# Measurement of the CP violating phase $\phi_s$ and $\phi_s^{sq\bar{q}}$ at LHCb

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Centro Brasileiro de **Pesquisas Físicas** 

# Introduction

- goals of the LHCb experiment Probe to physics beyond the Standard Model (SM).
- $\bullet \phi_s$  is related to the interference of  $B_s^0$  mixing and decay amplitudes

$$\phi_s^{SM} \equiv -2\beta_s = -2arg(-\frac{1}{\sqrt{2}})$$

Neglecting penguin diagram contributions, PhysRevD.91.073007

**Experimentally, can be accessed via the time-dependent asymmetries** 

$$\mathscr{A}_{CP}(t) = \frac{\Gamma_{\overline{B}_s^0}(t) - \Gamma_{B_s^0}(t)}{\Gamma_{\overline{B}_s^0}(t) + \Gamma_{B_s^0}(t)} = \frac{S_f \sin(\Delta m_s t) - C_f \cos(\Delta m_s t)}{\cosh(\frac{\Delta \Gamma_s t}{2}) + A^{\Delta \Gamma} \sinh(\frac{\Delta \Gamma_s t}{2})},$$

• The measurement of the mixing-induced CP-violating phase  $\phi_s$  in the  $B_s^0 - \bar{B}_s^0$  system is one of the key

 $\frac{-V_{ts}V_{tb}^*}{V_{cs}V_{cb}^*}),$ 

Predicted to be very precise

**Parameters** 

 $C_f$ : Direct CP asymmetry  $S_f$  and  $A^{\Delta\Gamma}$ : Mixing induced CP asymmetries  $\Gamma_{B_{s}^{0}(\bar{B_{s}^{0}})}$ : Time-dependent decay rate  $\Delta \Gamma_s \equiv \Gamma_L - \Gamma_H$ : Difference in the decay width between two mass eigenstates,  $B_L$  and  $B_H$  $\Delta m_s \equiv m_H - m_L$ : Mass difference



# Introduction

 ${ullet}$  These parameters are related to  $\phi_{\scriptscriptstyle S}$  by

$$S_f = \eta_f \sin \phi_s$$
, and  $A^{\Delta \Gamma} =$ 

The parameters of CP-violation are obtained experimentally through a flavor-tagger time-dependent angular analysis



t: Decay time  $\eta_f$ : CP eigenvalue of the final state  $\Gamma_s$ : Average width of  $B_s^0$ 

#### $= -\eta_f \cos \phi_s$



# Outline

#### Measurement of $\phi_s$ in $B_s^0 \to J/\psi K^+ K^-$ decays

•  $\mathcal{L} = 6 \text{ fb}^{-1}$ , Run 2 data from 2015 to 2018, (arXiv: 2308.01468)

#### $\sim CP$ violation measurements in the penguin-mediated decay $B_{ m s}^0 ightarrow \phi \phi$

•  $\mathcal{L} = 6 \text{ fb}^{-1}$ , Run 2 data from 2015 to 2018, arXiv:2304.06198

• A measurement of  $\Delta \Gamma_s$  from  $B_s^0 \rightarrow J/\psi \eta'$  and  $B_s^0 \rightarrow J/\psi \pi^+ \pi^-$  decays

•  $\mathcal{L} = 9 \text{ fb}^{-1}$ , Run 1 2011 + 2012 and Run 2 2015 to 2018 data, LHCb-PAPER-2023-025

# • $\mathcal{L} = 6 \text{ fb}^{-1}$ , Run 2 data from 2015 to 2018, arXiv: 2308.01468

# Measurement of $\phi_{s}$ in $B_{s}^{0} \rightarrow J/\psi K^{+}K^{-}$ (arXiv: 2308.01468)

 $\phi(1020)$  resonance, which gives the best sensitivity in  $\phi_s$  [arXiv:1906.08356]

• Global fits to experimental data, gives  $-2\beta_s = -36.9^{+0.9}_{-0.6}$  mrad (CKMFitter arXiv:1501.05013),  $-2\beta_{s} = -37.0 \pm 1.0$  mrad (UTFit <u>arXiv:hep-ph/0606167</u>)

$$\phi_s = -2\beta_s + \Delta\phi_s^{NP}$$

 $B_s^0 \rightarrow J/\psi K^+ K^-$ , via  $b \rightarrow c \bar{c} s$  transition



