

Fuzzy dark matter constraints using a single VLBI observation of a gravitationally lensed radio jet

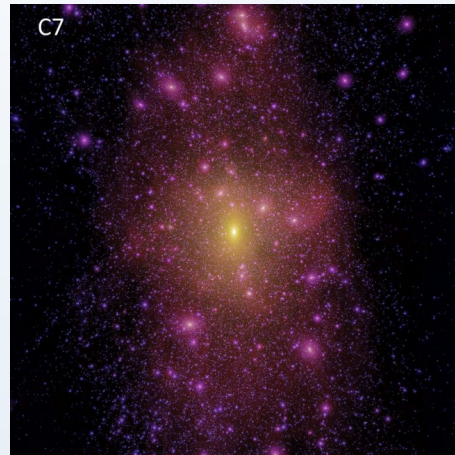
Devon M. Powell (Max Planck Institute for Astrophysics)

*with Simona Vegetti, John McKean, Simon White,
Elisa Ferreira, Simon May, Cristiana Spingola*

2302.10941 (this work, submitted to MNRAS Letters)
2207.03375 (smooth lens modeling, published in MNRAS)
2005.03609 (inference method, published in MNRAS)

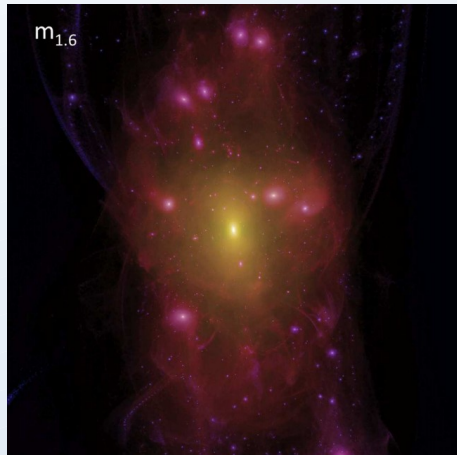
Background: Dark matter phenomenology

Cold DM



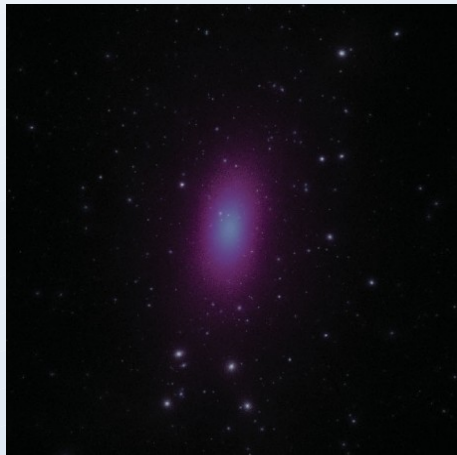
Lovell+2014

Warm DM



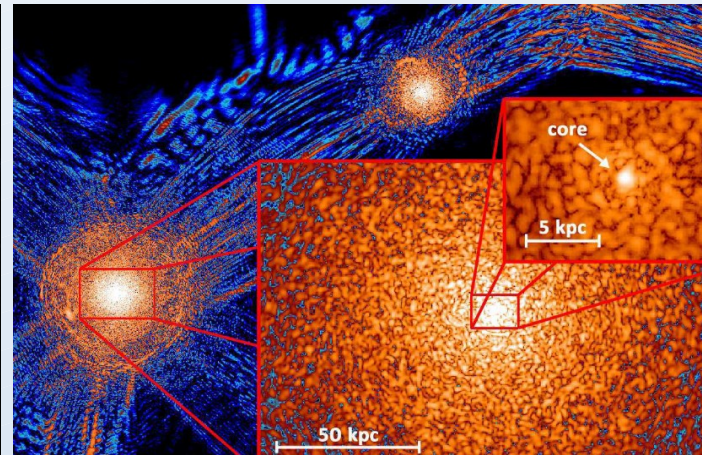
Lovell+2014

Self-interacting DM



Rocha+2013

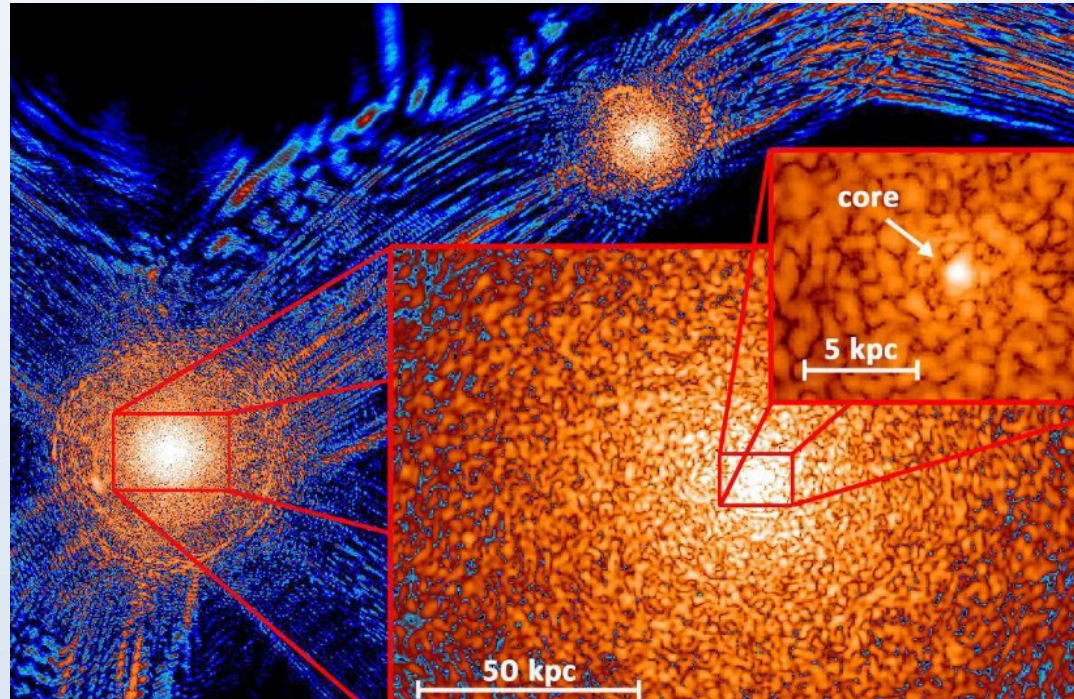
Fuzzy DM



Schive+2014

Background: Fuzzy dark matter

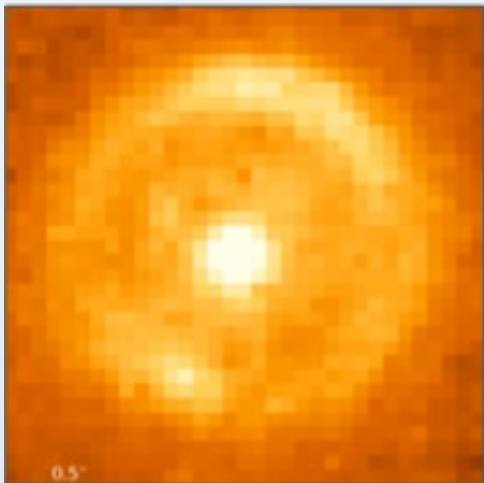
- Fuzzy dark matter (FDM) is a class of ultra-light DM that exhibits a \sim kpc-scale de Broglie wavelength (originally motivated by the mass of the QCD axion, but also may explain sub-galaxy-scale phenomena better than CDM)
- Main observable phenomena:
 - Suppressed halo mass function at low masses (Nadler+2021, Banik+2022, Laroche+2022)
 - Cored density profiles (most apparent in dwarf galaxies: Chen+2017, Safarzadeh+2020, Hayashi+2021)
 - “Granules” due to wave interference (This work, Marsh+2019, Laroche+2022)



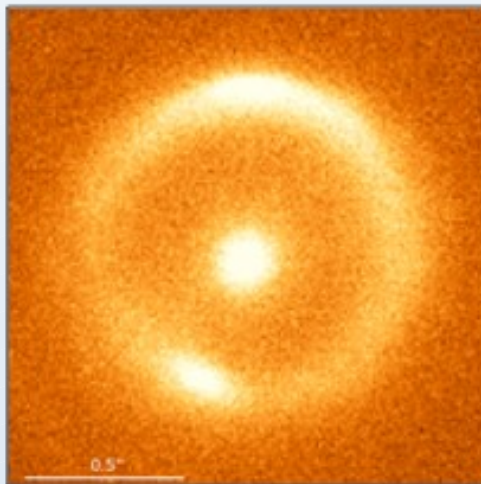
Background: angular resolution

- The sensitivity of a gravitational lens observation to low-mass dark structures is mainly determined by angular resolution.

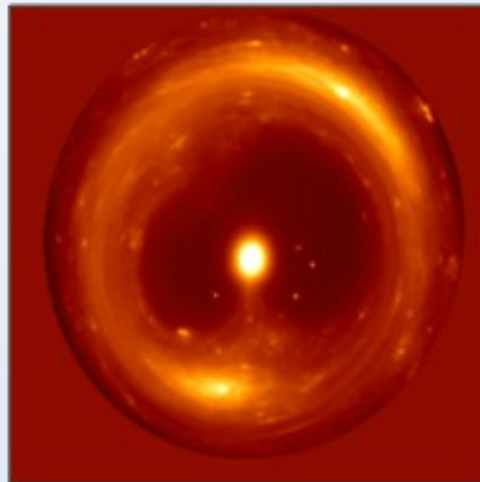
HST (*real data*)
 $\sim 10^9 M_{\text{sun}}$



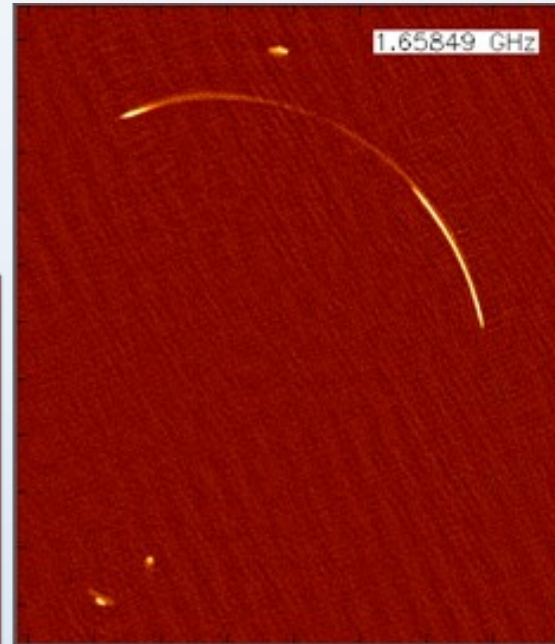
Keck AO (*real data*)
 $\sim 10^8 M_{\text{sun}}$



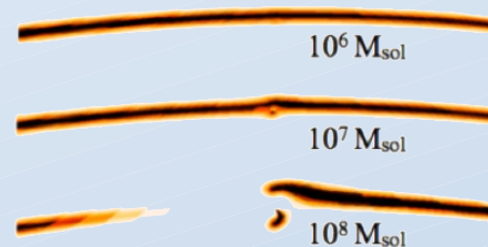
E-ELT (*mock data*)
 $\sim 10^7 - 10^6 M_{\text{sun}}$



Vegetti (MICADO simulator,
3 hours on-source)



