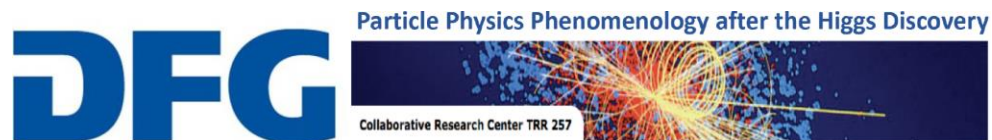


Standard Model Predictions and Global Fits for $b \rightarrow s\mu^+\mu^-$

Nico Gubernari

Based on
arXiv:2011.09813
arXiv:2206.03797
in collaboration with
Danny van Dyk, Javier Virto, and MÉRIL Reboud

BSM Forum
CERN, Switzerland
13-Oct-2022



Talk outline

Introduction

Theoretical framework

- $b \rightarrow s\ell^+\ell^-$ effective Hamiltonian
- parametrization for local and non-local form factors
- dispersive bound

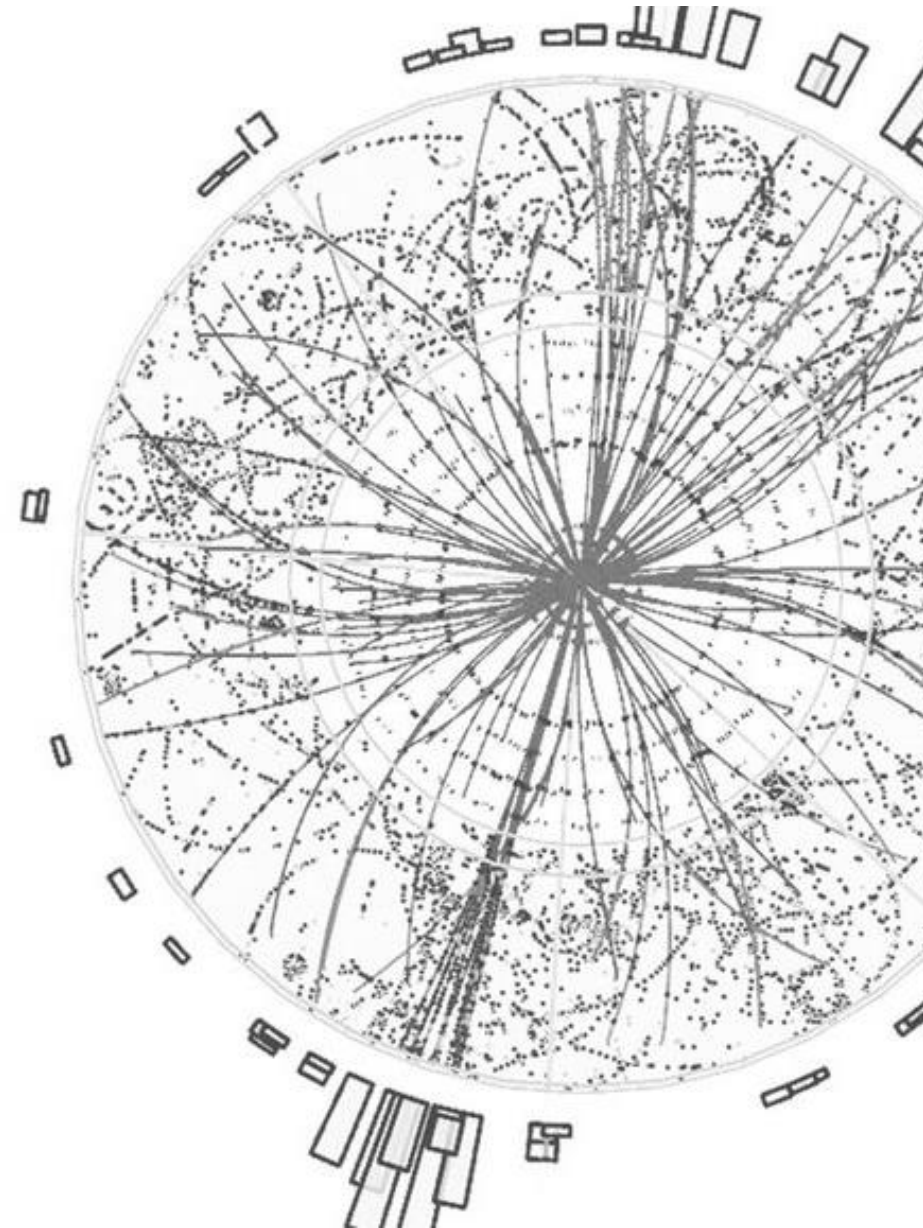
Theoretical predictions

- predictions for local and non-local form factors
- predictions of BRs and angular observables in $B_{(s)} \rightarrow \{K^{(*)}, \phi\}\ell^+\ell^-$

Confrontation with data

- comparison between SM predictions and data
- global fit to $b \rightarrow s\mu^+\mu^-$

Summary and outlook



Introduction

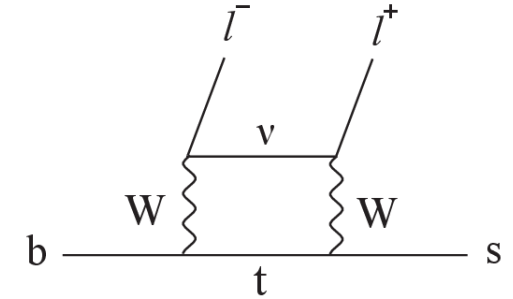
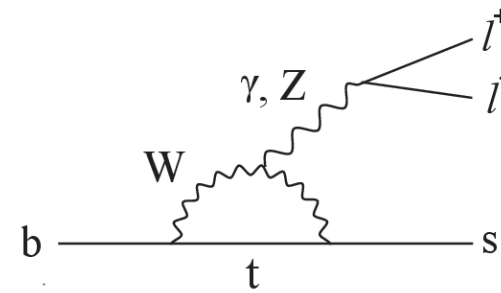
Flavour changing currents

flavour changing neutral currents (FCNC) absent at tree level in the SM

FCNC are loop, GIM and CKM suppressed in the SM

FCNC sensitive to new physics contributions probe the SM through indirect searches

focus on $b \rightarrow s \ell^+ \ell^-$ transitions



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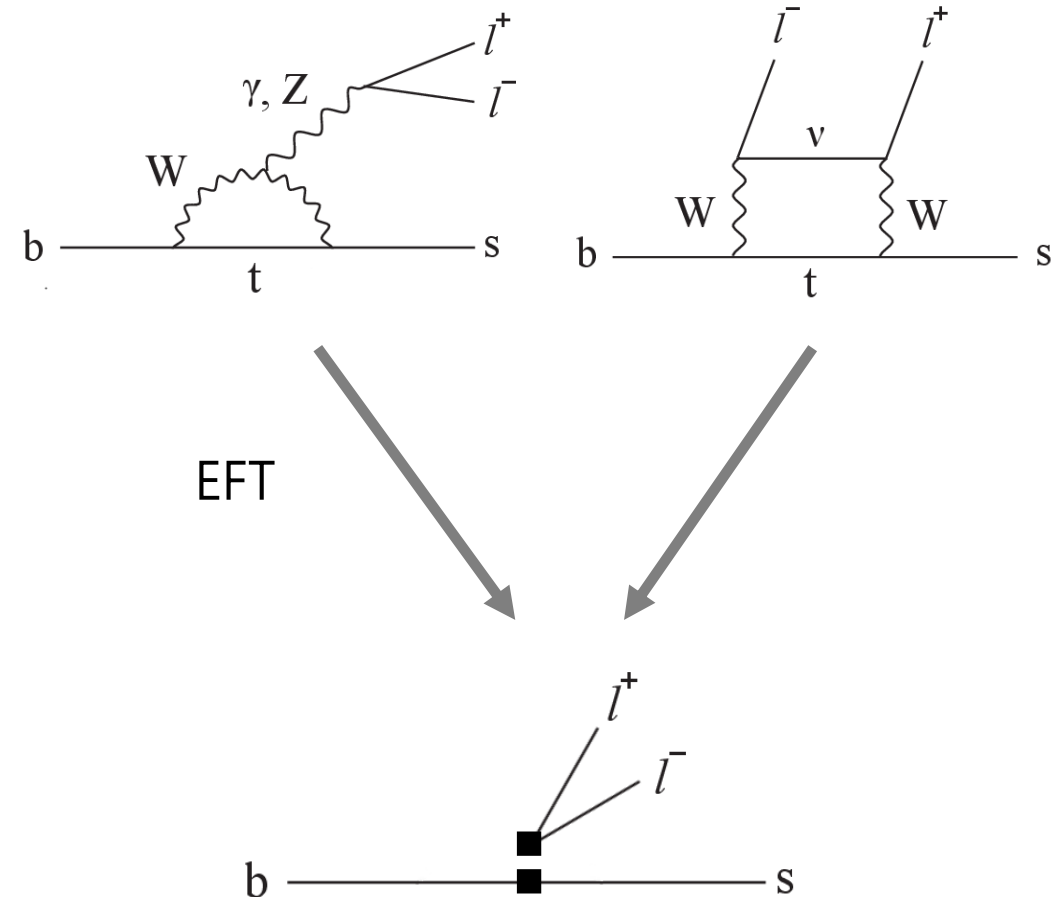
FCNC sensitive to new physics contributions probe the SM through indirect searches

focus on $b \rightarrow s \ell^+ \ell^-$ transitions

integrate out heavy degrees of freedom (W, Z , and Higgs boson, top quark)



weak effective field theory



Hadronic matrix elements

study **B**-meson decays to test the SM, focus on to $B \rightarrow K^{(*)} \ell^+ \ell^-$ and $B_s \rightarrow \phi \ell^+ \ell^-$
factorise decay amplitude as (neglecting QED corrections)

charged currents:
$$\langle \bar{D}^{(*)} \ell \nu_\ell | \mathcal{O}_{eff} | B \rangle = \langle \ell \nu_\ell | \mathcal{O}_{lep} | 0 \rangle \langle D^{(*)} | \mathcal{O}_{had} | B \rangle$$

FCNC:
$$\langle K^{(*)} \ell^+ \ell^- | \mathcal{O}_{eff} | B \rangle = \langle \ell \ell | \mathcal{O}_{lep} | 0 \rangle \langle K^{(*)} | \mathcal{O}_{had} | B \rangle + \text{non-fact.}$$

leptonic matrix elements: perturbative objects, high accuracy

hadronic matrix elements: non-perturbative QCD effects, usually large uncertainties

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leptonic matrix elements: perturbative objects, high accuracy

hadronic matrix elements: non-perturbative QCD effects, usually large uncertainties

decay amplitudes depend on:

- local hadronic matrix elements
(local form factors)
 $\langle K^{(*)} | \mathcal{O}(0) | B \rangle$
 $\langle D^{(*)} | \mathcal{O}(0) | B \rangle$
- nonlocal hadronic matrix elements
(soft gluon contributions
to the charm-loop)
 $\langle K^{(*)} | \mathcal{O}(0, x) | B \rangle$

