

Positron acceleration: a systematic overview

Severin Diederichs

Deutsches Elektronen-Synchrotron DESY, Germany

Lawrence Berkeley National Laboratory, USA

University of Hamburg, Germany

ALEGRO Workshop

23.03.2023

*“Key challenges to reach the high energy frontier include **a scheme** for positron bunch acceleration in plasma, that still needs to be demonstrated on paper.”*



Practical requirements for a linear collider

A plasma accelerator for a collider must fulfill:

1. High gradient (reduce the construction costs) $> \text{GV/m}$
2. Low emittance (ability to focus the beam) $< 100\text{s of nm}$
3. Low energy spread (ability to focus the beam, narrow energy spectrum) $< 1\%$
4. No intrinsic instability
5. High wall-plug efficiency (reduce run time costs) $> 5\%$

Practical requirements for a linear collider

A plasma accelerator for a collider must fulfill:

1. High gradient (reduce the construction costs) $> \text{GV/m}$
2. Low emittance (ability to focus the beam) $< 100\text{s of nm}$
3. Low energy spread (ability to focus the beam, narrow energy spectrum) $< 1\%$
4. No intrinsic instability
5. High wall-plug efficiency (reduce run time costs) $> 5\%$

Promising experiments:

[Corde Nature 2015](#)

[Gessner et al. Nat. Comm. 2016](#)

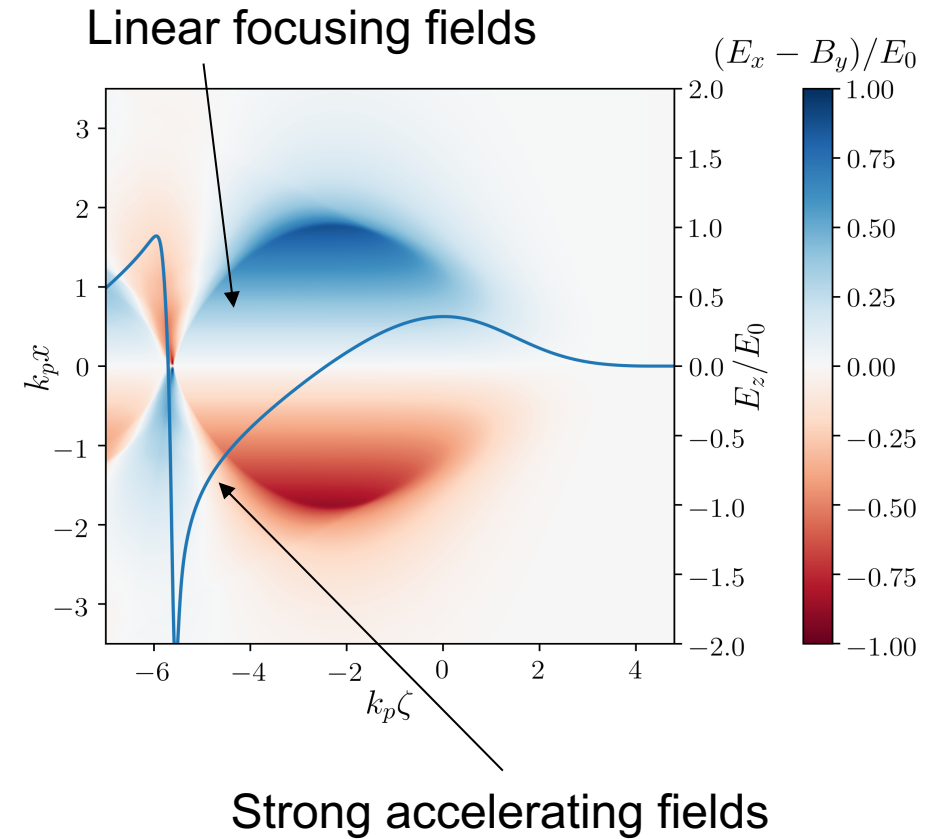
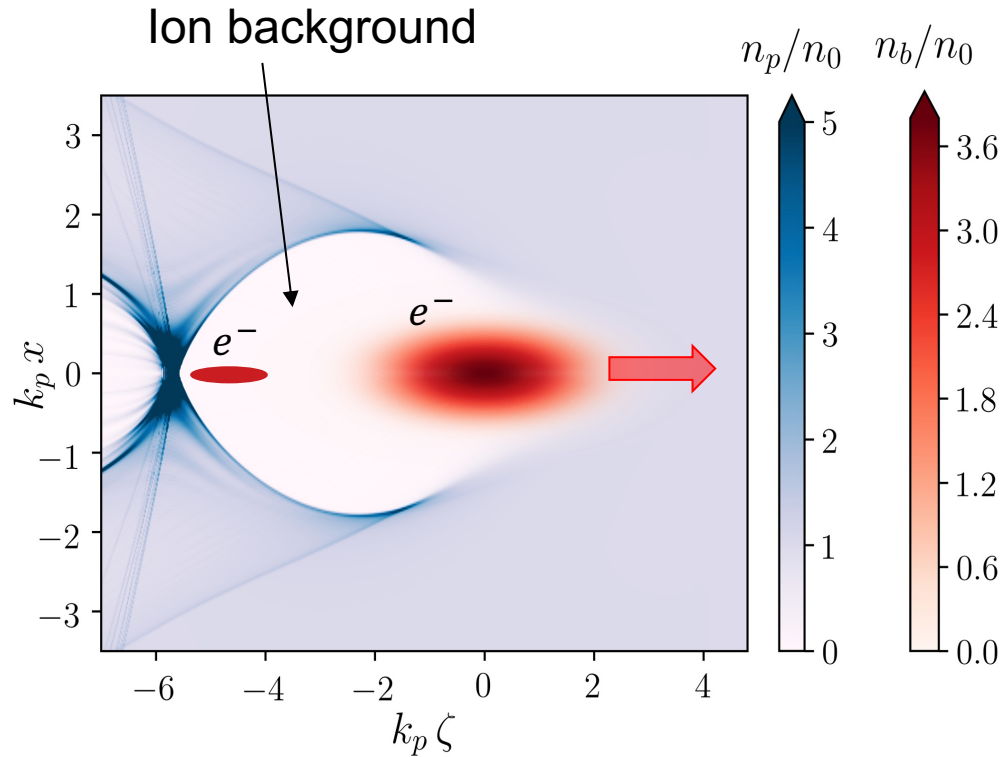
[Doche Sci. Rep. 2017](#)

[Lindstrøm PRL 2018](#)



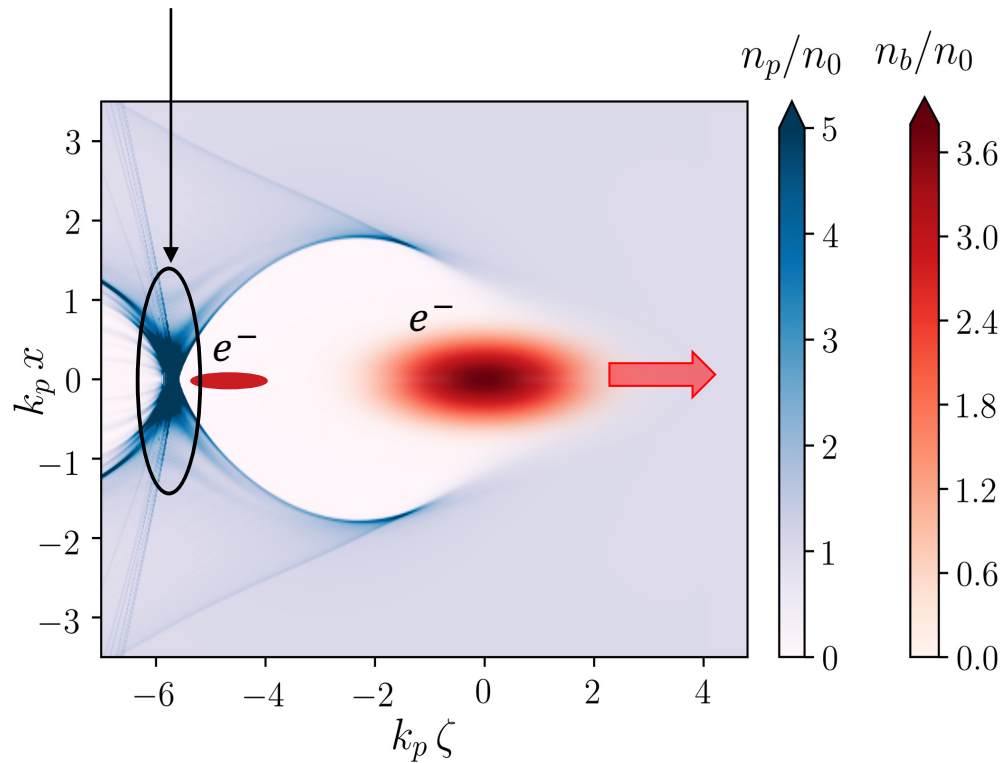
Emittance preservation and stability challenging
New concepts needed!

Plasma wakefield accelerators enable high-quality, high-gradient *electron* acceleration

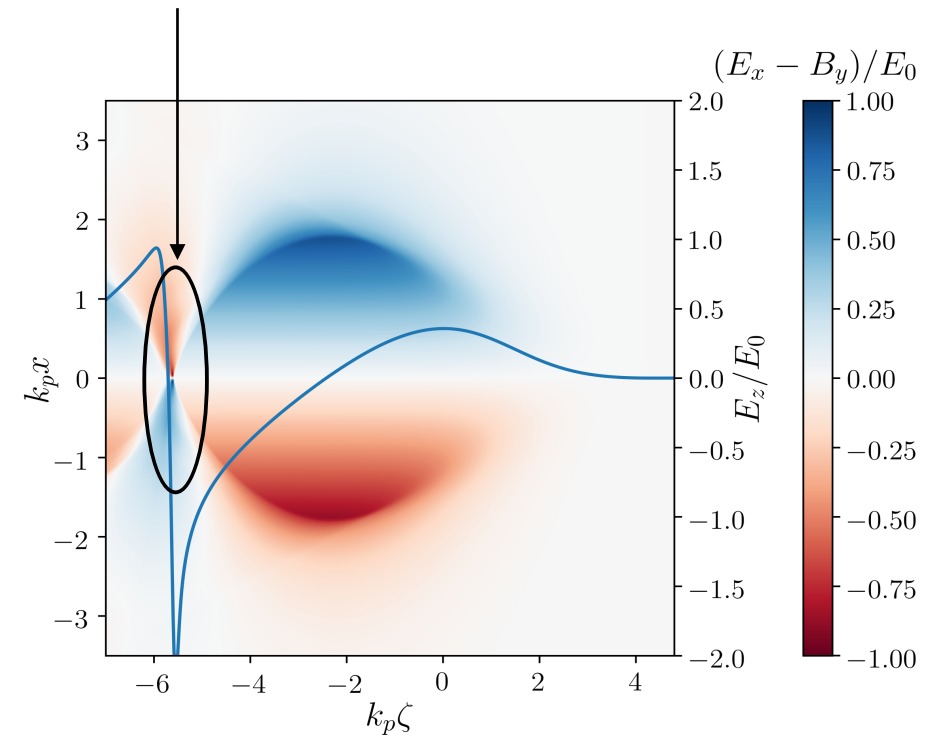


The electron spike at the back of the bubble enables positron acceleration

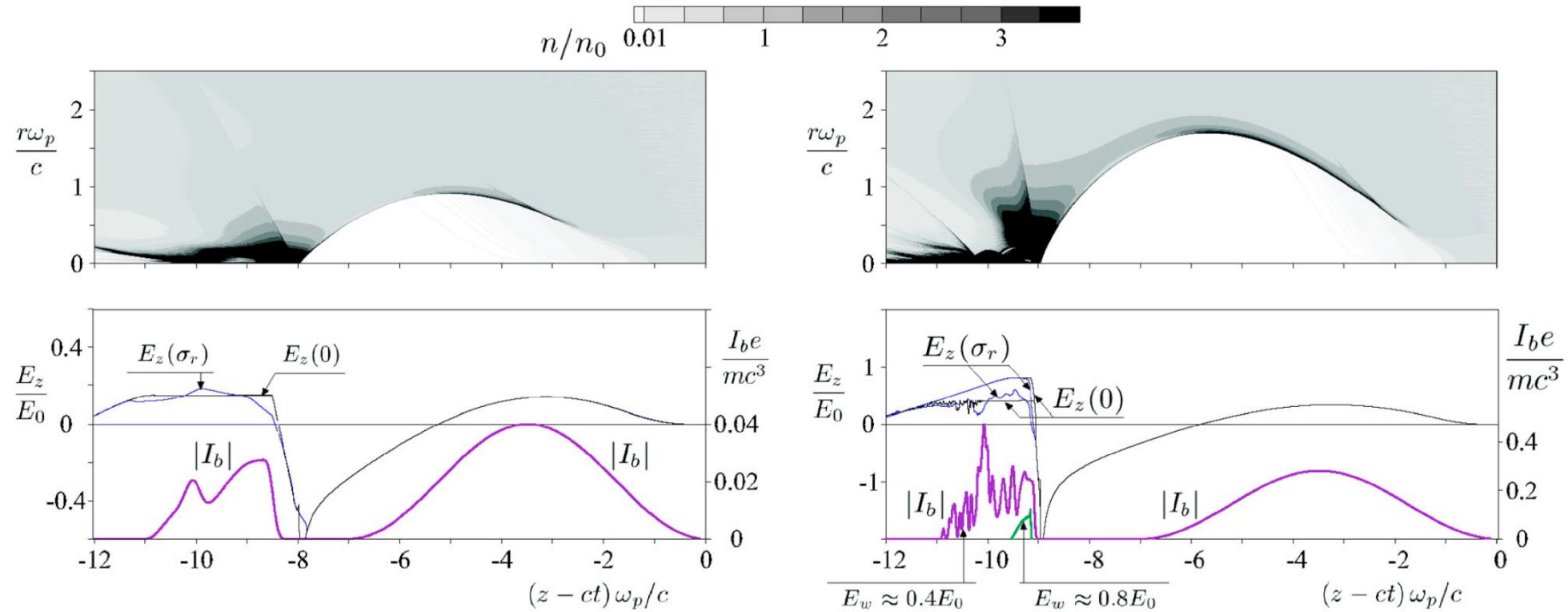
High density electron cusp



Focusing field for positrons

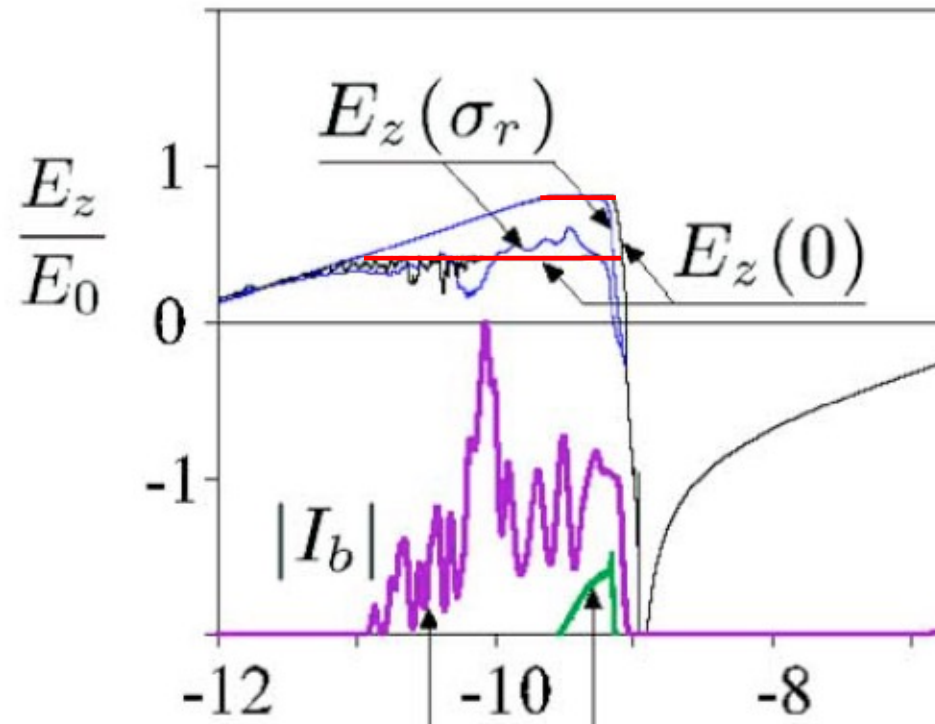


Proper beamloading enables positron acceleration at the back of the bubble



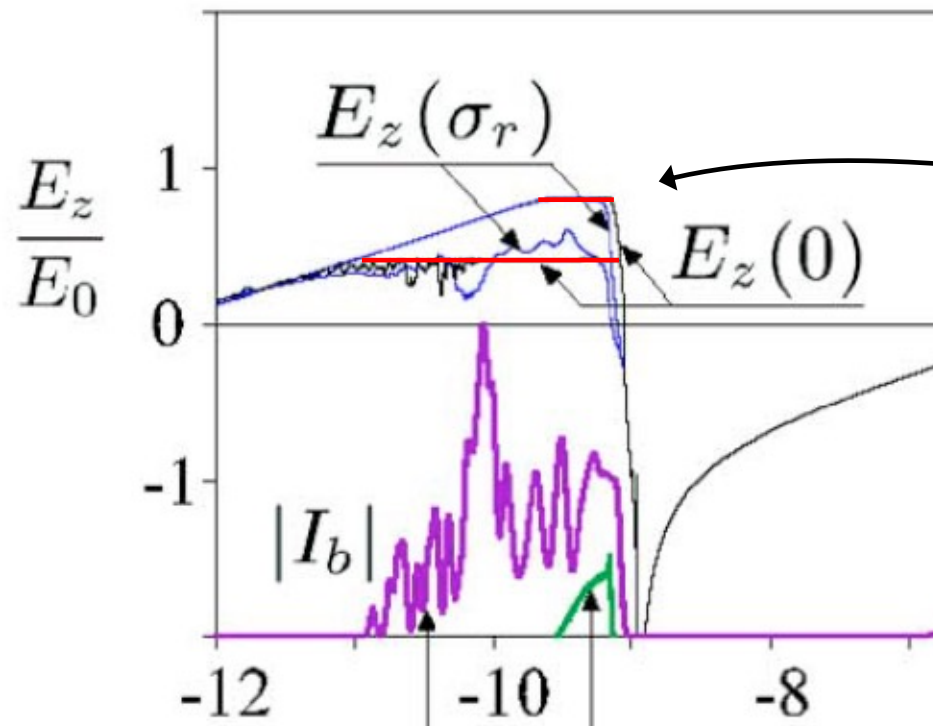
Lotov, PoP 14, 023101 (2007)

