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# Theory determination of $\gamma$ and $\phi_s$ from $B_{(s)} \rightarrow hh$ decays

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K. Keri Vos

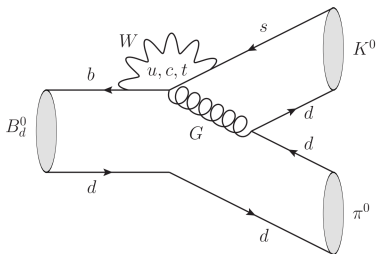
Maastricht University & Nikhef

in collaboration with Ruben Jaarsma and Robert Fleischer, JHEP02 (2023) 081

[2211.08346]

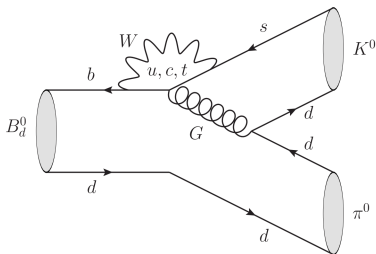
# The challenge of nonleptonic $B$ decays

- Nonleptonic decays are important probes of CP violation
  - Direct CP violation due to different strong and weak phases
  - **Mixing-induced CP violation in neutral decays probe mixing phase  $\phi_{d,s}$**
  - Sensitivity to NP in loops (penguins)
- CP violation in the SM is too small and peculiar!
  - CKM CP violating effects only from flavour changing currents
  - Flavour diagonal CP violation tiny in SM (EDMs)
  - Large CP asymmetries with processes with tiny BRs and vice versa



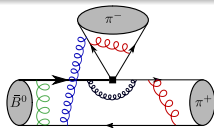
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Challenge: Calculation of Hadronic matrix elements

# How to handle nonleptonic B decays?



## QCD Factorization Beneke, Buchalla, Neubert, Sachrajda: Talk by T. Huber@CKM

- Disentangle perturbative (calculable) and non-perturbative dynamics using HQE

## Flavour symmetries (Isospin or $SU(3)$ )

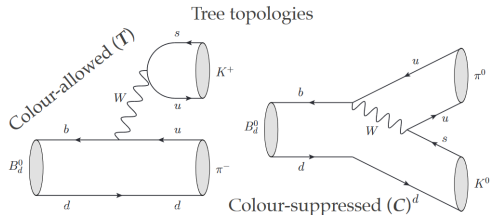
- Puzzles in  $B \rightarrow \pi K$  e.g. Fleischer, Jaarsma, KKV, Malami [2017,2018] and  $B \rightarrow DK$  Talk by E. Malami@CKM
- Global  $SU(3)$  fit to  $B \rightarrow PP$  decays Huber, Tetlalmatzi-Xolocotzi [2111.06418]

## Light-cone sumrules

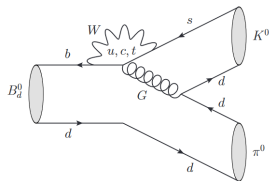
- Work in progress Jung, Melic, Khodjamirian

# Topologies for $B \rightarrow hh$ decays

- Main contributions to  $B \rightarrow hh$
- Tree and penguin contributions

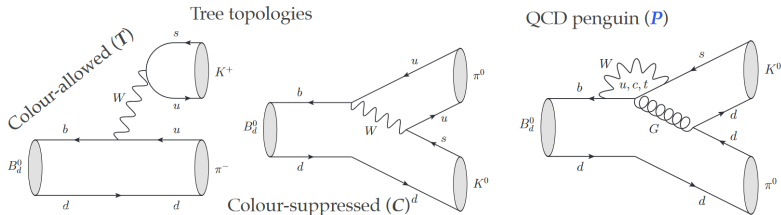


QCD penguin (P)



# Topologies for $B \rightarrow hh$ decays

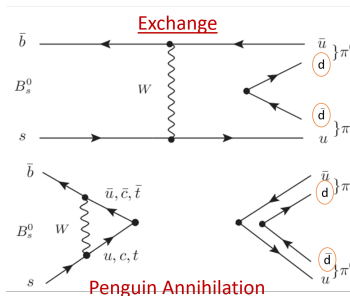
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Mode	Notation	Topologies			
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# Topologies for $B \rightarrow hh$ decays

- Suppressed (?) contributions to  $B \rightarrow hh$
- Exchange and Penguin Annihilation usually neglected



