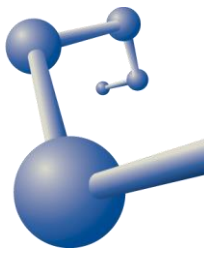




Instituto de
Ciencias
Nucleares
UNAM



“Hedgehog” events revisited

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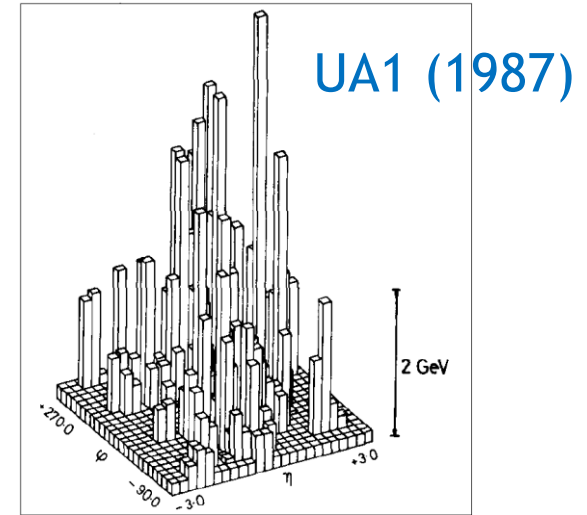
Winter Workshop on Nuclear Dynamics 2023, Puerto Vallarta

Introduction to “hedgehog” events

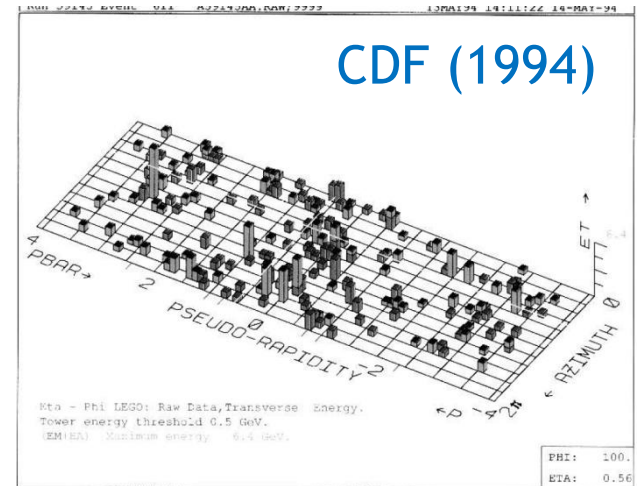
- The UA1 and CDF collaborations have reported the presence of events with a very extended structure of low momentum tracks filling in a uniform way the pseudorapidity-azimuth (η - ϕ) phase space.
- First dedicated analysis of highest E_T events seen in the UA1 detector at $\sqrt{s} = 630$ GeV (with isotropic events with $E_T \sim 210$ GeV) - no evidence for non-QCD mechanism for these events.
- Unusual events observed in ppbar collisions at $\sqrt{s} = 1.8$ TeV by CDF's Run 1 detector with more than 60 charged particles and ~ 320 GeV of transverse energy (E_T) - called “**hedgehog**” events by C. Quigg.



- Taken for granted that in these events with high E_T perturbative aspects of QCD dominate the event properties: multi-jet events.



[UA1 Collaboration, Zeit. für Phys. C, V. 36, p. 33 \(1987\)](#)



[C. Quigg, Il Nuovo Cimento, V. 33C, N. 5 p. 327 \(2010\)](#)

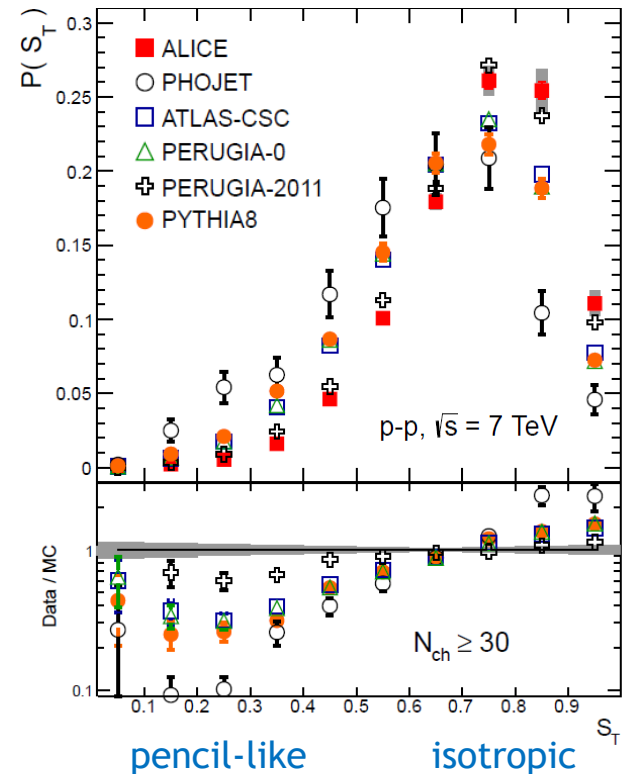
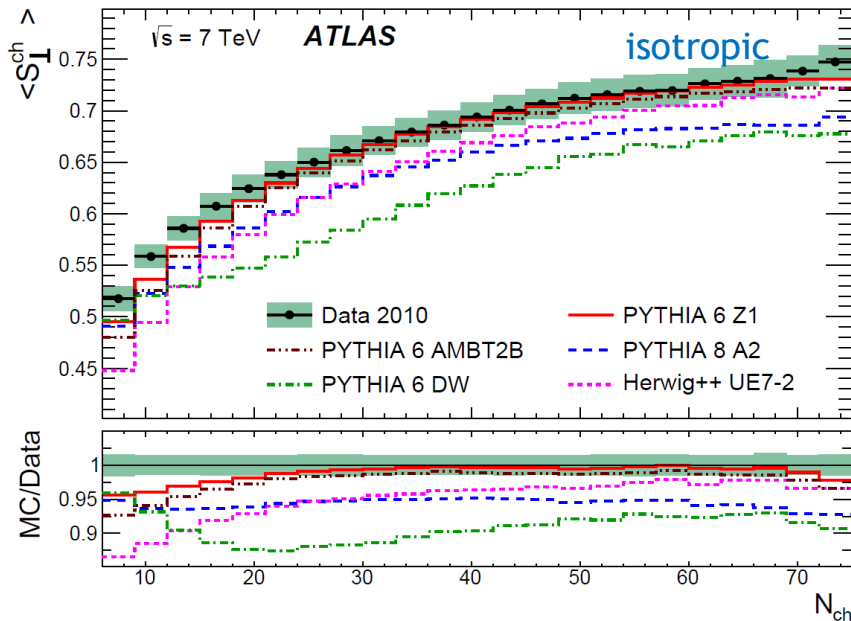
Characterisation of high-multiplicity events

- Attempts to characterise these high-multiplicity events: use of event shapes, i.e. using transverse sphericity:

$$S_{\perp} = \frac{2\lambda_2^{xy}}{\lambda_1^{xy} + \lambda_2^{xy}}, \quad S^{xy} = \sum_i \frac{1}{|\vec{p}_{T,i}|^2} \begin{bmatrix} p_{x,i}^2 & p_{x,i} p_{y,i} \\ p_{x,i} p_{y,i} & p_{y,i}^2 \end{bmatrix}$$

- Both ALICE and ATLAS observed an **under-estimation** of isotropic events by MC generators at high charged multiplicity ($N_{ch} \geq 30$)
 - ✓ Suggest that a very active underlying event (UE) is needed by the MC event generators in order to explain these high-multiplicity events

ATLAS Collaboration, Phys. Rev. D 88, 032004 (2013)

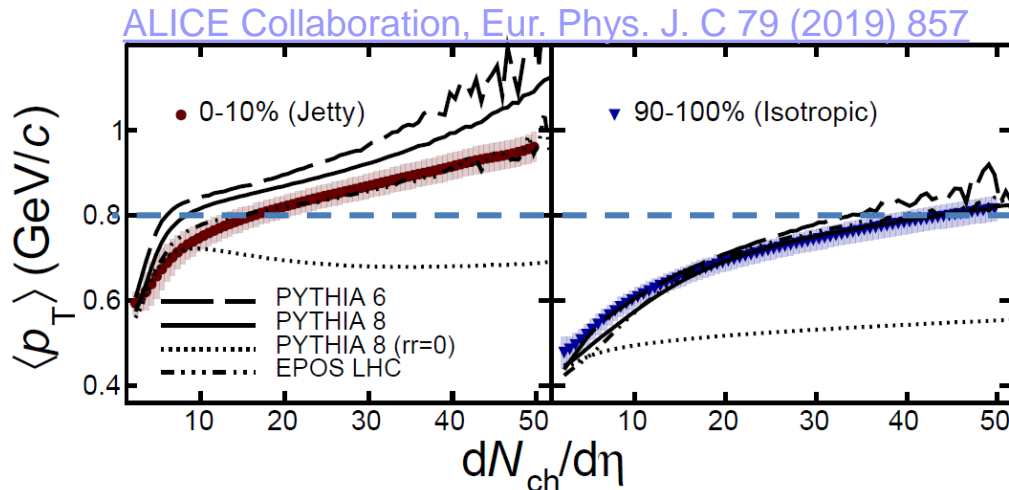


ALICE Collaboration, Eur. Phys. J. C 72 (2012) 2124

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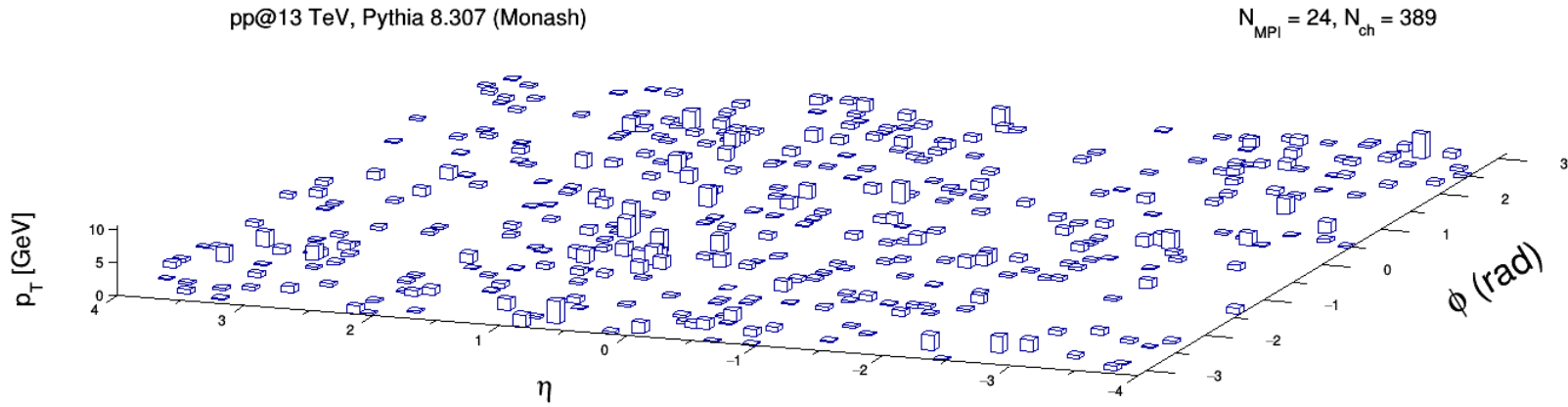


