(Lepton Flavor) Portal Matter

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Based in part on work in collaboration with George Wojcik, Shu Tian Eu, and Ricardo Ximenes 2211.09918 [PLB 841 (2023) 137931], 2303.12983



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Introduction/Motivation

Dark matter: gravitationally confirmed by a range of astrophysical observations, but wide range of possibilities for its properties (mass and couplings) Landscape of DM candidates has exploded in the past decade+



Image credit: APPEC Rept. (2020)

many reviews: see e.g. Battaglieri et al. '17, Gori et. al, Snowmass 2021 report

Here, interested in a particular category of theories:

"dark sector" paradigm with light DM, light mediator



Many possible "portals" for interaction with SM (Higgs, gauge, neutrino,...)

vast literature: see e.g. Pospelov et al. '08, Davoudiasl et al. '12, Curtin et al. '14, ...

Focus here on a certain sub-category:

Vector portal/kinetic mixing models

Dark gauge group: $U(1)_D \leq \mathcal{G}_D$ Dark matter field χ charged under $U(1)_D$ (SM uncharged) Kinetic mixing portal: $\frac{\epsilon}{2c_w} B_{\mu\nu} A_D^{\mu\nu}$ \longrightarrow dark photon coupling to SM proportional to $\epsilon J_{\rm EM}^{\mu}$

correct DM relic abundance for $m_{\chi}, m_{A_D} \sim 0.1 - 1$ GeV, $\epsilon \sim 10^{-(3-5)}$

Model-building framework: origin of KM parameter ϵ



heavy particles charged under SM hypercharge and $U(1)_D$

$$\epsilon = c_W \frac{g_D g_Y}{12\pi^2} \sum_i Q_{Y_i} Q_{D_i} \log\left(\frac{m_i^2}{\mu^2}\right)$$

finite and calculable
$$\epsilon \longrightarrow \sum_{i} Q_{Y_i} Q_{D_i} = 0$$

Holdom 1986,...

Portal Matter Theory/Phenomenology

Consider fermionic PM that in principle is reachable in current/near-future expts



PM vectorlike wrt SM and $U(1)_D$

(anomaly constraints, direct searches, precision EW, Higgs constraints,...)



PM mixes with SM – same SM quantum numbers as some SM field

Distinctive collider signatures!

decays to (highly boosted) SM fermion/jet +dark photon or dark Higgs

compare usual vectorlike fermion case – preferential decays to SM EW gauge, Higgs bosons



Portal Matter Models (I)

Minimal scenarios:

dark gauge group $\mathcal{G}_D = U(1)_D$ one dark Higgs h_D , single PM vectorlike pair "VLL" E^{\pm}, L^{\pm} "VLQ" $T^{\pm}, B^{\pm}, Q^{\pm}$ Example: "maverick top partners" $\frac{\Gamma(T \to t + h_2/\gamma_d)}{\Gamma(T \to t/b + W/Z/h_1)} \sim \left(\frac{M_T}{M_t}\right)^2 \left(\frac{v_{EW}}{v_d}\right)^2 \frac{1}{\left(1 + (M_T/M_t)^2 \sin^2 \theta_I^t\right)^2}$

production QCD strength, may be accessible at LHC dark photon decay length depends on KM ϵ

Rizzo 1810.07531 Kim et al. 1904.05893 Carvunis et al. 2209.14305,... Rizzo 2202.02222 (Snowmass report)



Portal Matter Models (II)

Non-minimal scenarios:

Extended dark gauge groups: $\mathcal{G}_D \longrightarrow U(1)_D$

Extended fermion PM and scalar content:

nontrivial fermion sets for anomaly cancellation multiple vacuum expectation value scales

Many BSM options

...

