

# Exotic opportunities in cryogenic helium

## Flow of normal and superfluid helium due to submerged oscillating objects

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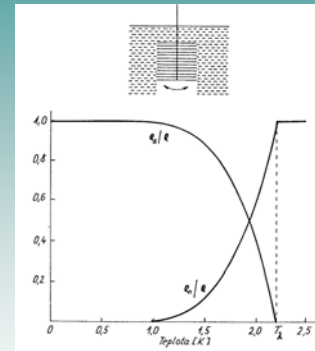
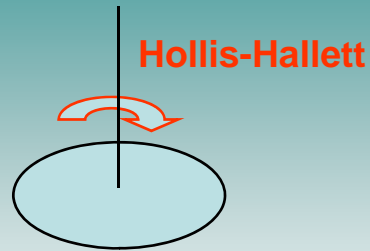
V Holešovičkách 2, 180 00 Prague 8,, Czech Republic



EUTUCHE Meeting, CERN, 2007

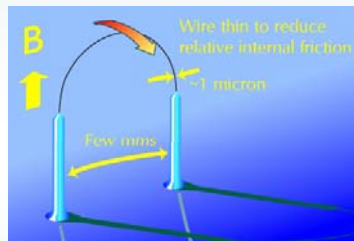
# Oscillating objects used in experiments in He II and in $^3\text{He}$

Discs and piles of discs



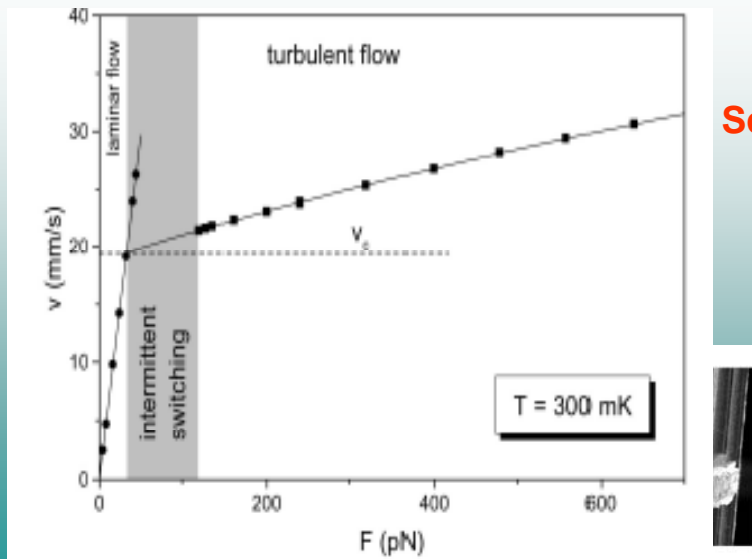
Andronikashvili

Wires  
He II and  $^3\text{He}$



Many authors – vibrating wire viscometers  
Vinen

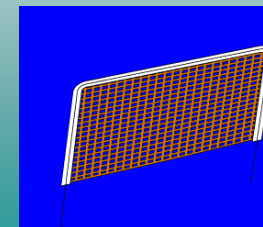
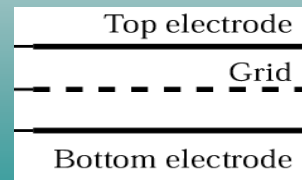
Morishita, Kuroda, Sawada, Satoh, *JLTP* **76**, 387 (1989)  
Lancaster – Pickett's group, Osaka – Yano et al.,  
Kosice Skyba et al., Moscow Dmitriev et al.,  
Helsinki- YKI group..., Grenoble Bunkov et al., ...



Lancaster – P. McClintock's group

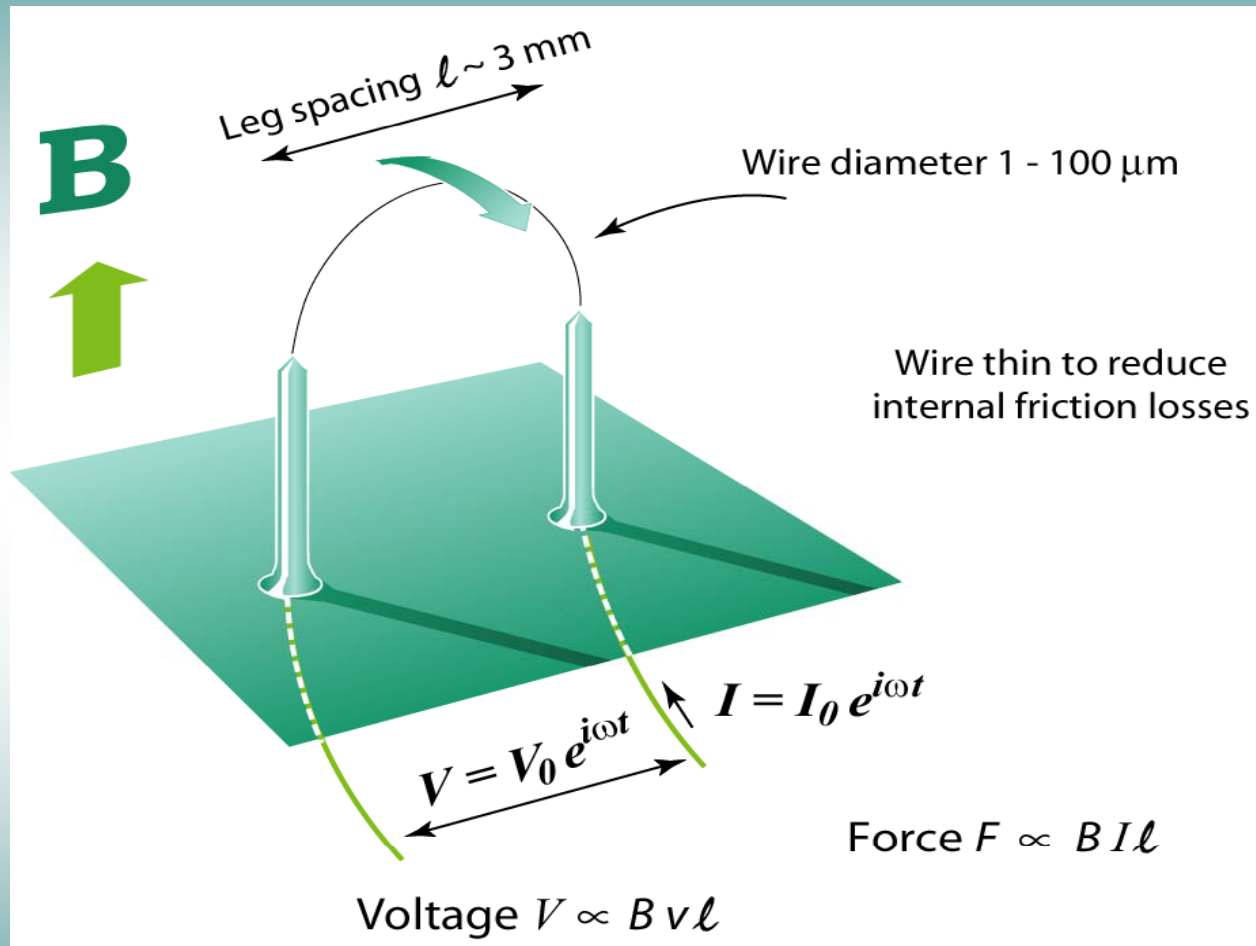


Lancaster – G. Pickett's group

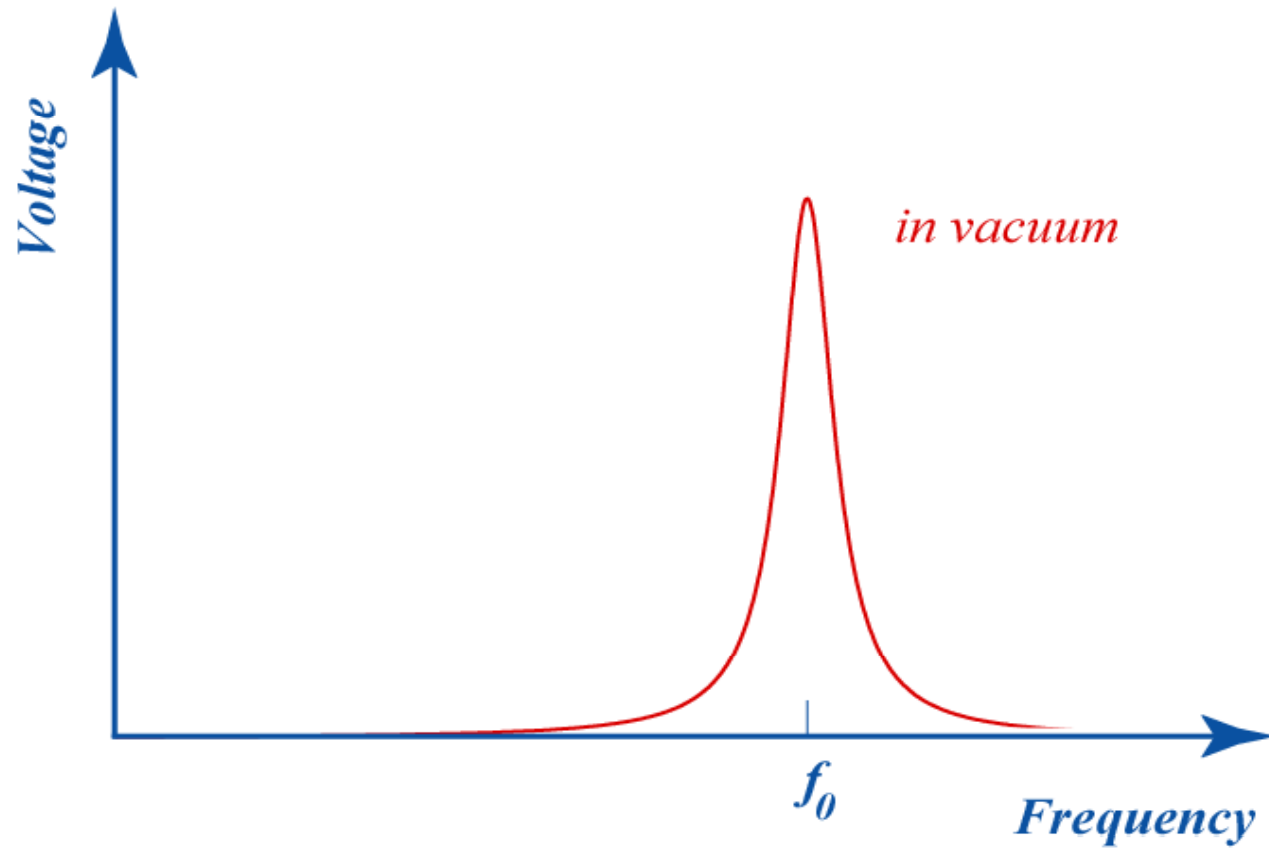


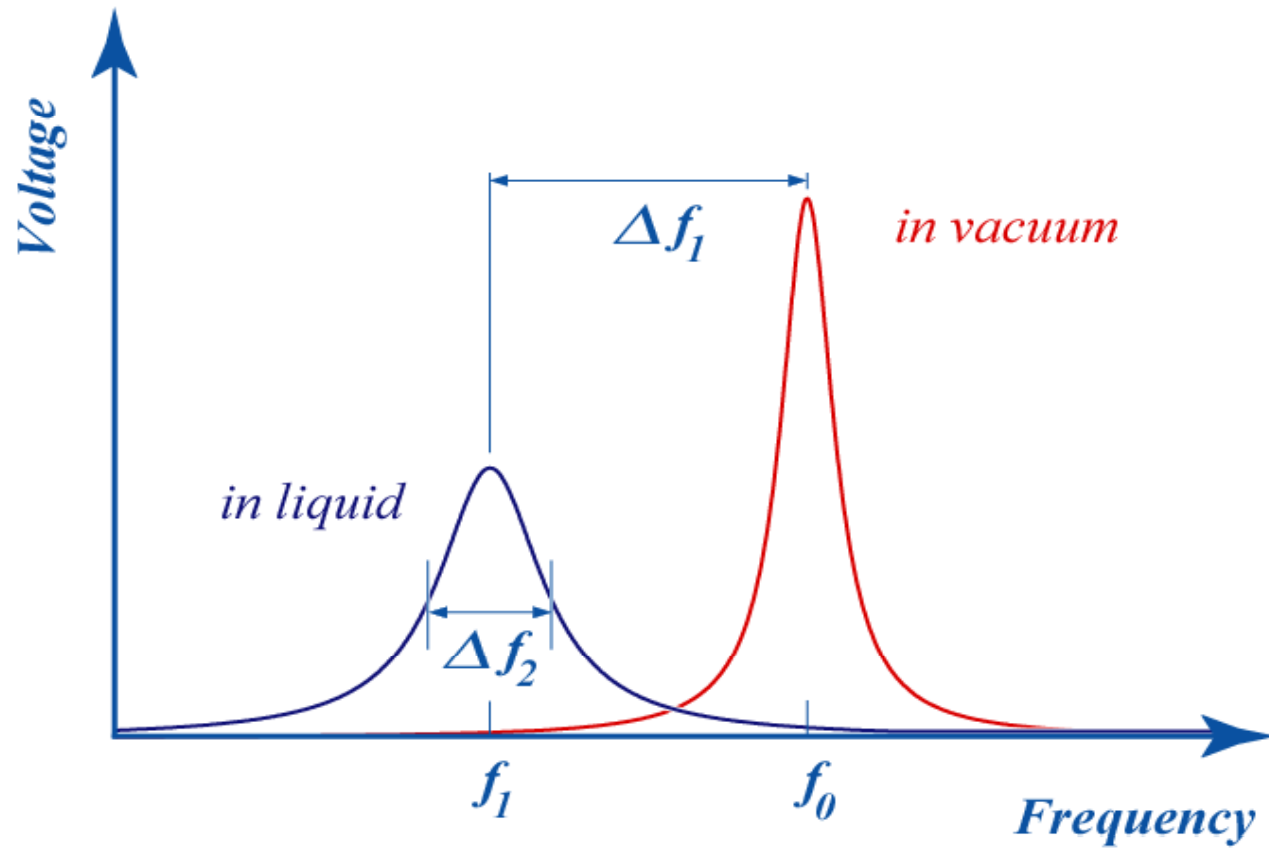
# Vibrating wires Lancaster, Helsinki, Kosice, Osaka, Grenoble....

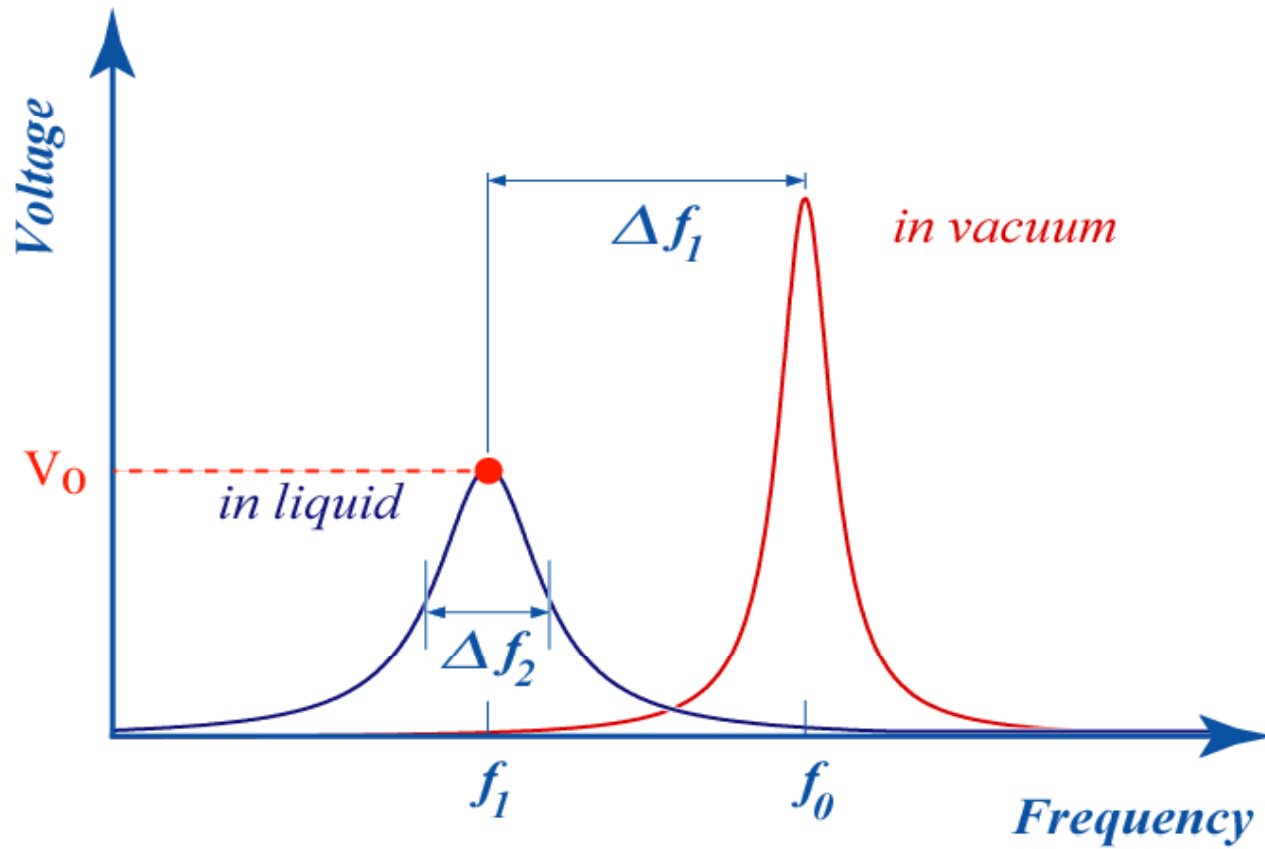
Both in He II and 3He, in mixtures



Note: care must be taken in order to distinguish between “superfluid” and “superconducting” effects, as applied magnetic field is usually of order of  $B_{c1}$  of the superconducting wire !