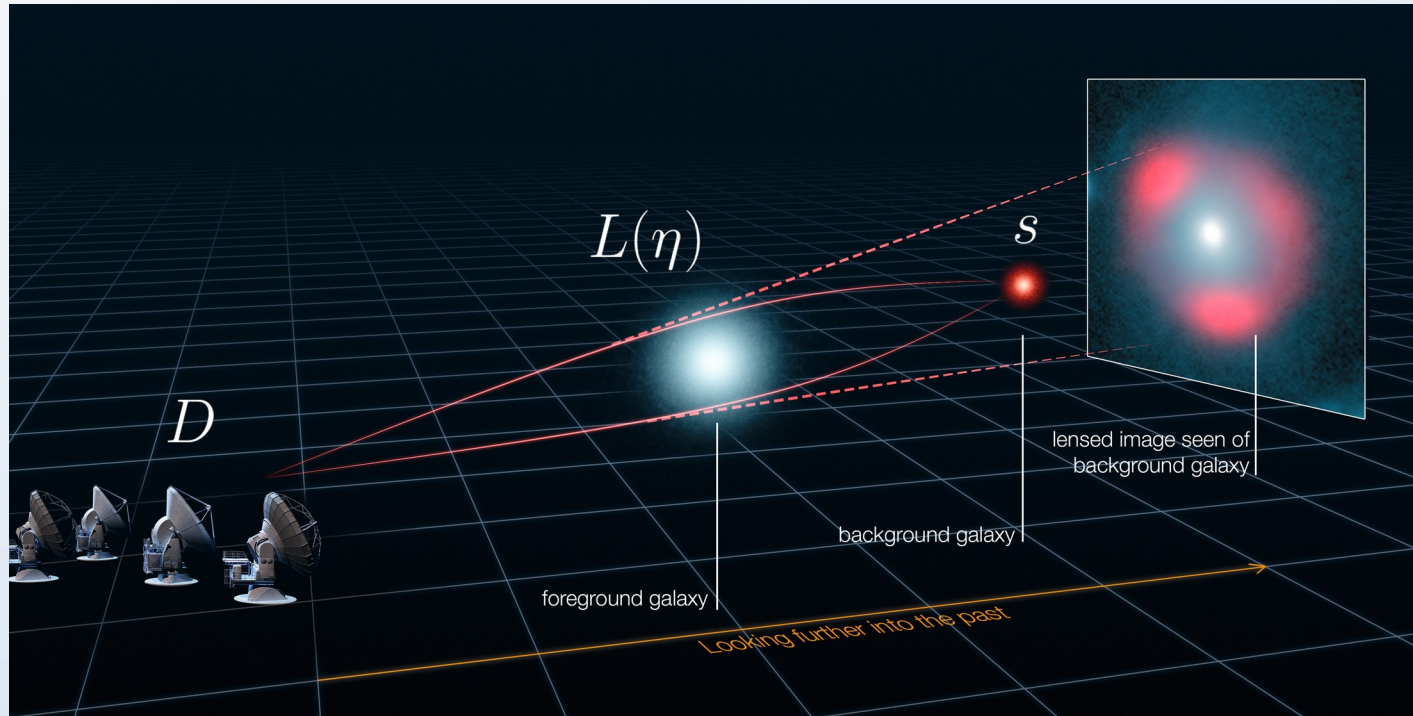
VLBI (*real data*)
 $\sim 10^6 M_{\text{sun}}$



McKean

Background: Radio interferometry

- Array of radio antennas samples Fourier modes of the sky brightness
- Each pair of antennas measures a “visibility” corresponding to one Fourier component
- The response of the instrument is a Fourier transform (D in the schematic below)
- **Distance between antennas and observing wavelength determines angular resolution $\sim \lambda/d$**

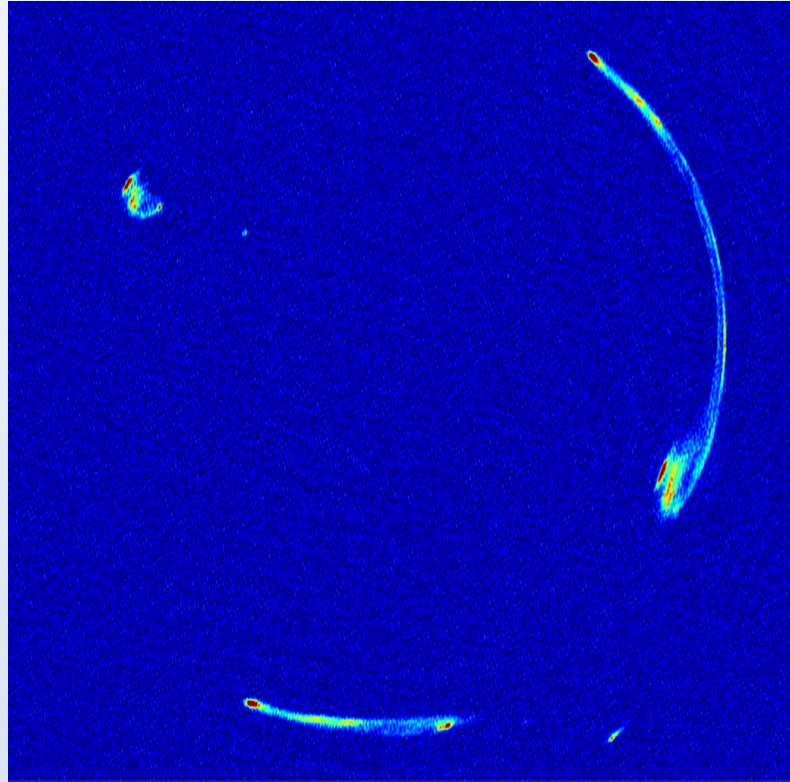
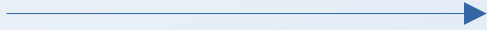


ALMA (ESO/NRAO/NAOJ), L. Calada (ESO), Y. Hezaveh et al.

Background: Gravitational lensing with VLBI

- We use global very long baseline interferometry (VLBI)
- Earth-scale antenna spacings give ~ 5 mas resolution at 1.6 GHz.
- Long, thin arcs are extremely sensitive to perturbations by low-mass dark structures in the lens!

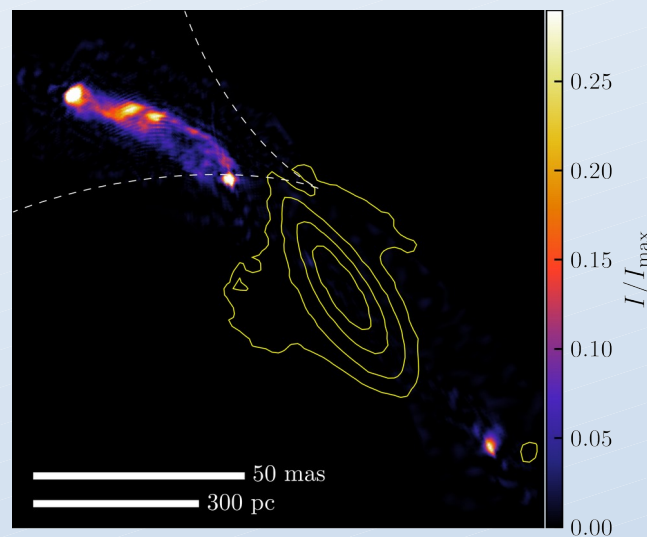
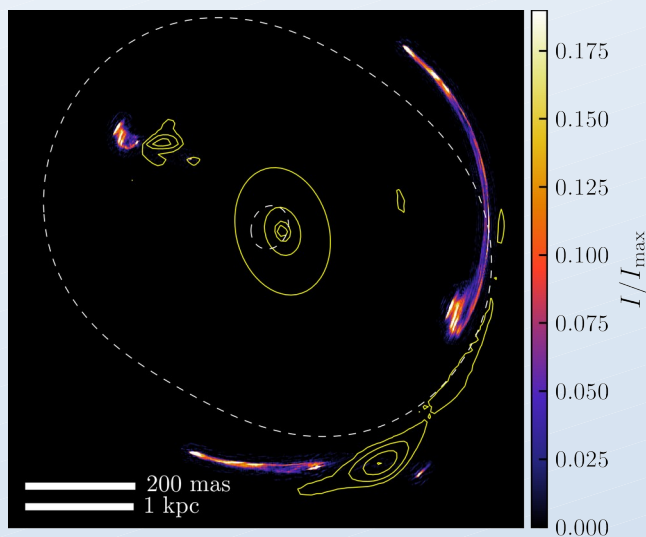
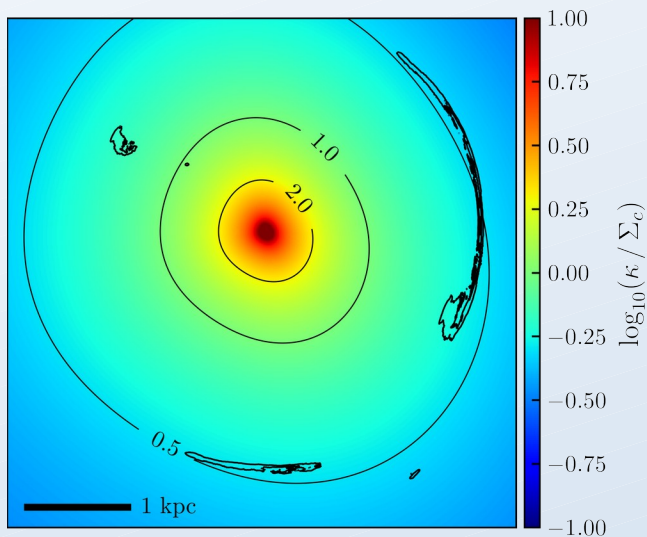
MG J0751+2716
Einstein radius is ~ 0.4 arcsec



Spingola+2018

Method: Forward modeling with VLBI data

- **Forward modeling:** Recover a pixellated source brightness model, as well as a likelihood, for a given lens model: Allow us to quantify how well a given lens mass distribution explains the observed data.
- I developed a tractable method for forward-modeling milli-arcsecond-resolution VLBI lens observations (Powell+2021).
- The first application to data was a global VLBI observation of the lensed radio jet MG J0751+2716 (Powell+2022, see below)
- **A smooth parametric lens model describes the data surprisingly well. This will be our baseline model for the FDM inference**



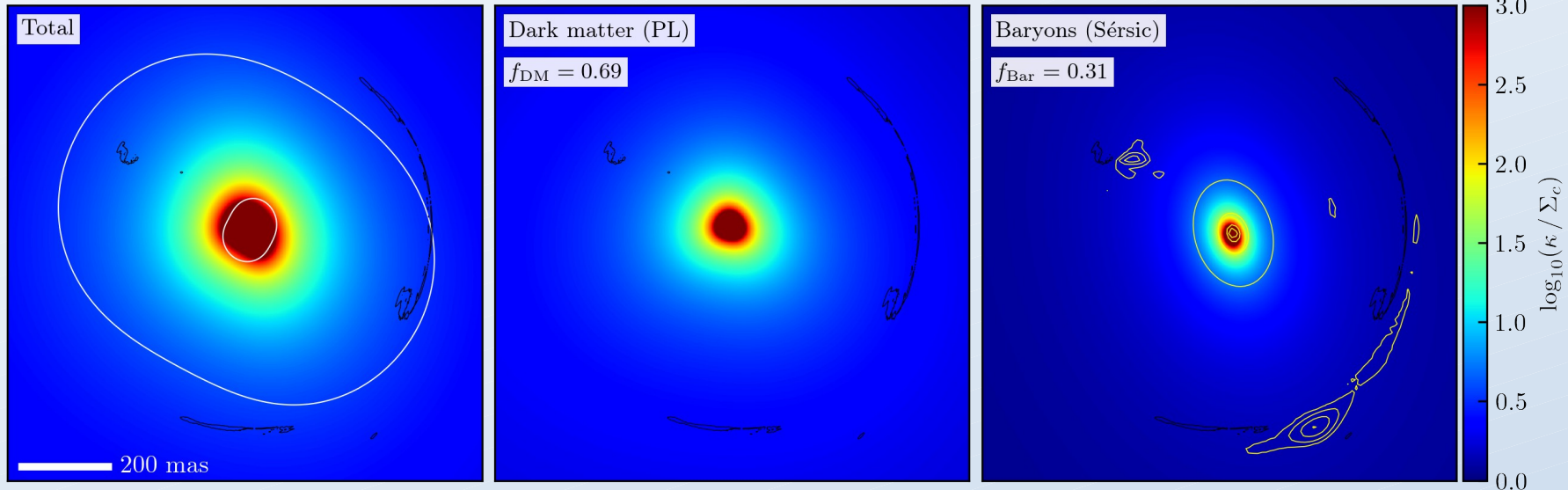
Method: Generating fuzzy lenses

- Chan+2020 analytically describes the density statistics of virialized wave dark matter in a potential well.
- The variance of the projected surface density fluctuations is a function of the dark matter density profile and the de Broglie wavelength:

$$\langle \delta\kappa^2 \rangle = \frac{\lambda\chi\sqrt{\pi}}{\Sigma_c^2} \int \rho_{\text{DM}}^2 dl,$$