Interesting observables

define observables smartly to reduce the hadronic uncertainties

e.g., observable P'_5 : angular observables in $B \rightarrow K^* \ell^+ \ell^-$

test the lepton flavour universality to test the SM

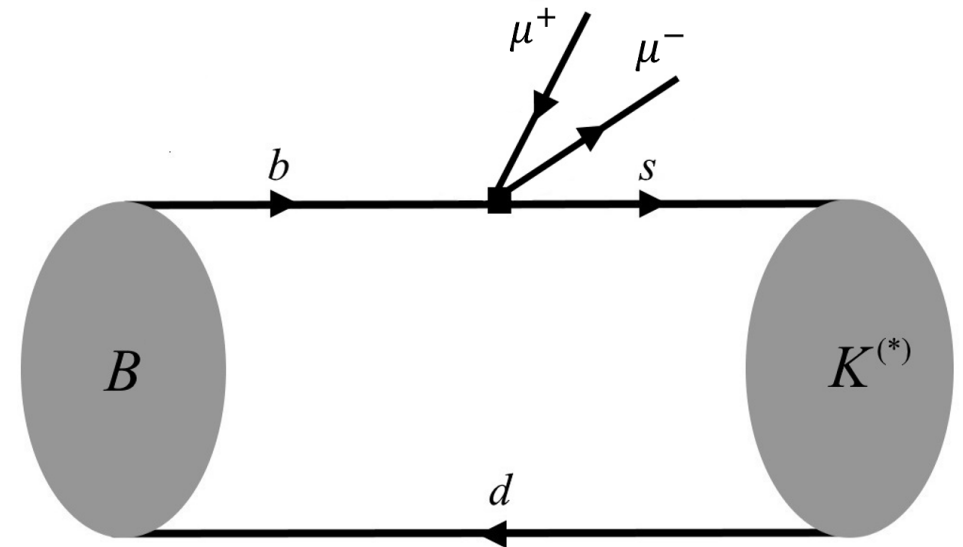
lepton flavour universality = the 3 lepton generations have the same couplings to the gauge bosons

violations of lepton flavour universality \Rightarrow new physics

observables to test LFU

$$R_K = \frac{\Gamma(B \rightarrow K \mu^+ \mu^-)}{\Gamma(B \rightarrow K e^+ e^-)}$$

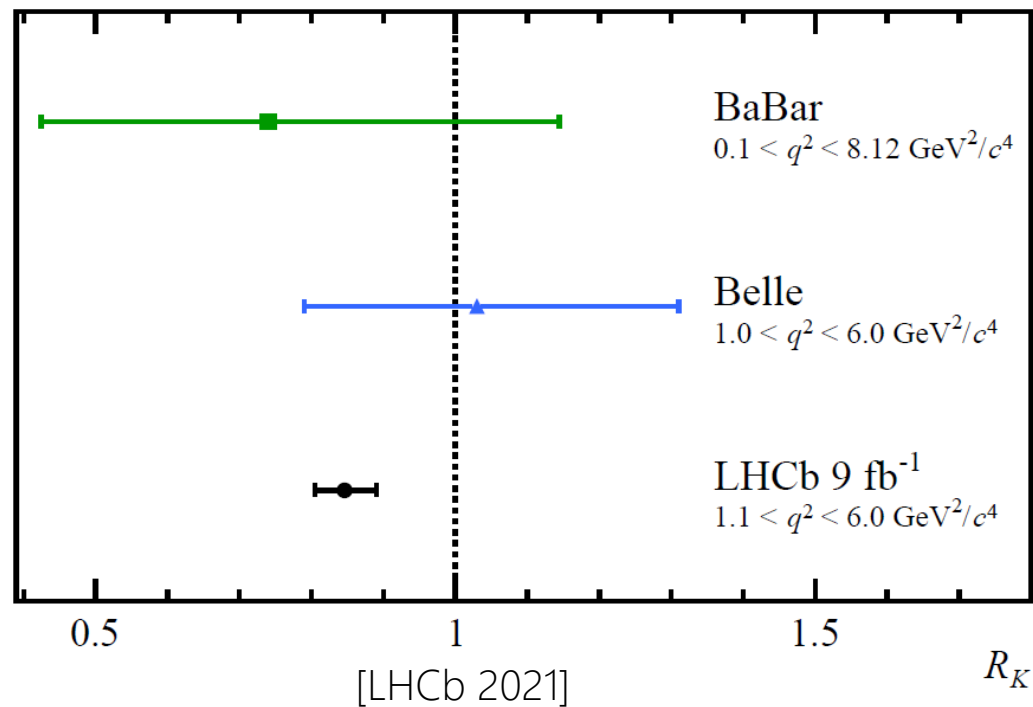
$$R_{K^*} = \frac{\Gamma(B \rightarrow K^* \mu^+ \mu^-)}{\Gamma(B \rightarrow K^* e^+ e^-)}$$



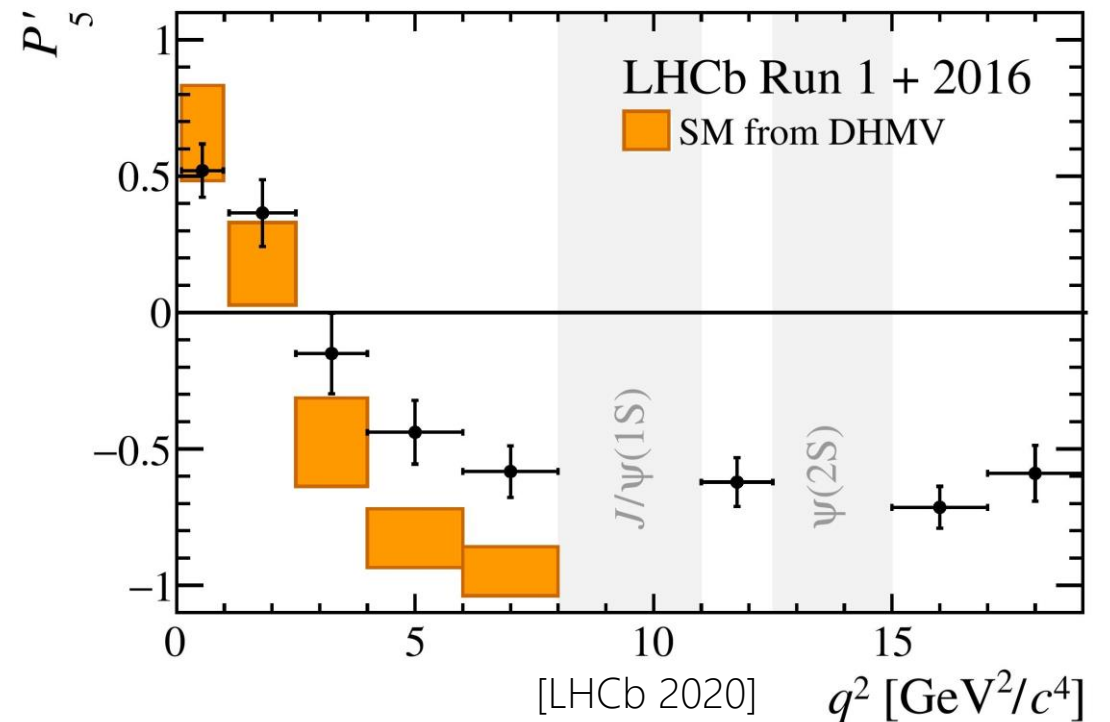
$b(\rightarrow s\ell^+\ell^-)$ anomalies

$b \rightarrow s\ell^+\ell^-$ anomalies = tension between experimental measurements and theoretical predictions in rare B -meson decays involving different observables ($R_K, R_{K^*}, P'_5, B_s \rightarrow \phi\mu^+\mu^-$, branching ratio, ...)

3.1 σ tension



$\sim 3\sigma$ tension



Theoretical framework

$b \rightarrow s \ell^+ \ell^-$ effective Hamiltonian

transitions described by the effective Hamiltonian

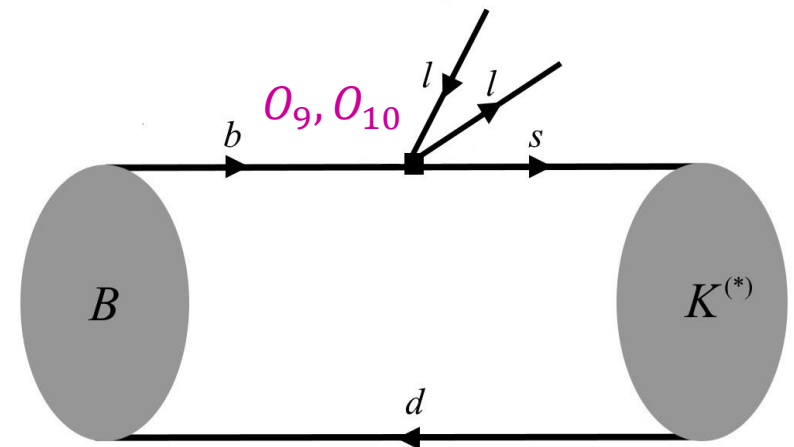
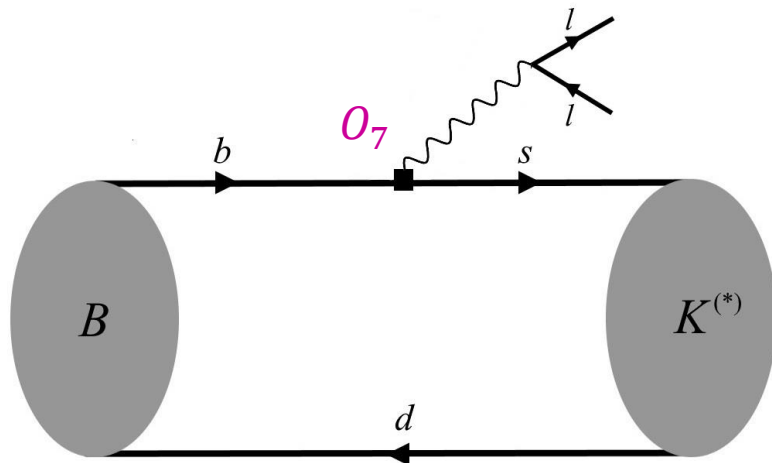
$$\mathcal{H}(b \rightarrow s \ell^+ \ell^-) = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_{i=1}^{10} C_i(\mu) O_i(\mu) \quad \mu = m_b$$

main contributions to $B_{(s)} \rightarrow \{K^{(*)}, \phi\} \ell^+ \ell^-$ in the SM given by local operators O_7, O_9, O_{10}

$$O_7 = \frac{e}{16\pi^2} m_b (\bar{s}_L \sigma^{\mu\nu} b_R) F_{\mu\nu}$$

$$O_9 = \frac{e^2}{16\pi^2} (\bar{s}_L \gamma^\mu b_L) \sum_\ell (\bar{\ell} \gamma_\mu \ell)$$

$$O_{10} = \frac{e^2}{16\pi^2} (\bar{s}_L \gamma^\mu b_L) \sum_\ell (\bar{\ell} \gamma_\mu \gamma_5 \ell)$$

