

# Testing tension with GR using the mass profiles of galaxy clusters



Lorenzo Pizzuti – OAVdA  
In collaboration with I. D. Saltas, K. Umetsu, L. Amendola, A. Biviano, B. Sartoris,

Tensions in Cosmology  
7<sup>th</sup> -12<sup>th</sup> September 2022

# Outline of the talk

---

- Kinematic and lensing mass profiles of a galaxy cluster
- The MG-MAMPOSSt code
  - Forecasts: kinematic + (weak) lensing
  - Application to CLASH clusters
- Conclusions

# Galaxy cluster mass profiles: dynamics vs lensing analysis

---

Spacetime of a galaxy cluster: linear perturbation of the Friedmann-Robertson-Walker metric

$$ds^2 = a^2(\tau) \left[ - \left( 1 + \frac{2\Phi}{c^2} \right) c^2 d\tau^2 + \left( 1 - \frac{2\Psi}{c^2} \right) dl^2 \right], \quad \Phi, \Psi \sim 10^{-4} c^2 \text{ gravitational potentials}$$

In standard GR:  $\Phi = \Psi \equiv \Phi_N$

$\Phi \neq \Psi \rightarrow$  Signatures of modified gravity

# Galaxy cluster mass profiles: dynamics vs lensing analysis

Spacetime of a galaxy cluster: linear perturbation of the Friedmann-Robertson-Walker metric

$$ds^2 = a^2(\tau) \left[ - \left( 1 + \frac{2\Phi}{c^2} \right) c^2 d\tau^2 + \left( 1 - \frac{2\Psi}{c^2} \right) dl^2 \right], \quad \Phi, \Psi \sim 10^{-4} c^2 \text{ gravitational potentials}$$

In standard GR:  $\Phi = \Psi \equiv \Phi_N$

$\Phi \neq \Psi \rightarrow$  Signatures of modified gravity

Motion of galaxies (kinematic analysis)



**TIME-TIME** component of the metric  $\Phi$

Photons (lensing analysis)



**TIME-TIME** + **SPACE-SPACE** components of the metric  $\Phi_{lens} = \frac{1}{2} (\Phi + \Psi)$

# Galaxy cluster mass profiles: dynamics vs lensing analysis

Spacetime of a galaxy cluster: linear perturbation of the Friedmann-Robertson-Walker metric

$$ds^2 = a^2(\tau) \left[ - \left( 1 + \frac{2\Phi}{c^2} \right) c^2 d\tau^2 + \left( 1 - \frac{2\Psi}{c^2} \right) dl^2 \right], \quad \Phi, \Psi \sim 10^{-4} c^2 \text{ gravitational potentials}$$

In standard GR:  $\Phi = \Psi \equiv \Phi_N$

$\Phi \neq \Psi \rightarrow$  Signatures of modified gravity

Motion of galaxies (kinematic analysis)



**TIME-TIME** component of the metric  $\Phi$

Photons (lensing analysis)



**TIME-TIME** + **SPACE-SPACE** components of the metric  $\Phi_{lens} = \frac{1}{2} (\Phi + \Psi)$

**LENSING** AND **KINEMATIC** DETERMINATIONS OF A GALAXY CLUSTER MASS PROFILE  
COULD BE USED TO DETECT POSSIBLE SIGNATURES OF MODIFIED GRAVITY

# The MG-MAMPOSSt code

Version of the **MAMPOSSt** code aimed at constraining modified gravity models using the internal kinematic of galaxy clusters

**MAMPOSSt**= *Modelling Anisotropy and Mass Profile of Observed Spherical System*

Developed Mamon, Biviano, Boué (MNRAS 429 (Mar., 2013)3079–3098) to derive cluster mass profiles by the analysis of galaxies kinematics

# The MG-MAMPOSSt code

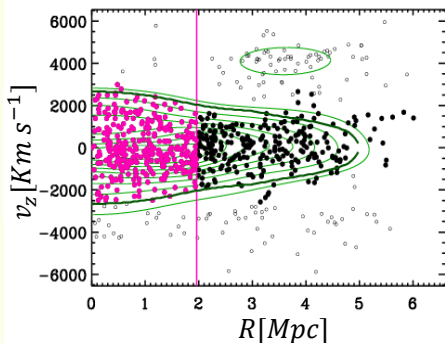
Version of the **MAMPOSSt** code aimed at constraining modified gravity models using the internal kinematic of galaxy clusters