Grand unification (-inspired) Extra dimensions/Kaluza-Klein PM Rizzo, Reuter 1909.09160 Rizzo, Wojcik 2012.05406 Rizzo 2209.00688,... Wojcik 2205.11545

More generally: KM/PM as model-building framework for BSM physics

Example: E_6 inspired dark sector Rizzo, Reuter 1909.09160 $E_6 \longrightarrow SU(6) \times SU(2)_I \rightarrow SU(5) \times SU(2)_I \times U(1)_6$ $27 \rightarrow (\overline{5}, 2) + (5, 1) + (1, 2) + (10, 1) \quad (SU(5), SU(2)_I)$ SM fermion content + vectorlike pair $(5, \overline{5})$ + singlets important point: SM neutral wrt $U(1)_D$ can't arise from E₆ subgroup! E_6 inspired dark group $\mathcal{G}_D = SU(2)_I \times U(1)_{I_Y} \longrightarrow U(1)_D$ Example: "flavorful" PM in Pati-Salam Rizzo, Wojcik 2012.05406

 $\begin{array}{lll} \text{SM embedded in PS:} & \text{dark gauge group:} & SU(4)_F \times U(1)_F \\ \cdot & \cdot \\ SU(4)_c \times SU(2)_L \times SU(2)_R. \end{array} \\ & \text{PM as vectorlike 4^{th} generation, singlets with respect to} & SU(3)_F \end{array}$

Example: Kaluza-Klein PM

Wojcik 2205.11545

SM and PM fermions propagate in bulk, together in 5D gauge multiplets concrete 5D orbifold model with dark gauge group SU(2)

Rich phenomenology, differs from "standard" case with VLL, VLQ minimal cases – dark gauge charges lead to distinctive collider signatures non-minimal – also have nontrivial new gauge bosons, scalars, KK towers, etc...

Focus here on lepton sector

lepton flavor portal matter

minimal workable PM scenario that can accommodate $\Delta a_{\mu} = (g_{\mu} - 2)/2$

See talk here by George Wojcik

(effect insensitive to DM details)

non-minimal extension with $\mathcal{G}_D = SU(2)_A \times SU(2)_B$

rich phenomenology, interesting framework for lepton flavor model-building

Dark photon models and muon *g*-2

 $\Delta a_{\mu} = a_{\mu}^{\exp} - a_{\mu}^{SM} = (251 \pm 59) \times 10^{-11}$

IF discrepancy is due to new physics

Abi et al. (Muon g-2), PRL 126, 141801 (2021) Aoyama et al., Phys. Rept. 887, 1 (2020),...

can KM/PM framework provide a possible resolution?

(i) dark photon, no PM mixed with muon – too small (vector coupling, small KM) $~\sim \epsilon^2$

Davoudiasl et al. 1402.3620,...

Rizzo 1810.07531,...

(ii) mix muon with single lepton PM pair – still too small!

Field $SU(2)_L \times U(1)_Y$ Q_D $l_L = (v_L^{\mu}, \mu_L)^T$ $\begin{pmatrix} 2, -\frac{1}{2} \end{pmatrix}$ 0 μ_R (1, -1)0 $E_{L,R}^{\pm}$ (1, -1) ± 1 $S = v_S + h_D/\sqrt{2}$ (1, 0)+1



A minimal workable framework

See talk here by George Wojcik

Wojcik, LE, Eu, Ximenes 2211.09918

Must couple new physics to **both** chiralities of the muon:

Field	$SU(2)_L \times U(1)_Y$	Q_D
$\boldsymbol{l}_{L}=\left(\boldsymbol{\nu}_{L}^{\mu},\boldsymbol{\mu}_{L}\right)^{T}$	$\left(2,-\frac{1}{2}\right)$	0
μ_R	(1 , −1)	0
$\boldsymbol{L}_{\boldsymbol{L},\boldsymbol{R}}^{\pm} = \left(N_{L,R}^{\pm}, L_{L,R}^{\pm}\right)^{T}$	$\left(2,-\frac{1}{2}\right)$	±1
$E_{L,R}^{\pm}$	(1 , −1)	±1
$S = v_S + h_D / \sqrt{2}$	(1,0)	+1