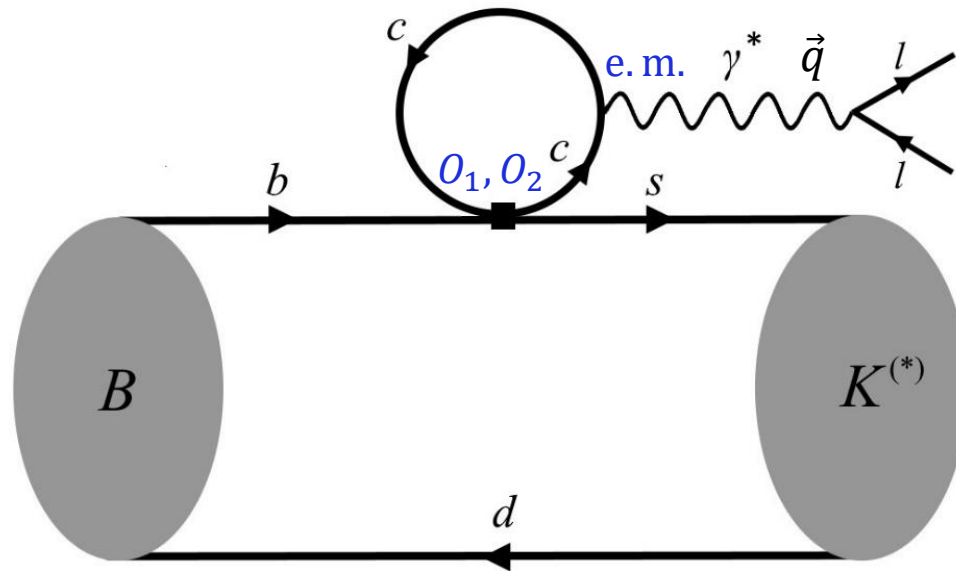


Charm loop in $B \rightarrow K^{(*)} \ell^+ \ell^-$

additional **non-local contributions** come from O_1^c and O_2^c combined with the **e.m.** current (charm-loop contribution)

$$O_1^c = (\bar{s}_L \gamma^\mu c_L)(\bar{c}_L \gamma_\mu b_L)$$

$$O_2^c = (\bar{s}_L^j \gamma^\mu c_L^i)(\bar{c}_L^i \gamma_\mu b_L^j)$$



Decay amplitude for $B \rightarrow K^{(*)} \ell^+ \ell^-$ decays

calculate decay amplitudes precisely to probe the SM

B -anomalies: NP or underestimated systematic uncertainties?

(analogous formulas apply to $B_s \rightarrow \phi \ell^+ \ell^-$ decays)

$$\mathcal{A}(B \rightarrow K^{(*)} \ell^+ \ell^-) = \mathcal{N} \left[(C_9 L_V^\mu + C_{10} L_A^\mu) \mathcal{F}_\mu - \frac{L_V^\mu}{q^2} (C_7 \mathcal{F}_{T,\mu} + \mathcal{H}_\mu) \right]$$

local hadronic matrix elements

$$\mathcal{F}_\mu = \langle K^{(*)}(k) | O_{7,9,10} | B(k+q) \rangle$$

non-local hadronic matrix elements

$$\mathcal{H}_\mu = i \int d^4x e^{iq \cdot x} \langle K^{(*)}(k) | T \{ j_\mu^{\text{em}}(x), (C_1 O_1^c + C_2 O_2^c)(0) \} | B(k+q) \rangle$$

Form factors definitions

form factors (FFs) parametrize hadronic matrix elements

FFs are functions of the momentum transfer squared q^2

local FFs

$$\mathcal{F}_\mu(k, q) = \sum_\lambda \mathcal{S}_\mu^\lambda(k, q) \mathcal{F}_\lambda(q^2)$$

computed with lattice QCD and sum rules with good precision $\sim 10\%$

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non-local FFs

$$\mathcal{H}_\mu(k, q) = \sum_\lambda \mathcal{S}_\mu^\lambda(k, q) \mathcal{H}_\lambda(q^2)$$

calculated using an **Operator Product Expansion (OPE)** or QCD factorization or ...
(variety of approaches, most of them model-dependent)

large uncertainties \rightarrow reduce uncertainties for a better understanding of rare B decays

Parametrization for \mathcal{F}_λ

obtain local FFs \mathcal{F}_λ in the whole semileptonic region by combining

- lattice QCD (**LQCD**) calculations at high q^2
- light-cone sum rule (**LCSR**) calculation at low q^2

Parametrization for \mathcal{F}_λ

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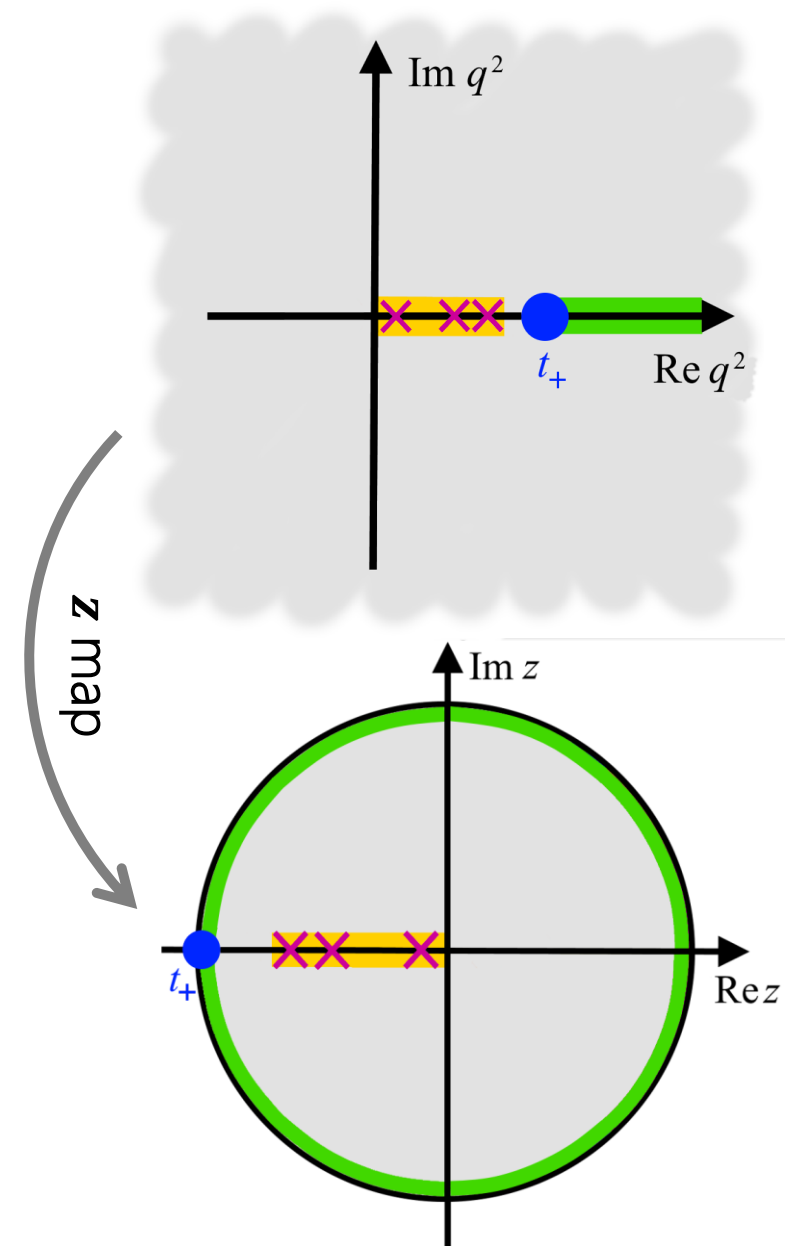
- lattice QCD (LQCD) calculations at high q^2
- light-cone sum rule (LCSR) calculation at low q^2

\mathcal{F}_λ analytic functions of q^2 (branch cut for $q^2 > t_+ = (M_B + M_{K^{(*)}})^2$)

fit results to a **z parametrization** (standard approach)

[Boyd/Grinstein/Lebed 1997]

$$\mathcal{F}_\lambda \propto \sum_{k=0}^{\infty} \alpha_k^{\mathcal{F}} z^k$$
$$z(q^2) = \frac{\sqrt{t_+ - q^2} - \sqrt{t_+}}{\sqrt{t_+ - q^2} + \sqrt{t_+}}$$



Calculation of \mathcal{H}_λ at negative q^2

compute the non-local FFs \mathcal{H}_λ using a light-cone OPE for $q^2 \ll 4m_c^2$ ($q^2 < 0$)

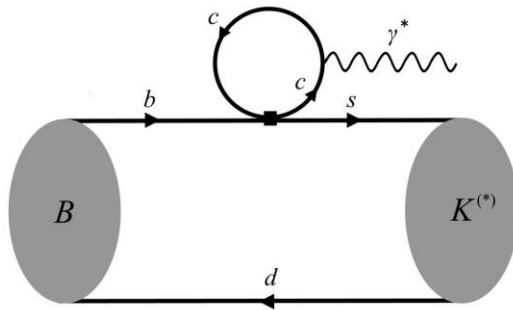
$$\mathcal{H}_\lambda(q^2) = C_\lambda(q^2)\mathcal{F}_\lambda(q^2) + \tilde{C}_\lambda(q^2)\mathcal{V}_\lambda(q^2) + \dots$$

Calculation of \mathcal{H}_λ at negative q^2

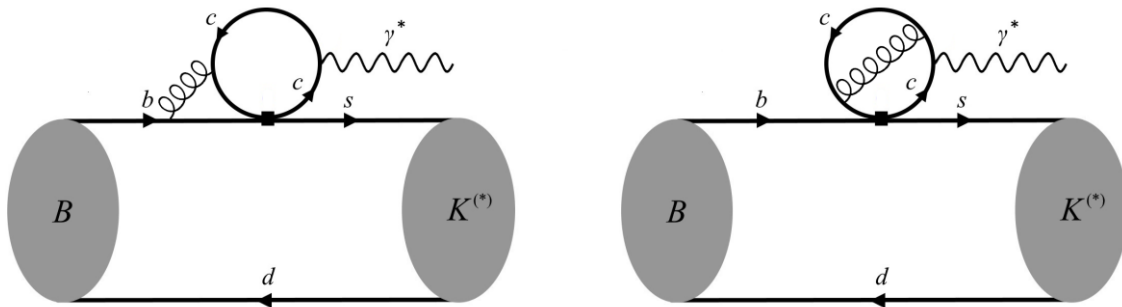
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leading power (LO in α_s)