- Attempts to characterise these high-multiplicity events: use of event shapes, i.e. using transverse sphericity:

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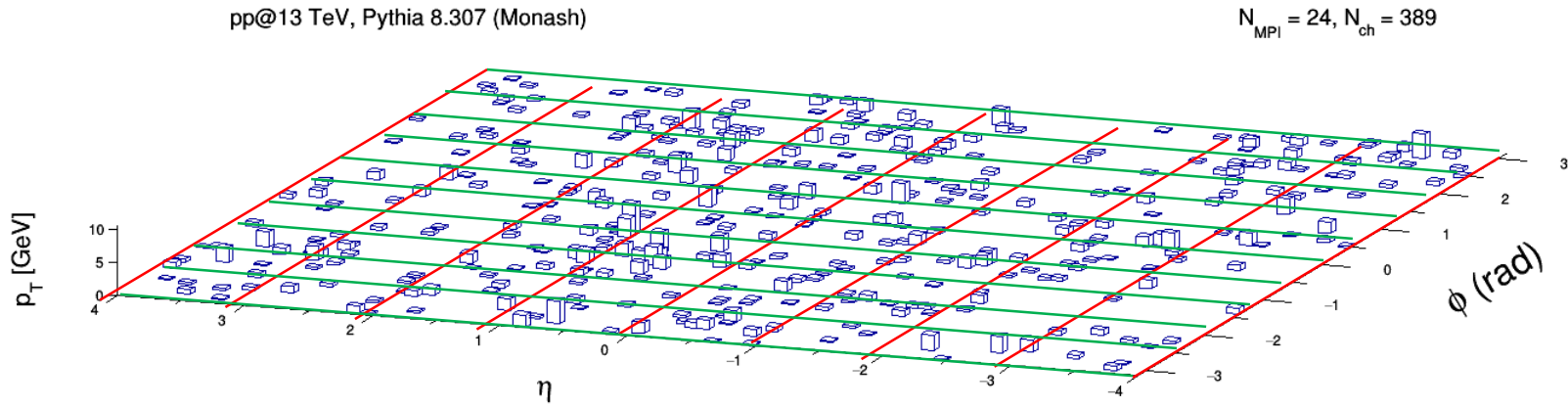
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- Recently, a new event shape parameter, **flattenicity**, was proposed [[A. Ortiz, G. Paic, Rev. Mex. Fis. Suppl. 3 \(2022\) 4, 040911](#)] that allows one to identify and characterise high-multiplicity events with a quasi-isotropic distribution in a wide pseudorapidity range in proton-proton collisions.
- MC event generators are able to model “hedgehog” events, which opens the possibility to study their properties and find a potential way to experimentally trigger these events.

- The idea: find out how uniform the p_T of tracks is distributed in a given event!



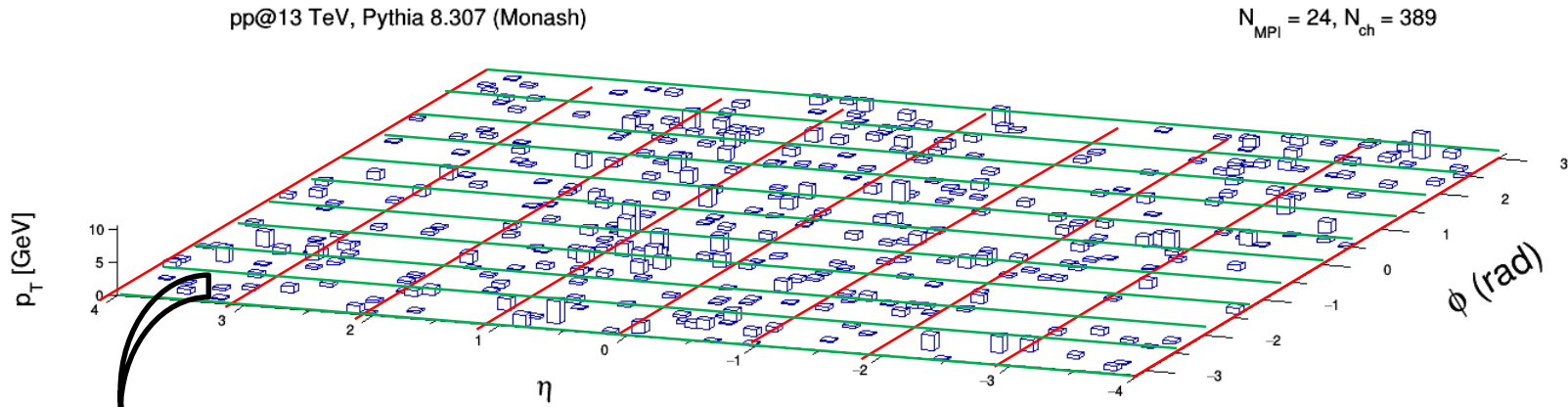
Calculating flattenicity

- Build **8** x **10** grid in (η - ϕ) space:

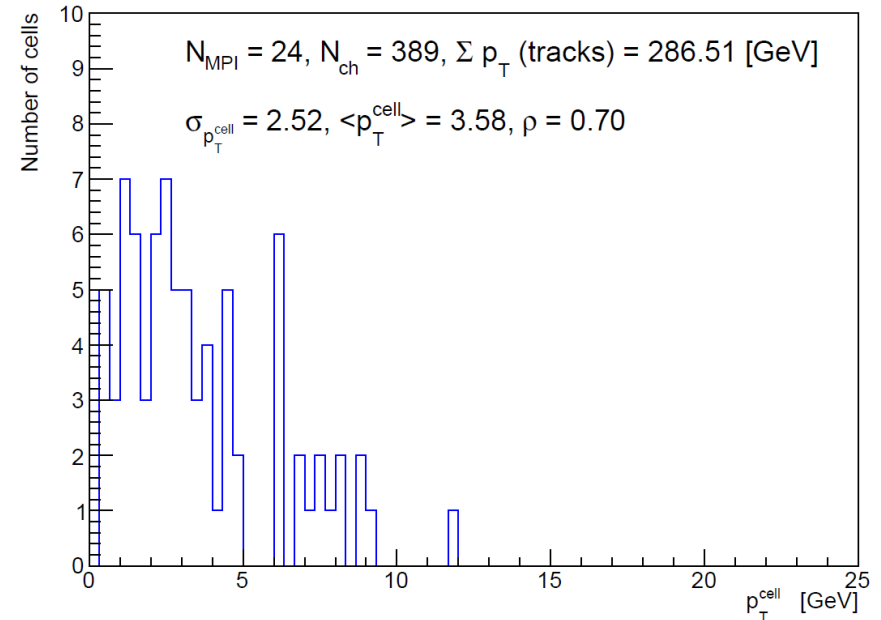


Calculating flattenicity

- Build 8 x 10 grid in (η - ϕ) space:

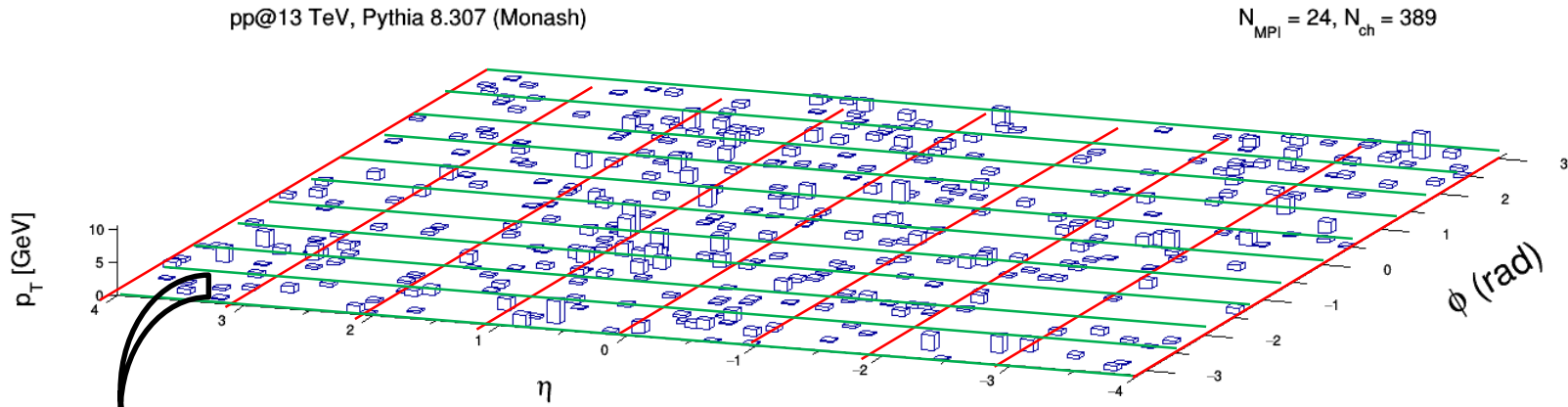


In each cell, the average transverse momentum is calculated: $p_{\text{T}}^{\text{cell}}$