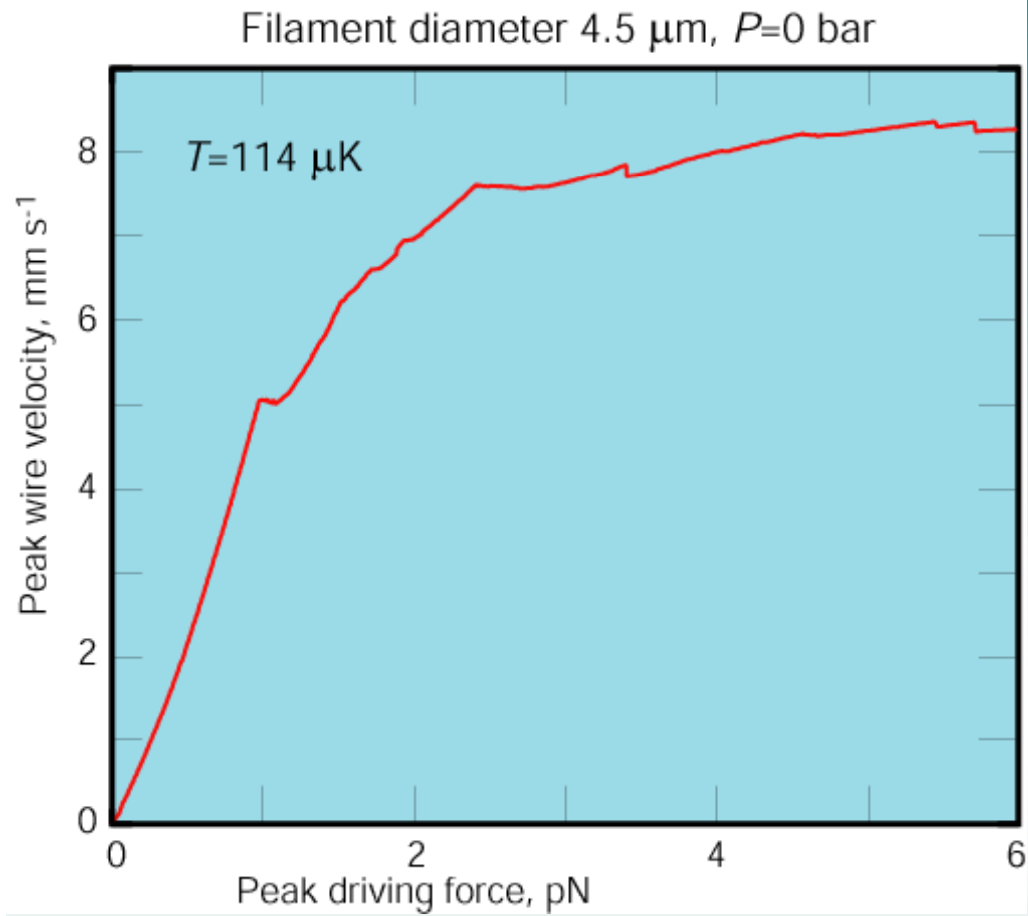






Resonant Signal Voltage,  $V_0 \sim 1/\Delta f_2$

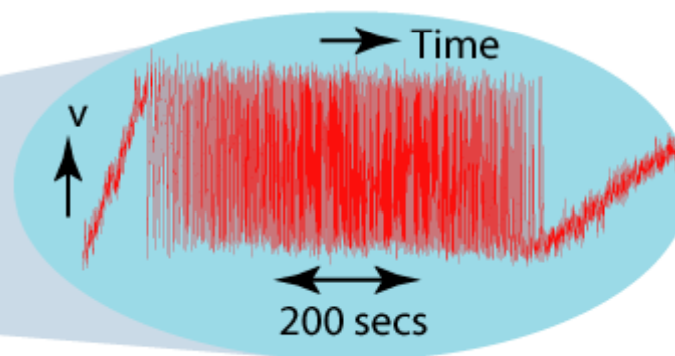
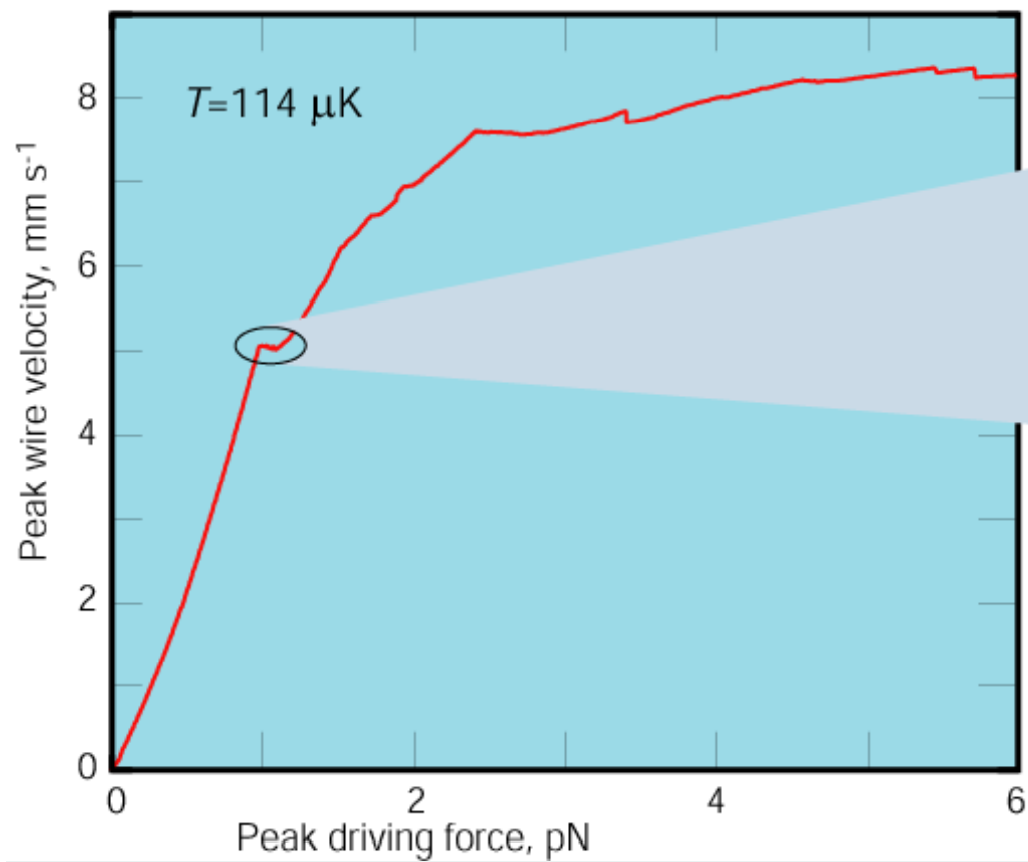
## Single vortex creation



Superfluid  $^3\text{He}$  B-phase  
 $P=0$  bar  
 $T \sim 110 - 300$  mK

Filament diameter  $4.5 \mu\text{m}$ ,  $P=0$  bar

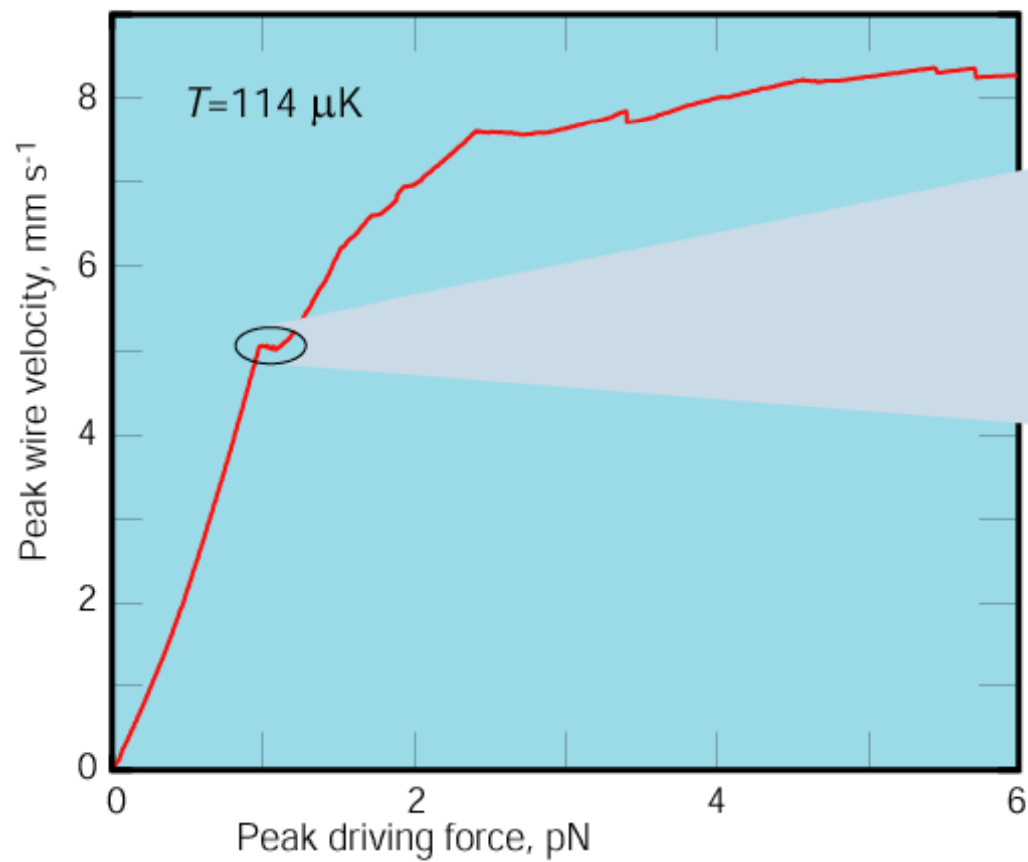
Single vortex creation



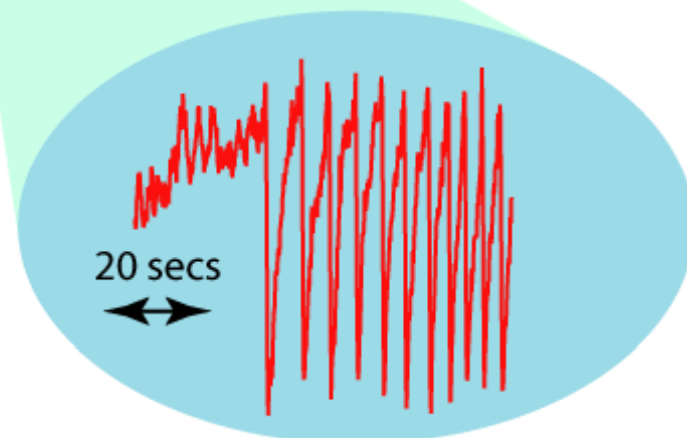
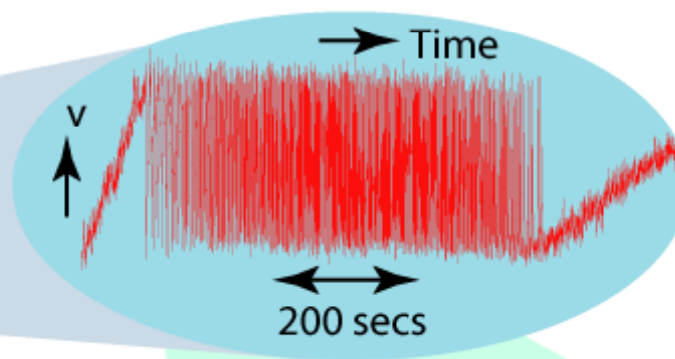


Filament diameter  $4.5 \mu\text{m}$ ,  $P=0$  bar

Single vortex creation

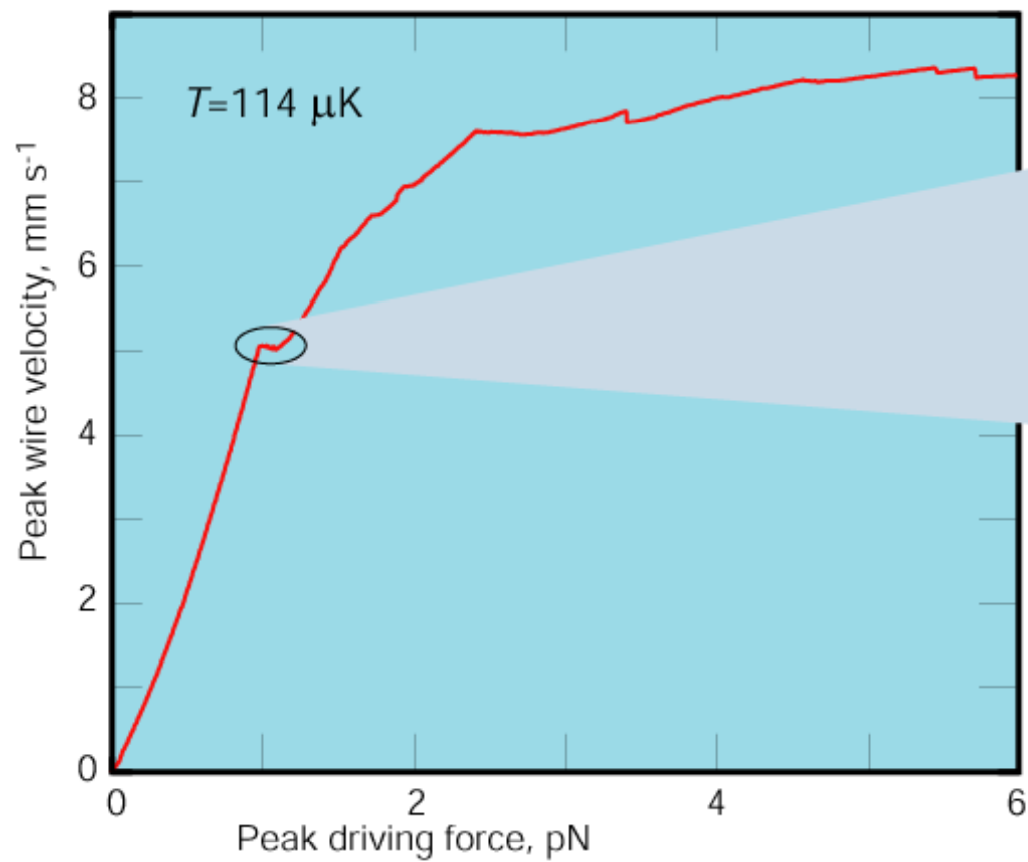


D I Bradley, *Phys. Rev. Lett.* **84**, 1252, 2000

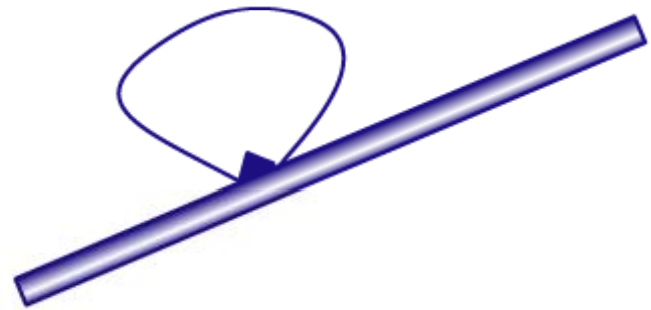
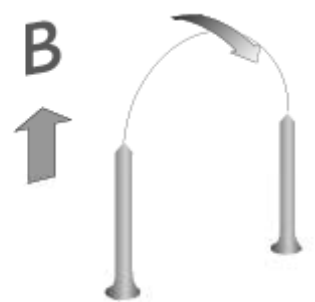
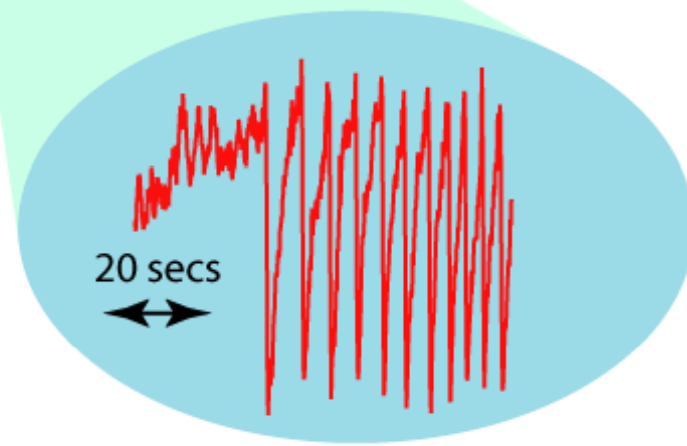
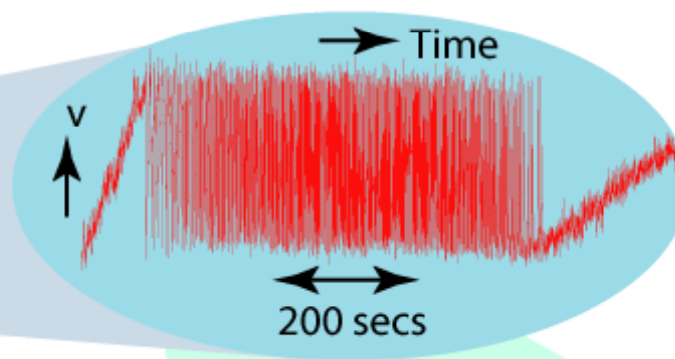