+ hard gluons (α_s) corrections

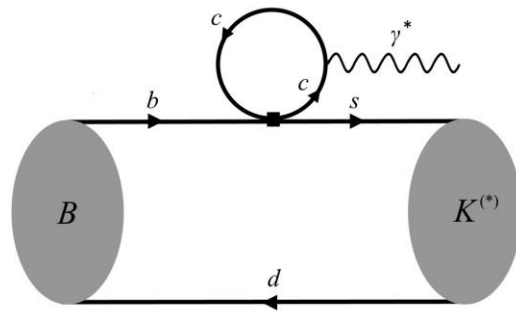


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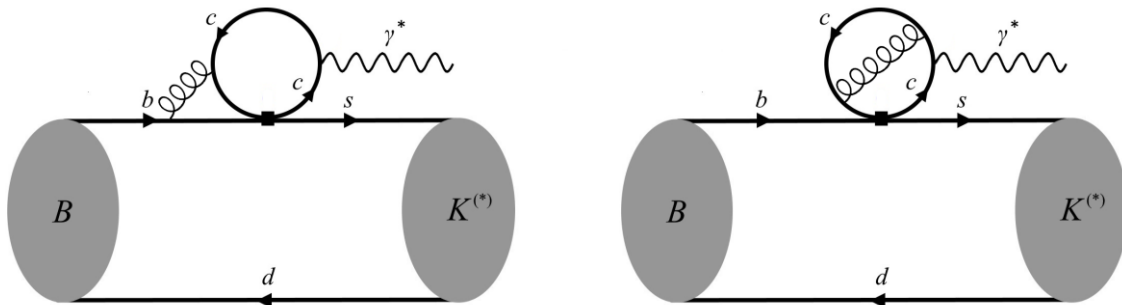
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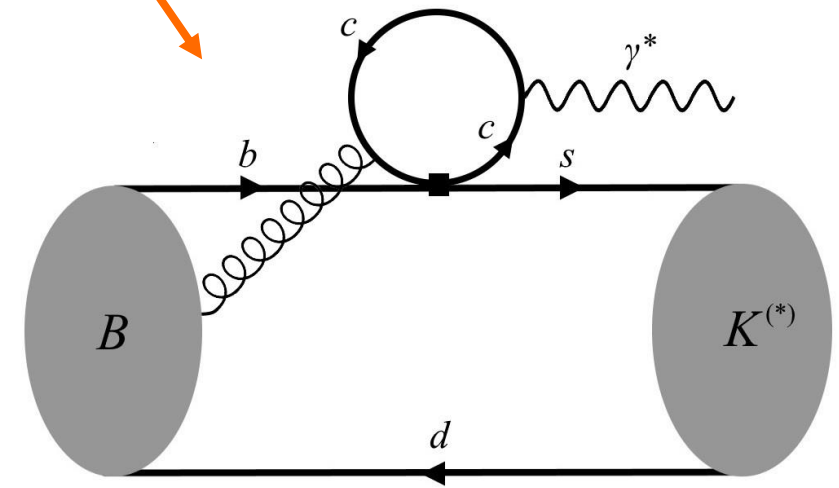
leading power (LO in α_s)



+ hard gluons (α_s) corrections



soft gluon correction
non-perturbative
 \Rightarrow not α_s suppressed



NLP of the light-cone OPE

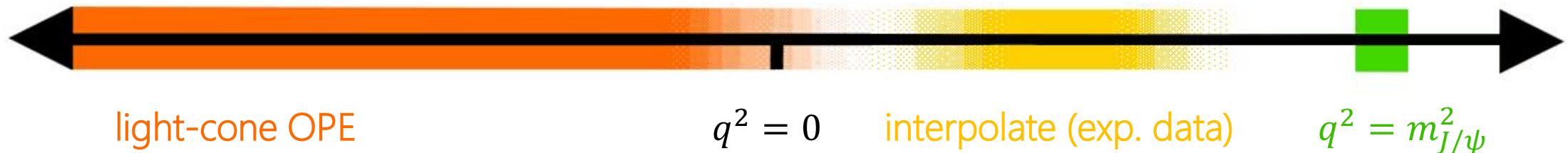
$\Delta\mathcal{C}_9(q^2 = 1 \text{ GeV}^2)$		KMPW2010	GvDV2020
leading power (LO α_s)		0.27	0.27
$B \rightarrow K\ell\ell$	\mathcal{V}_A	$-0.09^{+0.06}_{-0.07}$	$(1.9^{+0.6}_{-0.6}) \cdot 10^{-4}$
$B \rightarrow K^*\ell\ell$	\mathcal{V}_1	$0.6^{+0.7}_{-0.5}$	$(1.2^{+0.4}_{-0.4}) \cdot 10^{-3}$
	\mathcal{V}_2	$0.6^{+0.7}_{-0.5}$	$(2.1^{+0.7}_{-0.7}) \cdot 10^{-3}$
	\mathcal{V}_3	$1.0^{+1.6}_{-0.8}$	$(3.0^{+1.0}_{-1.0}) \cdot 10^{-3}$
$B_s \rightarrow \phi\ell\ell$	\mathcal{V}_i	—	see paper

- results represented as a q^2 dependent correction to \mathcal{C}_9
- we can reproduce the analytical results given in KMWP2010
- our results are **two orders of magnitude smaller** than in KMWP2010 (\Rightarrow smaller unc.)
- quick convergence of the light-cone OPE

Obtaining theoretical predictions for \mathcal{H}_λ

1. extract \mathcal{H}_λ at $q^2 = m_{J/\psi}^2$ from $B \rightarrow K^{(*)}J/\psi$ and $B_s \rightarrow \phi J/\psi$ measurements (no local contribution)
2. **interpolate** the OPE calculation at **negative q^2** and the experimental results at $q^2 = m_{J/\psi}^2$ to obtain \mathcal{H}_λ for $q^2 < m_{J/\psi}^2$
3. **new approach** to obtain theoretical predictions in the **low q^2 ($0 < q^2 < 8 \text{ GeV}^2$)** region \Rightarrow compare with experimental data

need a parametrization to interpolate \mathcal{H}_λ : which is the optimal parametrization?



Parametrizations for \mathcal{H}_λ

- q^2 parametrization [Jäger/Camalich 2012, Ciuchini et al. 2015]

$$\mathcal{H}_\lambda(q^2) = \mathcal{H}_\lambda^{\text{QCDF}}(q^2) + \mathcal{H}_\lambda^{\text{rest}}(0) + \frac{q^2}{M_B^2} \mathcal{H}_\lambda^{\text{rest},'}(0) + \frac{(q^2)^2}{M_B^4} \mathcal{H}_\lambda^{\text{rest},''}(0) + \dots$$

- dispersion relation [Khodjamirian et al. 2010]

$$\mathcal{H}_\lambda(q^2) = \mathcal{H}_\lambda(0) + \sum_{\psi=J/\psi, \psi(2S)} \frac{f_\psi \mathcal{A}_\psi}{M_\psi^2 (M_\psi^2 - q^2)} + \int_{4M_D^2}^{\infty} dt \frac{\rho(t)}{t(t - q^2)}$$

- z expansion [Bobeth/Chrzaszcz/van Dyk/Virto 2017]

$$\mathcal{H}_\lambda(z) = \sum_{n=0}^{\infty} c_n z^n$$

- we propose a new parametrization (\hat{z} polynomials) [NG/van Dyk/Virto 2020]

$$\hat{\mathcal{H}}_\lambda(\hat{z}) = \sum_{n=0}^{\infty} \beta_n p_n(\hat{z})$$

Derivation of the dispersive bound

define the correlator

$$\Pi(k, q) = i \int d^4x e^{ikx} \langle 0 | T \{ \mathcal{O}^\mu(x), \mathcal{O}_\mu(y) \} | 0 \rangle$$

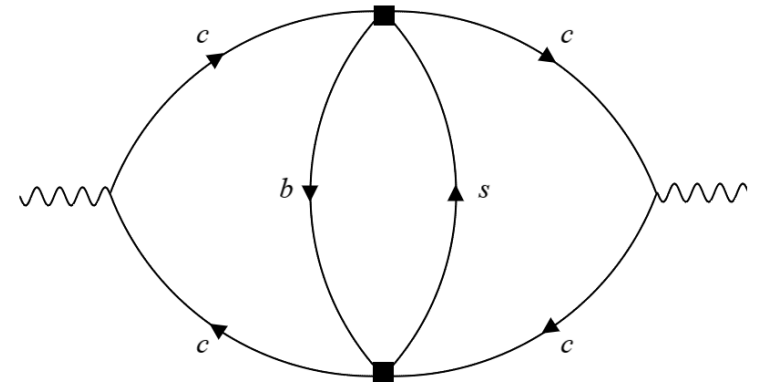
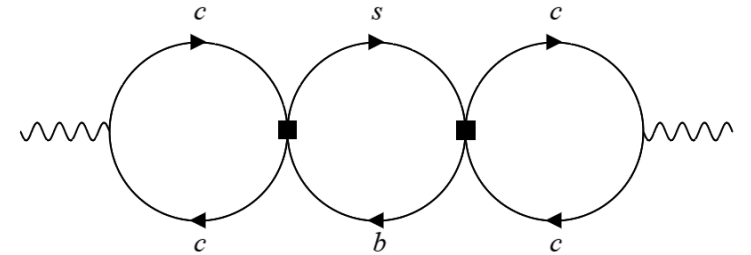
where

$$\mathcal{O}_\mu \propto \int d^4x e^{iq \cdot x} T \{ j_\mu^{em}(x), (C_1 \mathcal{O}_1^c + C_2 \mathcal{O}_2^c)(0) \}$$

use a subtracted dispersion relation

$$\chi(q^2) \propto \int_{(M_B + M_K)^2}^{\infty} ds \frac{\text{Disc}_{bs} \Pi(s)}{(q^2 - s)^3}$$

calculate $\chi(q^2)$ perturbatively and $\text{Disc}_{bs} \Pi(q^2)$ using unitarity



Dispersive bound

using unitarity and dispersion relation, we obtain a constraint on the non-local form factors \mathcal{H}_λ

dispersive bound

$$1 > \int_{(M_B+M_K)^2}^{\infty} ds |\phi^{B \rightarrow K}(z)|^2 |\mathcal{H}^{B \rightarrow K}(s)|^2 + B \rightarrow K^* \text{ and } B_S \rightarrow \phi \text{ contr.}$$

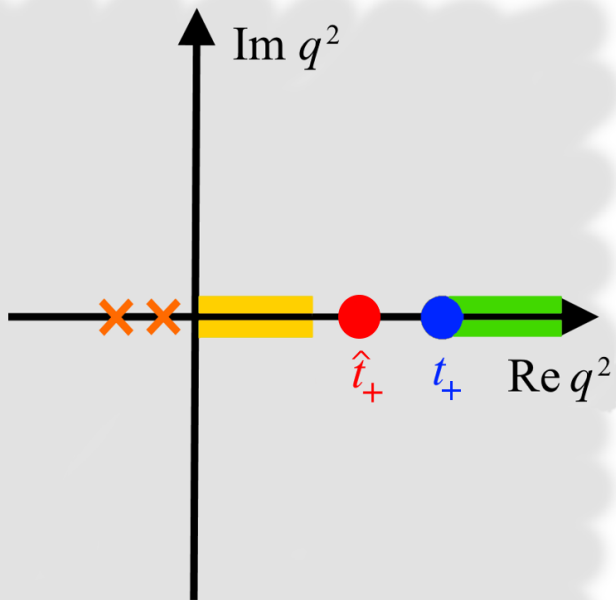
- first dispersive bound for $\mathcal{H}^{B \rightarrow K}$, $\mathcal{H}_\lambda^{B \rightarrow K^*}$, $\mathcal{H}_\lambda^{B_S \rightarrow \phi}$
- model independent constraint
- strengthen the bound by adding additional contributions (baryons)