Any wakefield can be flattened by proper bunch shaping

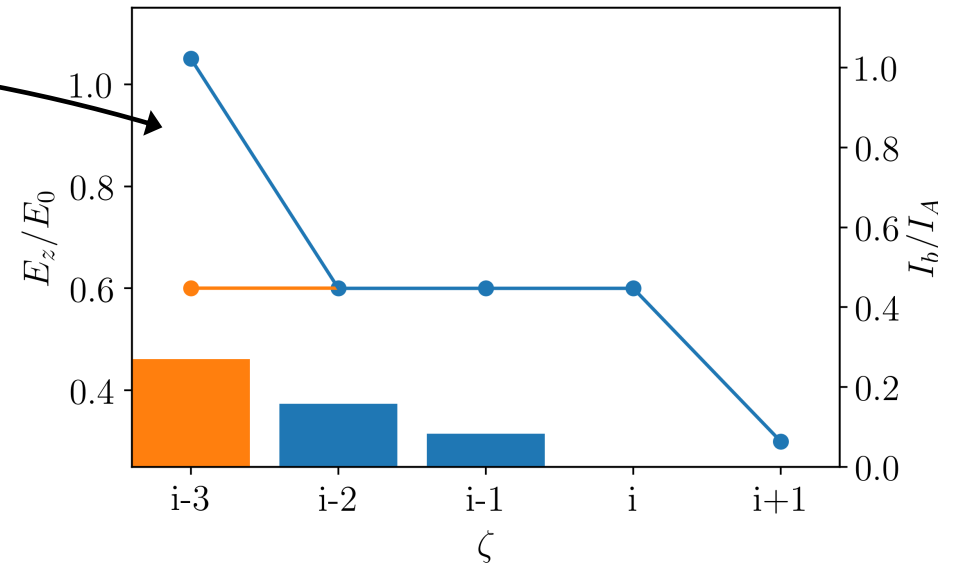


Lotov, PoP 14, 023101 (2007)

Any wakefield can be flattened by proper bunch shaping

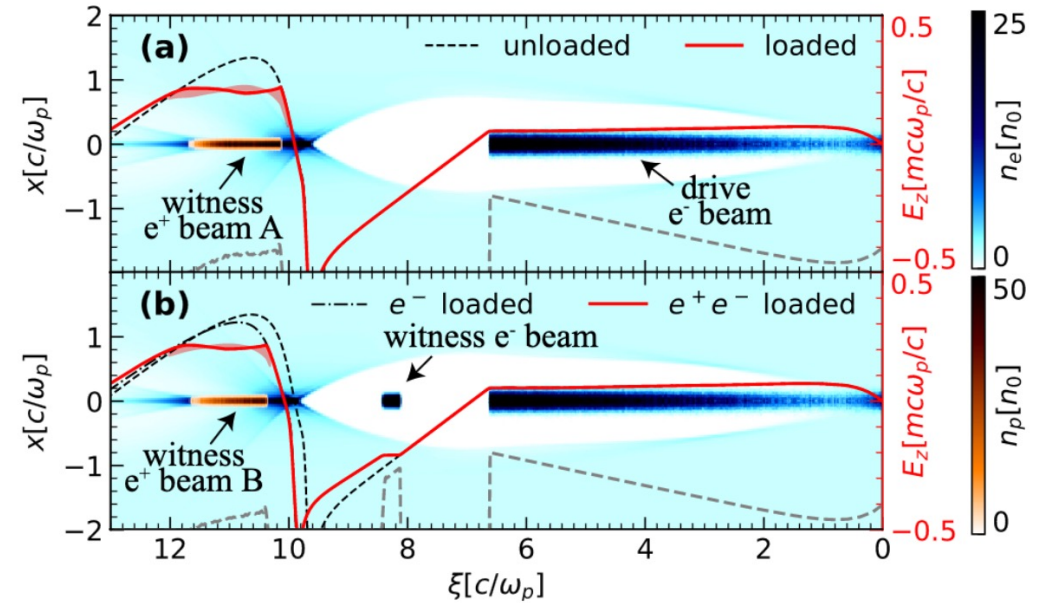
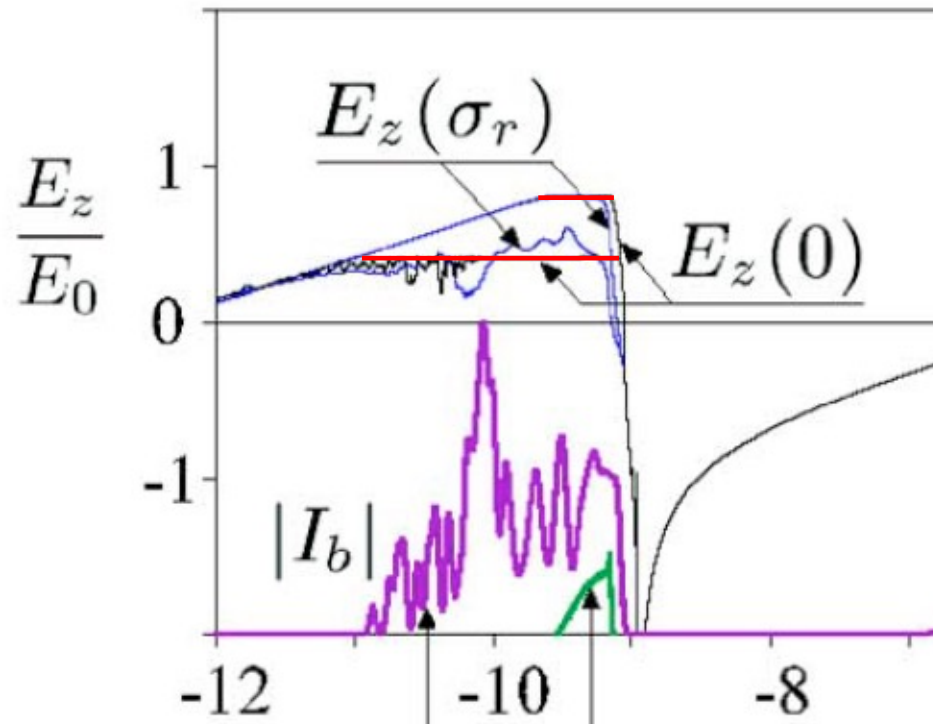


Slicing Advanced Loading Algorithm for Minimizing Energy spread (SALAME)



More information on the algorithm:
Diederichs et al., PRAB 2020
Lotov, PoP 12, 053105 (2005)
Lotov, PoP 14, 023101 (2007)

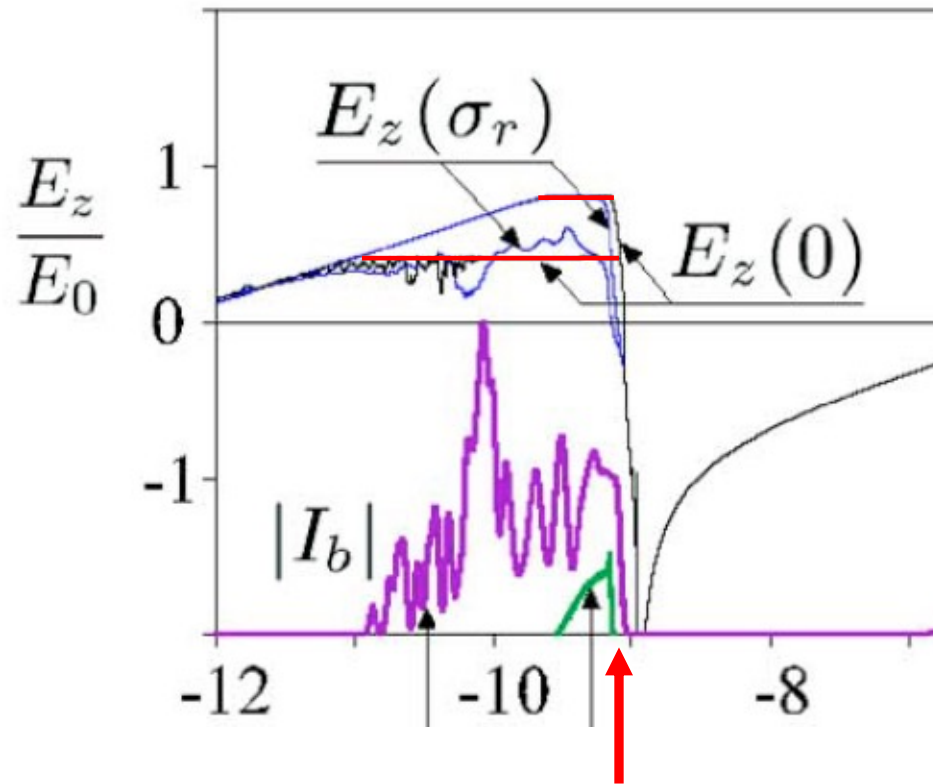
Any wakefield can be flattened by proper bunch shaping



Optimized to:
 130 pC
 2% rms energy spread
 < 10 μ m emittance
 35% transfer efficiency

Lotov, PoP 14, 023101 (2007)
 Zhou et al. arXiv:2211.07962v1

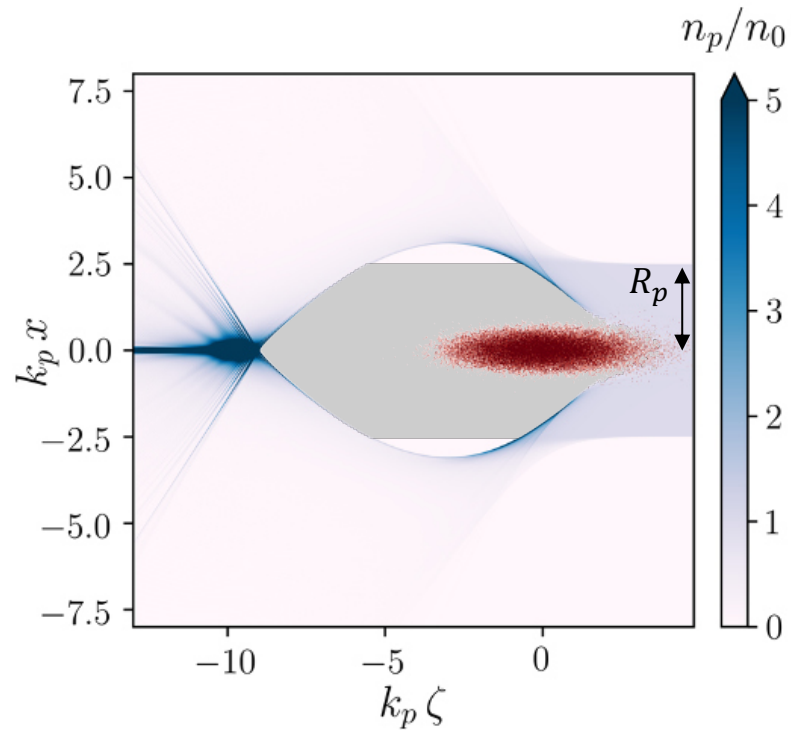
Required bunch shape in the electron spike sensitive to starting position



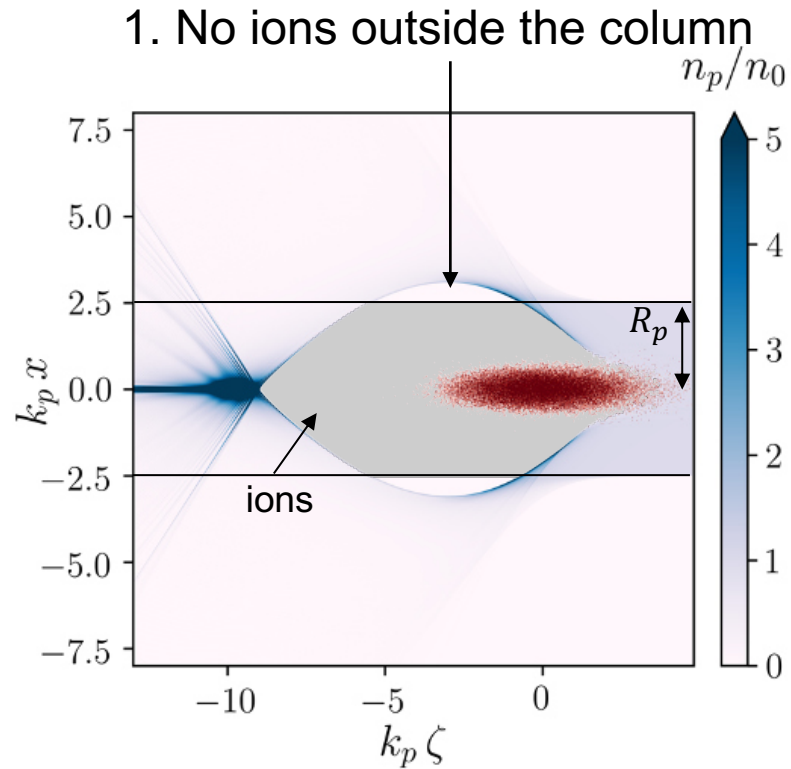
Can we relax the constraints?

Lotov, PoP 14, 023101 (2007)
Zhou et al. arXiv:2211.07962v1

Elongated plasma electron trajectories induce positron acc. field in pre-ionized plasma columns

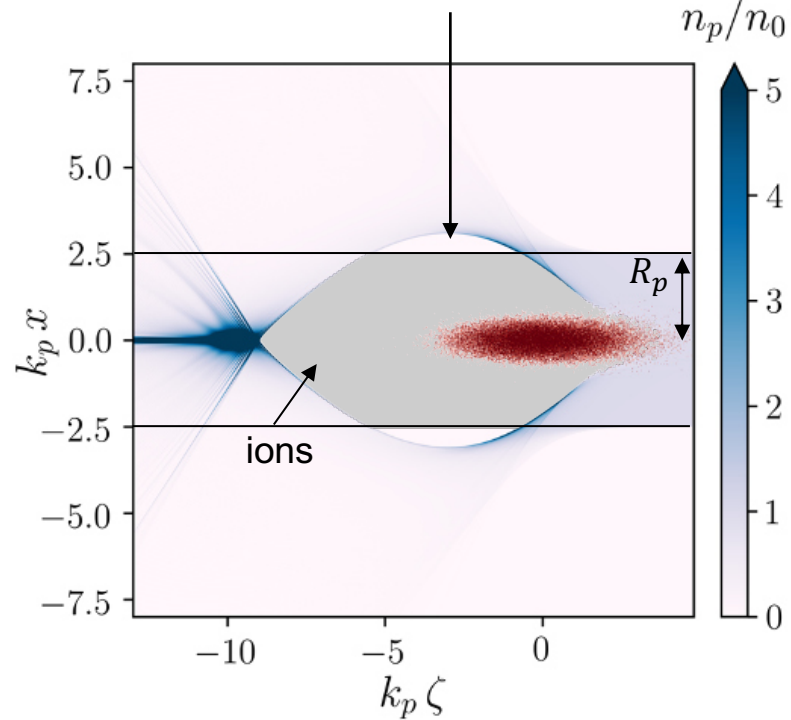


Elongated plasma electron trajectories induce positron acc. field in pre-ionized plasma columns

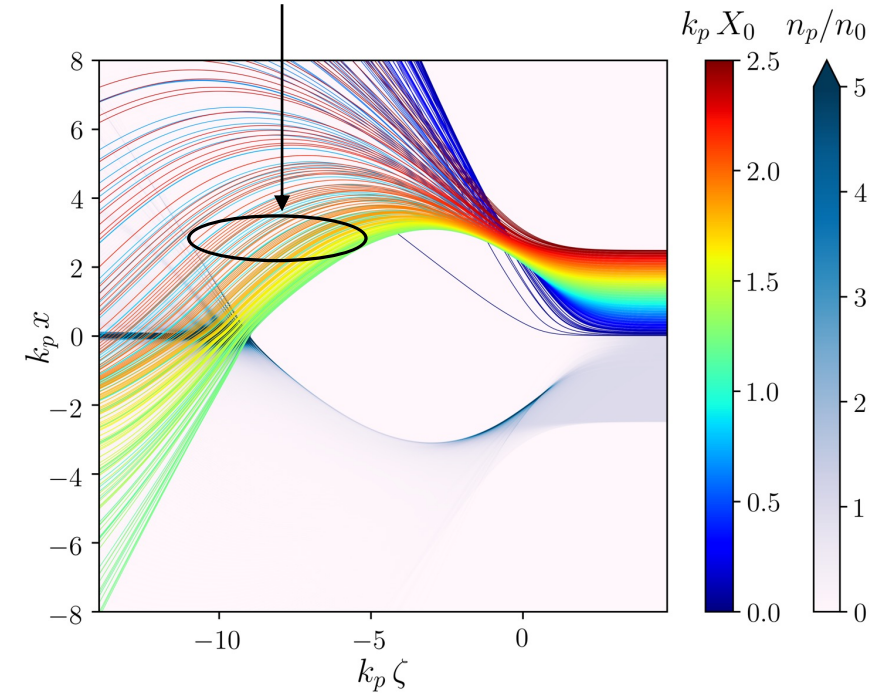


Elongated plasma electron trajectories induce positron acc. field in pre-ionized plasma columns

