

# Neutrino Mass Ordering - Circumventing the Challenges using Synergy between INO, T2HK and JUNO

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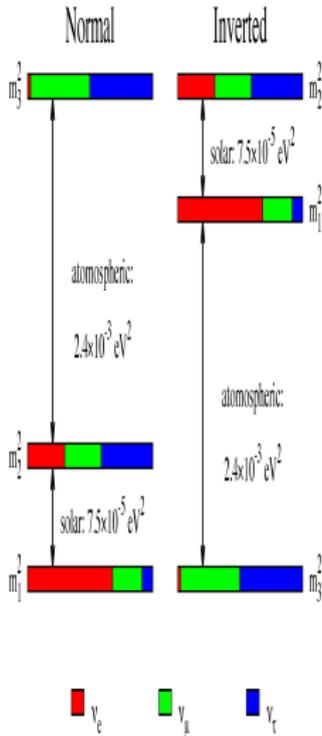
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# Table of Contents

- 1 Neutrino mass ordering
  - Experiments Features
  - Experiments Physics Potential
  - Simulating data for INO@ICAL
  - Simulating data for LBL end Reactor Experiments
  - Results

# Neutrino mass ordering



- The neutrino mass ordering (NMO) is one of the most important questions to be solved in the field of neutrino oscillation physics.
- It impacts the limit on the absolute sum of neutrino masses from cosmology.
- important implications for the searches for neutrino-less double  $\beta$  decay .
- In addition, knowledge of the NMO is an important prerequisite for unambiguously measuring leptonic charge-parity (CP) violation.
- For better understanding of the (flavor-mass) mixing in the lepton sector.

# Experiments Features

Experiments			
Properties	INO@ICAL	JUNO	T2HK
Source	Atmospheric	Reactor	Accelerator
E range	0.5GeV- 25GeV	2MeV-8MeV	0.2GeV- 10GeV
Base line	0-12742 km	53 km	295 km
No of energy bins	15	200	98
Channels	$\nu_\mu/\bar{\nu}_\mu$ app. and dis.	$\bar{\nu}_e$ dis.	$\nu_\mu/\bar{\nu}_\mu$ dis. and $\nu_e/\bar{\nu}_e$ app.
Run time (years)	10	6	10
Matter effect	large	no	very small
Magnetic filed	1.5 Tesla	no	no
Fiducial volume	50kt	20kt	187kt

# Experiments Physics Potential

Experiments		
INO	JUNO	T2HK
$3\sigma$ MO no CP sens poor octant sens -	$3\sigma$ MO no CP sens no octant sens $\theta_{13}$ precise measurement	$2(5)\sigma$ MO CP sens $>5\sigma$ octant sens $>5\sigma$ -
NSI LIV Earth tomography Sterile neutrino - indirect detection of DM -	NSI LIV - Sterile neutrino proton decay indirect detection of DM DSNB	NSI LIV - Sterile neutrino proton decay indirect detection of DM DSNB

# Simulating data for INO@ICAL

- We use honda fluxes calculated by honda etal. for theni site INDIA.
- We use full detector geometry developed by INO collaboration with geant4 detector simulation tool.
- We used Genie montecarlo event generator for neutrino nucleon interaction calculation and it generates events with unoscillated neutrino fluxes.
- We use re-weighting algorithm to include neutrino oscillation for different physics cases.
- We use muon and hadron look-up tables to include detector efficiency and resolution.
- We bin the data in specific binning scheme chosen for specific physics scenarios.
- We do statistical  $\chi^2$  analysis for hypothesis testing.

# Simulating data for LBL end Reactor Experiments

- We use Globes software package to simulate events for long baseline experiments and reactor experiments.
- We use TDR(technical design reports) to make .gls file which includes detector configurations, neutrino channels for signals and backgrounds, baseline density profile, binning scheme etc.
- We add a new probability engine to calculate neutrino oscillation probability for BSM(LIV, NSI, LRF etc.) physics.