# Motivation: New puzzles?

LHCb [2012.05319], Fleischer, Jaarsma, KKV, JHEP 02 (2023) 081 [2211.08346]

- **New!** First observation of CP violation in penguin dominated  $B_s \rightarrow K^- K^+$  [LHCb]
  - Allows determination of  $\gamma$  and  $\phi_s$
  - Interesting to compare loops with tree!
- Updated measurements of CP asymmetries for other  $B \rightarrow hh$  modes [LHCb]



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## New Puzzle?

$$\mathcal{A}_{\text{CP}}^{\text{dir}}(B_s^0 \rightarrow K^- K^+) - \mathcal{A}_{\text{CP}}^{\text{dir}}(B_d^0 \rightarrow \pi^- K^+) = 0.089 \pm 0.031$$

$$\mathcal{A}_{\text{CP}}^{\text{dir}}(B_d^0 \rightarrow \pi^- \pi^+) - \mathcal{A}_{\text{CP}}^{\text{dir}}(B_s^0 \rightarrow K^- \pi^+) = -0.095 \pm 0.040$$

- Modes only differ by their spectator quark!
- Can exchange and penguin annihilation contributions cause this?

Today: New determinations of  $\gamma, \phi_s$  and of exchange and penguin annihilation effects!

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# Extracting $\gamma$ from QCD penguin decays

# Flavor symmetries in $B_s^0 \rightarrow K^- K^+$ and $B_d \rightarrow \pi^- \pi^+$

Fleischer [1999, 2007]; Fleischer, Kneijens [2011]

$$A(B_s \rightarrow K^+ K^-) = \sqrt{\epsilon} e^{i\gamma} C' \left[ 1 + \frac{1}{\epsilon} d' e^{i\theta'} e^{-i\gamma} \right]$$

$$A(B_d \rightarrow \pi^+ \pi^-) = e^{i\gamma} C [1 - d e^{i\theta} e^{-i\gamma}]$$

$$C' \propto T' + P^{(ut)'} + E' + PA^{(ut)'} \quad \text{and} \quad d' e^{i\theta'} \propto \frac{P^{(ct)'} + PA^{(ct)'}}{T' + P^{(ut)'} + E' + PA^{(ut)'}}$$

- $d$  and  $\theta$  penguin parameters [ $\epsilon \sim 0.04$ ]
- Extract hadronic parameters from direct and mixing-induced CP asymmetries

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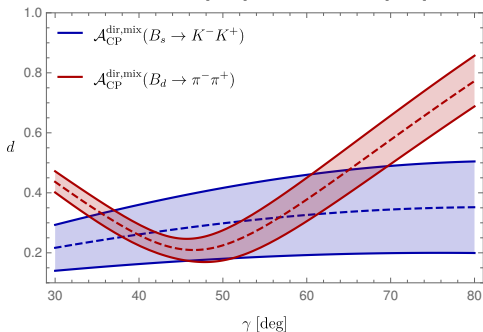
## U-spin symmetry

$$d e^{i\theta} = d' e^{i\theta'}$$

- Or assume  $d = d'$  and extract  $\gamma$
- Limited by  $U$ -spin breaking corrections

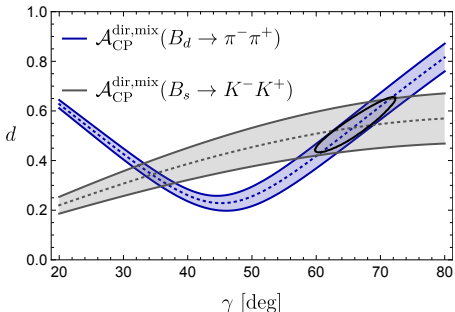
# CKM-angle $\gamma$ from non-tree decays

Fleischer [1999,2007]; Fleischer, Knegjens [2011]; Fleischer, Malami, Jaarsma, KKV [2016]  
Cuichini, Franco, Mishima, Silvestrini [2012], Data from LHCb [2022] **Fleischer, Jaarsma, KKV [2211.08346]**