1. No ions outside the column

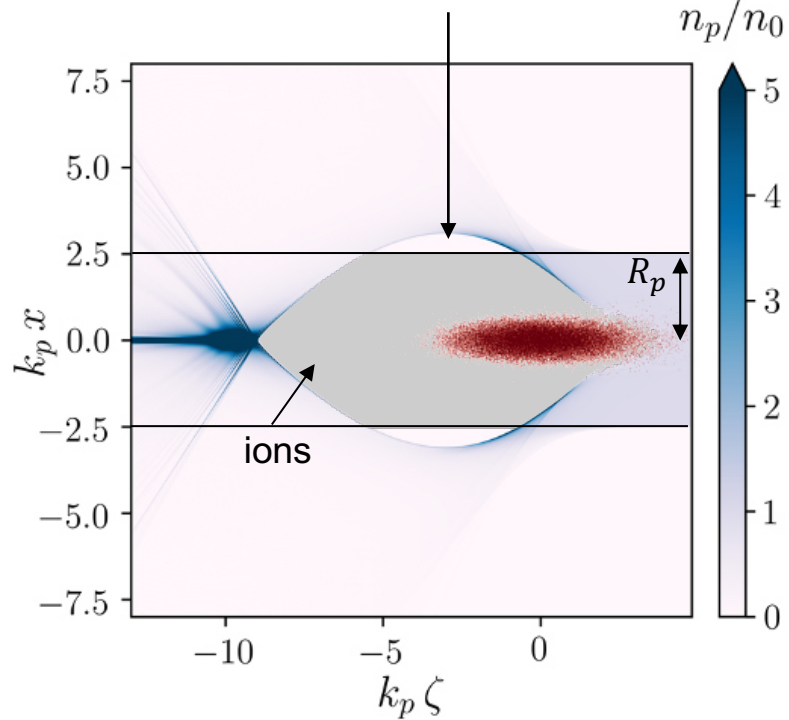


2. Elongated electron trajectories

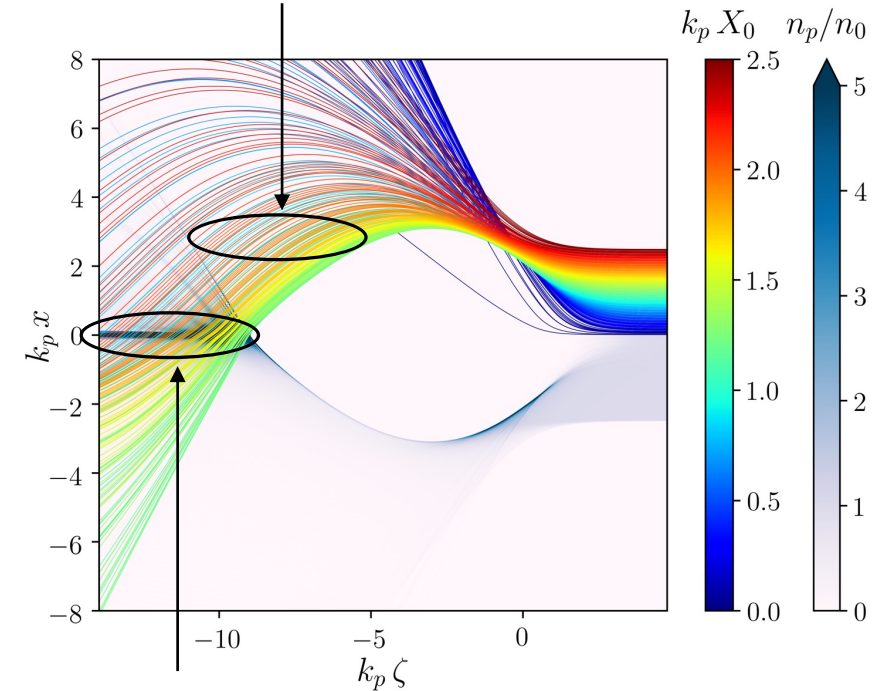


Elongated plasma electron trajectories induce positron acc. field in pre-ionized plasma columns

1. No ions outside the column



2. Elongated electron trajectories

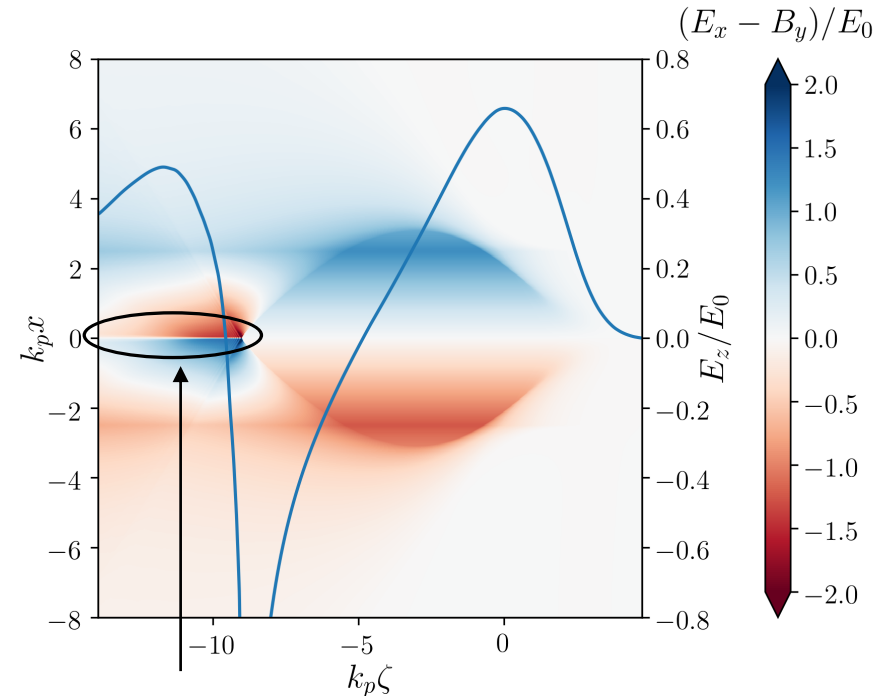
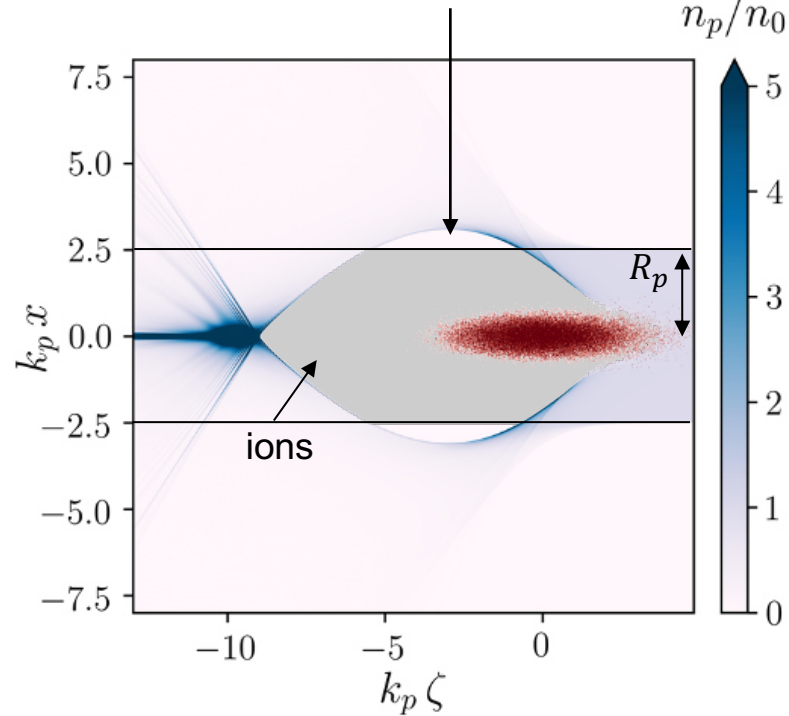


3. Long, high-density electron filament

Elongated plasma electron trajectories induce positron acc. field

in pre-ionized plasma columns

1. No ions outside the column



4. Accelerating and focusing fields for e^+

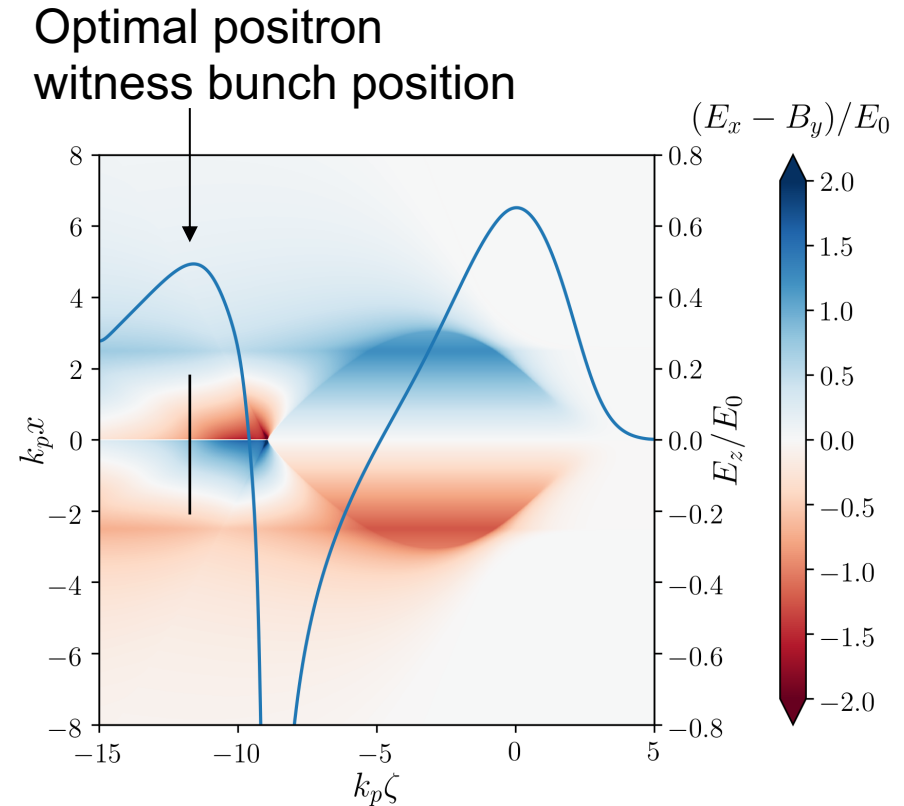
$$0.5E_0 \approx 15 \text{ GV/m} \quad \text{at } n_0 = 1 \times 10^{17} \text{ cm}^{-3}$$

Practical requirements for a linear collider

A plasma accelerator for a collider must fulfill:

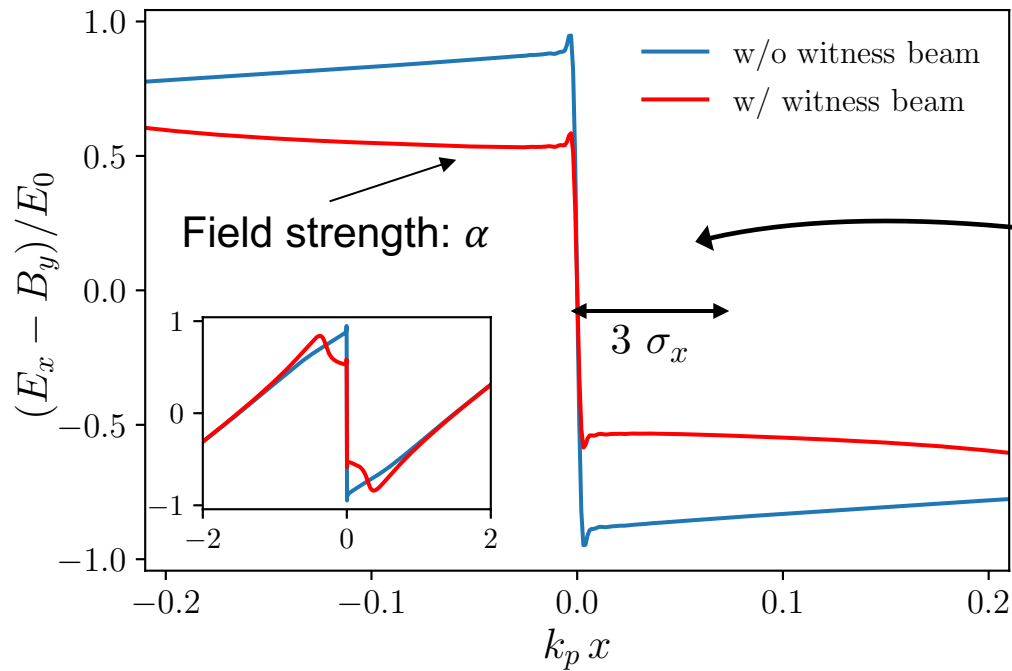
- | | | |
|---|--------------|-----------|
| 1. High gradient (reduce the construction costs) | > GV/m | 15 GV/m ✓ |
| 2. Low emittance (ability to focus the beam) | < 100s of nm | |
| 3. Low energy spread (ability to focus the beam, narrow energy spectrum) | < 1% | |
| 4. No intrinsic instability | | |
| 5. High wall-plug efficiency (reduce run time costs) | > 5% | |

Emittance preservation requires matched beams



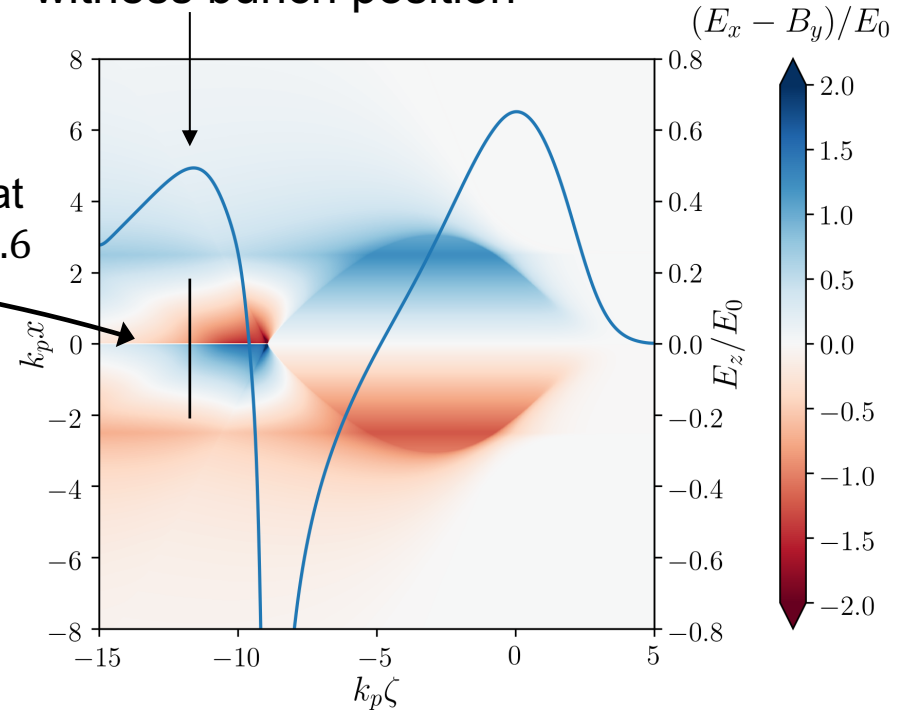
Emittance preservation requires matched beams

Ultra-high resolution simulation with INF&RNO (RZ)



Optimal positron witness bunch position

Line-out at $\zeta \approx -11.6$



Witness beam parameters:

$$k_p \sigma_x = 0.025, k_p \sigma_z = 0.5, n_b/n_0 = 500$$

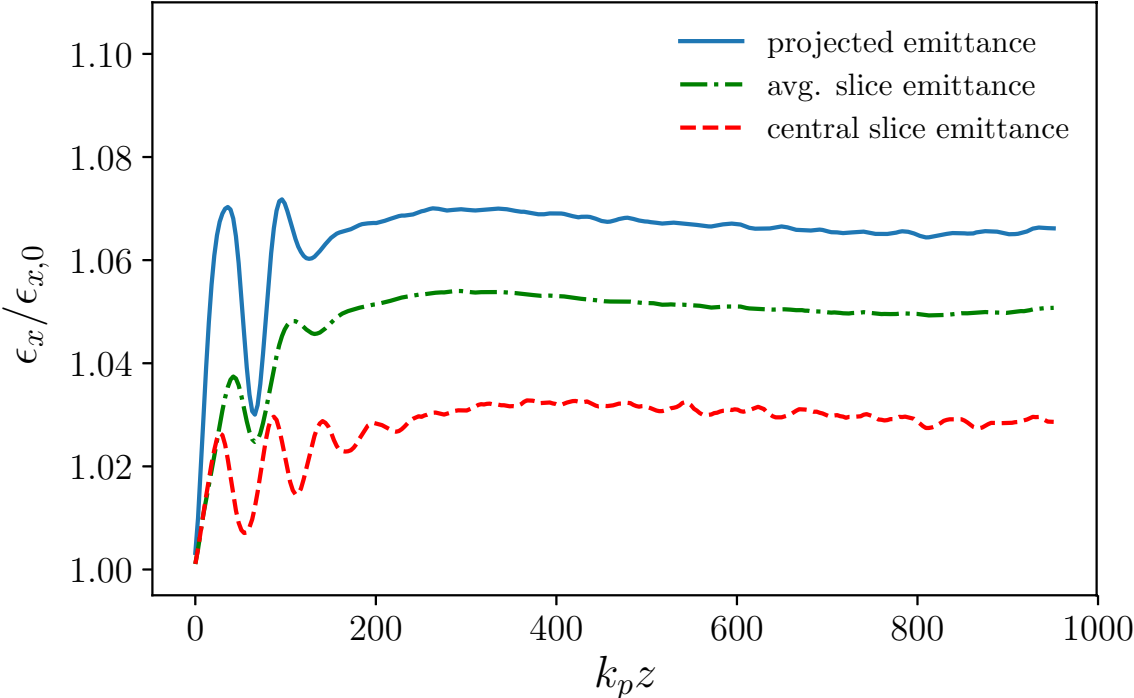
Non-linear field induces emittance growth
Quasi-matching?