# Binning Scheme for INO@ICAL

Marginalization is done only on  $\theta_{23}$ . Rest of the parameters are fixed in whole analysis.

Observable	Range	Bin width	No. of bins
$E_{\mu}^{obs}$ (GeV) (15 bins)	[0.5,4]	0.5	7
	[4,7]	1	3
	[7,11]	4	1
	[11,12.5]	1.5	1
	[12.5,15]	2.5	1
	[15,25]	5	2
$\cos\theta_{\mu}^{obs}$ (21 bins)	[-1.0,-0.4]	0.05	12
	[-0.4,0.0]	0.1	4
	[0,1]	0.2	5
$E_{had}^{obs}$ (GeV)	[0,2]	1	2
	[2,4]	2	1
	[4,15]	11	1

# Results

## Mass Ordering Sensitivity - The Role of $|\Delta m_{31}^2|$

- From the figure we see that the minimum of  $\Delta P_{\mu\mu}$  occurs at  $\Delta m_{31}^2(\text{IO}) \sim -2.300 \times 10^{-3} \text{ eV}^2$  (smaller values of  $|\Delta m_{31}^2|$ ) for neutrinos and at  $\Delta m_{31}^2(\text{IO}) \sim -2.600 \times 10^{-3} \text{ eV}^2$  (larger values of  $|\Delta m_{31}^2|$ ) for antineutrinos.

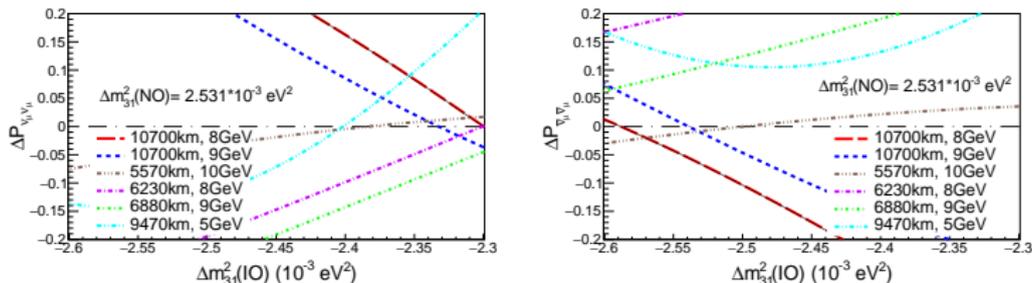


Figure 1: Left panel shows the  $P_{\nu_\mu \nu_\mu}(\text{NO}) - P_{\nu_\mu \nu_\mu}(\text{IO})$  for neutrino and right panel shows the  $P_{\bar{\nu}_\mu \bar{\nu}_\mu}(\text{NO}) - P_{\bar{\nu}_\mu \bar{\nu}_\mu}(\text{IO})$  for anti-neutrinos. These combinations of the energy and baseline have the maximum contribution towards the hierarchy sensitivity

# MO sensitivity of INO as $\chi^2$ plot

- From these curves we see that for neutrinos the  $\chi^2$  minimum is shifted towards  $\Delta m_{31}^2(\text{test}) = -2.380 \times 10^{-3} \text{ eV}^2$  and for the antineutrinos the minimum is shifted towards  $\Delta m_{31}^2(\text{test}) = -2.480 \times 10^{-3} \text{ eV}^2$ .

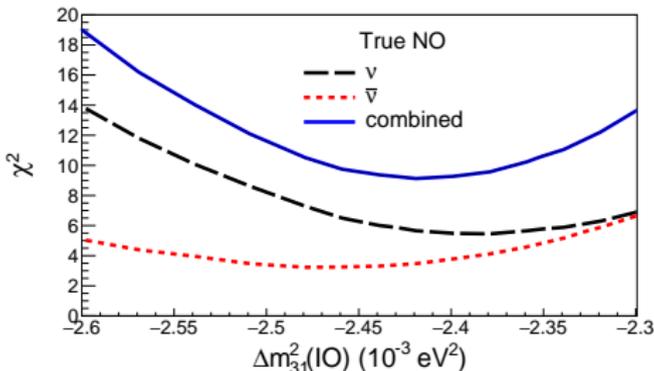


Figure 2: Mass ordering sensitivity  $\chi^2$  as a function of  $\Delta m_{31}^2(\text{INO})$  for ICAL in  $\nu$ ,  $\bar{\nu}$  and combined analysis. Red line is for  $\bar{\nu}_\mu$  and black line for  $\nu_\mu$  data and combined results are shown in blue lines.