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The LHCb collaboration has previously measured  $\phi_s$  in the golden channel  $B_s^0 \to J/\psi(\mu^+\mu^-)K^+K^-$  in the region of

Penguin pollution is small



# Measurement of $\phi_{s}$ in $B_{s}^{0} \rightarrow J/\psi K^{+}K^{-}$ (arXiv: 2308.01468)

with  $h = K, \pi$  using 5 fb<sup>-1</sup> [PDG2022]

 $\bullet$  In this analysis an update of the CP-violating phase  $\phi_s^{ccs}$  is performed as well of the physics parameter  $|\lambda|, \Delta\Gamma_s, \Gamma_s - \Gamma_d$  and the  $B_s^0$  mass difference  $\Delta m_s$ , using the  $B_s^0 \to J/\psi K^+ K^-$  channel, in the vicinity of  $\phi(1020)$ resonance with the full Run 2 dataset. P-wave S-wave • The polarization amplitudes  $A_0, A_{||}, A_{\perp} + A_s$  regarding to the polarization states of the  $K^+K^-$  system and CP-odd KK S-wave component are also determined.





• The current World Average value for  $\phi_s^{c\bar{c}s} = -0.049 \pm 0.019$  rad, dominated by LHCb result in  $B_s^0 \to J/\psi h^+ h^-$ ,





# Measurement of $\phi_{S}$ in $B_{S}^{0} \rightarrow J/\psi K^{+}K^{-}$ (arXiv: 2308.01468)

#### **Analysis Strategy**

Very similar to previous analysis [arXiv:1906.08356]

A selection criteria considering the  $K^+K^$ invariant mass region [990, 1050] MeV/c<sup>2.</sup>

The data sample is divided in 48 independent subsamples: 6 bins in the  $\phi(1020)$  regions; two trigger categories, and four years of data taking

A yield of about 349 000 signal decays

**Extended maximum likelihood fit to extract**  $B_{\rm s}^0 \rightarrow J/\psi K^+ K^-$  signal yields.



(arXiv: 2308.01468)

 $\bullet$  To extract  $\phi_{c}$ , CP-even and CP-odd decay-amplitudes need to be disentangled.

basis is performed.

•For each of the 48 sub-sample the fit function accounts for

- Decay-time resolution
- The decay-time
- Flavor tagging
- Angular efficiencies



- A weighted simultaneous fit to decay time distribution and decays angles ( $cos\theta_K, cos\theta_\mu, \phi_h$ ) in the helicity

Time dependent angular rate:  $t, \theta_K, \theta_l, \phi$ 



# Measurement of $\phi_S$ in $B_S^0 \rightarrow J/\psi K^+ K^-$ (arXiv: 2308.01468)



#### **Background-substracted data distribution** with fit overlaid for Decay-time and decayangles.

Parameter	Values		
$\phi_s$ [rad]	$-0.039 \pm 0.022 \pm 0.00$		
$ \lambda $	$1.001 \pm 0.011 \pm 0.00$		
$\Gamma_s - \Gamma_d  [\mathrm{ps}^{-1}]$	$-0.0056 \begin{array}{c} + 0.0013 \\ - 0.0015 \end{array} \pm 0.00$		
$\Delta \Gamma_s  [\mathrm{ps}^{-1}]$	$0.0845 \pm 0.0044 \pm 0.00$		
$\Delta m_s  [\mathrm{ps}^{-1}]$	$17.743 \pm 0.033 \pm 0.00$		
$ A_{\perp} ^2$	$0.2463 \pm 0.0023 \pm 0.00$		
$ A_0 ^2$	$0.5179 \pm 0.0017 \pm 0.00$		
$\delta_{\perp} - \delta_0 \text{ [rad]}$	$2.903 \begin{array}{c} + 0.075 \\ - 0.074 \end{array} \pm 0.04$		
$\delta_{\parallel} - \delta_0 \; [{ m rad}]$	$3.146 \pm 0.061 \pm 0.05$		

#### arXiv: 2308.01468

Results are in good agreement with LHCb Run 1 and 2015+2016 measurements

![](_page_9_Figure_6.jpeg)

![](_page_9_Figure_7.jpeg)

