



**SISSA**



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# Enlightening Cold Dark Matter's darkest sides (via non-minimal coupling)

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# Outline

**PhD PROJECT:** Testing and developing a model in which Cold Dark Matter is dynamically non-minimally coupled with gravity

## Reference papers:

**Self-gravitating Equilibria of Non-minimally Coupled Dark Matter Halos**

GIOVANNI GANDOLFI,<sup>1,2</sup> ANDREA LAPI,<sup>1,2,3,4</sup> AND STEFANO LIBERATI<sup>1,2,3</sup>

Gandolfi+21 - ApJ 910 76

**Empirical Evidence of Non-Minimally Coupled Dark Matter in the Dynamics of Local Spiral Galaxies?**

GIOVANNI GANDOLFI <sup>1,2</sup> ANDREA LAPI <sup>1,2,3,4</sup> AND STEFANO LIBERATI <sup>1,2,4</sup>

Gandolfi+22a - ApJ 929 48

Gandolfi+22b - in prep.

Introduction + motivation

Theoretical remarks

Results

Conclusion

# Motivation

Cold Dark Matter (**CDM**): a story of great successes and issues.

## ISSUE 1: the Core-Cusp problem

**CUSPY** profiles

(e.g. Navarro-Frenk-White, NFW)

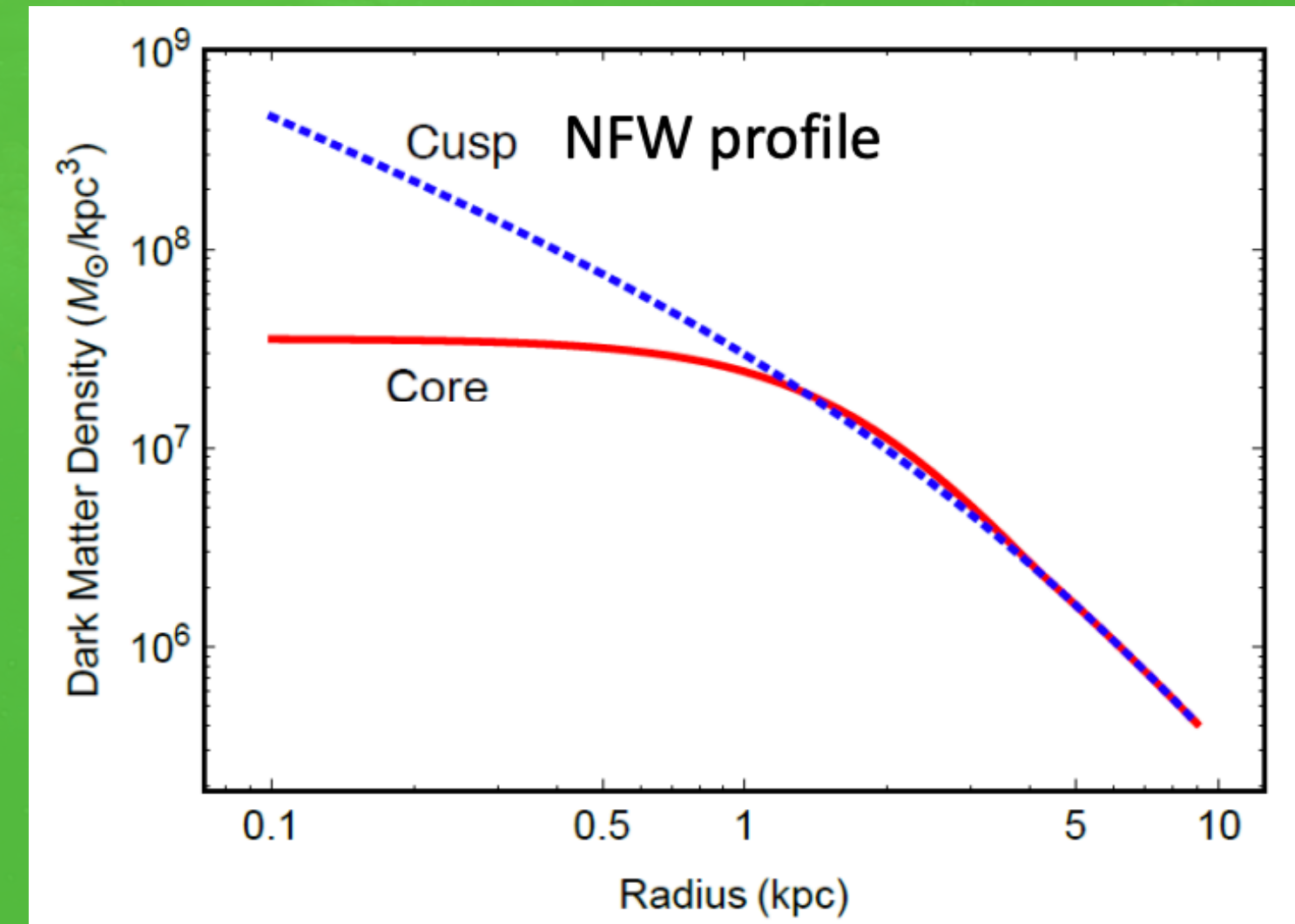
$$\rho_{\text{NFW}}(r) = \frac{\delta_c \rho_c r_s^3}{r (r + r_s)^2}$$

VS

**CORED** profiles

(e.g. the Burkert profile)

$$\rho(r)_{\text{Burk}} = \rho_0 \cdot \frac{r_0^3}{(r + r_0) \cdot (r^2 + r_0^2)}$$