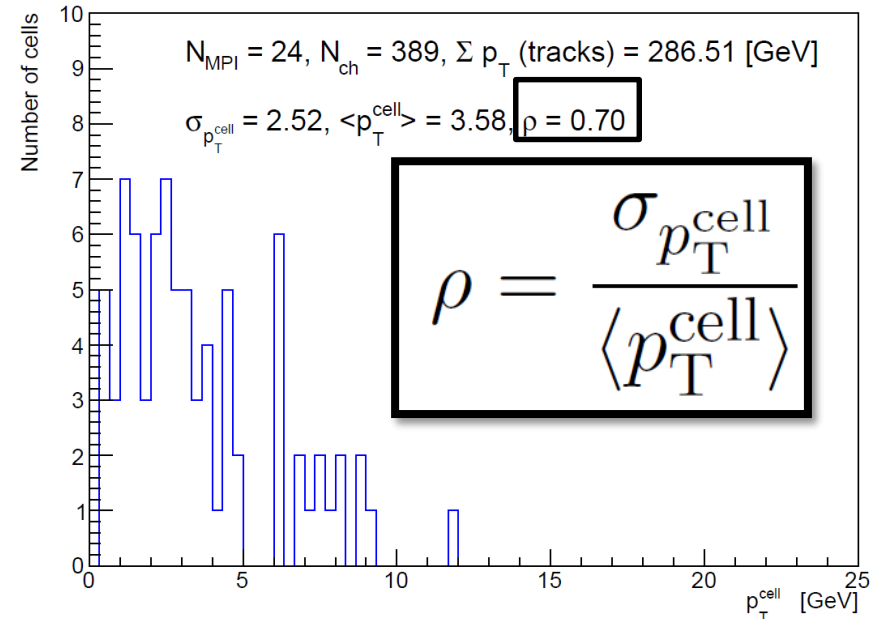
Calculating flattenicity

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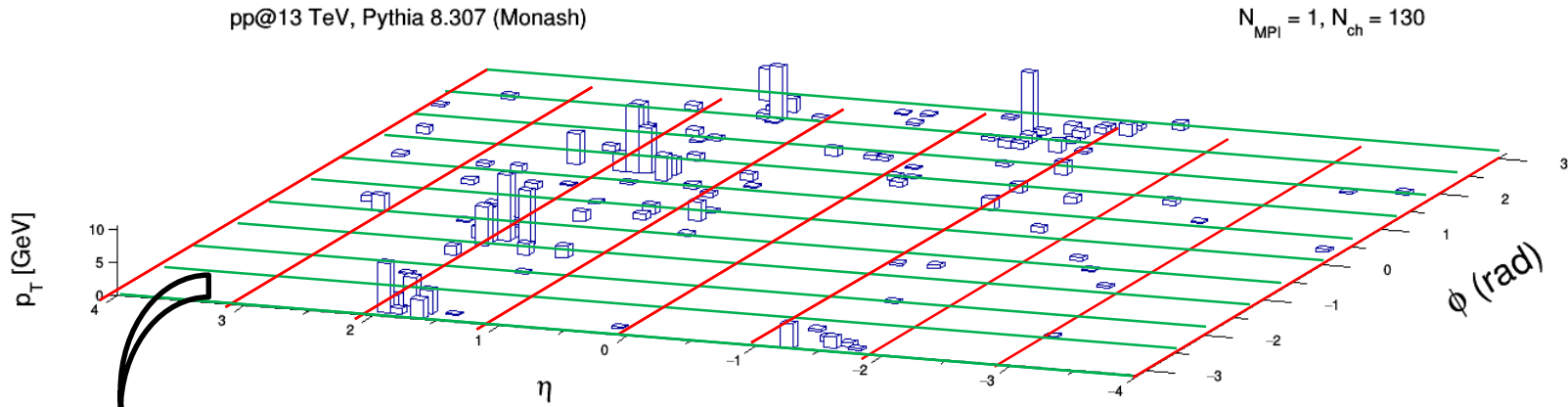


In each cell, the average transverse momentum is calculated: p_T^{cell}

- Event-by-event, the relative standard deviation of the p_T^{cell} distribution is obtained - flattenicity.
- Events with isotropic distribution of particles (“hedgehogs”) are expected to have a small value of flattenicity ($\rho < 1$).

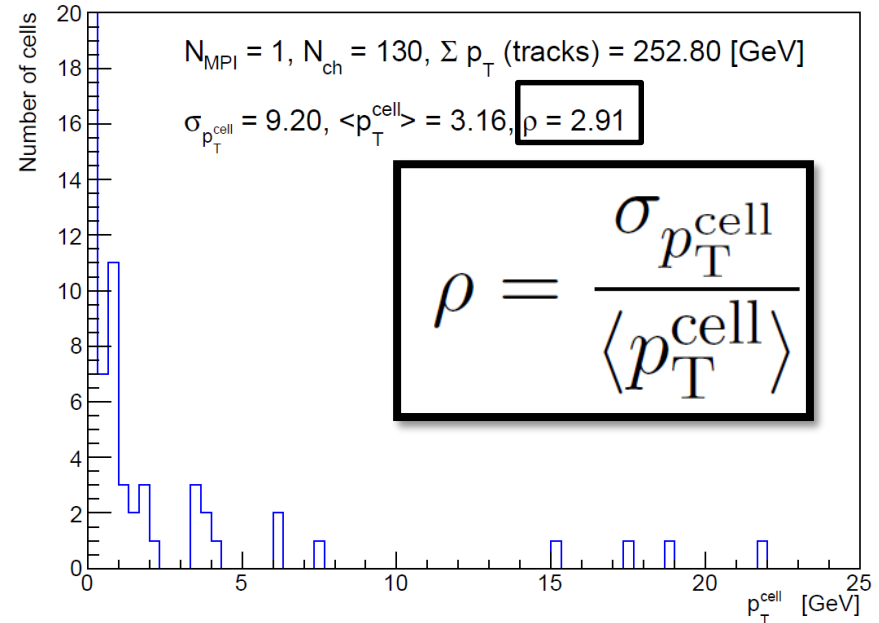


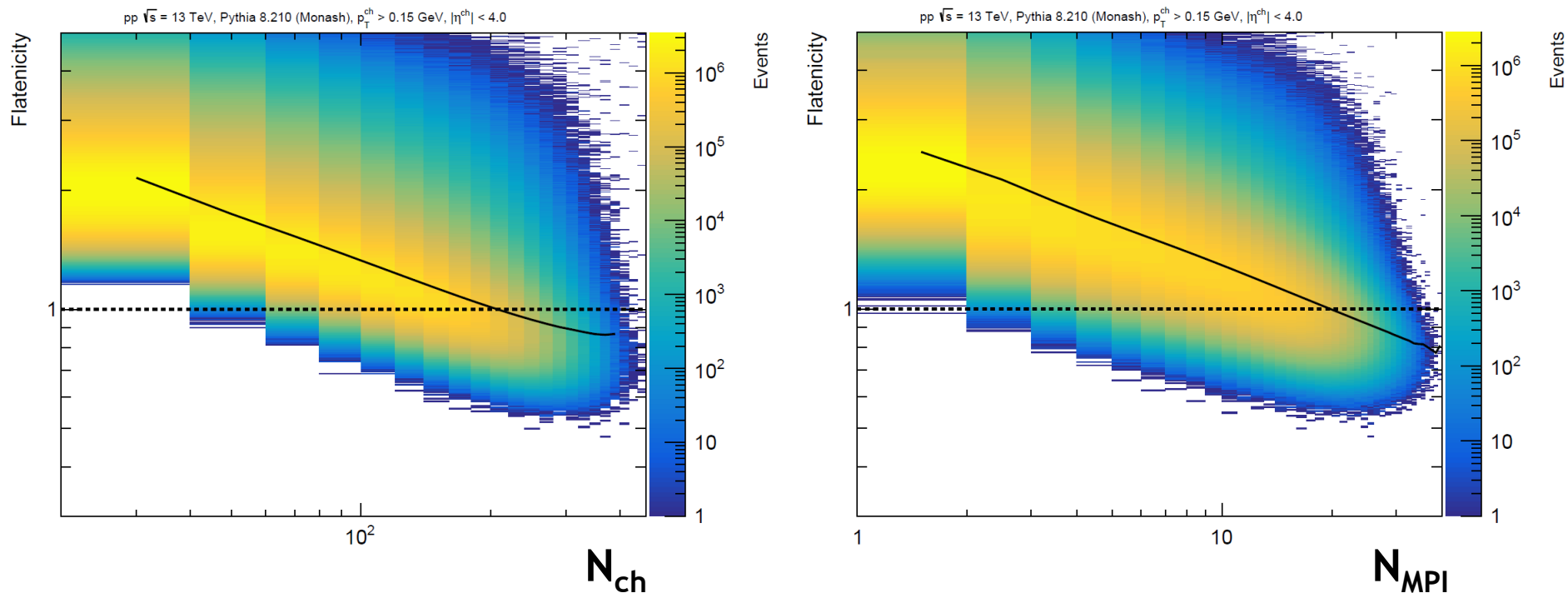
- Build **8** x **10** grid in (η - ϕ) space:



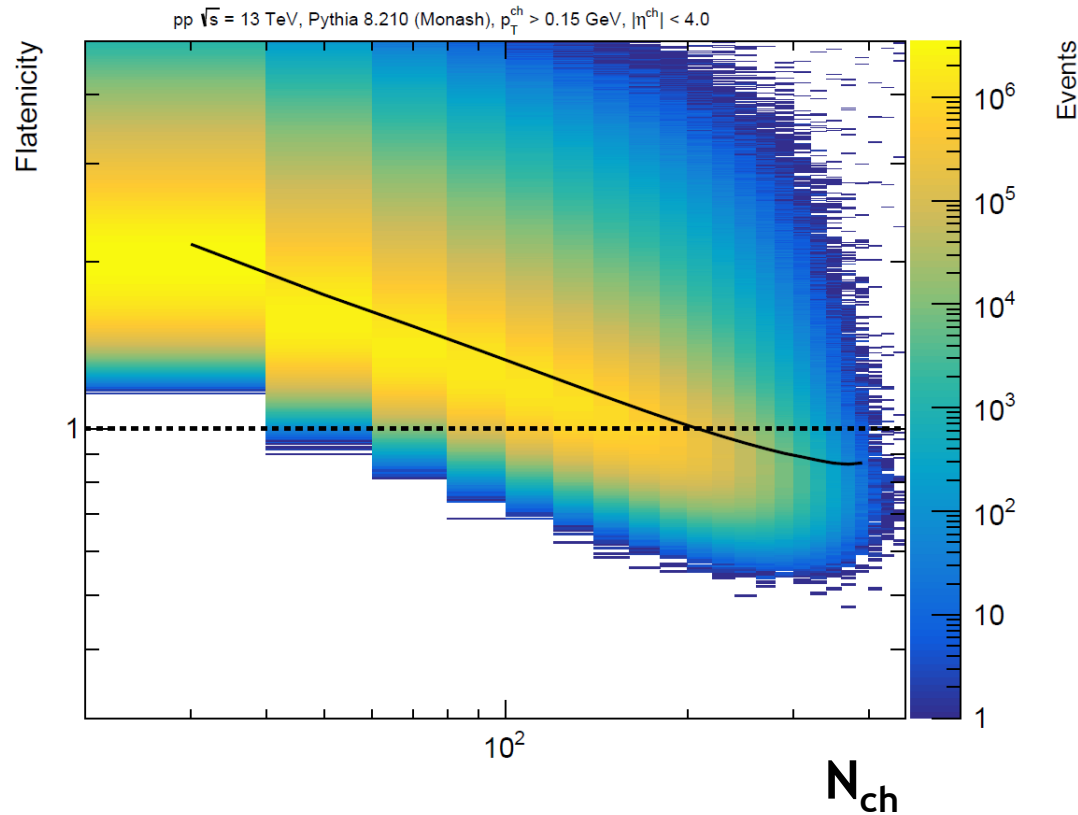
In each cell, the average transverse momentum is calculated: p_T^{cell}

- Event-by-event, the relative standard deviation of the p_T^{cell} distribution is obtained - flattenicity.
- Events with **jet-like** structures are expected to have **larger values** of ρ .