- The (reduced) de Broglie wavelength is:

$$\lambda\chi = \hbar / (m_\chi \sigma_v)$$



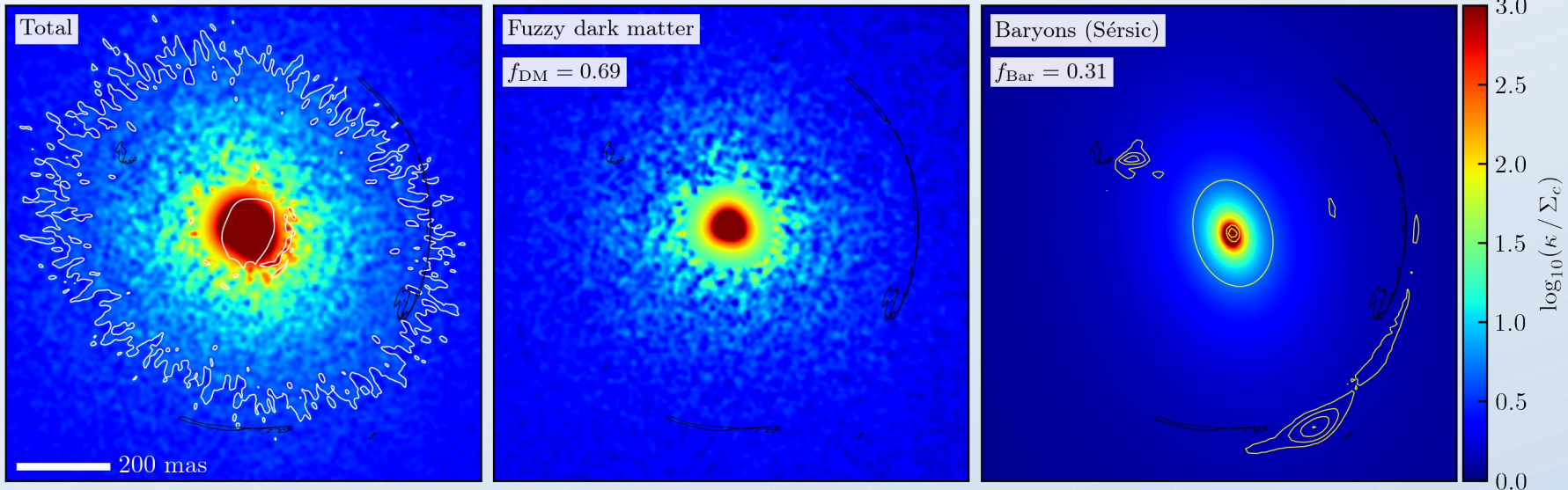
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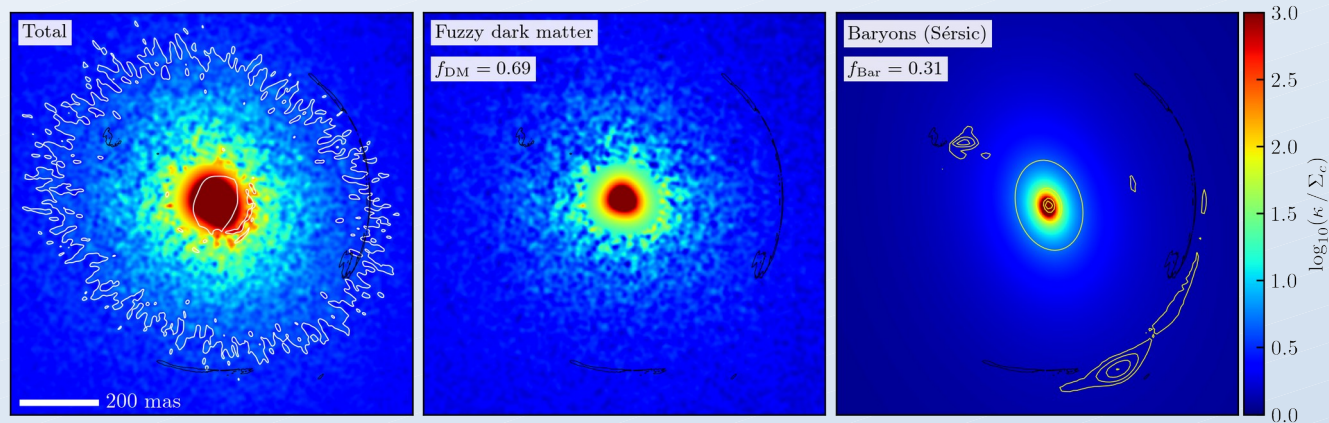
- The (reduced) de Broglie wavelength is:

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Method: Inference on FDM lens models

- 1) For a single fuzzy lens realization, we compute the likelihood $P_i(\mathbf{d} \mid m_\chi, f_{\text{DM}}, \sigma_v, \boldsymbol{\eta}, \lambda_s)$, where:
- \mathbf{d} are the data (interferometric visibilities)
 - m_χ is the DM particle mass
 - FDM is the dark matter fraction in the lens
 - σ_v is the velocity dispersion of the dark matter (a proxy for the depth of the potential well)
 - $\boldsymbol{\eta}$ are the smooth lens model parameters
 - λ_s is a hyper-parameter that controls the source regularization strength.
 - The subscript i denotes that this likelihood is one of an infinite number of random fuzzy DM realizations that are possible given these parameters.



Method: Inference on FDM lens models

2) We generate $\sim 40k$ fuzzy lens realizations, with parameters drawn from the following priors:

Parameter	Description	Prior
$\log_{10}(m_\chi)$	DM particle mass (eV)	$\mathcal{U}(-21.5, -19.0)$
f_{DM}	Projected DM mass fraction	$\mathcal{U}(0.5, 0.8)$
σ_v	DM velocity dispersion (km/s)	$\mathcal{U}(100, 110)$
η	Smooth lens model parameters	$\mathcal{N}(\mu_{\eta, \lambda_s}, \Sigma_{\eta, \lambda_s})$
λ_s	Source regularization strength	

3) We accept a sample if its likelihood P_i is above the 3σ contours of the baseline smooth model.

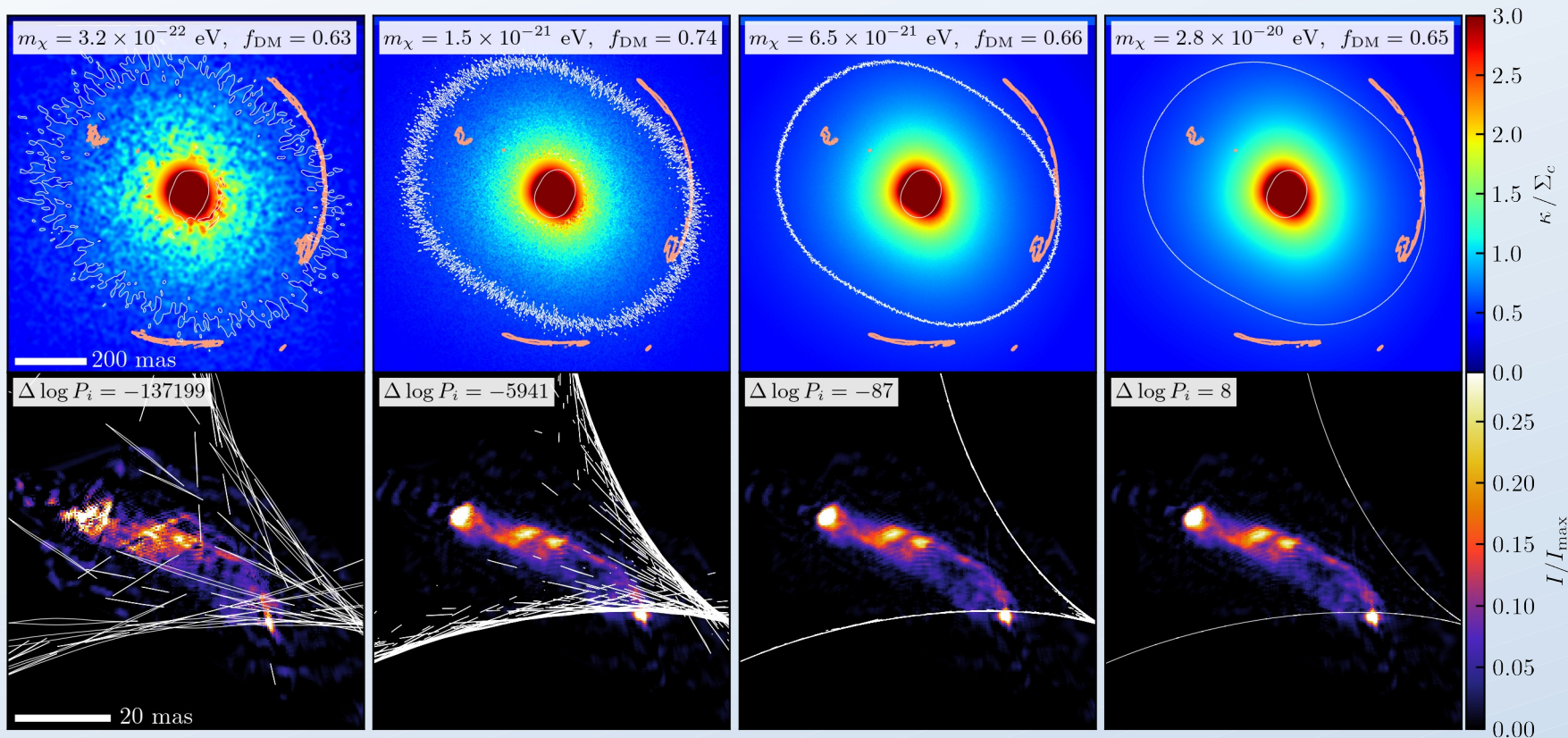
- i.e., for a FDM lens realization to be accepted, it must explain the data at least as well as the worst 0.3% of the smooth model posterior samples.
- In practice, we define a relative log-likelihood $\Delta \log P_i$, where samples are accepted if $\Delta \log P_i > 0$.

4) We build a histogram of the accepted samples to obtain an empirical posterior on m_χ

- All other parameters are marginalized over automatically
- In principle, it is possible to compute an analytic posterior, but the large random variance between individual realizations makes a converged posterior computationally prohibitive
- We instead opt for a conservative threshold, and uniformly weight the accepted samples

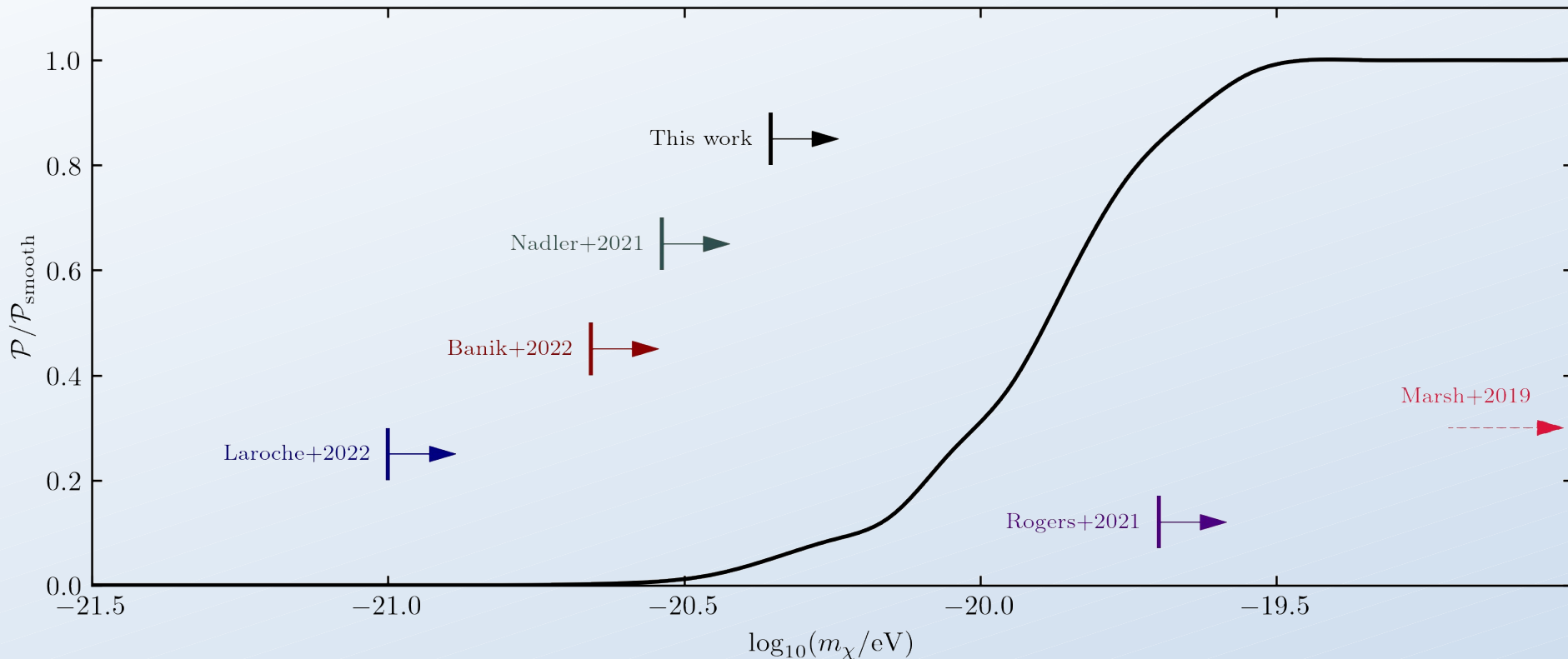
Results: disruption of the source morphology

