# Tilted cosmology and tensions with the $\Lambda$ CDM model using SNla 

Kerkyra Asvesta

Department of Physics<br>Section of Astrophysics, Astronomy and Mechanics<br>Aristotle University of Thessaloniki

Tensions in Cosmology 7-12 September, Corfu

## Motivation for the tilted model

- Several alternative cosmological models have been proposed to explain observations, but most of them assume some forms of dark energy or abandon FRLW
- Large-scale peculiar motions are not wisely taken into account
- No robust analysis of the peculiar-velocity effects

The tilted cosmological scenario can in principle explain the late-time cosmic acceleration without the need of dark energy/modified gravity or new physics

## The Tilted Cosmological Model



Employ General Relativity
observers with 4-velocity $u_{a} \rightarrow$ idealised observers following the smooth Hubble expansion
observers with 4-velocity $\tilde{v}_{a} \rightarrow$ real observers in galaxies like ours, moving relative to the Hubble frame

## The tilted cosmological model - Kinematics (1/2)

In a perturbed FRW universe, using linear cosmological perturbation theory:

- The three velocities are related through the reduced Lorentz boost :

$$
\begin{equation*}
\tilde{u}_{a} \approx u_{a}+\tilde{v_{a}} \tag{1}
\end{equation*}
$$

for non-relativistic peculiar velocities ( $\tilde{v}^{2}=\tilde{v}^{a} \tilde{v}_{a} \ll 1$ )

- The expansion rates between the two frames are:

$$
\begin{equation*}
\tilde{\Theta}=\Theta+\tilde{\vartheta} \quad \text { and } \quad \tilde{\Theta}^{\prime}=\dot{\Theta}+\tilde{\vartheta}^{\prime} \tag{2}
\end{equation*}
$$

with $\Theta=3 H, \tilde{\vartheta}=\tilde{D}^{a} \tilde{v}_{a}$ and $\tilde{\vartheta} / \Theta \ll 1$ (in the linear regime).
$\tilde{\Theta} \neq \Theta$ and $\tilde{\Theta}^{\prime} \neq \dot{\Theta} \quad$ because of peculiar motion effects only

## The tilted cosmological model - Kinematics (2/2)

In a perturbed Einstein-de Sitter universe ( $p=0$ and $\Omega=1$ ) the deceleration parameter measured by the real observers is:

$$
\begin{equation*}
\tilde{q}=q+\frac{1}{9}\left(\frac{\lambda_{H}}{\lambda}\right)^{2} \frac{\tilde{\vartheta}}{H} \quad \text { with } \lambda_{H}=1 / H \text { and }|\tilde{\vartheta}| / H \ll 1 \tag{3}
\end{equation*}
$$

- When $\lambda \gtrsim \lambda_{H}, \quad \tilde{q} \rightarrow q$ and the peculiar motions fade away
- On subhorizon scales $\left(\lambda \ll \lambda_{H}\right), \quad \tilde{q} \neq q$ and the difference can be large depending on the bulk flow scale
- The difference depends on the sign of $\tilde{\vartheta}$. For contracting bulk-flows $(\tilde{\vartheta}<0), \quad \tilde{q}<0 \longrightarrow$ local apparent accelerated expansion for the real observers


## Parametrization of $\tilde{\vartheta}$

- We assume that locally the bulk flow contracts $(\tilde{\vartheta}<0)$ and $q=\frac{1}{2}$
- We consider a physically motivated form of the local volume scalar $\tilde{\vartheta}$ in the tilted frame ${ }^{1}$

- The deceleration parameter in the tilted frame now becomes

$$
\begin{equation*}
\tilde{q}=\tilde{q}(\lambda)=\frac{1}{2}\left(1-\frac{m}{p+r \lambda^{3}}\right) \tag{5}
\end{equation*}
$$

${ }^{1}$ K. Asvesta, L. Kazantzidis, L. Perivolaropoulos, C. Tsagas, 2022, DOI: $10.1093 / \mathrm{mnras} /$ stac922

## The Pantheon compilation

JLA + additional Snla from PanStarrs and HST (Scolnic et al. (2018) arXiv:1710.00845)