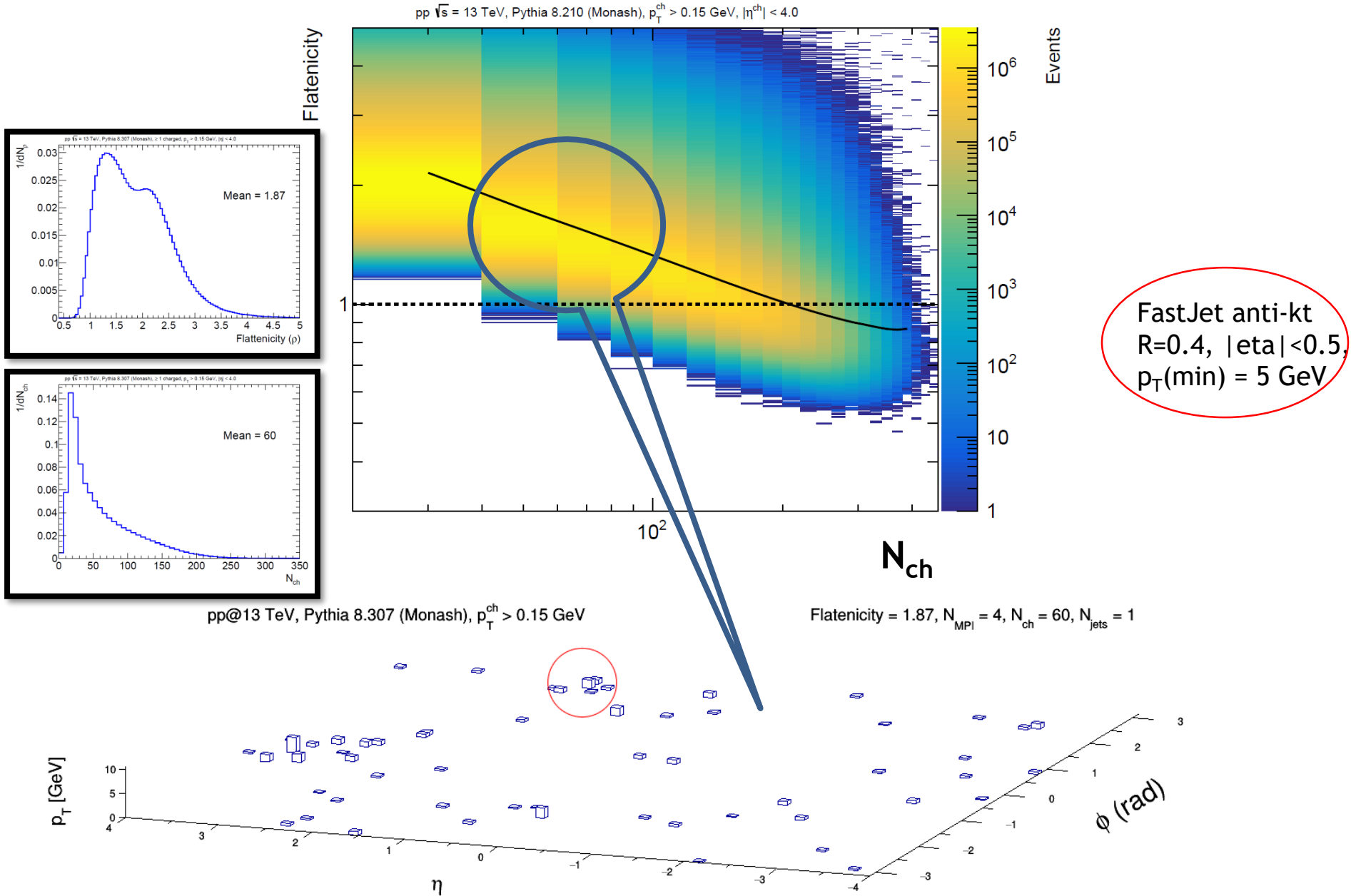




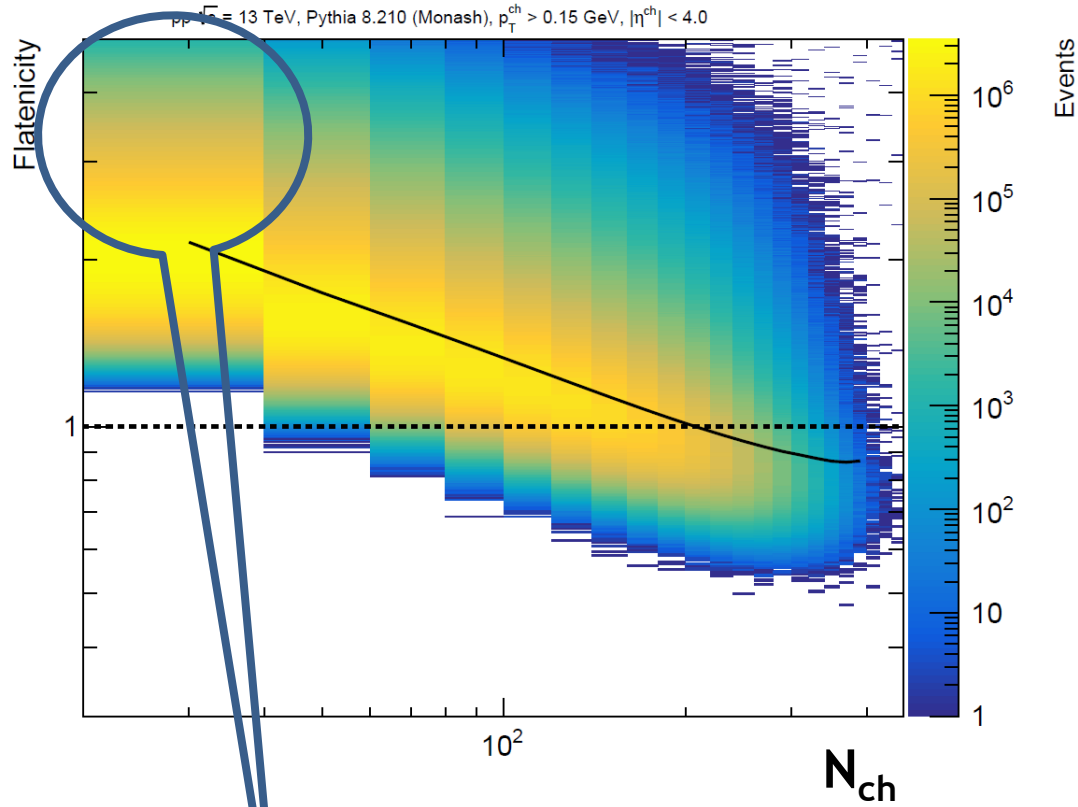
- Pythia 8.3 pp@13 TeV events with minimum-bias (SoftQCD:nonDiffractive) settings, Monash 2013 tune, with $|\eta| < 4$ and min p_T (chgd. particles) of 0.15 GeV.
- At low N_{ch} the flattenicity distribution is very wide, $\langle \rho \rangle$ is significantly above unity.
- $\langle \rho \rangle$ goes below unity with $N_{ch} > 200$, and for very high values of N_{ch} , flattenicity approaches 0.5 as the particles get to be quite uniformly distributed in the η - ϕ space.
- Similar correlation between flattenicity and the number of multiparton interactions.



- Almost all of the results rely on “means” and “averages” of the distributions, yet the interesting (and by definition rare) effects lie on the “outliers”!
- Flattenicity opens a new way to study pp collisions and analyse those outliers: looking for **hedgehog events**!



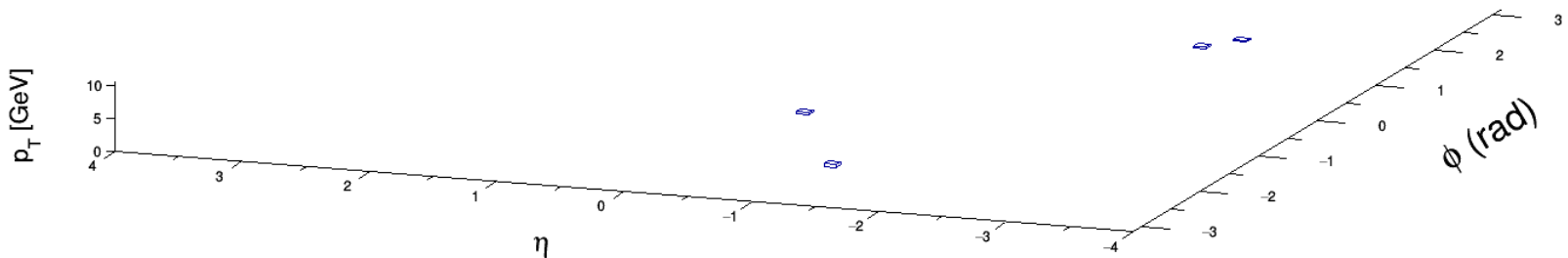
Analysing flattonicity vs N_{ch}

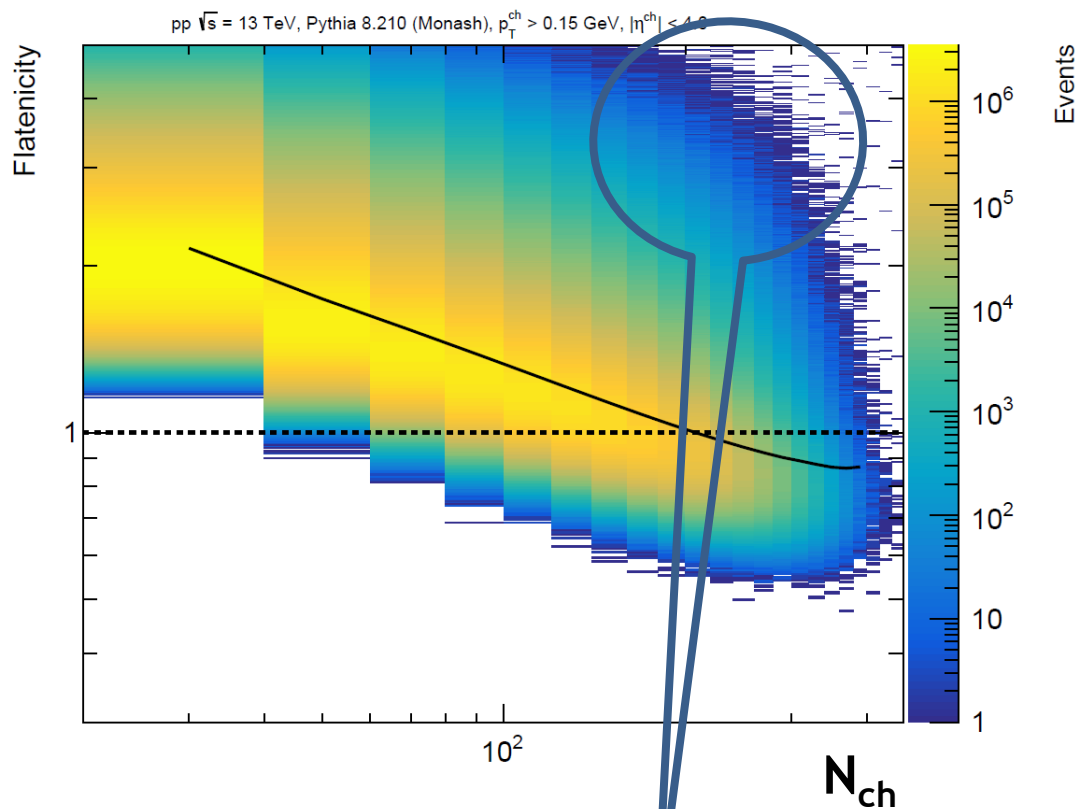


FastJet anti-kt
 $R=0.4$, $|\eta| < 0.5$,
 $p_T(\text{min}) = 5$ GeV

pp@13 TeV, Pythia 8.307 (Monash), $p_T^{ch} > 0.15$ GeV, $p_T^{\text{jet with } R=0.4} > 5$ GeV