- When the particle mass m_χ is low, the FDM density granules make the proposed lens model too lumpy
- The inferred source model takes on a disrupted morphology in an attempt to fit the data, given the lens model
- The inability of a fuzzy lens realization to explain the data is penalized in the likelihood, $\Delta \log P_i$



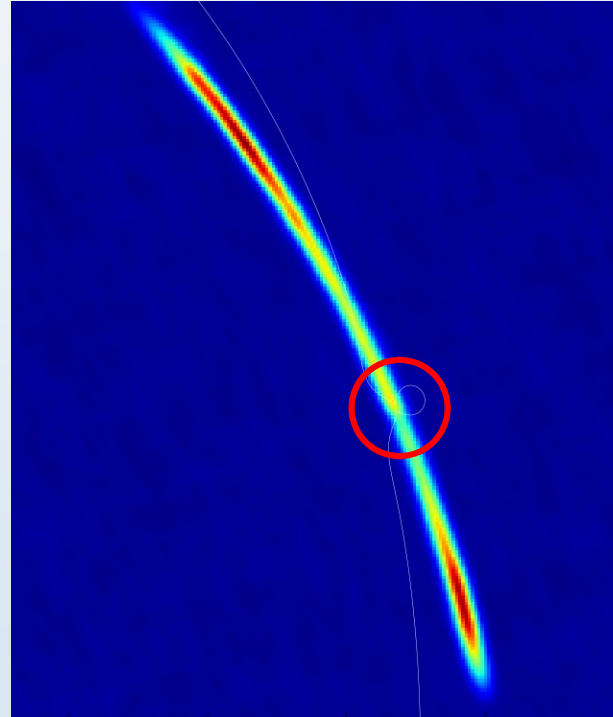
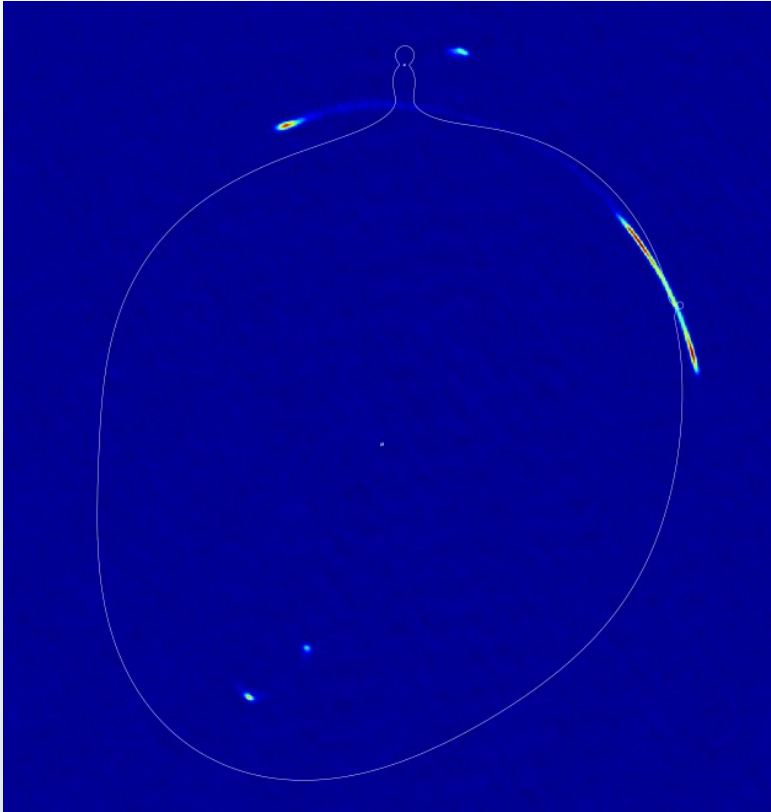
Results: Posterior odds ratio, relative to the smooth model

- $m_\chi = 4.4 \times 10^{-21}$ eV is ruled out with a 20:1 posterior odds ratio (POR)
- For vector fuzzy DM (3 DOF), $m_\chi > 1.4 \times 10^{-21}$
- This constraint is from a single lens observation!



Work in progress: B1938+666

- Very compact source sitting right on the caustic produces extremely smooth arcs.
- A “kink” in the arc indicates a low-mass perturber object near the critical curve.
- This dataset has ~ 5 mas resolution at 1.6 GHz, and the feature also appears in the 5GHz data at < 2 mas resolution.



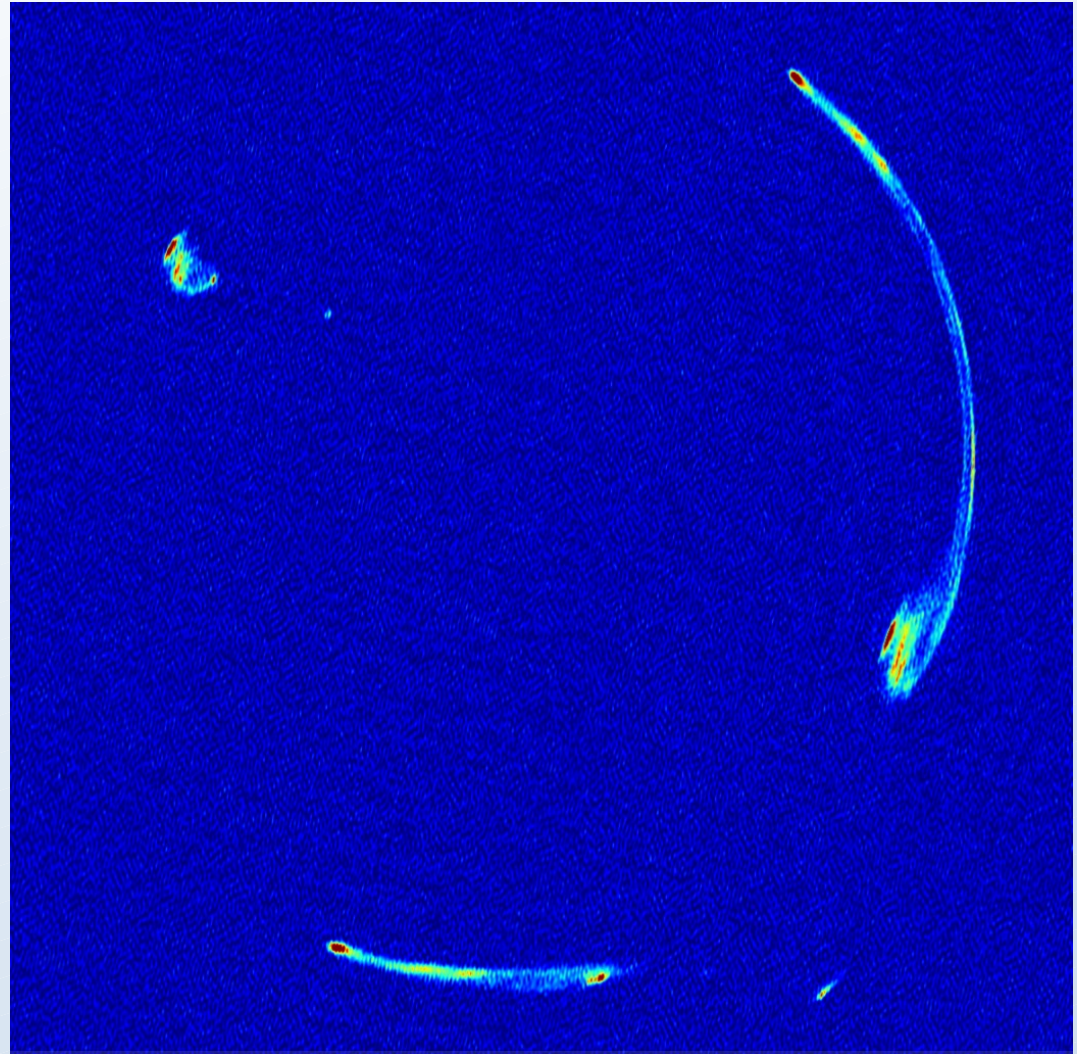
PRELIMINARY:

- $\sim 4 \times 10^6 M_{\text{sun}}$, assuming truncated PL
- Must also consider different possible density profiles, as well as redshift.

Observation and data reduction by John McKean

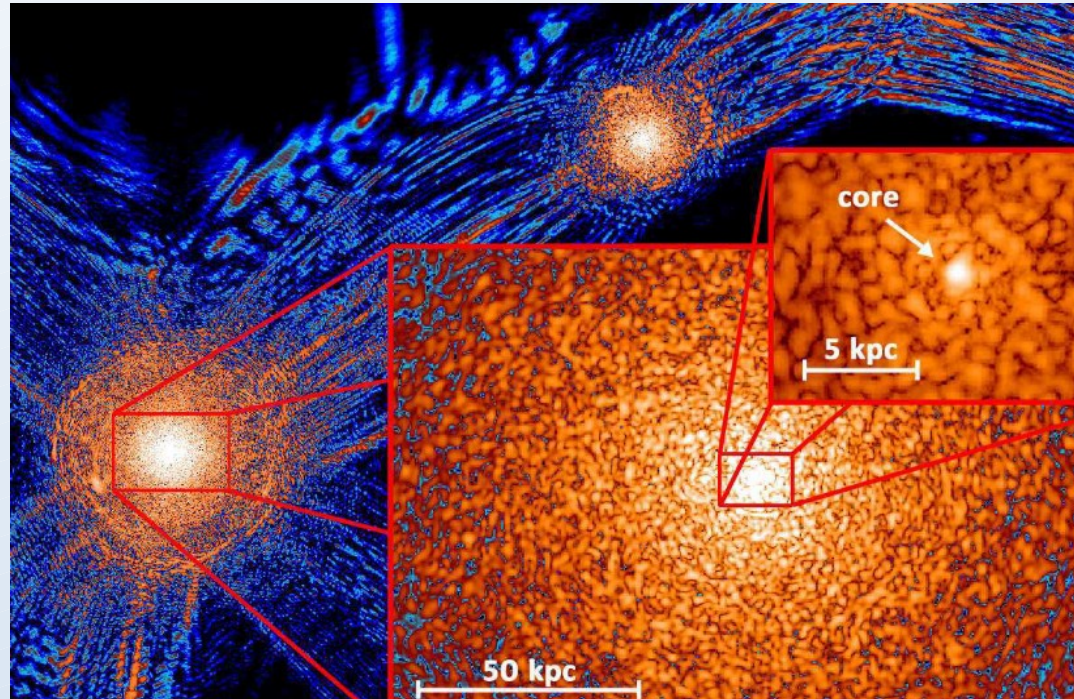
Conclusions

- VLBI provides the highest-resolution lens observations available to date. (< 5 mas, future will push to < 1 mas)
- Long, thin, smooth arcs are great for probing small-scale dark structure in strong lenses: Gives us direct sensitivity to the presence or absence of fuzzy DM granules in the lens.
- We expect sensitivity in m_χ to scale with angular resolution.
- SKA will discover tons of new radio-bright lenses with extended structure like this one.
- Sensitive to $10^6 M_{\text{sun}}$ subhaloes in WDM, analysis for WDM population statistics is ongoing
- Characterizing the sub/LOS-halo population should give constraints on WDM $m_\chi \sim 20$ keV