Exploit the dispersive bound

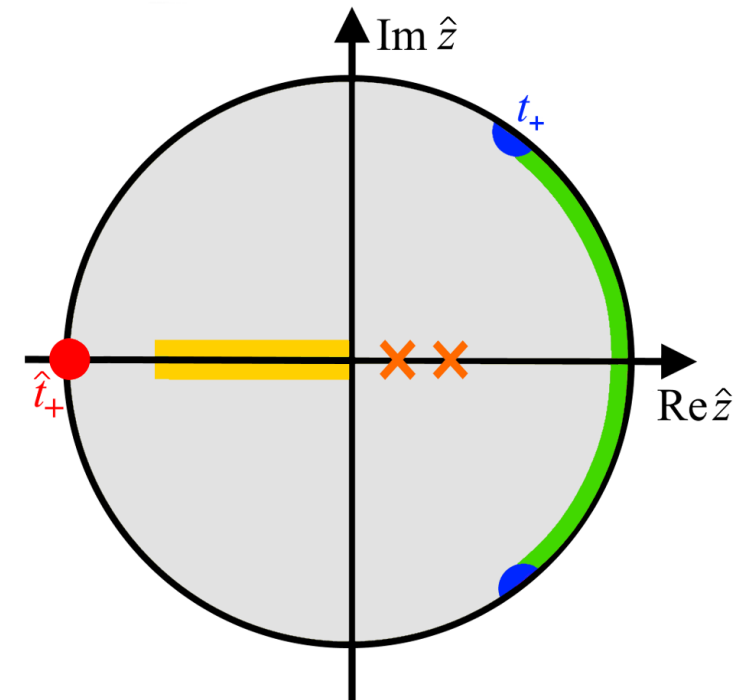
\mathcal{H}_λ has a branch cut for $q^2 > \hat{t}_+ = 4M_D^2$ — note that $\hat{t}_+ \neq t_+ \equiv (M_B + M_{K^{(*)}})^2$

define the \hat{z} mapping

$$\hat{z}(q^2) = \frac{\sqrt{\hat{t}_+ - q^2} - \sqrt{\hat{t}_+}}{\sqrt{\hat{t}_+ - q^2} + \sqrt{\hat{t}_+}}$$



q^2 plane
real axis $q^2 > \hat{t}_+$ \Rightarrow \hat{z} plane
arc of unit circle



Exploit the dispersive bound

$$1 > \int_{(M_B+M_K)^2}^{\infty} ds |\phi^{B \rightarrow K}(s)|^2 |\mathcal{H}^{B \rightarrow K}(s)|^2 + B \rightarrow K^* \text{ and } B_S \rightarrow \phi \text{ contr.}$$

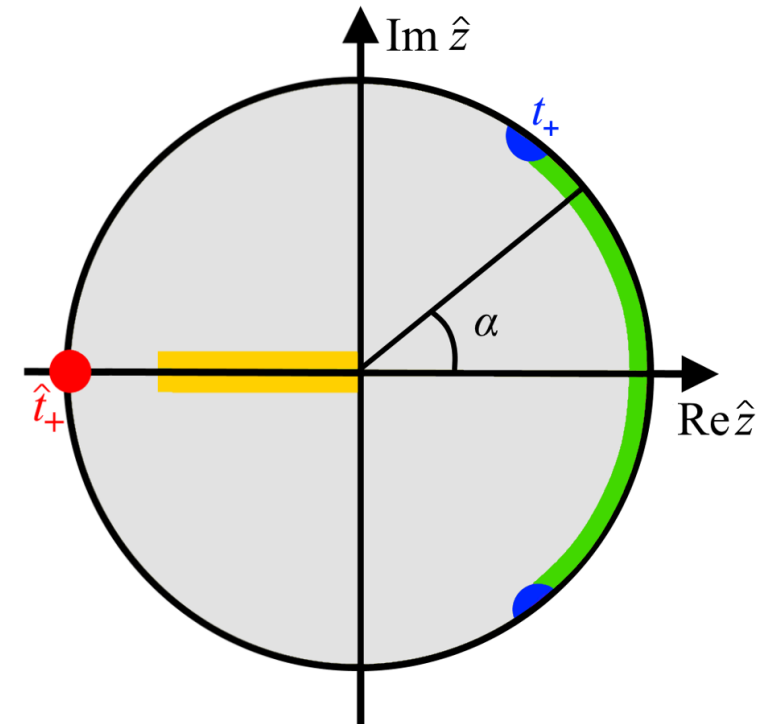
apply the \hat{z} mapping

$$1 > \int_{-\alpha_{BK}}^{+\alpha_{BK}} d\alpha \sum_{\lambda} |\hat{\mathcal{H}}^{B \rightarrow K}(\hat{z})|^2 + B \rightarrow K^* \text{ and } B_S \rightarrow \phi \text{ contr.}$$

where $\hat{z} = e^{i\alpha}$ and

$$\hat{\mathcal{H}}^{B \rightarrow K}(\hat{z}) = \mathcal{P}(\hat{z}) \phi^{B \rightarrow K}(\hat{z}) \mathcal{H}_{\lambda}^{B \rightarrow K}(\hat{z})$$

Blaschke factor \mathcal{P} , outer function $\phi^{B \rightarrow K}$



$\hat{\mathcal{H}}_\lambda$ parametrization

$$1 > \int_{-\alpha_{BK}}^{+\alpha_{BK}} d\alpha |\hat{\mathcal{H}}^{B \rightarrow K}(\hat{z})|^2 + B \rightarrow K^* \text{ and } B_S \rightarrow \phi \text{ contr.}$$

expand $\hat{\mathcal{H}}_\lambda$ in orthogonal polynomials $p_n(\hat{z})$

$$\hat{\mathcal{H}}(\hat{z}) = \sum_{n=0}^{\infty} \beta_n p_n(\hat{z})$$

now the dispersive bound reads

$$1 > \sum_{n=0}^{\infty} |\beta_n^{B \rightarrow K}|^2 + \sum_{\lambda} \left(2 \sum_{n=0}^{\infty} |\beta_{\lambda,n}^{B \rightarrow K^*}|^2 + \sum_{n=0}^{\infty} |\beta_{\lambda,n}^{B_S \rightarrow \phi}|^2 \right)$$

no bound for the \hat{z} monomials
(coefficient of the Taylor expansion)

$$p_0^{B \rightarrow K}(\hat{z}) = \frac{1}{\sqrt{2\alpha_{BK}}}$$

$$p_1^{B \rightarrow K}(\hat{z}) = \left(\hat{z} - \frac{\sin(\alpha_{BK})}{\alpha_{BK}} \right) \sqrt{\frac{\alpha_{BK}}{2\alpha_{BK}^2 + \cos(2\alpha_{BK}) - 1}}$$

$$p_2^{B \rightarrow K}(\hat{z}) = \left(\hat{z}^2 + \frac{\sin(\alpha_{BK})(\sin(2\alpha_{BK}) - 2\alpha_{BK})}{2\alpha_{BK}^2 + \cos(2\alpha_{BK}) - 1} \hat{z} + \frac{2 \sin^2(\alpha_{BK})}{2\alpha_{BK}^2 + \cos(2\alpha_{BK}) - 1} \right) \sqrt{\frac{\alpha_{BK}}{2\alpha_{BK}^2 + \cos(2\alpha_{BK}) - 1}}$$

$$p_3^{B \rightarrow K}(\hat{z}) = \dots$$

Theoretical predictions

Local form factors predictions

$$\mathcal{A}(B \rightarrow K^{(*)}\ell^+\ell^-) = \mathcal{N} \left[(C_9 L_V^\mu + C_{10} L_A^\mu) \mathcal{F}_\mu - \frac{L_V^\mu}{q^2} (C_7 \mathcal{F}_{T,\mu} + \mathcal{H}_\mu) \right]$$

obtain numerical results for the local FFs

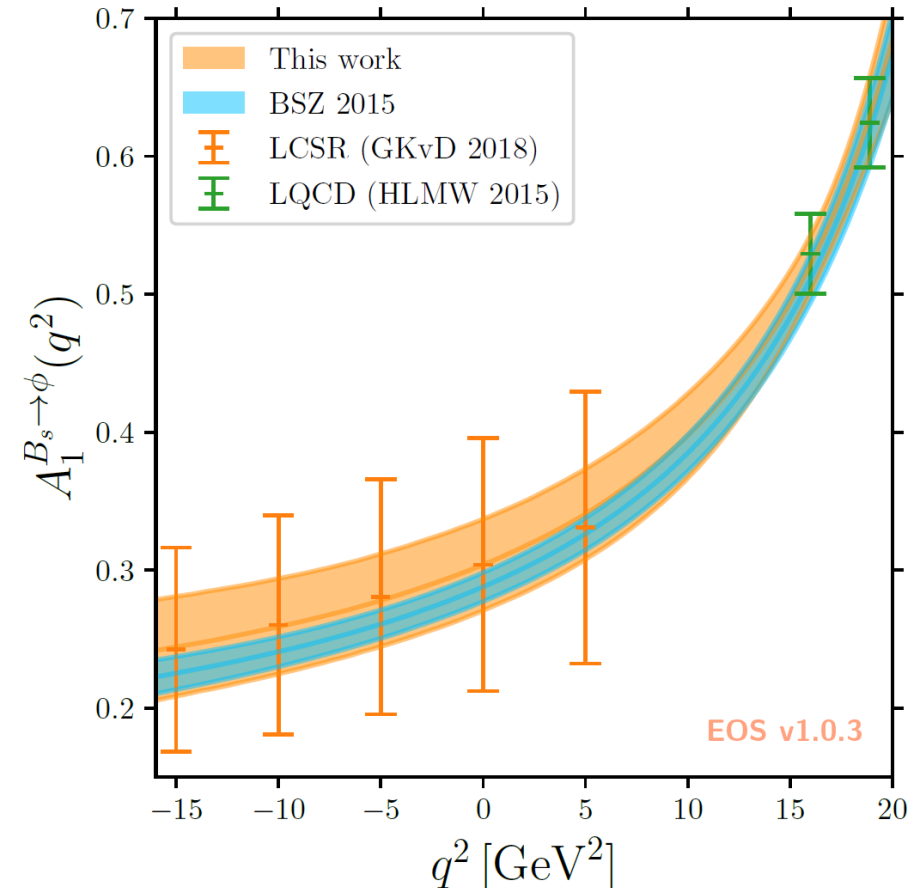
$$\mathcal{F}_\lambda \cong \mathcal{P} \sum_{k=0}^3 \alpha_k^{\mathcal{F}} z^k$$

for $B \rightarrow K^{(*)}\ell^+\ell^-$ and $B_s \rightarrow \phi\ell^+\ell^-$ fit the \mathbf{z} parametrization to

