

# Varying fundamental constants may solve the $H_0$ tension

Latest constraints from HARPS and ESPRESSO

Dinko Milaković, Institute for Fundamental Physics of the Universe, Trieste

In collaboration with the ESPRESSO Working Group on Fundamental Physics, John Webb, Chung-Chi Lee and others.



**SISSA**



**Fundamental constants are those  
“whose value we cannot calculate with  
precision in terms of more fundamental  
constants, not just because the  
calculation is too complicated (...) but  
because we do not know of anything  
more fundamental.”**

**Steven Weinberg in “Overview of theoretical prospects for understanding  
the values of fundamental constants” RSPTA (1983) 310 249**

# Today's fundamental constants

## are parameters of the Standard Cosmological Model

Based on Uzan 2011

General relativity + Standard model + Copernican principle + Simply connected topology  
+ dark matter +  
+  $\Lambda$

# Today's fundamental constants

## are parameters of the Standard Cosmological Model

Based on Uzan 2011



Constant	Symbol	Value
Speed of light in vacuum	$c$	$299\,792\,458\text{ m s}^{-1}$
Planck constant (reduced)	$\hbar$	$1.054\,571\,726(47) \times 10^{-34}\text{ J s}$
Newton constant	$G$	$6.673\,84(80) \times 10^{-11}\text{ m}^2\text{ kg}^{-1}\text{ s}^{-2}$
Weak coupling constant (at $m_Z$ )	$g_2(m_Z)$	$0.6520 \pm 0.0001$
Strong coupling constant (at $m_Z$ )	$g_3(m_Z)$	$1.221 \pm 0.022$
Weinberg angle		$0.2229(3)$
Electron Yukawa coupling	$h_e$	$2.935 \times 10^{-6}$
Muon Yukawa coupling	$h_\mu$	$0.000607$
Tauon Yukawa coupling	$h_\tau$	$0.0102057$
Up Yukawa coupling	$h_u$	$0.0000126 \pm 0.000003$
Down Yukawa coupling	$h_d$	$0.000027 \pm 0.000002$
Charmed Yukawa coupling	$h_c$	$0.00732 \pm 0.00002$
Strange Yukawa coupling	$h_s$	$0.00055 \pm 0.00003$
Top Yukawa coupling	$h_t$	$0.994 \pm 0.002$
Bottom Yukawa coupling	$h_b$	$0.0240 \pm 0.0002$
Quark CKM matrix angle	$\sin \theta_{12}$	$0.2244 \pm 0.0014$
	$\sin \theta_{23}$	$0.04221 \pm 0.0014$
	$\sin \theta_{13}$	$0.0249 \pm 0.0005$
Quark CKM matrix phase	$\delta_{\text{CKM}}$	$1.05 \pm 0.24$
Higgs potential quadratic coefficient	$\hat{\mu}^2$	$7835.02 \pm 20.03\text{ GeV}^2$
Higgs potential quartic coefficient	$\lambda$	$0.1295 \pm 0.021$
QCD vacuum phase	$\theta_{\text{QCD}}$	$< 10^{-9}$

Parametre	Symbol	Value
Reduced Hubble constant	$h$	$0.73(3)$
baryon-to-photon ratio	$\eta = n_b/n_\gamma$	$6.12(19) \times 10^{-10}$
Photon density	$\Omega_\gamma h^2$	$2.471 \times 10^{-5}$
Dark matter density	$\Omega_{\text{CDM}} h^2$	$0.105(8)$
Cosmological constant	$\Omega_\Lambda$	$0.73(3)$
Spatial curvature	$\Omega_K$	$0.011(12)$
Scalar modes amplitude	$Q$	$(2.0 \pm 0.2) \times 10^{-5}$
Scalar spectral index	$n_S$	$0.958(16)$
Neutrino density	$\Omega_\nu h^2$	$(0.0005 - 0.023)$
Dark energy equation of state	$w$	$-0.97(7)$
Scalar running spectral index	$\alpha_S$	$-0.05 \pm 0.03$
Tensor-to-scalar ratio	T/S	$< 0.36$
Tensor spectral index	$n_T$	$< 0.001$
Tensor running spectral index	$\alpha_T$	?
Baryon density	$\Omega_b h^2$	$0.0223(7)$

# Dimensionless quantities are easier to measure in terrestrial and astronomical settings









Quantity	Algebraic ratio	Numerical value	Related to
$\alpha_{\text{EM}}$	$\frac{e^2}{4\pi\epsilon_0\hbar c}$	1/137.03599976	Strength of the electromagnetic force
$\alpha_{\text{W}}$	$\frac{G_{\text{F}}m_p^2 c}{\hbar^3}$	$1.03 \times 10^{-5}$	Strength of the weak force
$\alpha_{\text{S}}(E)$	$\frac{g_s^2(E)}{\hbar c}$		Strength of the strong force
$\alpha_{\text{G}}$	$\frac{Gm_p^2}{\hbar c}$	$5 \times 10^{-39}$	Strength of the gravitational force
$\mu$	$\frac{m_e}{m_p}$	$5.44617 \times 10^{-4}$	
$x$	$g_p\alpha_{\text{EM}}^2\mu$	$1.62 \times 10^{-7}$	
$y$	$g_p\alpha_{\text{EM}}^2$	$2.977 \times 10^{-4}$	