Filament diameter  $4.5 \mu\text{m}$ ,  $P=0$  bar

## Single vortex creation

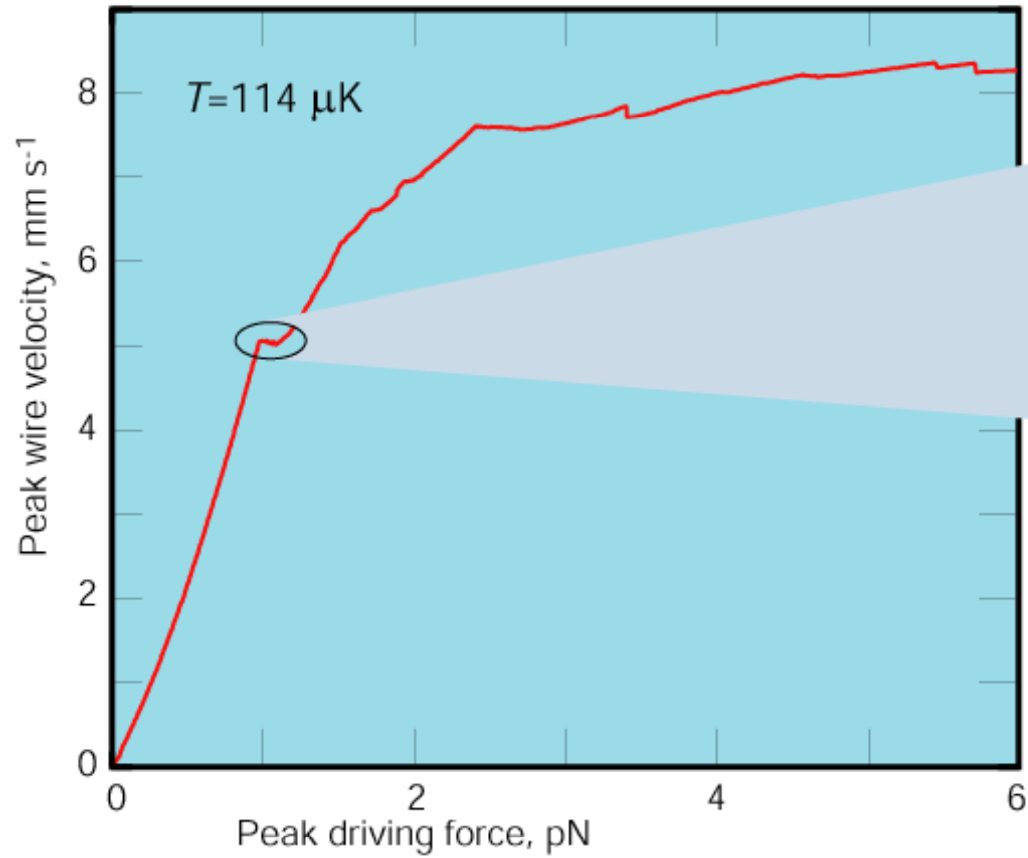


D I Bradley, *Phys. Rev. Lett.* **84**, 1252, 2000

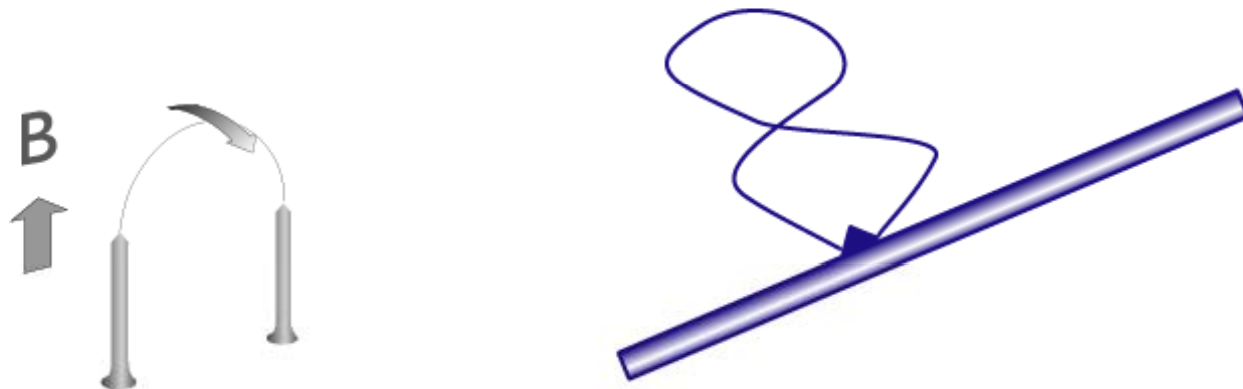
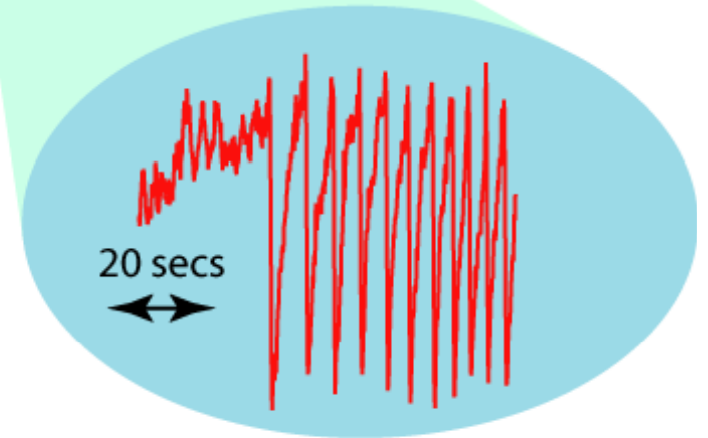
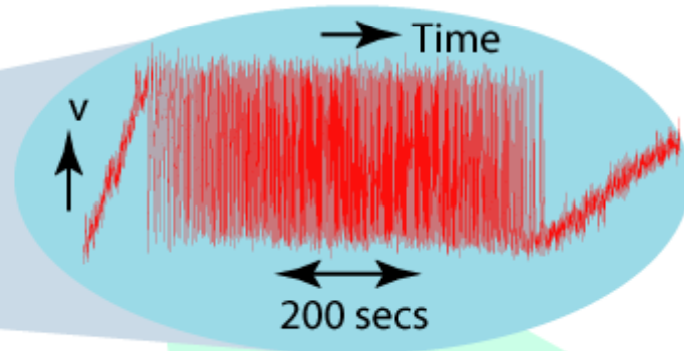


Filament diameter  $4.5 \mu\text{m}$ ,  $P=0$  bar

## Single vortex creation

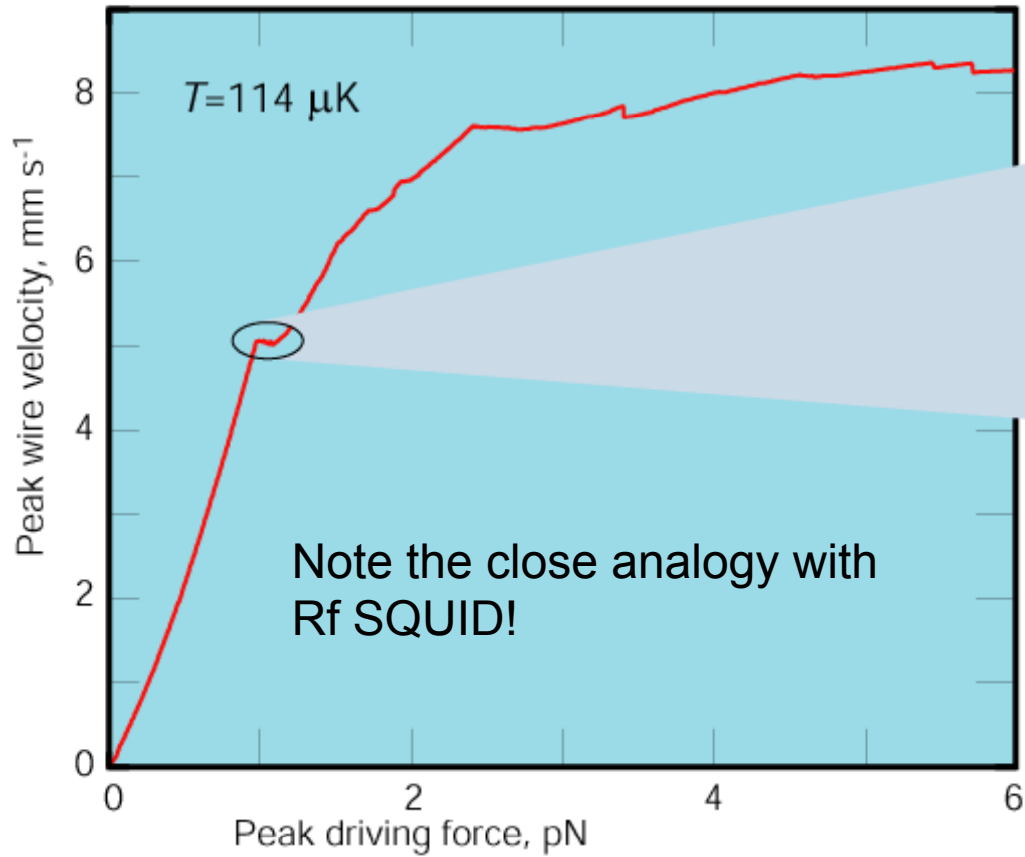


D I Bradley, *Phys. Rev. Lett.* **84**, 1252, 2000



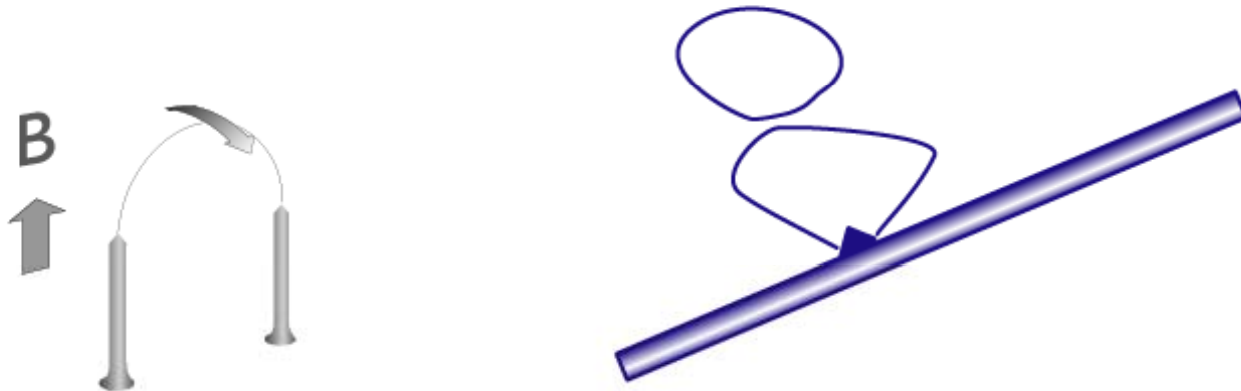
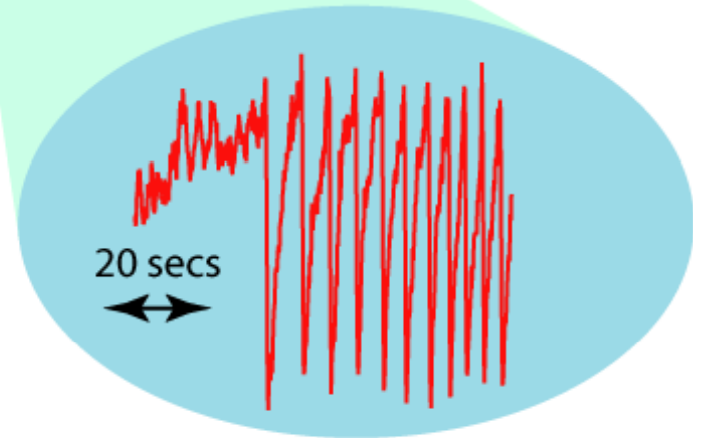
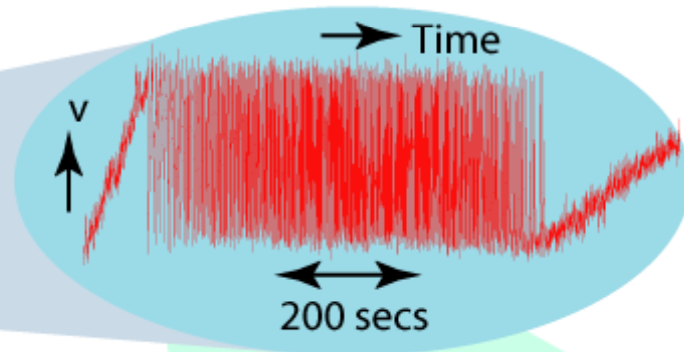
Filament diameter  $4.5 \mu\text{m}$ ,  $P=0$  bar

## Single vortex creation



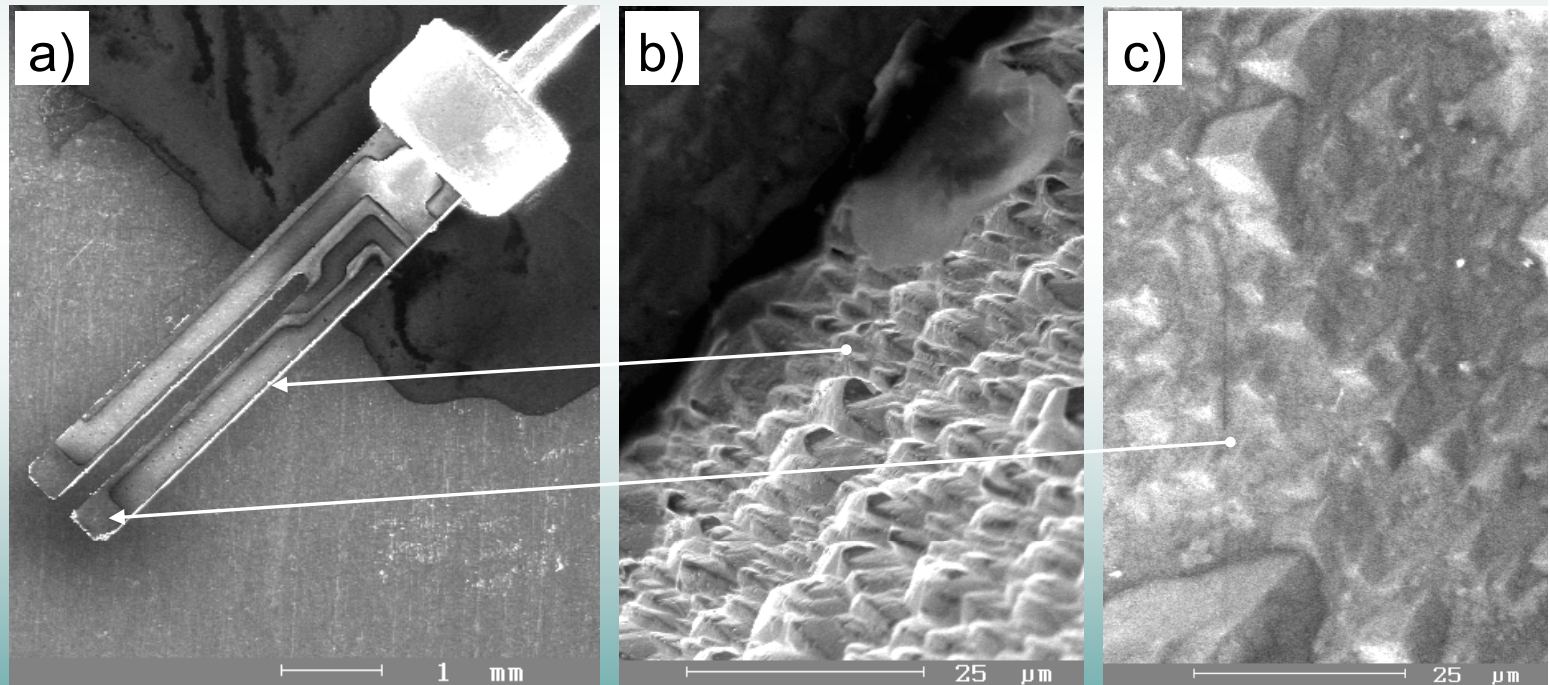
Note the close analogy with Rf SQUID!

D I Bradley, *Phys. Rev. Lett.* **84**, 1252, 2000



## Quartz tuning forks –

- Commercially produced piezoelectric oscillators, used as frequency standards in watches ( $2^{15}$  Hz = 32 768 Hz at room temperature)
- New addition to a family of oscillating objects, a probe to investigate physical properties of cryogenic fluids, especially gaseous He, He I, He II and  $^3\text{He-B}$
- Cheap, robust, widely available, easy to install and use, extremely sensitive ( $Q \approx 10^5 - 10^6$  in vacuum at low T)



An electron micrograph of the quartz tuning fork (a) and details of its side (b) and top (c) quartz surface.

# Oscillations of a submerged body in a viscous fluid

Simple harmonic oscillator:

$$m\ddot{x} + \underbrace{\gamma}_{\text{damping}}\dot{x} + kx = F_0 \cos(\omega t) \leftarrow \text{harmonic drive}$$

Damping in a Newtonian viscous fluid:

$$F_{damp} = \underbrace{\Delta m}_{\text{hydrodynamic mass enhancement}}\ddot{x} + \gamma\dot{x} \leftarrow \text{viscous drag}$$

These depend on liquid density and viscosity.