$$\begin{aligned} \mathcal{L}_{Y} \supset -y_{\mu} \overline{l}_{L} H \mu_{R} - y_{L}^{+} \overline{l}_{L} S^{\dagger} L_{R}^{+} - y_{L}^{-} \overline{l}_{L} S L_{R}^{-} - y_{E}^{+} \overline{E}_{L}^{+} S \mu_{R} - y_{E}^{-} \overline{E}_{L}^{-} S^{\dagger} \mu_{R} \\ &- y_{LE}^{+} \overline{L}_{L}^{+} H E_{R}^{+} - y_{EL}^{+} \overline{E}_{L}^{+} H^{\dagger} L_{R}^{+} - y_{LE}^{-} \overline{L}_{L}^{-} H E_{R}^{-} - y_{EL}^{-} \overline{E}_{L}^{-} H^{\dagger} L_{R}^{-} \\ &- M_{L}^{+} \overline{L}_{L}^{+} L_{R}^{+} - M_{E}^{+} \overline{E}_{L}^{+} E_{R}^{+} - M_{L}^{-} \overline{L}_{L}^{-} L_{R}^{-} - M_{E}^{-} \overline{E}_{L}^{-} E_{R}^{-} + h.c., \end{aligned}$$



Chirally-enhanced (dominant) contribution:

$$\Delta a_{\mu} \approx -\Delta a_{\mu}^{(\text{obs})} \left(\frac{y_{LE}^{+}/y_{\mu}}{36}\right) \left(\frac{1 \text{ TeV}}{M_{L}^{+}/y_{L}^{+}}\right) \left(\frac{1 \text{ TeV}}{M_{E}^{+}/y_{E}^{+}}\right)$$



Similar mechanism as Carcamo Hernandez et al. 1910.10734, but very different constraints

Lepton Flavor Portal Matter

Extension to non-Abelian dark gauge group

finite and calculable kinetic mixing parameter ϵ

origin of $U(1)_D$ charge quantization

origin of PM field content and mixing with muon

 $|y_{LE}^{\pm}|v \sim O(\text{few GeV}) \implies \text{perhaps suggestive of } y_{LE}^{\pm} \sim y_{\tau}$

distinguish lepton generations via their couplings to PM/dark sector fields

Lepton Flavor Portal Matter – extended model

Dark gauge group:

Wojcik, LE, Eu, Ximenes 2303.12983

 $\begin{aligned} \mathcal{G}_D &= SU(2)_A \times SU(2)_B \\ SU(2)_A \times SU(2)_B \times Z_2 &\longrightarrow U(1)_D \times Z_2 \longrightarrow Z'_2 \\ \text{(global)} & \langle \Phi \rangle \sim \text{TeV} & \langle \Delta_A, \Delta_B \rangle \sim \text{GeV} \end{aligned}$

Scalar Fields	$SU(2)_L \times U(1)_Y$	$SU(2)_A$	$SU(2)_B$	Z_2
Φ	(1,0)	2	2	+1
Δ_A	(1,0)	3	1	-1
Δ_B	(1,0)	1	3	-1
Н	(2 , 1/2)	1	1	+1

Fermion field content

Fermion Fields	$SU(2)_L \times U(1)_Y$	$SU(2)_A$	$SU(2)_B$	Z ₂
L_L , e_R	(2 , −1/2), (1 , −1)	1	1	+1
Ψ_L , Ψ_R	(2 , −1/2), (1 , −1)	2	2	+1
V_L , V_R	(1 , −1), (2 , −1/2)	1	3	+1
S_L, S_R	(2 ,−1/2), (1 ,−1)	1	1	-1

 $SU(2)_A \times SU(2)_B \times Z_2$ singlets:

1 SM lepton family(identified with electron)

 $SU(2)_A \times SU(2)_B \times Z_2$ charged:

- 2 SM lepton families(identified with muon, tau)
- $\implies \text{ portal matter, VLL} \\ (U(1)_D \text{ charged}) \quad (U(1)_D \text{ neutral})$

Gauge Symmetry Breaking and Scalar Sector

**ignoring Higgs portal interactions - must be highly suppressed (generic in these constructions)

Boson masses: $e_D = g_A \cos \theta_D = g_B \sin \theta_D$ $r_\Delta = v_\Delta/v_\Phi$ $M_{Z_D} \sim e_D v_\Phi \sim \text{TeV}$ $m_{A_D} \sim r_\Delta M_{Z_D}$ $r_\Delta \ll 1$

	Gauge Bosons	Mass	Z'_2	Q_D
	Z_D	$M_{Z_D} \sim { m TeV}$	+1	0
	W_l^{\pm}	$M_{W_l} \sim { m TeV}$	-1	<u>±1</u>
	W_h^{\pm}	$M_{W_h} \sim { m TeV}$	-1	±1
dark photon 🛛 🗕 🛶	A_D	$m_{A_D} \sim { m GeV}$	+1	*

 $m_{h_3} = r_\Delta r_3 M_{h^\pm}$

	Scalars	Mass	Z ' ₂	Q_D
	h_1, h_2, h_4	$M_{h1,h2,h4} \sim { m TeV}$	+1	0
	h^{\pm}	$M_h^{\pm} \sim \text{TeV}$	+1	± 1
	h_{5}, h_{6}	$M_{h5,h6} \sim { m TeV}$	-1	0
dark Higgs 🛛 🛶	h_3	$m_{h3} \sim { m GeV}$	+1	*

$$\mathcal{L}_{Y} = y_{H} \left[\operatorname{Tr}(\overline{\Psi_{L}} H \Psi_{R}) + \text{h.c.} \right] + y_{HV} \left[\operatorname{Tr}(\overline{V_{L}} H V_{R}) + \text{h.c.} \right] + y_{HS} \left[\operatorname{Tr}(\overline{S_{L}} H S_{R}) + \text{h.c.} \right] \\ + y_{P} \left[\operatorname{Tr}(\overline{\Psi_{L}} \Phi V_{R}) + \text{h.c.} \right] + \tilde{y}_{P} \left[\operatorname{Tr}(\overline{\Psi_{L}} \Phi V_{R}) + \text{h.c.} \right] + y_{P'} \left[\operatorname{Tr}(\overline{V_{L}} \Phi^{\dagger} \Psi_{R}) + \text{h.c.} \right] \\ + \tilde{y}_{P}' \left[\operatorname{Tr}\left(\overline{V_{L}} \tilde{\Phi}^{\dagger} \Psi_{R}\right) + \text{h.c.} \right] + y_{SE} \left[\operatorname{Tr}(\overline{V_{L}} S_{R} \Delta_{B}) + \text{h.c.} \right] + y_{SL} \left[\operatorname{Tr}(\overline{S_{L}} V_{R} \Delta_{B}) + \text{h.c.} \right]$$

$$y_P = y_L \cos \theta_L \quad \tilde{y}_P = y_L \sin \theta_L \qquad M_L^+ = v_\Phi y_L \cos(\theta_L - \theta_\Phi)$$
$$y'_P = y_E \cos \theta_E \qquad \tilde{y}'_P = y_E \sin \theta_E \qquad M_E^+ = v_\Phi y_E \cos(\theta_E - \theta_\Phi)$$

 $M_L^- = v_\Phi y_L \sin(\theta_L + \theta_\Phi)$

 $M_E^- = v_\Phi y_E |\sin(\theta_E + \theta_\Phi)|$

basis choice: (all couplings assumed to be real) $y_{L,E,SL,SE,HS} > 0$ $c_{\theta_L - \theta_{\Phi}}, c_{\theta_E - \theta_{\Phi}}, s_{\theta_L + \theta_{\Phi}} > 0$