# Varying constants and the $H_0$ olympics

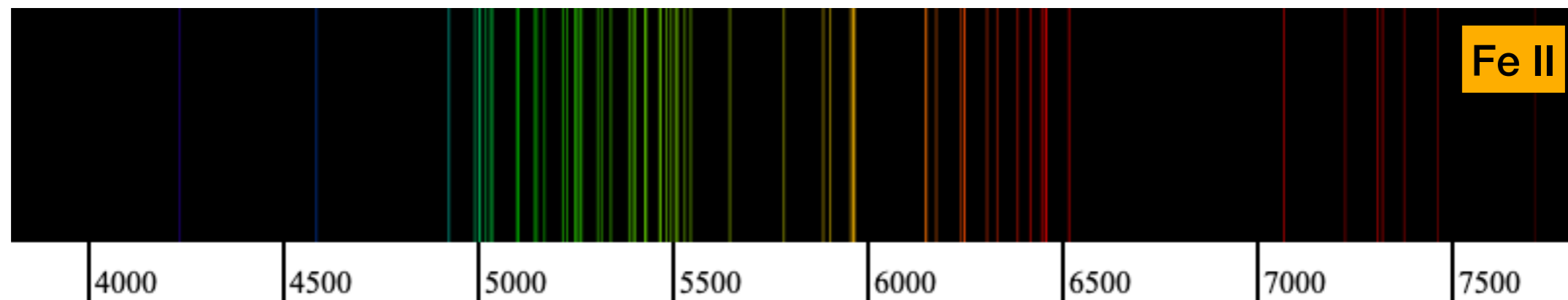
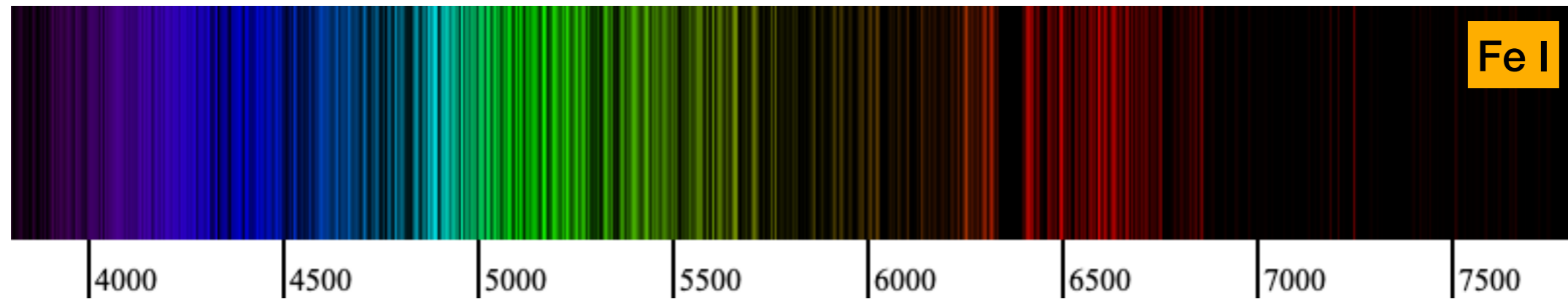
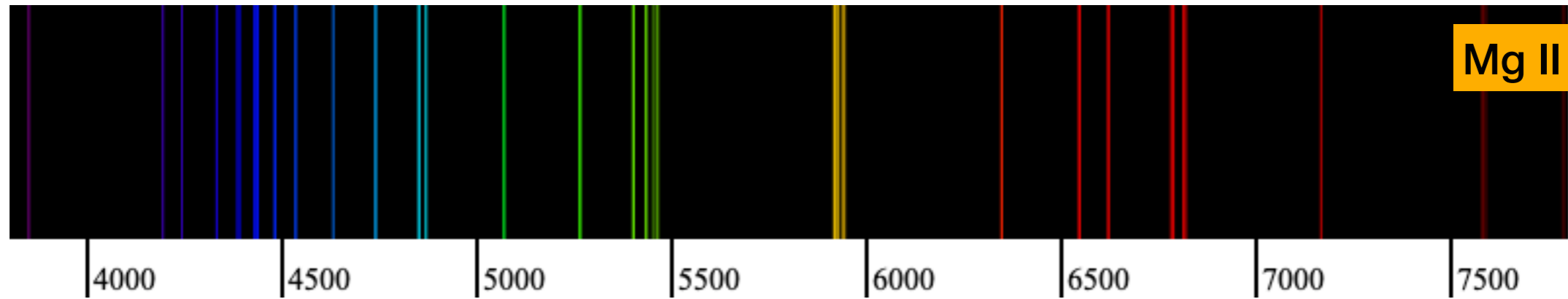
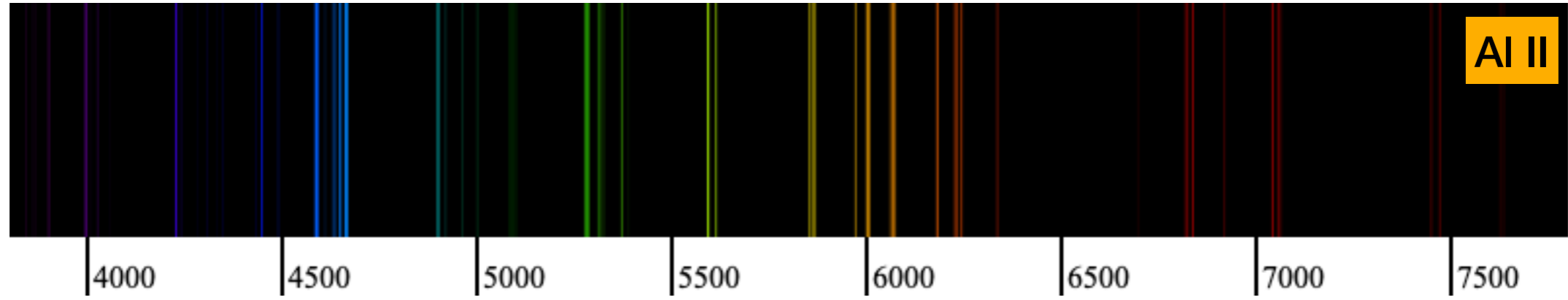
Model	$\Delta N_{\text{param}}$	$M_B$	Gaussian Tension	$Q_{\text{DMAP}}$ Tension		$\Delta\chi^2$	$\Delta\text{AIC}$		One test passed
$\Lambda\text{CDM}$	0	$-19.416 \pm 0.012$	$4.4\sigma$	$4.5\sigma$	<b>X</b>	0.00	0.00	<b>X</b>	<b>X</b>
$\Delta N_{\text{ur}}$	1	$-19.395 \pm 0.019$	$3.6\sigma$	$3.8\sigma$	<b>X</b>	-6.10	-4.10	<b>X</b>	<b>X</b>
SIDR	1	$-19.385 \pm 0.024$	$3.2\sigma$	$3.3\sigma$	<b>X</b>	-9.57	-7.57	✓	✓
mixed DR	2	$-19.413 \pm 0.036$	$3.3\sigma$	$3.4\sigma$	<b>X</b>	-8.83	-4.83	<b>X</b>	<b>X</b>
DR-DM	2	$-19.388 \pm 0.026$	$3.2\sigma$	$3.1\sigma$	<b>X</b>	-8.92	-4.92	<b>X</b>	<b>X</b>
$\text{SI}\nu\text{+DR}$	3	$-19.440^{+0.037}_{-0.039}$	$3.8\sigma$	$3.9\sigma$	<b>X</b>	-4.98	1.02	<b>X</b>	<b>X</b>
Majoron	3	$-19.380^{+0.027}_{-0.021}$	$3.0\sigma$	$2.9\sigma$	✓	-15.49	-9.49	✓	✓
primordial B	1	$-19.390^{+0.018}_{-0.024}$	$3.5\sigma$	$3.5\sigma$	<b>X</b>	-11.42	-9.42	✓	✓
→ varying $m_e$	1	$-19.391 \pm 0.034$	$2.9\sigma$	$2.9\sigma$	✓	-12.27	-10.27	✓	✓
→ varying $m_e + \Omega_k$	2	$-19.368 \pm 0.048$	$2.0\sigma$	$1.9\sigma$	✓	-17.26	-13.26	✓	✓
EDE	3	$-19.390^{+0.016}_{-0.035}$	$3.6\sigma$	$1.6\sigma$	✓	-21.98	-15.98	✓	✓
NEDE	3	$-19.380^{+0.023}_{-0.040}$	$3.1\sigma$	$1.9\sigma$	✓	-18.93	-12.93	✓	✓
EMG	3	$-19.397^{+0.017}_{-0.023}$	$3.7\sigma$	$2.3\sigma$	✓	-18.56	-12.56	✓	✓
CPL	2	$-19.400 \pm 0.020$	$3.7\sigma$	$4.1\sigma$	<b>X</b>	-4.94	-0.94	<b>X</b>	<b>X</b>
PEDE	0	$-19.349 \pm 0.013$	$2.7\sigma$	$2.8\sigma$	✓	2.24	2.24	<b>X</b>	<b>X</b>
GPEDE	1	$-19.400 \pm 0.022$	$3.6\sigma$	$4.6\sigma$	<b>X</b>	-0.45	1.55	<b>X</b>	<b>X</b>
DM $\rightarrow$ DR+WDM	2	$-19.420 \pm 0.012$	$4.5\sigma$	$4.5\sigma$	<b>X</b>	-0.19	3.81	<b>X</b>	<b>X</b>
DM $\rightarrow$ DR	2	$-19.410 \pm 0.011$	$4.3\sigma$	$4.5\sigma$	<b>X</b>	-0.53	3.47	<b>X</b>	<b>X</b>