# JUNO

- The reactor antineutrino event spectrum that we consider for JUNO varies between  $E = 1.8$  MeV to 8 MeV and is divided into 200 equispaced bins, with bin width 0.031 MeV.
- The different  $E$  bins give  $\chi^2$  minimum at different values of  $\Delta m_{31}^2(\text{IO})$  and  $\chi^2_{\min} \simeq 0$  in each of the individual bins, albeit at a different value of  $\Delta m_{31}^2(\text{IO})$ .

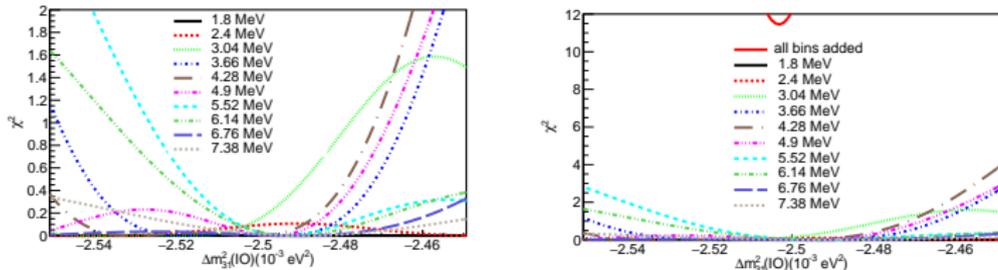


Figure 3: Mass ordering  $\chi^2$  in JUNO for 10 energy bins out of the total 200 energy bins. Systematic uncertainties are neglected.

## T2HK

- the effect of combining the disappearance and the appearance channels in T2HK in a  $\chi^2$  plot. One can see that the minima in  $\Delta m_{31}^2(\text{IO})$  for the disappearance channel comes very close to that predicted and different as compared to the assumed true value.
- Combining both channels gives us the final  $\chi^2$  which higher to simple sum of both the channels.

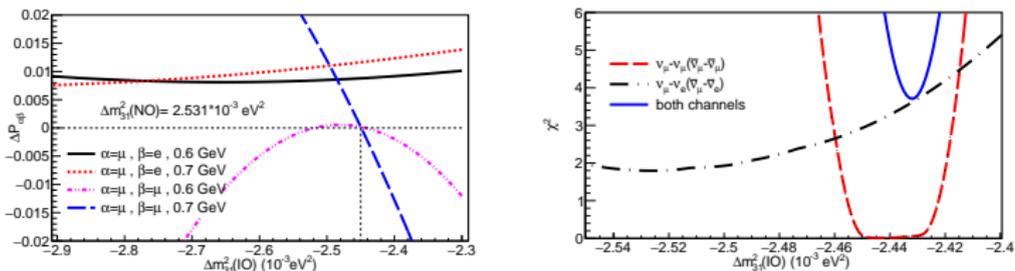


Figure 4: Mass ordering sensitivity  $\chi^2$  as a function of  $\Delta m_{31}^2(\text{IO})$  for T2HK. Red dotted line is for  $\nu_\mu$  and  $\bar{\nu}_\mu$  disappearance channel. The black dotted line is for  $\nu_e$  and  $\bar{\nu}_e$  appearance channel. Blue solid line is for after combining all channels.