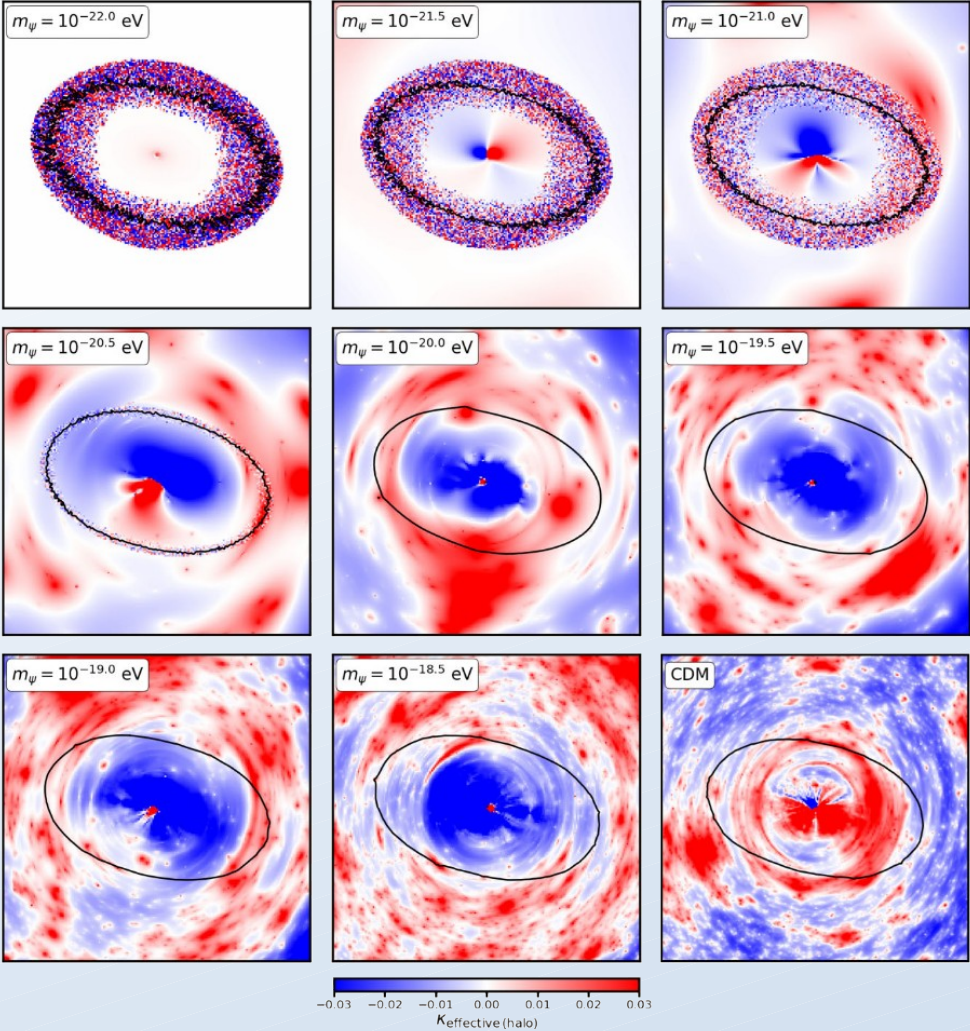


Recap: Fuzzy dark matter

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- Main observable phenomena:
 - Suppressed halo mass function at low masses (Nadler+2021, Banik+2022, Laroche+2022)
 - Cored density profiles (most apparent in dwarf galaxies: Chen+2017, Safarzadeh+2020, Hayashi+2021)
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Subhaloes in FDM

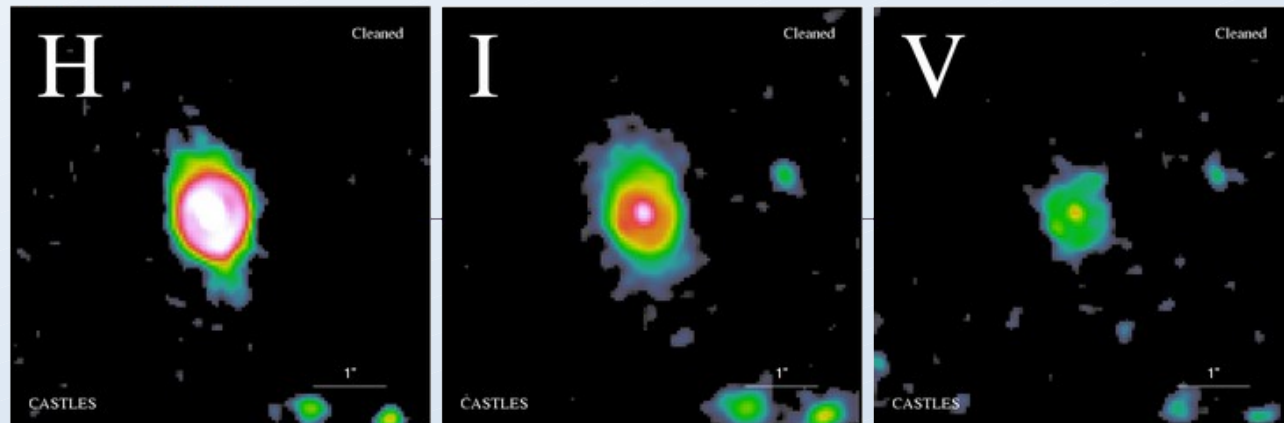


f_{DM} from HST photometry

- WFPC2 V- and I-band photometry gives $\sim 8 \times 10^9 M_{\text{sun}}$ stellar mass component.
- In good agreement with our composite smooth lens modeling, which gives $8.6 \times 10^9 M_{\text{sun}}$

Data from Castles			
Observations		G	Source
Position	RA(arcsec)	0	-0.634 ± 0.021
	Dec(arcsec)	0	-0.225 ± 0.026
fluxes	F160W	18.87 ± 0.16	21.66 ± 0.25
	F555W	23.24 ± 0.11	25.10 ± 0.25
	F814W	21.26 ± 0.03	23.72 ± 0.05

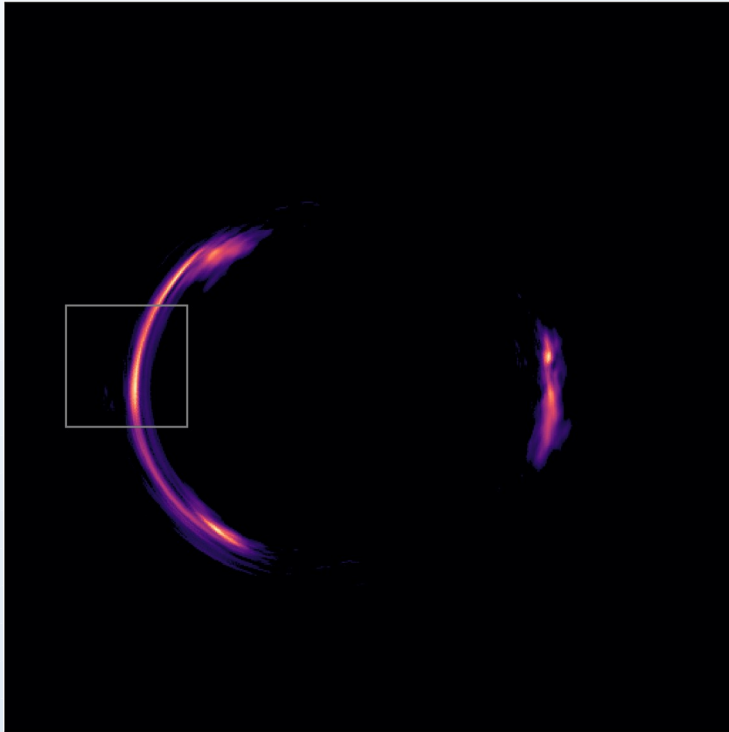
Cleaned data:



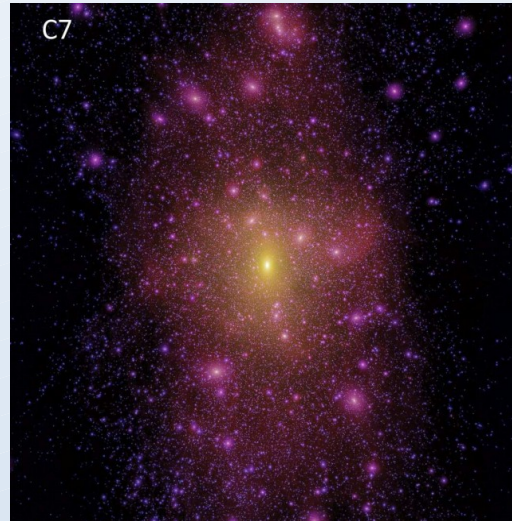
CASTLES survey

Background: Strong gravitational lensing (galaxy-galaxy)

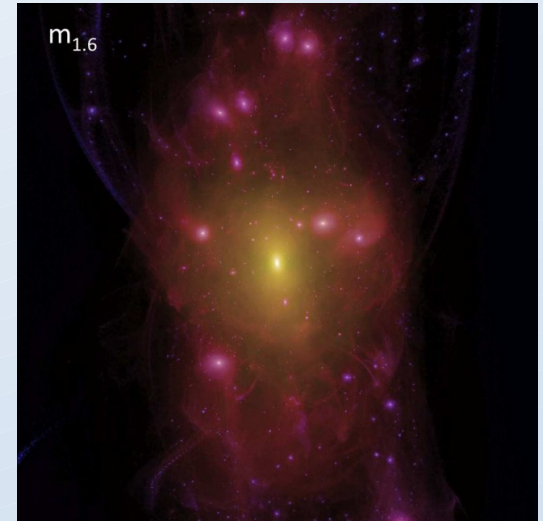
- We can infer the properties of subhaloes (or granules, or other dark structures) via their effect on the lensed arcs.
- In this talk, we are focusing on the case of extended (resolved) sources, *not* unresolved point images.
- This slide is just an illustrative example of a single subhalo in CDM/WDM. The rest of the talk is about fuzzy DM, which produces a very different mass distribution in the lens galaxy (wait a few slides).