$\delta_c$  : dim.less characteristic overdensity

$\rho_c$  : local critical density

$r_s$  : scale radius

$\rho_0$  : core density

$r_0$  : core radius

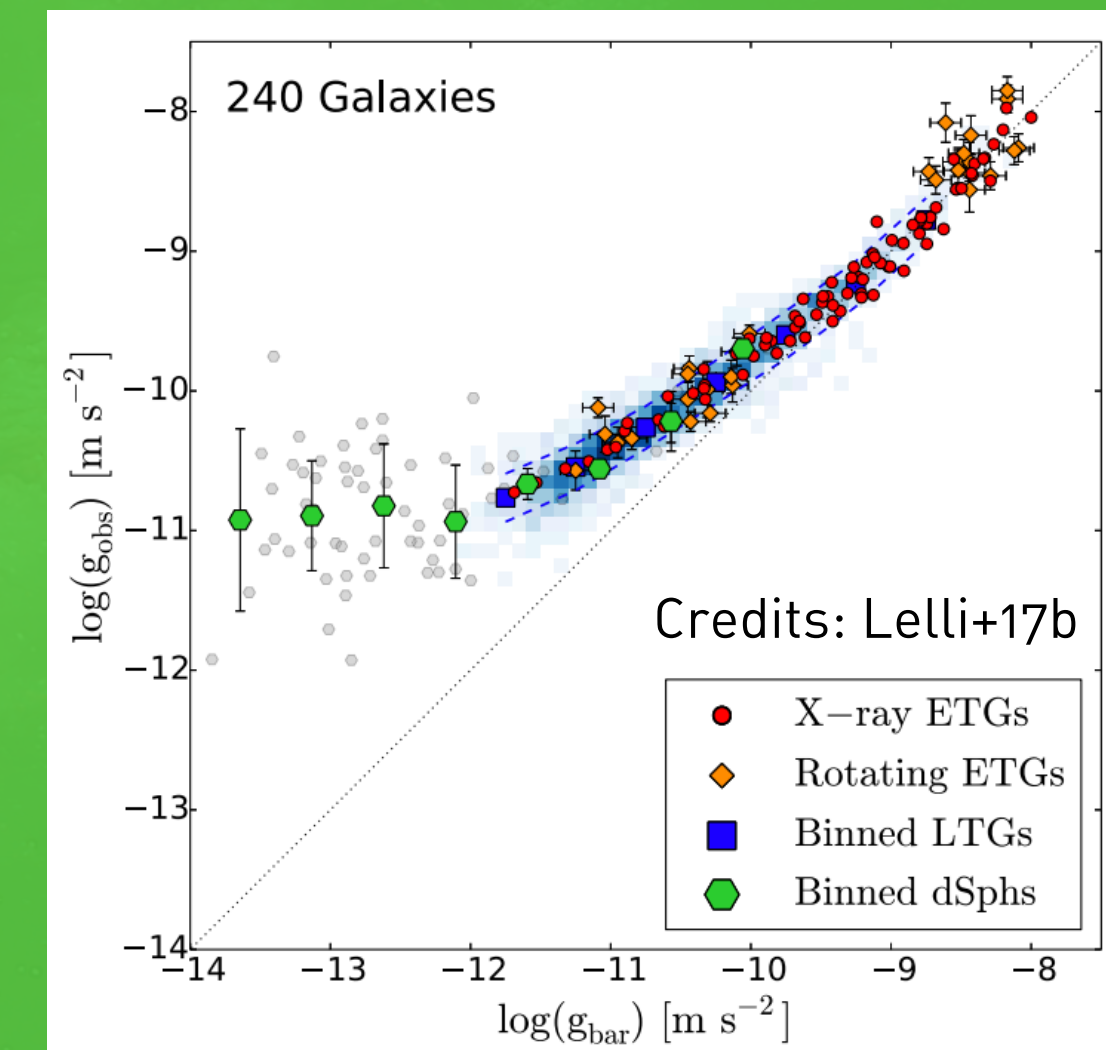
# Motivation

## ISSUE 2: the interplay between DM and baryons in galaxies

e.g. the **Radial Acceleration Relation** (RAR, see Lelli+17b)  
(most general one?)

$g_{\text{tot}}$  VS  $g_{\text{bar}}$

$g_{\text{tot}}$  : total radial acceleration  
 $g_{\text{bar}}$  : **baryonic** radial acceleration



Possible solutions: baryonic/AGN feedback (e.g. Di Cintio+14 from hydro simulations), dynamical friction, non-standard particle candidates...

or... **CDM** dynamically **non-minimally coupled** with **gravity!**

# Theoretical Background

**Idea:** DM dynamics provides an effective metric for baryons in galaxies (modified bkg)

**General Relativity (GR):**  
physical metric = gravitational metric



physical metric =  
gravitational metric & extra field

**Disformal transformations** (Bekenstein 1993):

$$\tilde{g}_{\mu\nu} = e^{2\varphi} \left[ \mathcal{A}(\mathcal{X}) g_{\mu\nu} + \mathcal{B}(\mathcal{X}) \nabla_{\mu}\varphi \nabla_{\nu}\varphi \right] \quad \mathcal{X} = -\frac{1}{2} g_{\mu\nu} \nabla^{\mu}\varphi \nabla^{\nu}\varphi$$

gravitational metric

physical metric

# Action of the model

EINSTEIN  
FRAME

$$S = S_{\text{EH}} [g_{\mu\nu}] + S_{\text{bar}} [\tilde{g}_{\mu\nu}, \psi] + S_{\text{DM}} [g_{\mu\nu}, \varphi]$$

How do we obtain such effective disformally-shaped metric  $\tilde{g}_{\mu\nu}$ ? We need to go in the Jordan frame...