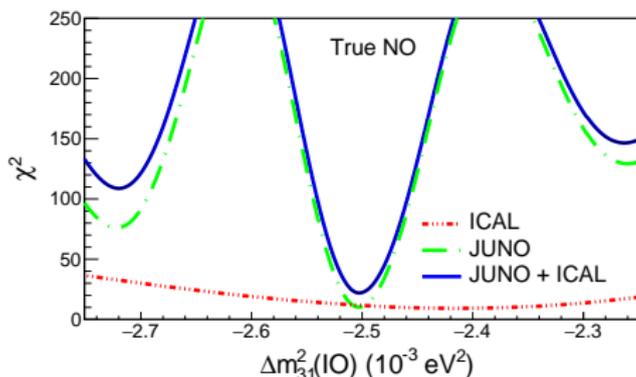
# Juno and ICAL

$\Delta m_{31}^2$ (True)	$\Delta m_{31}^2$ (JUNO)	$\Delta m_{31}^2$ (ICAL)	$\Delta m_{31}^2$ (Combined)
2.531	-2.503	-2.419	-2.503

Table 1:  $\Delta m_{31}^2$ (IO) (in units of  $10^{-3} \text{ eV}^2$ )

JUNO	ICAL	JUNO+ICAL	Combined	% increase
10.23	9.12	19.35	22.01	13.7

Table 2: Mass-ordering  $\chi^2$  for true NO and test IO.

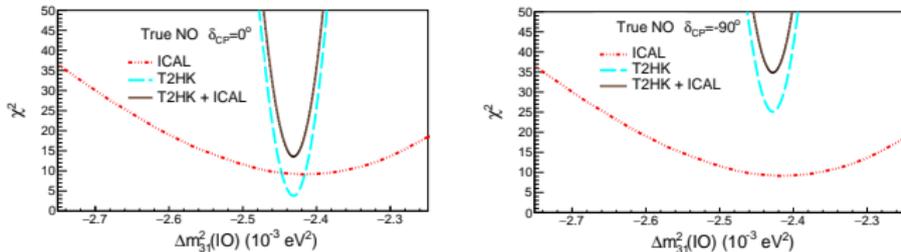


## ICAL and T2HK

	$\Delta m_{31}^2$ (True)	$\Delta m_{31}^2$ (ICAL)	$\Delta m_{31}^2$ (T2HK)	$\Delta m_{31}^2$ (Combined)
$\delta_{CP} = 0$	2.531	-2.419	-2.431	-2.431
$\delta_{CP} = -90$	2.531	-2.419	-2.428	-2.428

Table 3:  $\Delta m_{31}^2(\text{IO})$  (in units of  $10^{-3} \text{ eV}^2$ )

	ICAL	T2HK	T2HK+ICAL	Combined	% increase
$\delta_{CP} = 0$	9.12	3.77	12.89	13.55	5
$\delta_{CP} = -90$	9.12	25.09	34.21	34.84	1.8

Table 4: Mass-ordering  $\chi^2$  for true NO and test IO.Figure 6: Mass ordering sensitivity as a function of  $\Delta m_{31}^2$  (test).

# JUNO and T2HK

	JUNO	T2HK	Combined	True value
$\delta_{\text{CP}} = 0^\circ$	-2.503	-2.432	-2.481	2.531
$\delta_{\text{CP}} = -90^\circ$	-2.503	-2.429	-2.479	2.531

Table 5: Values of  $\Delta m_{31}^2(\text{IO})$  (in units of  $10^{-3} \text{ eV}^2$ ).

NH	$\chi_J^2$	$\chi_T^2$	$\chi_J^2 + \chi_T^2$	$\chi_{\text{Comb.}}^2$	% increase
$\delta_{\text{CP}} = 0$	10.23	3.70	13.93	86.87	523
$\delta_{\text{CP}} = -90$	10.23	25.07	35.30	113.22	220

Table 6: Mass ordering  $\chi^2$  for true NO and test IO.