Flatenicity = 5.14, $N_{MPI} = 1$, $N_{ch} = 4$, $N_{jets} = 0$

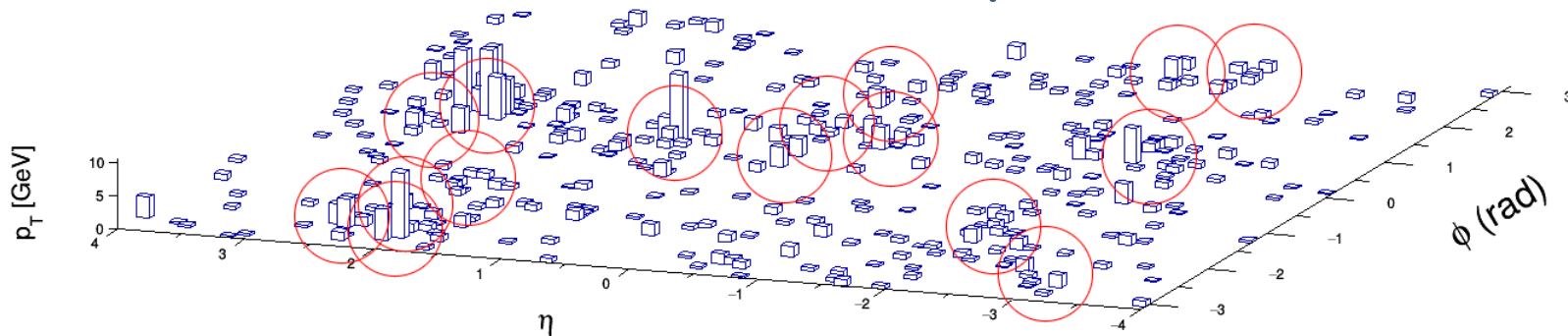


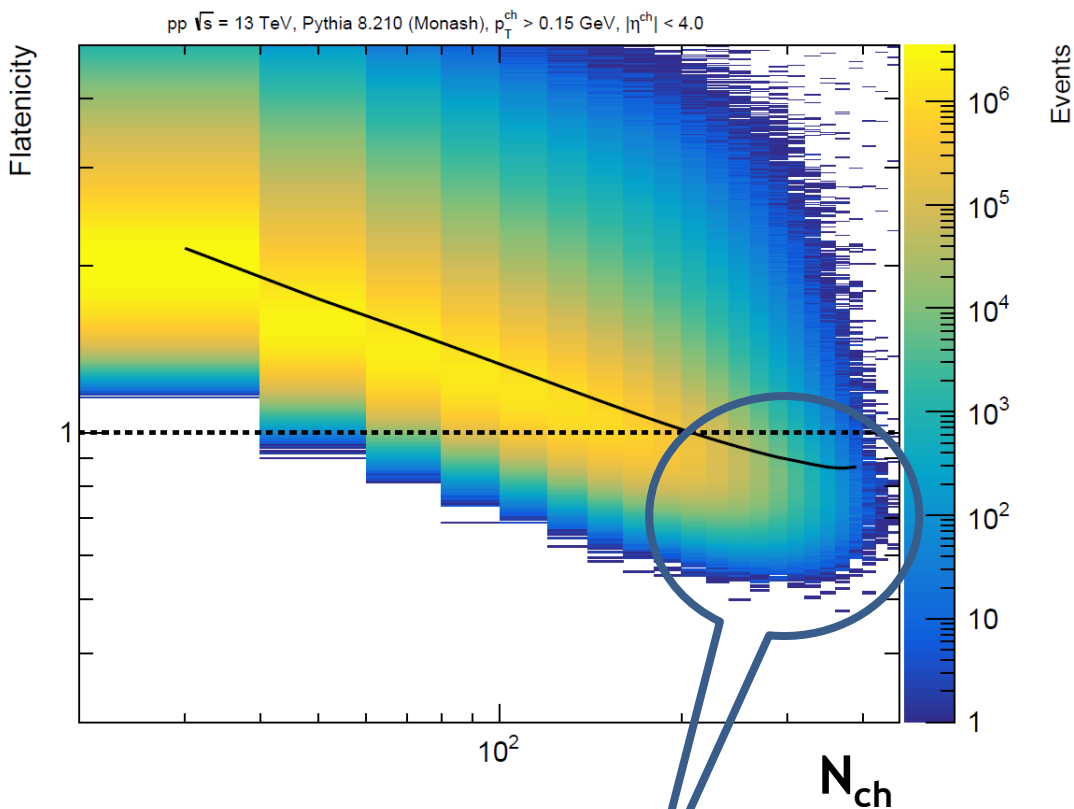


FastJet anti-kt
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 $p_T(\text{min}) = 5$ GeV

pp@13 TeV, Pythia 8.307 (Monash), $p_T^{ch} > 0.15$ GeV, $p_T^{\text{jet with } R=0.4} > 5$ GeV

Flatnenticity = 2.61, $N_{MPI} = 23$, $N_{ch} = 373$, $N_{jets} = 16$

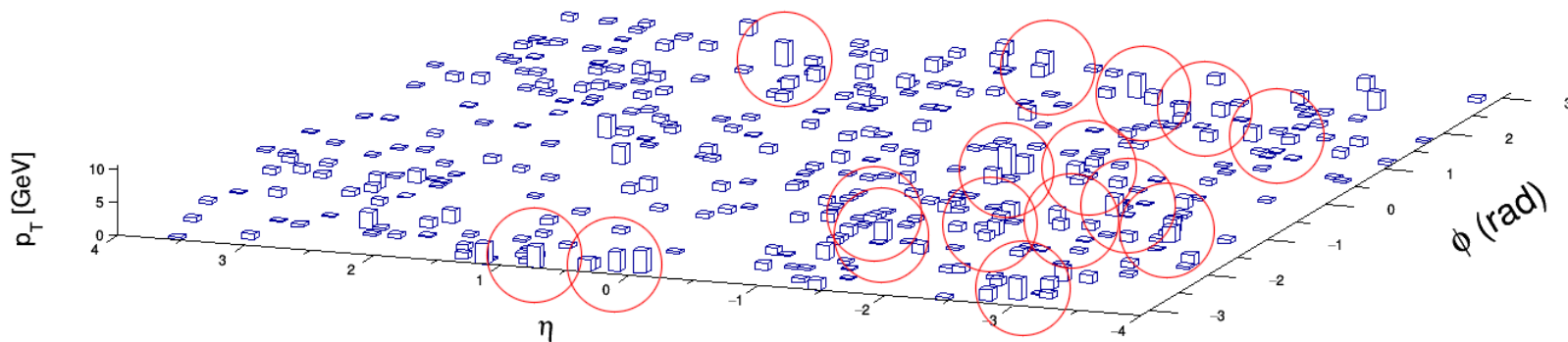




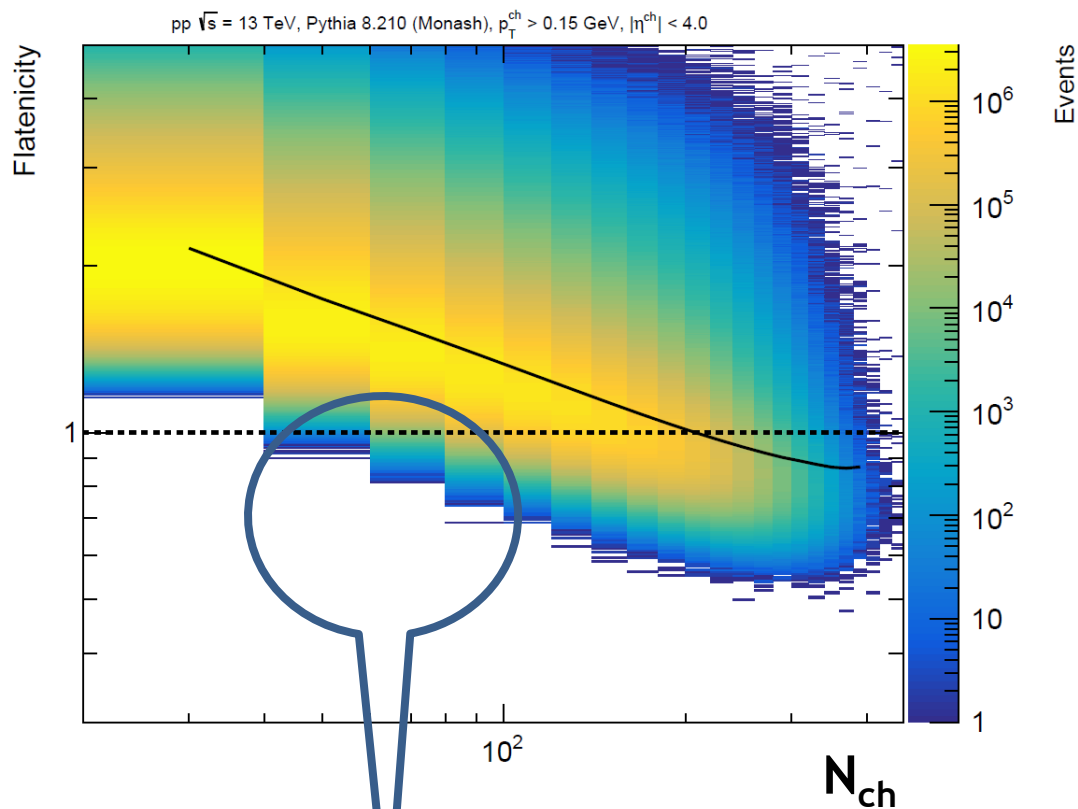
FastJet anti-kt
 $R=0.4$, $|\eta| < 0.5$,
 $p_T(\text{min}) = 5$ GeV

pp@13 TeV, Pythia 8.307 (Monash), $p_T^{ch} > 0.15$ GeV, $p_T^{\text{jet with } R=0.4} > 5$ GeV

