

Search for light Charged Higgs at the LHC

Abdesslam Arribib

Faculté des Sciences et Techniques Tangier, Morocco

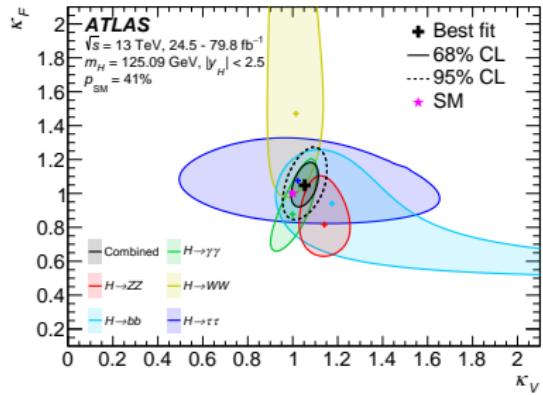
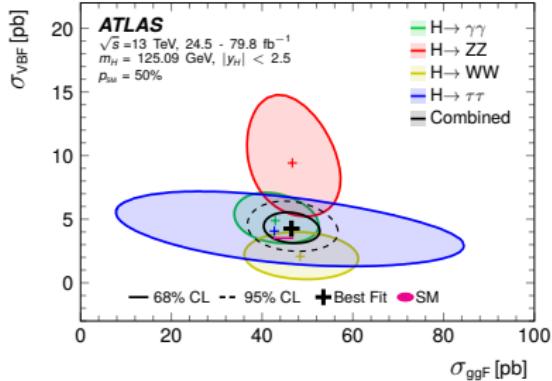
Particle Physics colloquium , KIT, 28th July 2022



كلية العلوم والتكنولوجيات . ملتقى

- Introduction
- Two Higgs doublet model (2HDM)
- Charged Higgs production at the LHC and decays
- Bosonic decays of charged Higgs: $H^\pm \rightarrow W^\pm A^0/W^\pm h^0$
- $W4\gamma$, $W4b$, $W2b2\tau$ signatures for a light H^\pm at the LHC.
- CP violation in charged Higgs production and decays.
- Conclusions

Introduction:



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- The improvement of the Higgs-like mass and Higgs-like coupling measurements.
- Find a clear hint of new physics beyond SM

Introduction:

After the Higgs-like discovery at $7 \oplus 8 \oplus 13$ TeV LHC, the mission of the LHC run at 13.6 TeV is:

- The improvement of the Higgs-like mass and Higgs-like coupling measurements.
- Find a clear hint of new physics beyond SM
- Accurate measurements of the Higgs-like couplings to SM particles would help to determine if the Higgs-like particle is the SM Higgs or a Higgs that belongs to a higher representations:
more doublets, doublet & triplets, doublet & singlets
- Most of the High representations predicts:
singly and/or doubly charged Higgs

Extended Higgs sector: EWPT

mass terms:

$$\sum_i (D_\mu \Phi_i)^+ (D_\mu \Phi_i) \quad , \quad D_\mu = \partial_\mu + ig \vec{T}_a \vec{W}^a_\mu + ig' \frac{Y}{2} B_\mu$$

$$m_W^2 = \sum_i g^2 \frac{v_i^2}{2} (I_i(I_i + 1) - \frac{Y_i^2}{4}) \quad , \quad m_Z^2 = \frac{g^2}{4c_W^2} \sum_i v_i^2 Y_i^2$$

$$\rho = \frac{m_W^2}{c_W^2 m_Z^2} = \frac{\sum_i v_i^2 (I_i(I_i + 1) - \frac{Y_i^2}{4})}{\sum_i v_i^2 \frac{Y_i^2}{2}} \approx 1.00037 \pm 0.00023$$

$$\delta\rho = \frac{\Sigma_{WW}(0)}{m_W^2} - \frac{\Sigma_{ZZ}(0)}{m_Z^2} \approx \frac{3G_F m_t^2}{8\pi^2 \sqrt{2}} + \dots$$

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1. Doublets ($I_i=1/2$, $Y_i=\pm 1$): it works at tree level;
but “radiative corrections can modify ”

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2. choose : $I = 3$ and $Y = 4$ such that $4I_i(I_i + 1) = 3Y_i^2$, but it is rather complicated

Extended Higgs sector: EWPT

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3. Triplet representation: like in type-II seesaw model
(one-doublet and one-triplet)

$$m_W^2 = \frac{g^2}{4} (v_d^2 + 2v_t^2) \quad , \quad m_Z^2 = \frac{g^2}{4 \cos^2_W} (v_d^2 + 4v_t^2) \quad , \quad \rho = \frac{v_d^2 + 2v_t^2}{v_d^2 + 4v_t^2} \neq 1$$

tune the triplet vev. In type-II see-saw: $v_t < 5 - 8 \text{ GeV}$

$$\Phi_1 = \begin{pmatrix} \phi_1^+ \\ \frac{1}{\sqrt{2}}(v_1 + \phi_1^0 + ia_1) \end{pmatrix}; \quad \Phi_2 = \begin{pmatrix} \phi_2^+ \\ \frac{1}{\sqrt{2}}(v_2 + \phi_2^0 + ia_2) \end{pmatrix}.$$

The most general potential for 2HDM:

$$\begin{aligned}
 V(\Phi_1, \Phi_2) &= m_1^2 \Phi_1^\dagger \Phi_1 + m_2^2 \Phi_2^\dagger \Phi_2 + (\textcolor{green}{m_{12}^2} \Phi_1^\dagger \Phi_2 + \text{h.c.}) \\
 &+ \frac{1}{2} \lambda_1 (\Phi_1^\dagger \Phi_1)^2 + \frac{1}{2} \lambda_2 (\Phi_2^\dagger \Phi_2)^2 \\
 &+ \lambda_3 (\Phi_1^\dagger \Phi_1)(\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2)(\Phi_2^\dagger \Phi_1) \\
 &+ \frac{1}{2} [\lambda_5 (\Phi_1^\dagger \Phi_2)^2 + (\textcolor{red}{\lambda_6} \Phi_1^\dagger \Phi_1 + \textcolor{red}{\lambda_7} \Phi_2^\dagger \Phi_2) \Phi_1^\dagger \Phi_2 + \text{h.c.}],
 \end{aligned}$$

$$\Phi_1 = \begin{pmatrix} \phi_1^+ \\ \frac{1}{\sqrt{2}}(v_1 + \phi_1^0 + ia_1) \end{pmatrix}; \quad \Phi_2 = \begin{pmatrix} \phi_2^+ \\ \frac{1}{\sqrt{2}}(v_2 + \phi_2^0 + ia_2) \end{pmatrix}.$$

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 \end{aligned}$$

- \mathbb{Z}_2 : $\Phi_i \rightarrow -\Phi_i \Leftrightarrow \lambda_{6,7} = 0$
- No explicit CP violation: $Im(m_{12}^2 \lambda_{5,6,7}) = 0$

$$\Phi_1 = \begin{pmatrix} \phi_1^+ \\ \frac{1}{\sqrt{2}}(v_1 + \phi_1^0 + ia_1) \end{pmatrix}; \quad \Phi_2 = \begin{pmatrix} \phi_2^+ \\ \frac{1}{\sqrt{2}}(v_2 + \phi_2^0 + ia_2) \end{pmatrix}.$$

$$-\mathcal{L}_Y = \sum_{a=1,2} \left[\bar{Q}_L Y_d^a \Phi_a d_R + \bar{Q}_L Y_u^a \tilde{\Phi}_a u_R + \bar{L}_L Y_\ell^a \Phi_a \ell_R + \text{h.c.} \right],$$

leads to FCNCs at tree level.

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leads to FCNCs at tree level.

- Classification of 2HDMs satisfying the Glashow-Weinberg condition which guarantees the absence of tree-level FCNC.

Type-I	$Y_{u,d}^1 = 0, Y_\ell^1 = 0$
Type-II	$Y_u^1 = Y_{d,\ell}^2 = 0$
Type-III (X)	$Y_{u,d}^1 = Y_\ell^2 = 0$
Type-IV (Y)	$Y_{u,\ell}^1 = Y_d^2 = 0$

$$\Phi_1 = \begin{pmatrix} \phi_1^+ \\ \frac{1}{\sqrt{2}}(v_1 + \phi_1^0 + ia_1) \end{pmatrix}; \quad \Phi_2 = \begin{pmatrix} \phi_2^+ \\ \frac{1}{\sqrt{2}}(v_2 + \phi_2^0 + ia_2) \end{pmatrix}.$$

- first rotate a_i and ϕ_i^+ in order to obtain the goldstones G^0, G^\pm
- CP-odd $A^0 = -s_\beta a_1 + c_\beta a_2$ and a pair of $H^\pm = -s_\beta \phi_1^\pm + c_\beta \phi_2^\pm$.

$$\Phi_1 = \begin{pmatrix} \phi_1^+ \\ \frac{1}{\sqrt{2}}(v_1 + \phi_1^0 + ia_1) \end{pmatrix}; \quad \Phi_2 = \begin{pmatrix} \phi_2^+ \\ \frac{1}{\sqrt{2}}(v_2 + \phi_2^0 + ia_2) \end{pmatrix}.$$

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- CP-odd $A^0 = -s_\beta a_1 + c_\beta a_2$ and a pair of $H^\pm = -s_\beta \phi_1^\pm + c_\beta \phi_2^\pm$.
- In the general case with CP violation, the neutral mass matrix \mathcal{M}_0^2 is diagonalized by an orthogonal 3×3 matrix O :

$$(\phi_1^0, \phi_2^0, a)_\alpha^T = O_{\alpha i} (H_1, H_2, H_3)_i^T$$

such that $O^T \mathcal{M}_0^2 O = \text{diag}(M_{H_1}^2, M_{H_2}^2, M_{H_3}^2)$ with
 $M_{H_1} \leq M_{H_2} \leq M_{H_3}$.

$$\begin{aligned}
\mathcal{L}_{H_i \bar{f} f} &= -\frac{g m_f}{2m_W} \bar{f} \left(Y_{i,f}^S + i Y_{i,f}^P \gamma_5 \right) f H_i , \\
\mathcal{L}_{H^\pm tb} &= +\frac{g m_b}{\sqrt{2}m_W} \bar{b} (c_L P_L + c_R P_R) t H^- + \text{h.c.} , \\
\mathcal{L}_{H_i VV} &= -\frac{g m_V}{2c_W} \underbrace{(\cos \beta O_{\phi_2 i} + \sin \beta O_{\phi_1 i})}_{H_i VV} g_{\mu\nu} V^\mu V^\nu \\
\mathcal{L}_{H_i H^\pm W^\pm} &= -\frac{g}{2} (S_i + iP_i) \left[H^- \left(i \overset{\leftrightarrow}{\partial}_\mu \right) H_i \right] W^{+\mu} + \text{h.c.} , \\
S_i &= c_\beta O_{\phi_2 i} - s_\beta O_{\phi_1 i} , \quad P_i = O_{a i}
\end{aligned}$$