JORDAN  
FRAME

$$S = S_{\text{EH}} [\tilde{g}_{\mu\nu}] + S_{\text{bar}} [\tilde{g}_{\mu\nu}, \psi] + S_{\text{DM}} [\tilde{g}_{\mu\nu}, \varphi] + \epsilon L^2 \int d^4x \sqrt{-\tilde{g}} \tilde{G}^{\mu\nu} \nabla_{\mu} \varphi \nabla_{\nu} \varphi$$

Standard  $\Lambda$ CDM terms  
minimally coupled to gravity

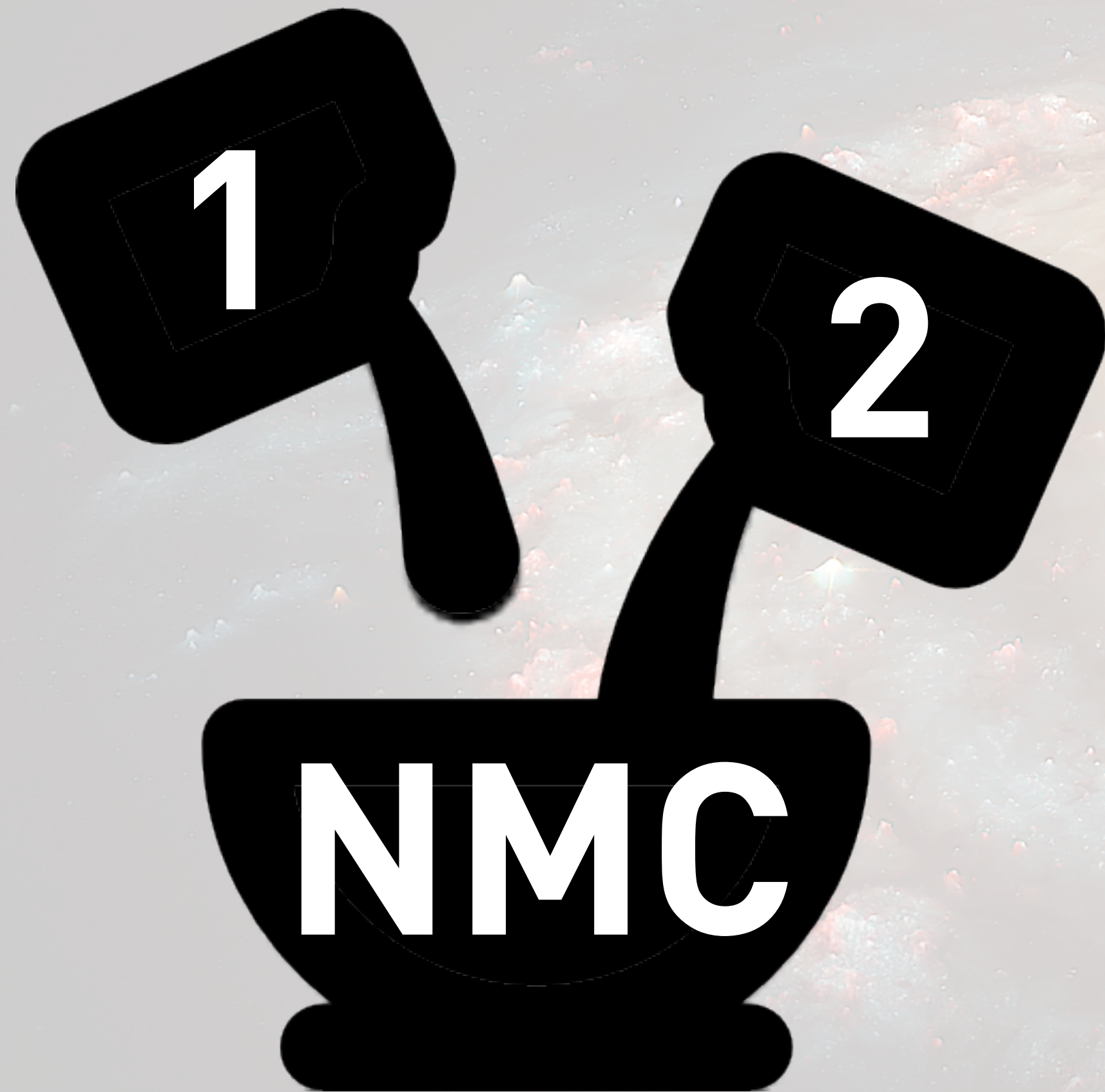
Non-Minimal Coupling (NMC)  
(Bettoni+14; Ivanov&Liberati20: A=1, B=1)

$\epsilon = \pm 1$  : NMC polarity

$L$  : NMC characteristic length-scale

# Crafting the non-minimal coupling

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## Ingredients:

1

A **dynamical process** generating a coherence length for DM

Condensation,  
EoS of DM,  
Fluid description of DM...

2

This coherence length is comparable to the **local curvature scale**

... this is not really a **modified gravity theory** ...

As a consequence,  $L$  **will not have a universal value!**

# Newtonian limit

$$\nabla^2\Phi = 4\pi G \left[ (\rho_{\text{DM}} + \rho_{\text{bar}}) - \epsilon L^2 \nabla^2 \rho_{\text{DM}} \right]$$



the source of gravity is not only density but also **inhomogeneities** in the DM density distribution!

The dynamics of galaxies will be **modified** by such NMC! Let's see how.