Emittance growth quickly saturates

At $n_0 = 5 \times 10^{17} \text{ cm}^{-3}$: $\epsilon_{x,0} = 0.7 \mu\text{m}$

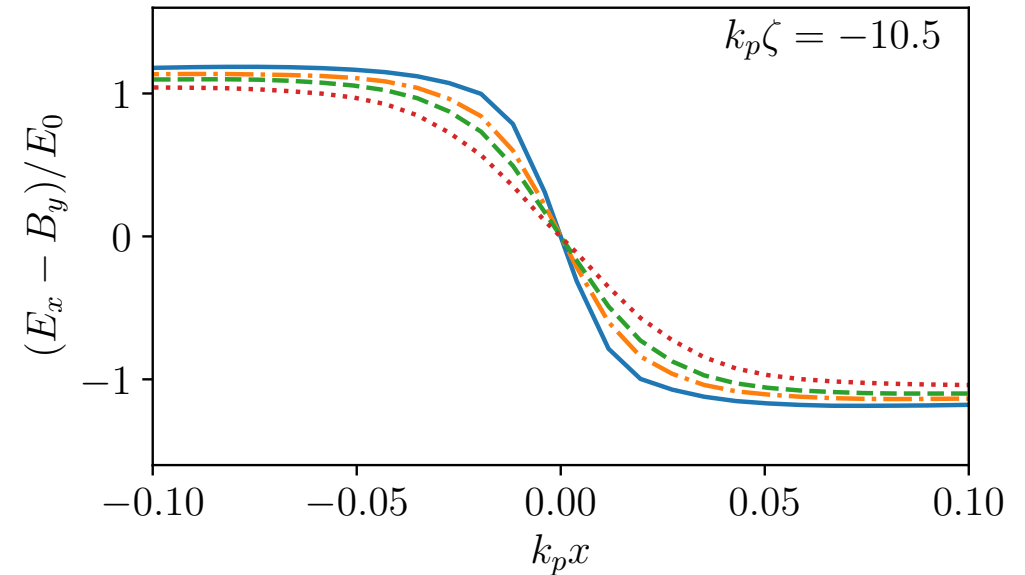
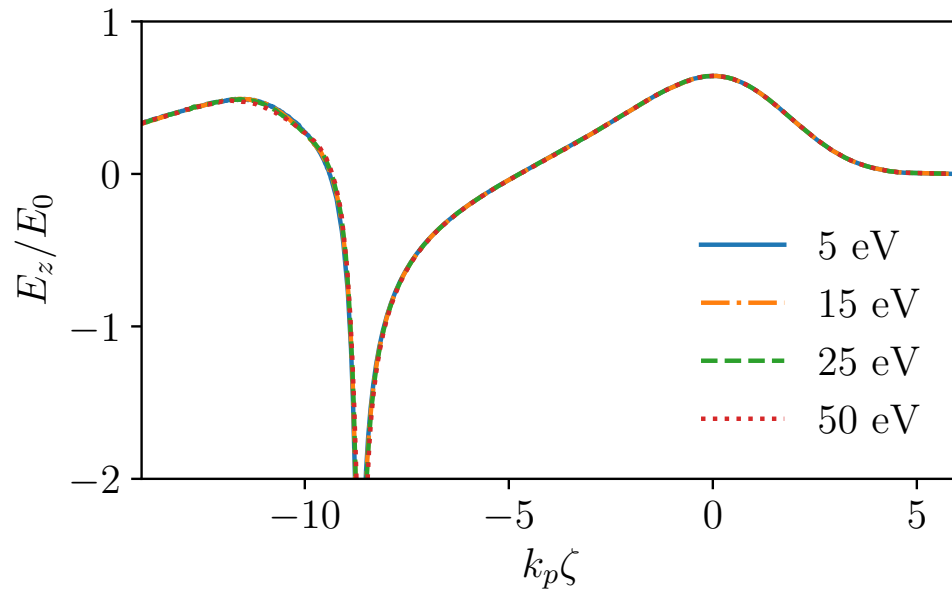
Emittance is resolution limited,
cannot resolve smaller beams

Positron beam emittance evolution
with a fixed driver



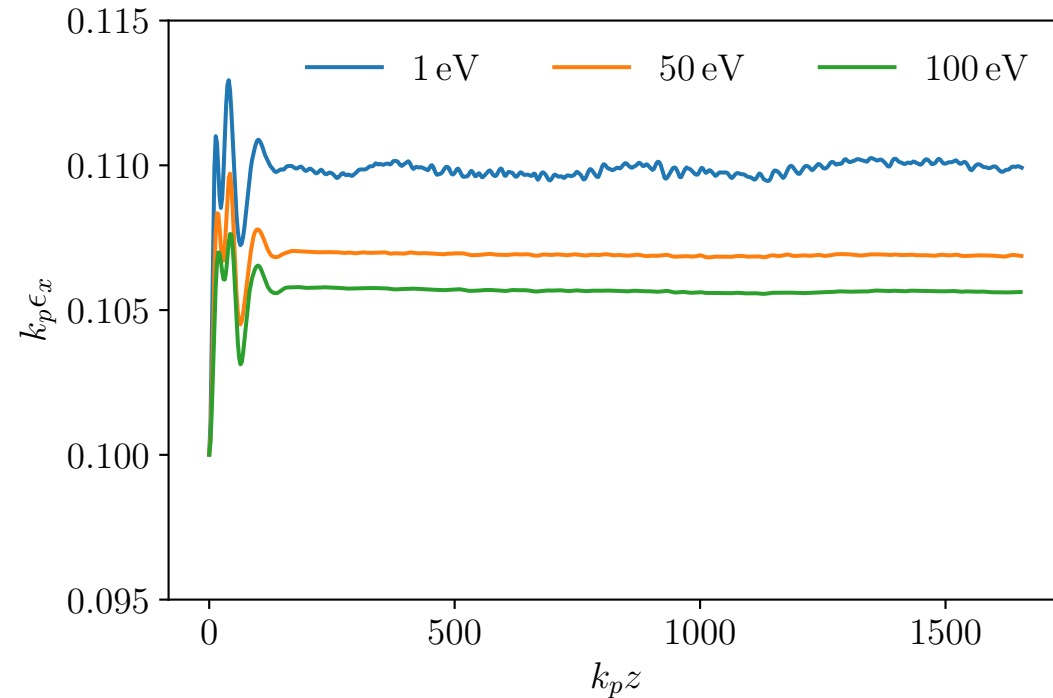
C. Benedetti et al., PRAB 2017
S. Diederichs et al., PRAB 2019

Temperature linearizes focusing field



Diederichs et al. (in preparation)
Wang et al., [arXiv:2110.10290](https://arxiv.org/abs/2110.10290) (2021)

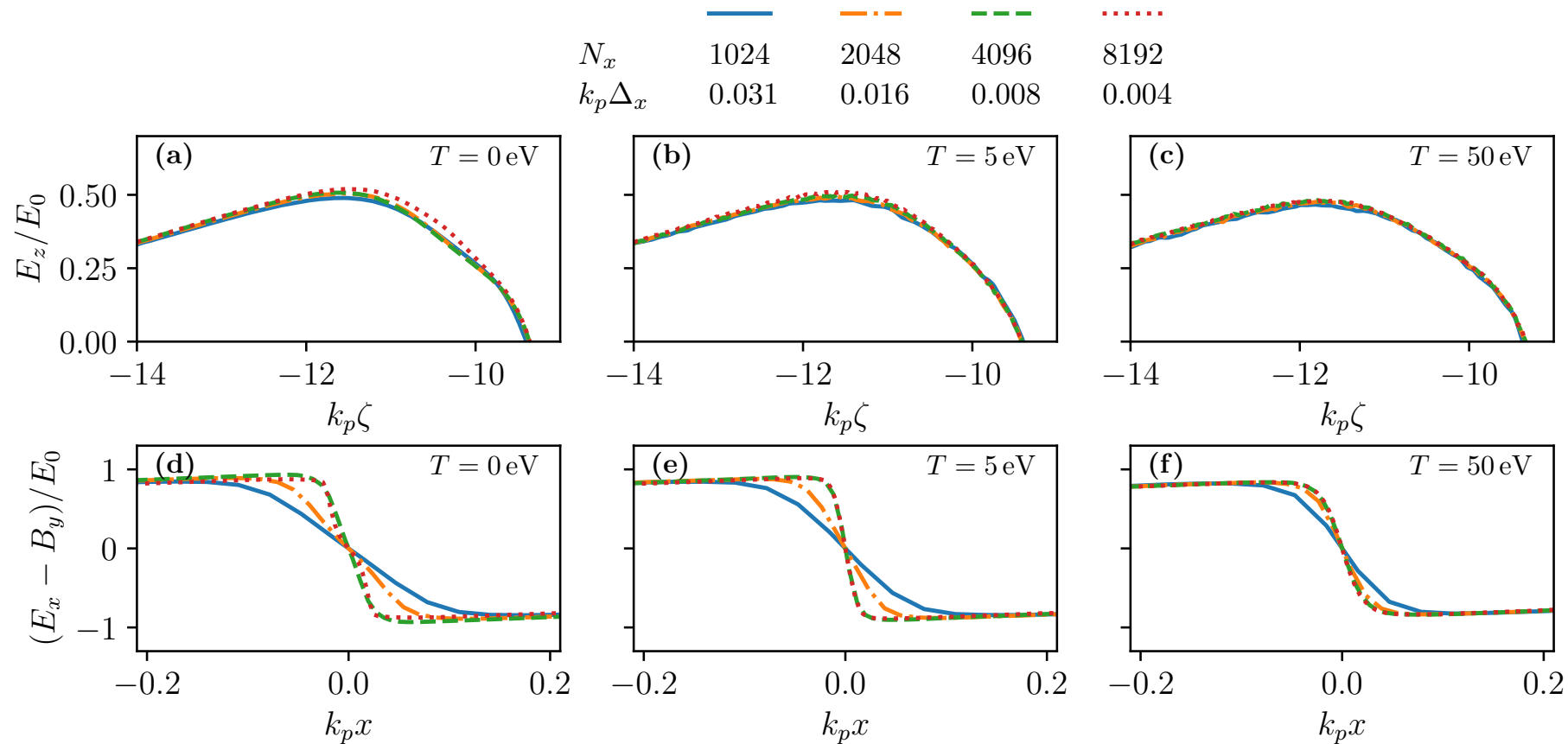
Temperature linearizes focusing field



Even better for emittance preservation!

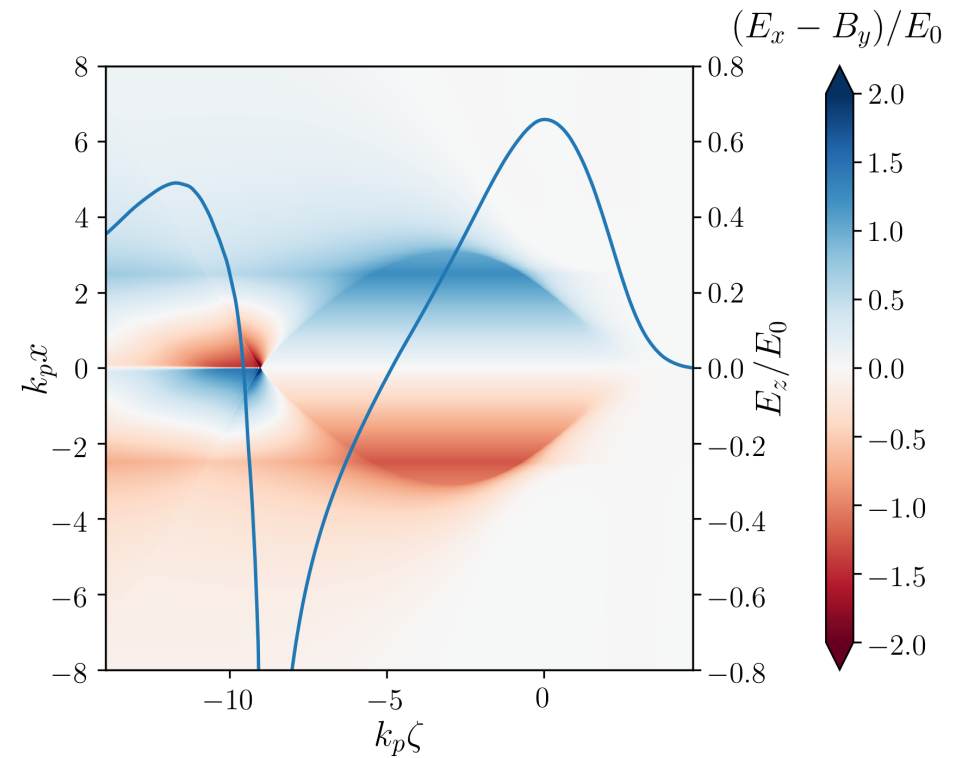
Diederichs et al. (in preparation)

Temperature mandatory for convergence

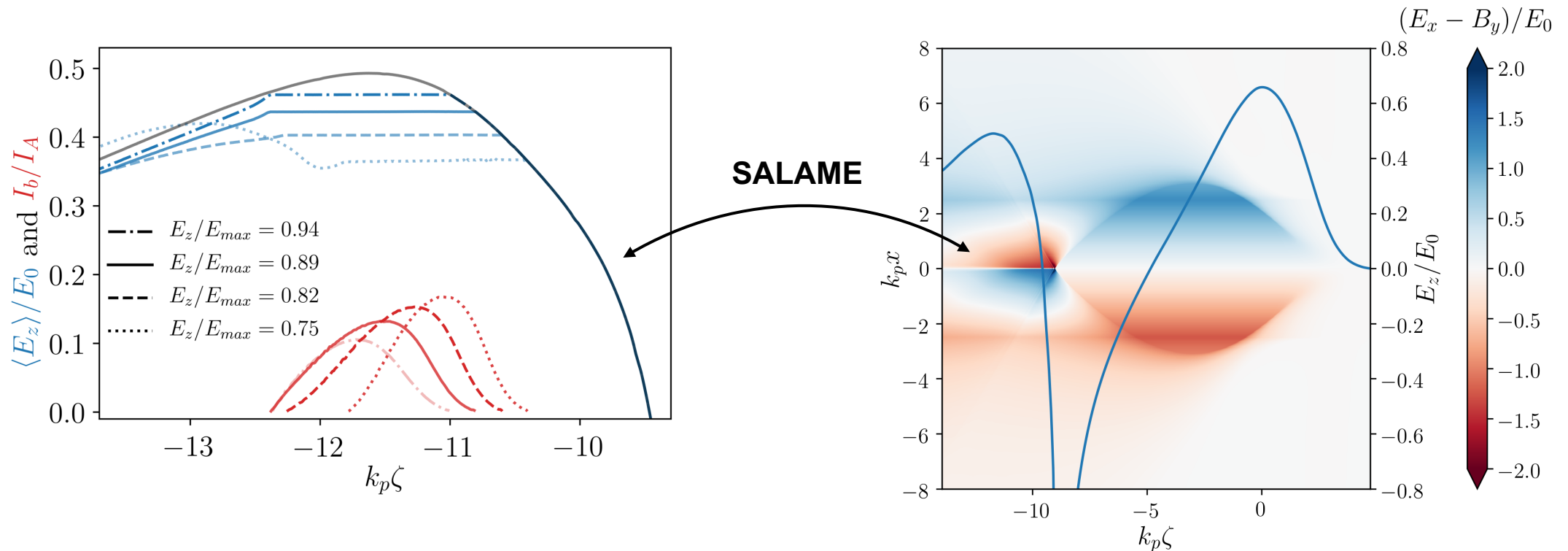


Diederichs et al. (in preparation)
 Wang et al., [arXiv:2110.10290](https://arxiv.org/abs/2110.10290) (2021)
 Jain et al. PoP (2015)

Positron accelerating field is non-uniform



Optimal beam loading enables low-energy-spread and low-emittance positron acceleration



witness beam: 50 pC
 < 0.5 μm normalized emittance
 < 1% relative energy spread
 \approx 3% transfer efficiency (to be optimized)

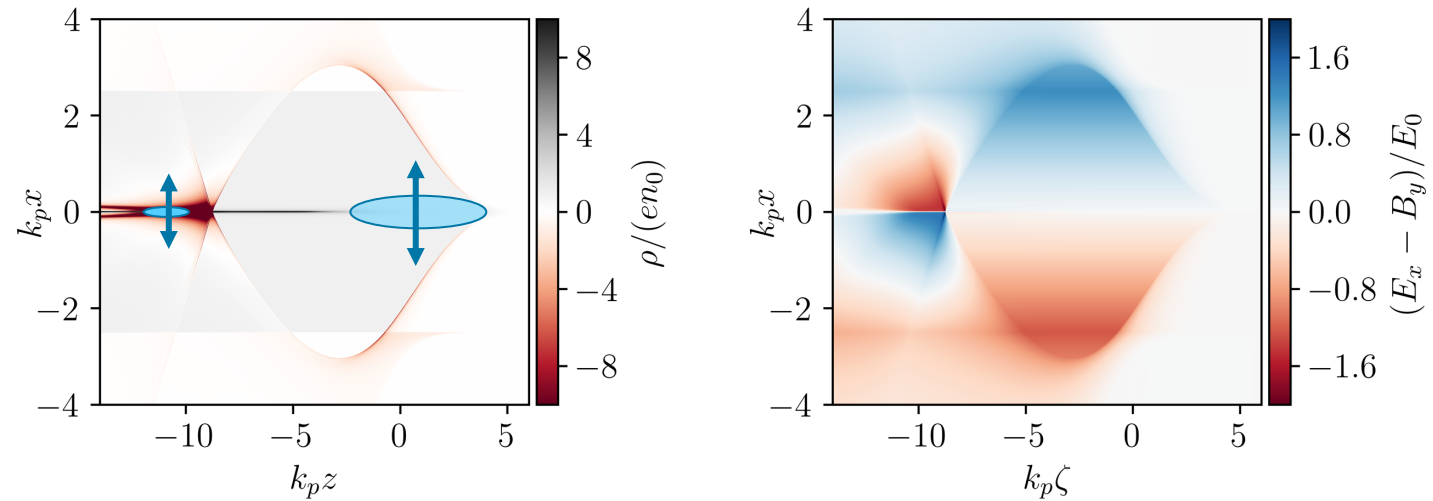
Diederichs et al., PRAB 2020

Practical requirements for a linear collider

A plasma accelerator for a collider must fulfill:

- | | | |
|--|--------------|------------|
| 1. High gradient (reduce the construction costs) | > GV/m | 15 GV/m ✓ |
| 2. Low emittance (ability to focus the beam) | < 100s of nm | < 500 nm ✓ |
| 3. Low energy spread (ability to focus the beam, narrow energy spectrum) | < 1% | < 1% ✓ |
| 4. No intrinsic instability | | |
| 5. High wall-plug efficiency (reduce run time costs) | > 5% | |