CDM

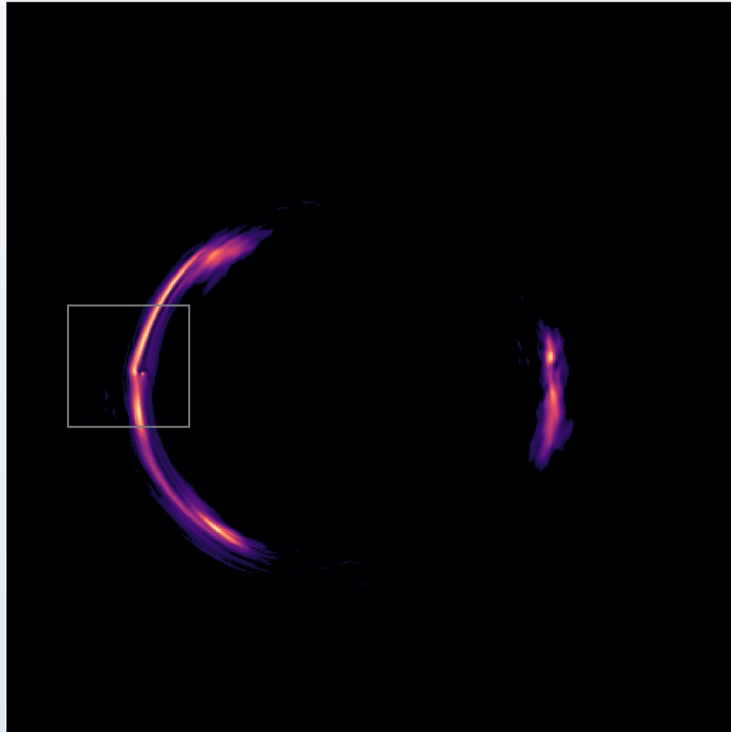


WDM

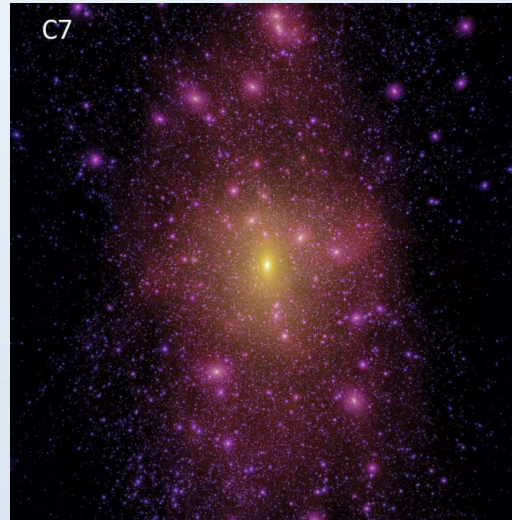


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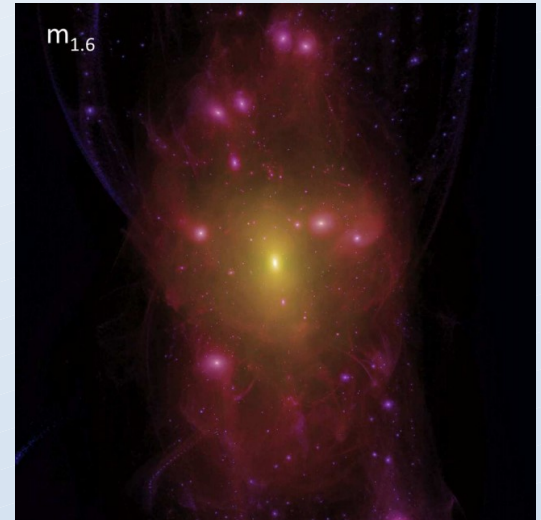
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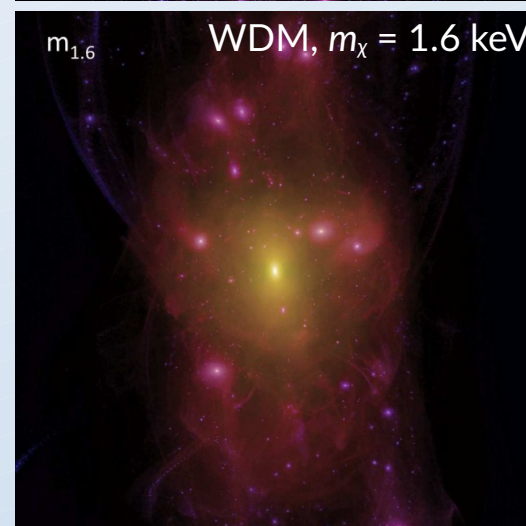
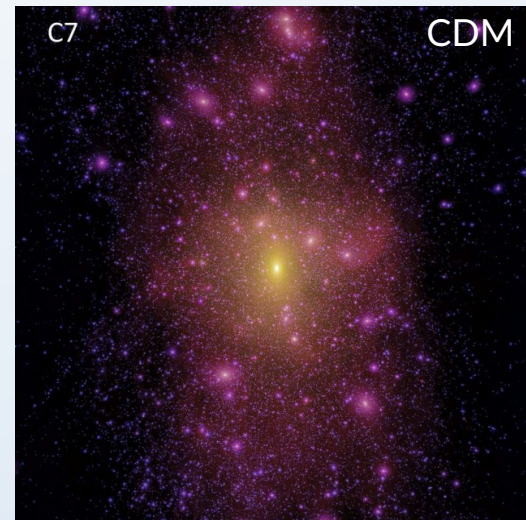
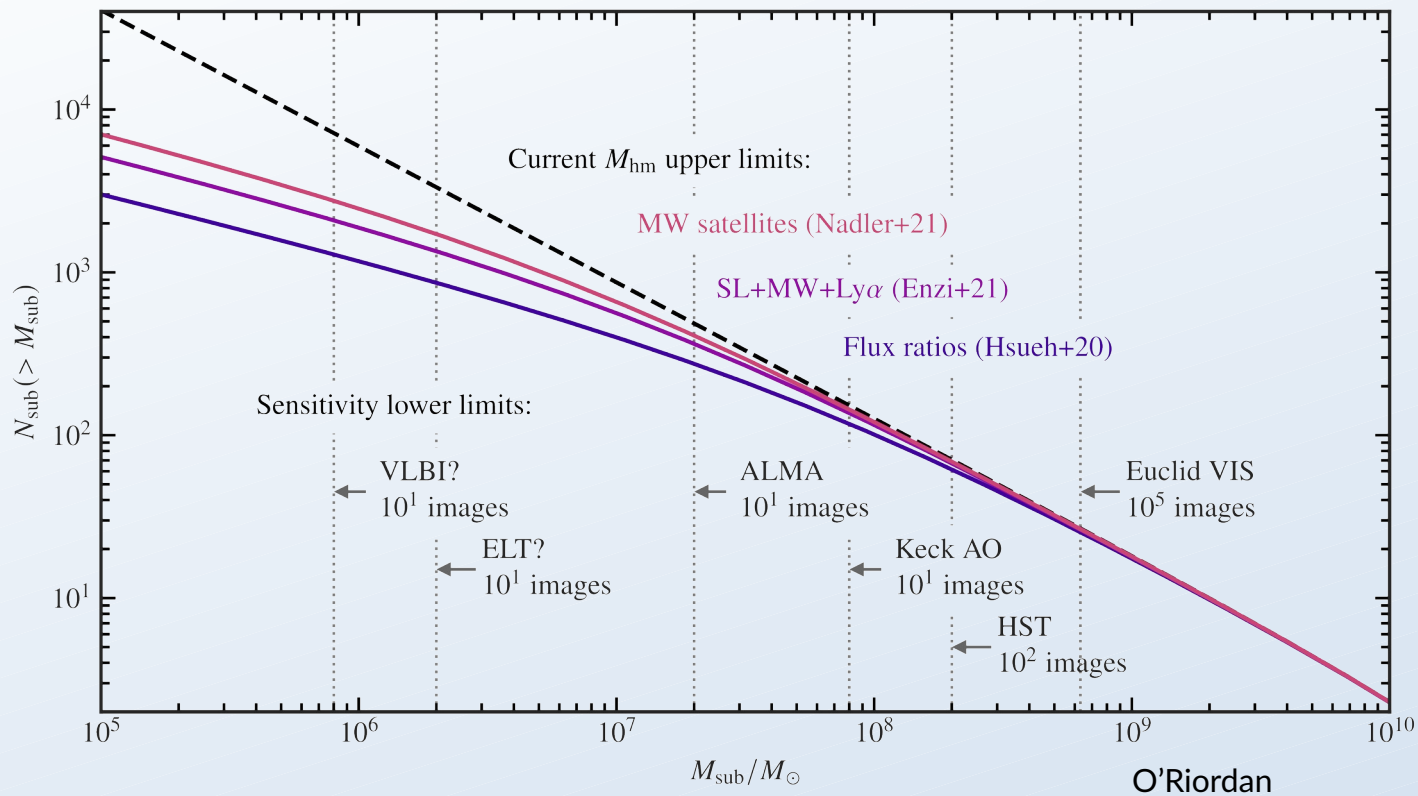
CDM



WDM



WDM constraints

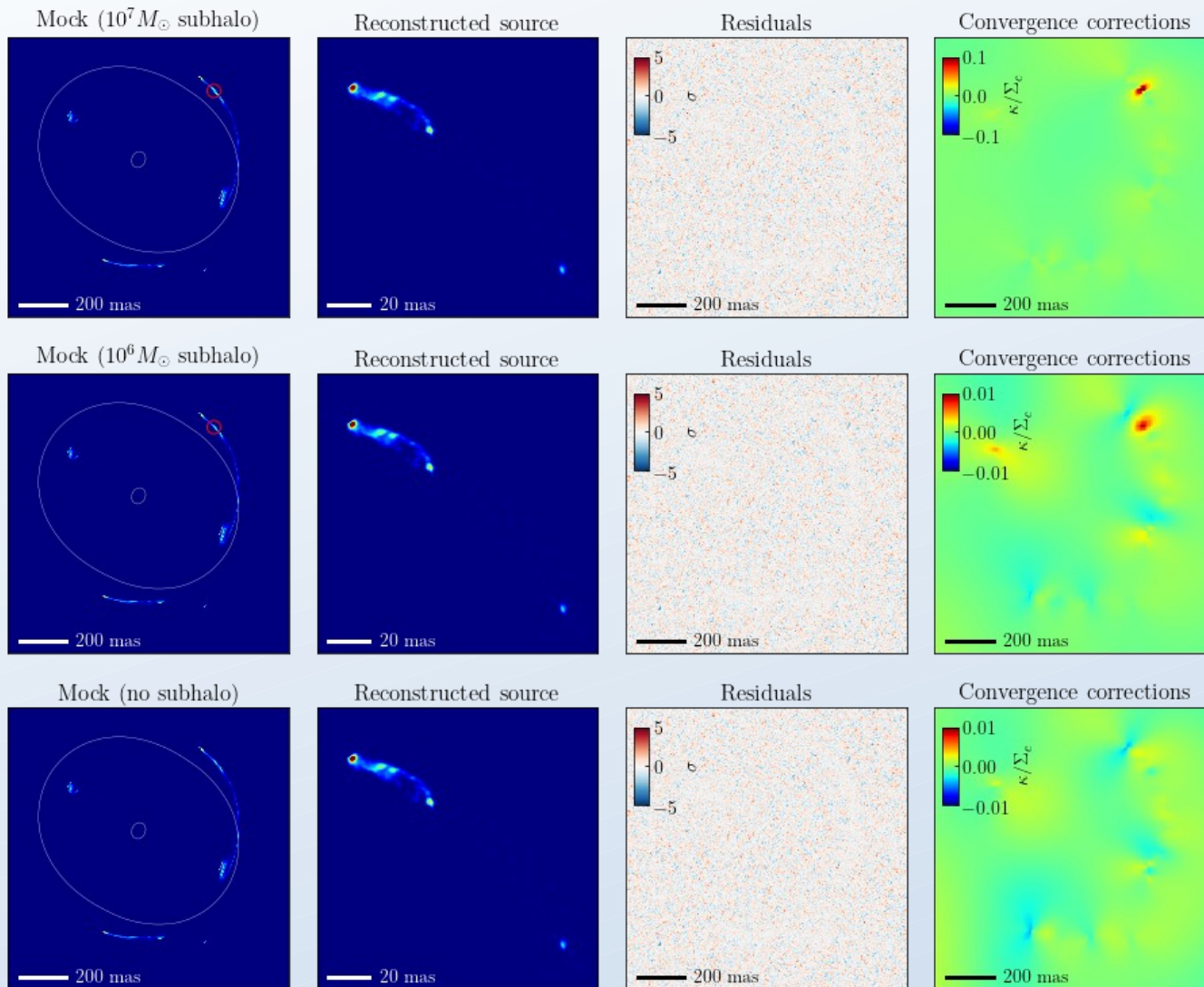


Lovell+2014

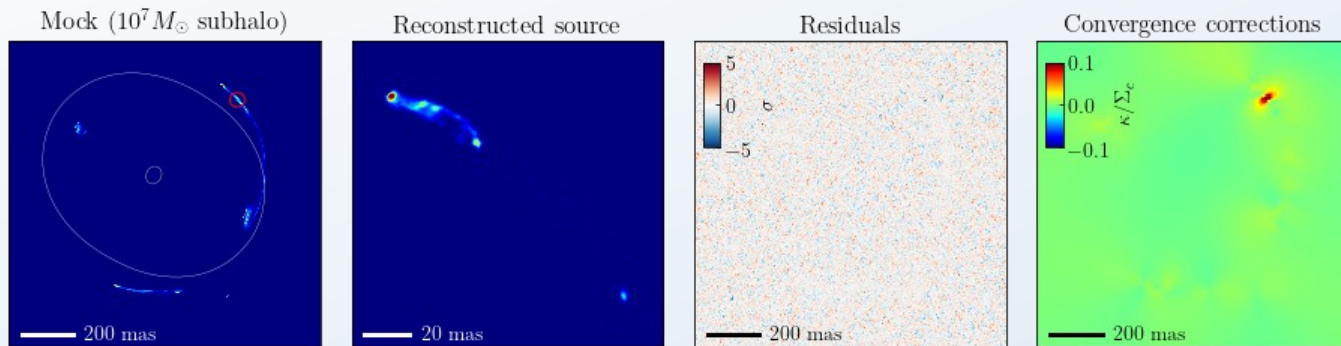
(Current best constraint is $m_{\chi} > 9.7$ keV by Nadler+2021)