![](_page_9_Figure_8.jpeg)

![](_page_9_Figure_9.jpeg)

Measurement of  $\phi_{s}$  in  $B_{s}^{0} \rightarrow J/\psi K^{+}K^{-}$ 

#### In summary

Using the full Run 2 dataset collected by the LHCb experiment, it is measured

• 
$$\phi_s = -0.039 \pm 0.022 \pm 0.006$$
 rad •  $\Gamma_s - \Gamma_d = -0.00$   
•  $|\lambda| = 1.001 \pm 0.011 \pm 0.005$  •  $\Delta \Gamma_s = 0.0845 \pm 0.0845$ 

The combination results in

$$\phi_s = -0.044 \pm 0.020$$
 rad  
 $|\lambda| = 0.990 \pm 0.010$ 

![](_page_10_Picture_6.jpeg)

arXiv: 2308.01468

![](_page_10_Picture_8.jpeg)

 $0.56^{+0.0013}_{-0.0015} \pm 0.0014$ 

 $\pm 0.0044 \pm 0.0024$ 

Superseding the previous Run 2 LHCb measurement in the same decay

No evidence for *CP* violation

Results consistent with previous measurements in  $B_s^0 \to J/\psi(\mu^+\mu^-)K^+K^-$  and  $B_s^0 \to J/\psi(e^+e^-)K^+K^-$  decays.

 $\phi_s$  measurements independently for each polarization state of the  $K^+K^-$  system

Shows no evidence for polarization dependence

![](_page_10_Picture_18.jpeg)

# Measurement of $\phi_s$ in $B_s^0 \rightarrow J/\psi K^+ K^-$ arXiv: 2308.01468

 $B_s^0 \rightarrow J/\psi(2S)K^+K^-$  and  $B_s^0 \rightarrow J/\psi K^+K^-$  gives

![](_page_11_Figure_3.jpeg)

Combination of all LHCb  $\phi_s$  measurements of  $B_s^0$  decays via  $b \to c\bar{c}s$ :  $B_s^0 \to J/\psi(\mu^+\mu^-)K^+K^-$ ,  $B_s^0 \to D_s^+D_s^-$ ,  $B_s^0 \to J/\psi\pi^+\pi^-$ ,

$$\phi_s = -0.031 \pm 0.018$$
 rad

#### This is the most precise measurement to date and is consistent with SM predictions

![](_page_11_Picture_8.jpeg)

![](_page_11_Picture_9.jpeg)

# • *CP* violation measurements in the penguin-mediated decay $B_s^0 \rightarrow \phi \phi$ • $\mathcal{L} = 6 \text{ fb}^{-1}$ , Run 2 data from 2015 to 2018, arXiv:2304.06198

![](_page_12_Picture_3.jpeg)

# CP violation measurements in the penguin-mediated decay $B_{ m c}^0 ightarrow \phi \phi$

Flavour-changing neutral current (FCNC) decays of B mesons are highly sensitive to new physics contribution entering via loop processes

 $B_s^0 \rightarrow \phi \phi \ (b \rightarrow s \bar{s} s \text{ transition})$ 

![](_page_13_Figure_3.jpeg)

• Measurements of the CP violation phase  $\phi_s^{s\bar{s}s}$  and parameter  $|\lambda|$  — New physics contributions entering in the penguin decay or mixing would be reflected in  $\phi_s^{s\bar{s}s}$  and  $|\lambda|$  values

• The  $\phi\phi$  system produce three linear polarization states, new physics effects could be polarization dependent.

**Benchmark channel at LHCb** 

•arXiv:2304.06198

![](_page_13_Figure_8.jpeg)

![](_page_13_Picture_10.jpeg)

![](_page_13_Figure_11.jpeg)

# CP violation measurements in the penguin-mediated decay $B^0_{ m c} ightarrow \phi \phi$

full Run 2 dataset (6 fb<sup>-1</sup>), performing an angular analysis

Measurement of the CP-violation parameters independently for all polarization states for the first time

Analysis Strategy (same as ref JHEP 12 (2019) 155)

 $B^0_{c} \rightarrow \phi \phi$  candidates selected in the mass region [5150, 5600] MeV/c<sup>2</sup>

