

Prospects for testing
late-time cosmology with
weak lensing of GW and
galaxy surveys

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In collaboration with:
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GW luminosity distance in LCDM

- Cosmological distances inferred through measures of fluxes are known as [luminosity distances](#).

- For GW the luminosity distance is directly associated to the dampening of the wave amplitude: $h(t) \propto \frac{1}{d_L^{GW}}$

- When only the background expansion is considered
$$\bar{d}_L^{GW}(z) = c(1+z) \int_z^\infty \frac{dz'}{H(z')}$$

- However, as GW propagate in a inhomogeneous Universe the measured d_L picks up corrections and an angular dependence

$$d_L^{GW}(z, \hat{n}) = \bar{d}_L^{GW}(z) + \Delta d_L^{GW}(z, \hat{n})$$

Bertacca et al. (2018) found

$$\frac{\Delta d_L^{GW}}{\bar{d}_L^{GW}} = \underbrace{-\kappa}_{\text{lensing}} - \underbrace{(\phi + \psi)}_{V \text{ dilation}} + \underbrace{\frac{1}{\chi} \int_0^\chi d\tilde{\chi}(\phi + \psi)}_{\text{time delay}} + \underbrace{\frac{1}{\chi \mathcal{H}} \phi}_{SW} + \underbrace{v_{\parallel} \left(1 - \frac{1}{\chi \mathcal{H}}\right)}_{\text{Doppler}} - \underbrace{\left(1 - \frac{1}{\chi \mathcal{H}}\right) \int_0^\chi d\tilde{\chi}(\phi' + \psi')}_{ISW}$$

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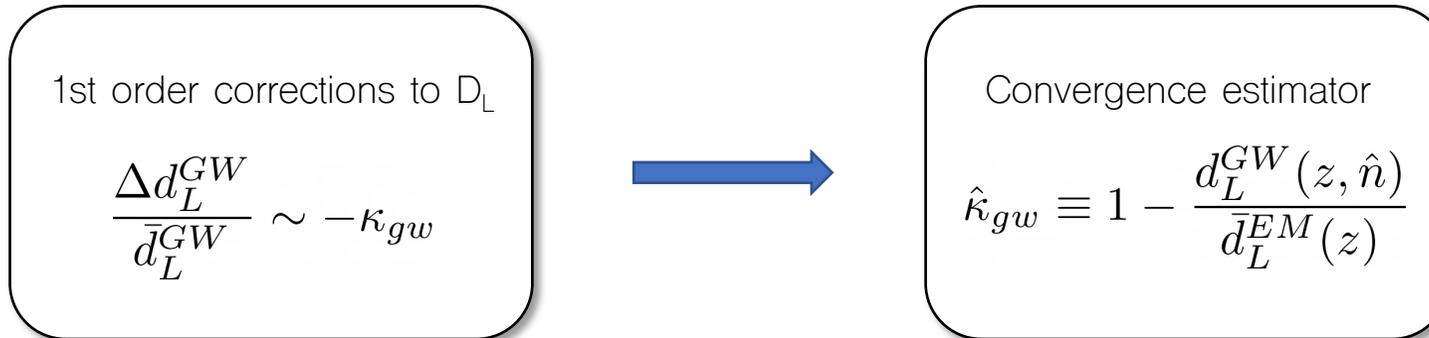
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Noise for measurements
of the BG expansion

Signal for measurements
of the perturbations

Tomographic observables



Ours observables then become the cross-correlations of density contrast field, galaxies weak lensing and GW weak lensing

$$C_{i,j}^{XY}(\ell) = \int_0^{z_{\max}} \frac{dz}{\chi^2(z)H(z)} W_X^i(k, z) W_Y^j(k, z) P_p(k)$$