- LQCD calculations at high q^2
[FLAG review 2021] [Horgan et al. 2013][Horgan et al. 2015]
- LCSR calculation at low q^2
[Khodjamirian/Rusov 2017] [NG/Kokulu/van Dyk 2018]
[NG/van Dyk/Virto 2020]

large p values

results given in machine readable files



Non-local form factors predictions

$$\mathcal{A}(B \rightarrow K^{(*)} \ell \ell) = \mathcal{N} \left[(C_9 L_V^\mu + C_{10} L_A^\mu) \mathcal{F}_\mu - \frac{L_V^\mu}{q^2} (C_7 \mathcal{F}_{T,\mu} + \mathcal{H}_\mu) \right]$$

obtain numerical results for the non-local FFs \mathcal{H}_λ

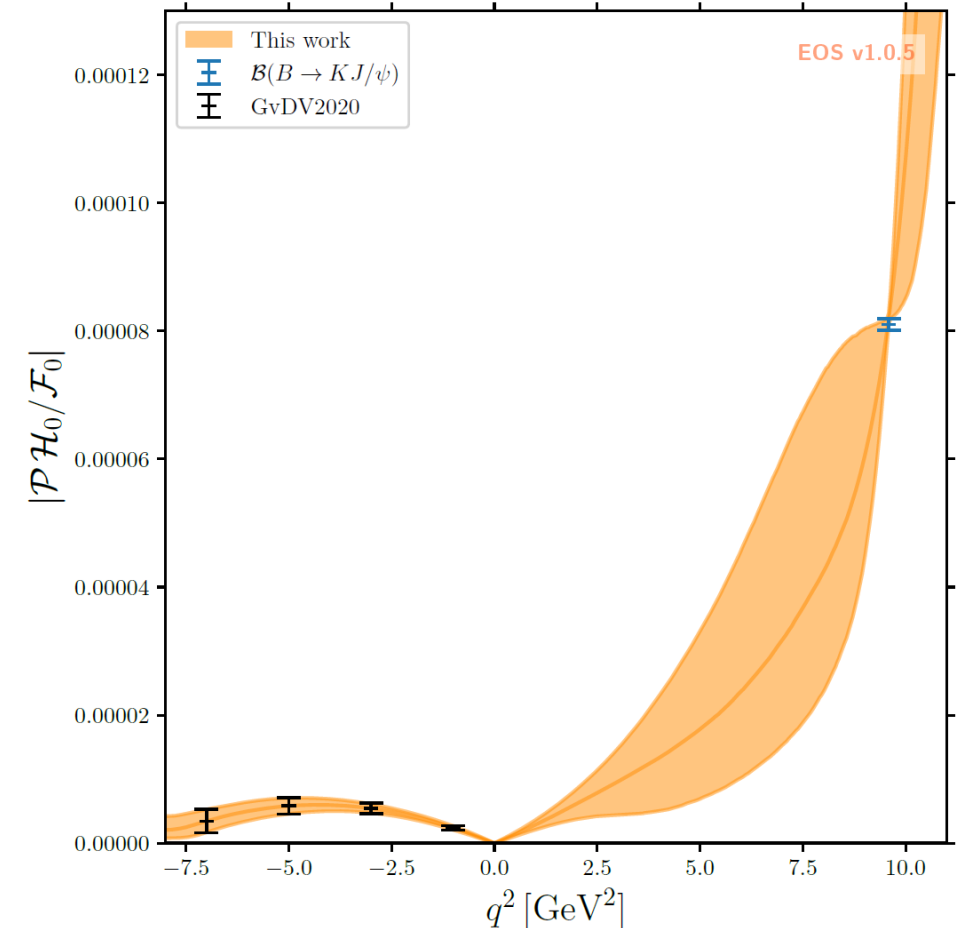
$$\hat{\mathcal{H}}_\lambda \cong \sum_{n=0}^5 \beta_n p_n(\hat{z})$$

fit the \hat{z} parametrization

- light-cone OPE calculation at **negative q^2**
 $\mathcal{H}_\lambda(q^2) = C_\lambda(q^2) \mathcal{F}_\lambda(q^2) + \tilde{C}_\lambda(q^2) \mathcal{V}_\lambda(q^2) + \dots$
- $B \rightarrow K^{(*)} J/\psi$ and $B_s \rightarrow \phi J/\psi$ measurements at $q^2 = m_{J/\psi}^2$
- dispersive bound

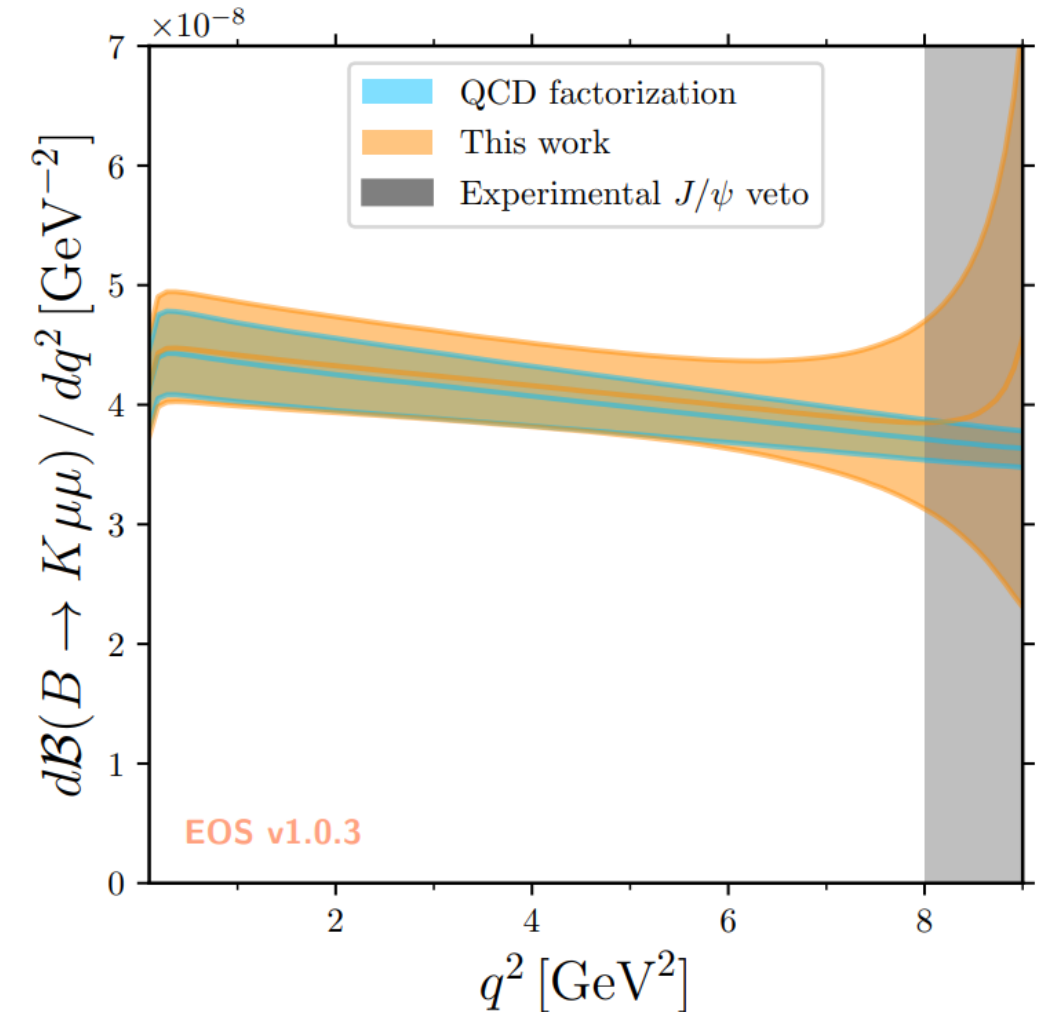
all p values > 11%

results given in machine readable files



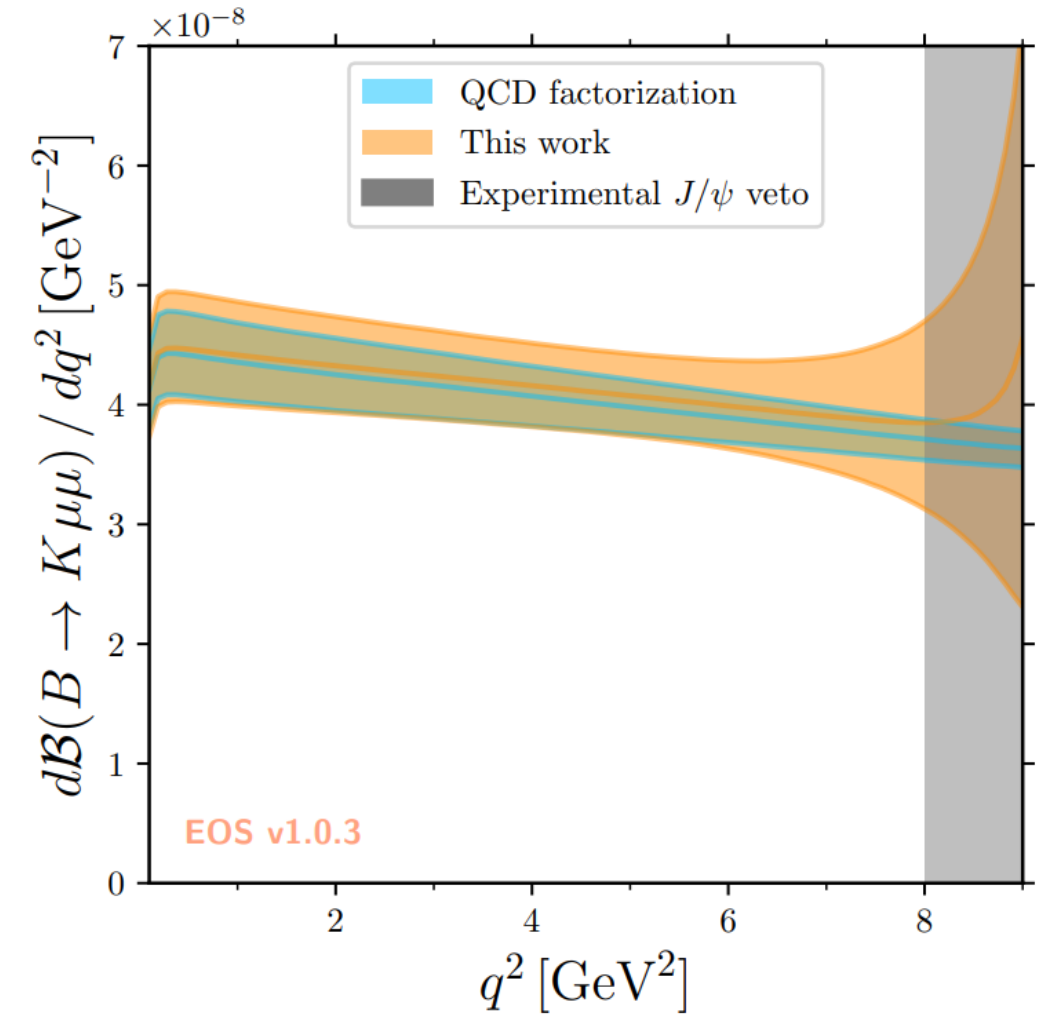
using our local and non-local FFs values
we predict branching ratios and angular observables in
 $B \rightarrow K\mu^+\mu^-$, $B \rightarrow K^*\mu^+\mu^-$, and $B_s \rightarrow \phi\mu^+\mu^-$ in the SM

- we do not use QCD factorization (QCDF) like all previous SM predictions (non-quantifiable systematic uncertainty)
- first predictions using dispersive bounds (control the truncation errors)
- systematically improvable approach (more precise form factor results, saturate the bound,...)