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\mathcal{L}_{H_i VV} &= -\frac{g m_V}{2c_W} \underbrace{(\cos \beta O_{\phi_2 i} + \sin \beta O_{\phi_1 i})}_{H_i VV} g_{\mu\nu} V^\mu V^\nu \\
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Sum rules:

- $\sum_i (H_i VV)^2 = 1$
- $(H_i VV)^2 + |H^\pm W^\mp H_i|^2 = 1$ for $i = 1, 2, 3$
- $\sin^2 \beta [(Y_{i,t}^S)^2 + (Y_{i,t}^P)^2] + \cos^2 \beta [(Y_{i,b}^S)^2 + (Y_{i,b}^P)^2] = 1$

The Yukawa Lagrangian:

$$\begin{aligned}
 -\mathcal{L}_{Yuk} = & \sum_{\psi=u,d,l} \left(\frac{m_\psi}{v} \kappa_\psi^h \bar{\psi} \psi h^0 + \frac{m_\psi}{v} \kappa_\psi^H \bar{\psi} \psi H^0 - i \frac{m_\psi}{v} \kappa_\psi^A \bar{\psi} \gamma_5 \psi A^0 \right) + \\
 & \left(\frac{V_{ud}}{\sqrt{2}v} \bar{u} (m_u \kappa_u^A P_L + m_d \kappa_d^A P_R) d H^+ + \frac{m_l \kappa_l^A}{\sqrt{2}v} \bar{\nu}_L I_R H^+ + H.c. \right)
 \end{aligned}$$

	κ_u^h	κ_d^h	κ_l^h	κ_u^A	κ_d^A	κ_l^A
Type-I	c_α/s_β	c_α/s_β	c_α/s_β	$\cot\beta$	$-\cot\beta$	$-\cot\beta$
Type-II	c_α/s_β	$-s_\alpha/c_\beta$	$-s_\alpha/c_\beta$	$\cot\beta$	$\tan\beta$	$\tan\beta$
Type-III	c_α/s_β	c_α/s_β	$-s_\alpha/c_\beta$	$\cot\beta$	$-\cot\beta$	$\tan\beta$
Type-IV	c_α/s_β	$-s_\alpha/c_\beta$	c_α/s_β	$\cot\beta$	$\tan\beta$	$-\cot\beta$

- Couplings:

$$hVV \propto \sin_{\beta-\alpha}, \quad HVV \propto \cos_{\beta-\alpha}, \quad AVV = 0$$

$$hH^\pm W^\mp \propto \cos_{\beta-\alpha}, \quad HH^\pm W^\mp \propto \sin_{\beta-\alpha}, \quad AH^\pm W^\mp \propto \frac{g}{2}$$

$$H^\pm W^\mp \gamma = 0 \text{ (e.m inv)}, \quad H^\pm W^\mp Z = 0 \text{ but loop mediated}$$

- 2 alignment limits:

- $h=125$ GeV SM-like: $\sin_{\beta-\alpha} = 1$ (Decoupling limit)
- $h < H=125$ GeV SM-like: $\cos_{\beta-\alpha} = 1$:
non-detected decays: $Br(H \rightarrow h^0 h^0, A^0 A^0, Z^* A^0) < 10\%$

Constraints

- Stability of the 2HDM potential requires that it should be bounded from below, i.e. that there is no direction in field space along which the potential becomes negative.

Deshpande and E. Ma, PRD18'1978

$$\lambda_1 > 0 \quad , \quad \lambda_2 > 0$$

$$\lambda_3 > -\sqrt{\lambda_1 \lambda_2}$$

$$\lambda_3 + \min(0, \lambda_4 - |\lambda_5|) > -\sqrt{\lambda_1 \lambda_2}$$

- The vacuum of the model is global one if and only if:
 $m_{12}^2(m_{11}^2 - k^2 m_{22}^2)(\tan \beta - k) > 0$; $k = \sqrt[4]{\frac{\lambda_1}{\lambda_2}}$
- Perturbative unitarity: $V_L^+ V_L^- \rightarrow V_L^+ V_L^-$, $h_i h_j \rightarrow h_i h_j \dots$

$$a_{\pm} = \frac{1}{16\pi} \left\{ \frac{3}{2}(\lambda_1 + \lambda_2) \pm \sqrt{\frac{9}{4}(\lambda_1 - \lambda_2)^2 + (2\lambda_3 + \lambda_4)^2} \right\},$$

$$b_{\pm} = \frac{1}{16\pi} \left\{ \frac{1}{2}(\lambda_1 + \lambda_2) \pm \sqrt{\frac{1}{4}(\lambda_1 - \lambda_2)^2 + \lambda_4^2} \right\},$$

$$c_{\pm} = d_{\pm} = \frac{1}{16\pi} \left\{ \frac{1}{2}(\lambda_1 + \lambda_2) \pm \sqrt{\frac{1}{4}(\lambda_1 - \lambda_2)^2 + \lambda_5^2} \right\},$$

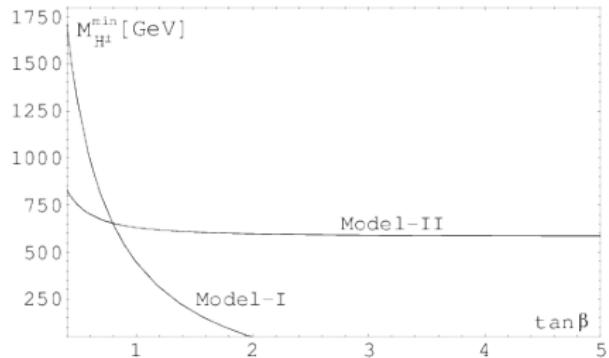
$$e_1 = \frac{1}{16\pi} (\lambda_3 + 2\lambda_4 - 3\lambda_5), \quad e_2 = \frac{1}{16\pi} (\lambda_3 - \lambda_5),$$

$$f_+ = \frac{1}{16\pi} (\lambda_3 + 2\lambda_4 + 3\lambda_5), \quad f_- = \frac{1}{16\pi} (\lambda_3 + \lambda_5),$$

$$f_1 = f_2 = \frac{1}{16\pi} (\lambda_3 + \lambda_4).$$

$b \rightarrow s\gamma$ constraints

- In 2HDM-II and IV: $m_{H^\pm} > 800$ GeV for any $\tan\beta > 1$
[Misiak et al EPJC'2017, JHEP'20]
- in 2HDM-I there is no limit on H^\pm for $\tan\beta \geq 2$



- in 2HDM-III, light charged Higgs ≤ 200 GeV with large $\tan\beta > 30$ is excluded from $\tau \rightarrow \mu\nu\nu$

[T. Enomoto and R. Watanabe JHEP'2016]

Charged Higgs production

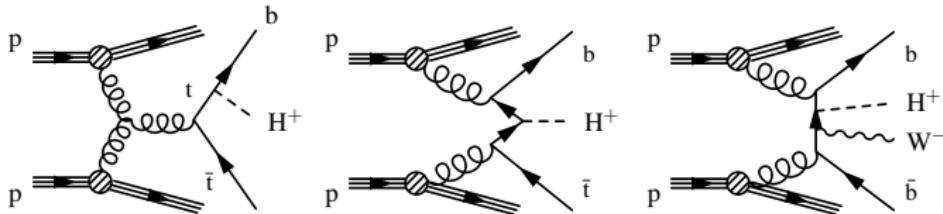
(See "Prospects for charged Higgs searches at the LHC,"
arXiv:1607.01320: A. Akeroyd et al)

- Light charged Higgs, i.e, with $m_{H^\pm} \leq m_t - m_b$: are copiously produced from $t\bar{t}$ production $pp \rightarrow t\bar{t}^* \rightarrow t\bar{b}H^- + \text{c.c.}$

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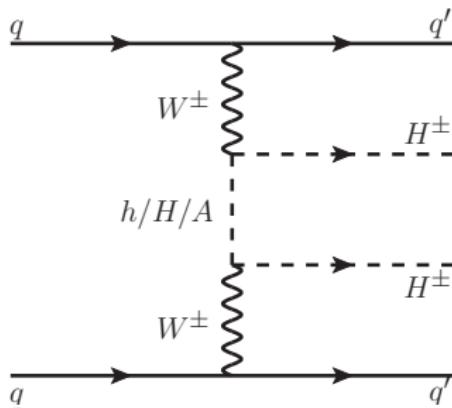
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- various direct production modes:
QCD: $gb \rightarrow tH^-$ and $gg \rightarrow t\bar{b}H^-$,



- $gg \rightarrow W^\pm H^\mp$ (loop) , $b\bar{b} \rightarrow h^*, H^*, A^* \rightarrow W^\pm H^\mp$
 $q\bar{q} \rightarrow \gamma^*, Z^* \rightarrow H^+ H^-$, $gg \rightarrow H^+ H^-$ (loop)
 $q\bar{q}' \rightarrow W^* \rightarrow \phi H^\pm$ where $\phi = h, H, A,$

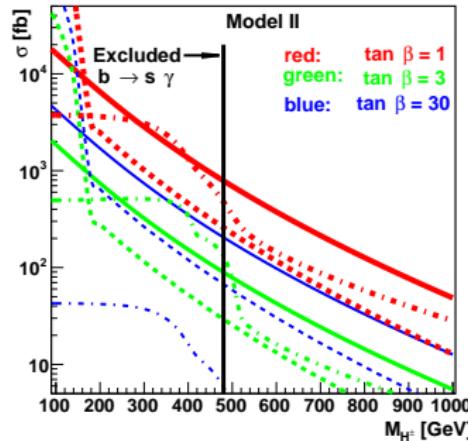
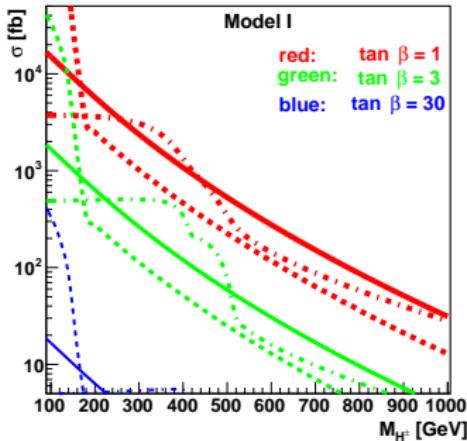
- $gg \rightarrow W^\pm H^\mp$ (loop) , $b\bar{b} \rightarrow h^*, H^*, A^* \rightarrow W^\pm H^\mp$
 $q\bar{q} \rightarrow \gamma^*, Z^* \rightarrow H^+ H^-$, $gg \rightarrow H^+ H^-$ (loop)
 $q\bar{q}' \rightarrow W^* \rightarrow \phi H^\pm$ where $\phi = h, H, A,$
- Resonant production: $c\bar{s}, c\bar{b} \rightarrow H^+$
- W-Z , W- γ fusion:
 $q\bar{q} \rightarrow W^\pm Z \rightarrow jjH^\pm$ or $W^\pm \gamma \rightarrow jjH^\pm$
(loop mediated in 2HDM)
- W-Z fusion: possible with triplet representation

$$pp \rightarrow j_F j_F W^{\pm *} W^{\pm *} \rightarrow H^\pm H^\pm j_F j_F$$



$$\propto \frac{m_H^2 - m_A^2}{(t - m_H^2)(t - m_A^2)}$$

Cross sections $pp \rightarrow H^\pm X$

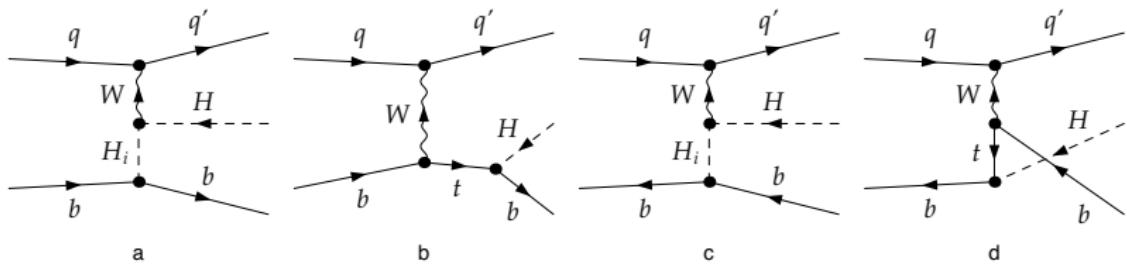


- “fermionic”: $g\bar{b} \rightarrow H^+\bar{t}$, (solid), $gg \rightarrow H^+b\bar{t}$, (dotted),
- “bosonic”: $gg \rightarrow H_j \rightarrow H^+W^-$, (dash-dotted).