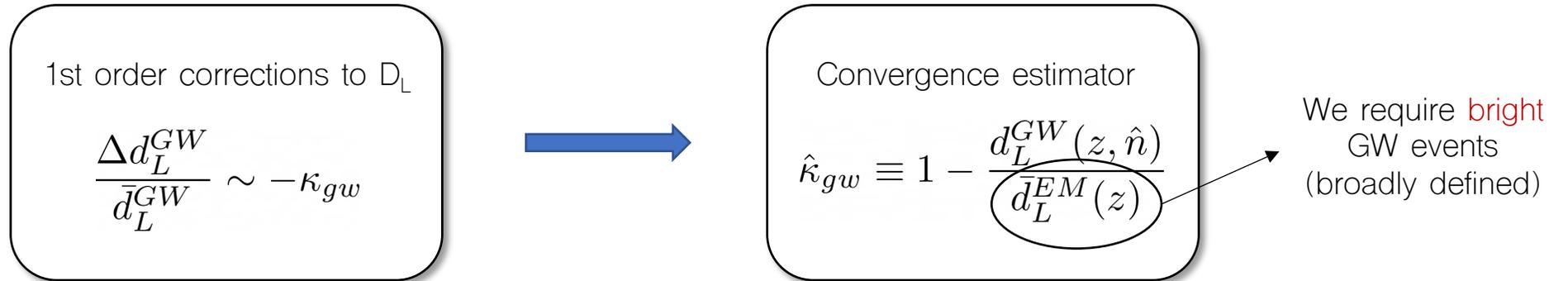
Galaxy-only observables

$$C_l^{\delta\delta}, C_l^{\kappa_g\kappa_g}, C_l^{\delta\kappa_g}$$

GW observables

$$C_l^{\kappa_{gw}\kappa_{gw}}, C_l^{\kappa_{gw}\delta}, C_l^{\kappa_{gw}\kappa_g}$$

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Effective Field Theory of Modified Gravity

- Unifying language that encompasses several DE models
- Separate background evolution from linear perturbations
- Write an action with all operators giving *at most* second order equations of motion and
- Reflecting the symmetries of the FLRW metric \rightarrow operators coefficients (EFT functions) are functions of time

We further restrict to Horndeski with $c_T^2 = 1$

With this set-up, to parametrize any model in a general way one only needs to choose

The background expansion history

✓ $w_{\text{DE}} = w_0 + w_a(1 - a)$

$$\rightarrow \begin{cases} \rho_{\text{DE}} = \rho_{\text{DE}}^0 a^{-3(1+w_0+w_a)} e^{-3w_a(1-a)} \\ \mathcal{H}^2 = \frac{8\pi G}{3} (\rho_m + \rho_\nu + \rho_{\text{DE}}) \end{cases}$$

3 EFT functions

$\Omega(a) \rightarrow$ non-minimal coupling

$\gamma_1(a) \rightarrow$ kineticity

$\gamma_2(a) \rightarrow$ braiding

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The non minimal coupling term introduces dissipation, so that the inferred background GW luminosity distance becomes

$$\bar{d}_L^{GW} = \sqrt{1 + \Omega(z)} \bar{d}_L^{EM}$$

In Horndeski theories, weak lensing is still the dominant correction to d_L and is not *explicitly* modified

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The GW convergence estimator then becomes

$$\hat{\kappa}_{GW} \equiv 1 - \frac{d_L^{GW}(z, \hat{n})}{\bar{d}_L^{EM}(z)} = 1 - \sqrt{1 + \Omega(z)}(1 - \kappa_{GW})$$

$$C_\ell^{X_i Y_j} = \int_0^{z_{\max}} \frac{dz}{\chi^2(z) H(z)} [\Theta_X(z) \Theta_Y(z)] W_{X,i}(k, z) W_{Y,i}(k, z) P_p(k), \quad \Theta_X(z) = \begin{cases} 1, & X = [\delta, \kappa_g] \\ \sqrt{1 + \Omega(z)}, & X = \kappa_{\text{gw}} \end{cases}$$

To obtain forecasts on cosmological parameters, we performed a Fisher matrix analysis

$$\mathcal{F}_{\alpha\beta} = \sum_{\ell=l_{\min}}^{\ell_{\max}} \frac{2\ell+1}{2} \sum_{i,j,m,n} \sum_{A,B,C,D} \frac{\partial C_{ij}^{AB}(\ell)}{\partial \theta_{\alpha}} [K^{-1}(\ell)]_{jm}^{BC} \frac{\partial C_{mn}^{CD}}{\partial \theta_{\beta}} [K^{-1}(\ell)]_{ni}^{DA}$$

We used **EFTCAMB** (Hu et al., 2014) for power spectra generation and **CosmicFish** (Raveri et al., 2016) for the Fisher matrix calculation

We considered different observational scenarios, varying:

- The number of measured bright GW sources
- The accuracy on the luminosity distance measurement
- The error on the counterpart redshift – either a spectroscopic or a photometric measurement