Comparison with QCD factorization

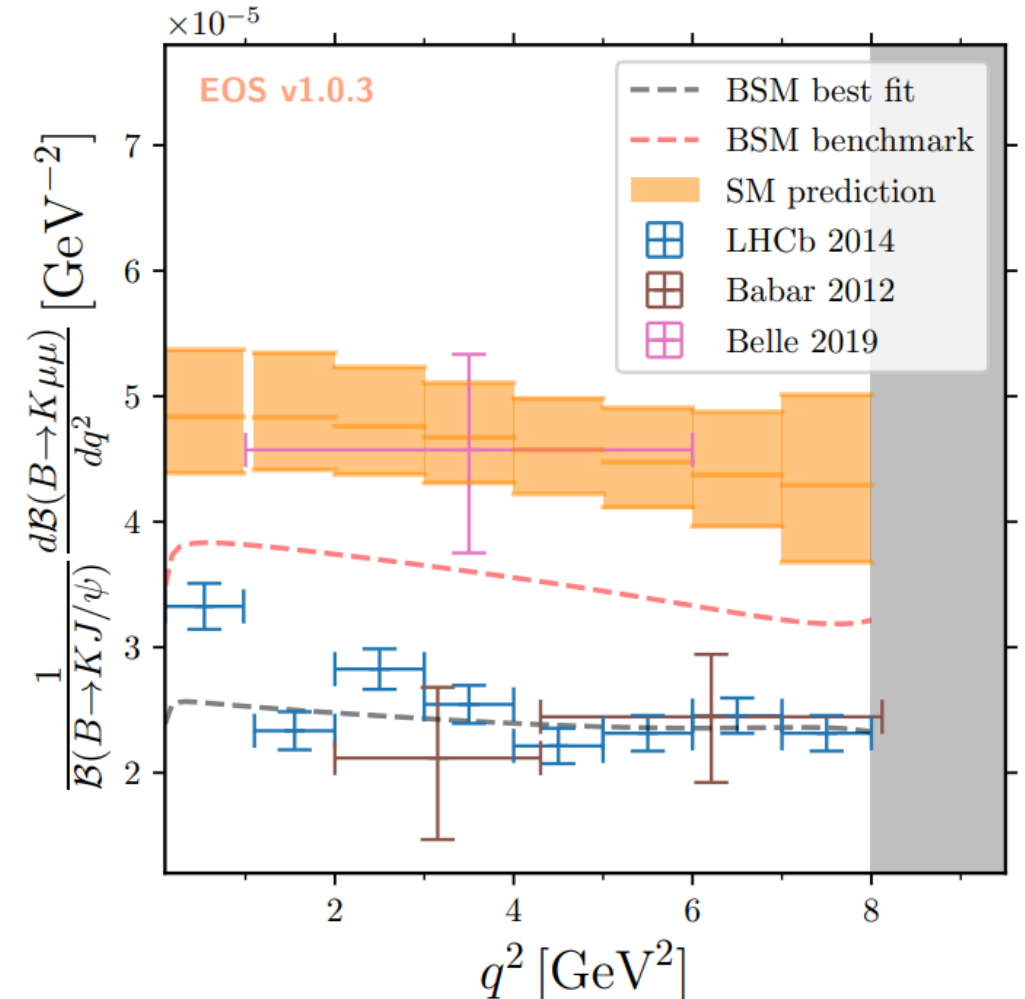
- plot produced with same FFs inputs
- **central values** in excellent **agreement** but **smaller uncertainties** in QCDF (systematic unc. not considered)
- **same shape** (also in $B \rightarrow K^* \mu^+ \mu^-$, deviation found in $B_s \rightarrow \phi \mu^+ \mu^-$)
- **no increasing uncertainty** at the J/ψ pole in QCDF (charm-loop treated perturbatively)



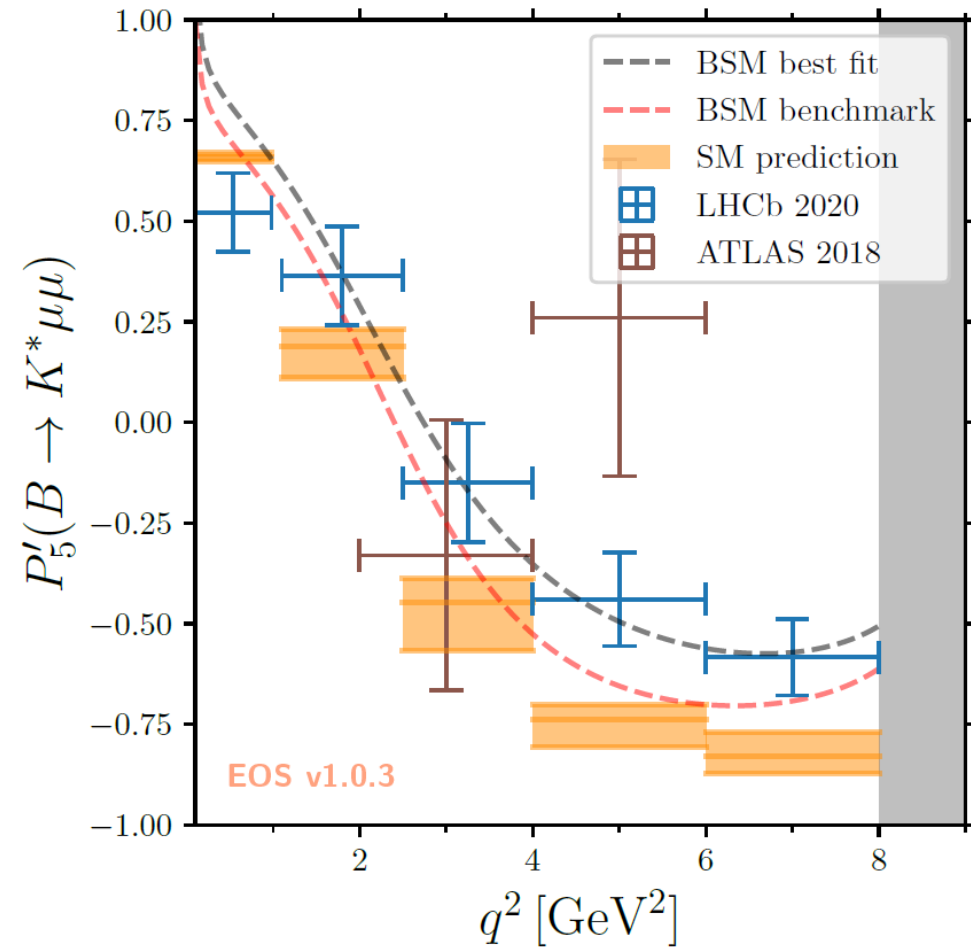
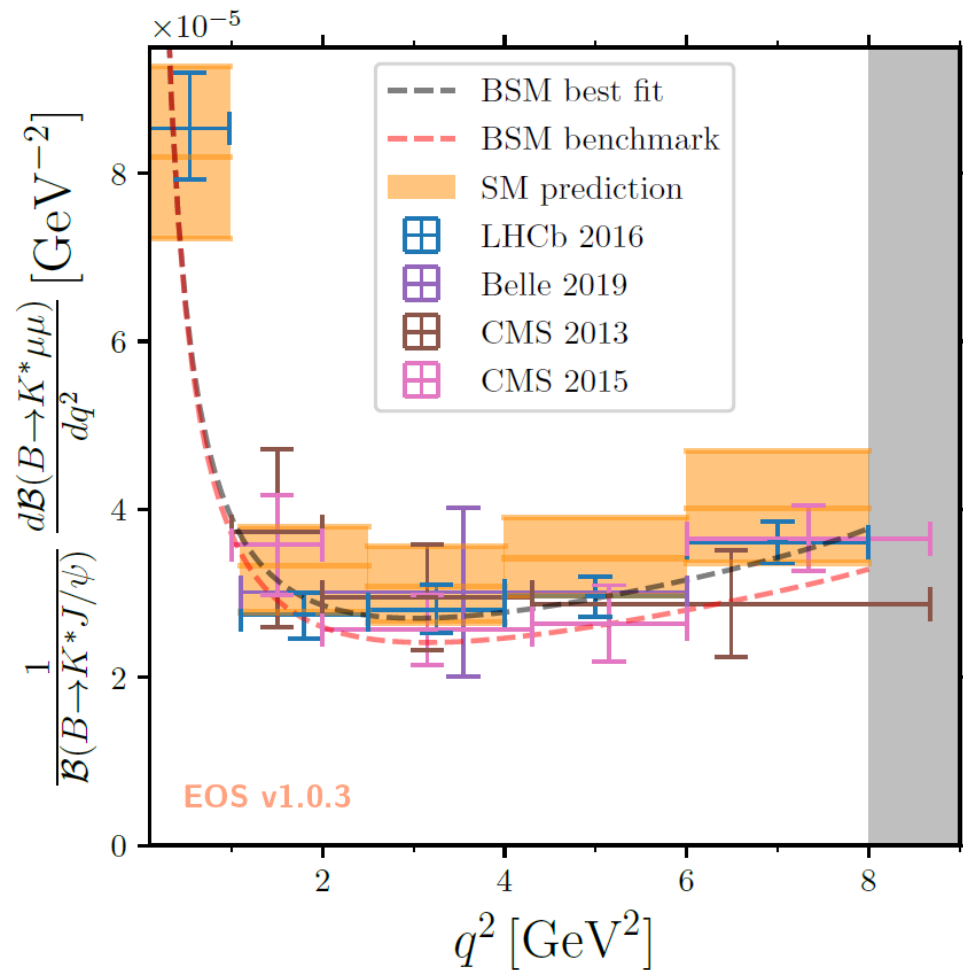
Confrontation with data