Schöneberg et al. 2022

# Varying constants: winners of the $H_0$ olympics

Model	$\Delta N_{\text{param}}$	$M_B$	Gaussian Tension	$Q_{\text{DMAP}}$ Tension		$\Delta\chi^2$	$\Delta\text{AIC}$		One test passed
$\Lambda\text{CDM}$	0	$-19.416 \pm 0.012$	$4.4\sigma$	$4.5\sigma$	<b>X</b>	0.00	0.00	<b>X</b>	<b>X</b>
$\Delta N_{\text{ur}}$	1	$-19.395 \pm 0.019$	$3.6\sigma$	$3.8\sigma$	<b>X</b>	-6.10	-4.10	<b>X</b>	<b>X</b>
SIDR	1	$-19.385 \pm 0.024$	$3.2\sigma$	$3.3\sigma$	<b>X</b>	-9.57	-7.57	✓	✓ 
mixed DR	2	$-19.413 \pm 0.036$	$3.3\sigma$	$3.4\sigma$	<b>X</b>	-8.83	-4.83	<b>X</b>	<b>X</b>
DR-DM	2	$-19.388 \pm 0.026$	$3.2\sigma$	$3.1\sigma$	<b>X</b>	-8.92	-4.92	<b>X</b>	<b>X</b>
$\text{SI}\nu\text{+DR}$	3	$-19.440^{+0.037}_{-0.039}$	$3.8\sigma$	$3.9\sigma$	<b>X</b>	-4.98	1.02	<b>X</b>	<b>X</b>
Majoron	3	$-19.380^{+0.027}_{-0.021}$	$3.0\sigma$	$2.9\sigma$	✓	-15.49	-9.49	✓	✓ 
primordial B	1	$-19.390^{+0.018}_{-0.024}$	$3.5\sigma$	$3.5\sigma$	<b>X</b>	-11.42	-9.42	✓	✓ 
→ varying $m_e$	1	$-19.391 \pm 0.034$	$2.9\sigma$	$2.9\sigma$	✓	-12.27	-10.27	✓	✓ 
→ varying $m_e + \Omega_k$	2	$-19.368 \pm 0.048$	$2.0\sigma$	$1.9\sigma$	✓	-17.26	-13.26	✓	✓ 
EDE	3	$-19.390^{+0.016}_{-0.035}$	$3.6\sigma$	$1.6\sigma$	✓	-21.98	-15.98	✓	✓ 
NEDE	3	$-19.380^{+0.023}_{-0.040}$	$3.1\sigma$	$1.9\sigma$	✓	-18.93	-12.93	✓	✓ 
EMG	3	$-19.397^{+0.017}_{-0.023}$	$3.7\sigma$	$2.3\sigma$	✓	-18.56	-12.56	✓	✓ 
CPL	2	$-19.400 \pm 0.020$	$3.7\sigma$	$4.1\sigma$	<b>X</b>	-4.94	-0.94	<b>X</b>	<b>X</b>
PEDE	0	$-19.349 \pm 0.013$	$2.7\sigma$	$2.8\sigma$	✓	2.24	2.24	<b>X</b>	<b>X</b>
GPEDE	1	$-19.400 \pm 0.022$	$3.6\sigma$	$4.6\sigma$	<b>X</b>	-0.45	1.55	<b>X</b>	<b>X</b>
DM $\rightarrow$ DR+WDM	2	$-19.420 \pm 0.012$	$4.5\sigma$	$4.5\sigma$	<b>X</b>	-0.19	3.81	<b>X</b>	<b>X</b>
DM $\rightarrow$ DR	2	$-19.410 \pm 0.011$	$4.3\sigma$	$4.5\sigma$	<b>X</b>	-0.53	3.47	<b>X</b>	<b>X</b>