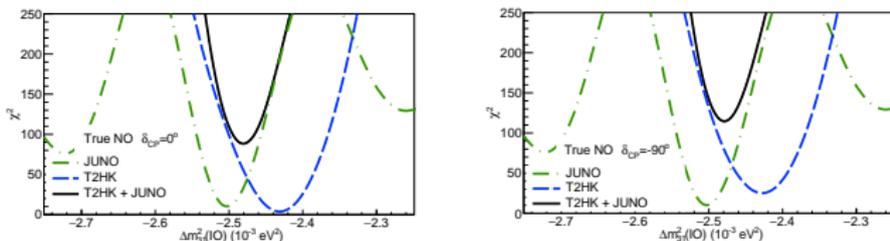


Figure 7: Mass ordering sensitivity expected from a combined analysis.

# ICAL, JUNO and T2HK combined

- All three experiments has  $\Delta m_{31}^2(\text{test})$  minima at different location.
- First  $\chi^2$  of ICAL and T2HK minimize over  $\theta_{23}$  and  $\Delta m_{31}^2(\text{test})$  then JUNO is added and minimized over  $\Delta m_{31}^2(\text{test})$ .

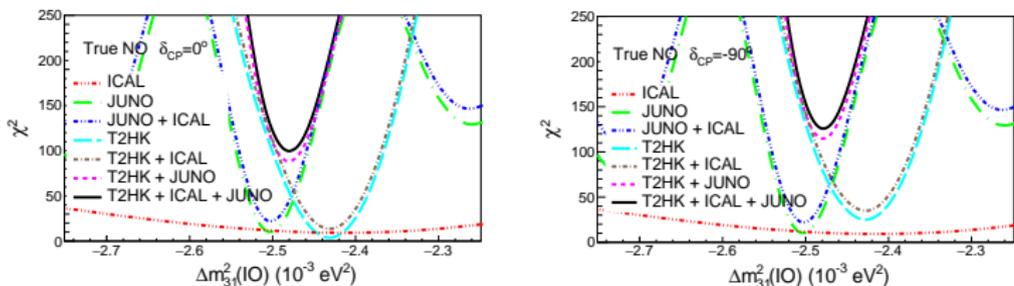


Figure 8: Mass ordering sensitivity as a function of  $\Delta m_{31}^2(\text{test})$ . Left panel is for  $\delta_{CP} = 0^\circ$  and the right panel is for  $\delta_{CP} = -90^\circ$  corresponding to T2HK.

- As we discussed earlier, for JUNO, the mass-ordering  $\chi^2$  is around 10 and for ICAL the mass ordering sensitivity is around  $3\sigma$ . The sensitivity of T2HK is around  $2\sigma$  for  $\delta_{CP} = 0^\circ$  and  $5\sigma$  for  $\delta_{CP} = -90^\circ$ .
- The true value of  $\Delta m_{31}^2$  is same for all these experiments, the  $\chi^2$  minimum occurs at different values of  $\Delta m_{31}^2$  (IO) for different experiments.

	$\Delta m_{31}^2$ (True value)	$\Delta m_{31}^2$ (ICAL)	$\Delta m_{31}^2$ (JUNO)	$\Delta m_{31}^2$ (T2HK)	$\Delta m_{31}^2$ (Combined)
NH( $\delta_{CP} = 0$ )	2.531	-2.419	-2.503	-2.431	-2.48
NH( $\delta_{CP} = -90$ )	2.531	-2.419	-2.503	-2.428	-2.479

Table 7: Values of  $\Delta m_{31}^2$  (IO) (in units of  $10^{-3} \text{ eV}^2$ ), for which we get mass-ordering  $\chi^2$  minimum.

	ICAL	JUNO	T2HK	JUNO + T2HK + ICAL	Combined	% increase
NH( $\delta_{CP} = 0$ )	9.12	10.23	3.77	23.12	99.76	331
NH( $\delta_{CP} = -90$ )	9.12	10.23	25.09	44.44	125.79	183

Table 8: Mass-ordering  $\chi^2$  for true NO and test IO.

# JUNO Resolution effect

- The sensitivity of JUNO goes from  $\chi^2 = 10$  to almost zero when the energy resolution is varied from  $3\%/\sqrt{E(\text{MeV})}$  to  $5\%/\sqrt{E(\text{MeV})}$ .
- For ICAL+JUNO+T2HK the  $\chi^2$  is around 52 (76) for  $\delta_{\text{CP}} = 0^\circ (-90^\circ)$  even if the JUNO energy resolution is  $5\%/\sqrt{E(\text{MeV})}$ .