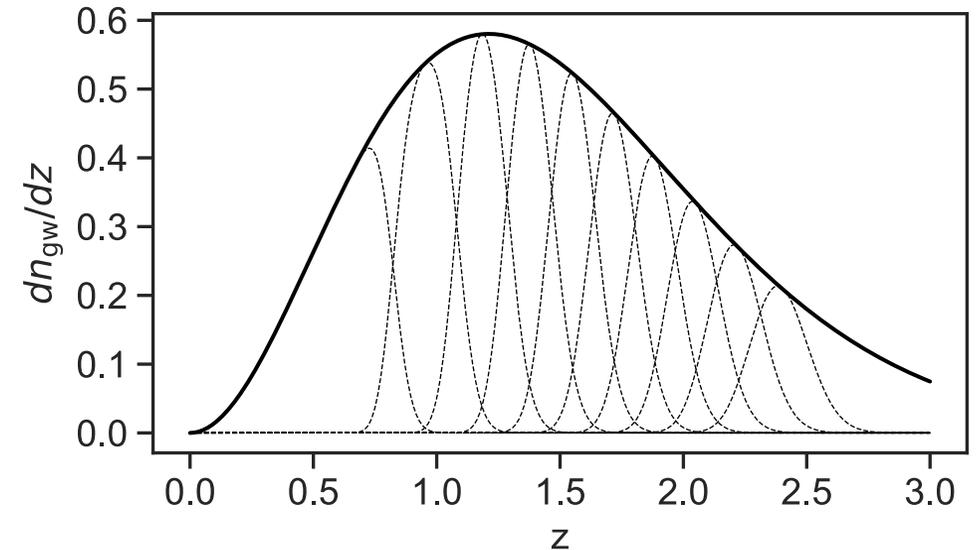


Figure: normalized GW sources distribution

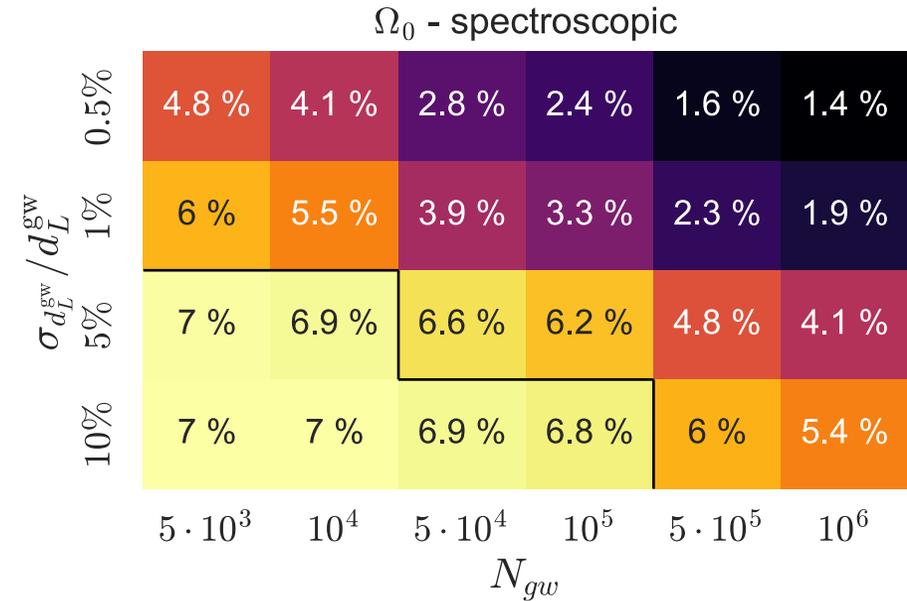
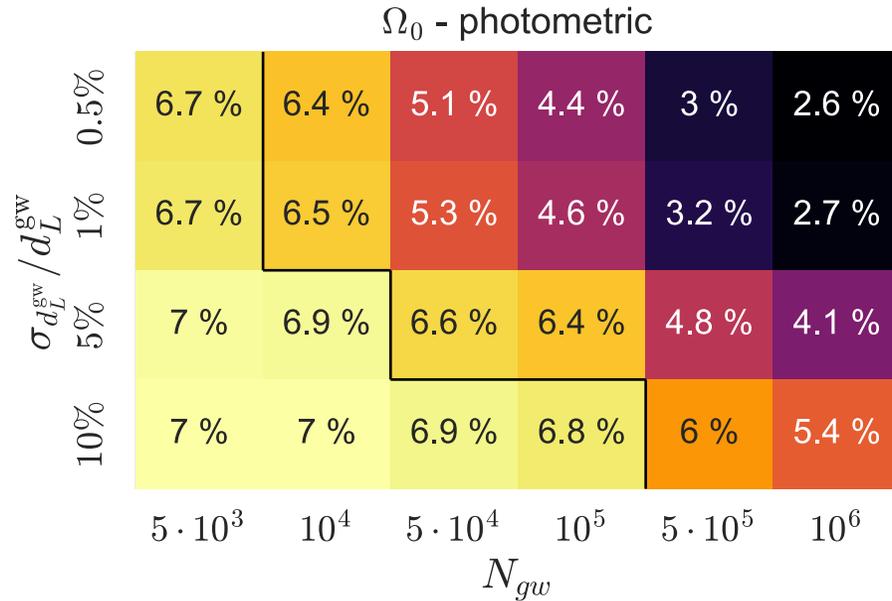
Each time, we varied all parameters! Noise, LCDM parameters and MG parameters