Stability is crucial for a cylindrical symmetric setup

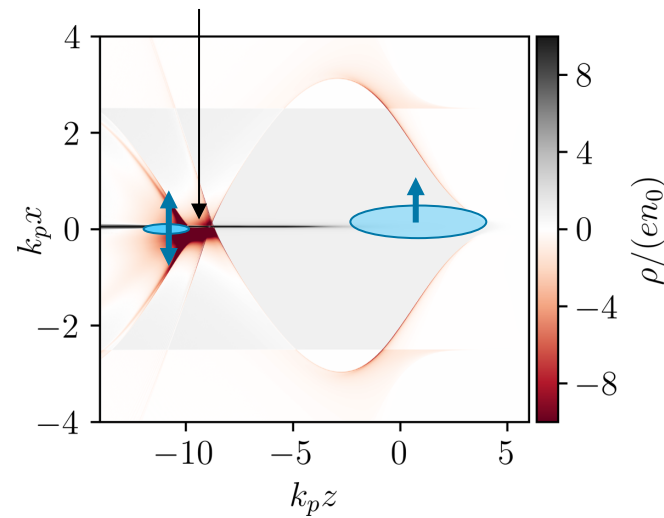


Instabilities can be induced by

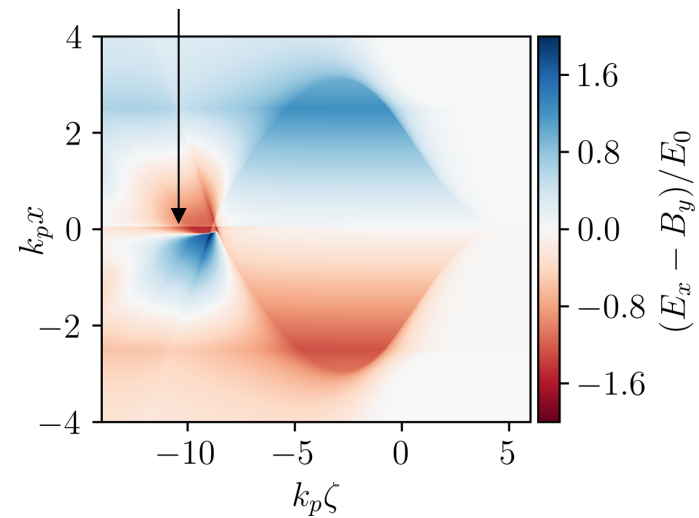
- Misalignment between driver and column
- Beam asymmetries, e.g., tilts

Stability is crucial for a cylindrical symmetric setup

Perturbed electron filament



Perturbed wakefield centroid $\langle W \rangle$

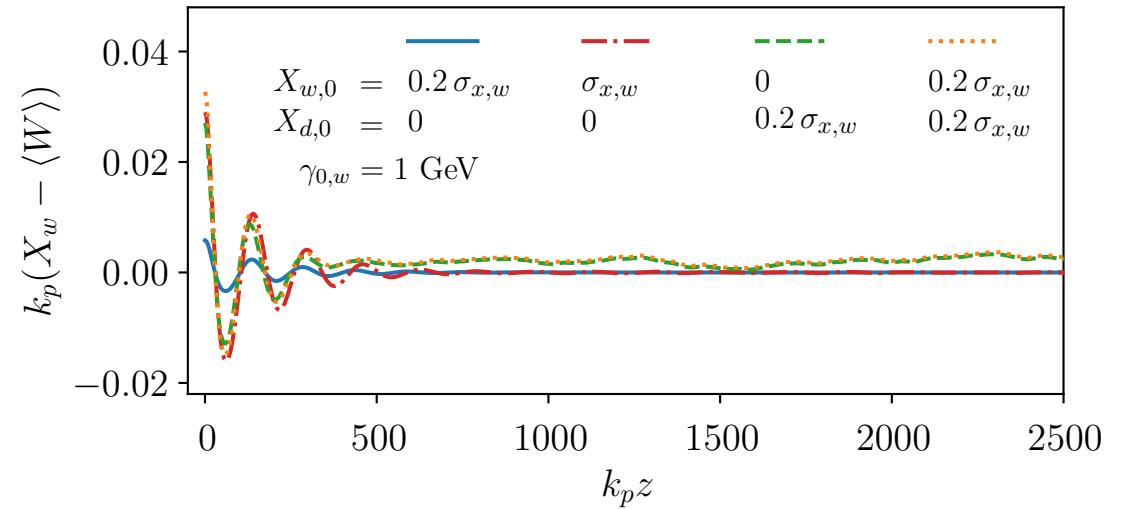
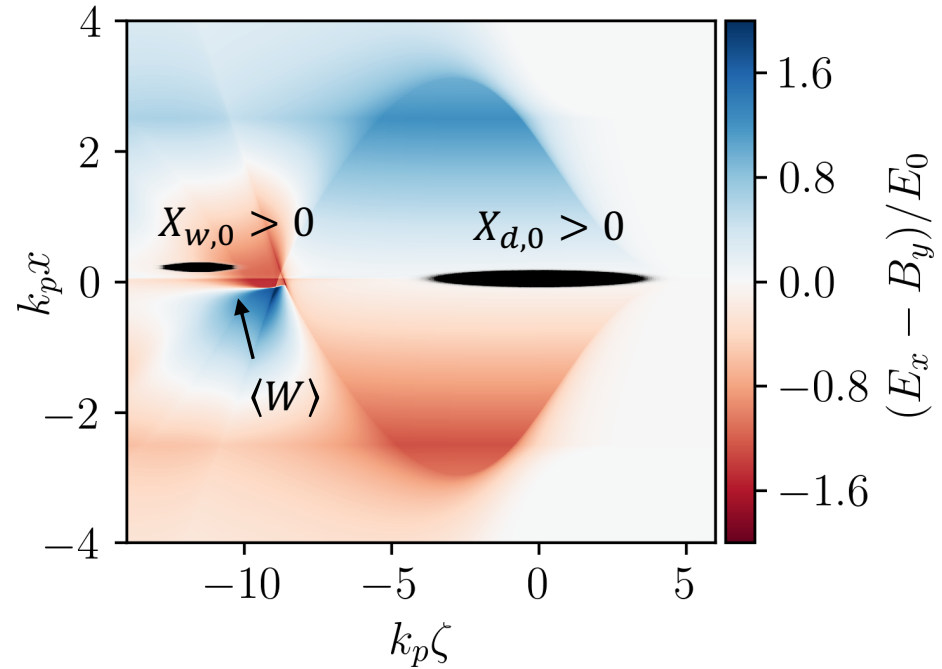


Instabilities can be induced by

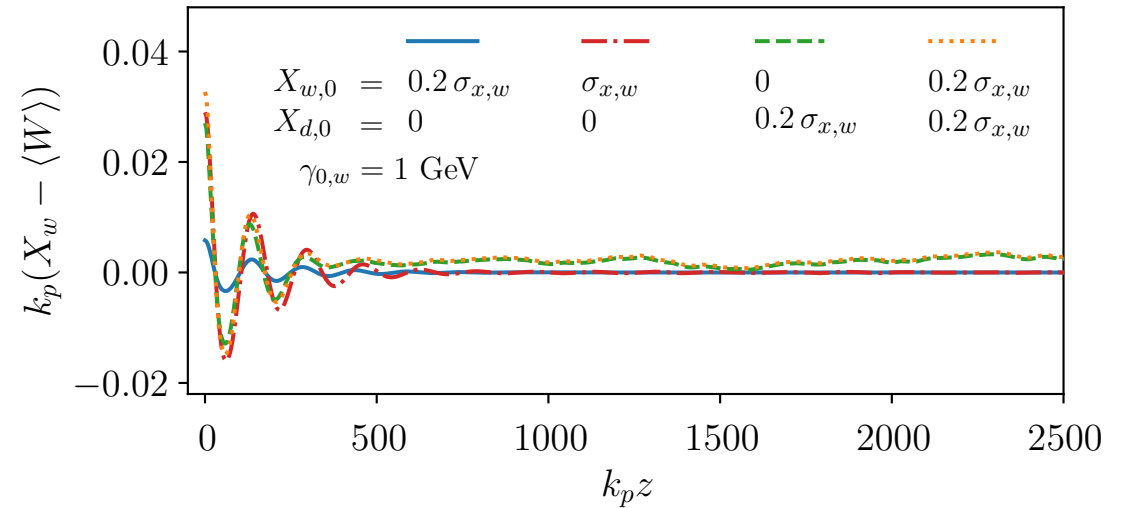
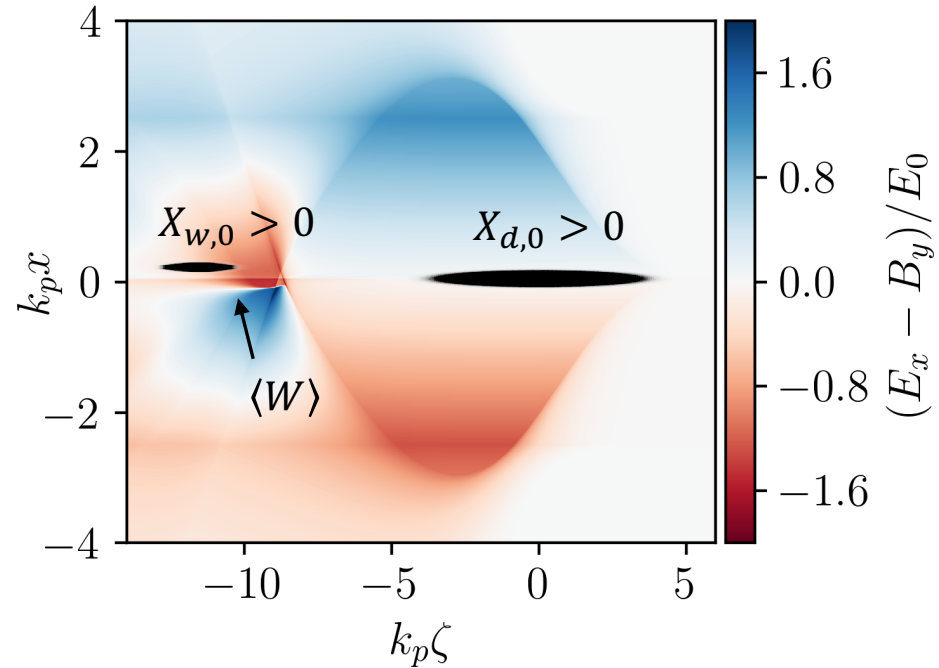
- Misalignment between driver and column
- Beam asymmetries, e.g., tilts

What is the impact on the witness beam quality?

Witness beam is not susceptible to hosing



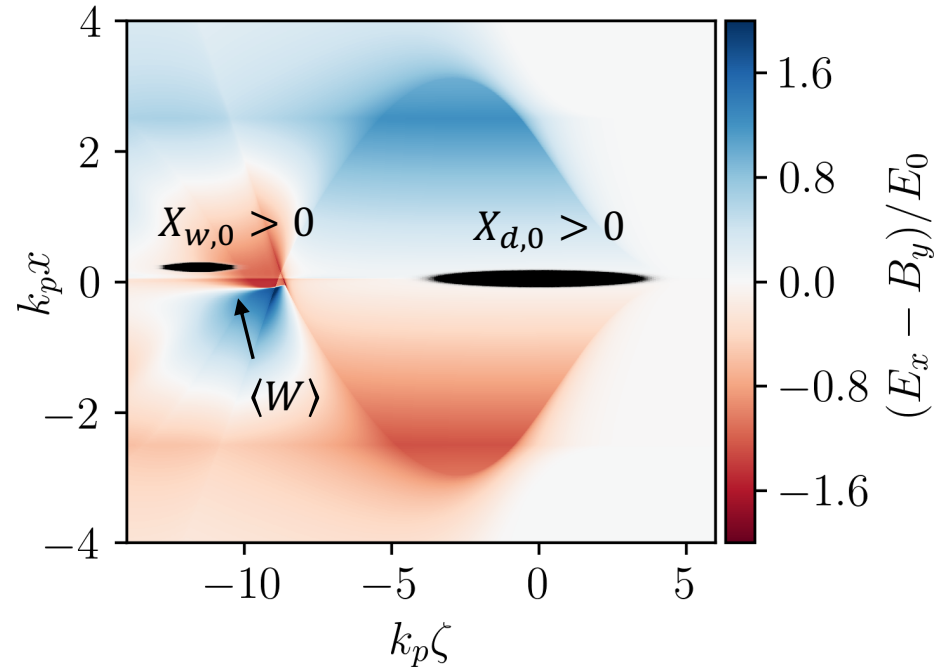
Witness beam is not susceptible to hosing



Hosing is prevented for 2 reasons:

1. **Longitudinally varying focusing field (BNS damping)**
2. Phase-mixing within each slice

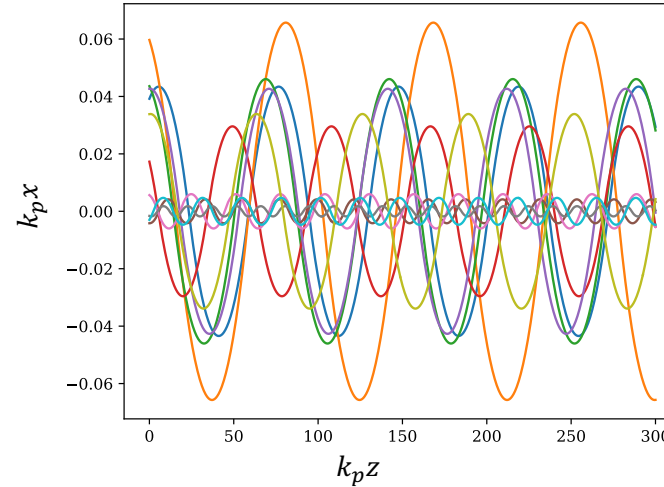
Witness beam is not susceptible to hosing



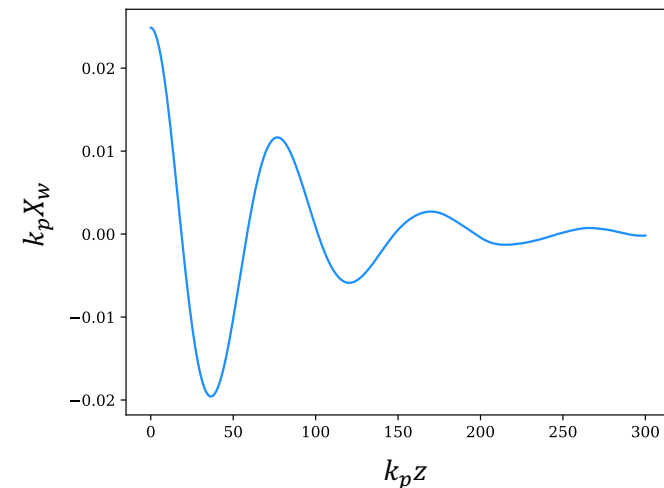
Hosing is prevented for 2 reasons:

1. Longitudinally varying focusing field (BNS)
2. **Phase-mixing within each slice**

Single-particle trajectories



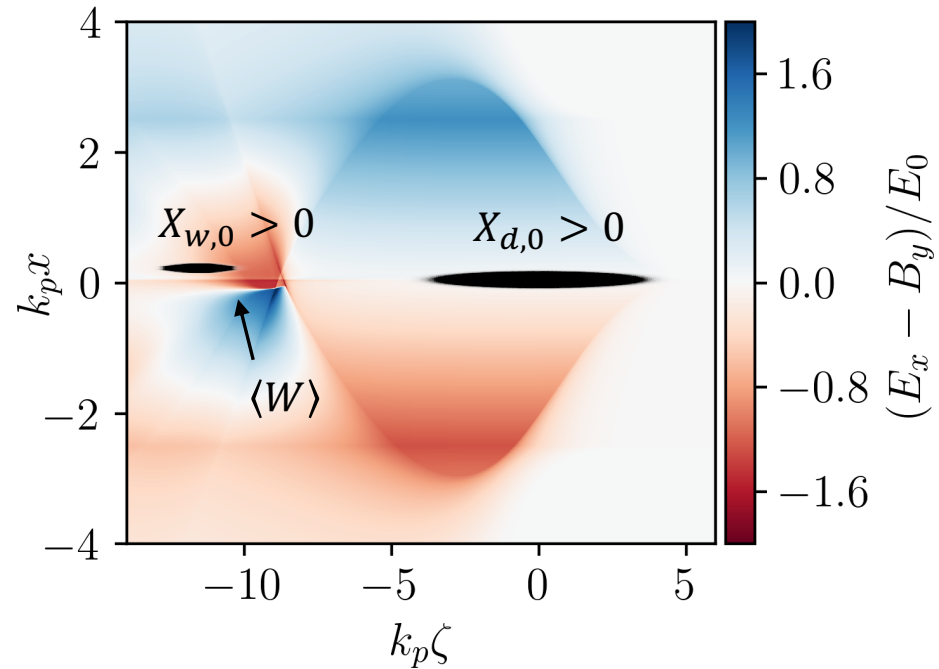
Bunch centroid trajectory



1D beam in step-like field
with field strength α
Damping length:

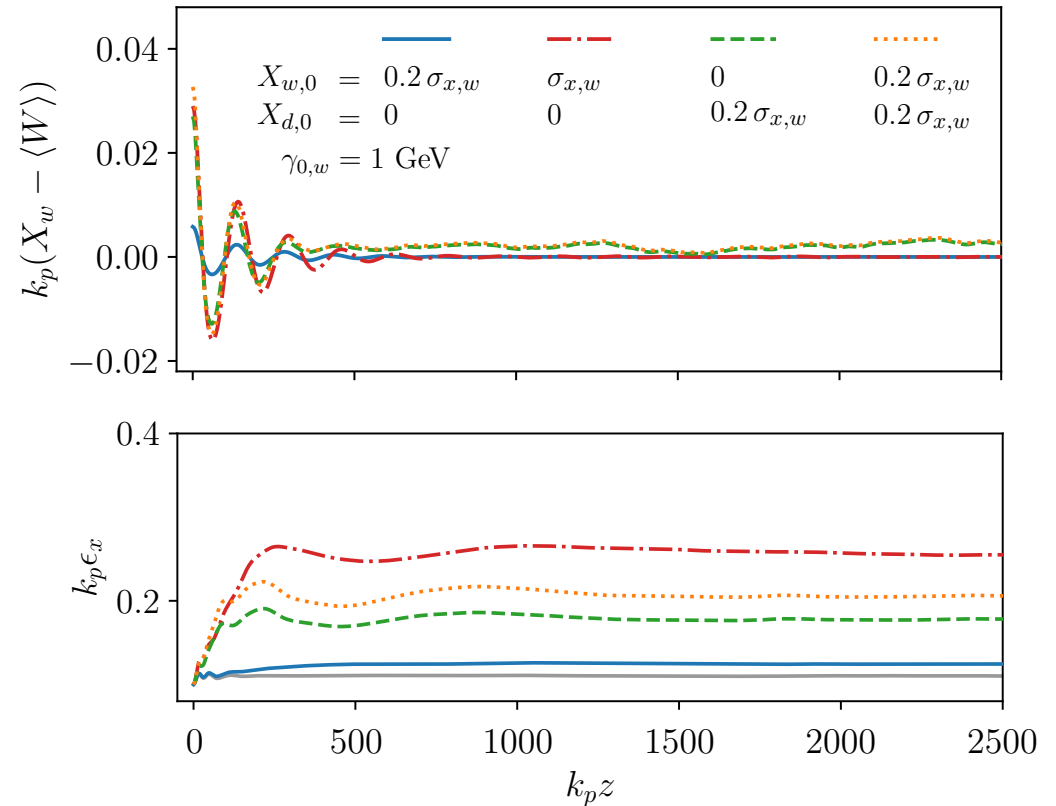
$$k_p S_{\text{damp}} \propto \sqrt{\frac{k_p \sigma_{x,w} \gamma}{\alpha}}$$