**MAMPOSSt**= *Modelling Anisotropy and Mass Profile of Observed Spherical System*

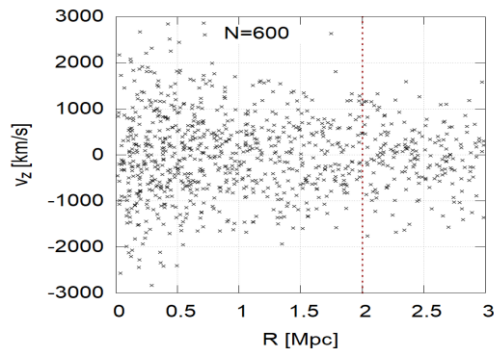
Developed Mamon, Biviano, Boué (MNRAS 429 (Mar., 2013)3079–3098) to derive cluster mass profiles by the analysis of galaxies kinematics

Jeans' equation solved in the **projected phase-space** ( $R, v_z$ )

Real cluster MACS 1206 (Biviano et al., 2013)



Synthetic cluster N=600 (Pizzuti et al., 2021)



# The MG-MAMPOSSt code

Version of the **MAMPOSSt** code aimed at constraining modified gravity models using the internal kinematic of galaxy clusters

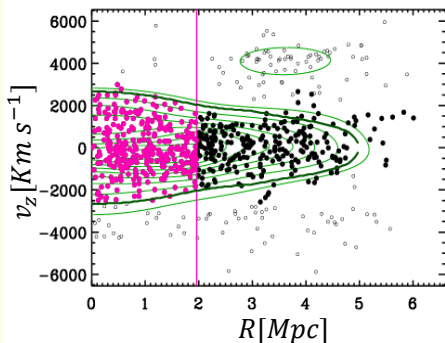
**MAMPOSSt**= *Modelling Anisotropy and Mass Profile of Observed Spherical System*

Developed Mamon, Biviano, Boué (MNRAS 429 (Mar., 2013)3079–3098) to derive cluster mass profiles by the analysis of galaxies kinematics

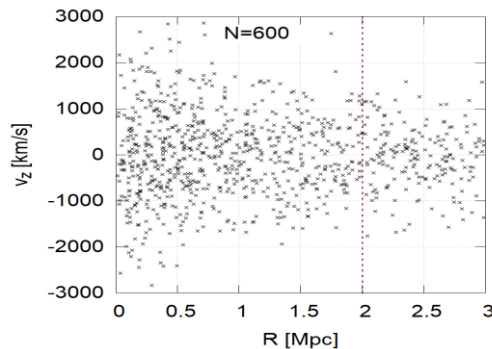
Jeans' equation solved in the **projected phase-space** ( $R, v_z$ )

maximum likelihood fit to obtain the parameters of the mass profile and the anisotropy profile assuming a 3D velocity Gaussian distribution

Real cluster MACS 1206 (Biviano et al., 2013)



Synthetic cluster N=600 (Pizzuti et al., 2021)





# The MG-MAMPOSSt code

Version of the **MAMPOSSt** code aimed at constraining modified gravity models using the internal kinematic of galaxy clusters

$$\sigma_r^2(r) = \frac{1}{v(r)} \int_r^\infty ds \exp \left[ 2 \int_r^s \frac{\beta(t)}{t} dt \right] v(s) \frac{d\Phi}{ds}$$

parameter space:  $r_s, r_{200}, r_v, \beta$

$\beta \rightarrow$  free parameter of the anisotropy profile

$r_v \rightarrow$  scale radius of the number density profile

**MG-MAMPOSSt:**

# The MG-MAMPOSSt code

Version of the **MAMPOSSt** code aimed at constraining modified gravity models using the internal kinematic of galaxy clusters

$$\sigma_r^2(r) = \frac{1}{v(r)} \int_r^\infty ds \exp \left[ 2 \int_r^s \frac{\beta(t)}{t} dt \right] v(s) \frac{d\Phi}{ds}$$

parameter space:  $r_s, r_{200}, r_v, \beta, \mathcal{M}_1, \mathcal{M}_2$

$\beta \rightarrow$  free parameter of the anisotropy profile

$r_v \rightarrow$  scale radius of the number density profile

## MG-MAMPOSSt:

- Chameleon screening, Vainshtein screening
- modified Newtonian potential (Navarro-Frenk-White)

$$\mathcal{M}_i = \begin{cases} Y_1, Y_2 & VS \\ Q, \phi_\infty & CS \end{cases}$$