1048 Snla out to redshift $z \sim 2.3$

$\checkmark$ Construct the theoretical apparent magnitude ( $m_{t h}$ ) for the tilted model
Eq. 5 can take the form

$$
\begin{equation*}
\tilde{q}(z)=\frac{1}{2}\left(1-\frac{1}{\alpha+b d_{r}^{3}(z)}\right) \quad \text { with } \quad d_{r}(z)=H_{0} \bar{\chi}(z) / c \tag{6}
\end{equation*}
$$

- The Hubble rate at any redshift connects with the deceleration parameter through

$$
\begin{equation*}
\tilde{H}(z)=H_{0} \exp \left[\int_{0}^{z}\left(\frac{1+\tilde{q}(u)}{1+u}\right) d u\right] \tag{7}
\end{equation*}
$$

- The Hubble free luminosity distance of the SNIa :

$$
\begin{equation*}
\tilde{D}_{L}(z)=H_{0}(1+z) \int_{0}^{z} \frac{d z^{\prime}}{\tilde{H}\left(z^{\prime}\right)} \tag{8}
\end{equation*}
$$

- The theoretically predicted apparent magnitude :
$m_{t h}(z)=5 \log _{10} \tilde{D}_{L}(z)+M+5 \log _{10}\left(\frac{c / H_{0}}{1 M p c}\right)+25=\mathcal{M}+5 \log _{10} \tilde{D}_{L}(z)$


## Results

$$
\begin{equation*}
\chi_{\min }^{2}(\mathcal{M}, \alpha, b)=\left(m_{o b s, i}(z)-m_{t h}(z)\right) C_{i j}^{-1}\left(m_{o b s, j}(z)-m_{t h}(z)\right) \tag{10}
\end{equation*}
$$

- $C_{i j}$ is the total covariance matrix of the SNIa (sys+stat)
- We calculate $\chi^{2}$ for the case of an Einstein-de Sitter bulk flow model

| Model | $\mathcal{M}$ | $\alpha$ | $b$ | $\Omega_{0 m}$ | $\chi_{\min }^{2}$ | $\chi_{\text {red }}^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{\Lambda C D M}$ | $\mathbf{2 3 . 8 0 9} \pm \mathbf{0 . 0 1 1}$ | - | - | $\mathbf{0 . 2 9 9} \pm \mathbf{0 . 0 2 2}$ | $\mathbf{1 0 2 6 . 6 7}$ | $\mathbf{0 . 9 8 1}$ |
| $\mathbf{T - E d S}$ | $\mathbf{2 3 . 8 1 3 _ { - 0 . 0 1 4 } ^ { + 0 . 0 1 5 }}$ | $\mathbf{0 . 5 1 2} \pm \mathbf{0 . 0 4 1}$ | $\mathbf{6 . 7 _ { - 3 . 8 } ^ { + 5 . 6 }}$ | $\mathbf{1 . 0}$ | $\mathbf{1 0 2 6 . 7 6}$ | $\mathbf{0 . 9 8 2}$ |

K. Asvesta, L. Kazantzidis, L. Perivolaropoulos, C. Tsagas, 2022, DOI: $10.1093 / \mathrm{mnras} /$ stac922

Result The tilted cosmological model performs equally well with $\Lambda$ CDM $\left(\chi_{r e d}^{2} \approx 1\right)$

## Evolutionary behaviour of $\tilde{q}$ and confidence levels



K. Asvesta, L. Kazantzidis, L. Perivolaropoulos, C. Tsagas, 2022, DOI: $10.1093 / \mathrm{mnras} /$ stac922

## 3 Things to take away from this talk

- The obtained profile of $\tilde{q}$ is very close to the one of $\Lambda$ CDM
- The transition redshift from deceleration to acceleration, in the tilted model using SNIa, is close to the one from the $\Lambda$ CDM model
- Fit the SNla data to the tilted model and found an apparent late-time cosmic acceleration without the need of dark energy/MG


## What comes next?

- One prediction of the model is the presence of a dipole in the distribution of deceleration measured in the tilted frame
- Allow for a directional dependence in the spatial distribution of $\tilde{\vartheta}$ and consequently on the tilted deceleration parameter $(\tilde{q}) \rightarrow$ test for dipolar modulation on $\tilde{q}$
- Test our results with the recently published SNla data, Pantheon+ and future SNla surveys (LSST) or galaxy clusters
- Test our results with other cosmological probes that extend in greater redshifts such as quasars