Witness beam is not susceptible to hosing



Hosing is prevented for 2 reasons:

1. Longitudinally varying focusing field (BNS)
2. **Phase-mixing within each slice**



Initial offsets increase the emittance but growth saturates quickly! Similar to e^-

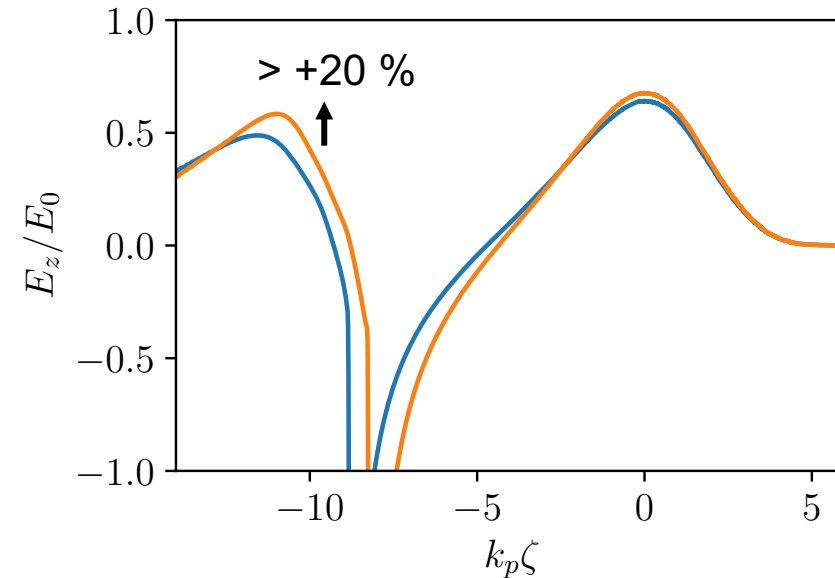
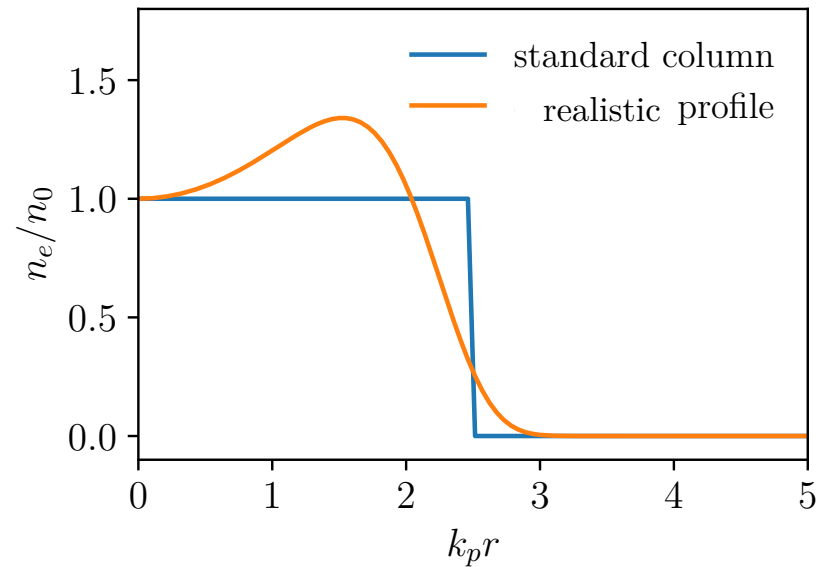
Diederichs et al., PRAB 2022

Practical requirements for a linear collider

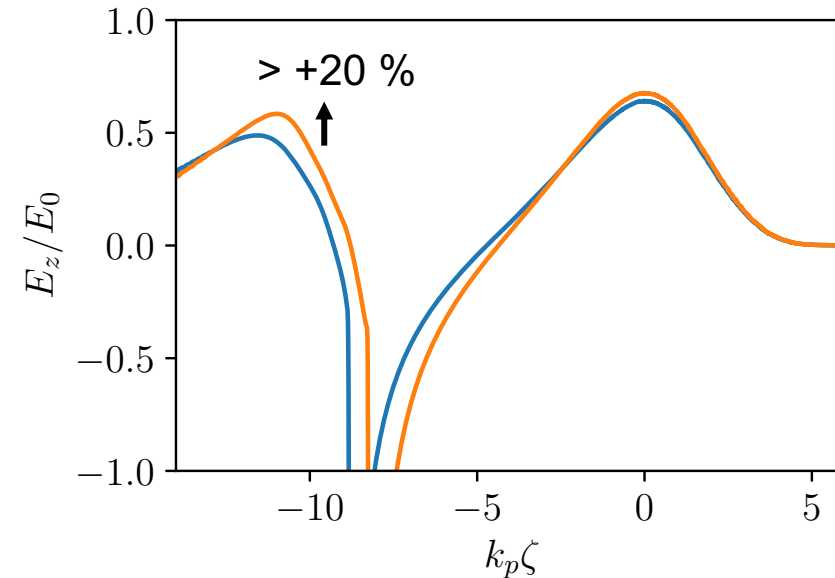
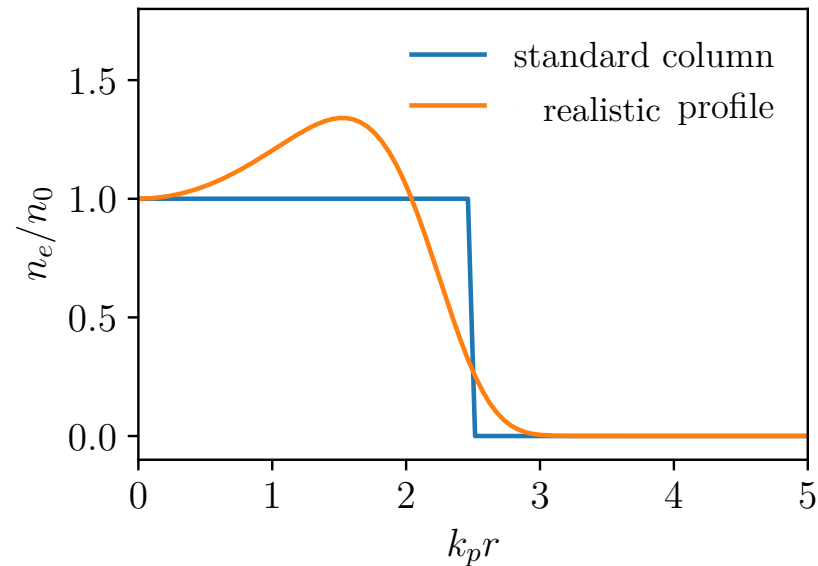
A plasma accelerator for a collider must fulfill:

- | | | | |
|--|--------------|----------|---|
| 1. High gradient (reduce the construction costs) | > GV/m | 15 GV/m | ✓ |
| 2. Low emittance (ability to focus the beam) | < 100s of nm | < 500 nm | ✓ |
| 3. Low energy spread (ability to focus the beam, narrow energy spectrum) | < 1% | < 1% | ✓ |
| 4. No intrinsic instability | | | ✓ |
| 5. High wall-plug efficiency (reduce run time costs) | > 5% | | |

Realistic plasma profiles increase the accelerating gradient



Realistic plasma profiles increase the accelerating gradient



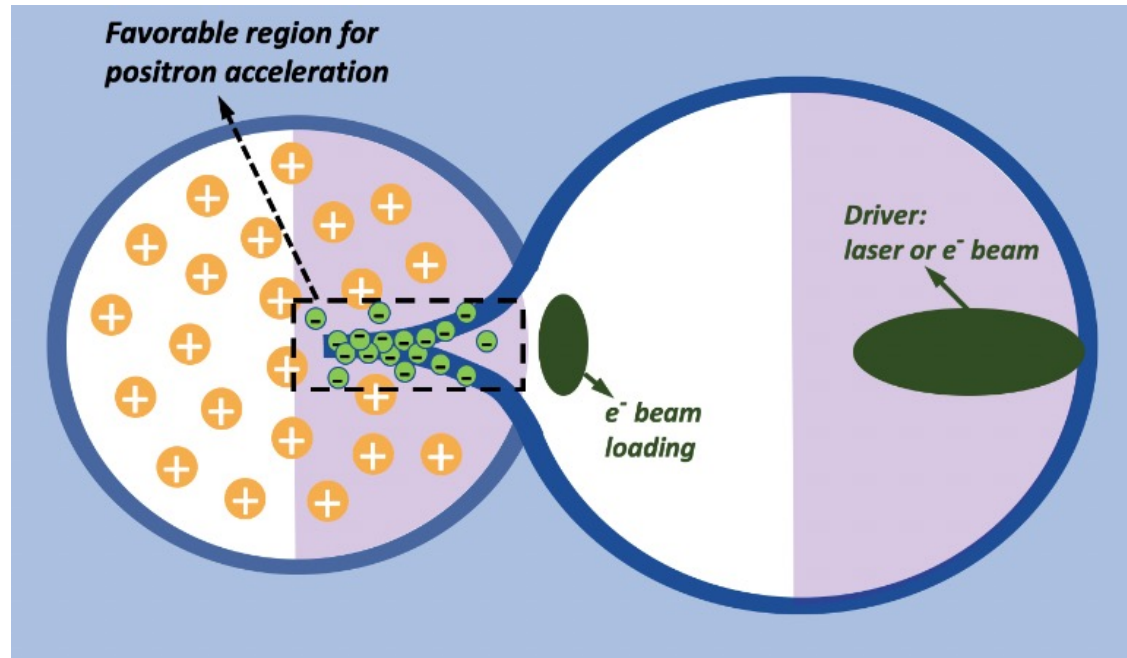
Efficiency can be further increased by tailoring drive beam profile
(Roussel PRL 2020, Loisch PRL 2018)

A lot of room for improvement of the efficiency

Other schemes to generate electron filaments

Statements on **stability**, **temperature effects**, and **tweaks for improvement** translate to other concepts using electron filaments

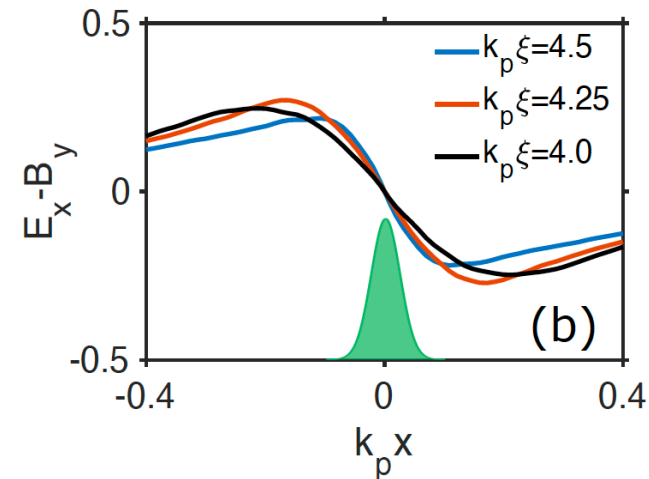
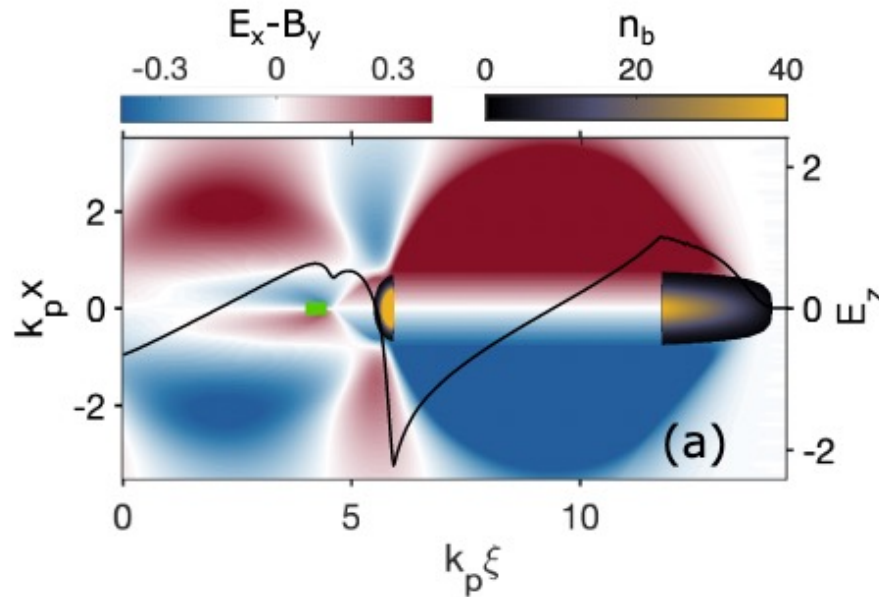
Electron witness bunch elongates plasma electron spike



Warm plasma (72 eV) spreads the electron filament

Wang et al. (arXiv. 2110.10290 2021)

Similar properties as in the plasma column can be achieved



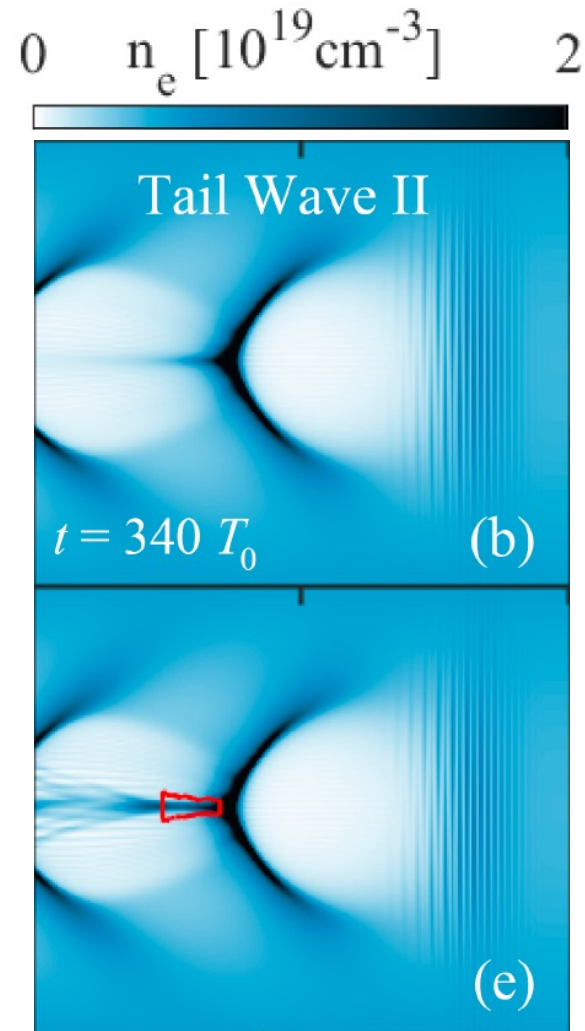
Linear focusing fields!
=> emittance preserved $< 0.9 \mu\text{m}$

1.4% rms energy spread
without beamloading

A lot of potential for optimization!

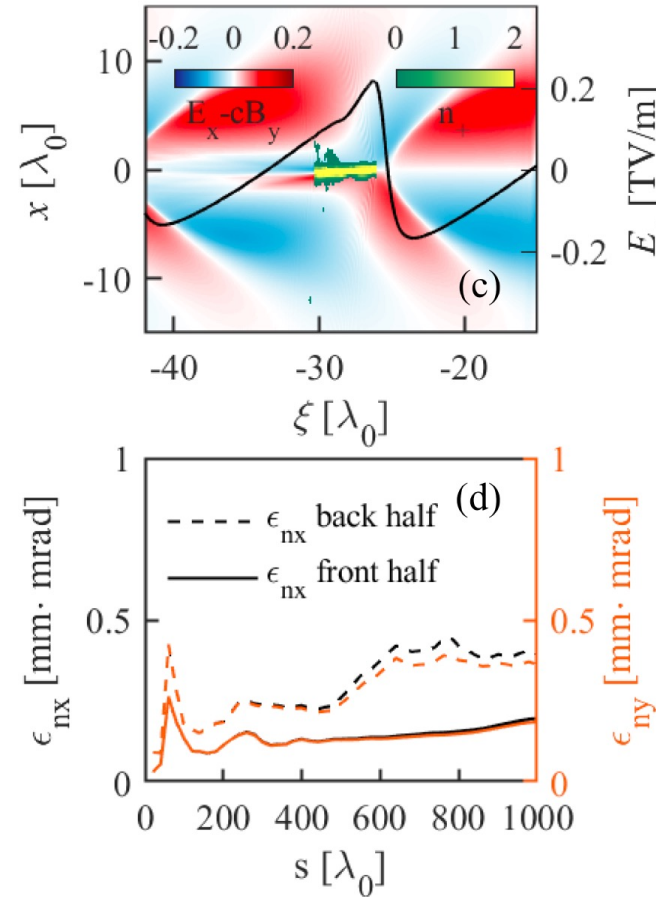
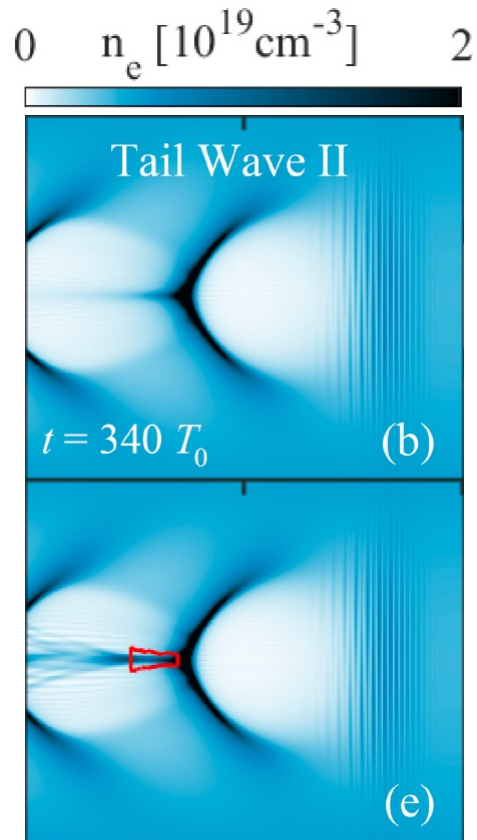
Wang et al. (arXiv. 2110.10290 2021)