# The MG-MAMPOSSt code

Version of the **MAMPOSSt** code aimed at constraining modified gravity models using the internal kinematic of galaxy clusters

$$\sigma_r^2(r) = \frac{1}{v(r)} \int_r^\infty ds \exp \left[ 2 \int_r^s \frac{\beta(t)}{t} dt \right] v(s) \frac{d\Phi}{ds}$$

parameter space:  $r_s, r_{200}, r_v, \beta, \mathcal{M}_1, \mathcal{M}_2$

$\beta \rightarrow$  free parameter of the anisotropy profile

$r_v \rightarrow$  scale radius of the number density profile

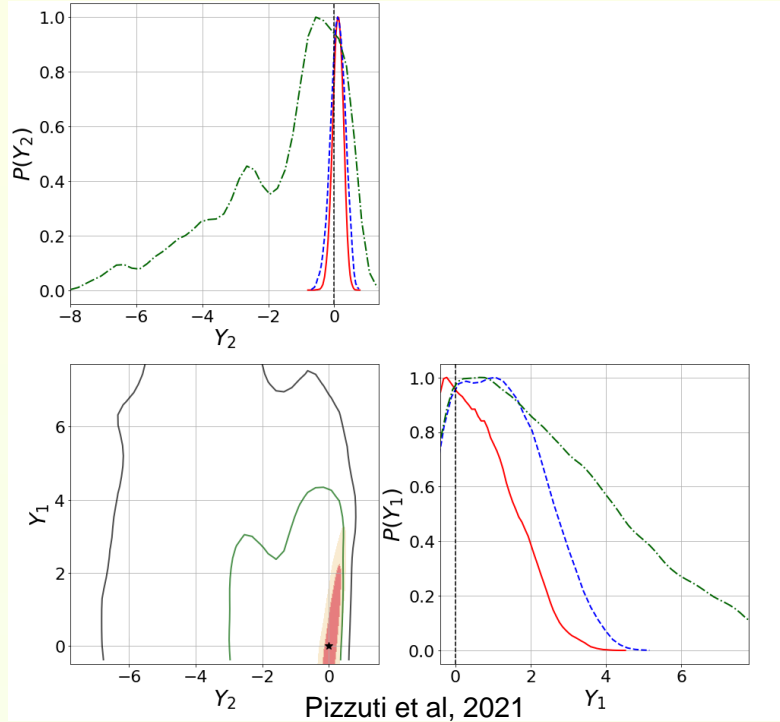
## MG-MAMPOSSt:

- Chameleon screening, Vainshtein screening
- modified Newtonian potential (Navarro-Frenk-White)
- Grid /MCMC (Metropolis-Hastings) parameter space exploration. **Few hours for a complete MCMC run.**
- Simulated (weak) lensing information

$$\mathcal{M}_i = \begin{cases} Y_1, Y_2 & VS \\ Q, \phi_\infty & CS \end{cases}$$

# Forecasts: Vainshtein screening

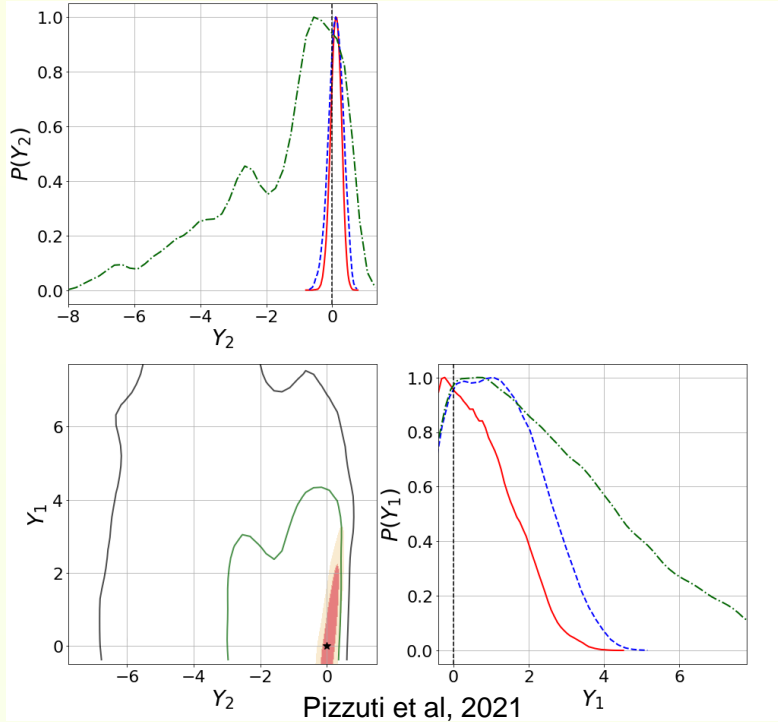
One cluster: (weak) lensing + kinematics  
(600 tracers and 100 tracers)