Flattenicity = 0.76, $N_{MPI} = 26$, $N_{ch} = 376$, $N_{jets} = 16$



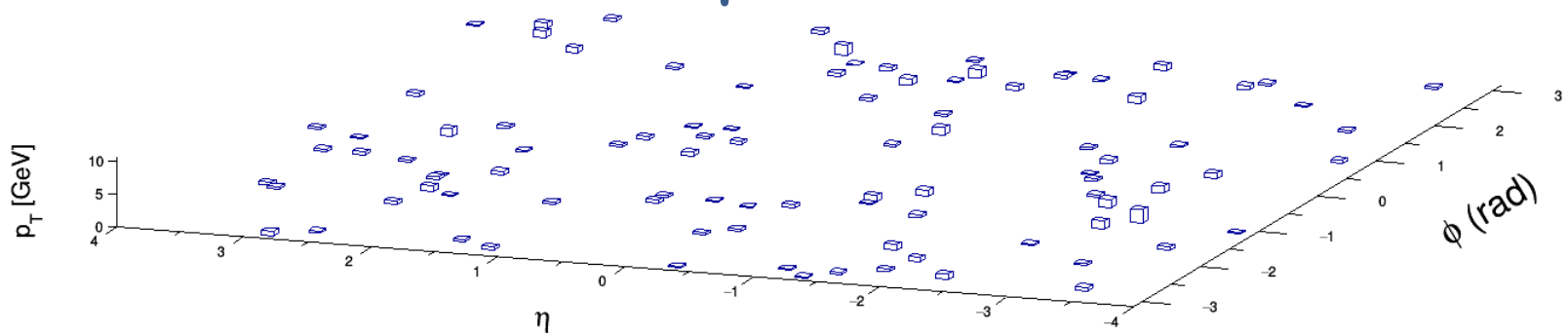
Analysing flattenicity vs N_{ch}

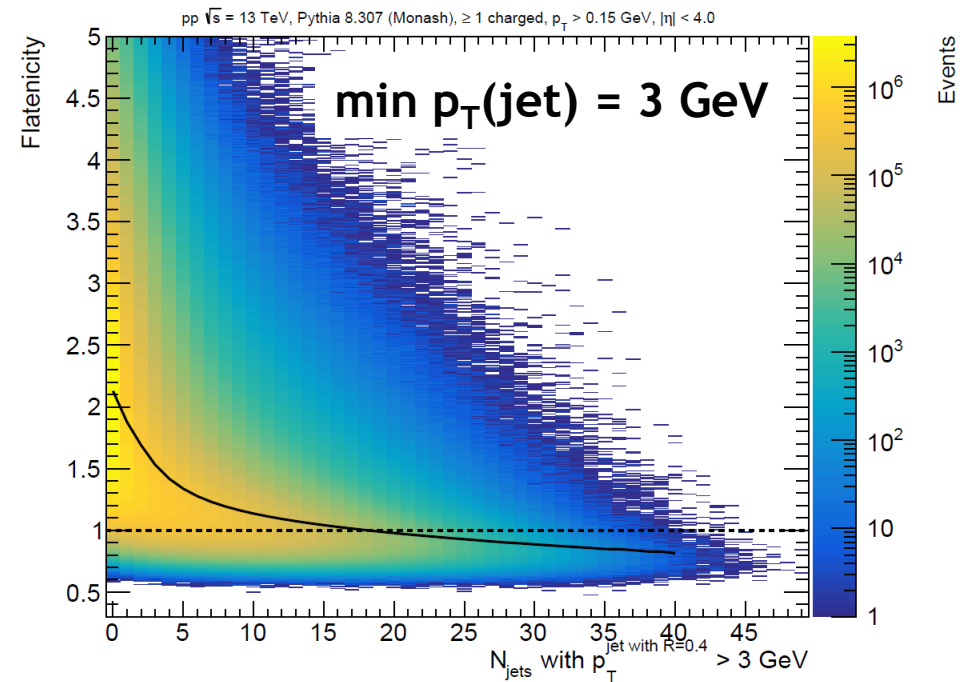
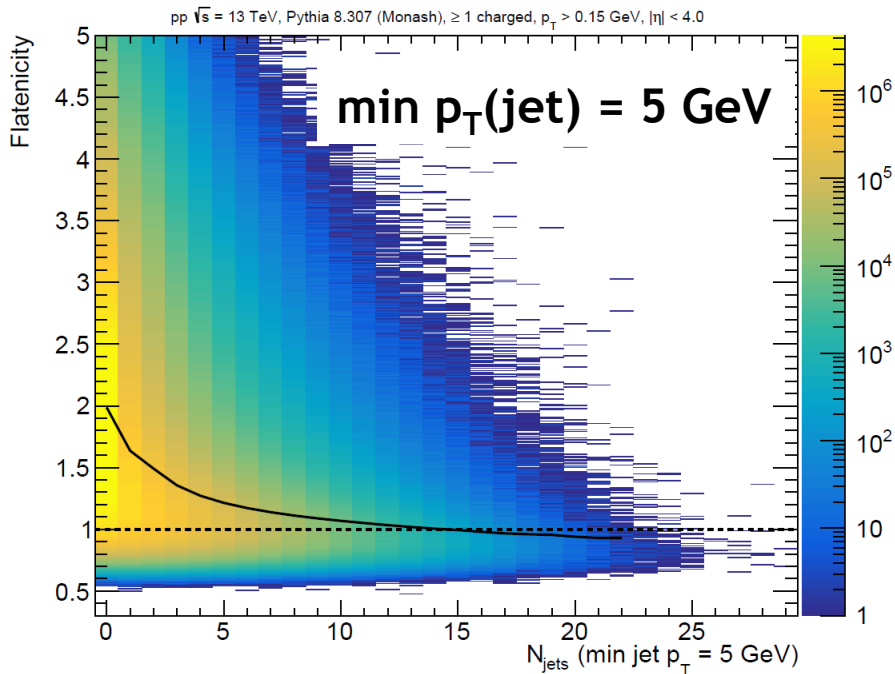


FastJet anti-kt
 $R=0.4$, $|\eta| < 0.5$,
 $p_T(\text{min}) = 5$ GeV

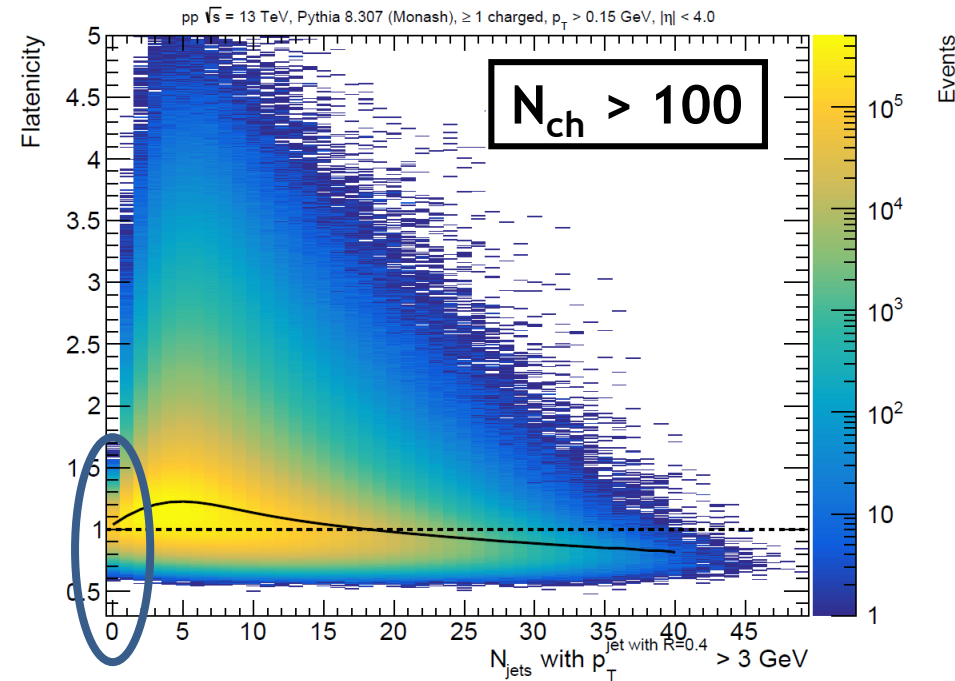
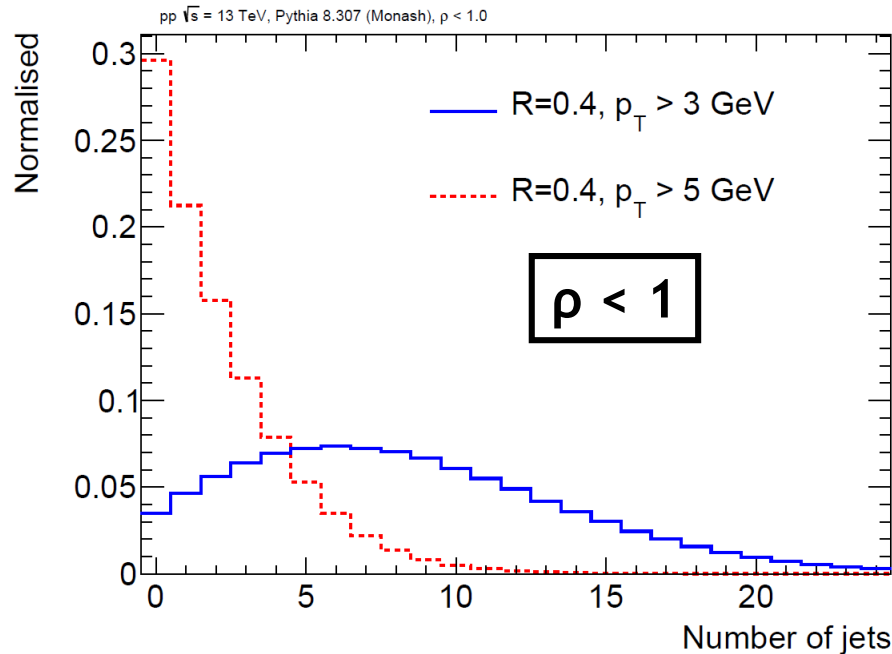
pp@13 TeV, Pythia 8.307 (Monash), $p_T^{ch} > 0.15$ GeV, $p_T^{\text{jet with } R=0.4} > 5$ GeV