# Cored profiles with NMC DM

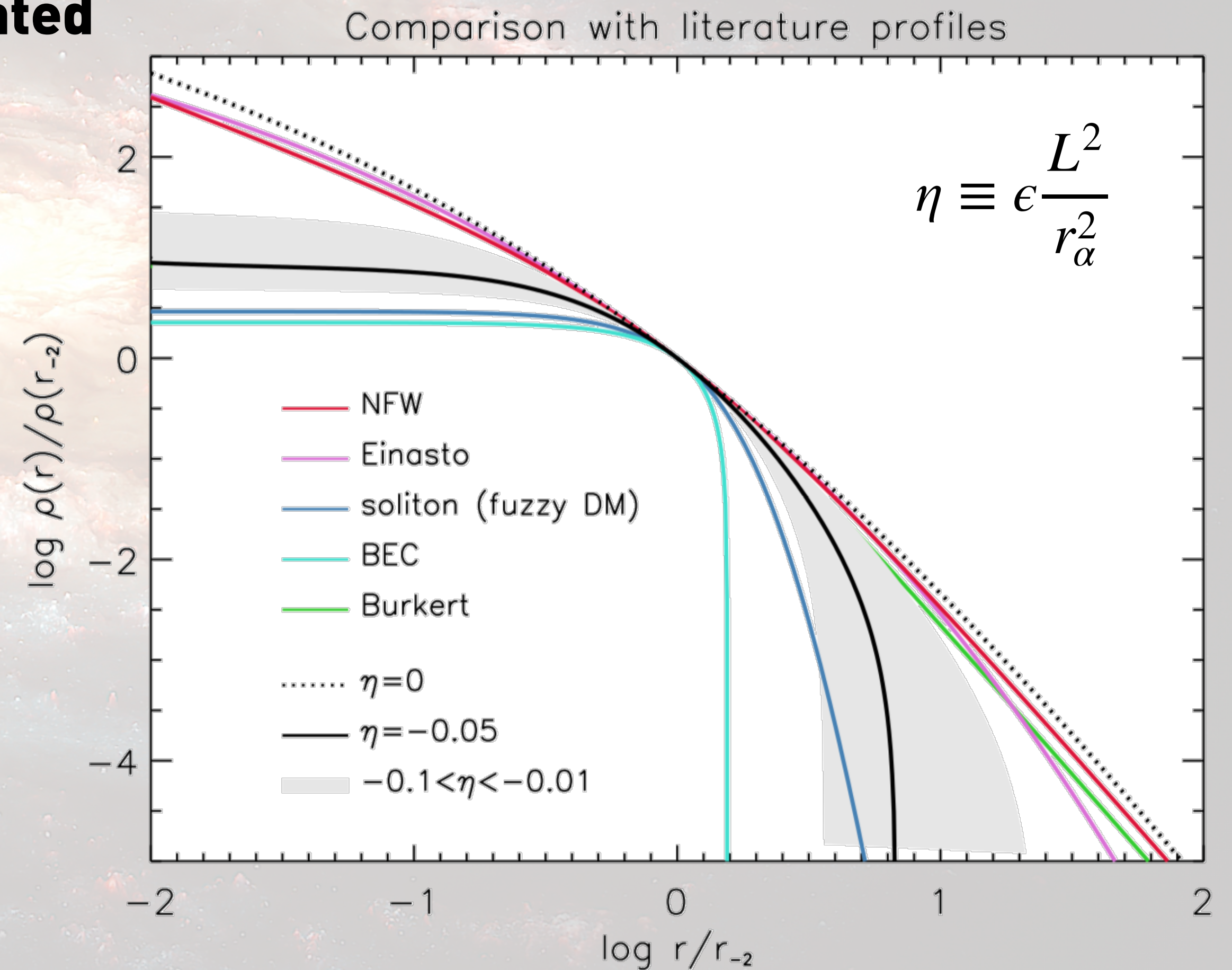
Testing the NMC DM model on dwarf, **DM-dominated** galaxies.

Self-gravitating Equilibria of Non-minimally Coupled Dark Matter Halos

GIOVANNI GANDOLFI,<sup>1,2</sup> ANDREA LAPI,<sup>1,2,3,4</sup> AND STEFANO LIBERATI<sup>1,2,3</sup>

(Gandolfi+21, published in the Astrophysical Journal)

- If  $\eta < 0$  NMC DM profiles are **cored**
- Their shape closely following out to several core scale radii the **phenomenological Burkert profile**
- NMC DM mass distribution yields comparable RC fits to the Burkert profile



# Core surface-density relation

Dwarf galaxies with halo mass  $\mathcal{M} \lesssim 10^{11} M_{\odot}$  seem to obey the following relation:

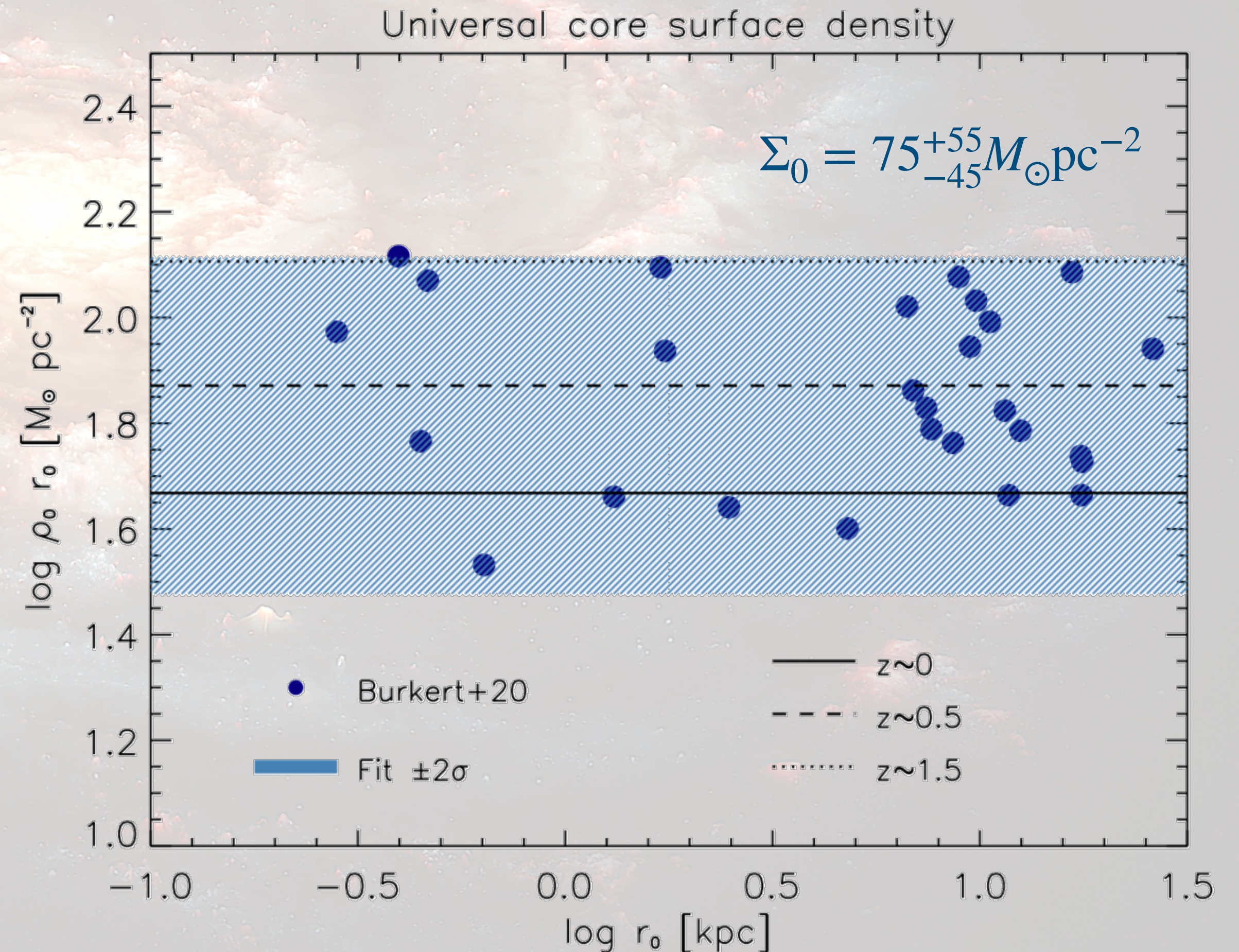
$$\rho_0 r_0 \approx 75^{+55}_{-45} M_{\odot} \text{pc}^{-2}$$

(Salucci&Burkert00; Burkert15)

$$\Sigma_0 \equiv \rho_0 \times r_0 \approx 50 \left( \frac{\Delta_{\text{vir}}}{100} \right) E_z^{0.3} M_{\odot} \text{pc}^{-2}$$

(Gandolfi+21)

A **challenge** to every model of core formation  
(e.g. Deng+18; Burkert 2020)