$N_h$ clusters	$N = 600$ (joint)		$N = 100$ (joint)	
	$Y_1$	$Y_2$	$Y_1$	$Y_2$
1	$\lesssim 2.75$	$0.08^{+0.32}_{-0.28}$	$\lesssim 3.56$	$0.10^{+0.44}_{-0.40}$
5	$\lesssim 1.65$	$0.06^{+0.20}_{-0.18}$	$\lesssim 1.87$	$-0.08^{+0.31}_{-0.20}$
10	$\lesssim 1.24$	$-0.05^{+0.17}_{-0.13}$	$\lesssim 1.65$	$0.01^{+0.24}_{-0.17}$
15	$0.04^{+1.00}_{-0.39}$	$0.01^{+0.12}_{-0.09}$	$\lesssim 1.20$	$-0.01^{+0.19}_{-0.16}$
20	$0.08^{+0.77}_{-0.34}$	$0.01^{+0.09}_{-0.08}$	$\lesssim 1.02$	$0.01^{+0.16}_{-0.14}$

# Forecasts: Vainshtein screening

One cluster: (weak) lensing + kinematics  
(600 tracers and 100 tracers)



$N_h$ clusters	$N = 600$ (joint)		$N = 100$ (joint)	
	$Y_1$	$Y_2$	$Y_1$	$Y_2$
1	$\lesssim 2.75$	$0.08^{+0.32}_{-0.28}$	$\lesssim 3.56$	$0.10^{+0.44}_{-0.40}$
5	$\lesssim 1.65$	$0.06^{+0.20}_{-0.18}$	$\lesssim 1.87$	$-0.08^{+0.31}_{-0.20}$
10	$\lesssim 1.24$	$-0.05^{+0.17}_{-0.13}$	$\lesssim 1.65$	$0.01^{+0.24}_{-0.17}$
15	$0.04^{+1.00}_{-0.39}$	$0.01^{+0.12}_{-0.09}$	$\lesssim 1.20$	$-0.01^{+0.19}_{-0.16}$
20	$0.08^{+0.77}_{-0.34}$	$0.01^{+0.09}_{-0.08}$	$\lesssim 1.02$	$0.01^{+0.16}_{-0.14}$

# Example: DHOST – real data

MG-MAMPOSSt applied to p.p.s. of two massive clusters analysed within the **CLASH** and **CLASH-VLT** collaborations

MACSJ-1206



Credits: Biviano et al., 2013

⇒ Subaru+HST

⇒ VLT/VIMOS+MUSE

Abell S1063

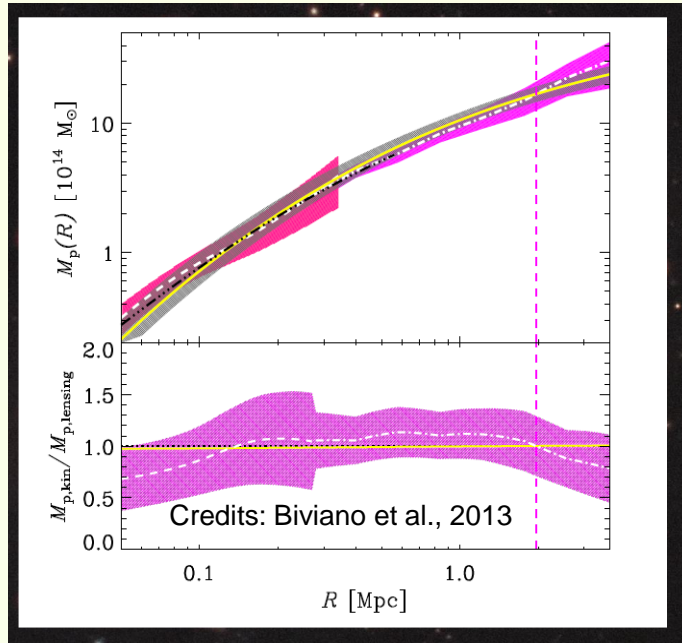


Credits: Sartoris et al., 2021

# Example: DHOST – real data

MG-MAMPOSSt applied to p.p.s. of two massive clusters analysed within the **CLASH** and **CLASH-VLT** collaborations

