst}}) \times 10^{-3}$$

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## KSe3 Branching Ratio and $V_{us}$

- Using the value:  $BR(K_S \rightarrow \pi^+ \pi^-) = 0.69196 \pm 0.00051$  measured by KLOE **Eur. Phys. J. C 48 (2006) 767**  
We obtain:

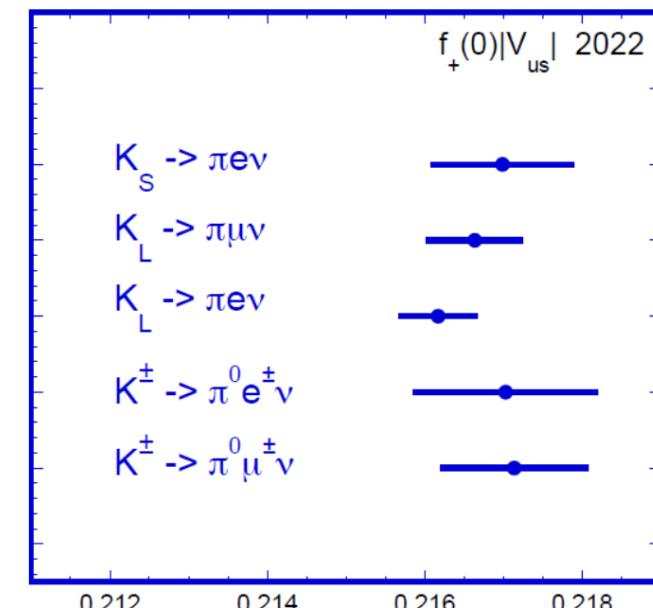
$$\mathcal{B}(K_S \rightarrow \pi e \nu) = (7.153 \pm 0.037_{\text{stat}} \pm 0.044_{\text{syst}}) \times 10^{-4} = (7.153 \pm 0.058) \times 10^{-4}$$

- Using the SM formula:  $\mathcal{B}(K_S \rightarrow \pi \ell \nu) = \frac{G^2(f_+(0)|V_{us}|)^2}{192\pi^3} \tau_S m_K^5 I_K^\ell S_{\text{EW}} (1 + \delta_{\text{EM}}^{K\ell})$

and taking the PDG values for  $\tau_S$  and  $m_K$  and the most recent calculations of the theoretical correction factors (Phys.Rev.D 105, (2022) 013005) we obtain:

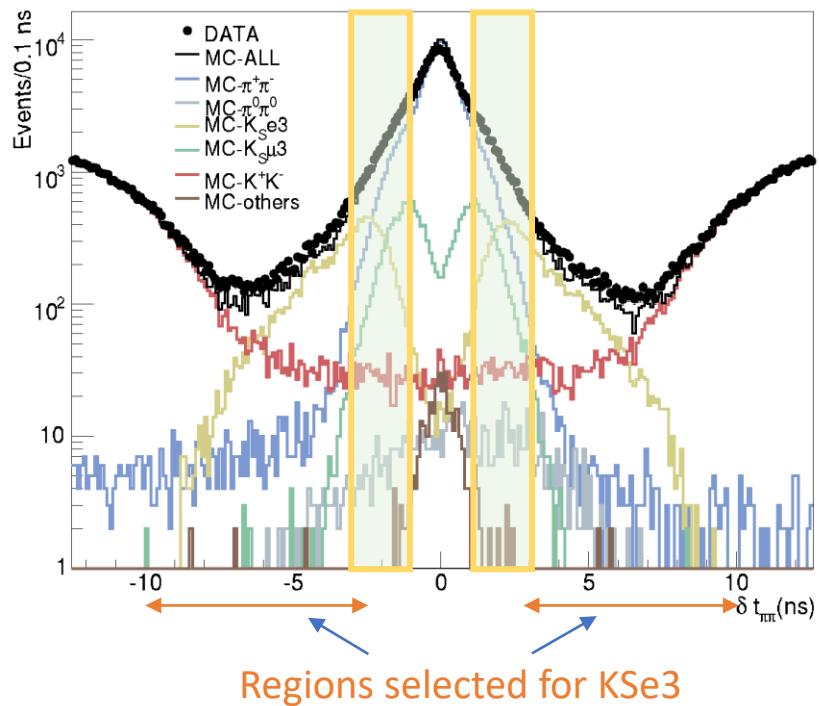
$$f_+(0)|V_{us}| = 0.2170 \pm 0.0009$$

Accuracy better than the one reached  
with charged kaon semileptonic decays



# A brief K $\mu$ 3 reminder

PLB 804 (2020) 135378



Regions selected for KSe3

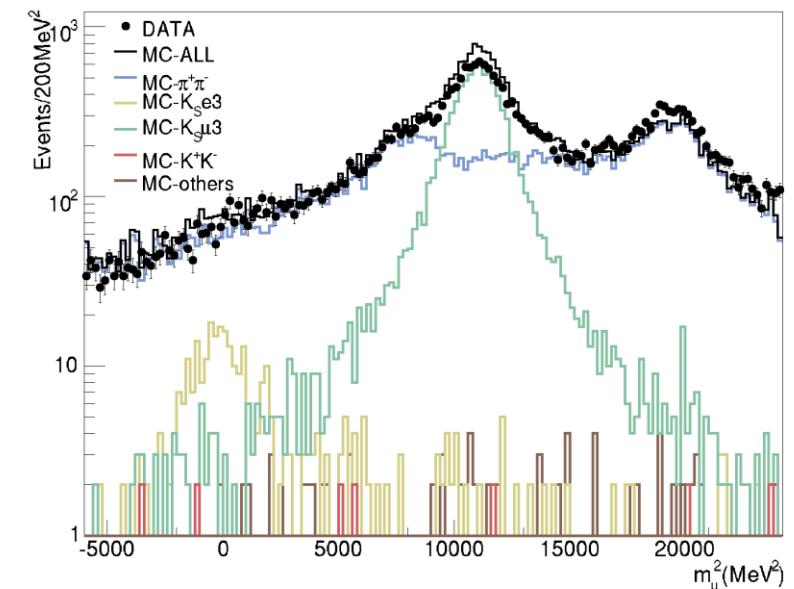
Same analysis technique as KSe3:

- Different  $\delta t_{\pi\pi}$  selection window  $1 \text{ ns} < |\delta t_{\pi\pi}| < 3 \text{ ns}$
- Cut on  $|\delta t_\mu| < 0.5$  and fit to  $m_\mu^2$  distribution
- Similar efficiency and systematics estimation via control sample

First ever measurement of this decay:

$$\mathcal{R}_\mu = (6.59 \pm 0.28) \times 10^{-4}$$

Partial anti-correlation with KSe3 measurement to be quantified



# Conclusions

The KLOE experiment has performed a new measurement of the  $K_s \rightarrow \pi e \nu$  branching fraction based on a 1.63 fb-1 data sample collected in 2004-05, with a < 1% overall uncertainty.

**Combination with the previous KLOE measurement yields a new determination of ( $K_s \rightarrow \pi e \nu$ ) branching fraction with 0.8% precision.**

The corresponding estimate of  $f_+(0)x|V_{us}|$  is competitive with those obtained by other K semileptonic decays

The sum of the four main  $K_s$  branching ratios measured by KLOE yields:

$$B_{\pi^+\pi^-} + B_{\pi^0\pi^0} + B_{\pi e \nu} + B_{\pi \mu \nu} > 0.9983 \text{ @95% CL}$$

# **SPARES**

## R <sub>$\epsilon$</sub> components from MC

Selection	$R_\epsilon = (\epsilon_{\pi\pi}/\epsilon_{\pi e \nu})_{\text{com}}$
Trigger	$1.0297 \pm 0.0003$
On-line filter	$1.0054 \pm 0.0001$
Event classification	$1.0635 \pm 0.0004$
T0 time	$1.0063 \pm 0.0001$
$K_L$ -crash	$1.0295 \pm 0.0010$
$K_S$ vertex reconstr.	$1.0418 \pm 0.0009$
$R_\epsilon$	$1.1882 \pm 0.0017$

## $\delta t_e$ resolution for signal and control sample