W -Higgs fusion

- W -Higgs fusion : $qb \rightarrow q'H^+b$

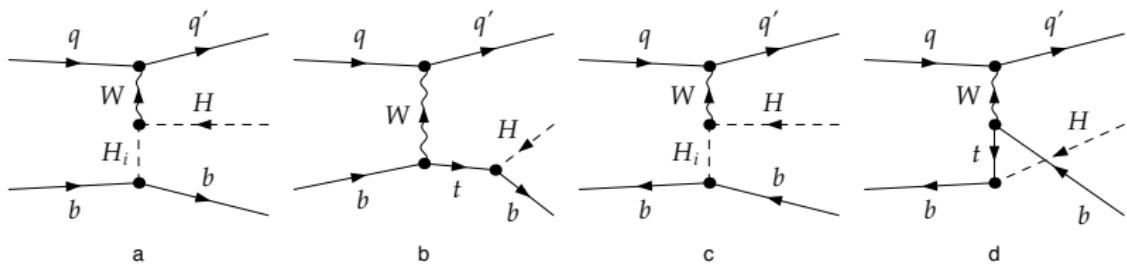
A.A, K.M. Cheung, J.S.Lee and C. T. Lu' JHEP'2016 (2HDM) , Moretti, Odagiri PRD'1997 (MSSM)



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Taking the type II model as an example, we find

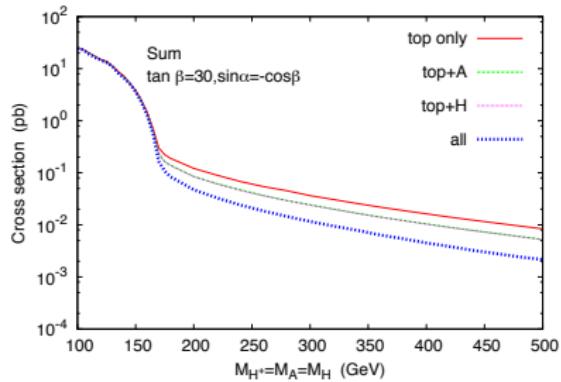
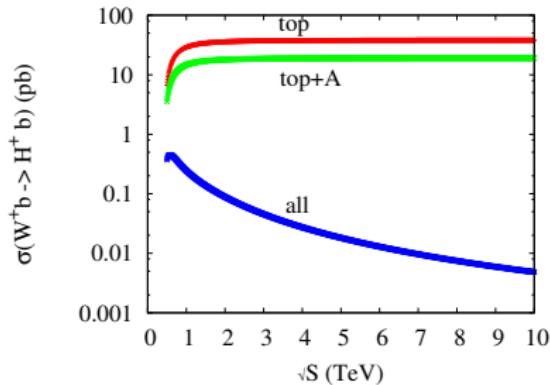
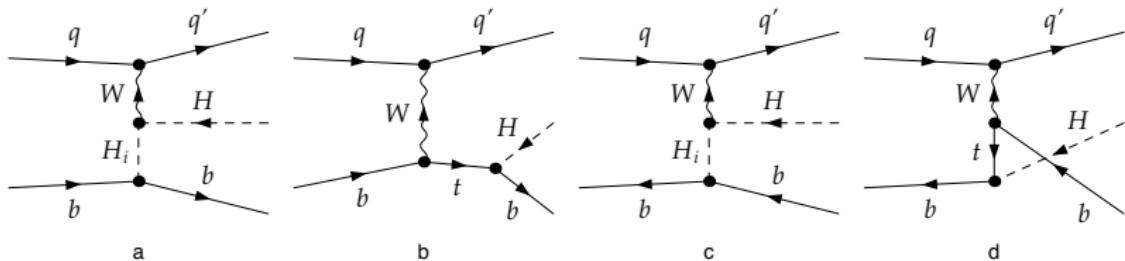
$$\sigma(W^+b \rightarrow H^+b)|_{t \text{ only}} \propto 4 \tan^2 \beta,$$

$$\sigma(t + H \text{ only}) = \sigma(t + A \text{ only}) \propto 2 \tan^2 \beta,$$

$$\sigma(W^+b \rightarrow H^+b)|_{t+H+A} \propto \mathcal{O}\left(\frac{m_t^2}{s} + \frac{M_{H_i}^2}{t}\right)$$

$pp \rightarrow jH^+b$ at LHC 14 TeV

A.A, K.M. Cheung, J.S.Lee and C. T. Lu'JHEP'2016



- $e^+e^- \rightarrow \gamma^*, Z^* \rightarrow H^+H^-$ S. Komamiya, PRD'38 (1988)

LO: cross section is a function of m_{H^\pm} only.

NLO: is model dependent w/o SUSY :

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- $e^+e^- \rightarrow \gamma^*, Z^* \rightarrow t\bar{b}H^-$

Gutierrez-Rodriguez and Sampayo, hep-ph/1999, Kanemura, Moretti and Odagiri JHEP 02 (2001)

H^\pm at linear collider

- $e^+e^- \rightarrow W^\pm H^\mp$ (loops mediated: triangles and boxes)
A.A , W. Hollik and G. Moultaka NPB 581 (2000), S. Kanemura EPJC 17 (2000)
- $e^+e^- \rightarrow Z^* \rightarrow W^\pm H^\mp$ (models with Higgs triplet)
- $e^+e^- \rightarrow \gamma^*, Z^* \rightarrow ZW^+H^- , SW^+H^- , S = h, H, A$

Charged Higgs decays

Fermionic decays

- $H^\pm \rightarrow \tau\nu$, cs , cb
- $H^\pm \rightarrow tb$

ATLAS report 3σ excess around $m_{H^\pm} = 130$ GeV: $H^+ \rightarrow cb$
[ATLAS-CONF-2021-037]

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[ATLAS-CONF-2021-037]

Bosonic decays

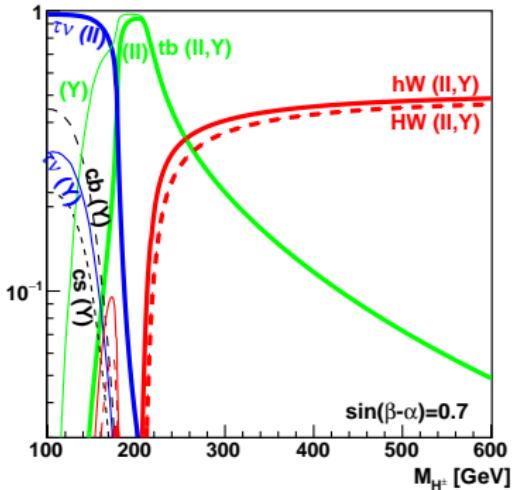
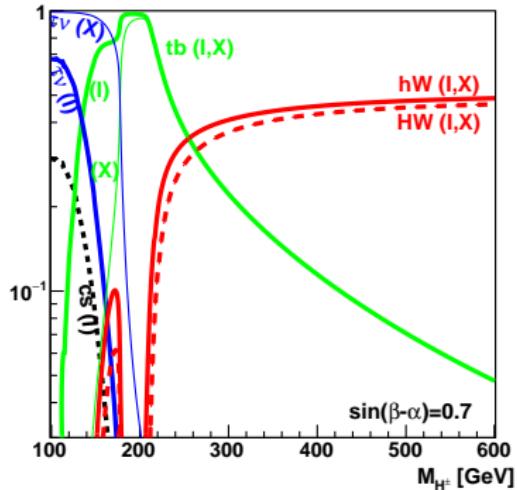
- $H^\pm \rightarrow W^\pm \phi^0$, $\phi^0 = h^0, A^0, H^0$
- $H^\pm \rightarrow W^\pm \gamma, W^\pm Z$: small because loop mediated

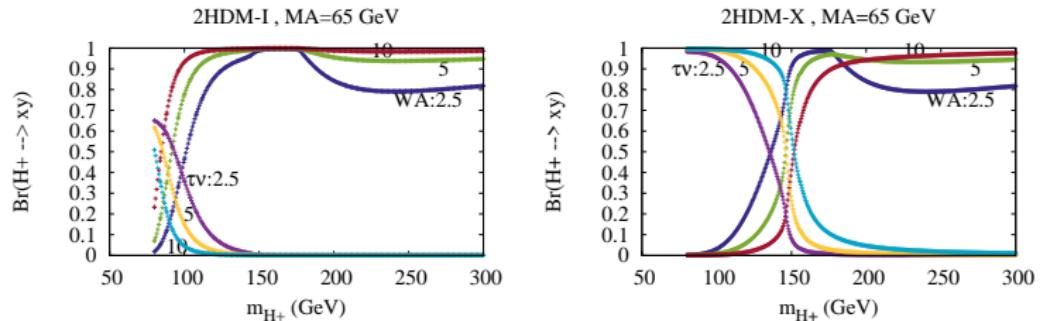
A.A, R. Benbrik, and TC.Yuan, IJMP2007

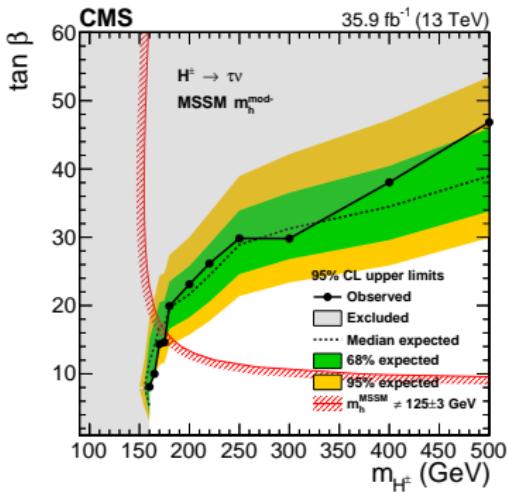
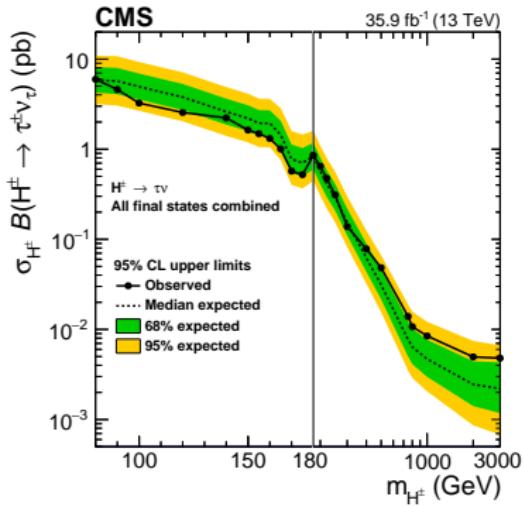
- $H^\pm \rightarrow W^\pm Z$ exists at tree level in triplet models.
(production through WZ fusion)