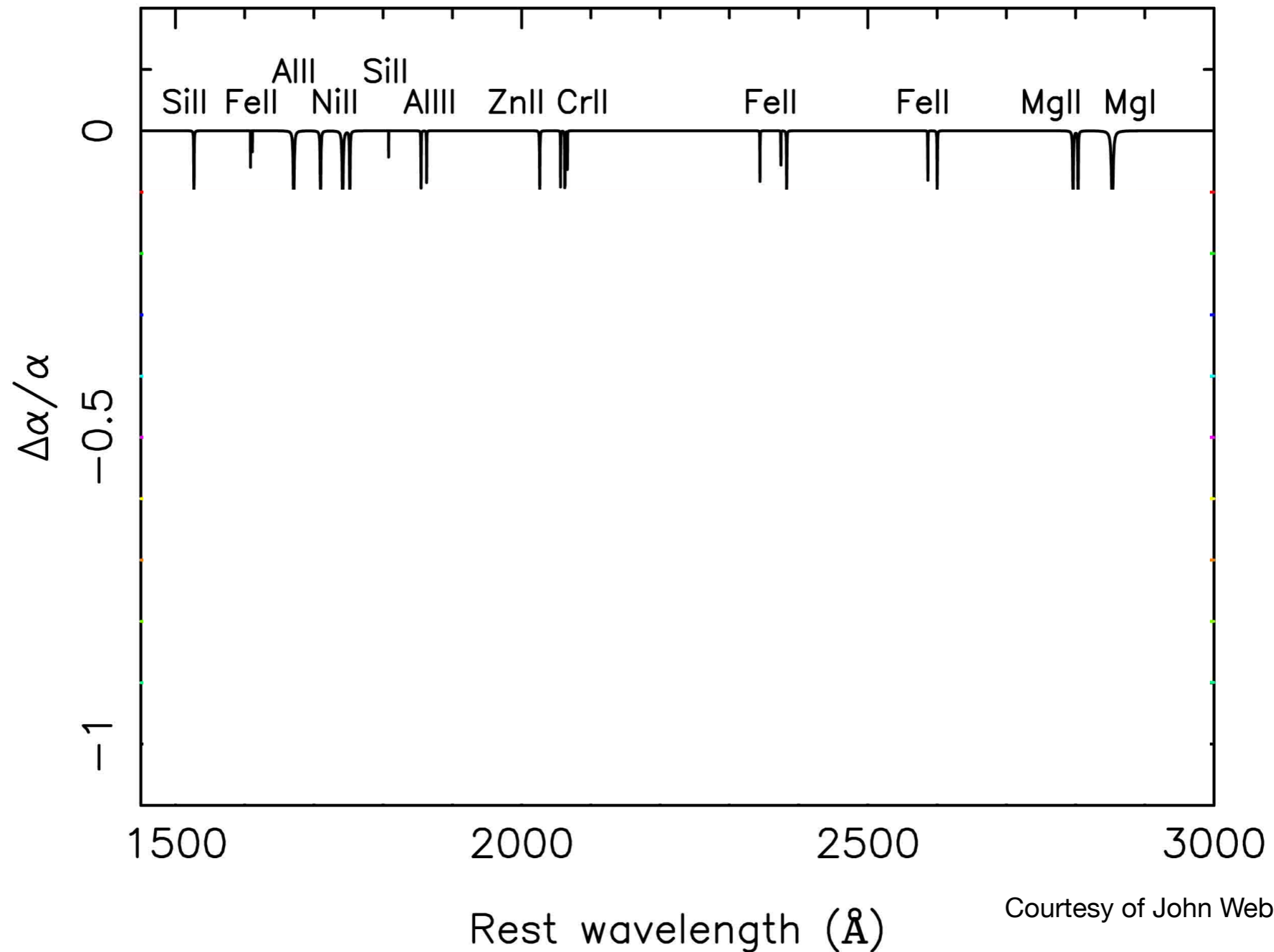
Schöneberg et al. 2022





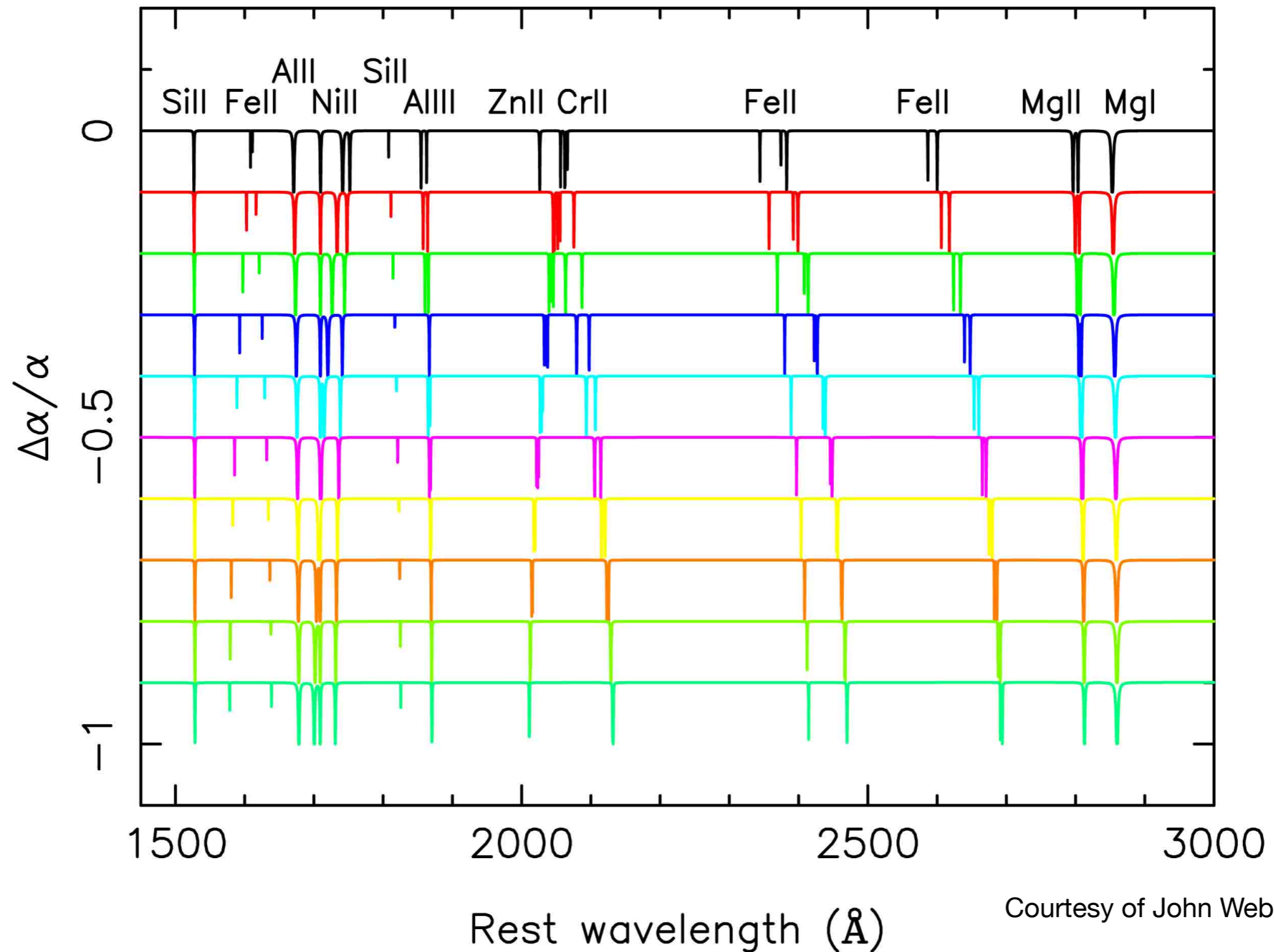
# Observable: a pattern of velocity shifts between transitions

$$\frac{\Delta v}{c} \approx \frac{\Delta \alpha}{\alpha} \frac{2q}{\omega}$$



# Observable: a pattern of velocity shifts between transitions

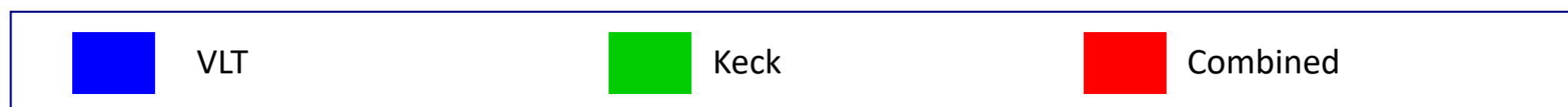
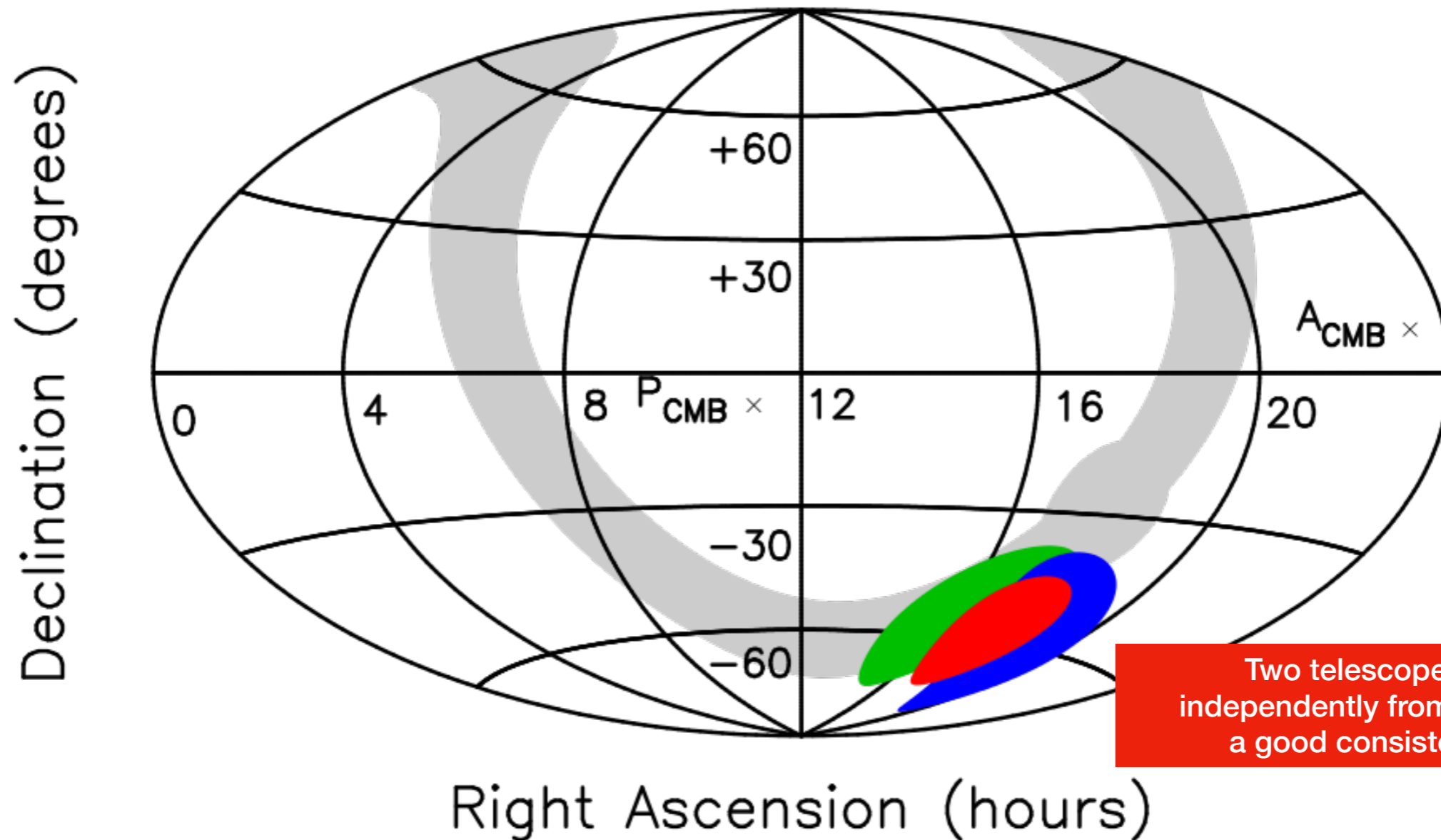
$$\frac{\Delta v}{c} \approx \frac{\Delta \alpha}{\alpha} \frac{2q}{\omega}$$