 $y_H, y_{HV}, s_{\theta_E} + \theta_{\Phi}$ may be positive or negative

Fermion masses:

(second and third SM generations + heavy states)

Fields	$SU(2)_L \times U(1)_Y$	$SU(2)_A$	$SU(2)_B$	Z_2
Ψ_L , Ψ_R	(2 , −1/2), (1 , −1)	2	2	+1
V_L , V_R	(1 , −1), (2 , −1/2)	1	3	+1
S_L, S_R	(2 , −1/2), (1 , −1)	1	1	-1

$$Z'_{2} = +1 \longrightarrow \\ \left(\Psi_{(L,R)_{11}}, \Psi_{(L,R)_{22}}, V^{0}_{(L,R)}\right)$$
$$Z'_{2} = -1 \longrightarrow \\ \left(S_{(L,R)}, \Psi^{+}_{(L,R)}, V^{+}_{(L,R)}, \Psi^{-}_{(L,R)}, V^{-}_{(L,R)}\right)$$

$$M_{F}^{(1)} = \begin{pmatrix} \frac{y_{H}v}{\sqrt{2}} & 0 & M_{L}^{+} \\ 0 & \frac{y_{H}v}{\sqrt{2}} & -M_{L}^{-} \\ M_{E}^{+} & \mp M_{E}^{-} & \frac{y_{H}vv}{\sqrt{2}} \end{pmatrix} \qquad M_{F}^{(2)} = \begin{pmatrix} \frac{y_{H}sv}{\sqrt{2}} & 0 & y_{SL}^{\Delta}r_{\Delta}v_{\Phi} & 0 & y_{SL}^{\Delta}r_{\Delta}v_{\Phi} \\ 0 & \frac{y_{H}v}{\sqrt{2}} & M_{L}^{+} & 0 & 0 \\ y_{SE}^{\Delta}r_{\Delta}v_{\Phi} & M_{E}^{+} & \frac{y_{H}vv}{\sqrt{2}} & 0 & 0 \\ 0 & 0 & 0 & \frac{y_{H}v}{\sqrt{2}} & M_{L}^{-} \\ y_{SE}^{\Delta}r_{\Delta}v_{\Phi} & 0 & 0 & \pm M_{E}^{-} & \frac{y_{H}vv}{\sqrt{2}} \end{pmatrix}$$

 $v \sim 100 \text{ GeV}$ $M_{L,E}^{\pm} \sim v_{\Phi} \sim \text{TeV}$

basis choice: $y_H, y_{HV}, s_{\theta_E + \theta_{\Phi}}$ may be positive or negative (all couplings assumed to be real)



dark sector gauge bosons, VLL)

Three relevant chirality-flipping mass terms: $m_a \approx \frac{y_{HS}v}{\sqrt{2}}$ $m_b \approx O(1) \left(\frac{y_Hv}{\sqrt{2}}\right)$ $m_{HV} = \frac{y_{HV}v}{\sqrt{2}}$ Muon *g*-2 Scenario A F^{\pm} h_3/h^{\mp} μ^{-} F^0 h_5/h_6 $e_b \rightarrow \tau$ F^{\pm} A_D $e_a \rightarrow \mu$ μ $\Delta a_{\mu} = \frac{y_{SL}y_{SE}}{16\pi^2} m_{\mu} (m_{\tau}a^{\tau} + m_{HV}a^{HV})$ $a^{\tau,HV} \sim O((M_{L,E}^{\pm})^{-2})$ Scenario B F^{\pm} W_{h}^{\pm}/W_{l}^{\pm} $e_b \rightarrow \mu$ F^0 F^0 F^0 $e_a \rightarrow \tau$ Z_D $\Delta a_{\mu} = \frac{e_D^2}{16\pi^2} m_{\mu} m_{HV} a^{HV}$

Scenario A





 $m_{HV} \gg m_{\tau}$

Scenario B

 $\sin\left(\theta_E + \theta_\Phi\right) > 0$

(constructive interference)