Results - EFT of MG

Model M1:

The background is not fixed, with

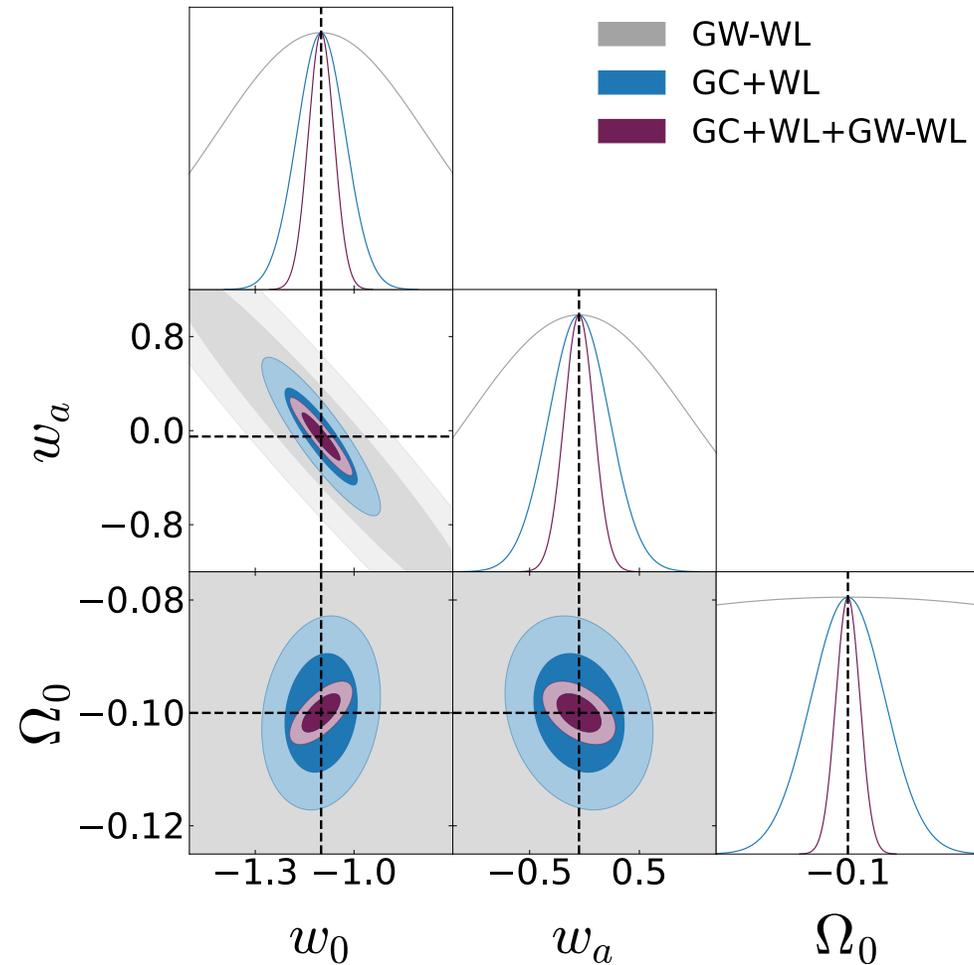
$$\rho_{DE} = \rho_{DE}^0 a^{-3(1+w_0+w_a)} e^{-3w_a(1-a)}, \quad \Omega(a) = \Omega_0 \frac{\rho_{DE}}{\rho_{DE}^0}, \quad \gamma_1(a) = 0, \quad \gamma_2(a) = 0$$



Balardo et al. (2022) [arXiv:2210.06398]