Courtesy of John Webb

# 154 VLT/UVES + 141 Keck/HIRES observations show evidence for a dipole on the sky, $4.2\sigma$ statistical

King et al. 2012  
Webb et al. 2011



# Precision measurements require

## 1. **Bright quasars:**

Sky surveys and dedicated searches (e.g. QUBRICS, Boutsia 2022)

## 2. **High resolution spectroscopy:**

Echelle gratings

## 3. **Accurate wavelength calibration:**

Laser Frequency Combs (Nobel prize for physics 2005)

**New!**

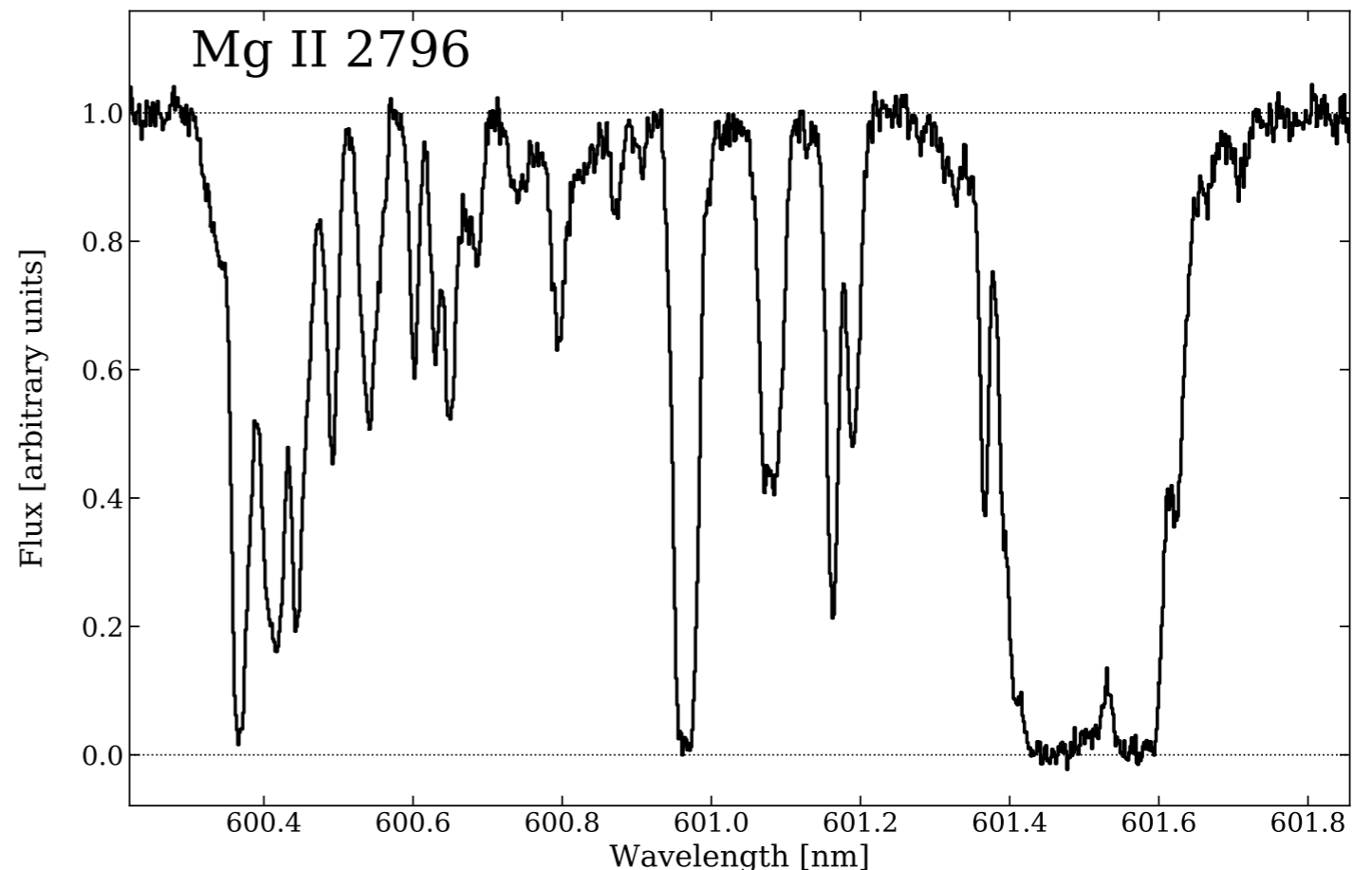
## 4. **Robust analysis methods:**

Artificial Intelligence Voigt Profile Fitting (AI-VPFIT, Lee et al. 2021)