 $\sin\left(\theta_E + \theta_\Phi\right) < 0$ (destructive interference)



 $(M_L^-, M_E^+, M_E^-) = (1.3, 1.5, 1.8) M_L^+ \quad (M_{h_1}, M_{h_2}, M_{h_4}) = (1.2, 1.4, 1) \text{ TeV} \quad M_{Z_D} = 0.7 \text{ TeV}$

Collider Phenomenology

Portal matter direct production \implies similar rates for scenarios A and B lightest heavy fermion state predicted to be PM $M_{L,E}^{\pm} \leq M_{L,E}^0 \leq M_{L,E}^{\pm}$

Scenario A

$$L^{\pm}, E^{\pm} \rightarrow \mu + A_D, h_D \longrightarrow M_E^{\pm} \ge 895 \text{ GeV}, M_L^{\pm} \ge 1050 \text{ GeV}$$

unless new decays via heavy scalars, gauge bosons

$$L^{\pm} \to \mu + W_{l,h}^{\pm}$$

Scenario B

PM decays to taus – weaker limits



VLL direct production ($U(1)_D$ neutral heavy fermions)

Scenario AScenario B
$$\Gamma(E^0 \to \tau, \mu + h, Z, W) \sim M_E^0 \times O\left(\frac{m_{\tau,\mu}^2}{v^2}\right)$$
 $\Gamma(E^0 \to L^0 + h, Z, W) \sim M_E^0 \times O\left(\frac{m_{\tau,\mu}^2}{v^2}, \frac{m_{HV}^2}{v^2}\right)$

 standard VLL bounds may be weakened if heavy gauge bosons and scalars are kinematically accessible for 2-body decays

if so, distinctive signature: **2** EW gauge bosons emitted instead of 1



can constrain m_{HV} via decays of heavy VLL to lighter VLL

Monophoton search (muon collider)



Diboson production

Scenario A

At muon collider, pair production of

 h_5h_5, h_6h_6, h_5h_6 $h^+h^-, h^\pm A_D, h^\pm h_D$

Scenario B

$h_{1,2}h_{1,2} \quad h_4h_4 \ Z_DZ_D \ Z_Dh_{1,2} \ W_{h,l}^{\pm}W_{h,l}^{\mp}$



Precision constraints

vectorlike new fermions — mild precision constraints kinetic mixing $\epsilon_{Z-A_D} = \frac{e_D e}{6\pi^2} \frac{s_w}{c_w} \log\left(\frac{M_L^+ M_E^+}{M_L^- M_E^-}\right)$ $\epsilon_{Z-Z_D} = \frac{e_D e}{12\pi^2 \sin(2\theta_D)} \frac{s_w}{c_w} \left[\frac{M_L^{+2} - M_L^{-2}}{M_L^{+2} + M_L^{-2}} \left(\frac{5}{6} + \log \frac{M_L^0}{m_Z} \right) + (1 - 2\cos(2\theta_D)) \log \frac{M_L^+}{M_L^-} + (L \to E) \right]$ $\longrightarrow M_{Z_D} - m_Z \gtrsim 10 \text{ GeV}$ Z_D couples at leading order to taus or muons Scenario A Scenario B

expect stronger constraints in Scenario B



Lepton flavor

(partial) lepton flavor symmetry (no theory yet of small Yukawa couplings)SM charged lepton generations distinguished by dark gauge group couplings

preserved Z'_2 isolates muon and tau lepton flavors

FCNC mediation via $W_{h,l}$ $h_{5,6}$ (suppressed) charged LFV constraints easily satisfied

Extend to include neutrino masses, lepton mixing -

requires violation of the preserved Z'_2

work in progress

Summary and conclusions

Portal matter – useful model-building framework for physics beyond the SM

rich phenomenology even in minimal implementations

can accommodate muon g-2 (portal matter effect – largely agnostic to DM sector) especially well-suited for muon collider probes

extended models provide intriguing setting for lepton flavor model-building



Muon g-2 for minimal PM scenarios

both vector and axial vector couplings of muon to dark photon...