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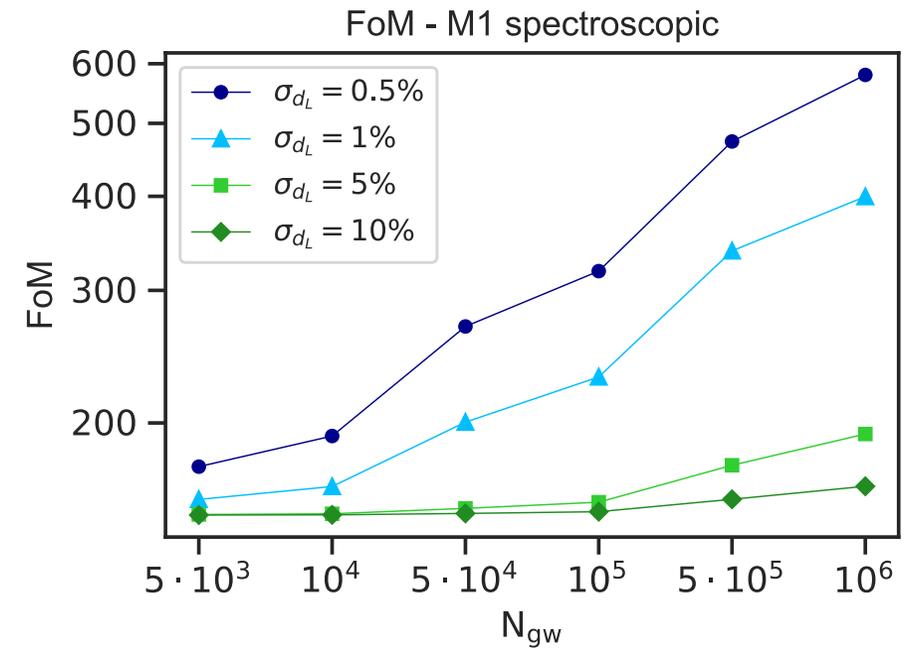
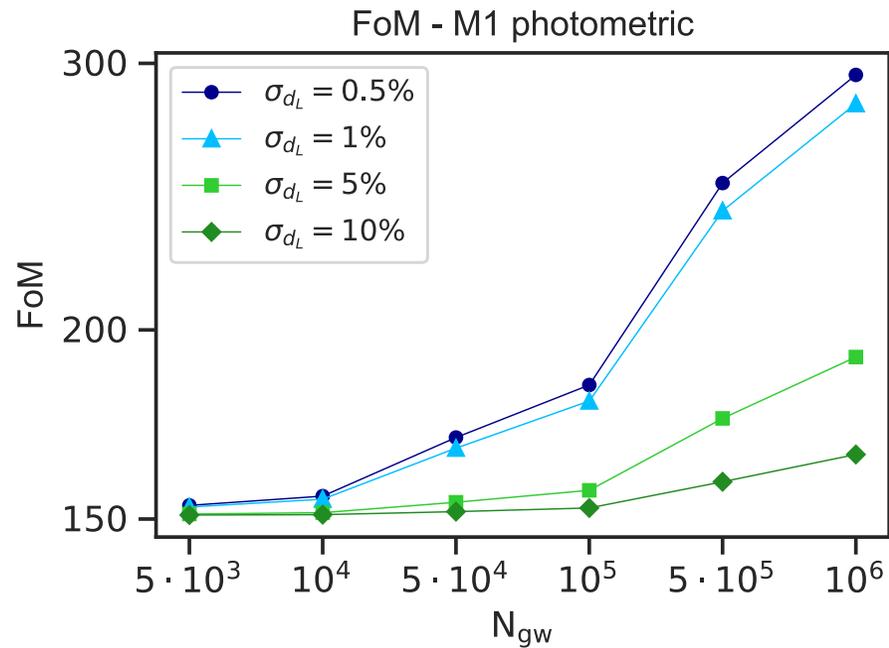


Marginalized forecasts on MG parameters, for a futuristic scenario in which 10^5 sources are detected with a spectroscopic redshift

Results - EFT of MG

We defined a Figure of Merit $\text{FoM} = \det(\mathcal{F}_{\alpha,\beta})^{\frac{1}{2N}}$ with N = number of free parameters

This FoM is inversely proportional to the N -th root of the 1σ volume in the parameter space



Balardo et al. (2022) [arXiv:22.10.06398]

Conclusions

- Single near future experiments might have too poor source statistics for GW weak lensing to provide crucial information
- We showed however that it is possible to define a convergence estimator containing crucial information over MG parameters
- Weak lensing could become a valuable source for GW experiments in the long run, especially to probe the growth parameters, that cannot be constrained through sirens
- In this optics, the main thing to improve on is the accuracy on luminosity distance and sky-location determination, to facilitate host identification

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Thank you!

And thanks to Alice Garoffolo, Matteo Martinelli, Suvodip Mukherjee and Alessandra Silvestri