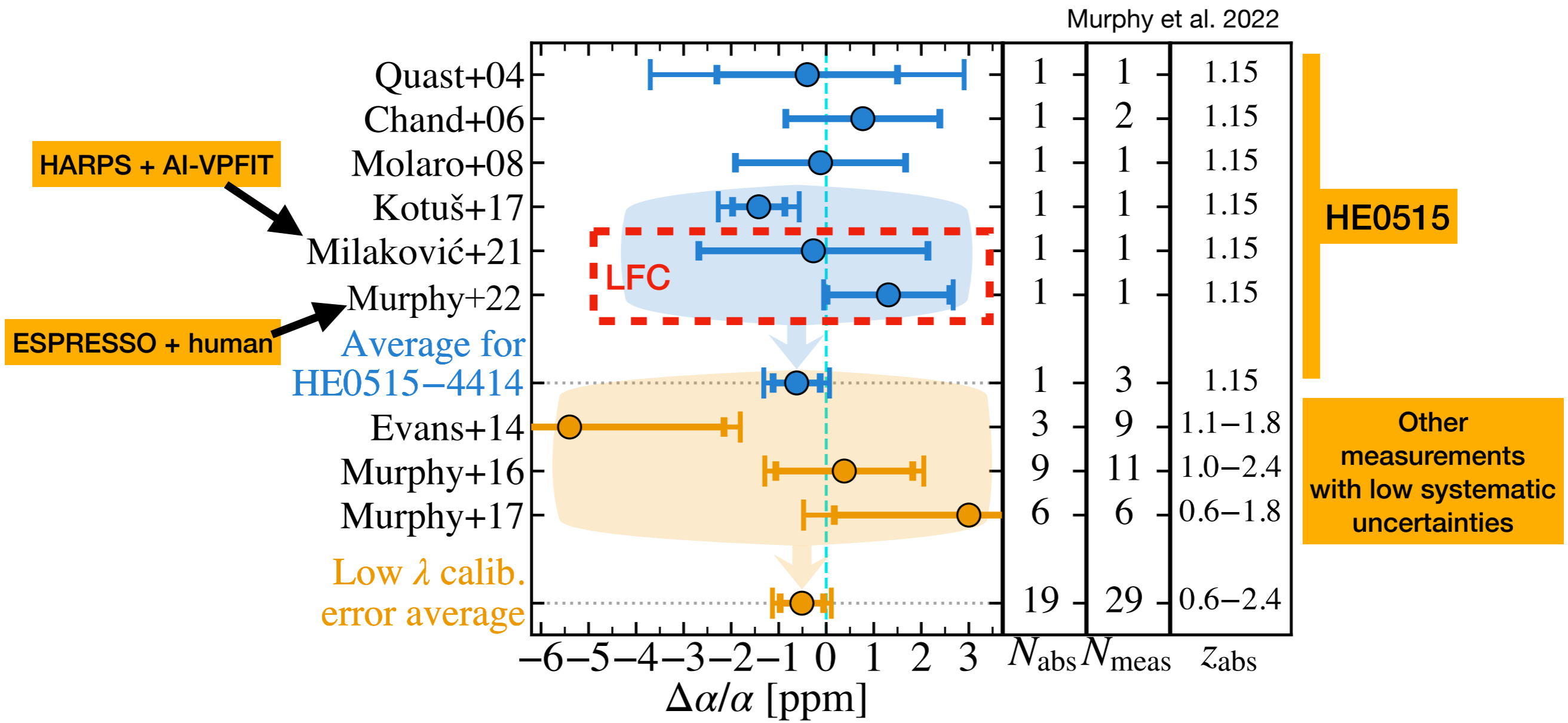
# Artificial intelligence methods quickly produce objective and reproducible models

**AI-VPFIT** Lee, Webb, Carswell, Milaković (2021) MNRAS 504 1787  
Lee, Webb, Milaković, Carswell (2021) MNRAS 507 27

- Genetic algorithms + Monte Carlo methods
- Information criterion as an **objective** criterion to choose the optimal model
- 100x increase in speed
- No human bias



# HE 0515-4414: no evidence for variation but this is consistent with dipole predictions



Overall, no evidence for variation in any particular system

# No evidence for time varying dark energy EoS

## A scalar field would couple to the electromagnetic sector

Martins et al. 2022 (but see also de Fonseca et al. 2022)

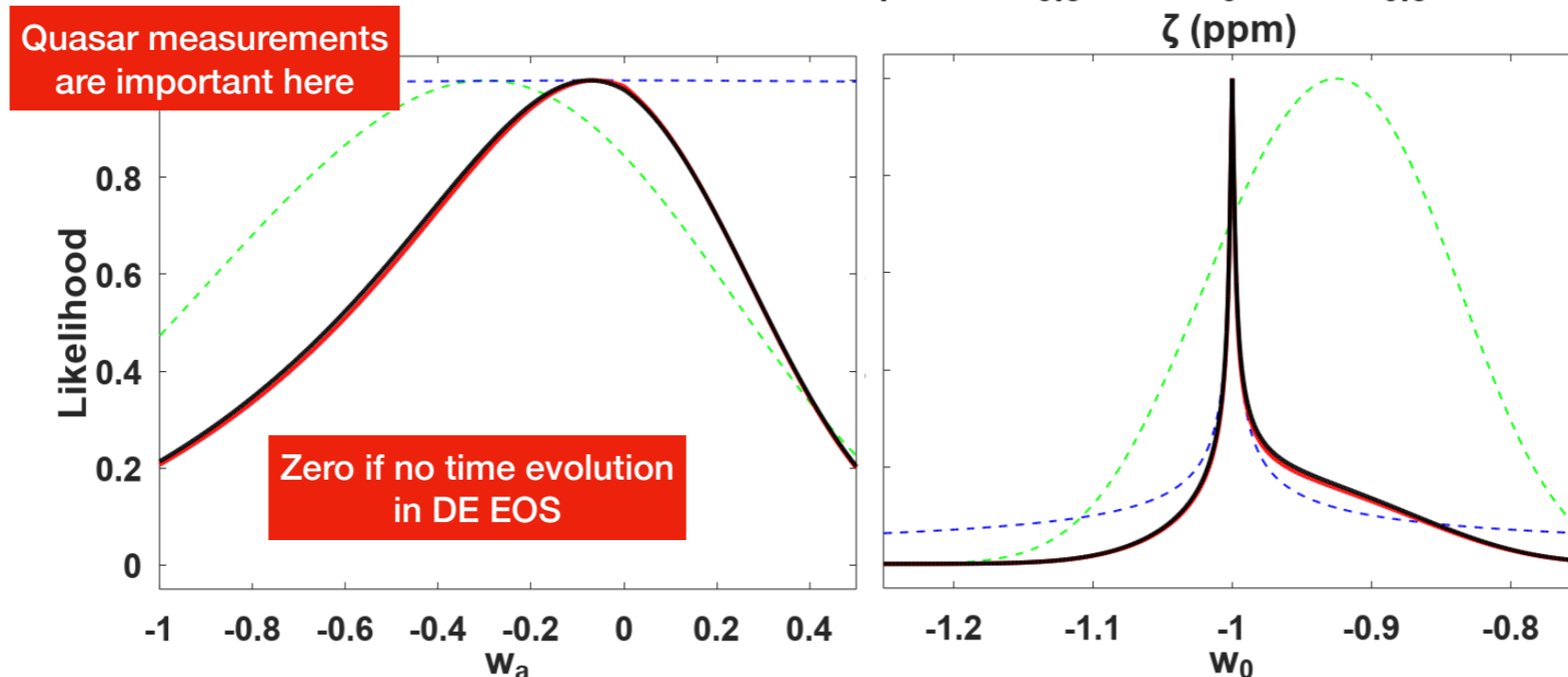
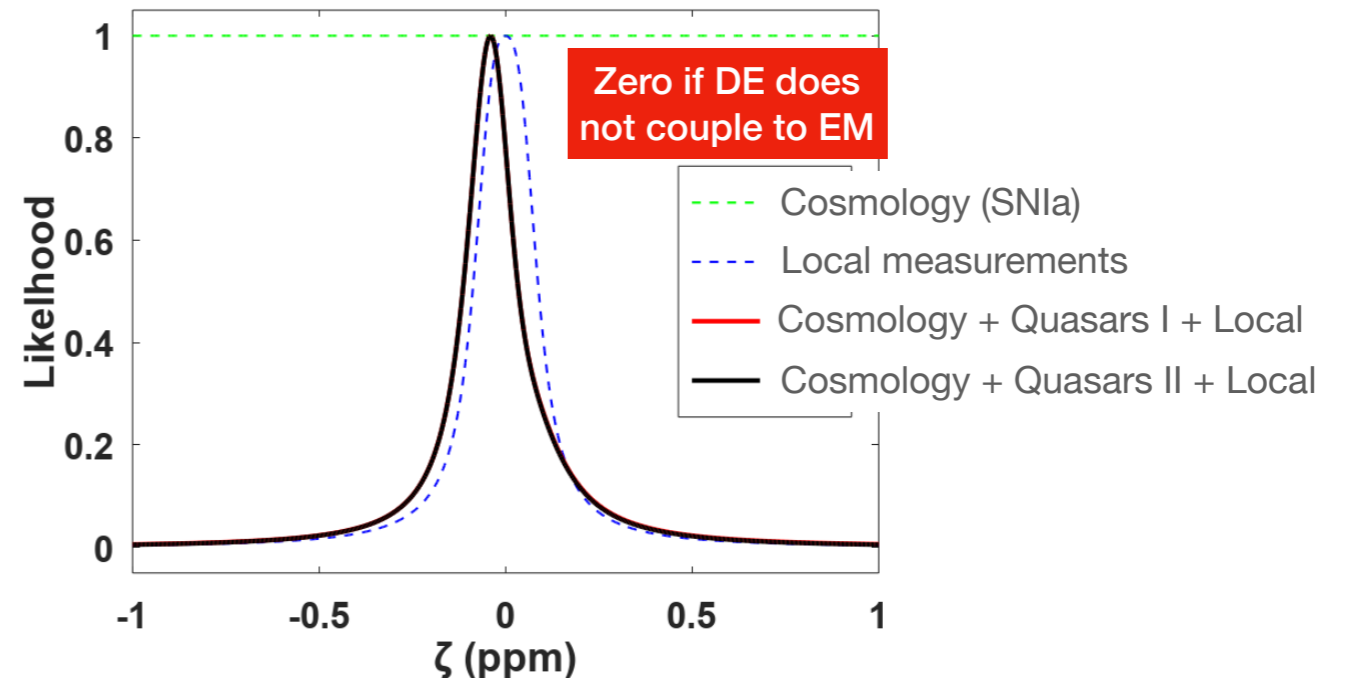
EM coupling      fractional DE density