Similar setting with laser driver demonstrated



Liu et al. (arXiv 2207.14749 2022)

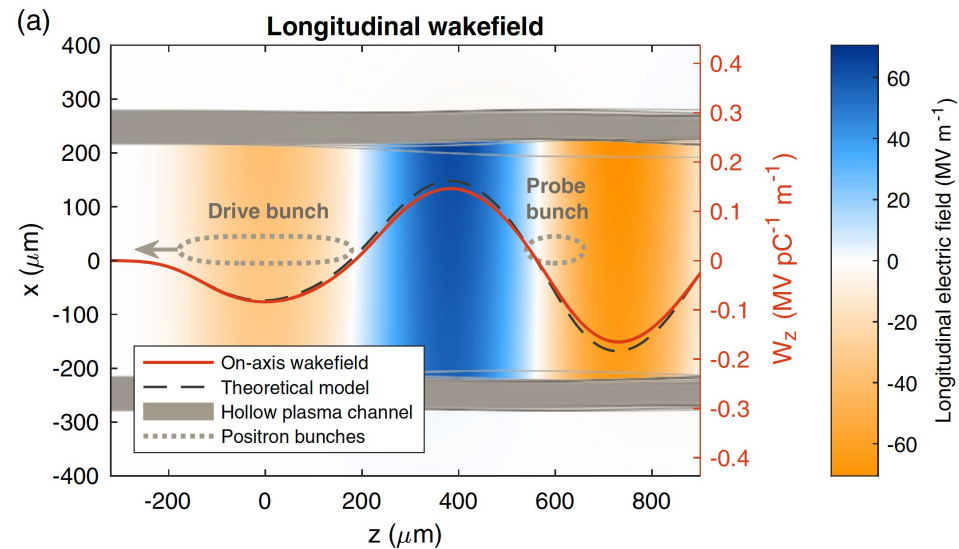
Similar setting with laser driver demonstrated



- Very simple setup
- High gradients: 100 GV/m fields
- A lot of potential for optimization

Liu et al. (arXiv 2207.14749 2022)

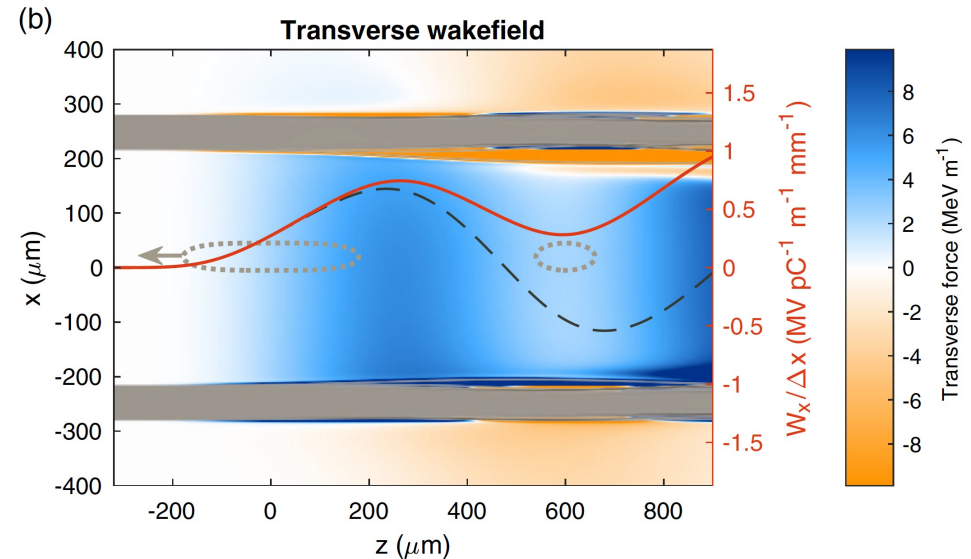
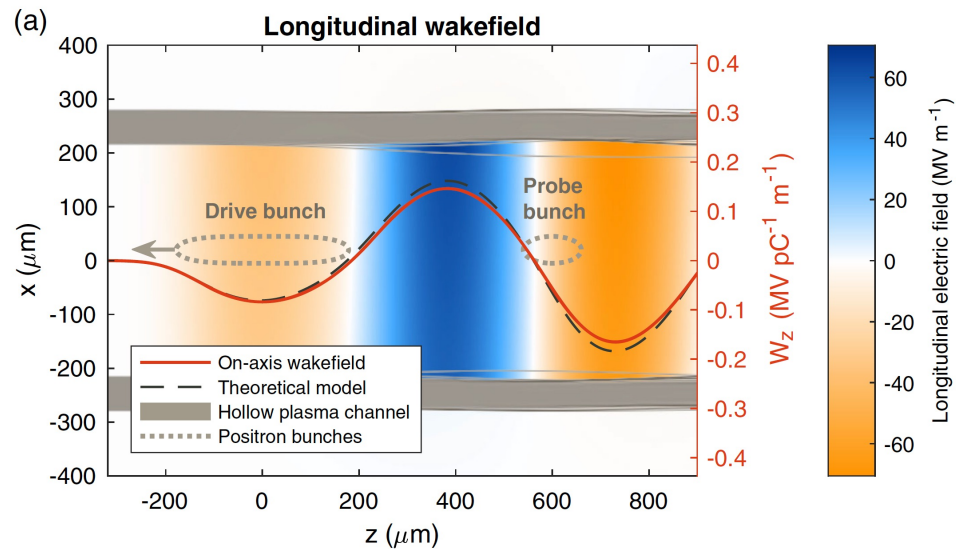
If ions defocus, let's ignore them altogether: Hollow core plasma accelerator



Hollow core plasma provides **accelerating, but no focusing fields**

Schroeder et al., PRL 82, 1177 (1999)
Lee et al., PRE 64, 045501 (2001)
Gessner et al., Nat. Comm. 7 11785 (2016)
Lindstrøm et al., PRL 120, 124802 (2018)

If ions defocus, let's ignore them altogether: Hollow core plasma accelerator



Hollow core plasma provides **accelerating, but no focusing fields**

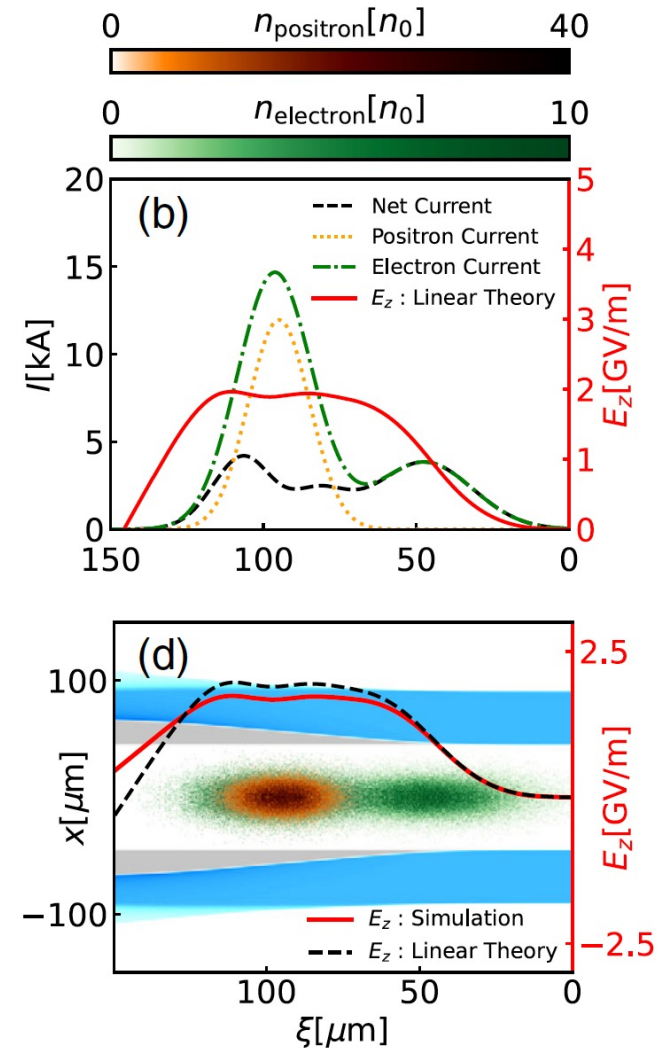
Misaligned beams are deflected

Schroeder et al., PRL 82, 1177 (1999)
Lee et al., PRE 64, 045501 (2001)
Gessner et al., Nat. Comm. 7 11785 (2016)
Lindstrøm et al., PRL 120, 124802 (2018)

Double loaded hollow core plasma channel yields extraordinary beam quality

- ~ nC charge
- ~ GV/m gradient
- ≲ 0.5% induced energy spread
- ~ 50% energy transfer efficiency

Zhou et al. (PRAB 25, 091303 2022)



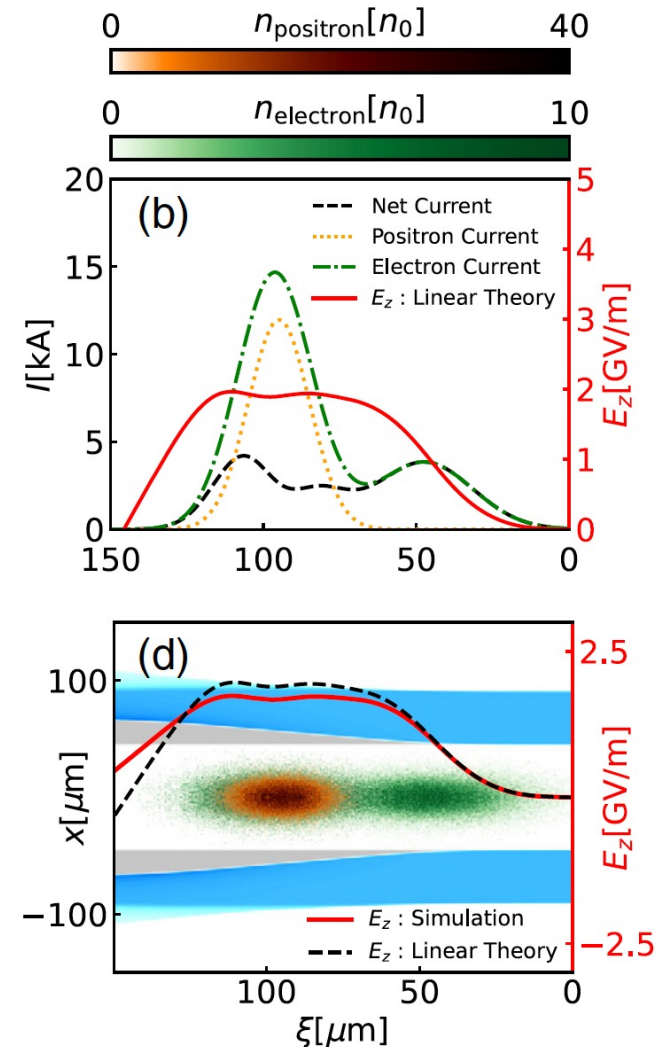
Double loaded hollow core plasma channel yields extraordinary beam quality

- ~ nC charge
- ~ GV/m gradient
- ≲ 0.5% induced energy spread
- ~ 50% energy transfer efficiency

Stability?

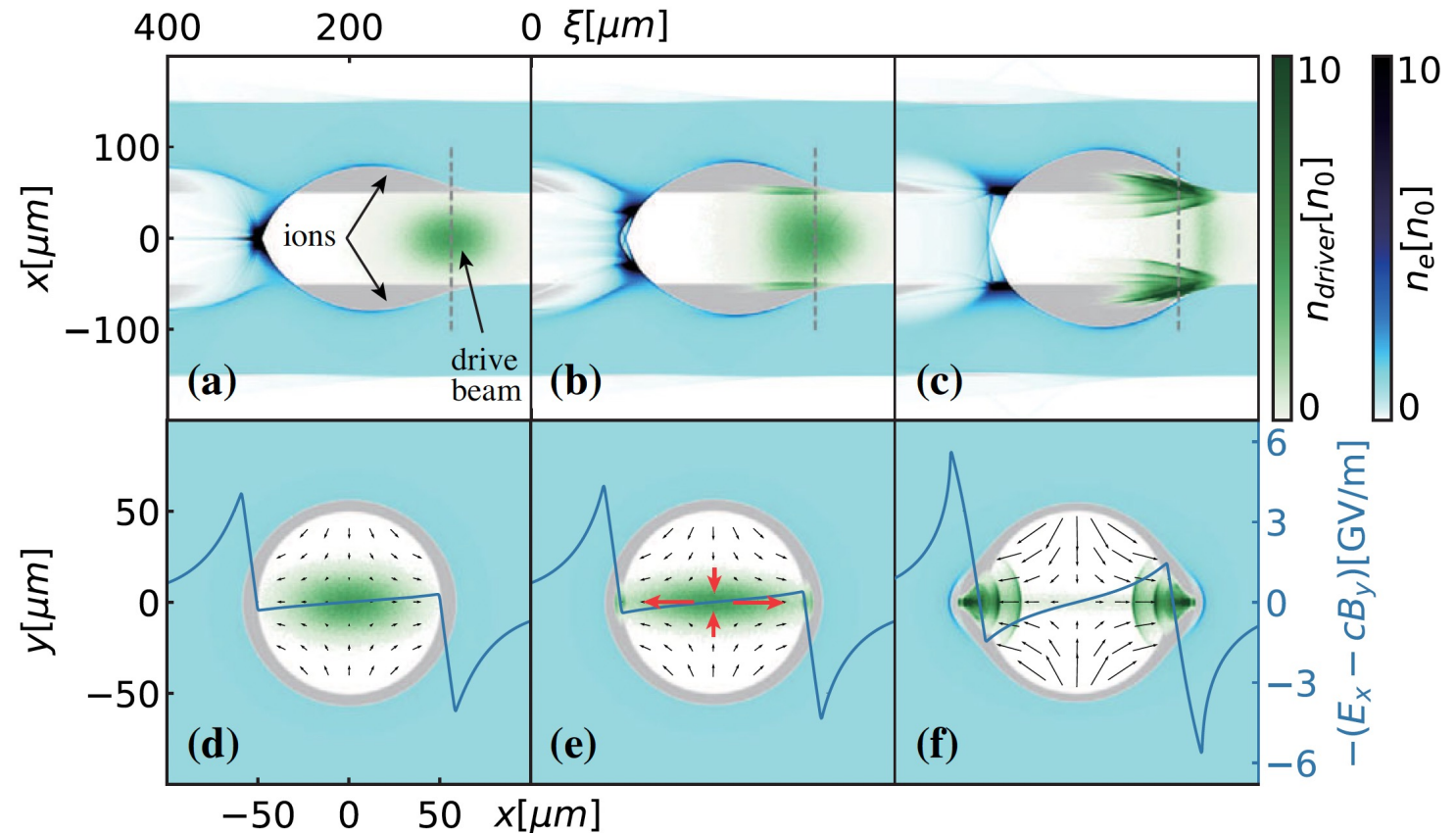
External focusing needs to be demonstrated

Zhou et al. (PRAB 25, 091303 2022)



Asymmetric drive beams stabilize hollow core plasma accelerator

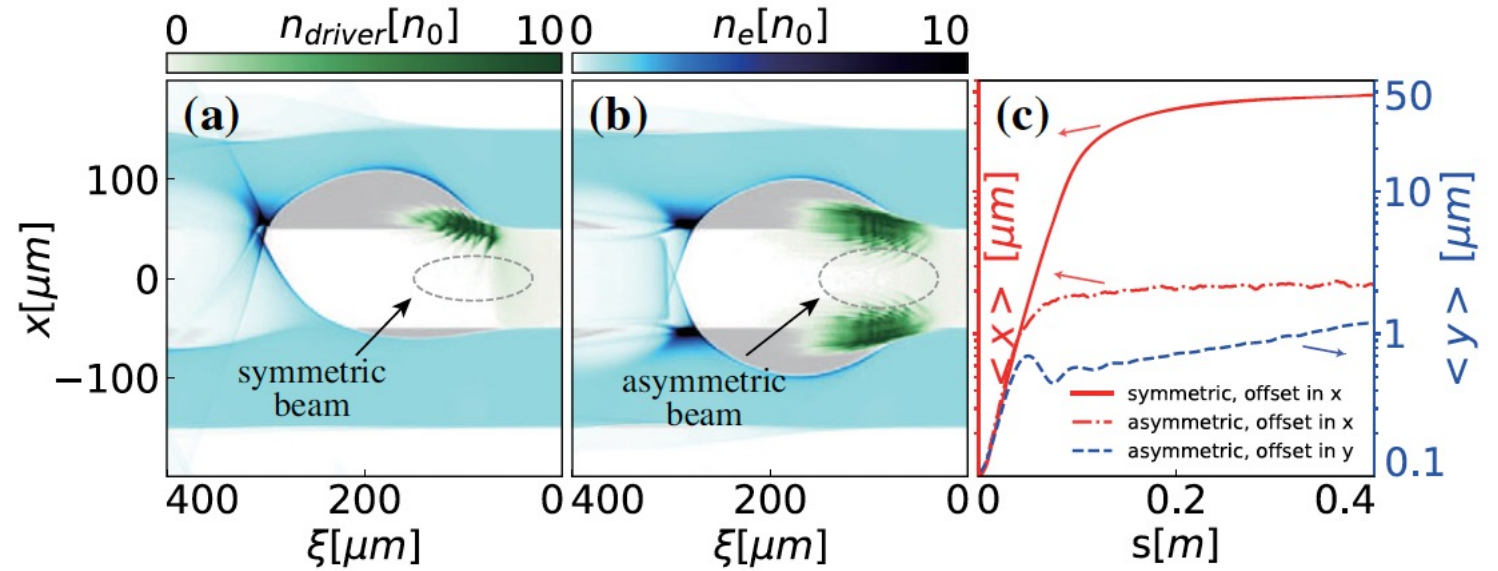
Quadrupole moment:
Drive beam hits channel wall
in a **controlled** manner



Zhou et al., PRL 127, 174801 (2021)

Asymmetric drive beams stabilize hollow core plasma accelerator

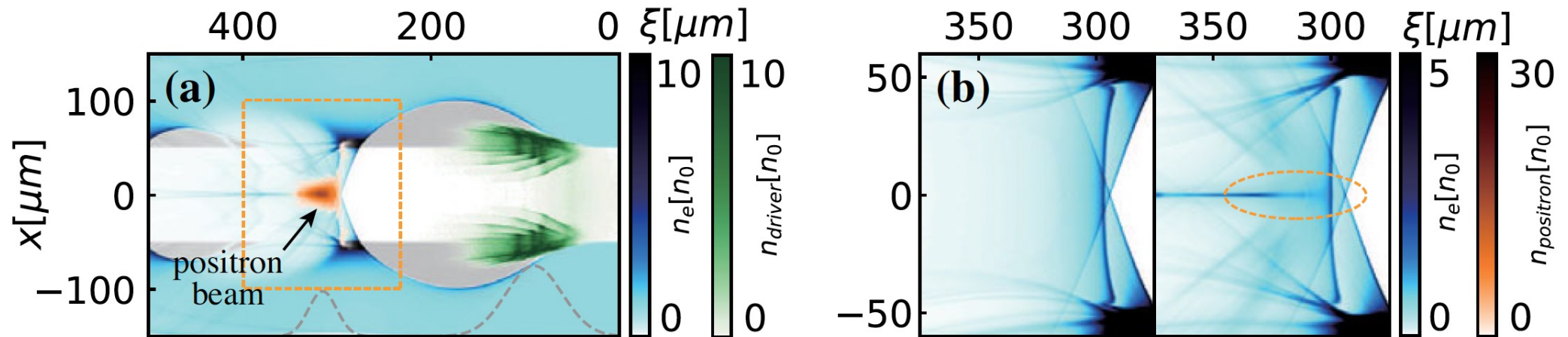
Quadrupole moment:
Drive beam hits channel wall
in a **controlled** manner



Stabilizes drive beam in hollow core channel!

