The fate of horizons under quantum corrections. Based on arXiv:2207.12721

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January 13, 2023





Table of Contents



▶ Introduction

 \blacktriangleright Results

▶ Summary and conclusions





- Gravity as an EFT
 - Einstein-Hilbert Lagrangian is the lowest order term.
 - Higher operators in curvature giving the corrections from an unknown UV theory.



Introduction Renormalization of GR.

- Renormalization of GR to one^1 and two $loops^2$ "introduces" the counterterms,

$$\begin{split} L_{\infty}^{(1)} &\propto \int d^4x \sqrt{|g|} \left(\frac{1}{60} R^2 + \frac{7}{10} R^2_{\mu\nu} \right) \xrightarrow{On-shell} 0 \\ L_{\infty}^{(2)} &\propto \int d^4x \sqrt{|g|} R_{\mu\nu\zeta\xi} R^{\zeta\xi\rho\sigma} R_{\rho\sigma}^{\mu\nu} \xrightarrow{On-shell} \int d^4x \sqrt{|g|} W_{\mu\nu\zeta\xi} W^{\zeta\xi\rho\sigma} W_{\rho\sigma}^{\mu\nu}, \end{split}$$

with $W_{\mu\nu\zeta\xi}$ the Weyl tensor.

¹G. 't Hooft and M. J. G. Veltman, 'One loop divergencies in the theory of gravitation', Ann. Inst. H. Poincare Phys. Theor. 20, 69–94 (1974).

²M. H. Goroff and A. Sagnotti, 'Quantum gravity at two loops', Physics Letters B 160 (1985).



Introduction Spherically-symmetric spacetimes I

• The action we considered is

$$S = \int d^4x \sqrt{|g|} \Big\{ -\frac{1}{2\kappa^2} R + \omega \kappa^2 W_{\mu\nu\zeta\xi} W^{\zeta\xi\rho\sigma} W_{\rho\sigma}^{\ \mu\nu} \Big\}$$

- **QUESTION:** Are Schwarzschild's solution and its horizon structurally stable under the GS perturbation?
- We only considered spherically-symmetric (S-S) spacetimes.



Introduction Spherically-symmetric spacetimes II

- In GR there is Birkhoff's Theorem \rightarrow Schwarzschild.
- Quadratic terms are compatible with Schwarzschild's solution.
- GS counterterm is Schwarzschild-excluding ³.
 - How bad is the incompatibility under small perturbations?
 - Do perturbations remove the event horizons?
 - Birkhoff?

 $^3 \rm S.$ Deser and B. Tekin, 'Shortcuts to high symmetry solutions in gravitational theories', Classical and Quantum Gravity 20, 4877–4883 (2003).

Table of Contents



▶ Introduction

 \blacktriangleright Results

▶ Summary and conclusions





- We could not find exact solutions to the complete EoM.
- Power series and perturbative solutions.
- Many non-trivial conformally-flat solutions to the GS counterterm.



Results Solutions of CG I.

• Let us compare with conformal gravity (CG).

$$S = \int d^4x \sqrt{|g|} \Big\{ W_{\mu\nu\zeta\xi} W^{\zeta\xi\mu\nu} \Big\}$$

vacuum solutions are related to the traceless Bach's tensor,

$$B_{\mu\nu} := \nabla^{\lambda} \nabla_{\lambda} K_{\mu\nu} - \nabla^{\lambda} \nabla_{\mu} K_{\lambda\nu} + K^{\lambda\beta} W_{\lambda\mu\beta\nu} = 0,$$

where the Schouten tensor is,

$$K_{\mu\nu} := \frac{1}{n-2} \left(R_{\mu\nu} - \frac{R}{n-1} g_{\mu\nu} \right)$$





• The equations of motion,

$$B_{\mu\nu} := \nabla^{\lambda} \nabla_{\lambda} K_{\mu\nu} - \nabla^{\lambda} \nabla_{\mu} K_{\lambda\nu} + K^{\lambda\beta} W_{\lambda\mu\beta\nu} = 0,$$

Admit Schwarzschild's spacetime, which is not conformally flat.

• They also admit any S-S conformally flat solution.





• Given an S-S spacetime with the line element,

$$ds^{2} = B(r,t) dt^{2} - A(r,t)dr^{2} - r^{2} d\Omega_{2}^{2},$$

• The GS counterterm,

$$S = \int d^4x \sqrt{|g|} \Big\{ W_{\mu\nu\zeta\xi} W^{\zeta\xi\rho\sigma} W_{\rho\sigma}^{\ \mu\nu} \Big\}$$

has S-S vacuum solutions satisfying a unique condition. The solutions have to be Weyl flat.





- Any S-S conformally flat metric will be a vacuum solution to the GS EoM.
- Since these solutions also belong to the set of solutions of CG, the proof for Birkhoff's theorem in CG⁴ holds.
 Thus, all the S-S vacuum solutions to the GS EoM are static.
- This is expected to hold for contractions of $p \ge 3$ Weyl tensors.

⁴Riegert, R. J.'Birkhoff's Theorem in Conformal Gravity', In Physical Review Letters (Vol. 53, Issue 4, pp. 315–318). American Physical Society (APS) (1984).





• As a way to probe the singular behavior near r = 0 we considered,

$$A(r) := r^{s} (a_{s} + a_{s+1} r + \cdots),$$

$$B(r) := b_{t} r^{t} (1 + b_{t+1} r + \cdots),$$

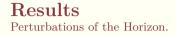
and see the (s, t) values that solve the EoM.

• Only,

$$(0,0)$$
 and $(2,2)$

The GS term *dominates* the EoM for $r \to 0$. The singularity cannot be that of Schwarzschild (1, -1).





- To test the horizon region we considered a perturbative expansion of the g_{00} component of the metric near the horizon.
- For arbitrarily small perturbations the horizon is just shifted.
- For a region of the parameter space there are horizonless solutions.

Table of Contents



▶ Introduction

 \blacktriangleright Results

► Summary and conclusions

Summary and Conclusions



- We found a unique condition that characterizes all the spherically symmetric vacuum solutions to the GS counterterm EoM.
- Quantum corrections induce the GS counterterm. This modifies the EoM. A perturbative analysis indicates that they might admit horizonless solutions.
- Open questions;
 - Can we put the absence of the horizon on solid ground with an exact solution?
 - Can we extend our conclusions to less symmetric spacetimes?





Thanks for your attention!