$$\frac{\Delta\alpha}{\alpha}(z) = \pm\zeta \int_0^z \sqrt{3\Omega_\psi(z')|1+w_\psi(z')|} \frac{dz'}{1+z'}$$

+ for canonical fields  
- for phantom fields

DE equation of state

$$w_\psi = w_0 + w_a \frac{z}{1+z}$$



# Conclusions

- Fundamental constants are expected to vary in many extensions of SM and  $\Lambda$ CDM (Uzan 2011; Martins 2017, many talks here)
- Existing measurements provide some evidence for a  $4\sigma$  variation in  $\alpha$  but are dominated by instrumental systematics (King et al. 2012; Whitmore & Murphy 2016)
- Measurements where this systematic is not present see no variation (Milaković et al. 2021; Murphy et al. 2022)
- High-quality data from ESPRESSO@VLT is becoming available, new measurements using AI-VPFIT (Webb et al. 2022, Lee et al. 2022) are coming soon
- This project is one of the science drivers for the ELT and ANDES





# Do we need a model?

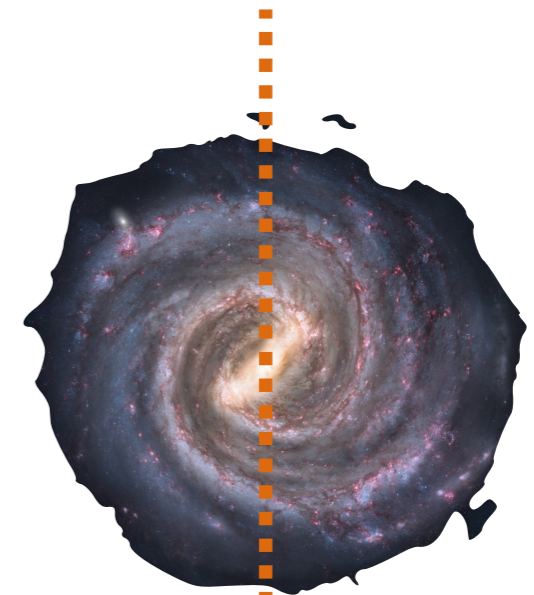
## Direct measurement of the expansion in real time

In FLRW metric, redshifts of distant objects change with time

Similar to, but different from, cosmic chronometers (M. Moresco's talk)