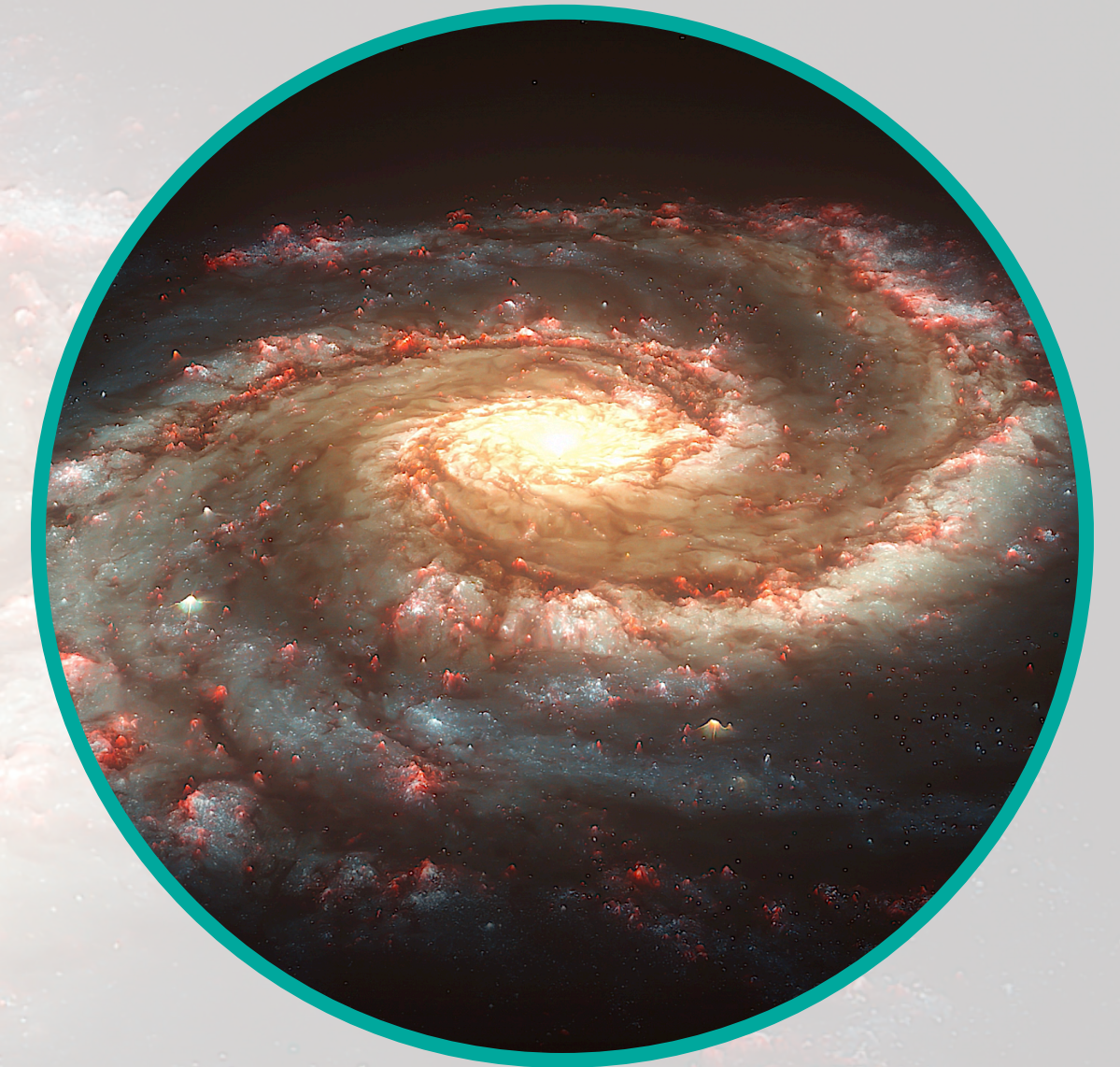
# NMC DM and Galactic Dynamics - I

We test the NMC DM model on local spiral galaxies (LTGs, LSBs, Dws).

Empirical Evidence of Non-Minimally Coupled Dark Matter  
in the Dynamics of Local Spiral Galaxies?

GIOVANNI GANDOLFI <sup>1,2</sup> ANDREA LAPI <sup>1,2,3,4</sup> AND STEFANO LIBERATI <sup>1,2,4</sup>

(Gandolfi+22, , published in the Astrophysical Journal)



**"Perturbative approach"**: NMC acts as a perturbation on a galaxy system characterized by the cuspy NFW profile

$$\rho_{\text{NMC}} = \rho_{\text{NFW}} - \epsilon L^2 \nabla^2 \rho_{\text{NFW}} \quad \rho_{\text{NFW}}(r) = \frac{\delta_c \rho_c r_s^3}{r (r + r_s)^2}$$

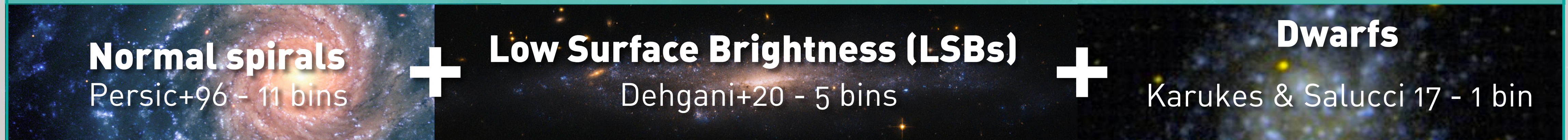
$\delta_c$  : dim.less characteristic overdensity  
 $\rho_c$  : local critical density  
 $r_s$  : scale radius

# Fitting stacked Rotation Curves - I

Mass-modelling of **stacked RCs** of **local spiral galaxies** with different velocities at the optical radius ( $r_{\text{opt}} = 3.2 r_d$  encompasses 83% of total luminosity)

One can co-add normalized high quality RCs to obtain some **benefits**: improved S/N ratio, smoothing data fluctuations...

## SAMPLES OF STACKED RCs (17 total average velocity bins)



Baryonic distribution = exponential thin disk, Dark matter component = ...?

BURKERT PROFILE

VS

NFW PROFILE

VS

NMC PROFILE

# Fitting stacked Rotation Curves - III

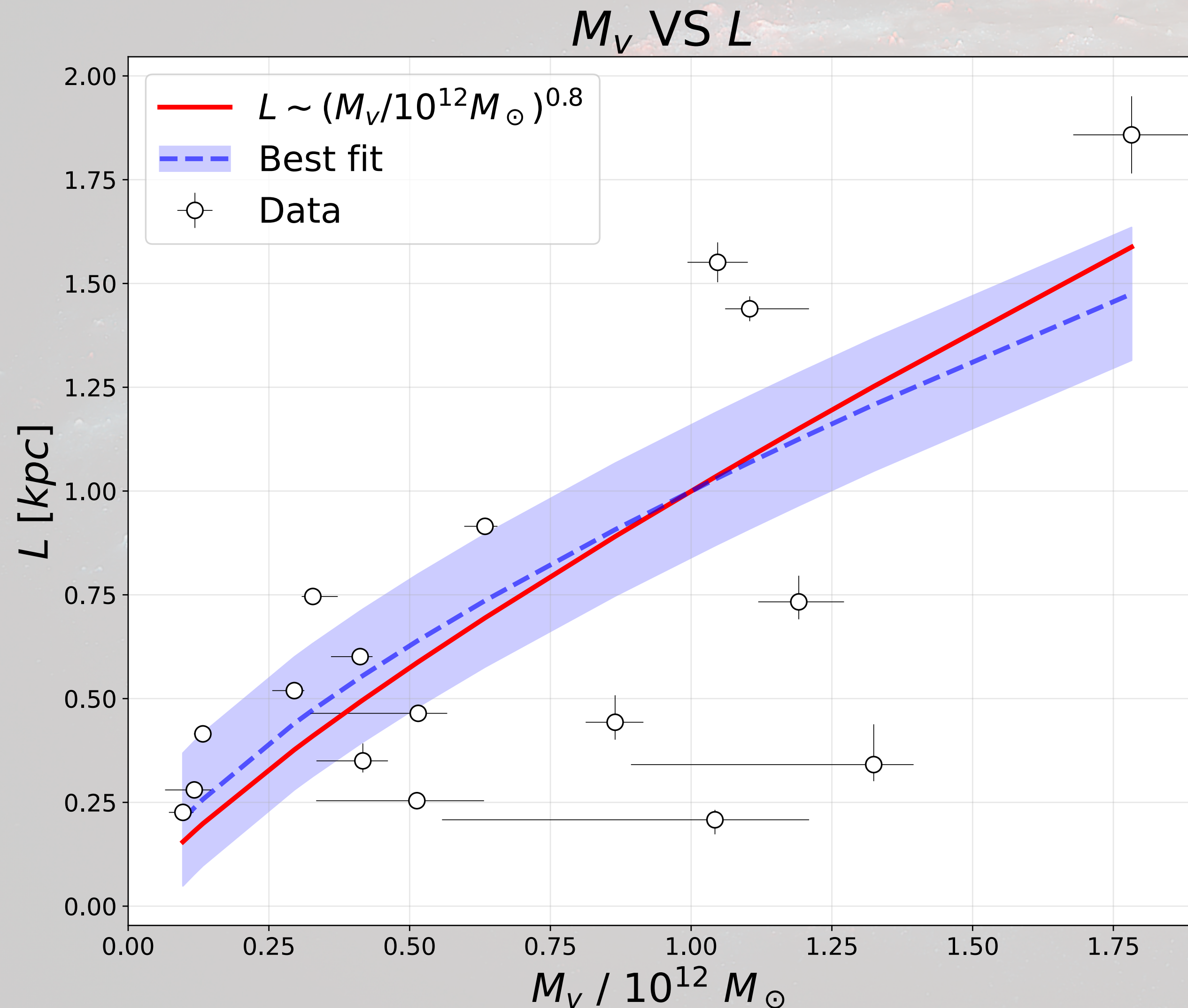
Overall results for the fitting procedure (w. Bayesian MCMC parameter estimation):