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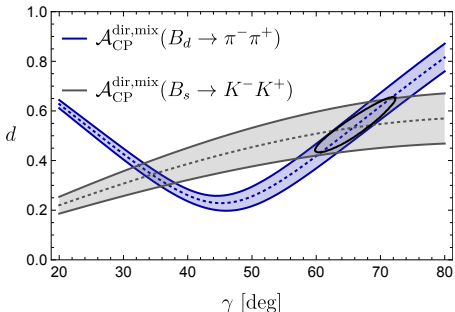
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- **New!** First observation of CP violation in penguin dominated  $B_s \rightarrow K^+ K^-$  LHCb 2022
- **New!** First determination of  $\gamma$  with only CP asymmetries
- $\gamma = (65_{-5}^{+7})^\circ$  [Fleischer, Jaarsma, KKV \[2111.08346\]](#)
- Agrees with tree determinations:  $\gamma = (64.9 \pm 4.5)^\circ$  LHCb [2021] without  $B_s$  modes

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# New puzzles?

LHCb [2012.05319], Fleischer, Jaarsma, KKV, JHEP 02 (2023) 081 [2211.08346]

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- Can exchange and penguin annihilation contributions cause this?
- Challenging to compute → data-driven approach

# How to determine $E$ and PA amplitudes?

- Difference between  $B_d^0 \rightarrow \pi^- \pi^+$ ,  $B_s^0 \rightarrow K^- K^+$  and  $B_d^0 \rightarrow \pi^- K^+$ ,  $B_s^0 \rightarrow K^- \pi^+$

$$\tilde{d}' e^{i\tilde{\theta}'} = \zeta' d' e^{i\theta'}$$

- Step 0: Use  $\gamma$  as input, use only direct CP asymmetry (no  $\phi$  input)
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- Mismatch parametrized by

$$\zeta' \equiv |\zeta'| e^{i\omega'} \equiv \frac{1 + x'}{1 + r'_{PA}}$$

$$x^{(l)} \equiv |x^{(l)}| e^{i\sigma^{(l)}} \equiv \frac{E^{(l)} + PA^{(ut)(l)}}{T^{(l)} + P^{(ut)(l)}}, \quad r'_{PA} \equiv |r'_{PA}| e^{i\theta'_{PA}} \equiv \frac{PA^{(ct)(l)}}{P^{(ct)(l)}}.$$

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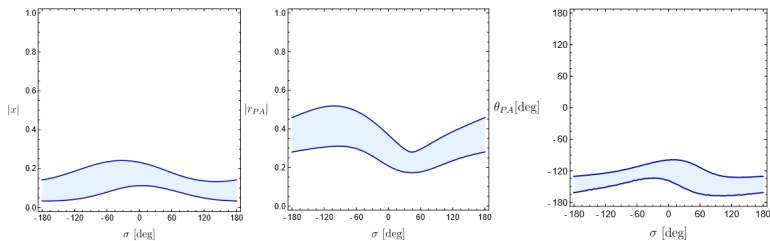
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- Cannot fully determine parameters yet!

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- Only branching ratios available

# Current constraints

Fleischer, Jaarsma, KKV [2211.08346]

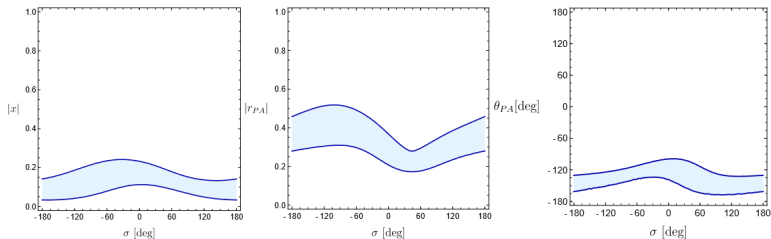


- $x$  and  $r_{PA}$  constrained at 20% and 30% level



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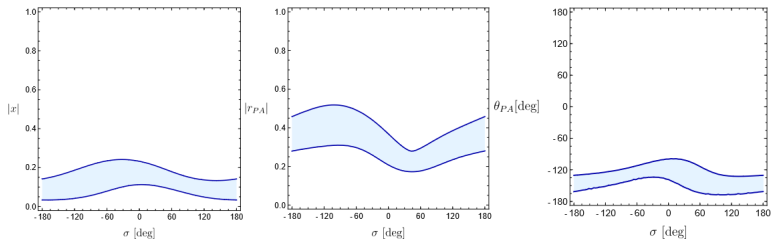
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- $x$  and  $r_{PA}$  constrained at 20% and 30% level
- The difference in the direct CP asymmetries can be accommodated by exchange and penguin annihilation effects at the level of (20–30)%.
- No anomalously enhanced rescattering effects

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Fleischer, Jaarsma, KKV [2211.08346]



- $x$  and  $r_{PA}$  constrained at 20% and 30% level
- The difference in the direct CP asymmetries can be accommodated by exchange and penguin annihilation effects at the level of (20–30)%.
- CP asymmetries in the  $B_s^0 \rightarrow \pi^- \pi^+$ ,  $B_d^0 \rightarrow K^- K^+$  system would provide even more info!