Enhancing selection of four kaons in the final state  $(K^{+}K^{-}K^{+}K^{-})$ 

Two sources of background: Combinatorial and from  $\Lambda_h^0 \rightarrow \phi K^- p$  decays

A maximum likelihood fit performed to  $m(K^+K^-K^+K^-)$  invariant mass

In this analysis the update measurements of the CP-violation parameters in  $B_s^0 \to \phi \phi$  decays is reported with

![](_page_14_Figure_9.jpeg)

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![](_page_14_Picture_11.jpeg)

![](_page_15_Figure_2.jpeg)

where  $\theta_1 = \theta_1, \theta_2$  denotes the helicity angles of the K mesons in the corresponding  $\phi$  rest frame.  $\chi$  is the angle between the two  $\phi \to K^+ K^-$  decay planes

CP violation measurements in the penguin-mediated decay  $B_{\rm s}^0 
ightarrow \phi \phi$ 

Fit projections onto background-subtracted distributions of angular variables and decay-time.

![](_page_15_Figure_6.jpeg)

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Measured observables in the polarization-independent fit

#### arXiv:2304.06198

Parameter	Result		
$\phi_s^{s\overline{s}s}$ [rad]	$-0.042 \pm 0.075 \pm 0.009$		
$ \lambda $	$1.004 \pm 0.030 \pm 0.009$		
$ A_0 ^2$	$0.384 \pm 0.007 \pm 0.003$		
$ A_{\perp} ^2$	$0.310 \pm 0.006 \pm 0.003$		
$\delta_{\parallel} - \delta_0 \; [ { m rad} \; ]$	$2.463 \pm 0.029 \pm 0.009$		
$\delta_{\perp} - \delta_0  [\text{rad} ]$	$2.769 \pm 0.105 \pm 0.011$		

In combination with LHCb Run 1 measurements

$$\phi^{s\bar{s}s} = -0.074 \pm 0.069$$
 ra

This is the most precise measurement of CP violation in  $B_{s}^{0} \rightarrow \phi \phi$  to date

The following parameters have been constrained to the measurements by LHCb collaboration

 $\Delta m_{\rm s} = 17.766 \pm 0.006 \, {\rm ps^{-1}}$ 

 $\Gamma_{\rm s} = 0.657 \pm 0.002 \ {\rm ps}^{-1}$ 

 $\Delta\Gamma_{\rm s}=0.078\pm0.006\,{\rm ps^{-1}}$  with correlation coefficient of -0.35

 $= 1.009 \pm 0.07 \pm 0.030$ ad and  $|\lambda|$ 

arXiv:2304.06198

![](_page_16_Picture_16.jpeg)

#### •arXiv: 2308.01468 CP violation measurements in the penguin-mediated decay $B_{ m c}^0 ightarrow \phi \phi$

![](_page_17_Figure_1.jpeg)

- The most precise measurement in  $B_s^0 \rightarrow \phi \phi$ \* and in any penguin-dominated *B* meson decay
- Agrees with SM expectation

The polarization-dependent measurements Shows no dependence in the polarization states of  $B_s^0 \rightarrow \phi \phi$ 

![](_page_17_Picture_6.jpeg)

![](_page_17_Picture_7.jpeg)

# • A measurement of $\Delta \Gamma_s$ from $B_s^0 \rightarrow J/\psi \eta'$ and $B_s^0 \rightarrow J/\psi \pi^+ \pi^-$ decays • $\mathcal{L} = 9 \text{ fb}^{-1}$ , Run 1 2011 + 2012 and Run 2 2015 to 2018 data, LHCb-PAPER-2023-025

# A measurement of $\Delta \Gamma_{s}$ from $B_{s}^{0} \rightarrow J/\psi \eta'$ and $B_{s}^{0} \rightarrow J/\psi \pi^{+} \pi^{-}$ decays

**Motivation** 

• The measurements of the  $B_s^0 - \bar{B}_s^0$  mixing parameters offer a powerful test of the Standard Model namely the *CP* violating phase  $\phi_s$  and the decay-width difference  $\Delta \Gamma_s = \Gamma_L - \Gamma_H$ 

![](_page_19_Figure_4.jpeg)

•  $\Delta\Gamma_s$  has been determined experimentally using the golden channel  $B_s^0 \to J/\psi\phi$  by ATLAS, CMS and LHCb experiments

Results precises but in tension with each other

This motivates independent measurements in other decays modes!