Branching ratio

Branching ratios for $\tan \beta = 3$

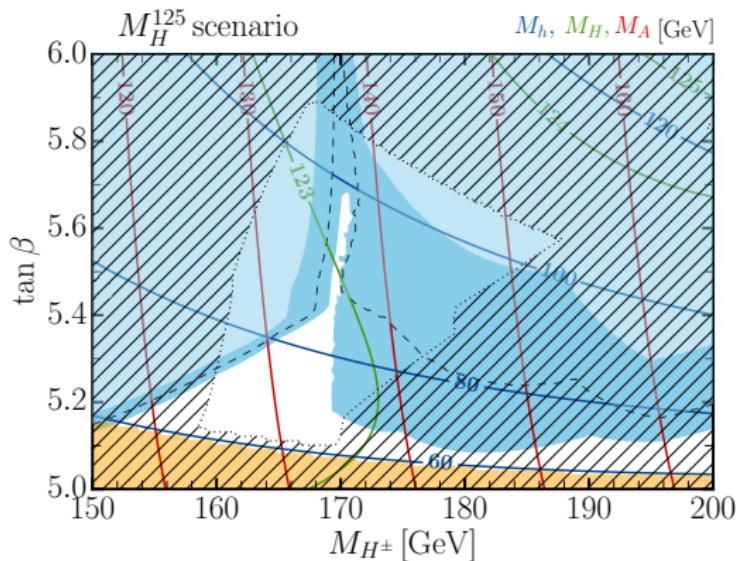




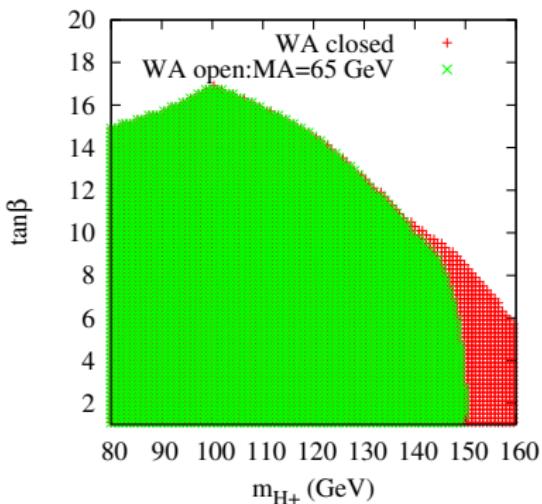
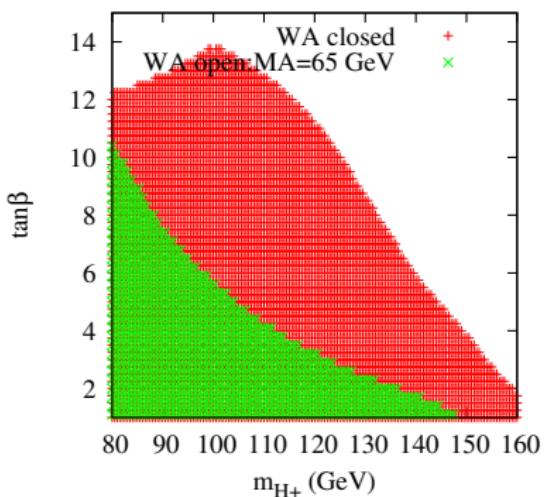


MSSM with $m_h < m_H = 125$ GeV:

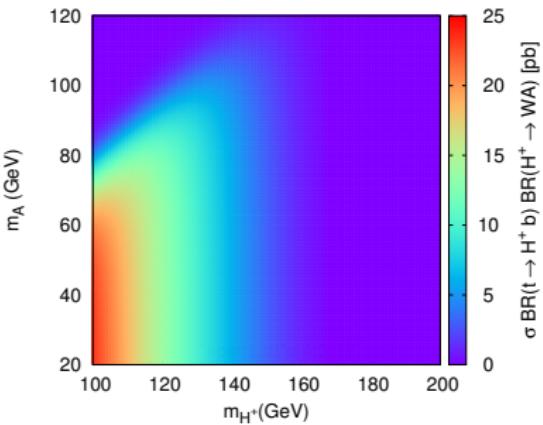
E. Bagnaschi et al EPJC'18 hep-ph/ arXiv:1808.07542



left: 2HDM-I, right: 2HDM-III, (WA open: $m_A = 65$ GeV)

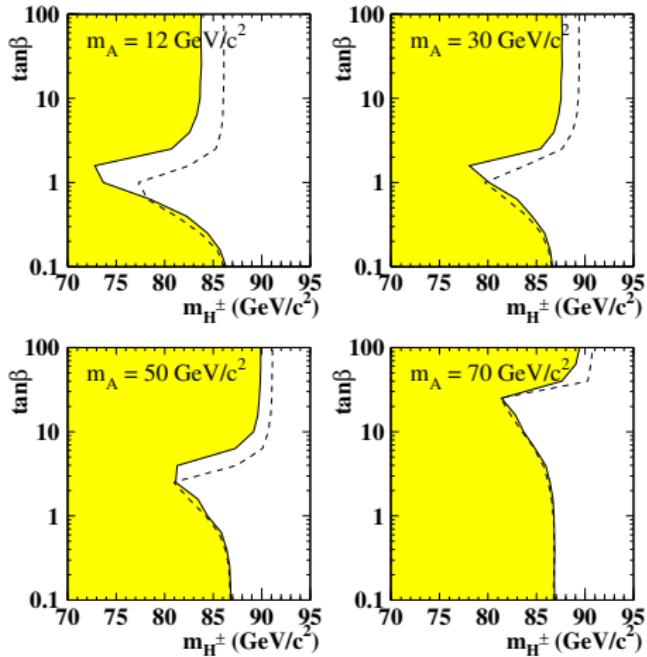


$$\sigma(t\bar{t}) \times Br(t \rightarrow bH^-) \times Br(H^- \rightarrow W^- A)$$



Search for $H^\pm \rightarrow W^\pm A^0$ at LEP-II

LEP 183-209 GeV



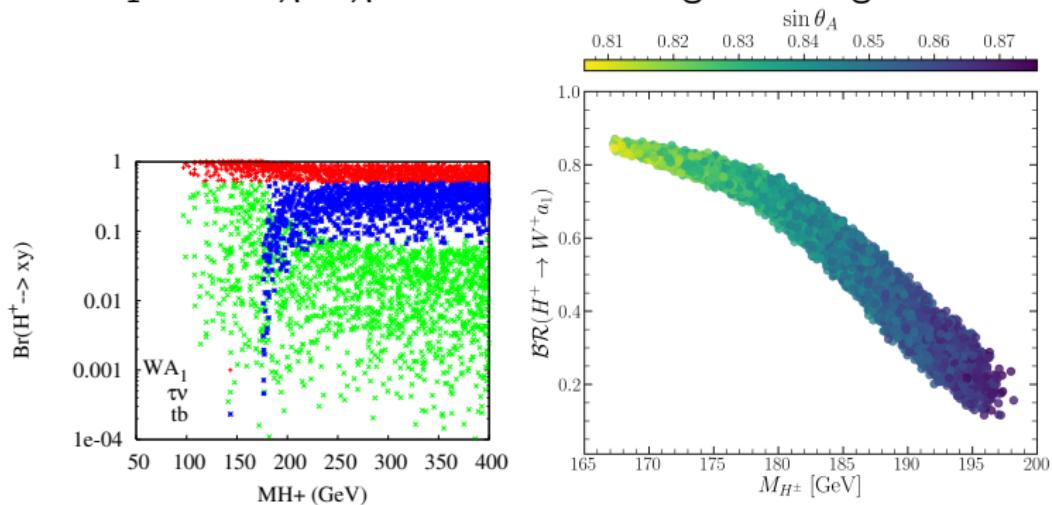
CMS searches: $H^\pm \rightarrow HW^\pm$ [hep-ex/2207.01046](#)

$H^\pm \rightarrow AW \rightarrow \mu^+ \mu^- W$ with $B(A \rightarrow \mu^+ \mu^-) = 1$ [hep-ex/1905.07453](#)

$H^\pm W^\mp a_1 \propto \cos \theta_A$: θ_A is the doublet-singlet mixing.

very light a_1 in the NMSSM: [A.Akeroyd, A.A and Q.S. Yan EPJC'07]

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H^0 -SM like ; $m_h < m_H = 125$ GeV

In the alignment limit $\cos(\beta - \alpha) \approx 1$, the heavy CP-even Higgs H^0 completely mimics the SM Higgs:

$$H^0 f\bar{f} = \frac{\sin \alpha}{\sin \beta} \approx 1$$

$$H^0 VV = \cos(\beta - \alpha) \approx 1$$

$$\begin{aligned} H^0 H^0 H^0 &= \frac{3g}{2m_W} \left(M_H^2 (c_{\beta-\alpha} \frac{\sin 2\alpha}{\sin 2\beta} - 2s_{\beta-\alpha}) + \lambda_5 v^2 s_{\beta-\alpha}^2 \right) \\ &\approx \frac{3g}{2m_W} m_H^2 \end{aligned}$$

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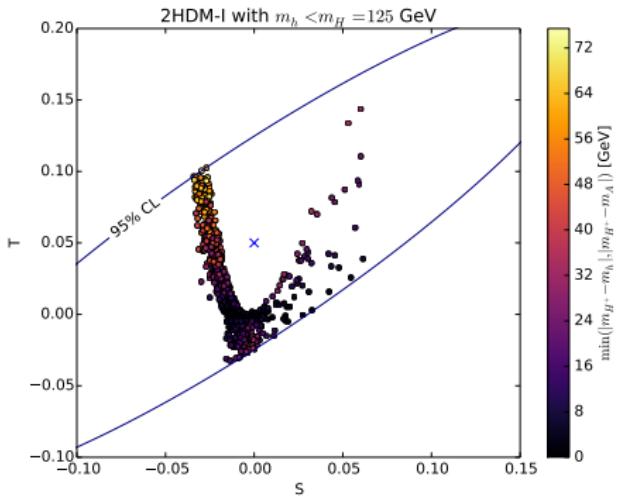
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- $m_h \leq m_H = 125$ GeV: $H^0 \rightarrow h^0 h^0$ and/or $H^0 \rightarrow A^0 A^0$ might be open: $Br(H^0 \rightarrow h^0 h^0) + Br(H^0 \rightarrow A^0 A^0) \leq 10\%$
- if h^0 and A^0 too light: $Z \rightarrow h^0 A^0 \propto \cos^2(\beta - \alpha)$
- For $m_h \leq 125$ GeV and $m_H = 125$ GeV: EWPT imply that H^\pm and A^0 would be also light.