Flattenicity = 0.99, $N_{MPI} = 9$, $N_{ch} = 97$, $N_{jets} = 0$



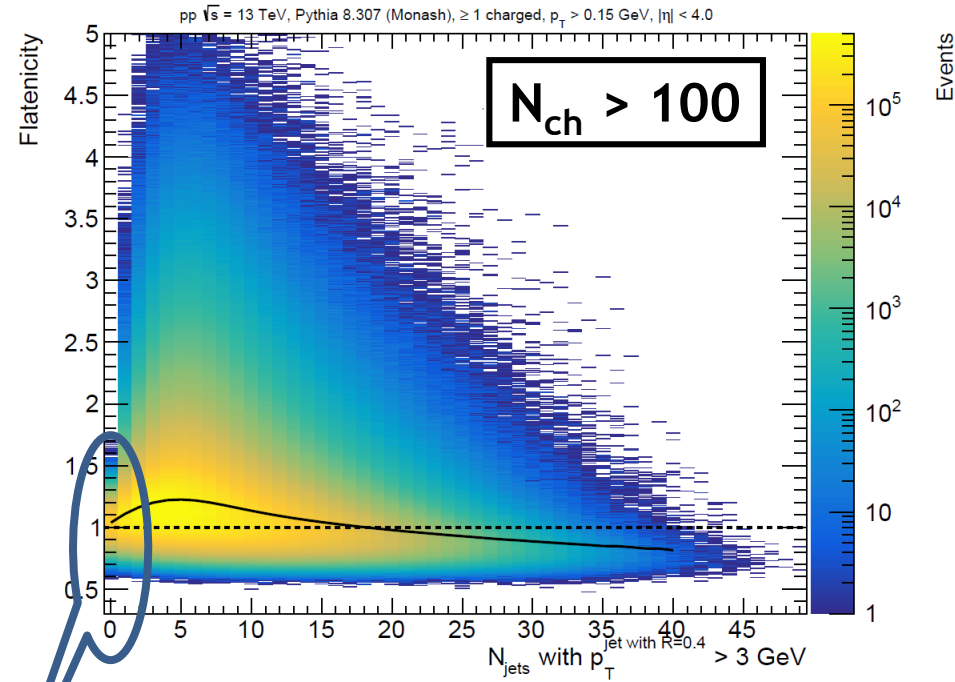
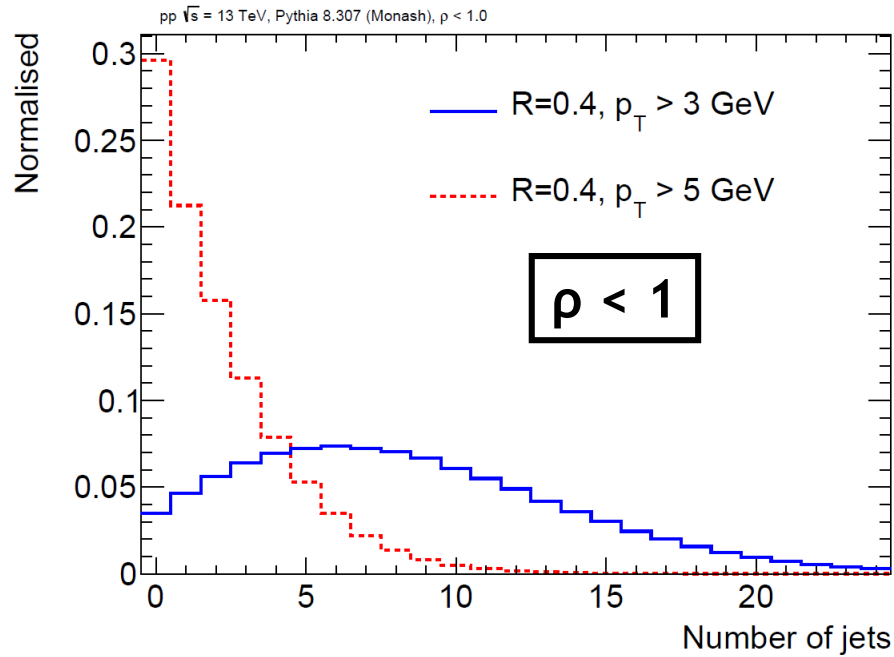


- As the jet energy decreases, the interpretation of the event topology becomes more difficult and the definition of a “jet” becomes arbitrary.
- Considering that events with high p_T are consistent with having a substantial component of QCD jets, the 3 GeV cut represents the lowest reasonable limit below which any attempt to separate experimentally soft production fluctuations from hard scattering would be unreliable.



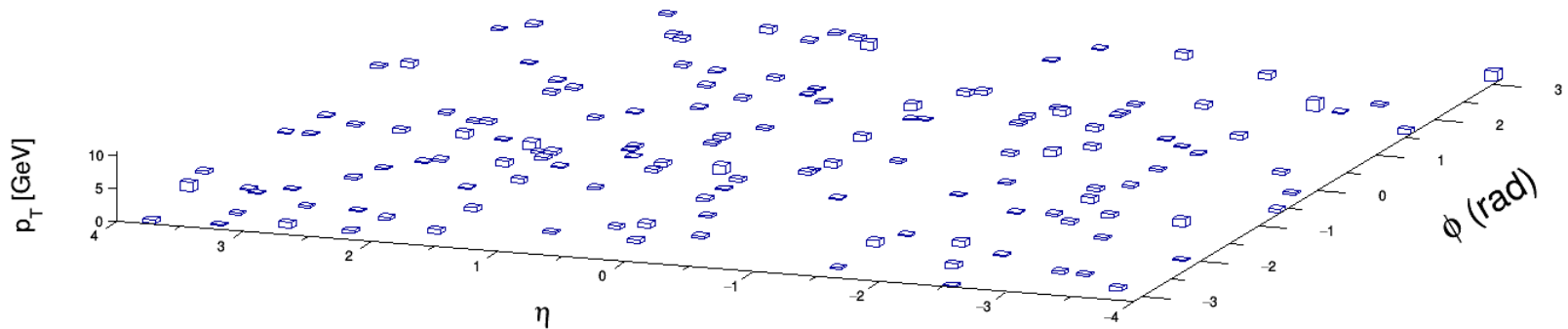
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- Considering that events with high p_T are consistent with having a substantial component of QCD jets, the 3 GeV cut represents the lowest reasonable limit below which any attempt to separate experimentally soft production fluctuations from hard scattering would be unreliable.
- In the **low flattenicity regime**, we are able to select hedgehog events with **high multiplicity** and with **no jet production** ($\sim 0.1\%$ of all events).

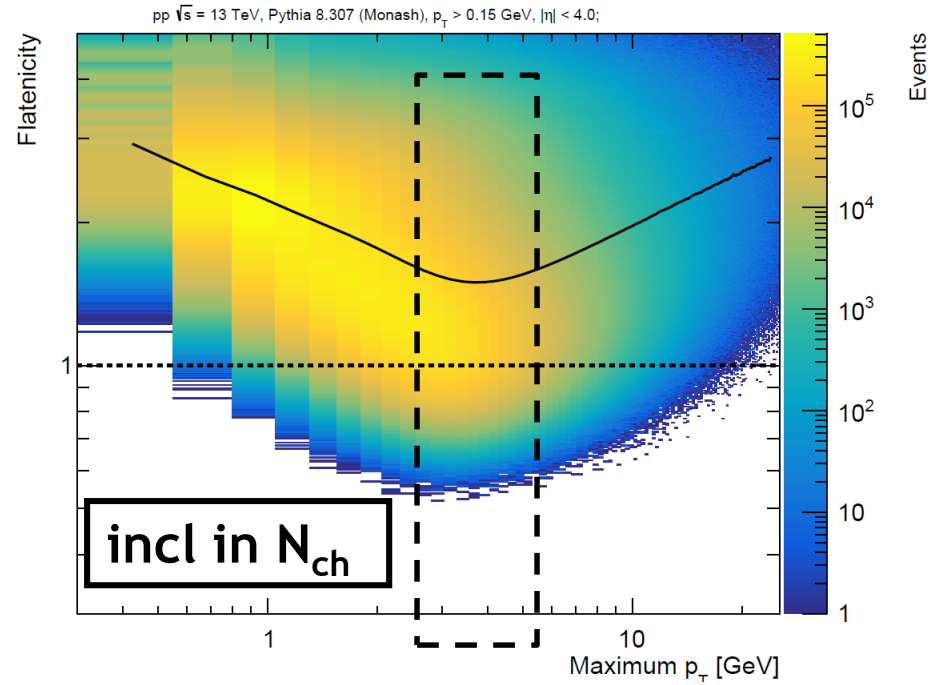
Analysing flattonicity vs N_{jets}



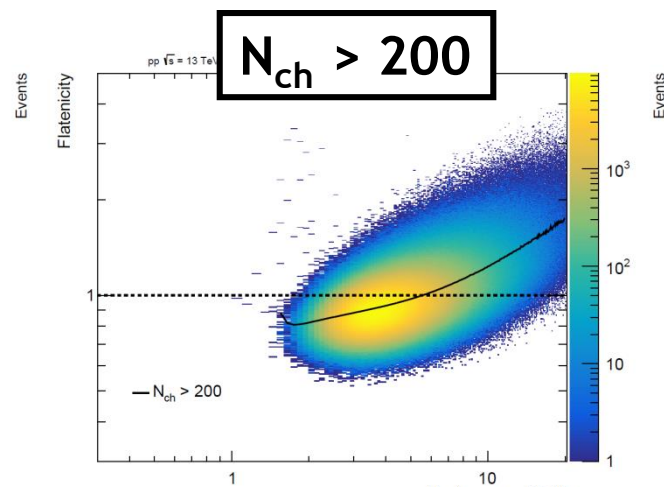
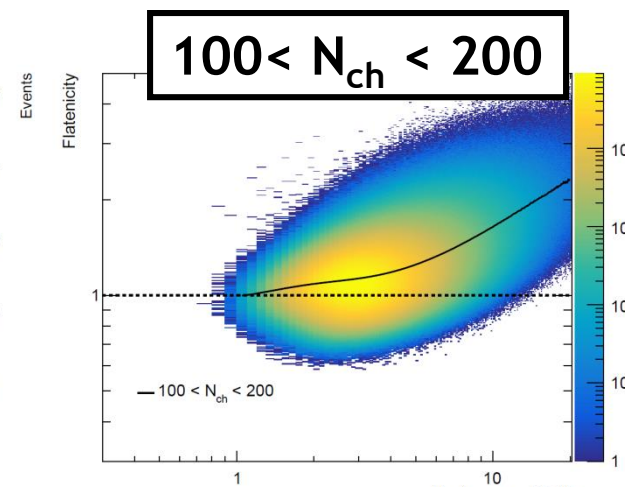
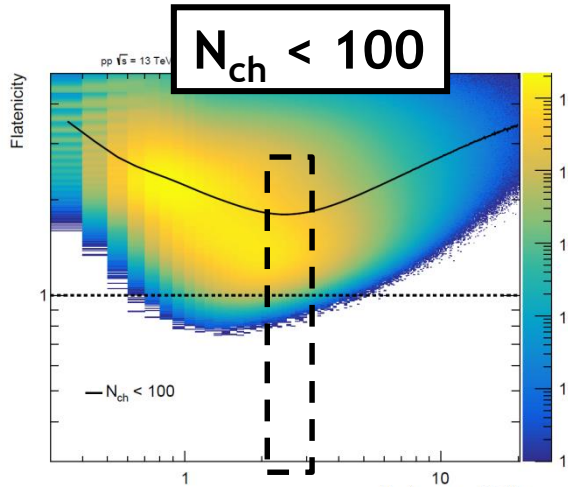
pp@13 TeV, Pythia 8.307 (Monash), $p_T^{\text{ch}} > 0.15 \text{ GeV}$