![](_page_19_Figure_10.jpeg)

![](_page_19_Picture_11.jpeg)

# A measurement of $\Delta \Gamma_s$ from $B_s^0 \to J/\psi \eta'$ and $B_s^0 \to J/\psi \pi^+ \pi^-$ decays

• *CP*-even modes measure the light mass eigenstates lifetime ( $\tau_L = 1/\Gamma_L$ ) As  $\phi_{s}$  is experimentally measured to be small • CP-odd modes measure the heavy mass eigenstates lifetime ( $\tau_H = 1/\Gamma_H$ )

Requirement of the dipion mass to be around 90 MeV around the  $f_0(980)$  mass

- $\Delta \Gamma_{s}$  can be determined from the difference in decay-widths between a CP-odd and a CP-even  $B_{s}^{0}$  mode.
  - In this analysis,  $\Delta\Gamma_{\rm s}$  is determined from decay-width difference between the *CP*-even decay  $B_s^0 \rightarrow J/\psi \eta'$  and *CP*-odd  $B_s^0 \rightarrow J/\psi f_0(980)$
  - Subsequent decays  $J/\psi \to \mu^+\mu^-$ ,  $\eta' \to \rho^0 \gamma$  and  $\rho^0 \to \pi^+\pi^-$  for signal and  $f_0(980) \to \pi^+\pi^-$

![](_page_20_Picture_11.jpeg)

### A measurement of $\Delta \Gamma_s$ from $B_s^0 \to J/$

**Method** If CP violation is negligible, the time dependent rate can be expressed as CP-odd CP-even  $\Gamma(B_s^0(t) \to f) \propto e^{-\Gamma_s t} \left[ \cosh(\frac{\Delta \Gamma_s t}{2}) - \sinh(\frac{\Delta \Gamma_s t}{2}) \right]$ 

Where  $\Gamma_s = (\Gamma_H + \Gamma_I)/2$ . Integrating both equations over a time bin  $[t_1, t_2]$  and making the ratio, we obtain

$$R(t) = \frac{N_L}{N_H} \propto \frac{[e^{-\Gamma_s t(1+y)}]_{t1}^{t2}}{[e^{-\Gamma_s t(1-y)}]_{t1}^{t2}} \cdot \frac{1-y}{1+y}$$

$$2y = \Delta \Gamma_s / \Gamma_s$$

$$/\psi\eta'$$
 and  $B_s^0 \to J/\psi\pi^+\pi^-$  decays

and 
$$\Gamma(B_s^0(t) \to f) \propto e^{-\Gamma_s t} \left[ \cosh(\frac{\Delta \Gamma_s t}{2}) + \sinh(\frac{\Delta \Gamma_s t}{2}) \right]$$

![](_page_21_Figure_6.jpeg)

![](_page_21_Picture_8.jpeg)

![](_page_21_Picture_9.jpeg)

## A measurement of $\Delta \Gamma_s$ from $B_s^0 \to J/\psi \eta'$ and $B_s^0 \to J/\psi \pi^+ \pi^-$ decays

Then  $\Delta\Gamma_s$  can be obtained from  $\chi^2$  minimization of the corrected R(t), with  $\Delta\Gamma_s$  as a free parameter and a arbitrary normalization factor

#### **Analysis Strategy**

Using simulation studies, a time bin scheme of eight bins with similar number of events is defined

Lower Limit 0.5 ps  $\rightarrow$  above this value time acceptance is relative flat Upper limit 10 ps  $\rightarrow$  above this value, contribution of  $B_{c}^{0} \rightarrow J/\psi \eta'$  is negligible

Binning Scheme LHCb-PAPER-2023-025 Preliminary

Bin number	Bin edges [ps]	
1	0.5 - 0.7	
2	0.7 - 0.9	
3	0.9 - 1.2	
4	1.2 - 1.5	
5	1.5 - 2.0	
6	2.0 - 2.5	
7	2.5 - 3.5	
8	3.5 - 10.0	

 $= A_{r}(t)$  is evaluated at the barycentre of the bin

![](_page_22_Picture_10.jpeg)