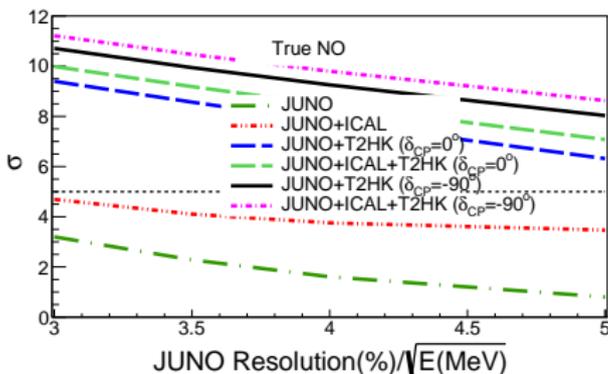


Figure 9: Neutrino mass ordering sensitivity as a function of energy resolution of JUNO.

# ICAL run time effect

- For a 20 years running of ICAL, the  $\chi^2$  for ICAL goes up to 16. When it is added with JUNO the  $\chi^2$  reaches 36.
- For the combination of ICAL+JUNO+T2HK one can have a mass-ordering  $\chi^2$  of 100 (144) for  $\delta_{CP} = 0^\circ$  ( $-90^\circ$ ) for 20 years running of ICAL.

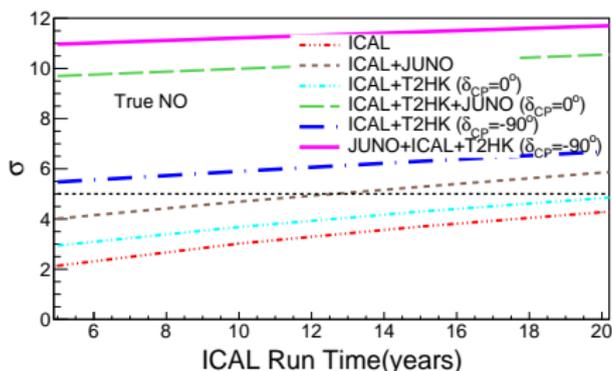


Figure 10: Neutrino mass ordering sensitivity as a function of run-time of ICAL.

# $\theta_{23}$ true effect on MO

- The  $\chi^2$  increases as  $\theta_{23}$  increases from  $42^\circ$  to  $45^\circ$  and when  $\theta_{23}$  increases further from  $45^\circ$ , the sensitivity decreases.

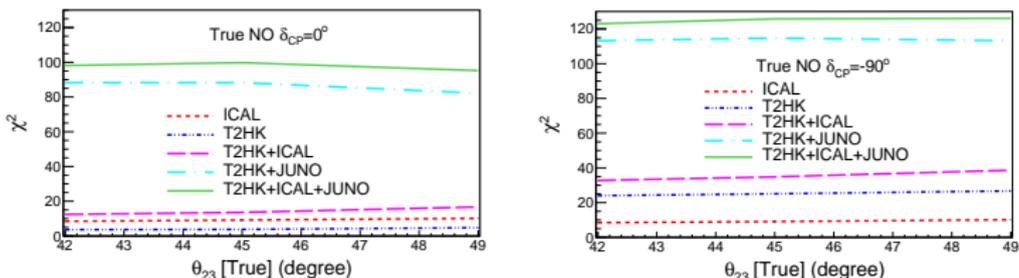


Figure 11: Neutrino mass ordering sensitivity as a function of  $\theta_{23}$  true. Left panel is for  $\delta_{CP} = 0^\circ$  and the right panel is for  $\delta_{CP} = -90^\circ$  corresponding to T2HK.