\*  $F = (\chi^2_{\text{NFW}} - \chi^2_{\text{NMC}}) / \chi^2_{\text{NMC,red}}$  (Bevington & Robinson 2003)

Null h.p.:  $L = 0$

# Virial mass VS NMC length-scale



$L$  depends on the **environment** (single parameter) with a very simple scaling law!

(... up to galaxy clusters scales, Gandolfi+22b, in prep.)

# The Radial Acceleration Relation

Can the NMC DM model reproduce the **most general** relation between DM and baryons, i.e. the RAR? (See Lelli+17b)

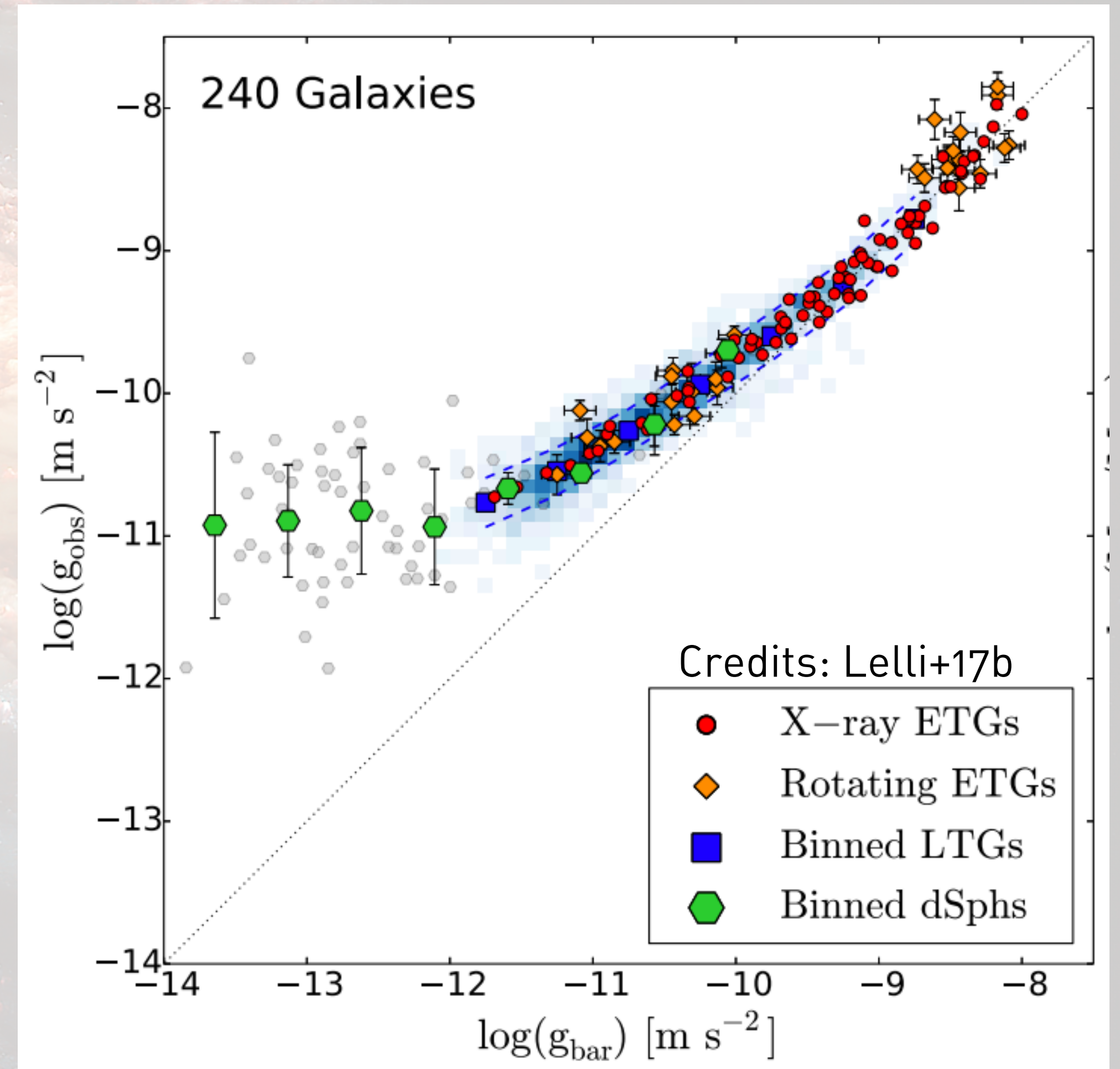
$g_{\text{tot}}$  VS  $g_{\text{bar}}$

$g_{\text{tot}}$ : from galaxy RCs with different masses/velocities

$g_{\text{bar}}$ : from luminous matter distribution (photometry)