# Determination of $\phi_s$

Fleischer, Jaarsma, KKV, JHEP 02 (2023) 081 [2211.08346]

- CP violation in  $B_s \rightarrow K^+ K^-$  also gives access to  $\phi_s$

$$\phi_s^{\text{eff}} = \frac{\mathcal{A}_{\text{CP}}^{\text{mix}}(B_s^0 \rightarrow K^- K^+)}{\sqrt{1 - (\mathcal{A}_{\text{CP}}^{\text{mix}}(B_s^0 \rightarrow K^- K^+))^2}}$$

- $\phi_s^{\text{eff}} \equiv \phi_s + \Delta\phi_{KK}$
- LHCb measurement:  $\phi_s^{\text{eff}} = -(8.1 \pm 1.9)^\circ$  LHCb 2022

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- $\Delta\phi_{KK}$  hadronic phase shift

$$\Delta\phi_{KK} = 2\epsilon \sin \gamma \left[ \frac{d' \cos \theta' + \epsilon \cos \gamma}{d'^2 + 2\epsilon d' \cos \theta' \cos \gamma + \epsilon^2 \cos 2\gamma} \right]$$

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How to determine the penguin parameters?

# Determination of $\phi_s$ (I)

## Strategy I:

Fleischer, Jaarsma, KKV, JHEP 02 (2023) 081 [2211.08346] (and [1612.07342])

- Use semileptonic decays

$$R_\pi \equiv \frac{\Gamma(B_d^0 \rightarrow \pi^- \pi^+)}{|d\Gamma(B_d^0 \rightarrow \pi^- \ell^+ \nu_\ell)/dq^2|_{q^2=m_\pi^2}} \quad R_K \equiv \frac{\Gamma(B_s^0 \rightarrow K^- K^+)_{\text{theo}}}{|d\Gamma(B_s^0 \rightarrow K^- \ell \nu_\ell)/dq^2|_{q^2=m_K^2}}$$

- Gives access to hadronic parameters  $r_K = (1 + \left(\frac{d'}{\epsilon}\right)^2 + 2d'/\epsilon \cos\theta' \cos\gamma)$
- Use ratios to get favorable structure!

$$r_K = \frac{R_K}{R_\pi} \left( \frac{|V_{ud}| f_\pi}{|V_{us}| f_K} \right)^2 \frac{X_\pi}{X_K} (\xi_{\text{NF}}^a)^2 r_\pi$$

- $X_{\pi,K}$  ratio of form factor  $\rightarrow$  input

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- Non-factorisable  $U$ -spin-breaking contributions:

$$\xi_{\text{NF}}^a \equiv \left| \frac{1 + r_P}{1 + r'_P} \right| \left| \frac{1 + x}{1 + x'} \right| \left| \frac{a_{\text{NF}}^T}{a_{\text{NF}}^{T'}} \right|,$$

- $a_{\text{NF}}^T$  tree-level contribution from QCDF

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- $a_{\text{NF}}^T$  tree-level contribution from QCDF
- $\xi_{\text{NF}}^a = 1.00 \pm 0.07 \rightarrow 0.8^\circ$  theoretical uncertainty on  $\Delta\phi_{KK}$



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- **Experimental input not available!**
- Theoretical control over penguin effects excellent!
- $\xi_{\text{NF}}^a = 1.00 \pm 0.07 \rightarrow 0.8^\circ$  theoretical uncertainty on  $\Delta\phi_{KK}$

# Determination of $\phi_s$ (II)

Fleischer, Jaarsma, KKV, JHEP 02 (2023) 081 [2211.08346]