EWPT: S and T



A.A, R. Benbrik, R. Enberg, W. Klemm, S. Moretti and S. Munir, PLB'17

$$M_W^{\text{CDF}} = 80.4435 \pm 0.0094 \text{ GeV.} [\text{CDF collaboration 'Science 2022'}]$$

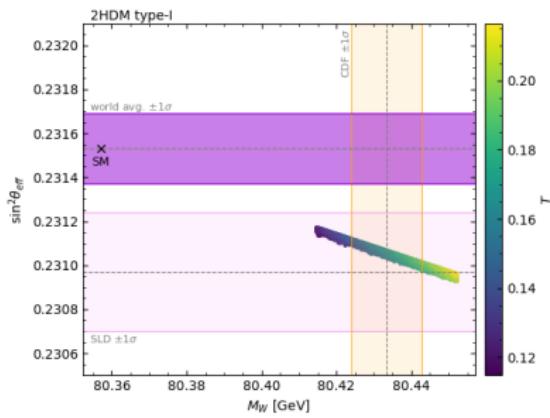
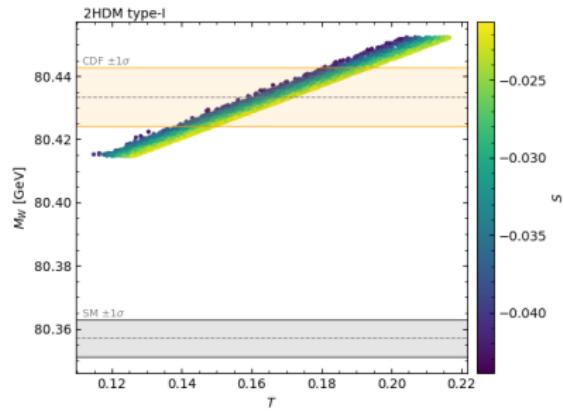
$$M_W^{\text{SM}} = 80.357 \pm 0.006 \text{ GeV.} [\text{Review of Particle Physics '2020}]$$

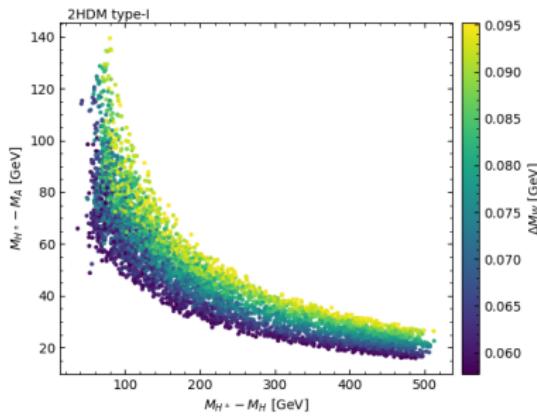
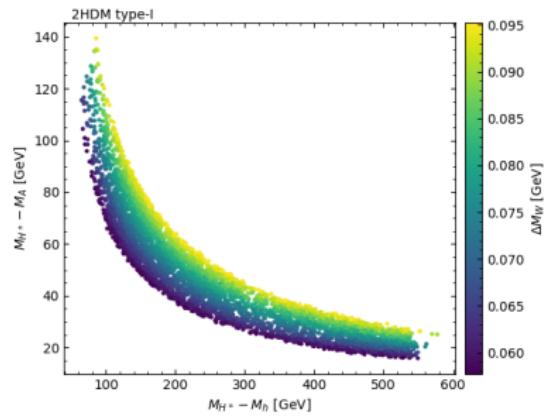
M_W^{CDF} presents a deviation from M_W^{SM} with a significance of 7.0σ .

$$(M_W^{2HDM})^2 - (M_W^{\text{SM}})^2 = \frac{\alpha_0 c_W^2 M_Z^2}{c_W^2 - s_W^2} \left[-\frac{1}{2}S + c_W^2 T + \frac{c_W^2 - s_W^2}{4s_W^2} U \right],$$

$$\Delta \sin^2 \theta_{\text{eff}} = \frac{\alpha_0}{c_W^2 - s_W^2} \left[\frac{1}{4}S - s_W^2 c_W^2 T \right].$$

[S. Hessenberger and W. Hollik : hep-ph/ 2207.03845: 2 loops improvement]



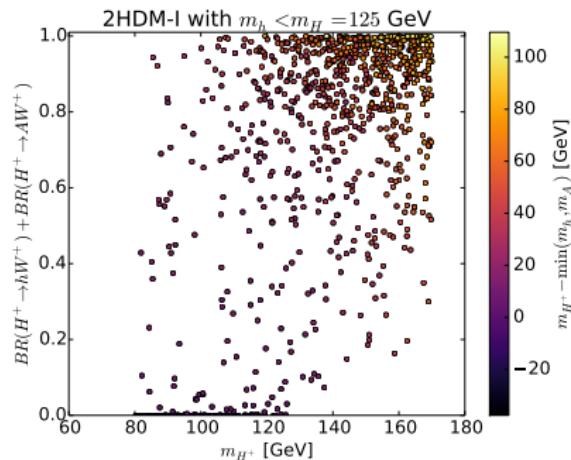


Can h^0 be Fermiophobic ?

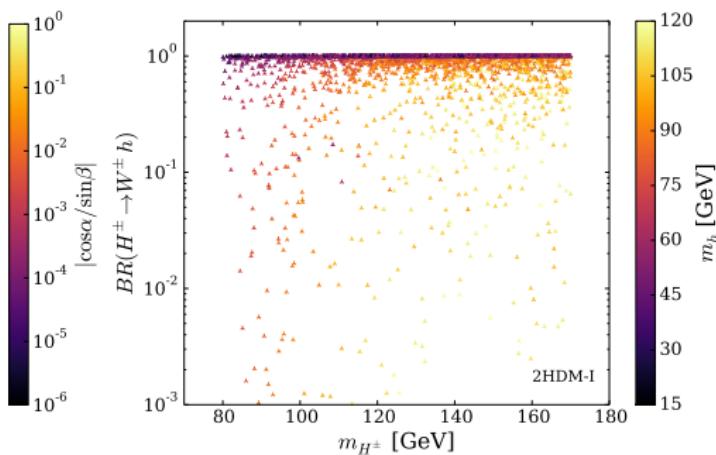
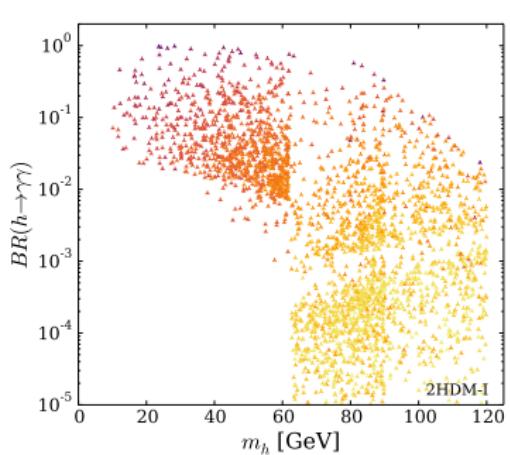
- In 2HDM-I, $h^0 f \bar{f} \propto \frac{\cos \alpha}{\sin \beta} = \sin(\beta - \alpha) + \cot \beta \cos(\beta - \alpha)$
For negative $\sin(\beta - \alpha)$ and positive $\cos(\beta - \alpha)$,
it is clear that $\cos \alpha \rightarrow 0$. h^0 becomes fermiophobic.
- $h^0 VV \propto \sin_{\beta-\alpha} \approx 0$; $h^0 \rightarrow \{VV^*, V^*V^*\}$ very suppressed;
 $h^0 \rightarrow \gamma\gamma$ could reach 100%

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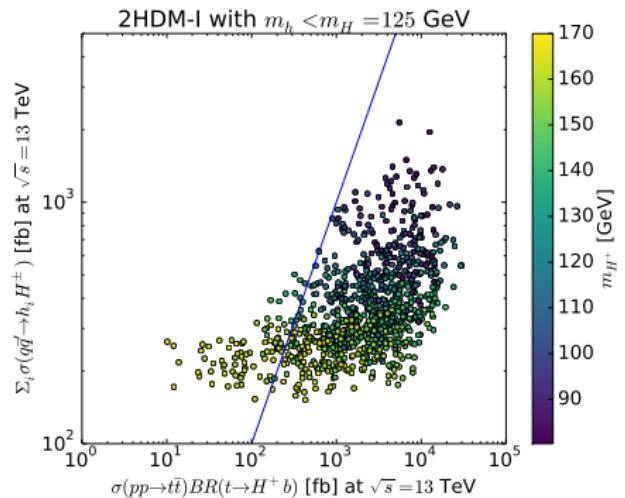
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- $h^0 VV \propto \sin_{\beta-\alpha} \approx 0$; $h^0 \rightarrow \{VV^*, V^*V^*\}$ very suppressed;
 $h^0 \rightarrow \gamma\gamma$ could reach 100%
- $H^\pm W^\mp h^0 \propto \cos(\beta - \alpha) \approx 1$
- light H^\pm can be produced from $t \rightarrow bH^+$ and also
 $pp \rightarrow W^* \rightarrow \{H^\pm h^0, H^\pm A^0\}$; $pp \rightarrow \gamma^*, Z^* \rightarrow H^\pm H^\mp$
- with h^0 close to fermiophobic,
 $pp \rightarrow t\bar{t} \rightarrow bWbH^+ \rightarrow 2b2Wh^0 \rightarrow 2b + 2W + 2\gamma$;
 $pp \rightarrow H^\pm h^0 \rightarrow Wh^0h^0 \rightarrow 4\gamma + W$



$\text{Br}(h^0 \rightarrow \gamma\gamma)$ and $\text{Br}(H^\pm \rightarrow W^\pm h^0)$