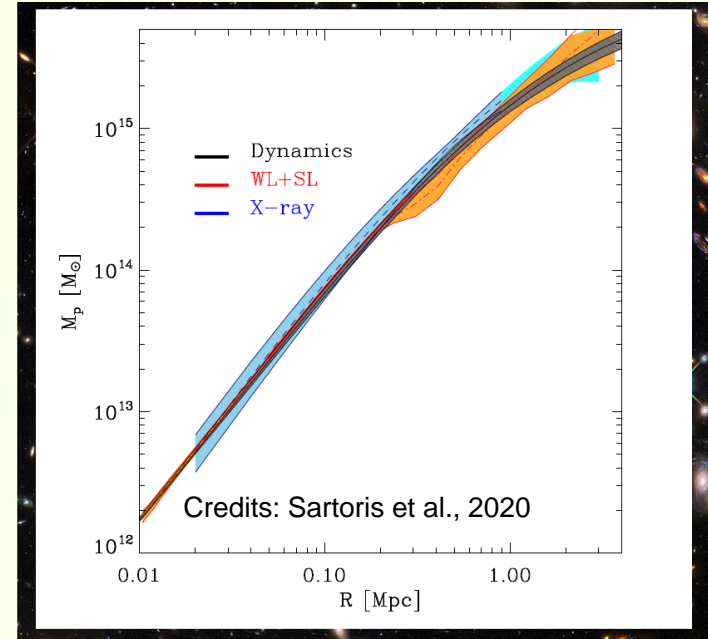
MACSJ-1206



➔ Subaru+HST

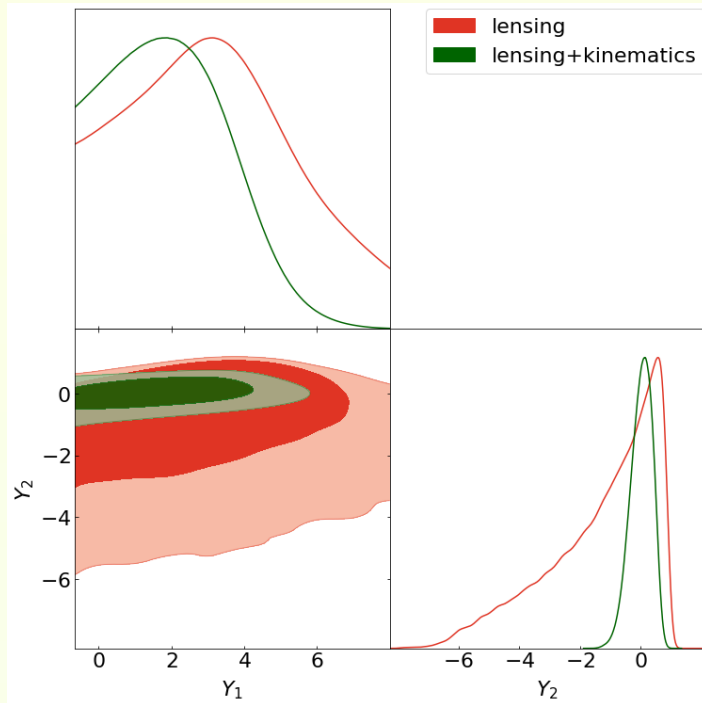
➔ VLT/VIMOS+MUSE

Abell S1063

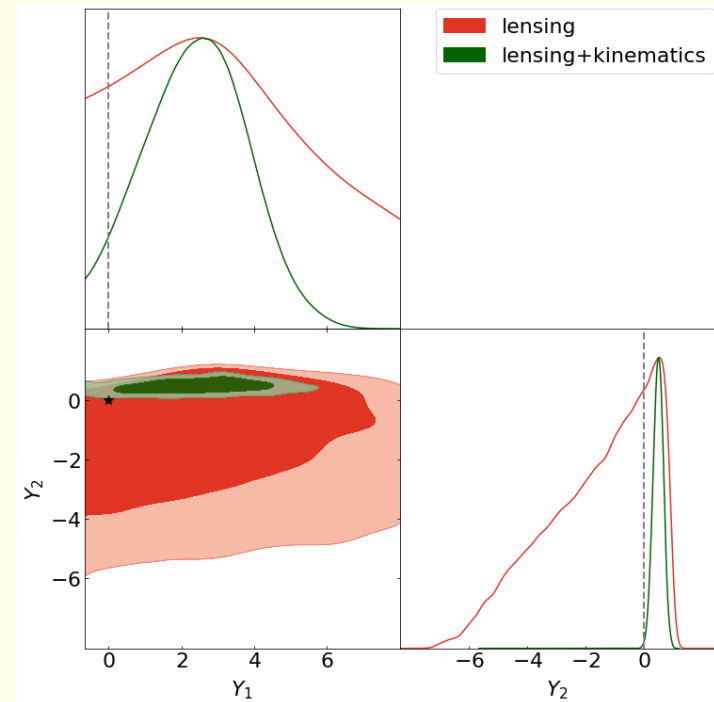


# Example: DHOST – real data

MACSJ-1206



Abell S1063

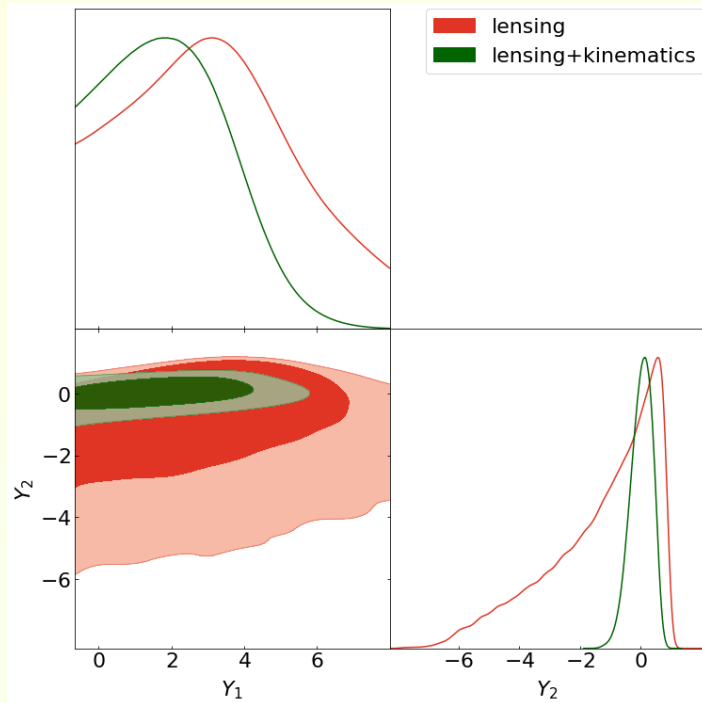


Pizzuti et al, 2022a

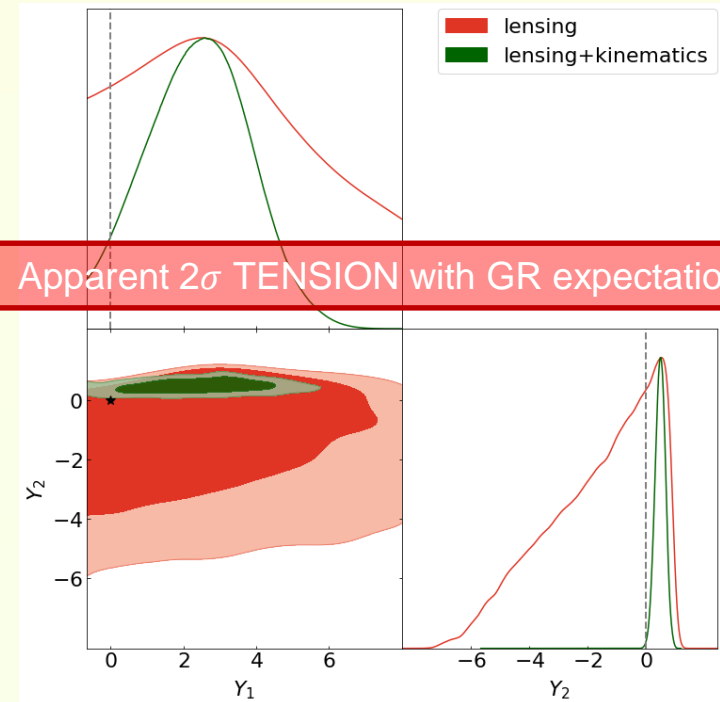


# Example: DHOST – real data

MACSJ-1206



Abell S1063



Pizzuti et al, 2022a

# Understanding the systematics: cosmological simulations

---