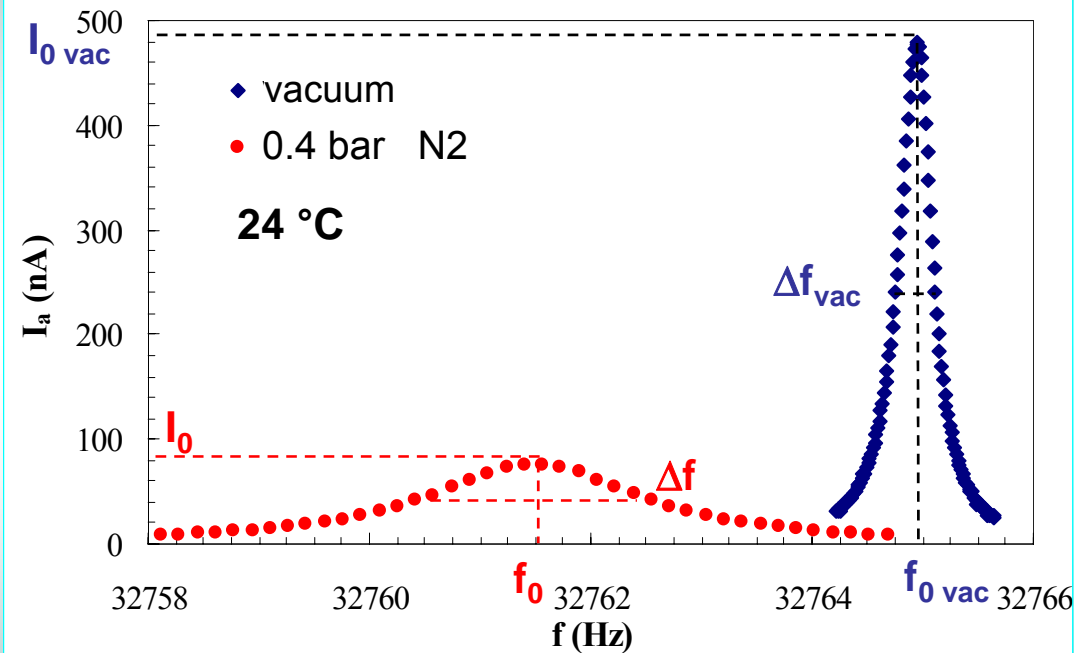
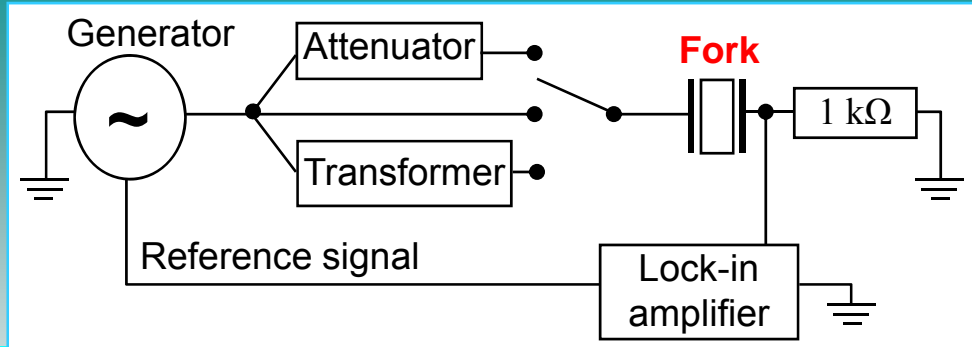
!  $F_{damp}$  is phase-shifted relative to velocity

Equation of motion:  $m_{eff}\ddot{x} + \gamma\dot{x} + kx = F_0 \cos(\omega t)$

# Forks are easy to use

Connection diagram

## Hydrodynamic mass enhancement



$\Delta f, f_0, I_0$

$\rho, \eta, v_0$

$$\left(\frac{f_{0vac}}{f_0}\right)^2 = 1 + \frac{\rho}{\rho_f} \left( \beta + B \frac{S}{V} \sqrt{\frac{\eta}{\pi \rho f_0}} \right)$$

$$\Delta f - \Delta f_{vac} = \frac{1}{2} \sqrt{\frac{\rho \eta f_0}{\pi}} \frac{CS}{m_{vac}} \left(\frac{f_0}{f_{0vac}}\right)^2$$

- $\rho_f$  Fork's density
- $\rho$  Density of the working fluid
- $\eta$  Dynamic viscosity
- $S$  Surface of the oscillating body
- $V$  Volume of the oscillating body
- $\beta, B, C$  numerical constants ~ geometry
- $\beta, B, C$  – fitting parameters, characterize determined fork

# Working fluids

1) gaseous  $N_2$ , room temperature, up to 30 bar

2) gaseous He, room temperature, up to 30 bar  
78 K, up to 30 bar

3) normal liquid He (2.17 K; 4.2 K), up to 30 bar

4) superfluid liquid He (1.3 K; 2.17 K), SVP

**Playground:**

**Kinematic viscosity:  $(1 \cdot 10^{-4} - 0.15)$  cm<sup>2</sup>/s**

**Dynamical response over 7 orders of magnitude of drive**



# Quartz Tuning Fork: Thermometer, Pressure- and Viscometer for Helium Liquids\*

JLTP, 2007

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 R. de Graaf,<sup>1</sup> J. Hosio,<sup>1</sup> M. Krusius,<sup>1</sup> D. Schmoranzer,<sup>5</sup> W. Schoepe,<sup>6</sup>  
 L. Skrbek,<sup>2,5</sup> P. Skyba,<sup>3</sup> R.E. Solntsev,<sup>1</sup> and D.E. Zmeev<sup>1,4</sup>

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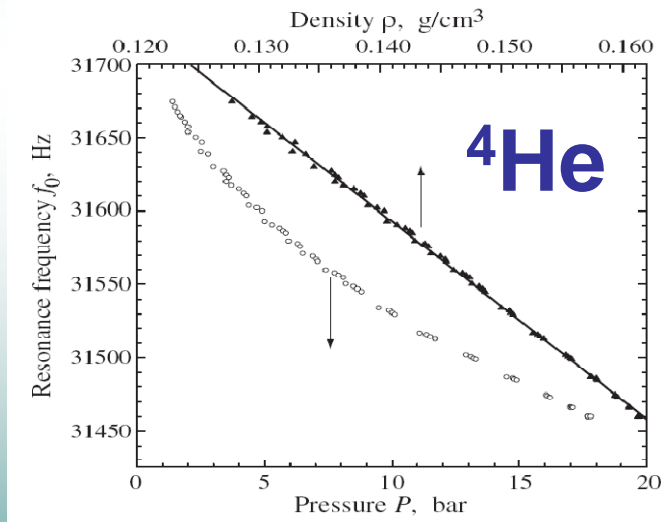
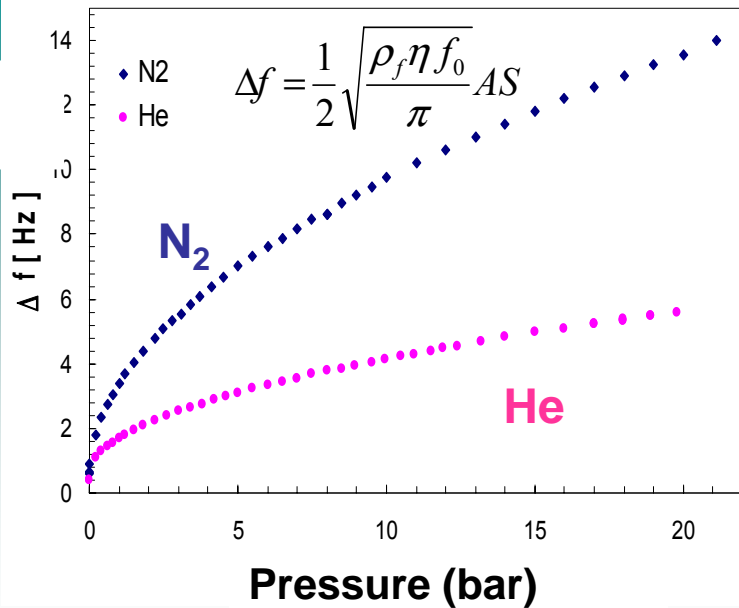
<sup>2</sup>Institute of Physics ASCR, Na Slovance 2, 182 21 Prague, Czech Republic

<sup>3</sup>Centre of Low Temperature Physics, Institute of Experimental Physics SAV, Košice, Slovakia

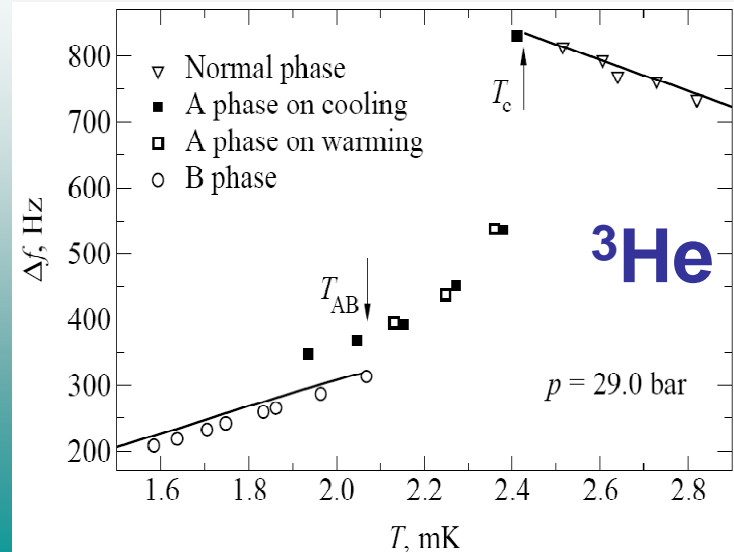
<sup>4</sup>Kapitza Institute for Physical Problems, Kosygina 2, Moscow 119334, Russia

<sup>5</sup>Faculty of Mathematics and Physics, Charles University, Ke Karlovu 3, 121 16 Prague, Czech Republic

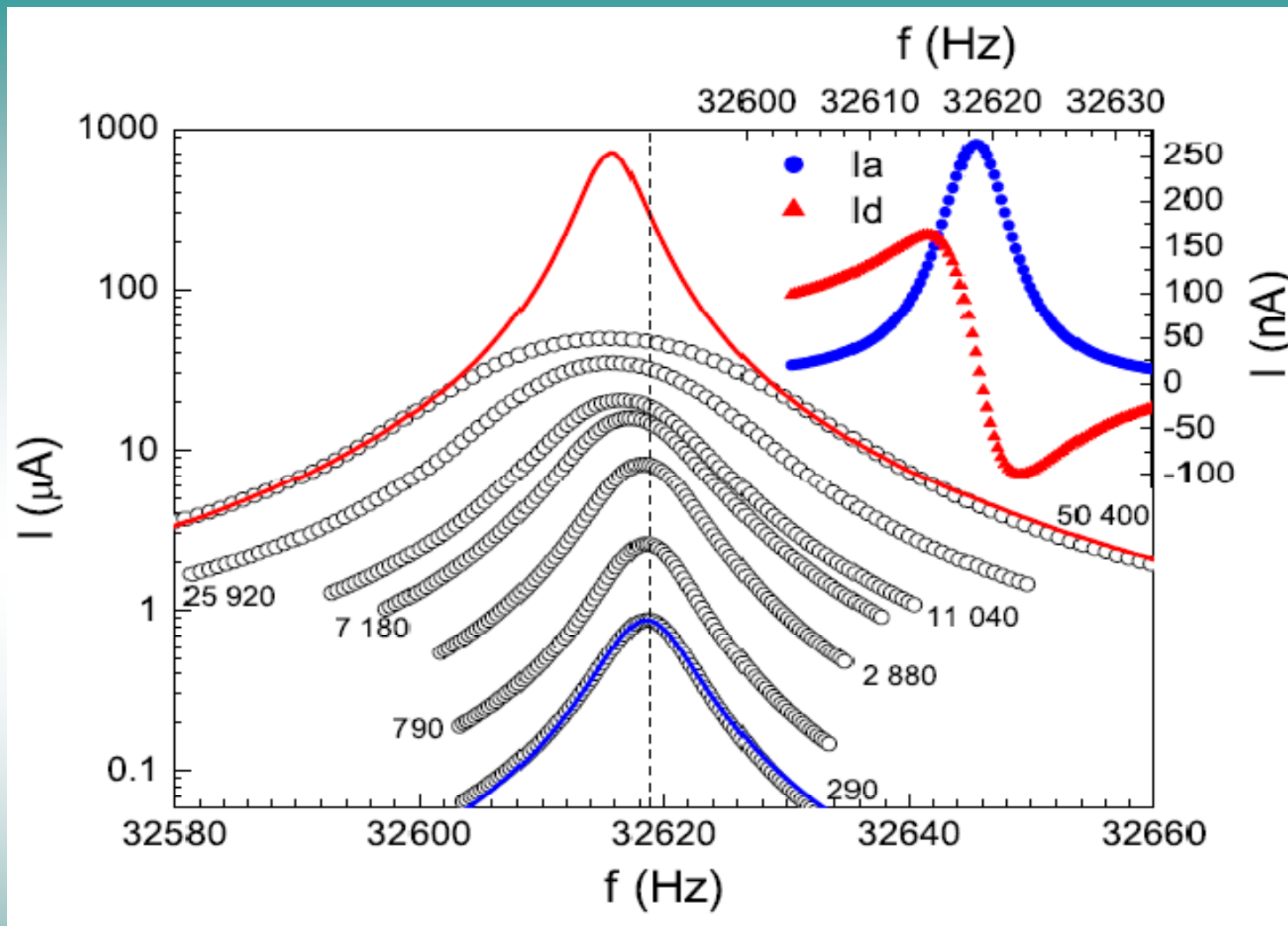
<sup>6</sup>Fakultät für Physik, Universität Regensburg, D-93040 Regensburg, Germany



$$\left( \frac{f_{0vac}}{f_0} \right)^2 = 1 + \frac{\rho}{\rho_f} \left( \beta + B \frac{S}{V} \sqrt{\frac{\eta}{\pi \rho f_0}} \right) + ???$$



# Quartz fork as a generator and detector of turbulence



The in-phase resonant response of the driven quartz fork versus applied frequency measured for various drive voltage levels (in  $\text{mV}_{\text{rms}}$ ) as indicated. The solid curves are Lorentzian fits to the data.

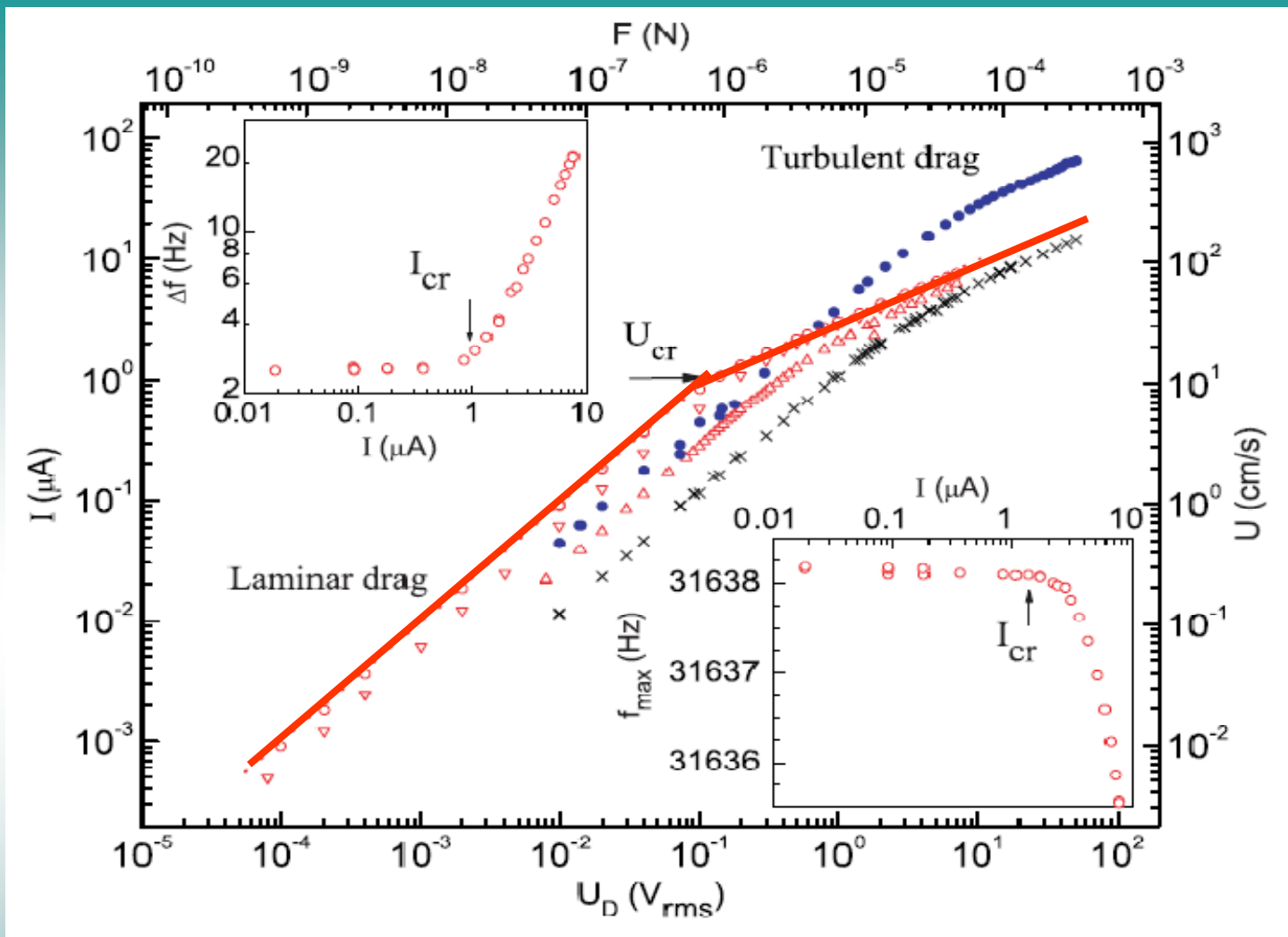


FIG. 2: Transition from laminar to turbulent drag regime as detected by the vibrating quartz fork A2 in He I at 4.2 K and 18.6 bar ( $\times$ ), in He II at SVP at 1.37 K ( $\circ$ ), 1.61 K ( $\nabla$ ), 2.06 K ( $\Delta$ ) and in gaseous helium at 78 K and 10.05 bar ( $\bullet$ ). For conversion of measured electrical quantities  $U_D$  and  $I$  to  $F$  and  $U$ , see [1]. The insets show the width  $\Delta f$  of the in-phase resonance response (top) and the frequency of maximum response  $f_{\max}$  (bottom) versus measured current; both being constant in a linear regime. Increase of  $\Delta f$  and decrease of  $f_{\max}$  indicate an onset of the turbulent drag regime.