Proposed in McGaugh+16 exploiting the **SPARC** sample (individual high-quality RCs, Lelli+16a)

Is it **fundamental**? Could it emerge naturally from the **self-similarity** of **CDM halos** (Navarro+17) or by baryonic effects (Di Cintio+14, ... , Wheeler+19)



# A semi-empirical method

To obtain the RAR we used a semi-empirical method (Di Cintio & Lelli 2016). We generated a large number of virial masses  $8 < \log(M_v/M_\odot) < 13.3$

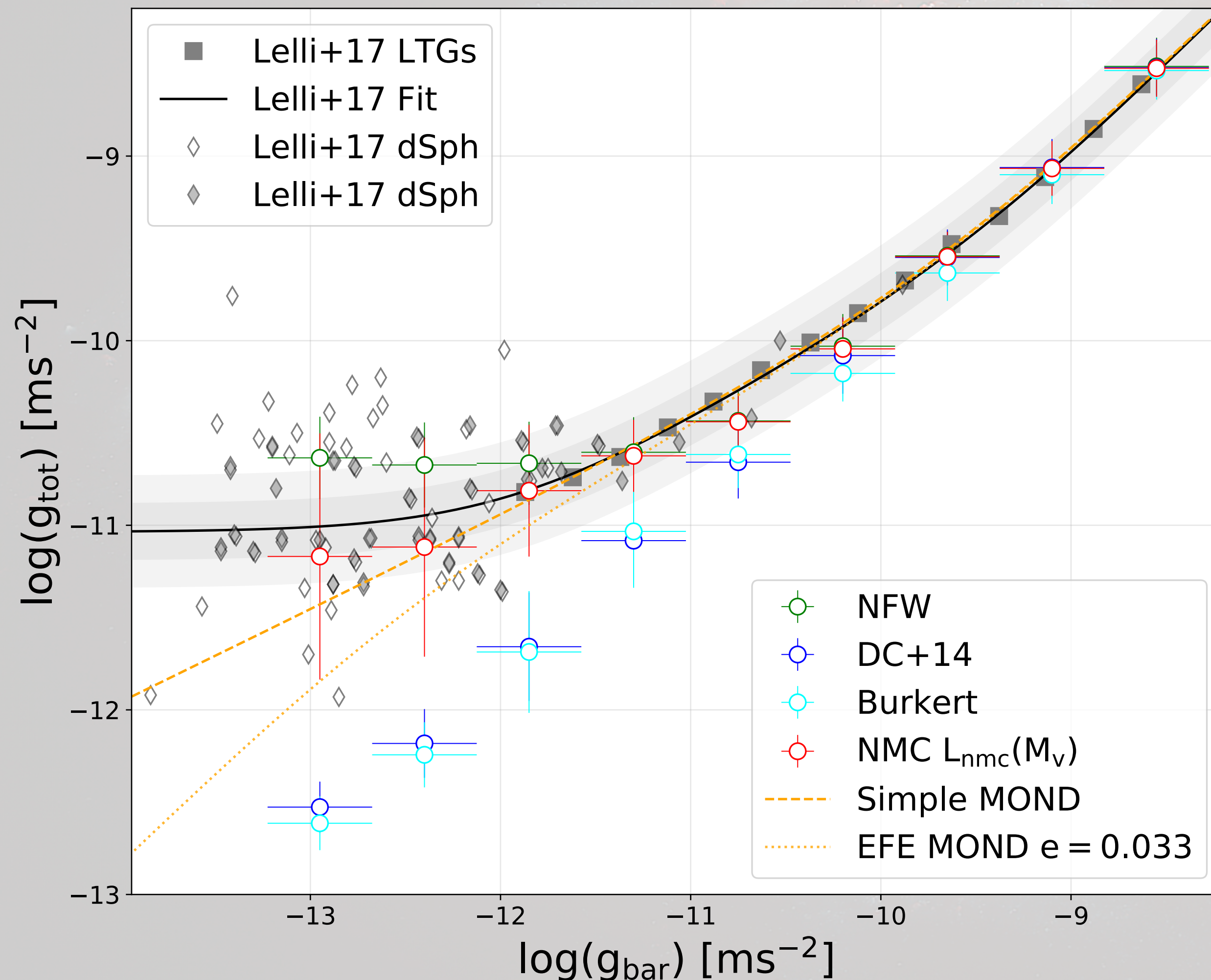
We used semi-empirical relationships linking virial masses to quantities characterizing the **distribution of baryons**.

As for the **DM component**, we assumed different DM density profiles to perform a comparison.





# Radial Acceleration Relation - results



- ✦ Data from Lelli+17 - LTGs + dSph
- ✦ Fitting function (Lelli+17)
- ✦ **Burkert + DC14 struggle** in reproducing the dSph curve
- ✦ **NFW** profile traces well the dSph curve BUT yields poor RC fits
- ✦ **NMC DM** with a mass-dependent scaling for  $L$  reproduces the dSph curve + yields good RC fits!

# Summary

We have hereby analyzed the phenomenology of our NMC DM model in DM-dominated systems and local spiral galaxies.



**TAKE HOME MESSAGE:** this is a **simple** model depending on a **single free parameter** ( $L$ ) showing a very **simple scaling** with the halo virial mass capable of solving consistently long-standing issues of the CDM paradigm.

Find my publications here:

**Thanks for your attention!**

Contact me at [giovanni.gandolfi@sissa.it](mailto:giovanni.gandolfi@sissa.it)