Zhou et al., PRL 127, 174801 (2021)

Strong drive beams + positron beam loading produce electron filament in hollow core plasma accelerator



Electron filament **stabilizes witness**

Zhou et al., PRL 127, 174801 (2021)

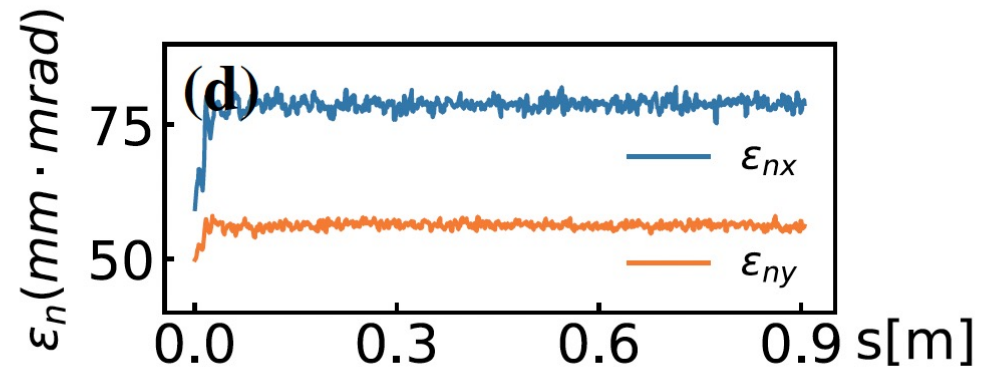
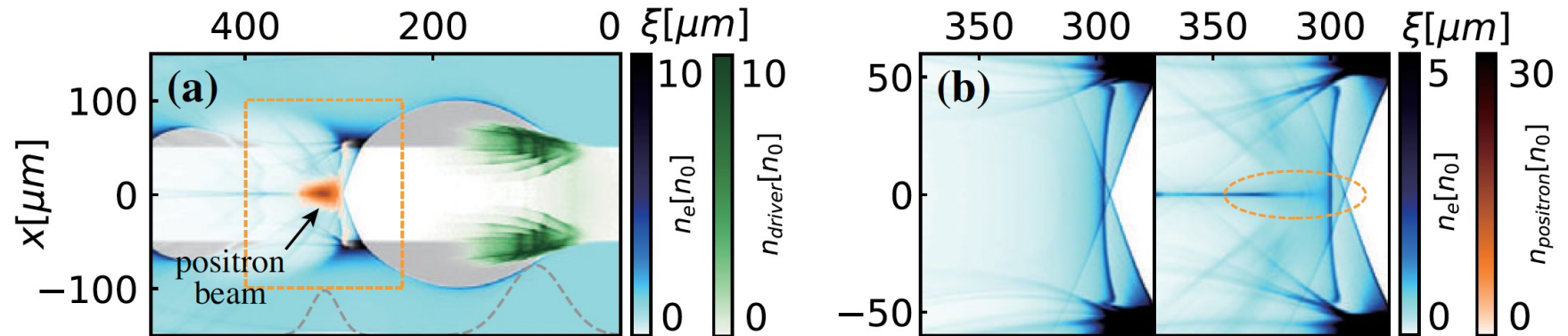
High-charge, low energy spread positron acceleration shown

0.49 nC charge
4.9 GV/m gradient
1.6% rms energy spread
33% energy transfer efficiency

> 50 μm central slice emittance

A lot of potential for optimization

Zhou et al., PRL 127, 174801 (2021)



High-charge, low energy spread positron acceleration shown

0.49 nC charge
4.9 GV/m gradient
1.6% rms energy spread
33% energy transfer efficiency

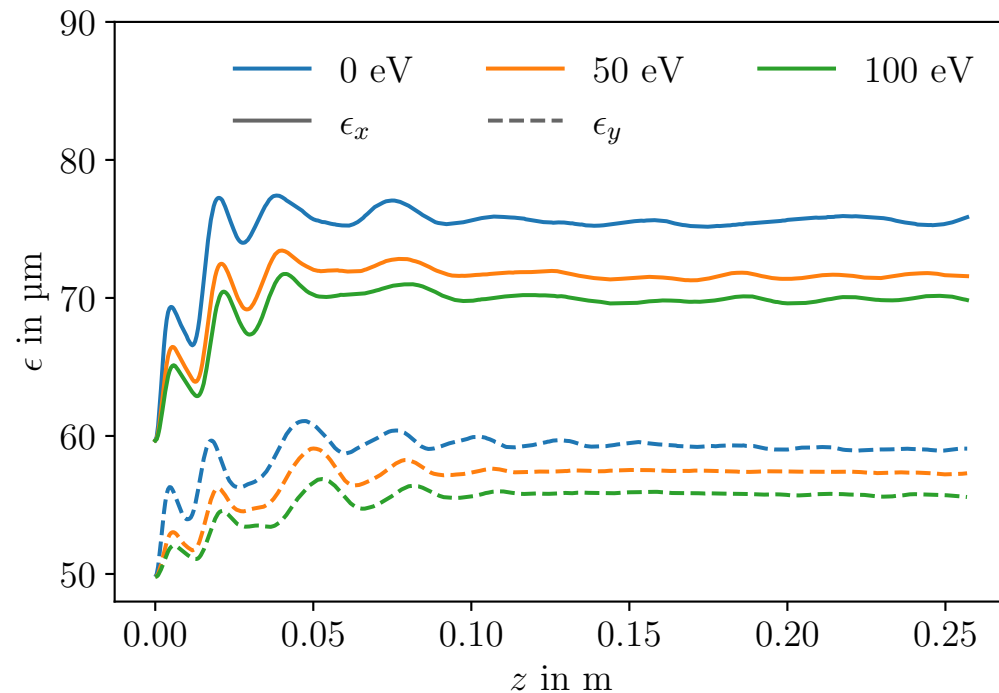
> 50 μm central slice emittance

A lot of potential for optimization

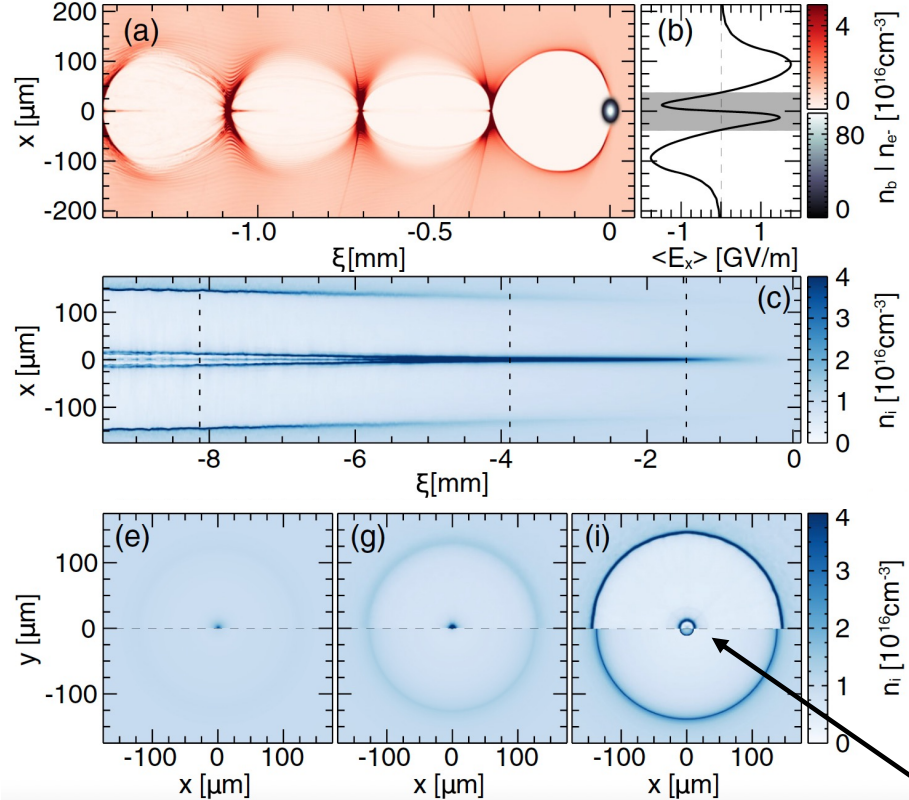
Zhou et al., PRL 127, 174801 (2021)

Diederichs et al. (in preparation)

Temperature mitigates emittance growth



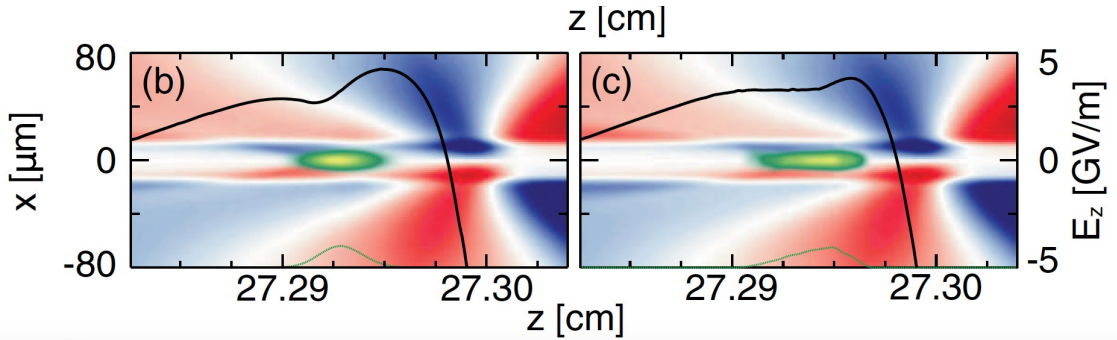
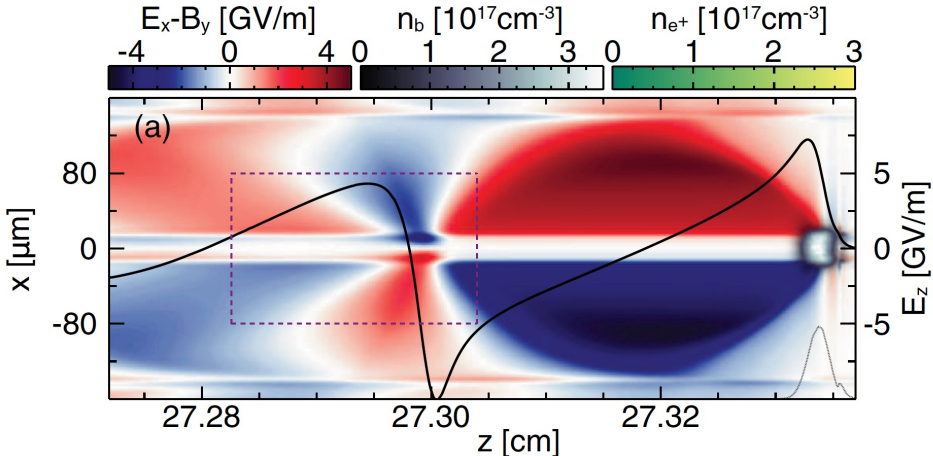
Blowout aftermath generates on-axis plasma filament



generates quasi-hollow plasma channel

Silva et al., PRL 127, 104801 (2021)

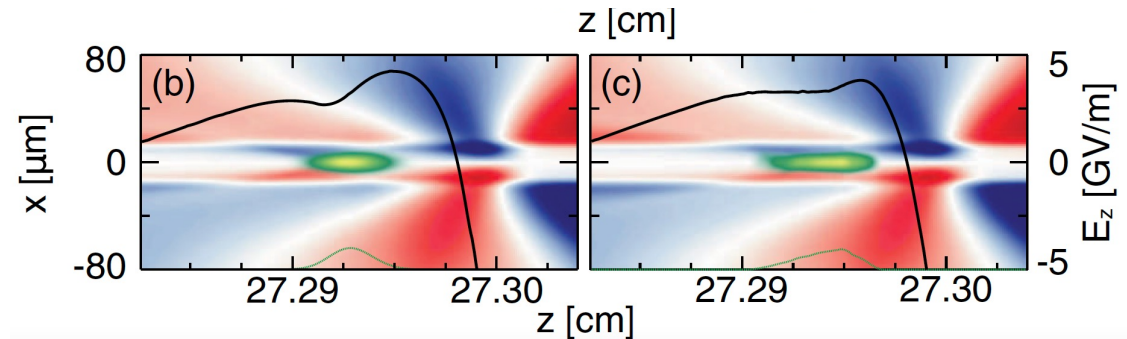
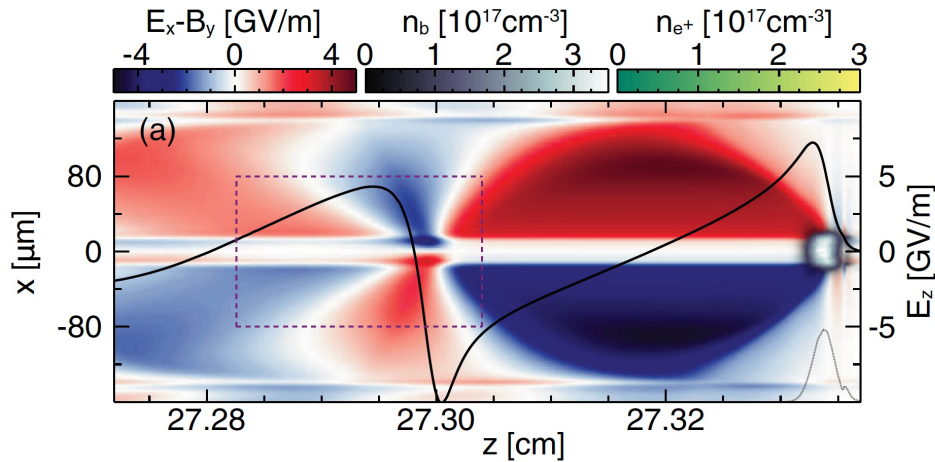
Blowout aftermath generates quasi-hollow plasma channel



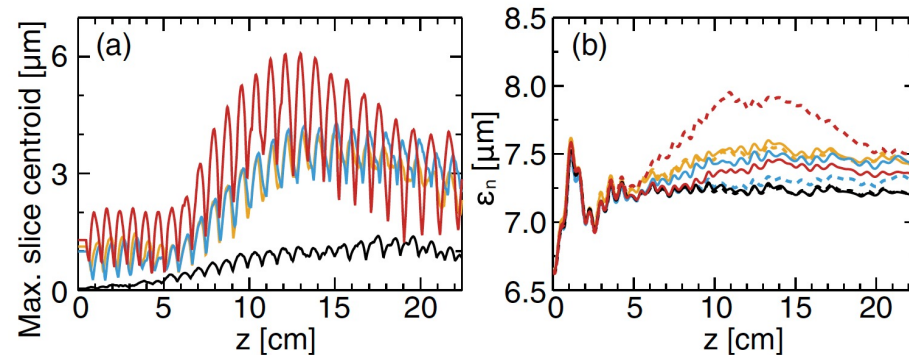
3.5 GV/m gradient
< 5% energy spread

Silva et al., PRL 127, 104801 (2021)

Blowout aftermath generates quasi-hollow plasma channel



3.5 GV/m gradient
< 5% energy spread
< $10\mu\text{m}$ emittance
Stability demonstrated



A lot of potential for optimization!

Silva et al., PRL 127, 104801 (2021)

There are more positron acceleration schemes...

Scheme	Highlights / Challenges	References
<ul style="list-style-type: none">• (Quasi)-Linear wakes	Simple setup, high-charge, high beam quality challenging	Hue PRR 2022, Blue PRL 2003
<ul style="list-style-type: none">• Long proton bunch	high, single-stage energy gain, emittance not yet studied	Lotov PPCF 2021
<ul style="list-style-type: none">• Short proton bunch in hollow channel	high, single-stage energy gain, short proton bunches not yet available	Yi PRSTAB 2013, Yi Sci Rep 2014
<ul style="list-style-type: none">• Ring-shaped drivers	Stability of driver challenging	Vieira PRL 2014, Jain PRL 2015 Hue PRR 2021
<ul style="list-style-type: none">• Double column structure	Ring-shaped witness beams, emittance preservation unclear	Reichwein PRE 2022

Promising advances for plasma-based positron acceleration

Many **new concepts** have been developed!

1. Using electron filaments:

- **Low-emittance, low-energy-spread positron acceleration** is possible
- Longitudinally varying focusing fields **provide stability** via BNS damping
- **Temperature effects** are required for numerical convergence and improve emittance preservation
- All schemes can be optimized for **higher efficiency**

2. Hollow core plasmas are promising, realistic design with external focusing has highest priority

We need to perform the simulation study to reach the deliverable for the ESPP!