# Quartz fork - a generator and detector of turbulence

## Transition from laminar to turbulent drag in $^4\text{He}$

Measured in: (i) He gas at 78 K and ambient and elevated pressure up to 30 bar  
(ii) He I at 4.2 K and various pressures and down to  $T_\lambda$  at SVP  
(iii) He II down to 1.3 K at saturated vapour pressure (SVP)

All these experiments (with three tuning forks A1, A2, B1) were performed in the **same experimental pressure cell** using the **same sample of He** throughout, starting with the highest density which was gradually released in order to prevent gathering of any solid particles on the fork's surface

$^4\text{He}$  properties are very well known and tabulated:

R. J. Donnelly and C. F. Barenghi, *J. Phys. Chem. Data* **27** (1998) 1217.

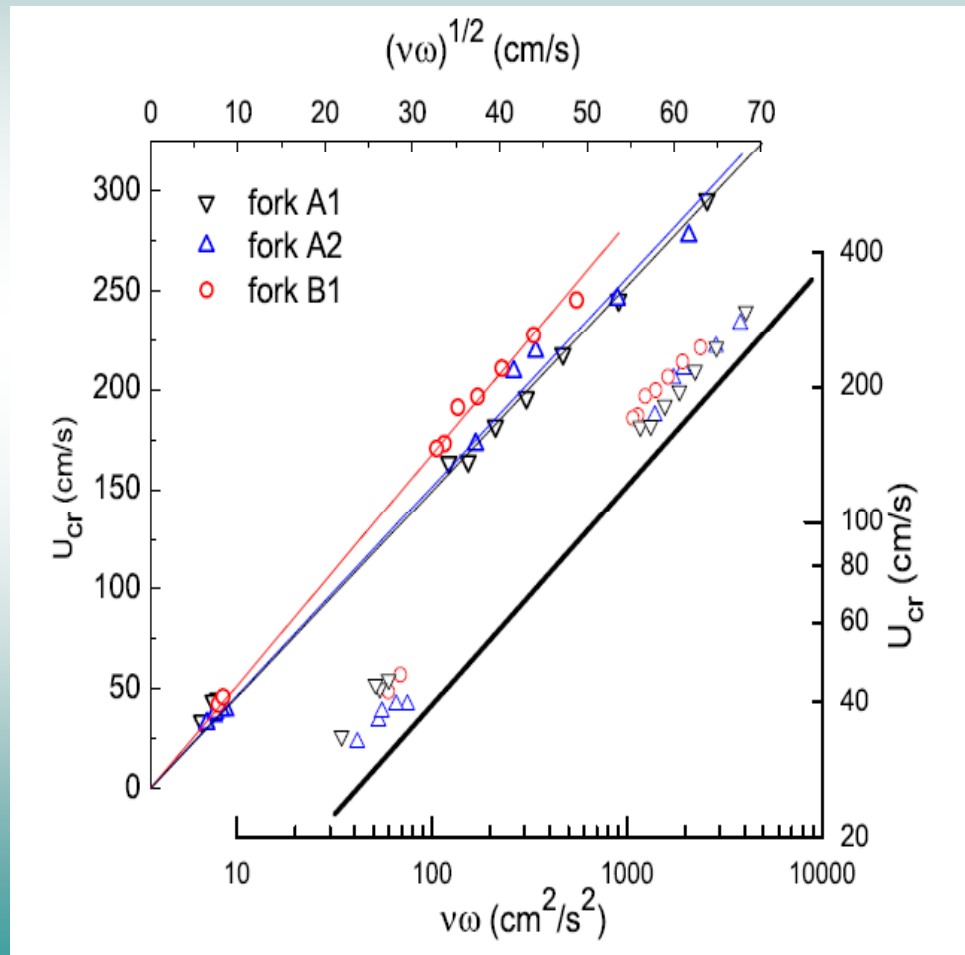
R.D. McCarty, *Technical Note* 631, National Bureau of Standards, Gaithersburg, Maryland (1972);

V.D. Arp, R.D. McCarty, *The properties of Critical Helium Gas*, Technical Report, Univ. Oregon (1998)

# Critical velocities (classical fluids)

**Critical velocity scaling:**

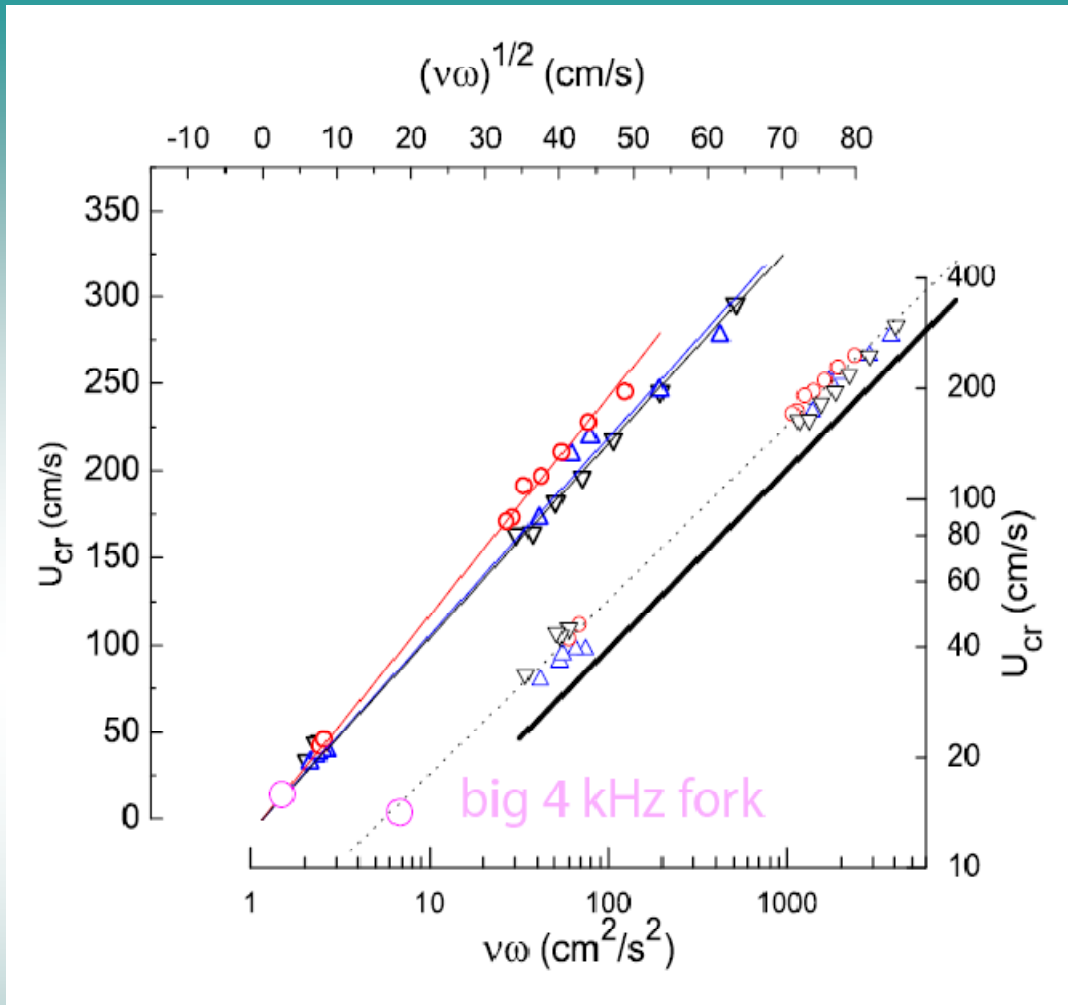
$$U_c \approx \sqrt{\nu\omega}$$



We experimentally verify (using He I at SVP and elevated pressures and He gas at nitrogen temperature as working fluids) that this scaling indeed holds.

The logarithmic graph gives a gradient  $0.48 \pm 0.04$

M. Blažková, D. Schmoranzer, L. Skrbek,  
*Phys. Rev. E* **75**, 025302R (2007)



The critical velocity is independent of the object size if

Steady viscous flows - transition from laminar to turbulent drag regime is characterized

$$Re_c = \frac{U_c D}{\nu}$$

Flow due to an oscillating object : another length scale:

$$\delta = \sqrt{2\nu / \omega}$$

$$Re_c^\delta = \frac{U_c \delta}{\nu}$$

$$\delta \ll D$$



$$U_c \approx \sqrt{\nu \omega}$$

To describe an oscillatory boundary layer flow,

Reynolds AND Strouhal numbers needed:

$$Re = \frac{UD}{\nu} \quad S = \frac{U\tau}{D}$$

However for the oscillating  
fork we assume:

Characteristic length scale –

**NOT** fork dimension  $D$ , but

**viscous penetration depth  $\delta$ !!!**

Replacing  $D$  by  $\delta$  in both  $Re$  and  $S$  we get:

•The transition to turbulence can be thus  
described by the Reynolds (Strouhal)  
number alone



Professor Čeněk Strouhal

$$\delta = \sqrt{\frac{2\nu}{\omega}} \approx 0.5\mu m \ll D \approx 100\mu m$$

$$S \propto Re \propto \frac{U}{\sqrt{\nu\omega}}$$

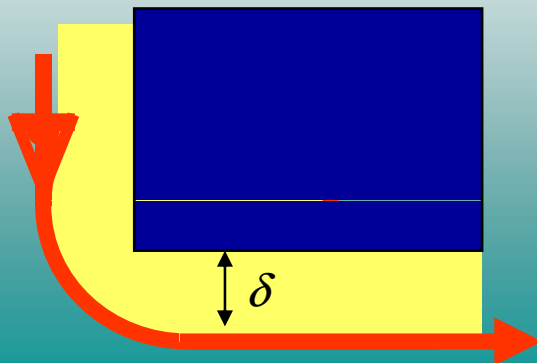
Exactly soluble example – an oscillating sphere in a limit  $R \gg \delta = \sqrt{2\nu/\omega}$

Laminar drag force  $F_{lam} = \lambda U = 6\pi\eta R U \left(1 + \frac{R}{\delta}\right) \Big|_{R \gg \delta} \approx 6\pi\eta R \frac{R}{\delta} U$

Turbulent drag force  $F_{turb} = \gamma U^2 = 0.5 C_D \pi \rho R^2 U^2$

Crossover  $U_C = \frac{\lambda}{\gamma} = \frac{6}{C_D} \sqrt{2\nu\omega} \approx 21 \sqrt{\nu\omega}$

This gives about 1.3 m/s for a sphere of **any** size, oscillating at 32 kHz in He I at SVP right above the superfluid transition  
(factor of 4 higher than what is observed for our forks)



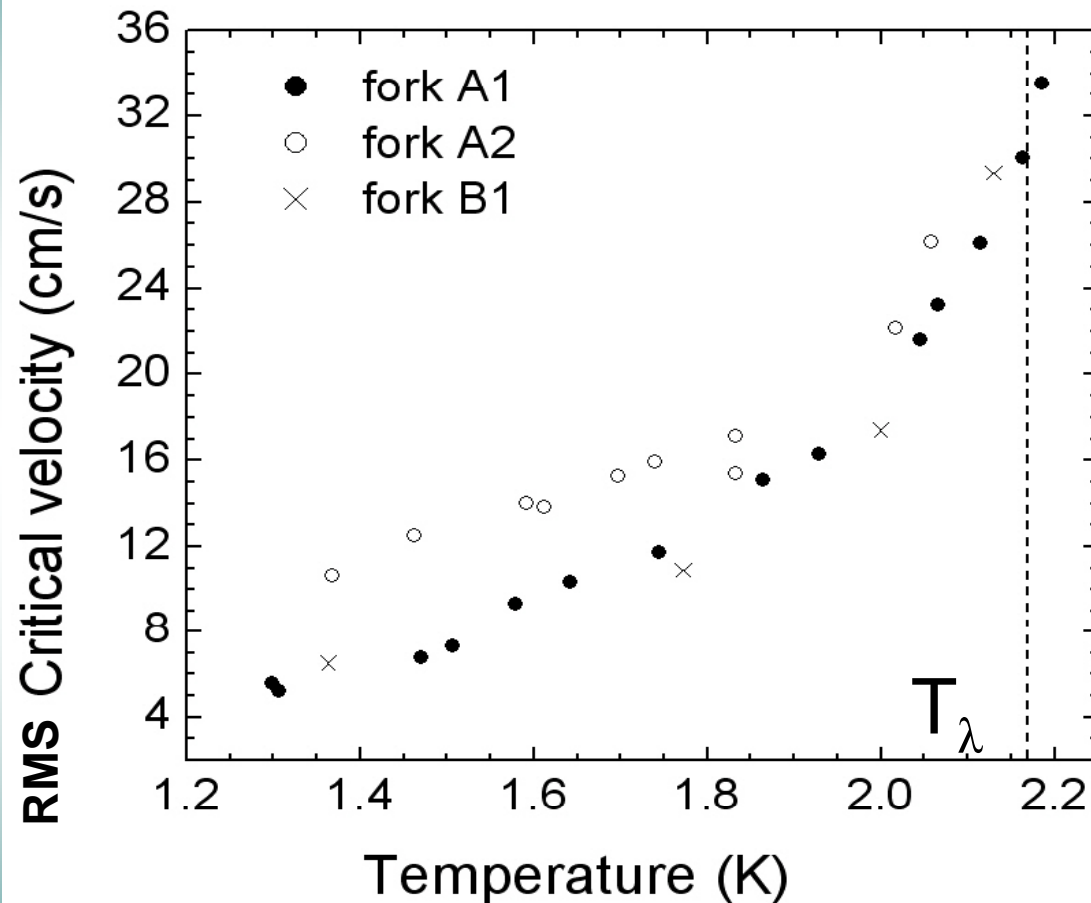
velocity enhancement at the corner

$$U_{enh} \approx (d/r)^{1/3} U \approx 5 U$$

gives even better agreement with the experiment



# Results in He II



These data allow extracting the T-dependence of the effective kinematic viscosity, using the scaling:

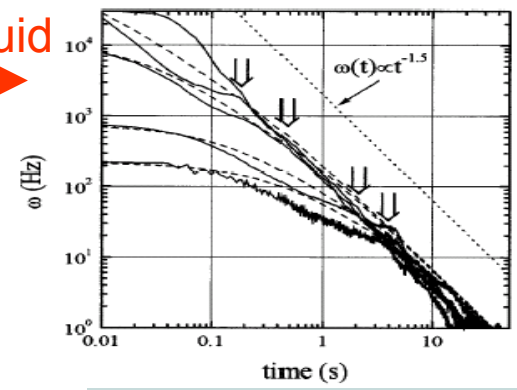
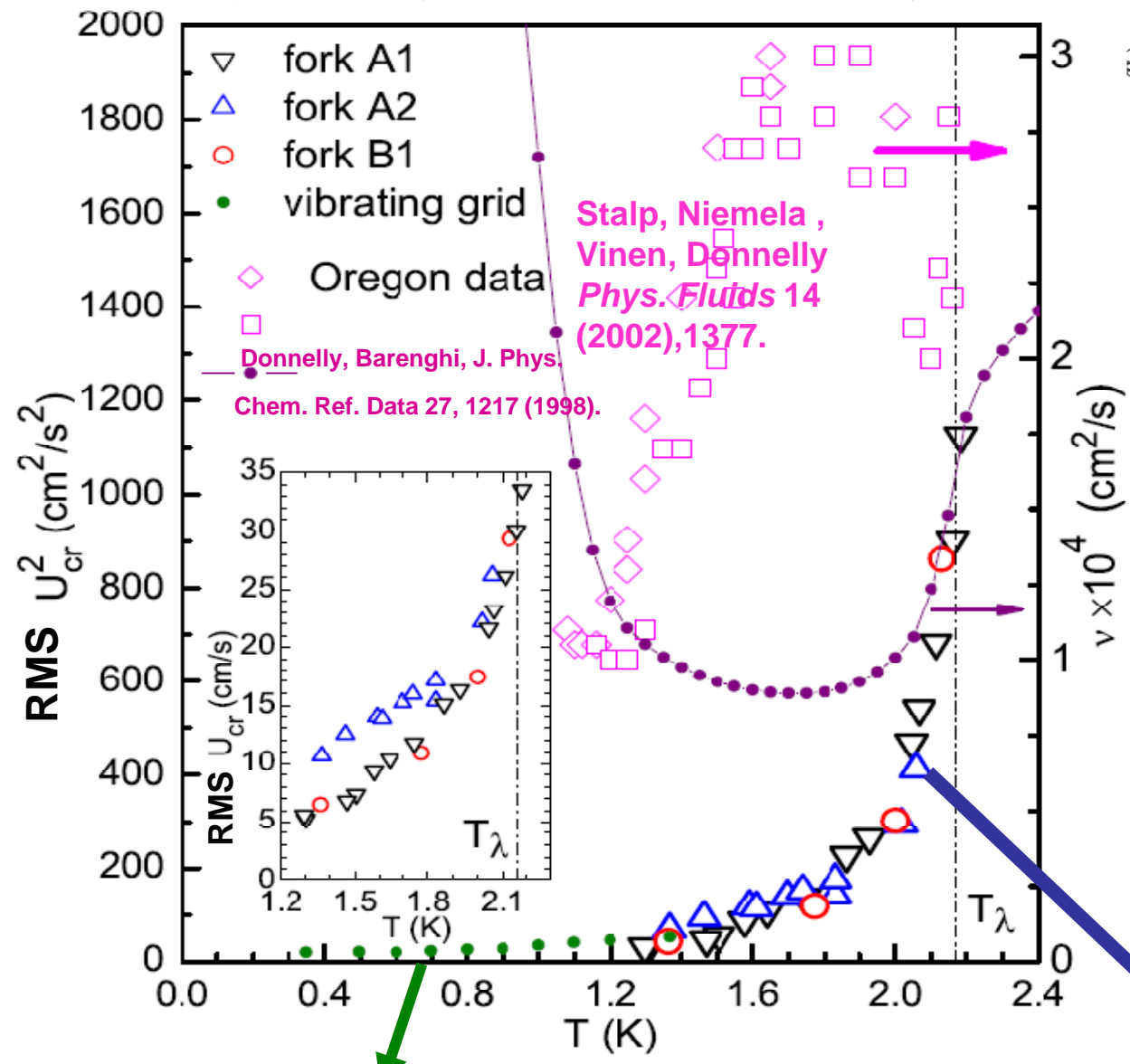
$$U_C \approx \sqrt{\nu\omega}$$

verified for classical viscous fluids, **if He II is treated as a single-component quasiclassical fluid.**

The unknown multiplicative constant is best determined by matching the data at  $T_\lambda$ .