In a GR Universe  $\sim 70\%$  of the cluster population leads to spurious detections of MG

**2 observational criteria related to systematics** DIRECTLY from the projected phase space (pps)

**Anderson-Darling coefficient  $A^2$**   $\rightarrow$  deviations from Gaussianity of the los velocity distribution:

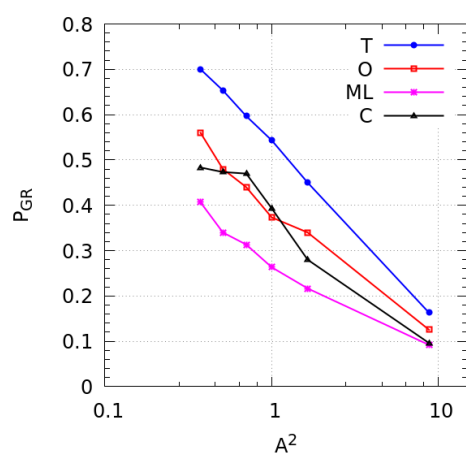
$$A^2 = -n - \frac{1}{n} \sum_{i=1}^n (2i - 1) [\ln \Phi(x_i) + \ln(1 - \Phi(x_{n+1-i}))]$$

$\chi^2$  from fitting the projected number density with a pNFW profile  $\rightarrow$

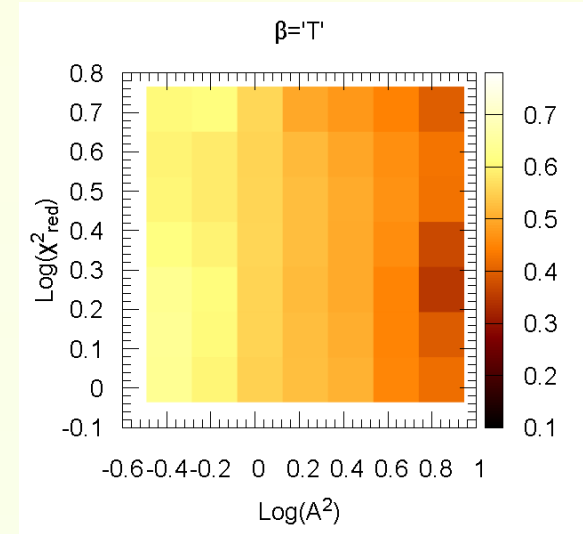
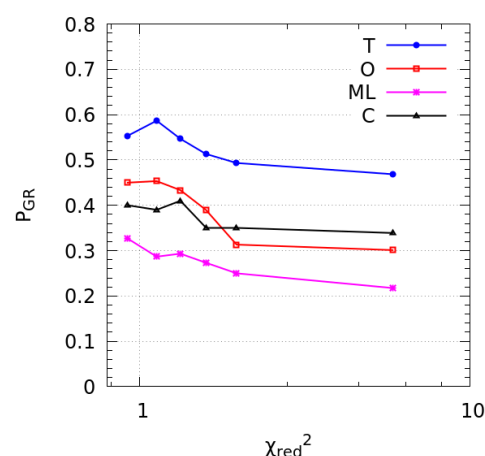
- deviations from sph. symmetry,
- parametrization of the profile,
- substructures in the pps

# Understanding the systematics: cosmological simulations

Systematics related to the lack of the main assumptions: **dynamical relaxation** and **sph. symmetry**  
 $A^2, \chi_v^2 \rightarrow$  help in selecting suitable halos