- For  $\delta_{\text{CP}} = 0^\circ$ , we note that though  $\chi^2$  for T2HK increases as  $\theta_{23}$  increases, the  $\chi^2$  minimum tends to shift towards the left.
- For  $\delta_{\text{CP}} = -90^\circ$ , the shift of the T2HK curve towards left for the value of  $\theta_{23} = 49^\circ$  is less prominent as compared to  $\delta_{\text{CP}} = 0^\circ$ . As a result,

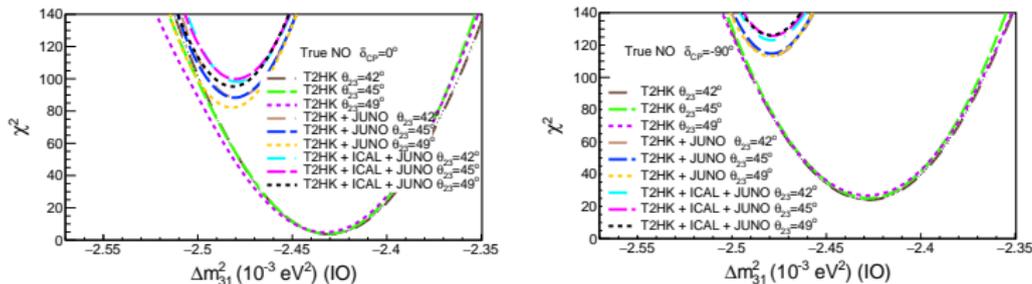


Figure 12: Mass ordering sensitivity as a function of  $\Delta m_{31}^2$  (test) for different values of  $\theta_{23}$ . Left panel is for  $\delta_{\text{CP}} = 0^\circ$  and the right panel is for  $\delta_{\text{CP}} = -90^\circ$  corresponding to T2HK.

# Octant effect on MO sensitivity

- For true  $\theta_{23}$  in the lower octant, the  $\chi^2$  minimum always occurs with the correct octant for both T2HK and ICAL.
- For  $\theta_{23}$  in the higher octant, the  $\chi^2$  minimum occurs at the wrong octant for ICAL. But when ICAL is added with T2HK, the minimum of the combined  $\chi^2$  occurs at the correct octant.

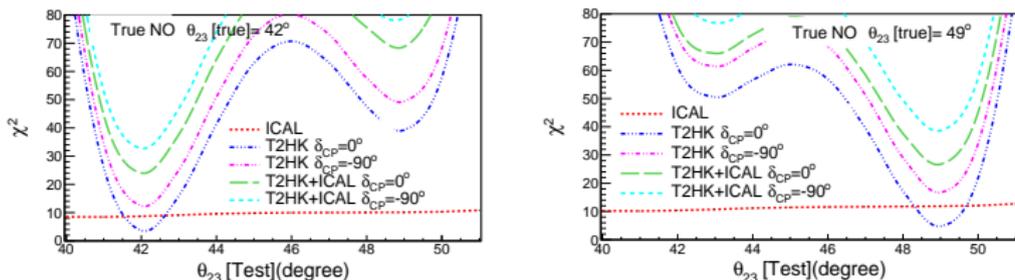


Figure 13: Neutrino mass ordering sensitivity as a function of  $\theta_{23}$  test. Left panel is for  $\delta_{CP} = 0^\circ$  and the right panel is for  $\delta_{CP} = -90^\circ$  corresponding to T2HK.



# References I

- [CGR22] Sandhya Choubey, Monojit Ghosh, and Deepak Raikwal. *Neutrino Mass Ordering – Circumventing the Challenges using Synergy between T2HK and JUNO*. 2022. DOI: [10.48550/ARXIV.2207.04784](https://doi.org/10.48550/ARXIV.2207.04784). URL: <https://arxiv.org/abs/2207.04784>.
- [RCG22] Deepak Raikwal, Sandhya Choubey, and Monojit Ghosh. *Determining Neutrino Mass Ordering with ICAL, JUNO and T2HK*. 2022. DOI: [10.48550/ARXIV.2207.06798](https://doi.org/10.48550/ARXIV.2207.06798). URL: <https://arxiv.org/abs/2207.06798>.