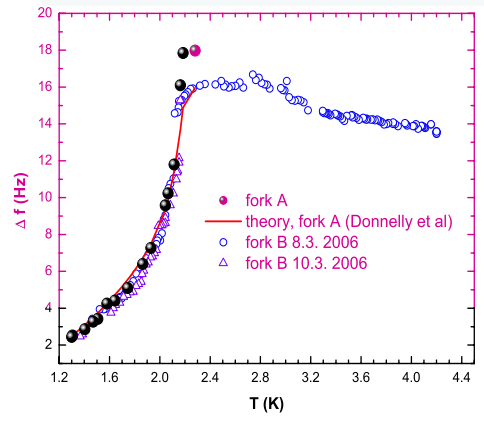
The observed critical velocity at which transition from laminar to turbulent drag regime occurs for three forks marked A1, A2 and B1.

Pure superfluid ← Two-fluid model → Classical fluid



Stalp, Skrbek, Donnelly: Phys. Rev. Lett. 82 (1999) 4831

$$L(t) = \frac{D(3C)^{3/2}}{2\pi\kappa\sqrt{v_{eff}}} (t+t^*)^{-3/2}$$

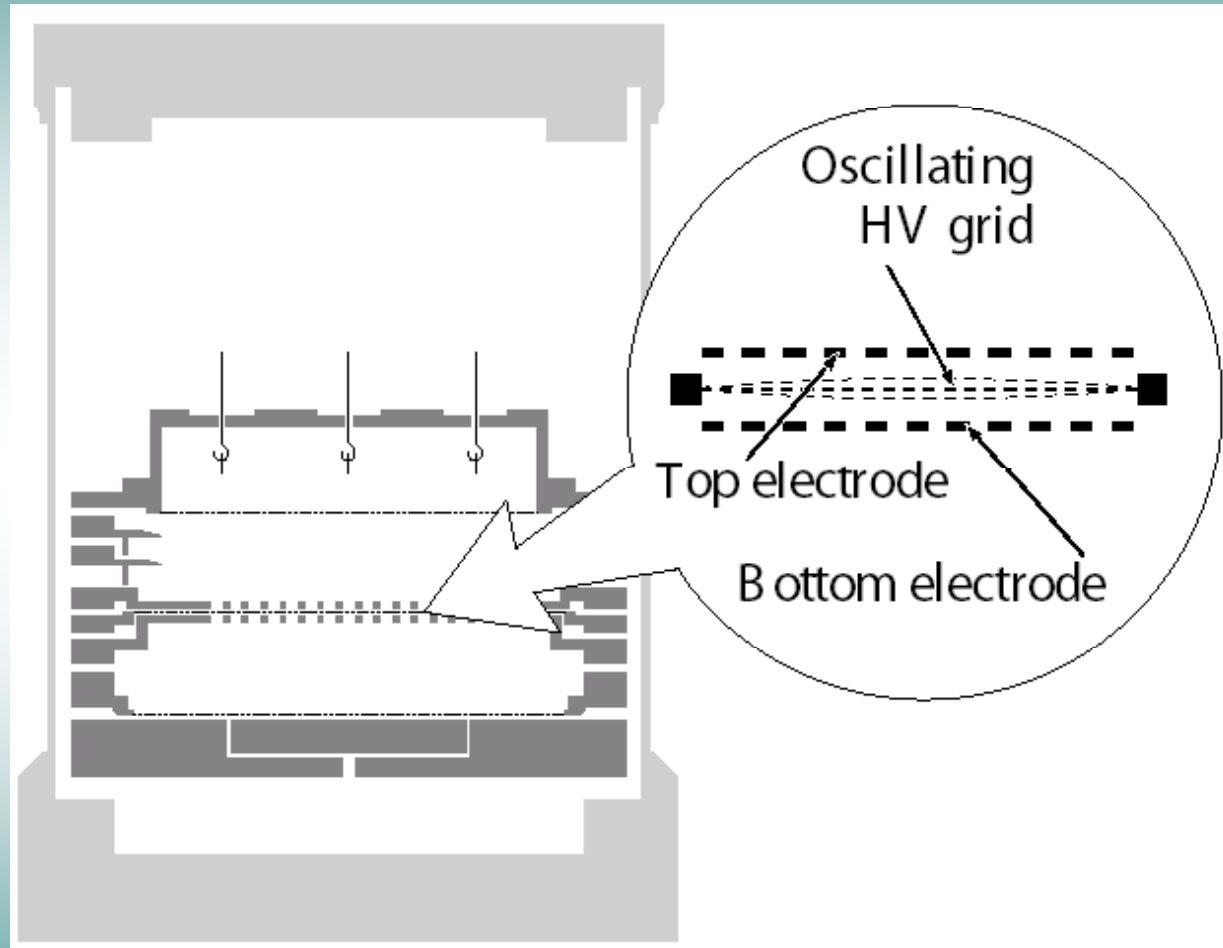


Our data, obtained via scaling

$$\sqrt{v_{eff}^{fork}(T)\omega}$$

D. Charalambous, L. Skrbek, P.C. Hendry, P.V.E. McClintock, W.F. Vinen, Phys. Rev. E 74, 036307 (2006)

**Experimental cell containing 1.5 litre of spectrally pure He-4,  
attached to the dilution refrigerator (base T about 10 mK)**

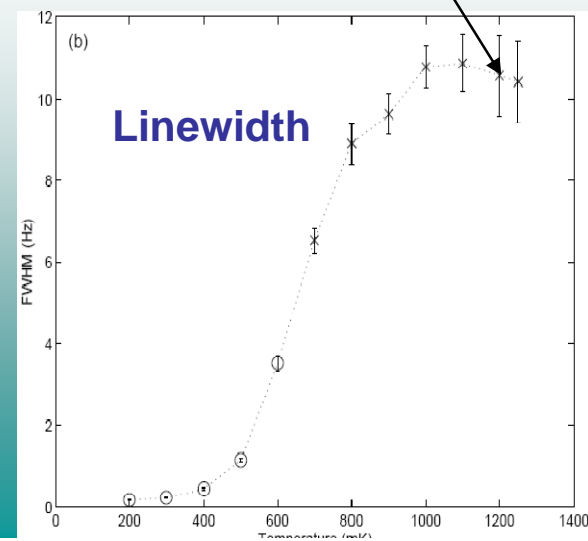
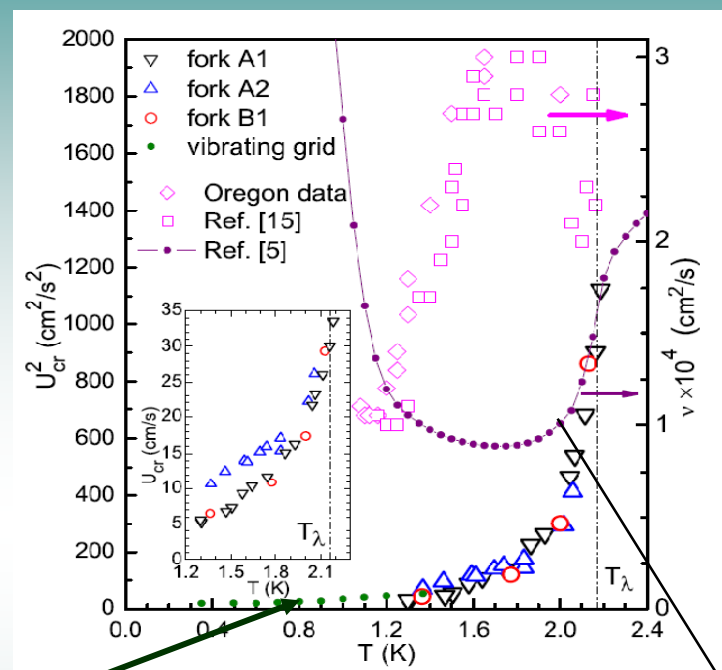
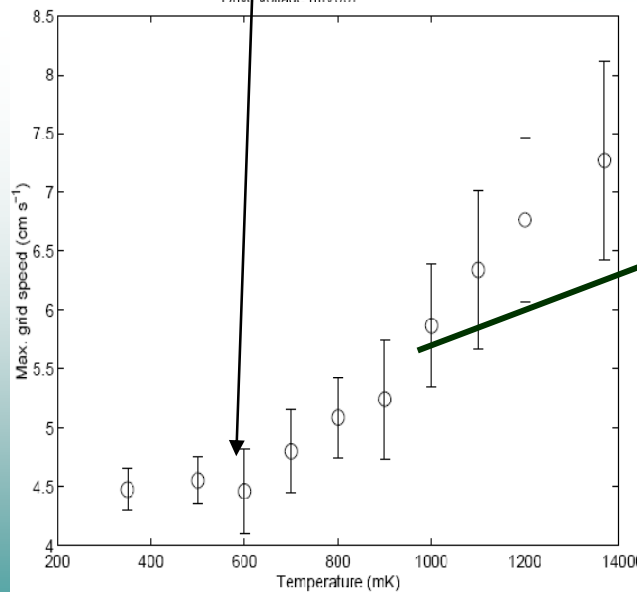
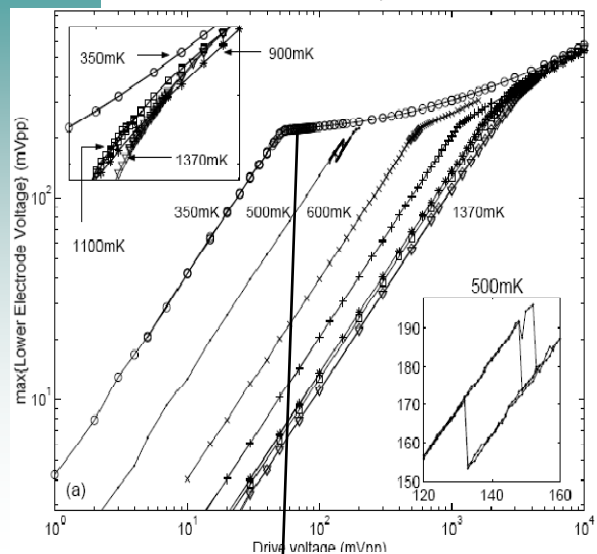


**$T < 130 \text{ mK}$**

**$0 < p < 25 \text{ bar}$**

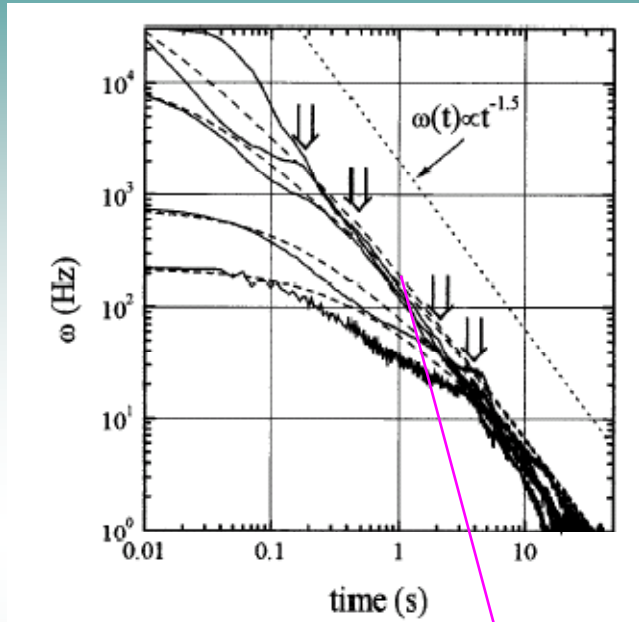
# Experimental Investigation of the Dynamics of a Vibrating Grid in Superfluid $^4\text{He}$ over a Range of Temperatures and Pressures

D. Charalambous,<sup>1,2,\*</sup> L. Skrbek,<sup>3</sup> P.C. Hendry,<sup>1</sup> P.V.E. McClintock,<sup>1</sup> and W.F. Vinen<sup>4</sup>



# Decay of towed grid turbulence in He II above 1K

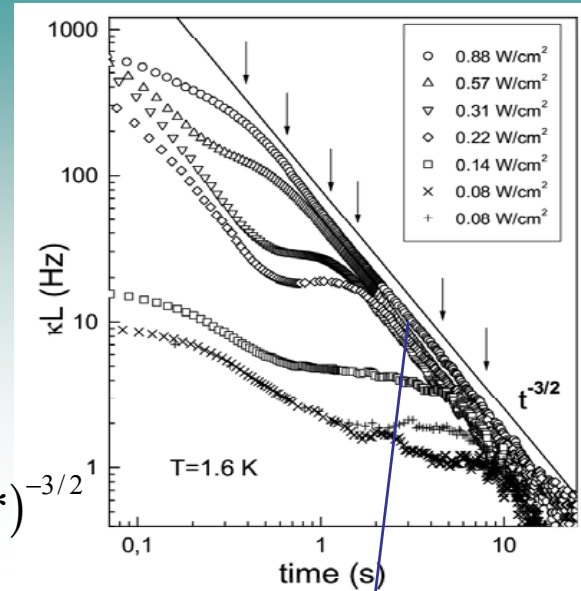
Stalp, Skrbek, Donnelly:  
PRL 82 (1999) 4831



$$L(t) = \frac{D(3C)^{3/2}}{2\pi\kappa\sqrt{v_{eff}}} (t+t^*)^{-3/2}$$

# counterflow turbulence

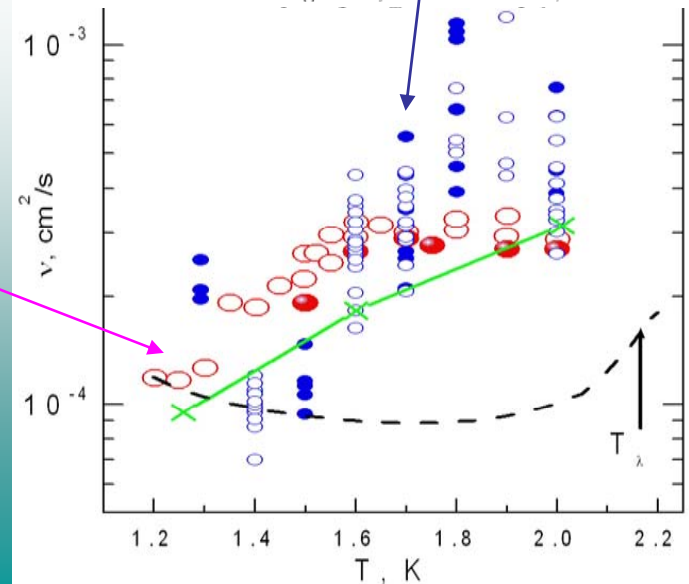
Skrbek, Gordeev, Soukup: PRE 67, 047302 (2003)



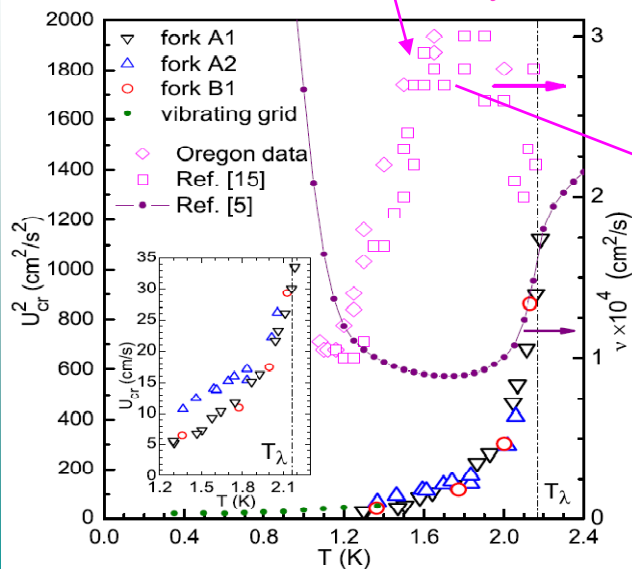
## Effective Kinematic Viscosity of Turbulent He II

Subm. to PRE

T.V. Chagovets<sup>1</sup>, A.V. Gordeev<sup>1</sup>, L. Skrbek<sup>2</sup>

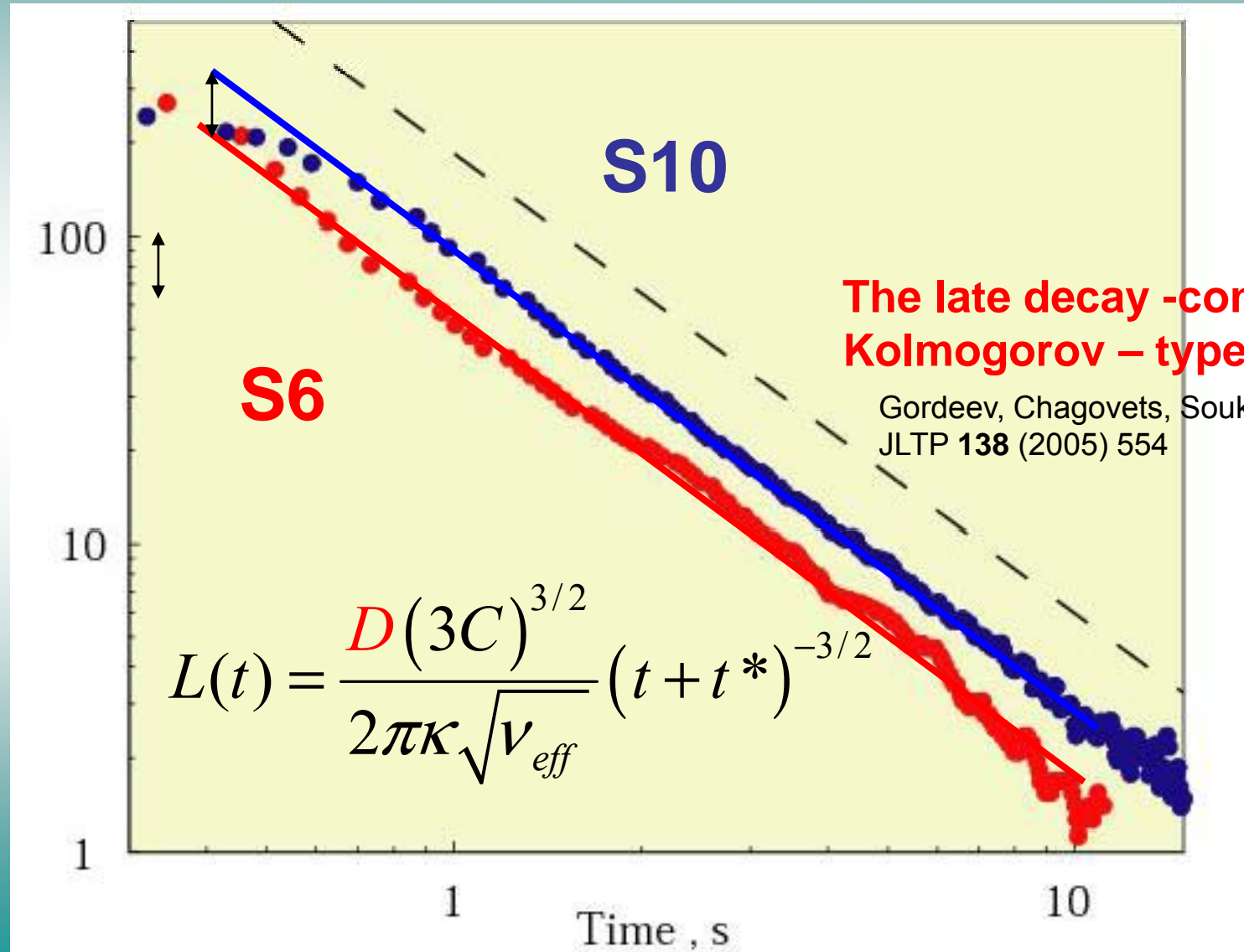


Stalp, Niemela, Vinen, Donnelly  
Phys. Fluids 14 (2002), 1377.