$$-e\epsilon\bar{\mu}\gamma_{\mu}(1-y-y\gamma_{5})\mu A_{D}^{\mu} \qquad y\sim \left(\frac{g_{D}}{e\epsilon}\right)\left(\frac{(y_{E}^{+})^{2}v_{s}^{2}}{(M_{E}^{+})^{2}}-\frac{(y_{E}^{-})^{2}v_{s}^{2}}{(M_{E}^{-})^{2}}\right)$$
$$\Delta a_{\mu}^{(A_{D}^{(1)})}\sim 10^{-11}\left(\frac{\epsilon}{10^{-4}}\right)^{2}R(y,m_{A_{D}}) \qquad |y|\sim 0.01-0.5$$

+ scalar and gauge boson contributions with PM on internal line...

$$\Delta a_{\mu}^{(h_D)} \sim 10^{-10} \sum_{i=E^+,E^-} \left(\frac{200 \text{ GeV}}{m_i}\right)^2$$
$$\Delta a_{\mu}^{(A_D^{(2)})} \sim -(2 \times 10^{-4}) \left(\frac{g_D}{0.1}\right)^2 \left(\frac{100 MeV}{m_{A_D}}\right)^2 \sum_{i=E^+,E^-} \frac{y_i^2 v_s^2}{m_i^2}$$





still too small to accommodate the muon *g*-2 anomaly

Rizzo 1810.07531

Constraining the minimal model:

At LHC: PM decays – repurpose slepton searches $M_E^{\pm} \ge 895 \text{ GeV}, M_L^{\pm} \ge 1050 \text{ GeV}$ $y_E^{\pm}, y_L^{\pm}, y_{LE}^{\pm}$: perturbative unitarity

can do better at a (multi-TeV) muon collider: probe PM masses up to $\sqrt{s/2}$

 y_E^{\pm}, y_L^{\pm} constrained by monophoton searches

 y_{LE}^{\pm} more challenging – only enters in PM decays to other PM



Minimizing the potential:

$$\Phi = \frac{1}{2} \left(\operatorname{Re} \Phi_0 + i \operatorname{Im} \Phi_0 \right) + \sum_{a=x,y,z} \tau_a \left(\operatorname{Re} \Phi_a + i \operatorname{Im} \Phi_a \right) \qquad \Delta_{A,B} = \sum_{a=x,y,z} \tau_a \Delta_{A,B}^a \qquad \tau_a \equiv \sigma_a/2,$$

 $SU(2)_A \times SU(2)_B$ rotations: set Φ vev diagonal and real

$$\langle \operatorname{Re} \Phi_0 \rangle = v_{\Phi} (\cos \theta_{\Phi} + \sin \theta_{\Phi}) \quad \langle \operatorname{Re} \Phi_z \rangle = v_{\Phi} (\cos \theta_{\Phi} - \sin \theta_{\Phi}) \qquad 0 \le \theta_{\Phi} \le \pi$$

preserved subgroup

$$\langle \Delta_A^x \rangle = r_\Delta v_\Phi s_{\theta\Delta} c_{\phi_A} s_{\theta_A} \quad \langle \Delta_A^y \rangle = r_\Delta v_\Phi s_{\theta\Delta} s_{\phi_A} s_{\theta_A} \quad \langle \Delta_A^z \rangle = r_\Delta v_\Phi s_{\theta\Delta} c_{\theta_A}$$
$$\langle \Delta_B^x \rangle = r_\Delta v_\Phi c_{\theta\Delta} c_{\phi_B} s_{\theta_B} \quad \langle \Delta_B^y \rangle = r_\Delta v_\Phi c_{\theta\Delta} s_{\phi_B} s_{\theta_B} \quad \langle \Delta_B^z \rangle = r_\Delta v_\Phi c_{\theta\Delta} c_{\theta_B}$$

 $0 \le \theta_{A,B} \le \pi$ $0 \le \phi_{A,B} \le 2\pi$

 $0 \le \theta_{\Delta} \le \pi/2$

 $\times D_B(\hat{z},\pi) \times Z_2$

triplets!!