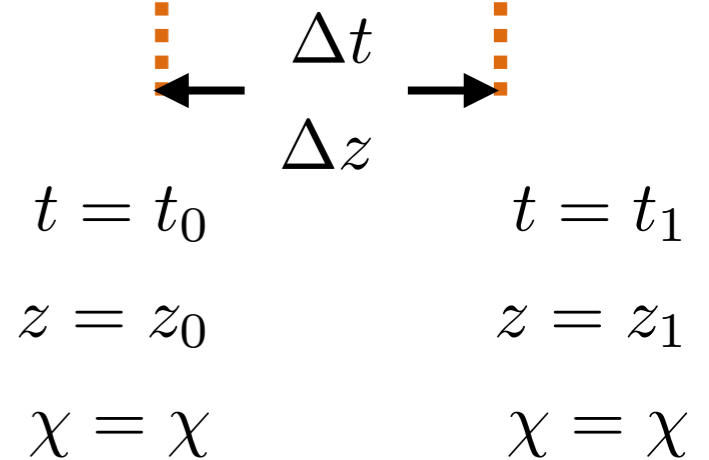
DISTANCE  $\chi$



$$1 + z(t_{obs}, t_{em}) = \frac{a(t_{obs})}{a(t_{em})}$$

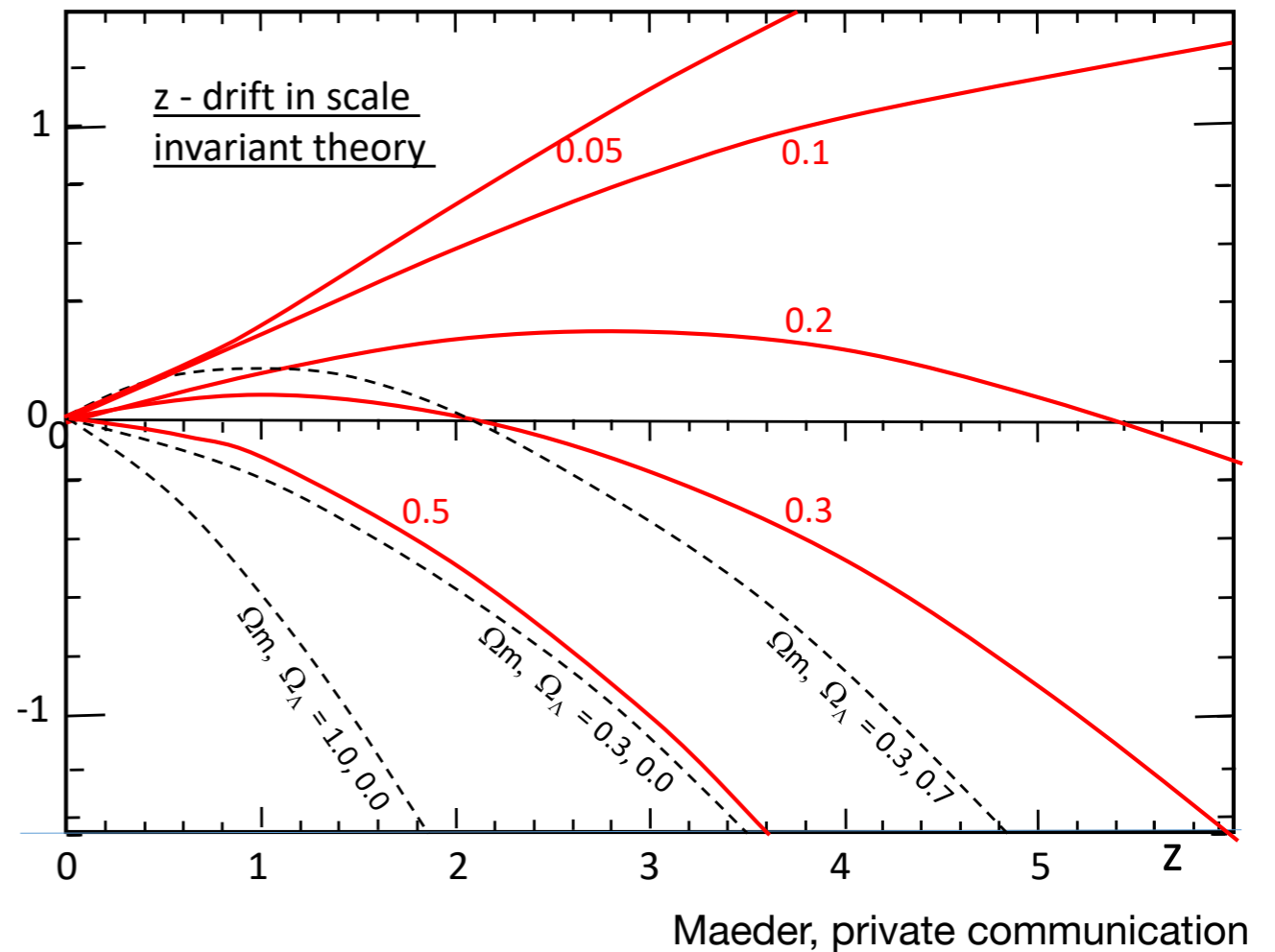
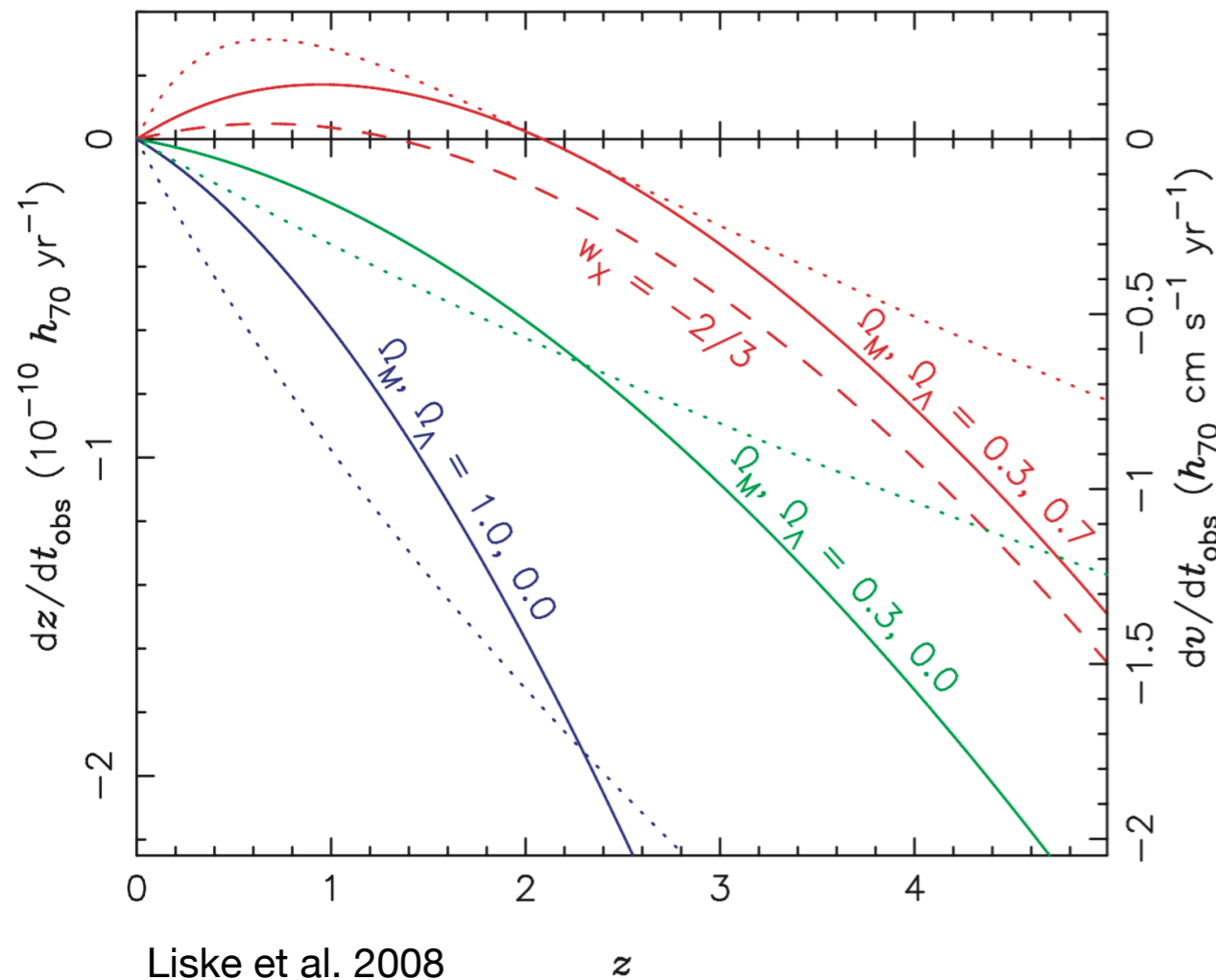
$$\frac{dz|_{\chi}}{dt_{obs}} = [1 + z|_{\chi}(t_{obs})]H(t_{obs}) - H(t_{em})$$

$$\frac{dz|_{\chi}}{dt_{obs}} \approx \frac{z|_{\chi}(t_{obs} + \Delta t_{obs}) - z|_{\chi}(t_{obs})}{\Delta t_{obs}}$$



# 10+ year project with the ELT and ANDES

Extremely difficult: line centre expected to shift by 0.01Å on the detector in 10 years



Ongoing project to observe two bright quasars with ESPRESSO with a baseline of 1 year