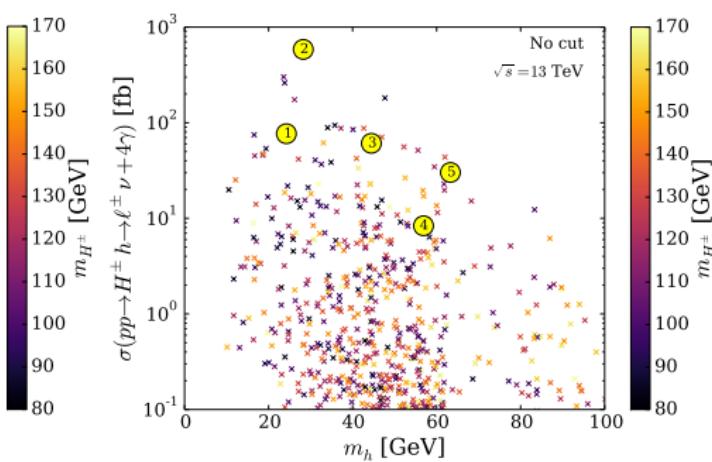
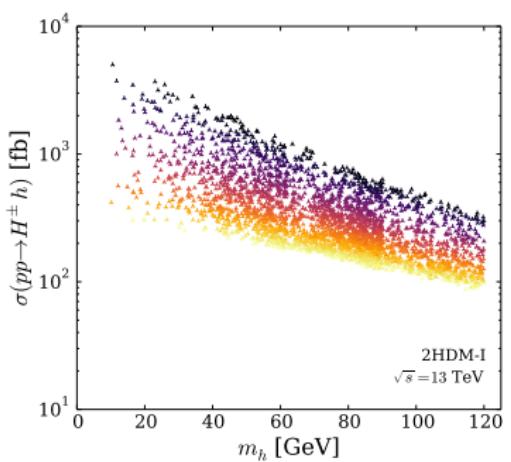


Comparison: $\sigma(pp \rightarrow t\bar{t}) \times BR(t \rightarrow H^+ b)$ vs. $\Sigma_i \sigma(q\bar{q}' \rightarrow H^\pm h_i)$



$$\sigma(q\bar{q}' \rightarrow H^\pm h^0); \sigma(q\bar{q}' \rightarrow l\nu 4\gamma)$$

BP	m_h	m_{H^\pm}	m_A	$\sin_{\beta-\alpha}$	$\tan \beta$	$\sigma_{W^\pm 4\gamma} [\text{fb}]$	$\text{Br}(h^0 \rightarrow \gamma\gamma)$
1	24.2	152.2	111.1	-0.048	20.9	359	0.94
2	28.3	83.7	109.1	-0.050	20.2	2740	0.97
3	44.5	123.1	119.9	-0.090	10.9	285	0.70
4	56.9	97.0	120.3	-0.174	5.9	39	0.22
5	63.3	148.0	129.2	-0.049	20.7	141	0.71



Cuts and selection efficiencies

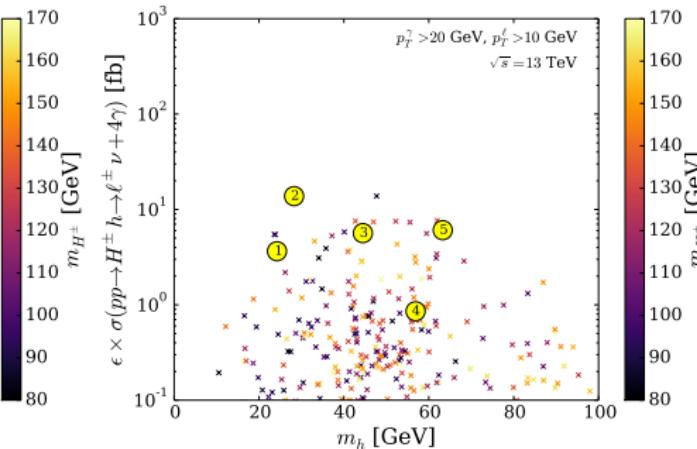
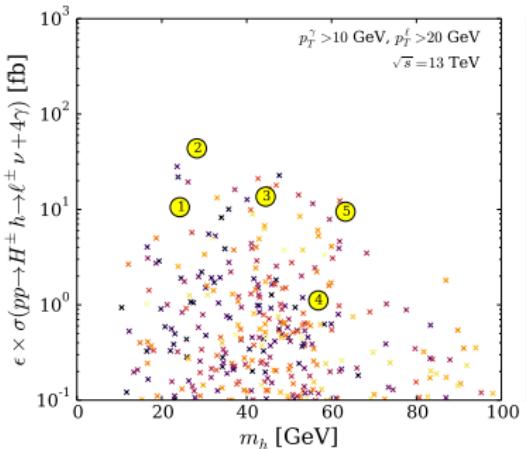
We require pseudorapidity $|\eta| < 2.5$ for the lepton and photons, and an isolation $\Delta R = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2} > 0.4$ for all objects.

- (i) all photons: $p_T^\gamma > 10$ GeV; charged lepton: $p_T^\ell > 20$ GeV,
- (ii) imposes that $p_T^\gamma > 20$ GeV and $p_T^\ell > 10$ GeV.
- The irreducible SM $W+4\gamma$ Background $< 10^{-6}$ pb.
- The selection efficiencies: $\epsilon = \sigma(\text{cuts})/\sigma(\text{no cuts})$.

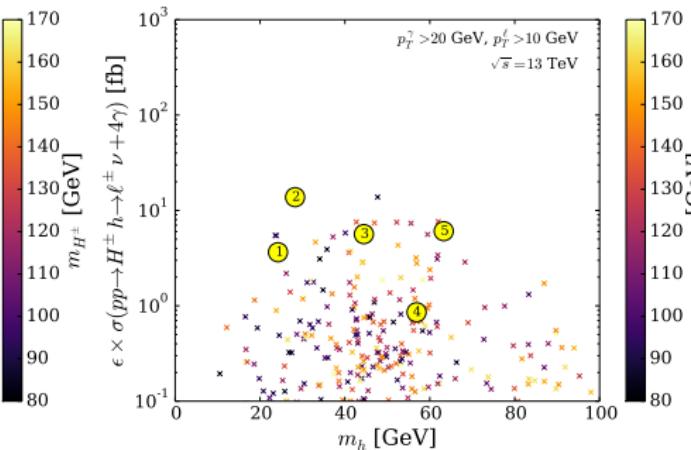
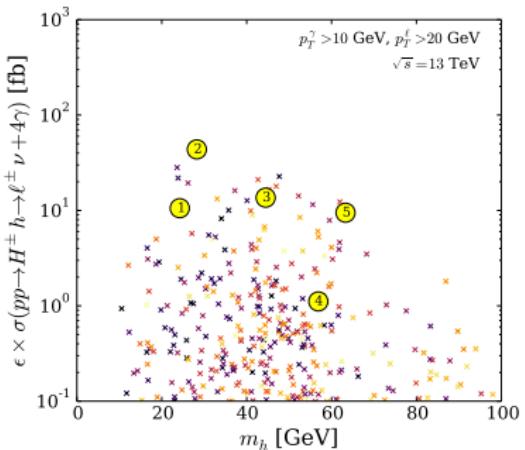
$p_T^\gamma > 10$ GeV, $p_T^\ell > 20$ GeV

$m_{H^+} \setminus m_h$	20	30	40	50	60	70	80	90	100
80	0.04	0.08	0.10	0.08	0.05	<0.01	/	/	/
90	0.05	0.10	0.13	0.13	0.10	0.06	<0.01	/	/
100	0.05	0.14	0.16	0.16	0.13	0.11	0.06	<0.01	/
110	0.06	0.13	0.18	0.19	0.17	0.16	0.13	0.07	<0.01
120	0.07	0.14	0.20	0.22	0.24	0.22	0.17	0.13	0.06
130	0.10	0.16	0.23	0.25	0.28	0.25	0.24	0.20	0.15
140	0.10	0.18	0.23	0.27	0.28	0.31	0.28	0.27	0.21
150	0.11	0.19	0.26	0.31	0.31	0.33	0.32	0.29	0.27
160	0.12	0.21	0.26	0.29	0.34	0.34	0.34	0.30	0.32

$\sigma(q\bar{q}' \rightarrow H^\pm h \rightarrow l\nu + 4\gamma)$ with cuts



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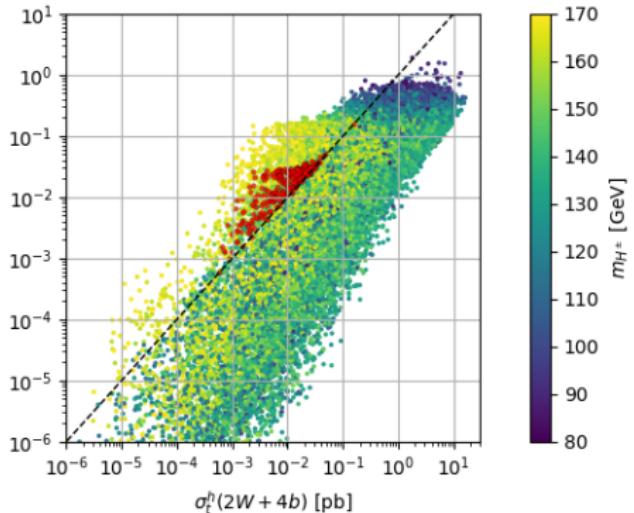
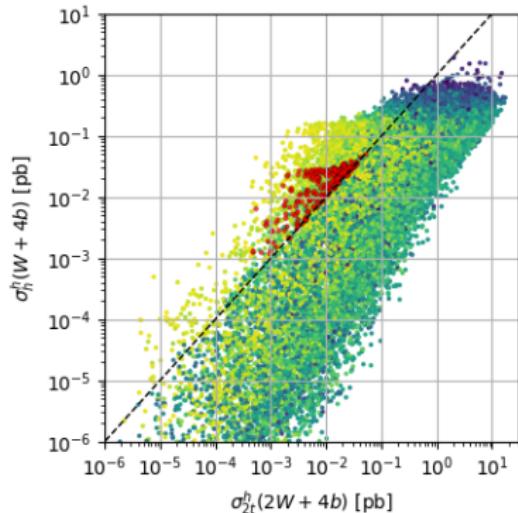
A full Monte Carlo (MC) analysis at the detector level shows that $W4\gamma$ signal is very promising, at the LHC with 300 fb^{-1} luminosity.