Comparison with measurements for $B \rightarrow K \mu^+ \mu^-$ 23

- "BSM best fit" \rightarrow best fit point of our BSM fit (see next slides)
- "BSM benchmark" \rightarrow set $C_9^{\text{NP}\mu} = -C_{10}^{\text{NP}\mu} = -0.5$
- **sizable tension** between SM predictions and experimental results
- tension larger than in other works in the literature \rightarrow inputs for the local FFs \mathcal{F}_λ
- results consistent with the deviations found in R_K



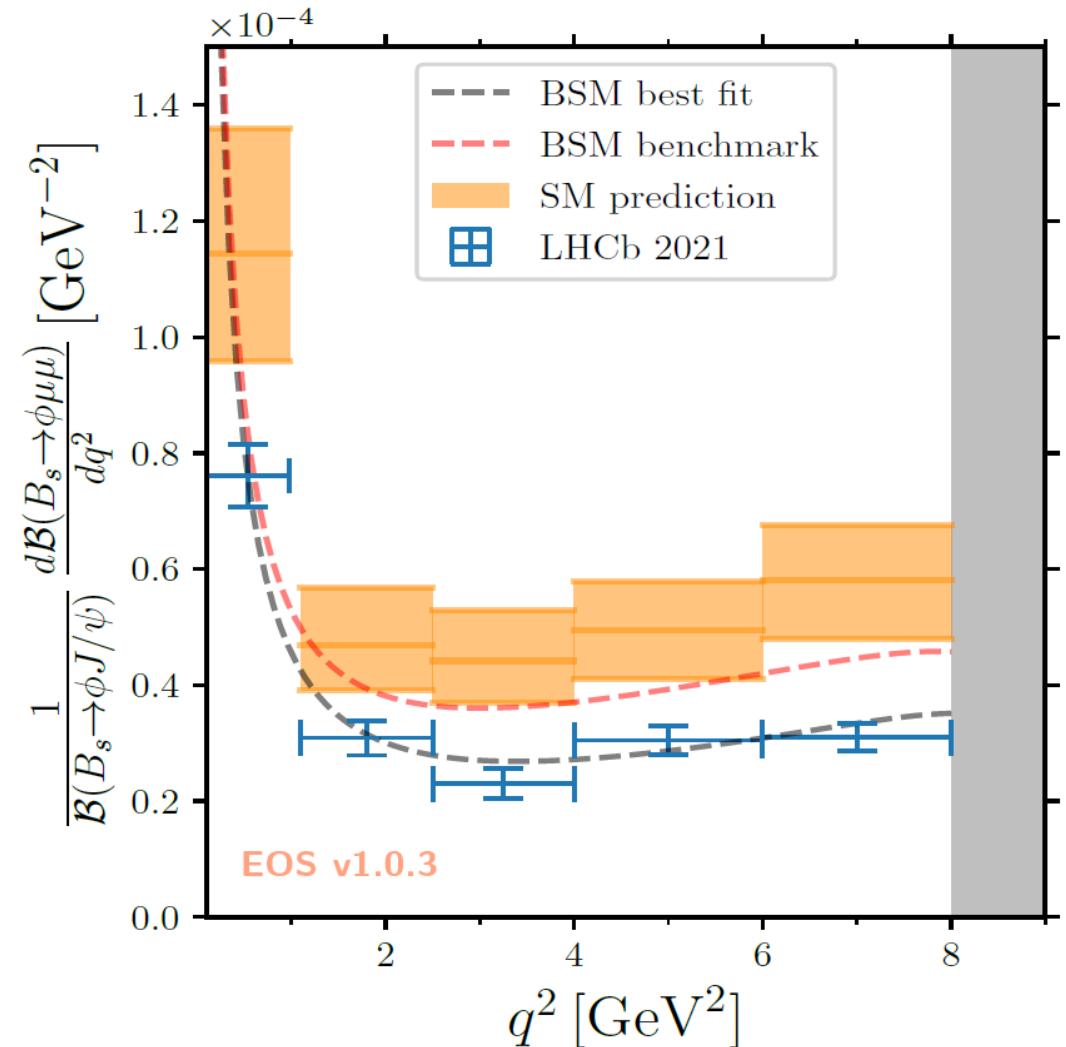
Comparison with measurements for $B \rightarrow K^* \mu^+ \mu^-$ 24



tension **smaller** than in other works in the literature \rightarrow inputs for the local FFs \mathcal{F}_λ

Comparison with measurements for $B_s \rightarrow \phi \mu^+ \mu^-$ 25

- consistent picture with the deviations in $B \rightarrow K \mu^+ \mu^-$, $B \rightarrow K^* \mu^+ \mu^-$
- choice of theory inputs (local FFs \mathcal{F}_λ) is decisive \rightarrow usage of light-meson LCSR rather than B -meson LCSR yields much larger tension w.r.t. data
- precise LQCD calculations at low q^2 essential to have more reliable theoretical predictions (already available for $B \rightarrow K \ell^+ \ell^-$ [HPQCD 2022])
- expect deviation in R_ϕ measurement (not measured yet)



Global fit to $b \rightarrow s\mu^+\mu^-$ (setup)

use our predictions for the local and non-local FFs as priors

fit the Wilson coefficients $C_9^{\text{NP}\mu}$ and $C_{10}^{\text{NP}\mu}$ to the available experimental measurements in $b \rightarrow s\mu^+\mu^-$ transitions
($C_{9,10} = C_{9,10}^{\text{SM}} + C_{9,10}^{\text{NP}\mu}$)

we perform **three fits**, one for each set of the following set of experimental measurements:
(BRs, angular observables, binned and not binned)

- $B \rightarrow K\mu^+\mu^- + B_s \rightarrow \mu^+\mu^-$
- $B \rightarrow K^*\mu^+\mu^-$
- $B_s \rightarrow \phi\mu^+\mu^-$

combined fit would be very challenging \rightarrow **130 nuisance parameter**

Global fit to $b \rightarrow s\mu^+\mu^-$ (results)

we obtain good fits, agreement between the three fits

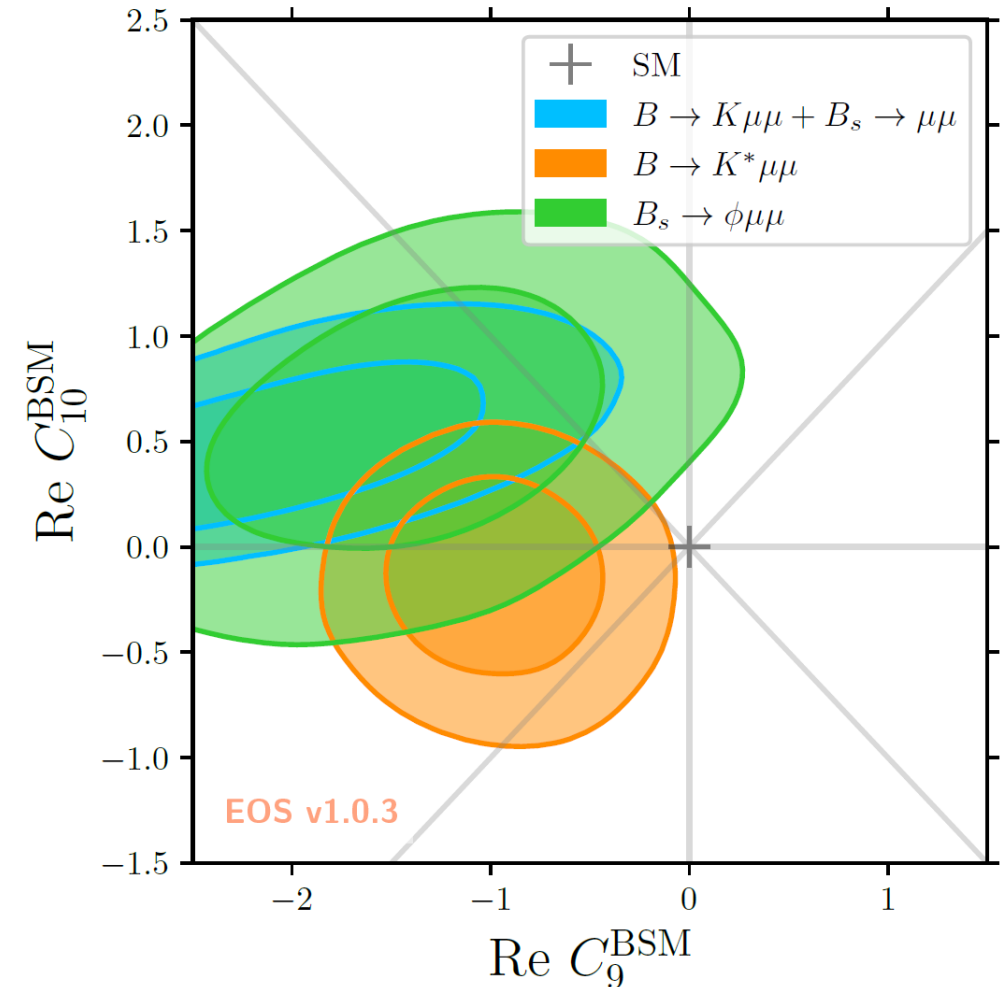
substantial tension w.r.t. SM (in agreement with the literature)

pulls (p value of the SM hypothesis):

- 5.7σ for $B \rightarrow K\mu^+\mu^- + B_s \rightarrow \mu^+\mu^-$
- 2.7σ for $B \rightarrow K^*\mu^+\mu^-$
- 2.6σ for $B_s \rightarrow \phi\mu^+\mu^-$

local FFs \mathcal{F}_λ main uncertainties

non-local FFs \mathcal{H}_λ cannot explain this tension



Summary and outlook

Summary

1. **new theoretical predictions** using our calculation for the non-local form factors \mathcal{H}_λ at $q^2 < 0$, experimental data for $B \rightarrow K^{(*)}J/\psi$, and a dispersive bound

dispersive bound allows to control truncation error

new approach — \mathcal{H}_λ uncertainties can be systematically reduced

predictions improvable with more precise local form factors \mathcal{F}_λ results (new lattice QCD results), saturating the dispersive bound, ...

2. fit the Wilson coefficients $C_9^{\text{NP}\mu}$ and $C_{10}^{\text{NP}\mu}$ using the available experimental data

good fit to the data, corroborate **substantial tension w.r.t. SM** (in agreement with the literature)
 \Rightarrow **coherent BSM explanation**

FFs predictions

- **dispersive analysis** of the local FFs
- include $\Lambda_b \rightarrow \Lambda \ell^+ \ell^-$ **decays** to further constrain the non-local FFs
- use $B \rightarrow K^{(*)} \psi(2S)$ and $B_s \rightarrow \phi \psi(2S)$ measurements

Global analysis

- perform a **simultaneous** analysis of the three decay modes
- include the LFU ratios $R_K^{(*)}$ (and R_ϕ) in the global fit
- include $\Lambda_b \rightarrow \Lambda \ell^+ \ell^-$ **decays** to further constrain the Wilson coefficients

Thank you!