3 inequivalent classes of vacua, all CP-preserving:

(i)
$$r_{\Delta} = 0$$

(ii) $r_{\Delta} \neq 0, 0 < \theta_{\Delta} < \pi/2, \theta_{A,B} = 0$
(iii) $r_{\Delta} \neq 0, 0 < \theta_{\Delta} < \pi/2, \theta_{A,B} = \pi/2$
 $\phi_A = \phi_B = 0.$ (simplicity)
 $U(1)_D \rightarrow D_A(\hat{z}, \phi) \times D_B(\hat{z}, \phi)$
 $U(1)_D \rightarrow D_A(\hat{z}, \phi) \times D_B(\hat{z}, \phi) \times Z_2$
need both triplets!!

Scalar masses:

eedom: 6 real scalars $h_1 = 1$ complex scalar i^+ of fr 8 degree

degrees of freedom: 6 real scalars
$$h_{1-6}$$
 1 complex scalar h^{\pm}
 $M_{h\pm}$ $M_{h_{1,2,4}} = r_{1,2,4}M_{h\pm}$ $M_{h_5} = \cos\theta_M M_{h\pm}$ $M_{h_6} = \sin\theta_M M_{h\pm}$ $r_{\Delta} \ll 1$
 $m_{h_3} = r_{\Delta}r_3 M_{h\pm}$ $|c_{2\theta_M}| > |c_{2\theta_{\Delta}}|$ $r_i \sim O(1)$
 $W_{l,h} \equiv h_3 \approx \cos\theta_{\Delta}(\Delta_B^x - r_{\Delta}v_{\Phi}\cos\theta_{\Delta}) + \sin\theta_{\Delta}(\Delta_A^x - r_{\Delta}v_{\Phi}\sin\theta_{\Delta})$

 $v_{\Delta} = \sqrt{v_{\Delta_A}^2 + v_{\Delta_B}^2}$

 $\tan\theta_{\Delta} = v_{\Delta_A}/v_{\Delta_B}$

Gauge boson masses:

$$e_D = g_A \cos \theta_D = g_B \sin \theta_D$$

$$Z_D = \cos \theta_D W_A^z + \sin \theta_D W_B^z \quad M_{Z_D} = \sqrt{2} v_{\Phi} e_D \csc(2\theta_D)$$

$$A_D = -\sin \theta_D W_A^z + \cos \theta_D W_B^z \quad m_{A_D} = \frac{1}{\sqrt{2}} r_{\Delta} \sin 2\theta_D M_{Z_D}$$

$$W_{l,h} \text{ admixtures of } W_{A,B}^{\pm} \qquad M_{W_l} = \sin \theta_{lh} M_{Z_D} \qquad M_{W_h} = \cos \theta_{lh} M_{Z_D}$$

$$\cos 2\theta_{lh} = \cos 2\theta_D \sqrt{1 + \sin^2 \theta_{\Phi} \tan^2 \theta_D}$$

Parameters of the extended model

 $(e_D, \lambda_1, M_{Z_D}, M_{h_{1,2,4}}, M_{h^{\pm}}, \theta_M, \theta_D, \theta_{\Delta}, \theta_{lh})$

 $(M_L^{\pm}, M_E^{\pm}, |y_{HV}|, |y_H|, |y_{SL}|, |y_{SE}|)$

 $\operatorname{sign}(y_{HV}, y_H, \sin(\theta_E + \theta_\Phi), \sin(2\theta_\Phi))$

Dark photon and dark Higgs masses (sub-GeV)

Other scalar quartics either expressible in terms of other parameters or only enter four-scalar interactions not of interest here