Pizzuti et al., 2021

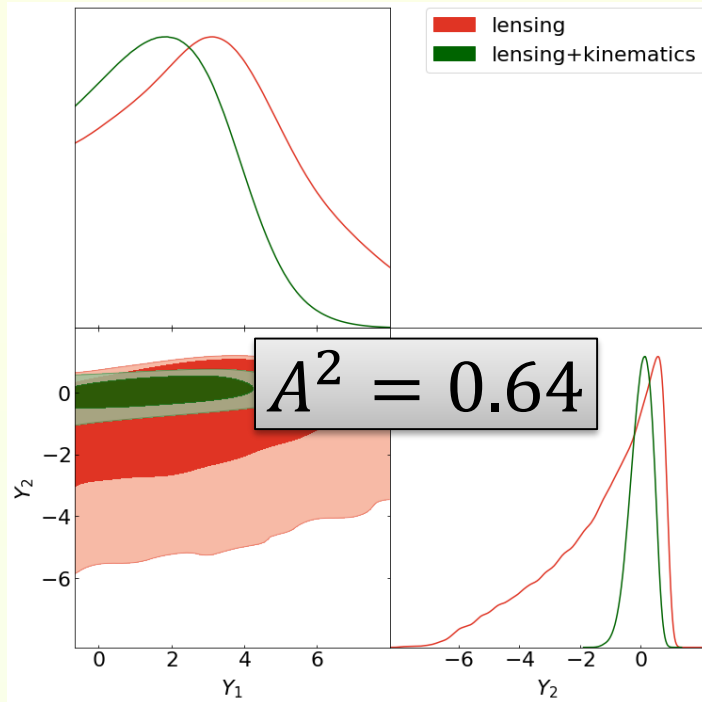


Percentage of spurious detection lowered **down to ~ 20%** for  $A^2 < 1, \chi_{red}^2 < 0.5$

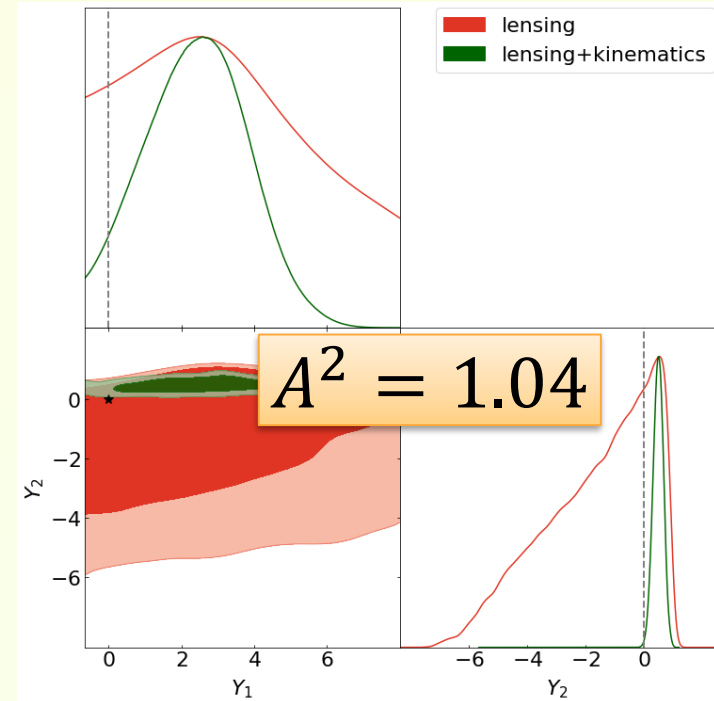
**TREND INDEPENDENT OF THE ANISOTROPY MODEL**

# Example: DHOST – real data

MACSJ-1206



Abell S1063



Pizzuti et al, 2022a

# Summary and conclusions

---

- **MG-MAMPOSSt**: powerful tool to constrain modified gravity models **when combined with other probes** (such as lensing information). Available on <https://github.com/Pizzuti92/MG-MAMPOSSt/>
- Applied in the case of **Vainsthein screening (DHOST)** to CLASH clusters:  $Y_2 \sim -0.12^{+0.66}_{-0.67}$  for MACS 1206
- **Apparent tension with GR expectation  $Y_2 = 0$**  for Abell S1063 which can be **fully explained in terms of systematics**

## NEXT...

- A few (suitable) dozen clusters are sufficient to bring down the uncertainties by one order of magnitude  
Accurate systematics calibration is necessary!
- Explore other mass parametrisations and new models (work in progress!)



Thanks for your attention

# That's all Folks!