Warm DM (mock data)

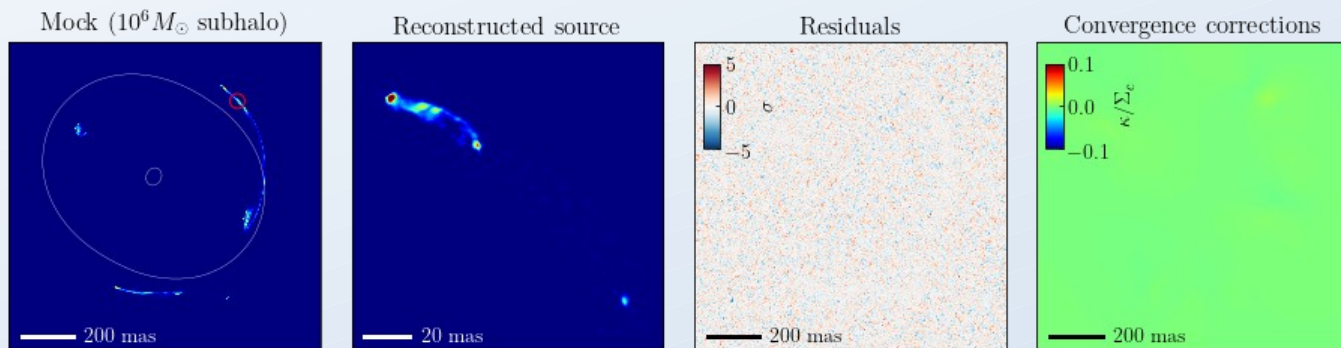
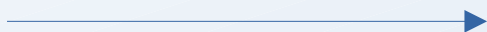
- Gravitational imaging analysis on mock data. Same resolution, array configuration, SNR as the real MG J0751+2716 observation.
- *Isolated* 10^6 and $10^7 M_{\text{sun}}$ subhaloes are easily detected with data of this quality.
- Halo mass function constraints will require a statistical approach, e.g. ABC (see Aleksandra Grudskaia)
- **Characterizing the sub/LOS-halo population will give constraints on $m_\chi \sim 20$ keV, using a single lens observation.**



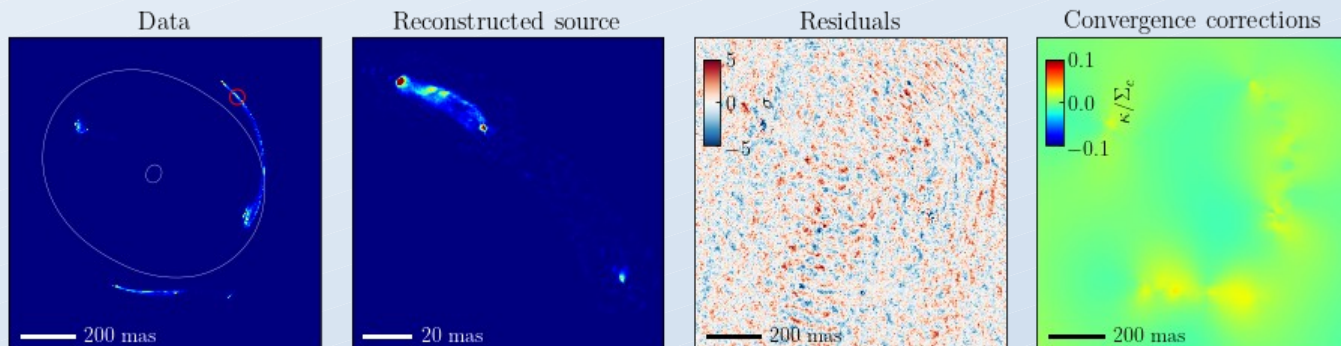
Warm DM (real data)



Color scales are consistent now

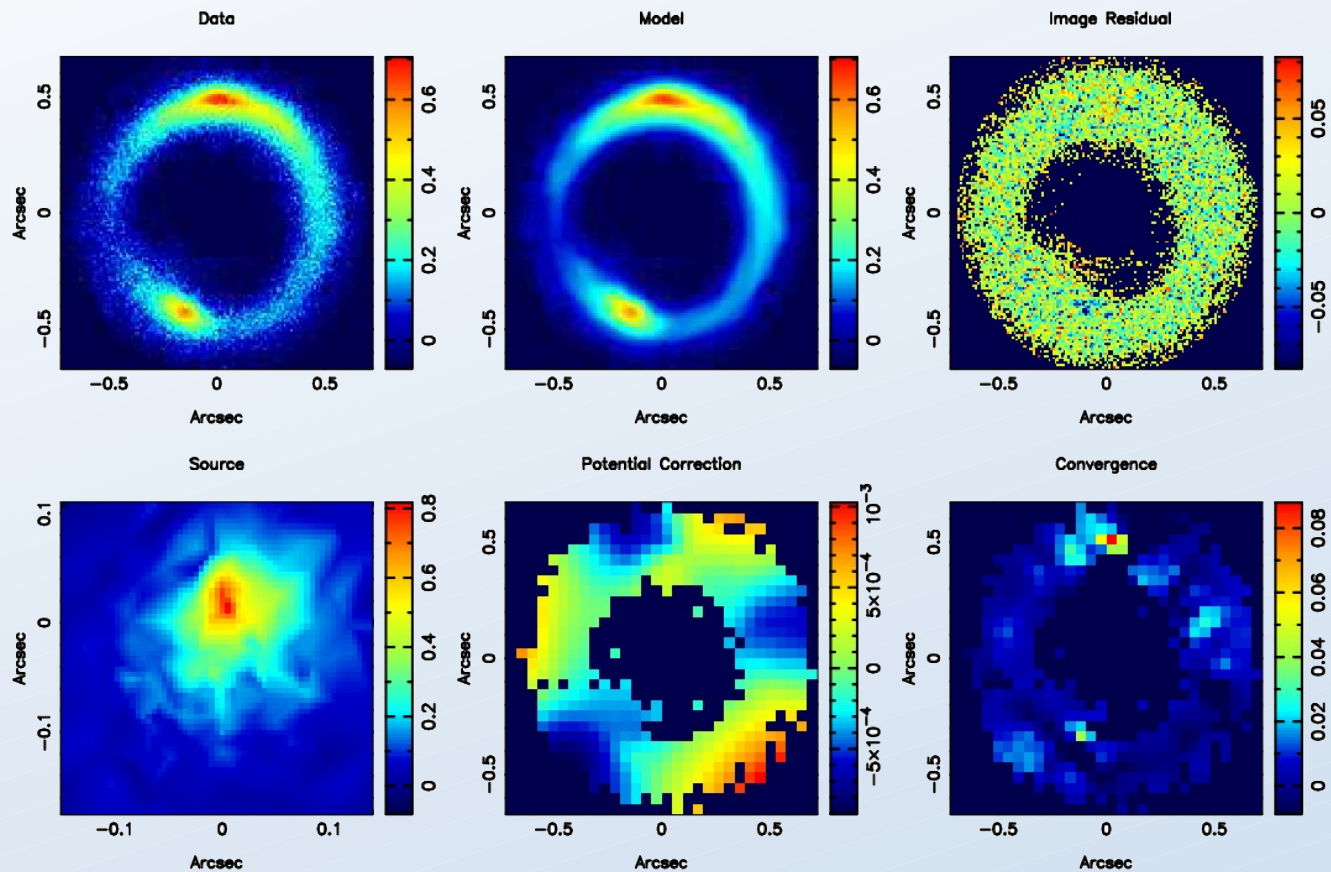


The real data show no obvious
 $10^7 M_{\text{sun}}$ features...



Gravitational imaging

A $\sim 10^8 M_{\text{sun}}$ dark structure detected in Keck AO data:
(Vegetti+2012)

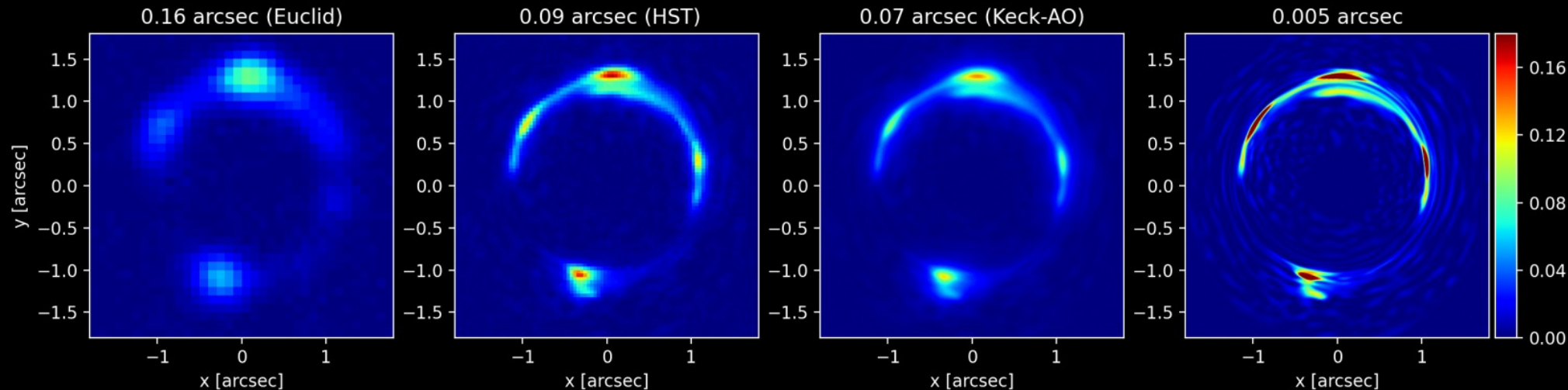


The Global VLBI - Array



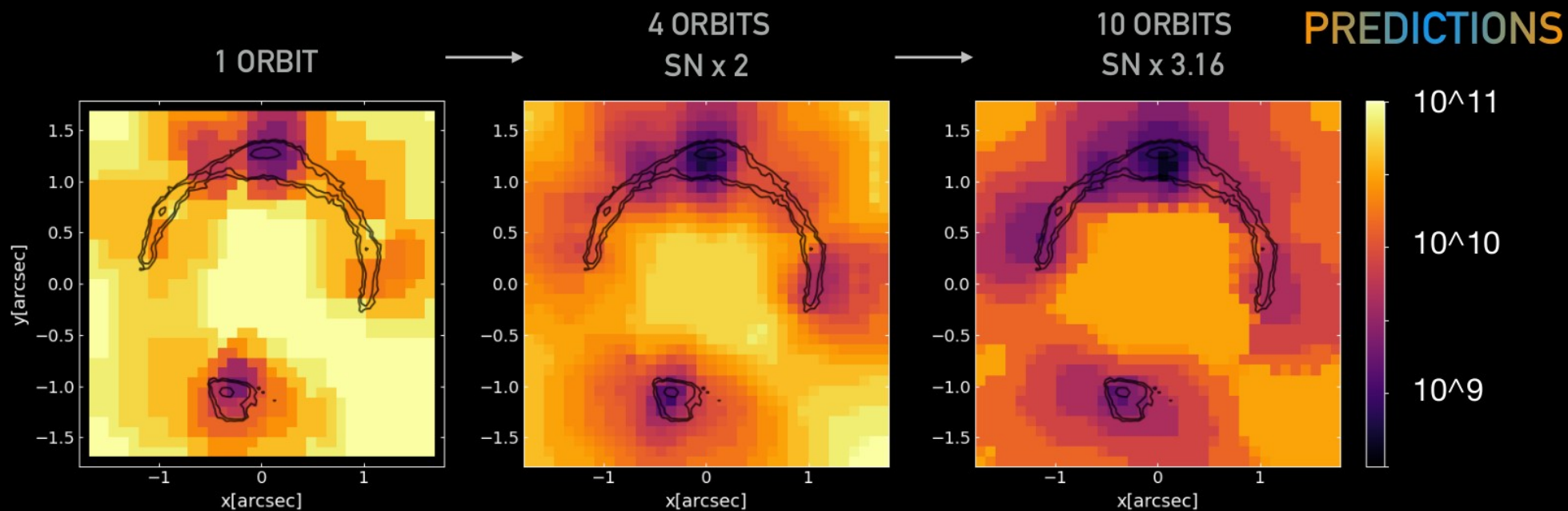
SENSITIVITY FUNCTION

increasing resolution →



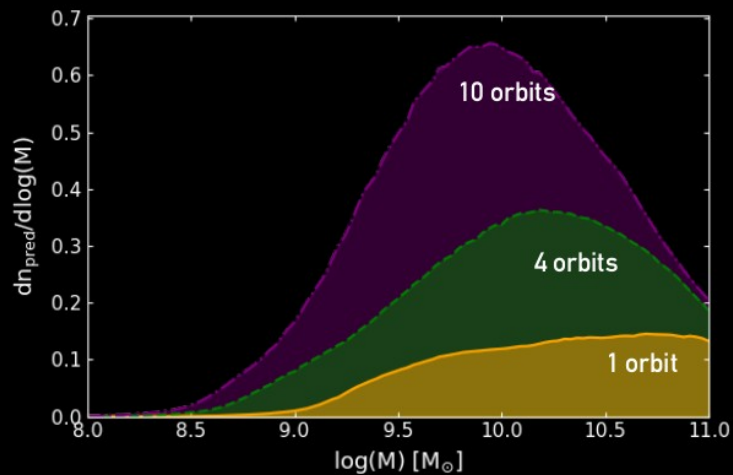
- HST images from the BELLS-GALLERY sample (*Ritondale et al. 2019*)
- Keck-AO images from the SHARP sample (*Vegetti et al. 2012*)
- ALMA data from *Stacey et al. 2021* (sub.)
- $z_l > 0.5$, $z_s > 2$