## Strategy II:

- Use ratio of branching ratios of  $B_d \rightarrow \pi\pi$  and  $B_s \rightarrow KK$  decays

$$K \equiv \frac{1}{\epsilon} \left[ \frac{m_{B_s}}{m_{B_d}} \frac{\Phi(m_\pi/m_{B_d}, m_\pi/m_{B_d})}{\Phi(m_K/m_{B_s}, m_K/m_{B_s})} \frac{\tau_{B_d}}{\tau_{B_s}} \right] \frac{\mathcal{B}(B_s^0 \rightarrow K^- K^+)_{\text{theo}}}{\mathcal{B}(B_d^0 \rightarrow \pi^- \pi^+)} = 105.3 \pm 9.6$$

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- Use ratio of branching ratios of  $B_d \rightarrow \pi\pi$  and  $B_s \rightarrow KK$  decays  $K = 105.3 \pm 9.6$
- Gives access to hadronic parameters

$$r_K = \left| \frac{C}{C'} \right|^2 K r_\pi = \left( 1 + \left( \frac{d'}{\epsilon} \right)^2 + 2d'/\epsilon \cos\theta' \cos\gamma \right)$$

$$\left| \frac{C}{C'} \right| = \frac{f_\pi}{f_K} \left[ \frac{m_{B_d}^2 - m_\pi^2}{m_{B_s}^2 - m_K^2} \right] \left[ \frac{F_0^{B_d\pi}(m_\pi^2)}{F_0^{B_s K}(m_K^2)} \right] \zeta_{\text{NF}}^a$$

- Non-factorisable  $U$ -spin-breaking contributions:

$$\zeta_{\text{NF}}^a \equiv \left| \frac{1 + r_P}{1 + r'_P} \right| \left| \frac{1 + x}{1 + x'} \right| \left| \frac{a_{\text{NF}}^T}{a_{\text{NF}}^{T'}} \right| = 1.00 \pm 0.07,$$

- $a_{\text{NF}}^T$  tree-level contribution from QCDF

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- Use form factor information: 10% uncertainty
- $\Delta\phi_{KK} = -(4.5 \pm 5.3)^\circ$
- With  $\phi_s^{\text{eff}} = -(8.1 \pm 1.9)^\circ \rightarrow \phi_s = -(3.6 \pm 5.7)^\circ$

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Remarkable agreement with  $B_s^0 \rightarrow J/\psi\phi$  determination:  $\phi_s = -(4.2 \pm 1.4)^\circ$

# Challenges in (nonleptonic) $B$ decays

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## We are in the High-precision Era in Flavour Physics!

- Nonleptonic decays are challenging but important!
- $B_s \rightarrow KK$  gives consistent  $\gamma$  and  $\phi_s$  determinations
- Exchange and Penguin Annihilation not anomalously large
- CP asymmetries in  $B_d \rightarrow KK$  and  $B_s \rightarrow \pi\pi$  would provide more input
- Link with semileptonic decays to be explored

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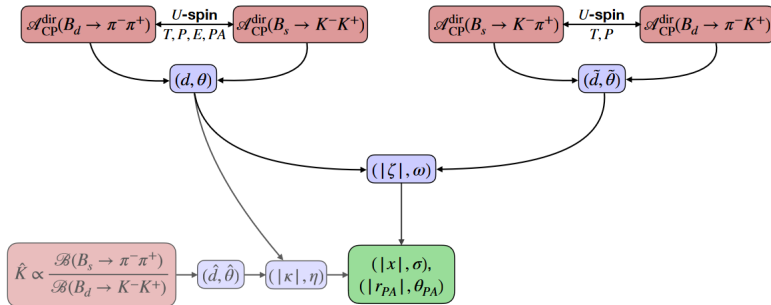
Close collaboration between theory and experiment necessary!

# Backup

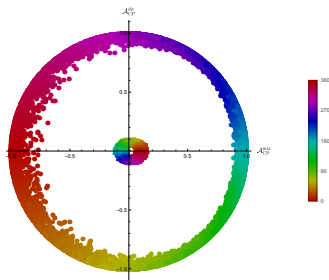
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# Strategy to extract E and PA

Fleischer, Jaarsma, KKV [2211.08346]



# CP asymmetries in $B_s \rightarrow \pi\pi$ and $B_d \rightarrow KK$



- Correlation between CP asymmetries in  $B_s \rightarrow \pi\pi$  (small circle) and  $B_d \rightarrow KK$  (wide) for different strong phases
- Important also to improve QCDF