Flattonicity = 0.80, $N_{\text{MPI}} = 9$, $N_{\text{ch}} = 146$, $N_{\text{jets}} \text{ with } R=0.4 \text{ and } p_T > 3 \text{ GeV} = 0$





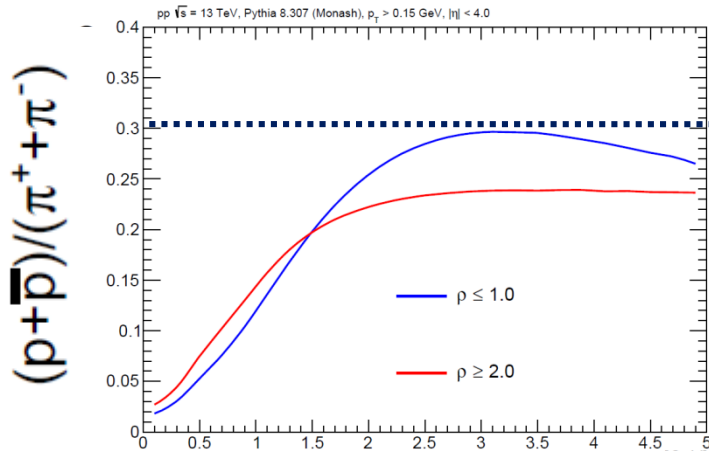
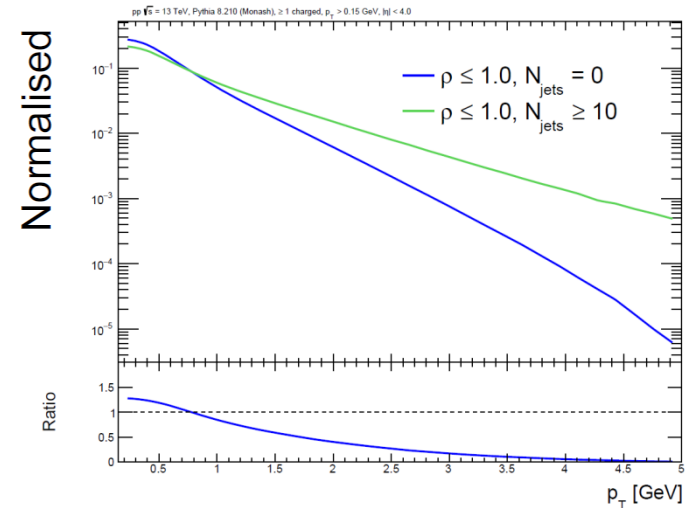
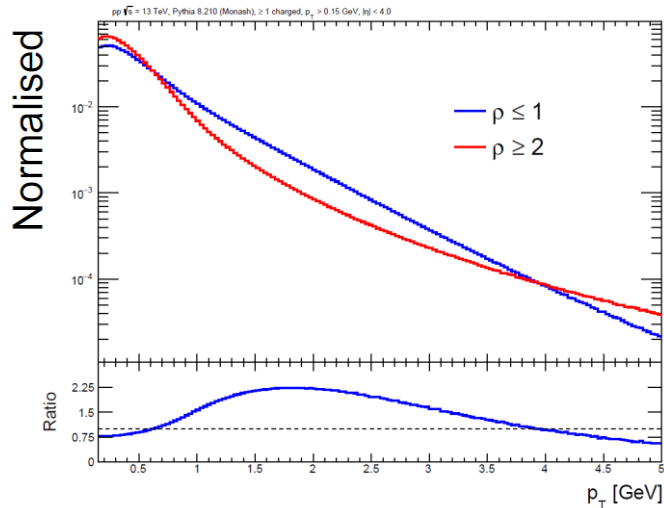
- Leading charged particle p_T shows a prominent feature: $\langle \rho \rangle$ has a dip around 3-5 GeV, while events with lower multiplicity show a dip at lower values (~ 2 -3 GeV)
- At higher N_{ch} , $\langle \rho \rangle$ shows a trend towards higher p_T values
- A step towards studying the underlying event by using the leading particle p_T



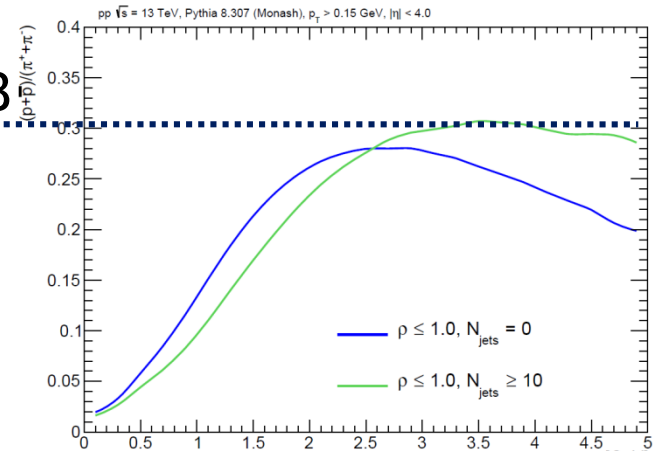
Leading p_T (chgd. particle) [GeV]

Analysing flattenicity vs chgd. particle p_T and ρ/π ratio

- We study the p_T (particle) as well as the proton-to-pion ratio in 0.15 to 5 GeV interval by selecting events with $\rho < 1$ and $\rho > 2$. For events with $\rho < 1$, we also select jetty events (≥ 10 jets with $\min p_T(\text{jet}) = 5$ GeV) and events with no jets at all.

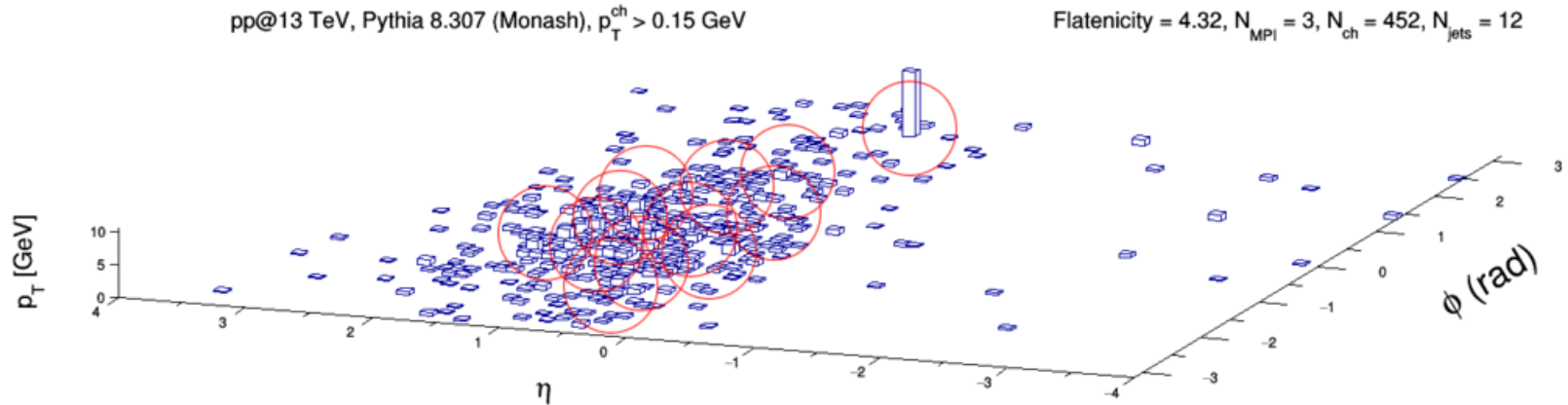


$\rho/\pi = 0.3$



p_T (chgd. particle) [GeV]

- Flattenicity allows one to find quite atypical (and rare 1/100M) events:
 - i.e. high chgd. multiplicities (>300) and low number of hard-scatterings (MPI=3)



- In some events we see one very high p_T charged particle (around which a jet is usually build, and particle p_T divided by jet p_T approaches unity!)
- Recoil jets are usually produced opposite in ϕ , and fragment into several particles.
- Nor the partonic hard-scattering p_T , nor the additional multiparton interactions p_T are high enough nor match the reconstructed energy for these events.
- Are we looking at the limit of fragmentation and/or ISR/FSR emissions?
- We are identifying an experimental way to find these events, and it would be a perfect place to study data and tune our generators!

- Hedgehog events have never been seriously studied in pp collisions at the LHC. These events are “rare” - but as rare as a Z-boson production!

Selection	Probability
$\rho < 1$	4×10^{-2}
$\rho < 0.75, N_{\text{ch}} > 100, N_{\text{jets}} = 0$	2×10^{-6}
$\rho < 0.75, N_{\text{ch}} > 400$	6×10^{-8}

- Flattenicity - the new event structure parameter - allows one to identify the hedgehog events and is more detailed than sphericity/spherocity/RT, as one can observe the evolution of events from jetty to hedgehog type.
- We are able to identify different classes of hedgehog events: those with high jet multiplicity (jetty) and with no jet production.
- Events with low flattenicity show an enhancement in the proton-to-pion ratio compared to those with high flattenicity.
- Studying these events may shed light to the search for the “energy re-distribution” effect in pp collisions.
- Next step: look for hedgehog events in data!

BACK-UP

sphericity is measured in the acceptance $|\eta| \leq 0.8$, for events with more than two tracks ($p_T \geq 0.5$ GeV/c). The observable is defined as follows:

$$S_T \equiv \frac{2\lambda_2}{\lambda_2 + \lambda_1} \quad (1)$$

where: $\lambda_1 > \lambda_2$ are the eigenvalues of the transverse momentum matrix:

$$\mathbf{S}_{xy}^L = \frac{1}{\sum_i p_{Ti}} \sum_i \frac{1}{p_{Ti}} \begin{pmatrix} p_{xi}^2 & p_{xi}p_{yi} \\ p_{xi}p_{yi} & p_{yi}^2 \end{pmatrix}$$

By construction, the limits of the variable are related to specific configurations in the transverse plane

$$S_T = \begin{cases} = 0 & \text{“pencil-like” limit} \\ = 1 & \text{“isotropic” limit} \end{cases} .$$