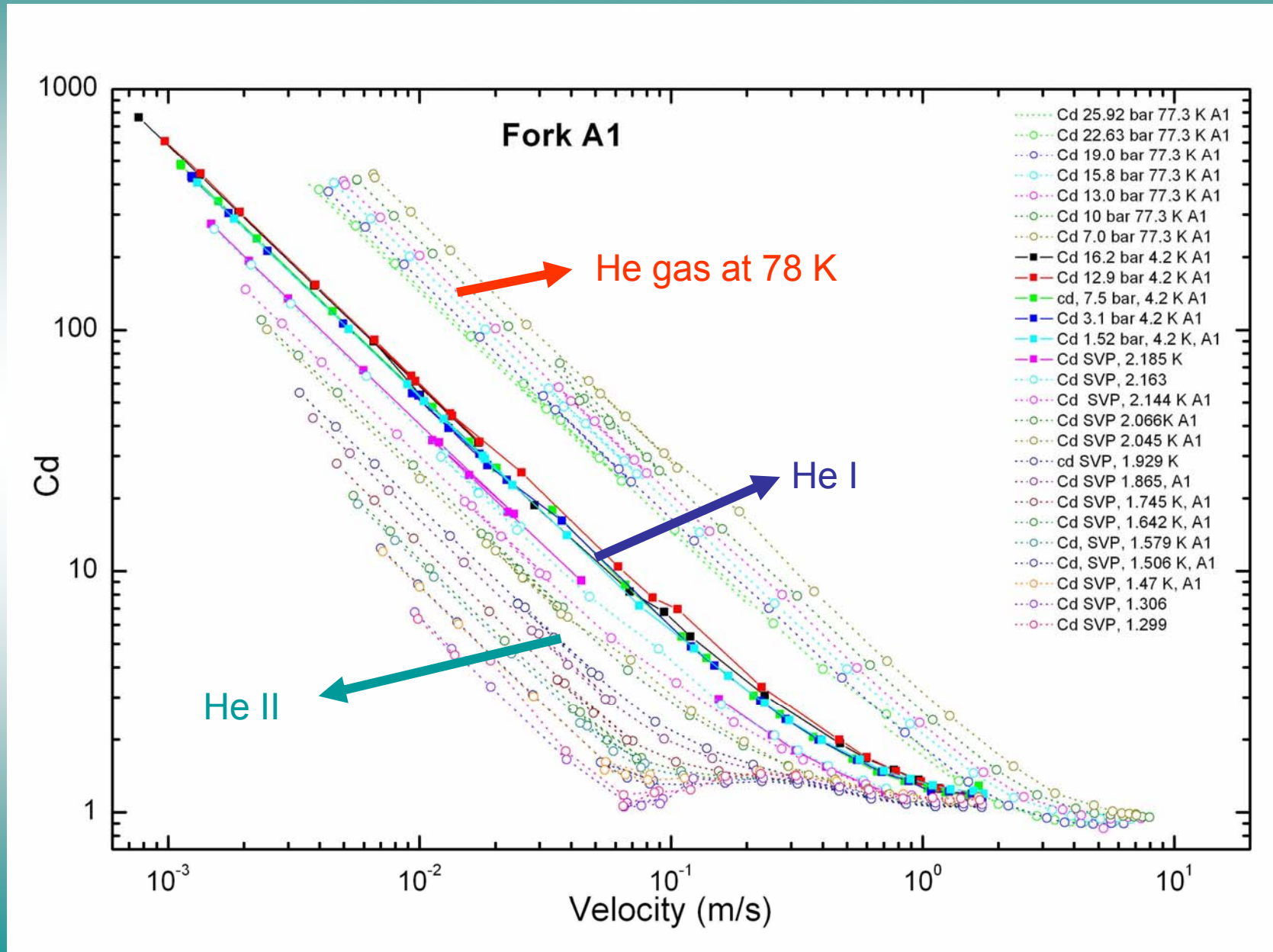


After saturation of the energy-containing length scale – universal decay law

Dependence on the channel size experimentally confirmed for the first time (even for classical turbulence)



# Drag coefficient versus velocity in helium gas, He I and He II



## Second approach – normal fluid and superfluid are fully independent

The fitting function for the **normal phase** is obtained simply by adding the drag coefficient appropriate to the laminar regime to that appropriate to the fully turbulent regime - the drag at all velocities is the sum of the laminar drag and the turbulent drag, both terms being present at all velocities, the dominant term being simply the larger one.

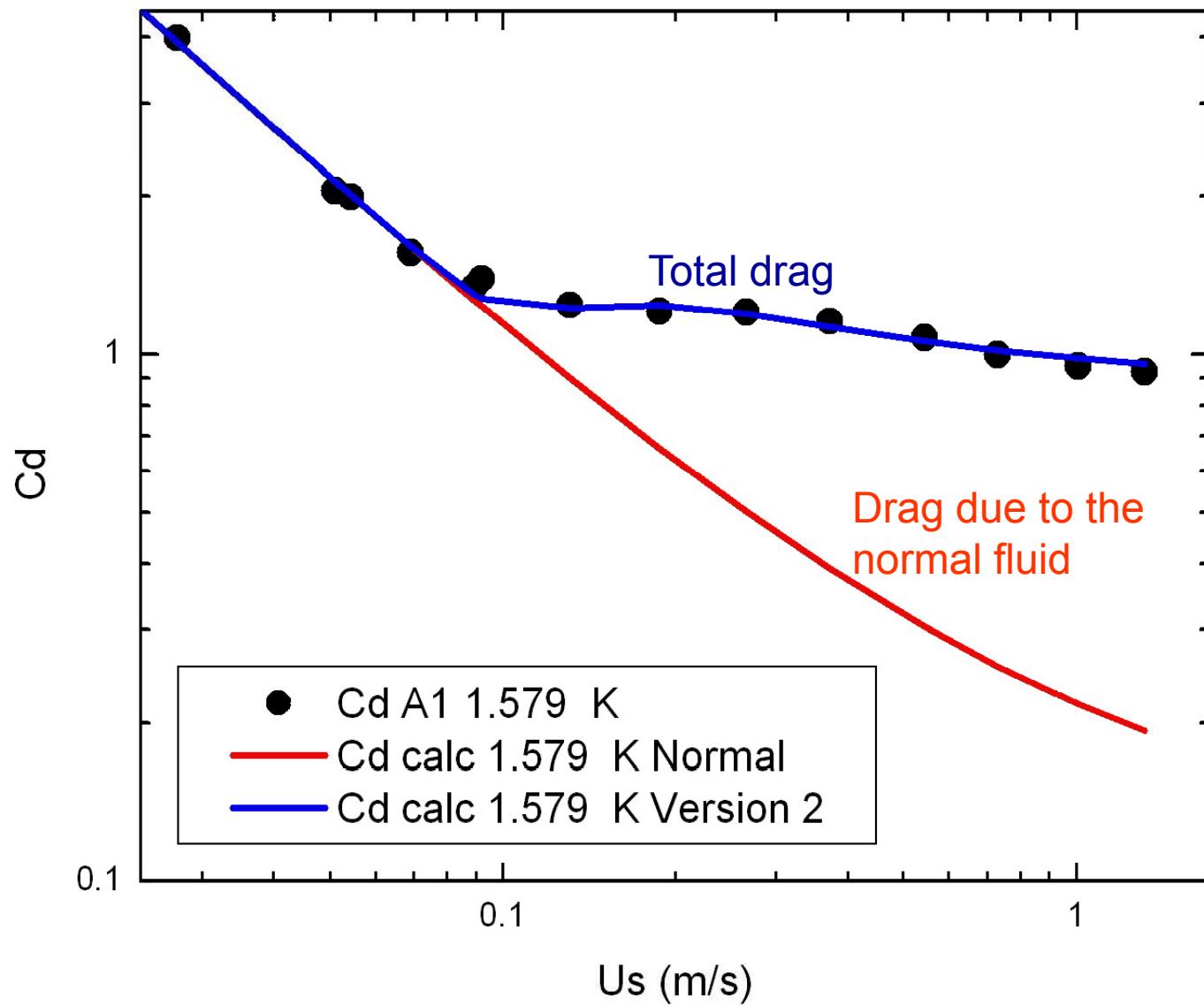
$$C_d\left(U, \frac{\rho_n}{\rho}, \nu\right) = \frac{\alpha' 2 S/A \sqrt{2\pi f_0 \frac{\rho_n}{\rho} \nu}}{U} \downarrow \text{N laminar} + \beta \frac{\rho_n}{\rho} \downarrow \text{N turbulent (const)} + \gamma \left(1 - \frac{\rho_n}{\rho}\right) \Phi(U-U_c) \downarrow \text{SF turbulent} \left[ \frac{(U-U_c)^2}{\epsilon + (U-U_c)^2} \right]$$

Step function

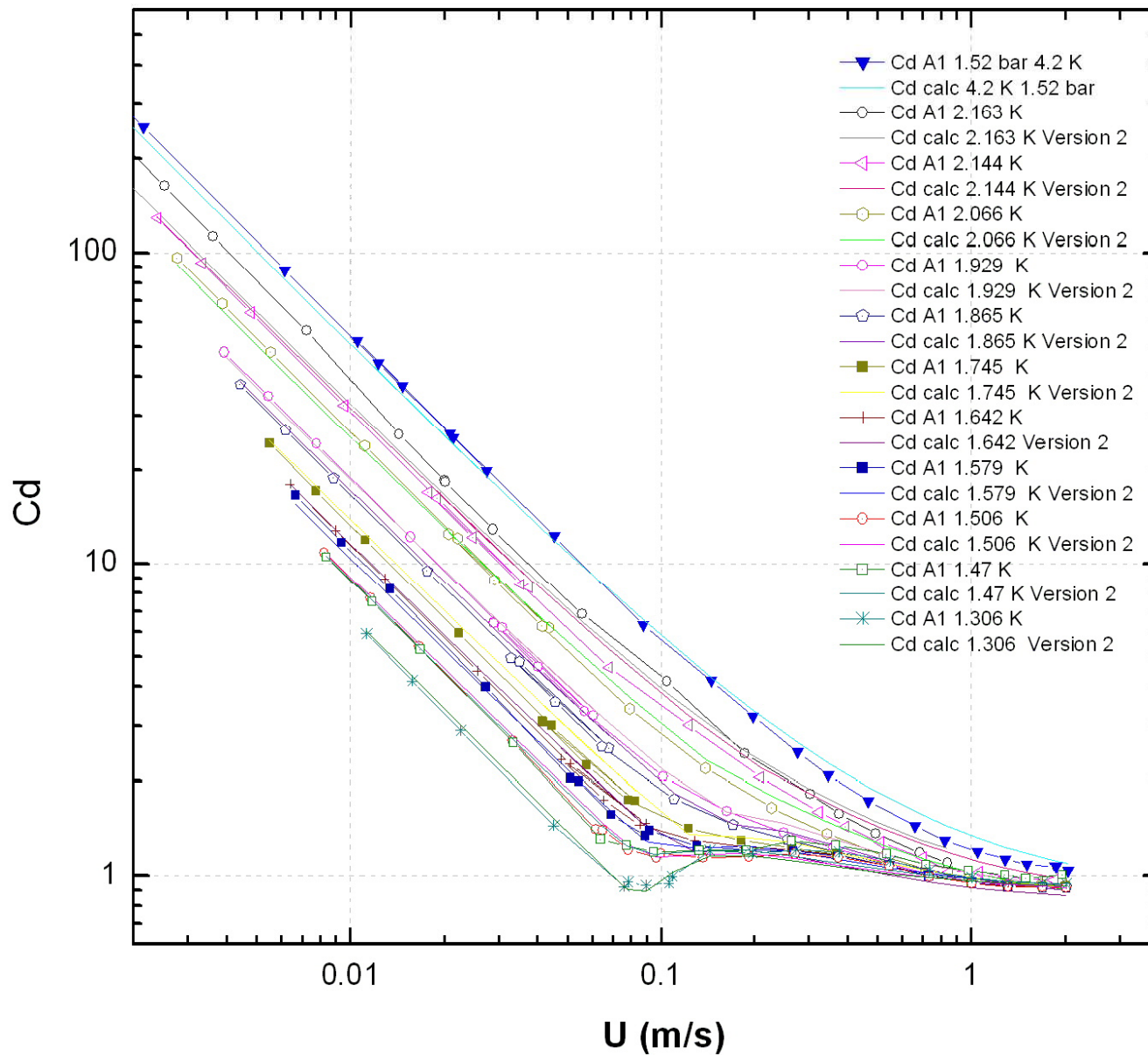
$U_c$  is the sharp critical velocity for onset of turbulence in the superfluid component.

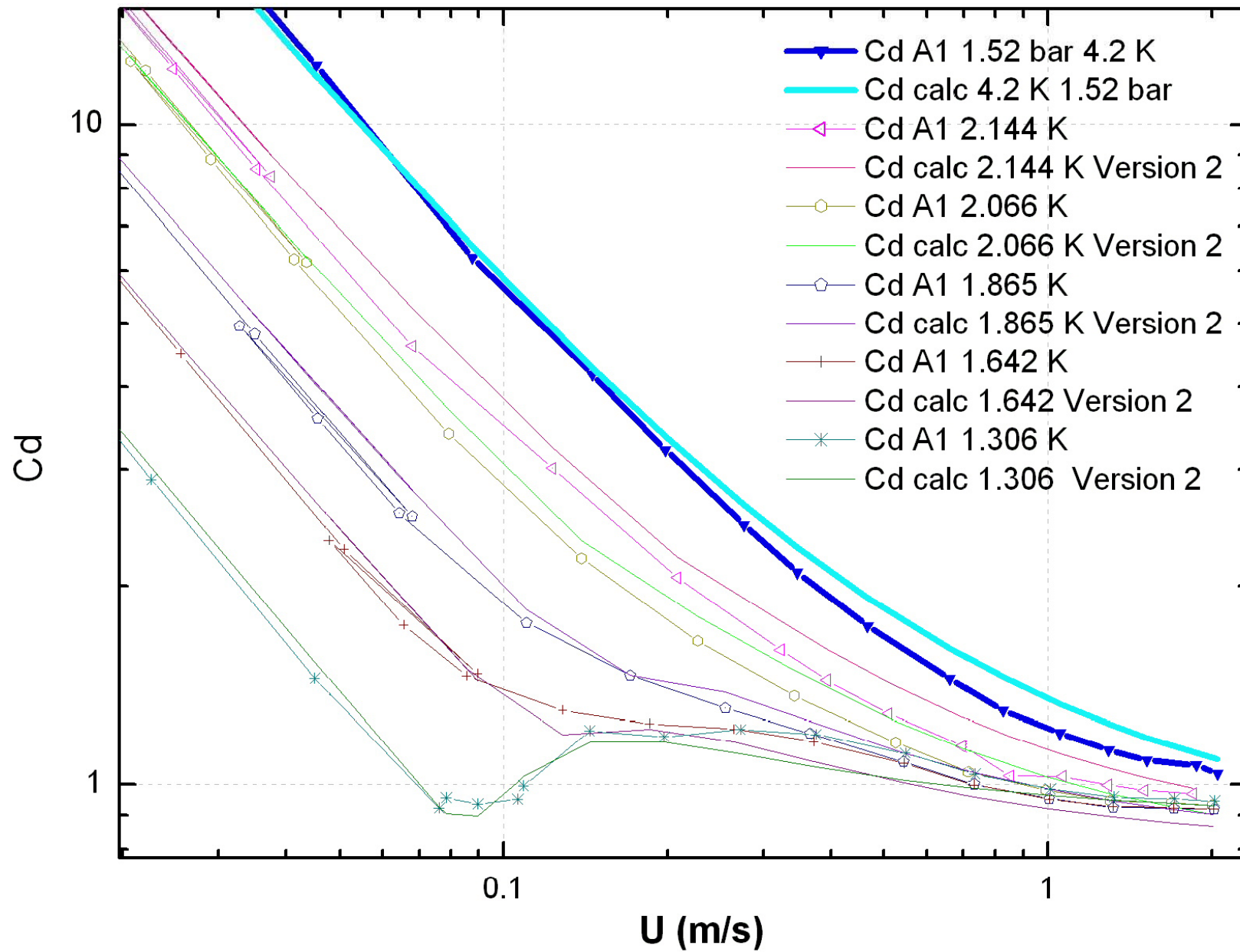
Does this functional dependence fit the experimental data?