fermionic decays of h^0 and A^0

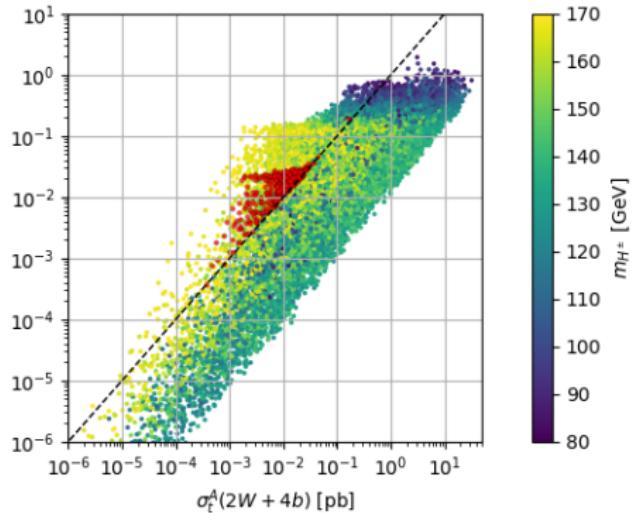
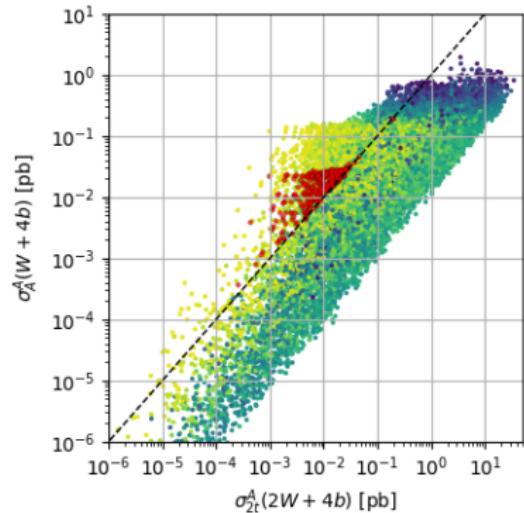
	production and decay chain
$\sigma_{2t}^{h_i}(2W2b2f)$	$2 \sigma_{t\bar{t}} \times \text{BR}(t \rightarrow bH^+) \times \text{BR}(\bar{t} \rightarrow \bar{b}W) \times \text{BR}(H^\pm \rightarrow Wh_i) \times \text{BR}(h_i \rightarrow f\bar{f})$
$\sigma_t^{h_i}(2W2b2f)$	$\sigma(pp \rightarrow t\bar{b}H^-) \times \text{BR}(t \rightarrow bW) \times \text{BR}(H^\pm \rightarrow Wh_i) \times \text{BR}(h_i \rightarrow f\bar{f})$

	Di-Higgs production and decay chain
$\sigma_{h_j}^{h_i}(2W2f2f')$	$\sigma(H^+H^-) \times \text{BR}(H^\pm \rightarrow W^\pm h_i) \times \text{BR}(H^\pm \rightarrow W^\pm h_j) \times (\text{BR}(h_i \rightarrow f\bar{f}) \times \text{BR}(h_j \rightarrow f'\bar{f}') + h_i \longleftrightarrow h_j) \frac{1}{1+\delta_{ff'}}$
$\sigma_{h_j}^{h_i}(W2f2f')$	$\frac{1}{1+\delta_{ff'}} \sigma(H^\pm h_i) \times \text{BR}(H^\pm \rightarrow W^\pm h_j) \times (\text{BR}(h_i \rightarrow f\bar{f}) \times \text{BR}(h_j \rightarrow f'\bar{f}') + h_i \longleftrightarrow h_j)$

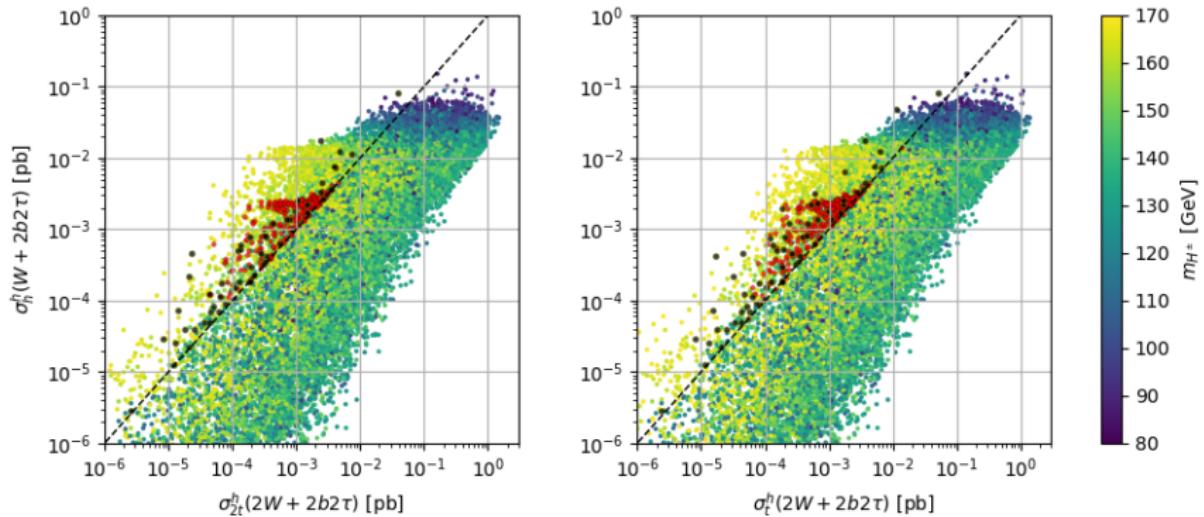
Table: $i, j = 1, 2$ and have $h_1 = h$ and $h_2 = A$; $f(f') = b$ or τ .



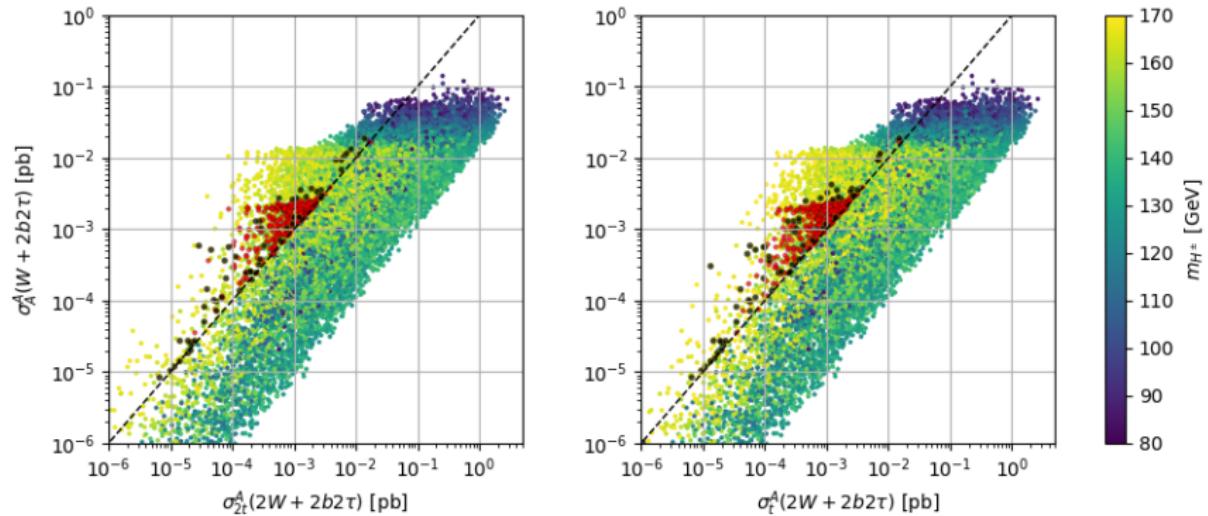
$\sigma(pp \rightarrow H^\pm h) \times \text{BR}(H^\pm \rightarrow W^\pm h) \times \text{BR}(h \rightarrow b\bar{b})^2$ compared to 2 σ_{2t} (left) and σ_t^h (right). Red points identify:
 $\sigma(H^+ H^-) \times \text{BR}(H^\pm \rightarrow W^\pm h)^2 \times \text{BR}(h \rightarrow b\bar{b})^2$ in 2HDM-I.



$\sigma(pp \rightarrow H^\pm A) \times \text{BR}(H^\pm \rightarrow W^\pm A) \times \text{BR}(A \rightarrow b\bar{b})^2$ compared to σ_{2t}^A (left) and σ_t^A (right). Red points identify:
 $\sigma(H^+ H^-) \times \text{BR}(H^\pm \rightarrow W^\pm A)^2 \times \text{BR}(A \rightarrow b\bar{b})^2$ in 2HDM-I.



$2\sigma(pp \rightarrow H^\pm h) \times \text{BR}(H^\pm \rightarrow Wh) \times \text{BR}(h \rightarrow b\bar{b}) \times \text{BR}(h \rightarrow \tau^+\tau^-)$
 compared to σ_{2t}^h (left) and σ_t^h (right). The red points identify
 $\sigma(H^+H^-)\times\text{BR}(H^\pm \rightarrow Wh)^2\times\text{BR}(h \rightarrow b\bar{b})\times\text{BR}(h \rightarrow \tau^+\tau^-)$ for
 2HDM-I while the black points are for 2HDM-X rates:
 $\sigma(pp \rightarrow H^\pm h) \times \text{BR}(H^\pm \rightarrow W^\pm h) \times \text{BR}(h \rightarrow \tau^+\tau^-)^2$.



$2\sigma(pp \rightarrow H^\pm A) \times \text{BR}(H^\pm \rightarrow WA) \times \text{BR}(A \rightarrow b\bar{b}) \times \text{BR}(A \rightarrow \tau^+\tau^-)$
 compared to σ_{2t}^A (left) and σ_t^A (right). The red points identify
 $\sigma(H^+H^-) \times \text{BR}(H^\pm \rightarrow WA)^2 \times \text{BR}(A \rightarrow b\bar{b}) \times \text{BR}(A \rightarrow \tau^+\tau^-)$ for
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 $\sigma(pp \rightarrow H^\pm A) \times \text{BR}(H^\pm \rightarrow W^\pm A) \times \text{BR}(A \rightarrow \tau^+\tau^-)^2$.

CP violation in H^\pm production and decays

We investigate the following CP violating H^\pm rate asymmetries:

- **Decay rate asymmetries** $A_{D,f}^{CP}$, defined by:

$$A_{D,f}^{CP} (H^\pm \rightarrow f) = \frac{\Gamma(H^+ \rightarrow f) - \Gamma(H^- \rightarrow \bar{f})}{2\Gamma_{\text{tree}}(H^+ \rightarrow f)}, \quad (1)$$

where $f = t\bar{b}; W^\pm H_i^0$ with $i = 1, 2$.