# A measurement of $\Delta \Gamma_s$ from $B_s^0 \to J/\psi \eta'$ and $B_s^0 \to J/\psi \pi^+ \pi^-$ decays

Selection criteria is based on the topology and kinematics of the decays.

the determines  $\Delta \Gamma_{s}$ 

2011+2012

![](_page_23_Figure_4.jpeg)

2017

![](_page_23_Picture_7.jpeg)

![](_page_23_Picture_8.jpeg)

# A measurement of $\Delta \Gamma_s$ from $B_s^0 \rightarrow J/\psi \eta'$ and $B_s^0 \rightarrow J/\psi \pi^+ \pi^-$ decays

![](_page_24_Figure_1.jpeg)

![](_page_24_Figure_2.jpeg)

2011+2012

![](_page_24_Figure_4.jpeg)

### A measurement of $\Delta \Gamma_s$ from $B_s^0 \to J/\psi \eta'$ and $B_s^0 \to J/\psi \pi^+ \pi^-$ decays

#### **Results**

Ratio of yields in each decay-time bin, corrected by the corresponding relative time acceptance and the  $\chi^2$  fit is performed.

![](_page_25_Figure_3.jpeg)

![](_page_25_Figure_4.jpeg)

#### LHCb-PAPER-2023-025

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 $\Delta \Gamma_s$  results and probability of  $\chi^2$ 

Dataset	$\Delta\Gamma_s \;[\mathrm{ps^{-1}}]$	$\mathrm{P}(\chi^2)$
2011 + 12	$0.039\pm0.026$	0.83
2015 + 16	$0.081 \pm 0.022$	0.77
2017	$0.117\pm0.024$	0.57
2018	$0.102\pm0.021$	0.78

#### **Summary**

Using full pp-collision dataset between 2011 and 2018,  $B_s^0 \rightarrow J/\psi \eta'$  and  $B_s^0 \rightarrow J/\psi \pi^+ \pi^-$ ,  $\Delta \Gamma_{\rm s}$  is measured to be

 $\Delta \Gamma_{\rm s} = 0.087 \pm 0.012 \pm 0.009 \text{ ps}^{-1}$ 

#### LHCb-PAPER-2023-025

#### **Comparison between the four data sets**

![](_page_26_Figure_9.jpeg)

 $\rightarrow$  This is the first  $\Delta \Gamma_s$  measurement using the  $B_s^0 \rightarrow J/\psi \eta'$ 

![](_page_26_Picture_12.jpeg)

# Summary

A lot of work ongoing in the LHCb experiment, with a very broad program in the search for CPasymmetries in b- and c-hadrons.

2 dataset.

- These results supersede previous LHCb measurement (2015+2016, [arXiv:1906.08356])
- No evidence of *CP* violation is found.
- Measurement of CP-observables in  $B^0_s \to \phi \phi$  decays
  - and any penguin-dominated B meson decay
  - First time polarization-dependent CP-violation parameters measurement.

 $\odot$  CP-violation and decay-width parameters in the decay  $B_s^0 \to J/\psi K^+ K^-$  are measured using the full Run

•  $\phi_s^{sss} = -0.074 \pm 0.069$  rad and  $|\lambda| = 1.009 \pm 0.030$ , most precise measurements in this decay

![](_page_27_Picture_14.jpeg)

# Summary

- $\Delta \Gamma_s = 0.087 \pm 0.012 \pm 0.009 \text{ ps}^{-1}$
- First time  $\Delta \Gamma_s$  measurement using the  $B_s^0 \rightarrow J/\psi \eta'$  decay model
- Result in agreement with the average value for  $\Delta\Gamma_{
  m s}$  from  $B^0_{
  m s} o J/\psi \phi$

Decay-width difference measurement,  $\Delta\Gamma_s$ , using the decay channels  $B_s^0 \to J/\psi \eta'$  and  $B_s^0 \to J/\psi \pi^+ \pi^-$ 

# Gracias!

# Measurement of $\phi_S$ in $B_S^0 \rightarrow J/\psi K^+ K^-$ arXiv: 2308.01468

![](_page_30_Figure_1.jpeg)

 $\phi_s$  world average:

 $\phi_s = -0.039 \pm 0.016$  rad  $\phi_s(J/\psi KK) = -0.050 \pm 0.017$  rad

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