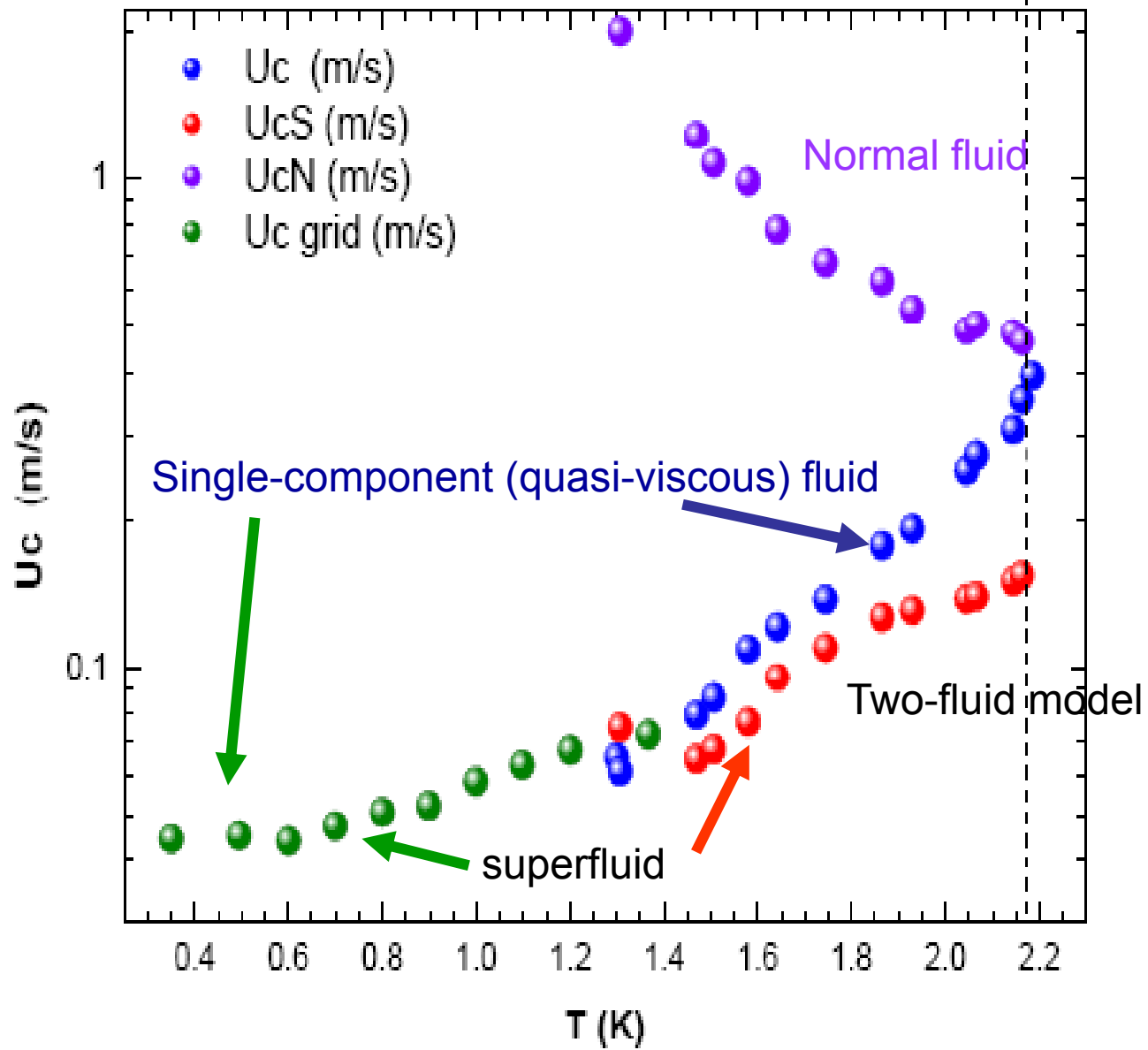




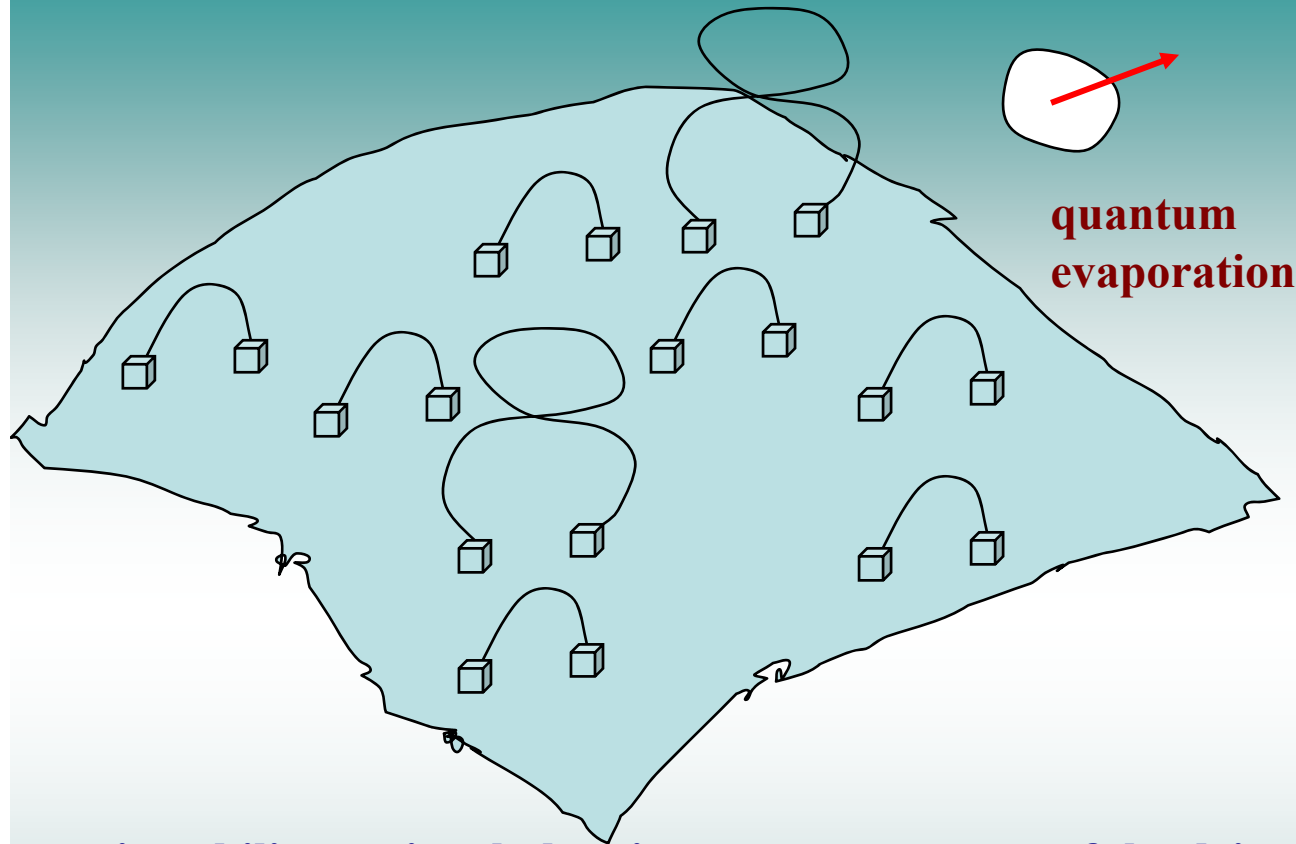
$$Cd(U, \frac{\rho_n}{\rho}, \nu) = \frac{\alpha' 2 S/A \sqrt{2\pi f_0 \frac{\rho_n}{\rho} \nu}}{U} + \beta \frac{\rho_n}{\rho} + \gamma \left(1 - \frac{\rho_n}{\rho}\right) \Phi(U - U_c) \left[ \frac{(U - U_c)^2}{\epsilon + (U - U_c)^2} \right]$$







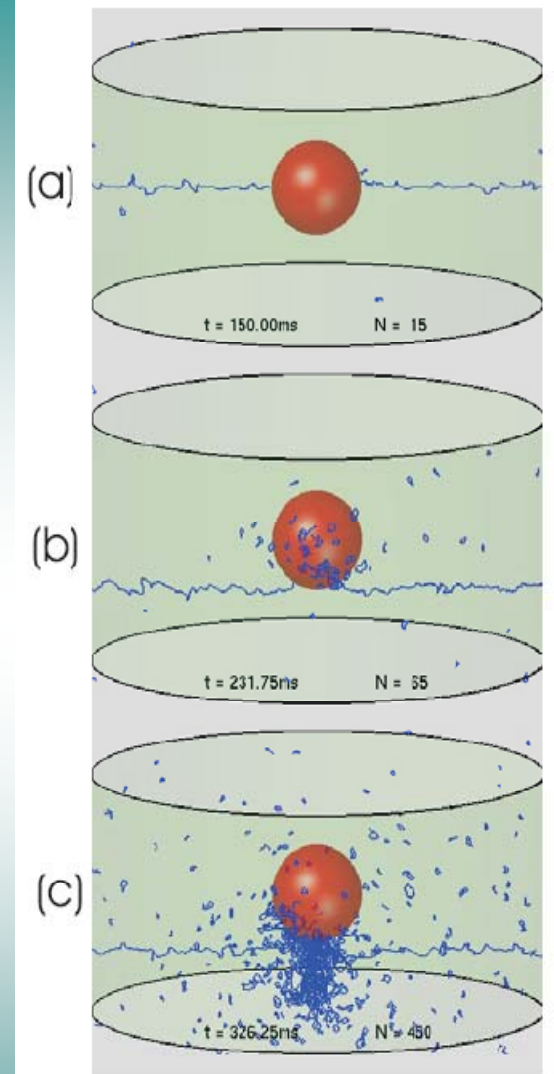
# Effective boundary layer constituent of vortex loops



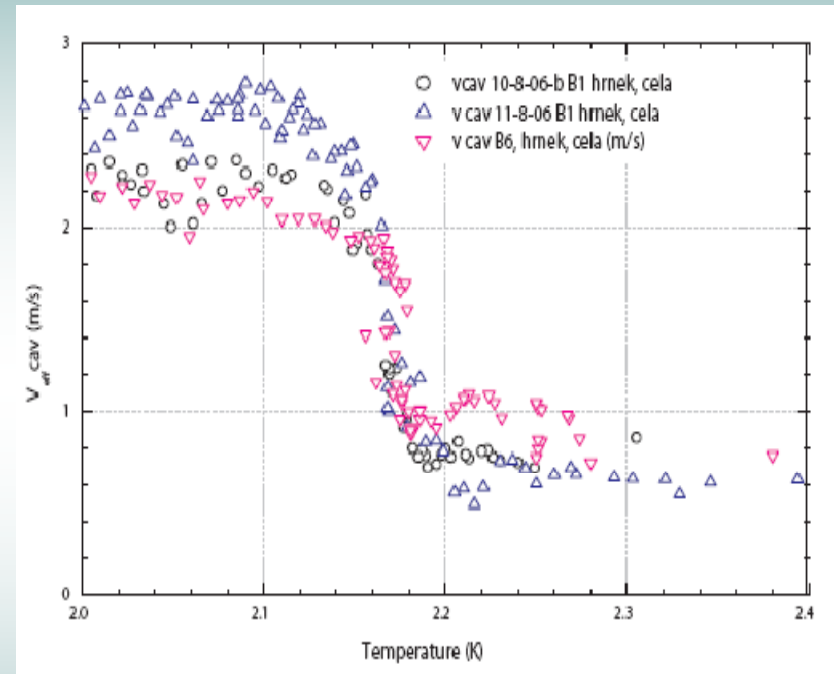
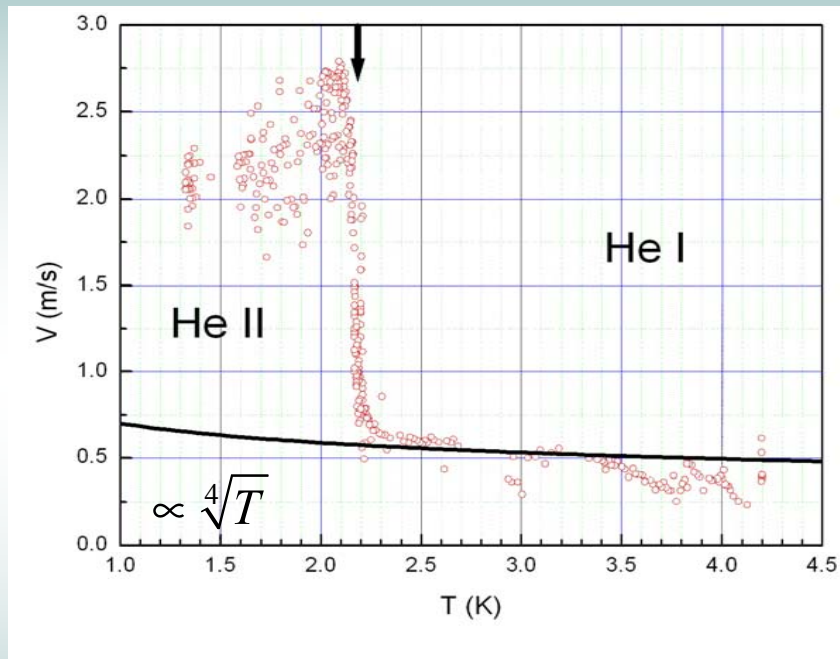
– instability against ballooning out, vortex wave of the drive frequency becomes excited, the loop twists, reconnects and the free vortex ring flies away – dissipation

## Dissipation can occur without reconnections

- According to Schwarz [PRL 57(1996)1448], even at zero temperature, dissipation occurs – by ends of vortex loops sliding the rough surface
- Dissipation due to sound emission – Kolmogorov cascade on the long enough vortex loop
- At finite T, mutual friction



# Cavitation (boiling?) in LHe – Fork Results

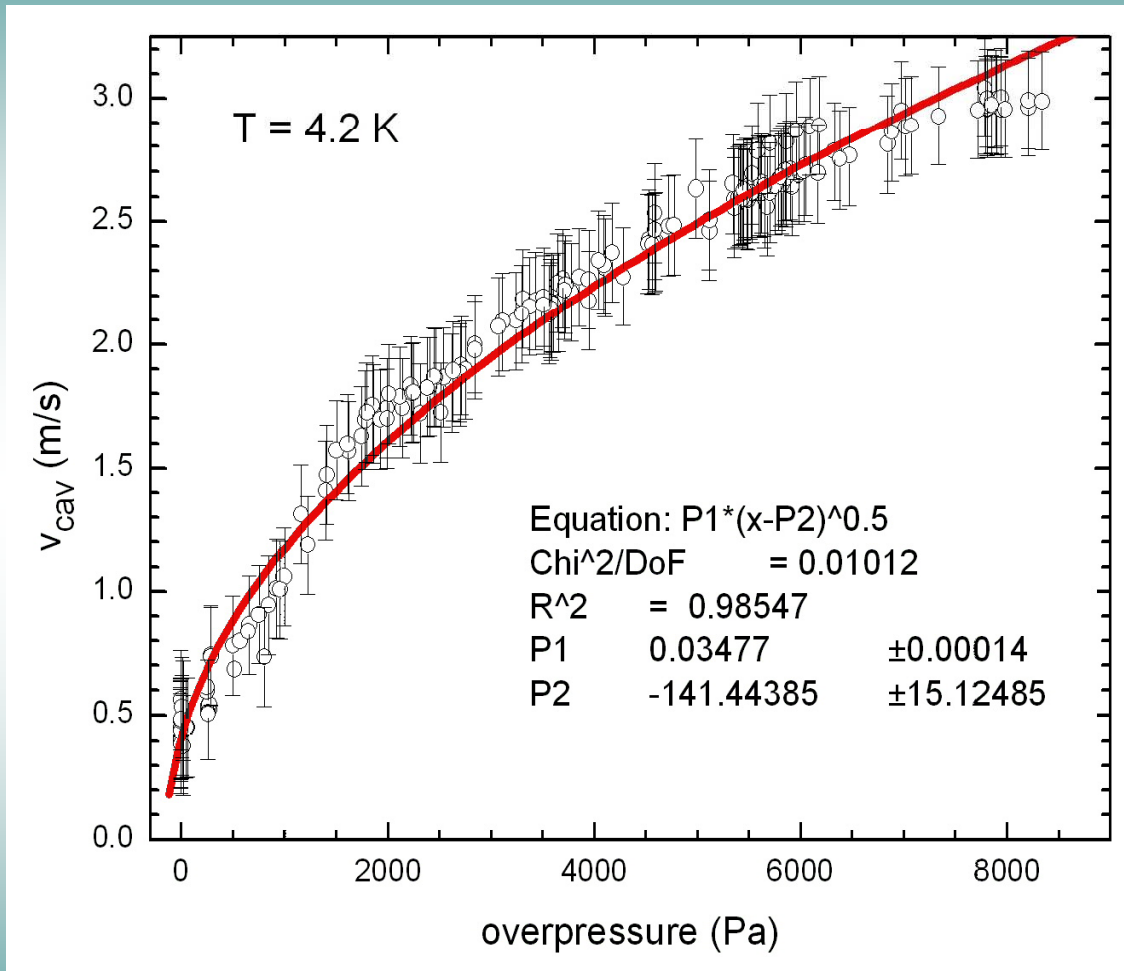


Standard nucleation theory does not explain the steep increase when crossing the superfluid transition

Explanation ????

# Bernoulli equation

$$p + \rho \frac{v^2}{2} = \text{const.}$$



# Conclusions

- Torsionally oscillating and vibrating submerged objects prove to be very useful tools to study classical fluid dynamics and superfluid hydrodynamics.
- Cryogenic helium offers an unprecedented range of easily tunable (p, T) flow properties, where response of these mechanical oscillators to an external drive of an externally applied flow can be monitored over many (8 ???) orders of magnitude.
- They can generate and detect turbulence (and transition to turbulence in particular) in gaseous helium, He I and He II as well as in  $^3\text{He}$ .
- Furthermore, vibrating quartz forks can be used to give us information about cavitation phenomena in He I and He II (quantum cavitation).