(*Despali et al. 2021*)

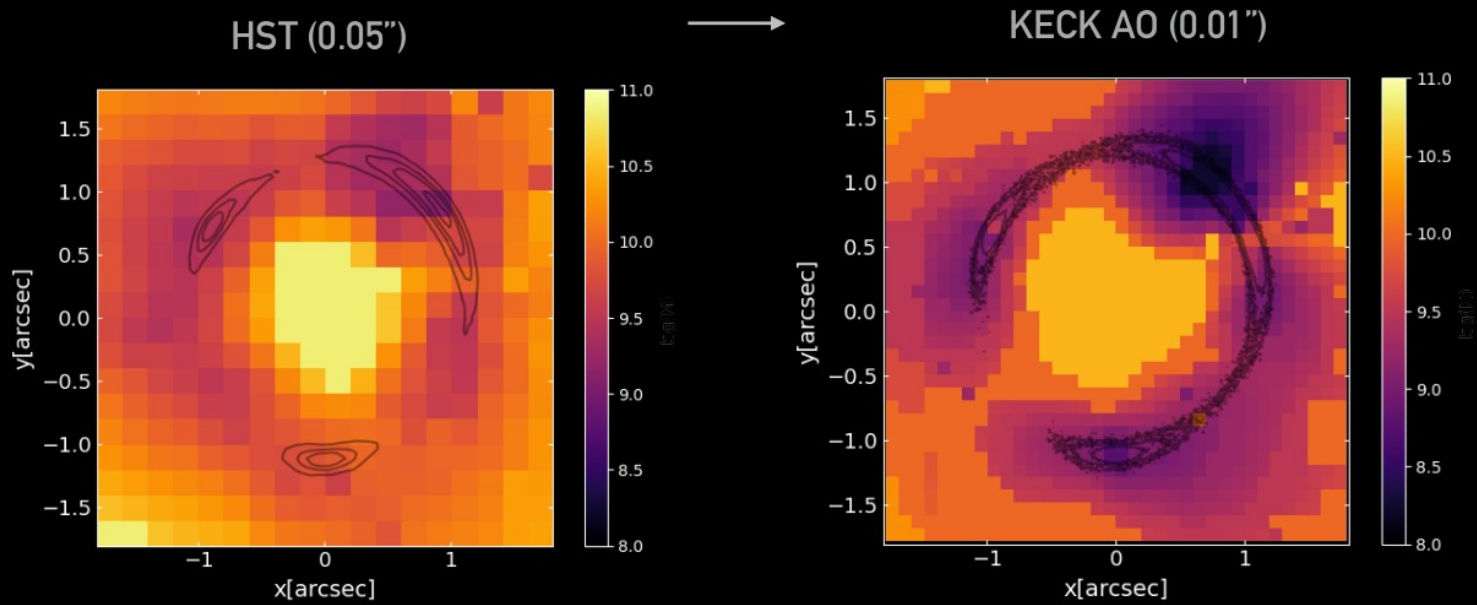


increasing SN ratio at
fixed resolution:

more detections

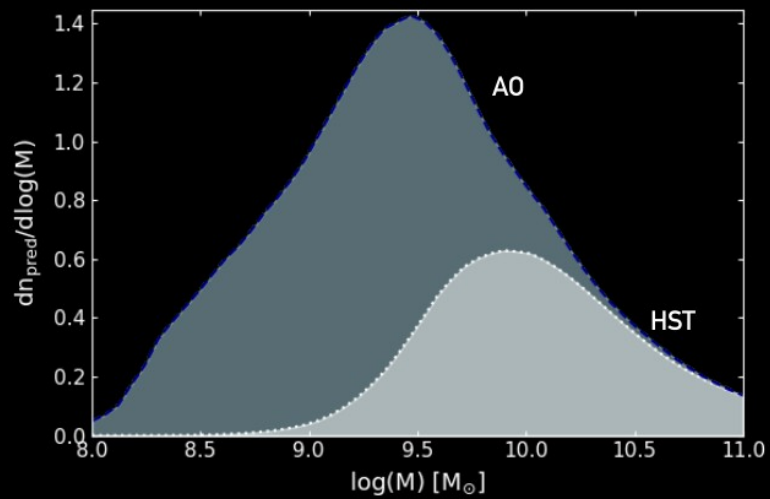


(Despali et al. 2021)



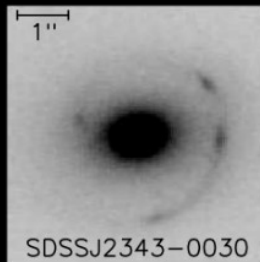
increasing resolution:

more detections
AND
lower mass limit

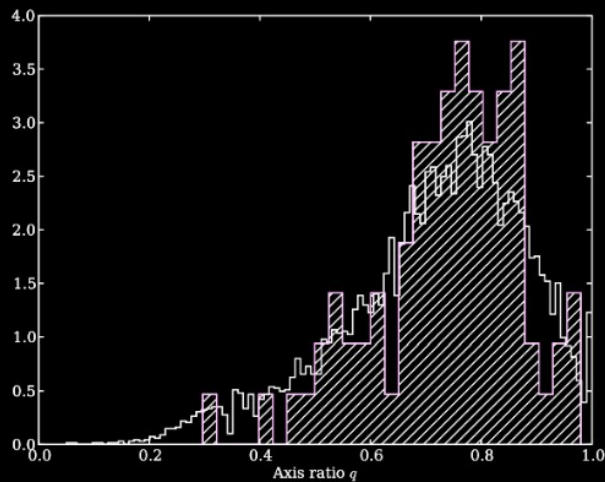


SHAPES IN SELF-INTERACTING DM

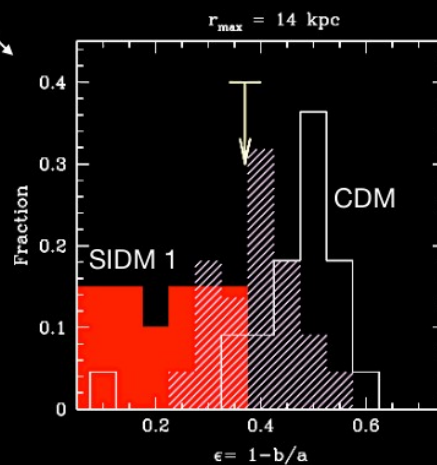
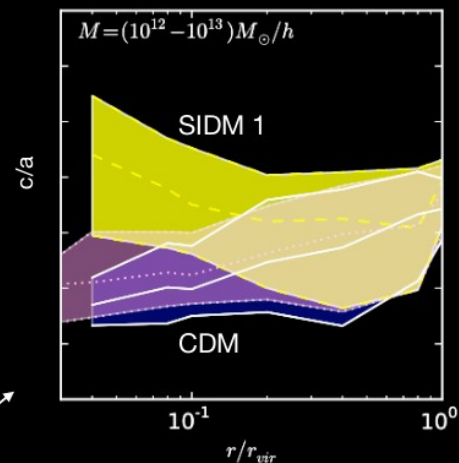
Grav. Lensing - galaxies are SIE with constant axis ratio in the center



(Auger+10)



(Peter+13) - SIDM produces rounder haloes

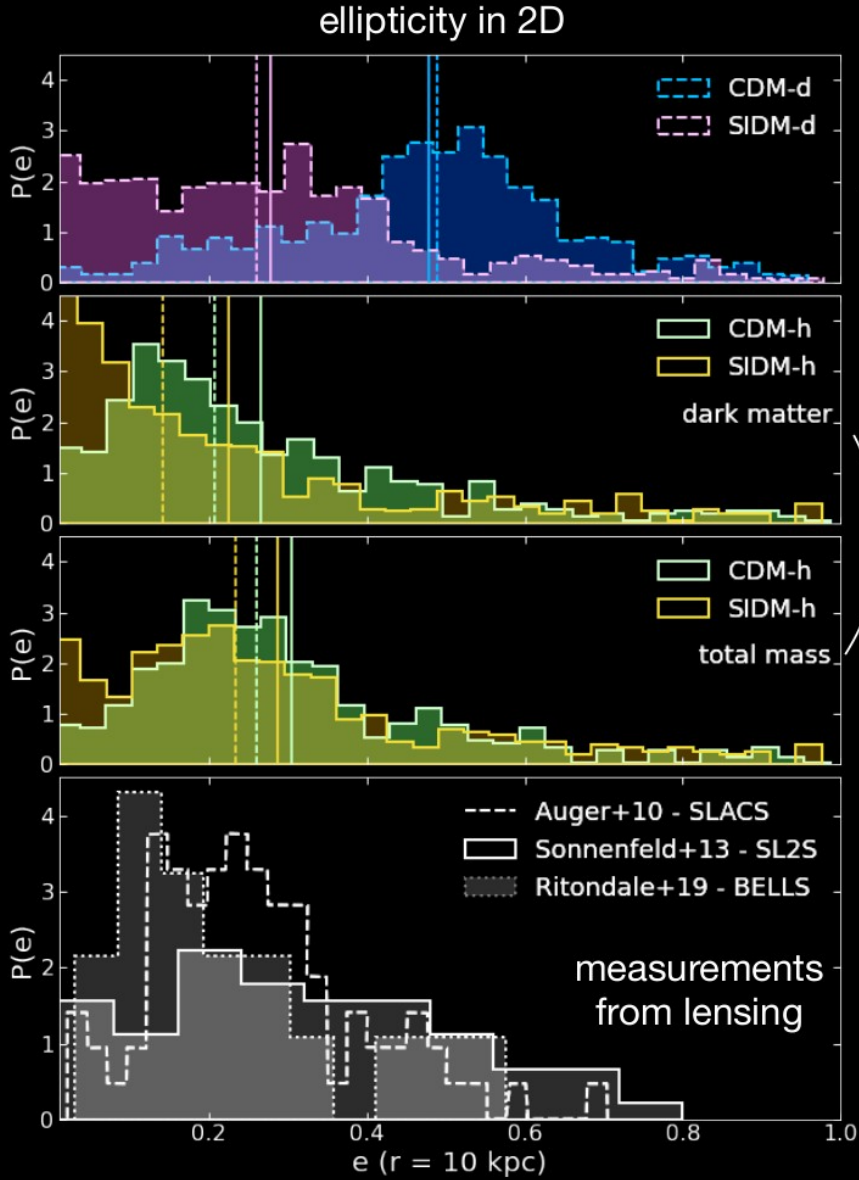


one of the strongest constraints on SIDM comes from shapes:
 $\sigma \leq 0.1$

BUT: based on DM-only simulations

SHAPES IN SELF-INTERACTING DM

(Despali et al. 2022)



hydro simulations with AREPO and TNG model in CDM and SIDM with $\sigma=1$

DM-only shapes are very different and SIDM is much more spherical

including baryons the two distributions are very similar

the comparison with lensing shapes prefers CDM hydro halos (higher p-value), but SIDM with $\sigma=1$ is not excluded

baryons can significantly alter the predictions