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- **Production rate asymmetry** A_P^{CP} :

$$A_P^{CP} = \frac{\sigma(pp \rightarrow H^+\bar{t}) - \sigma(pp \rightarrow H^-\bar{t})}{2\sigma^{\text{tree}}(pp \rightarrow H^+\bar{t})}, \quad (2)$$

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- **Production rate asymmetry** A_P^{CP} :

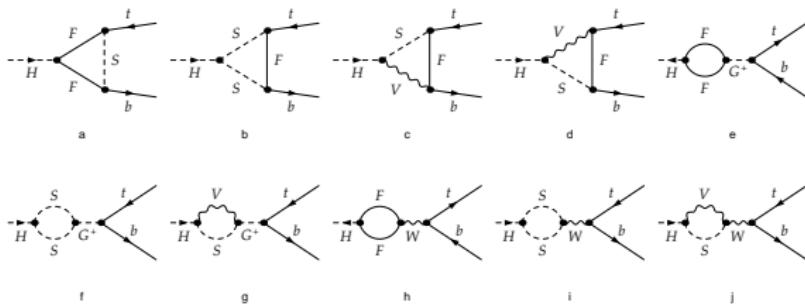
$$A_P^{CP} = \frac{\sigma(pp \rightarrow H^+ \bar{t}) - \sigma(pp \rightarrow H^- t)}{2\sigma^{\text{tree}}(pp \rightarrow H^+ \bar{t})}, \quad (2)$$

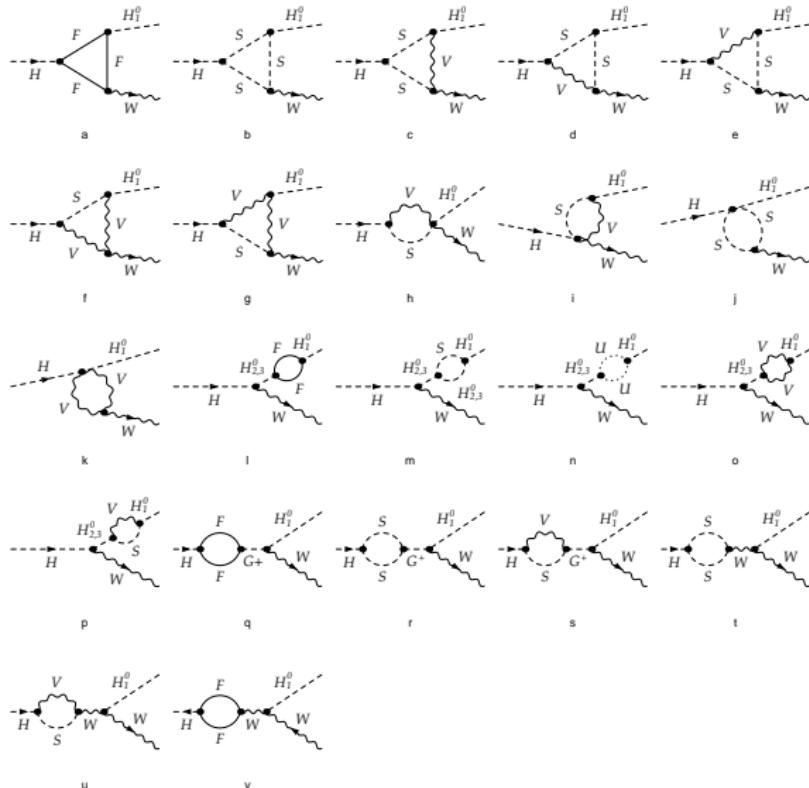
- **Combined Asymmetries** A_f^{CP} for H^\pm production and subsequent decays (using NWA):

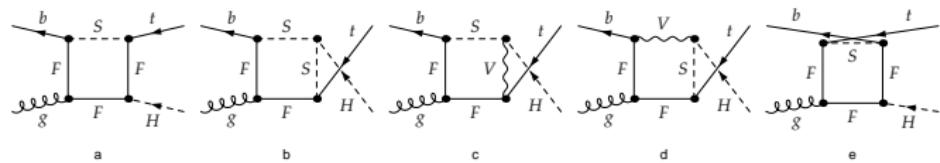
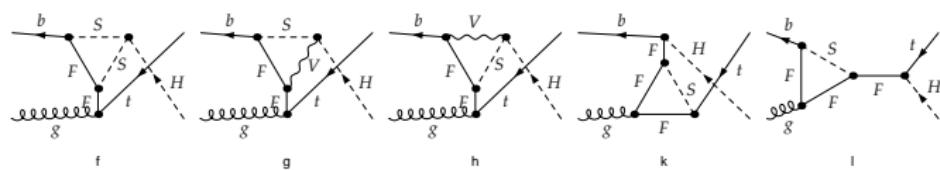
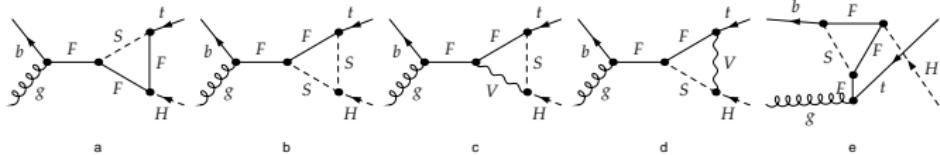
$$A_f^{CP} = \frac{\sigma(pp \rightarrow \bar{t}H^+ \rightarrow \bar{t}f) - \sigma(pp \rightarrow tH^- \rightarrow t\bar{f})}{2\sigma^{\text{tree}}(pp \rightarrow \bar{t}H^+ \rightarrow \bar{t}f)} = A_P^{CP} + A_{D,f}^{CP}$$

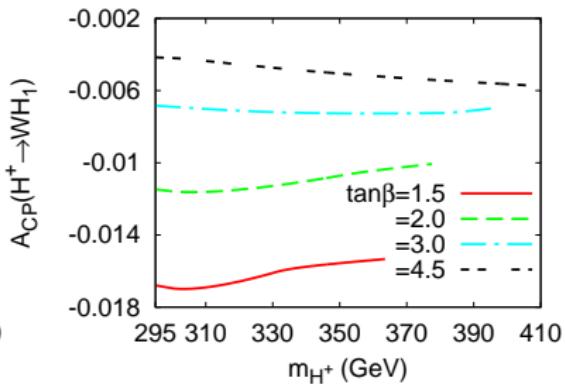
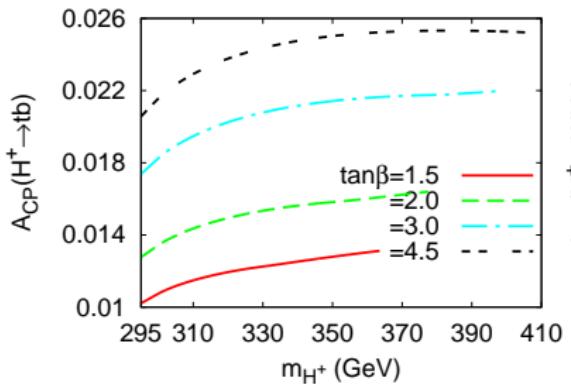
- In order to get CPV, we need both **non-zero CPV phases** in the Lagrangian and **CP conserving phases (strong phases)** in the absorptive parts of the one-loop amplitudes.
- In the C2HDM, the CP violating phases arise from:
 $h_i^0 ff$ couplings or $H^\pm W^\mp h_i^0$ couplings or $H^\pm G^\mp h_i^0$ couplings
- The strong phases: $t \rightarrow bW$, $H^\pm \rightarrow W^\pm h_i$; $h_i \rightarrow bb$ cuts

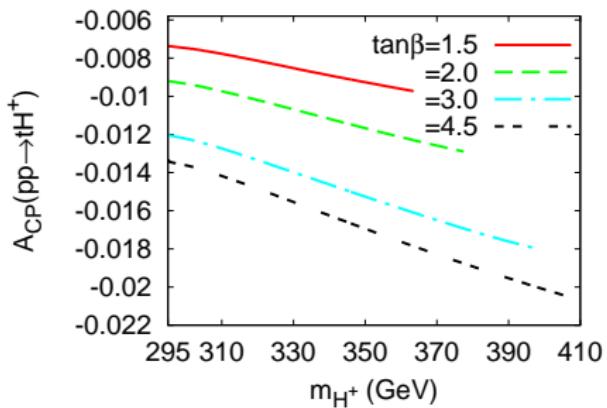
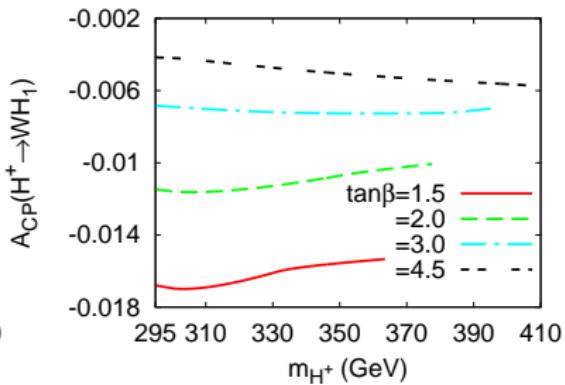
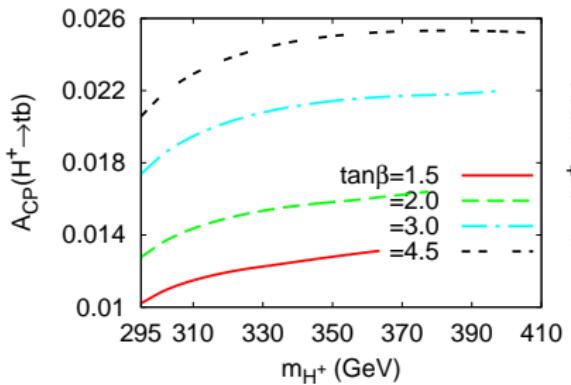
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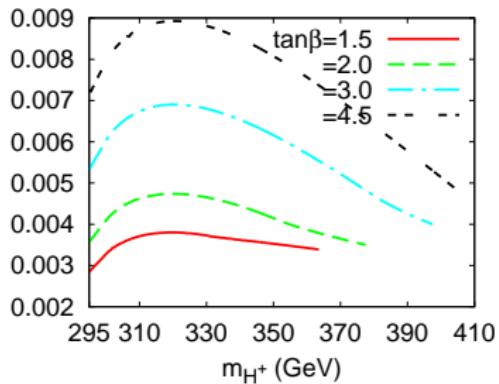
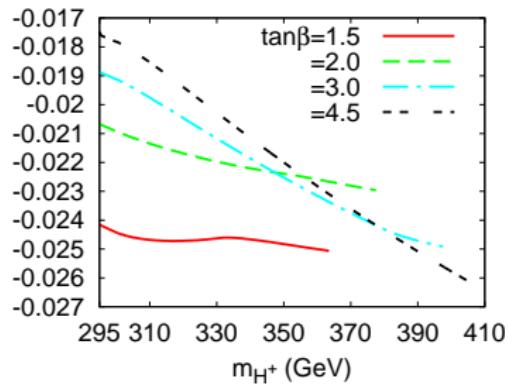










$A_{CP}(pp \rightarrow tt\bar{b})$  $A_{CP}(pp \rightarrow tWH_1)$ 

Conclusions

- In 2HDM-I there is regions of the parameter space compliant with all constraints yielding substantial BRs for $H^\pm \rightarrow W^{\pm*} h / W^{\pm*} A$ in which the $m_{H^\pm} < m_t - m_b$.
- $\sigma(pp \rightarrow t\bar{t} \rightarrow tbH^+ \rightarrow tbWA^0)$ and/or $pp \rightarrow H^\pm h / H^\pm A / H^\pm H^\mp$ could be sizeable
- light H^\pm in the 80–160 GeV mass range, still being consistent with all LHC, LEP Tevatron and B -physics data.

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- light H^\pm in the 80–160 GeV mass range, still being consistent with all LHC, LEP Tevatron and B -physics data.
- $pp \rightarrow H^\pm h^0 \rightarrow W^\pm + 4\gamma$ with significant events.
- After reasonable cuts on the p_T of the photons and the lepton, $\sigma_{W^\pm 4\gamma}$ can still enjoy a cross section of the order 10 fb and more in an essentially background-free environment.